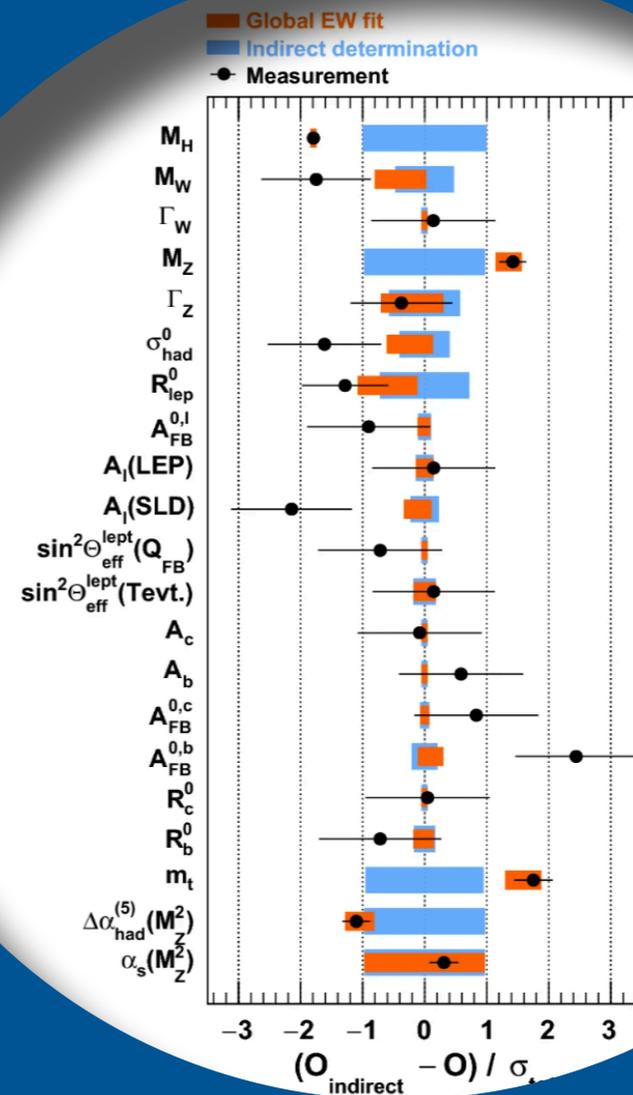
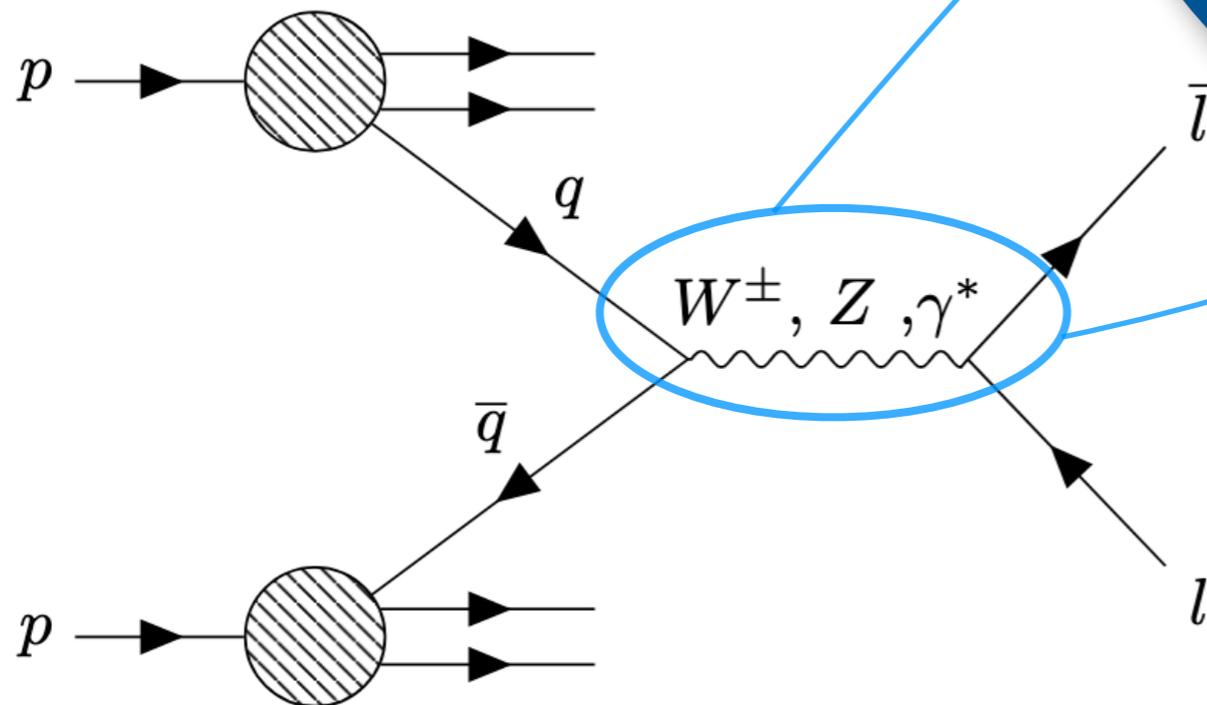


Precision Measurements at the Large Hadron Collider: Exploring the Foundations of Particle Physics



Ludovica Aperio Bella
Valencia - IFIC - 24/2/2026

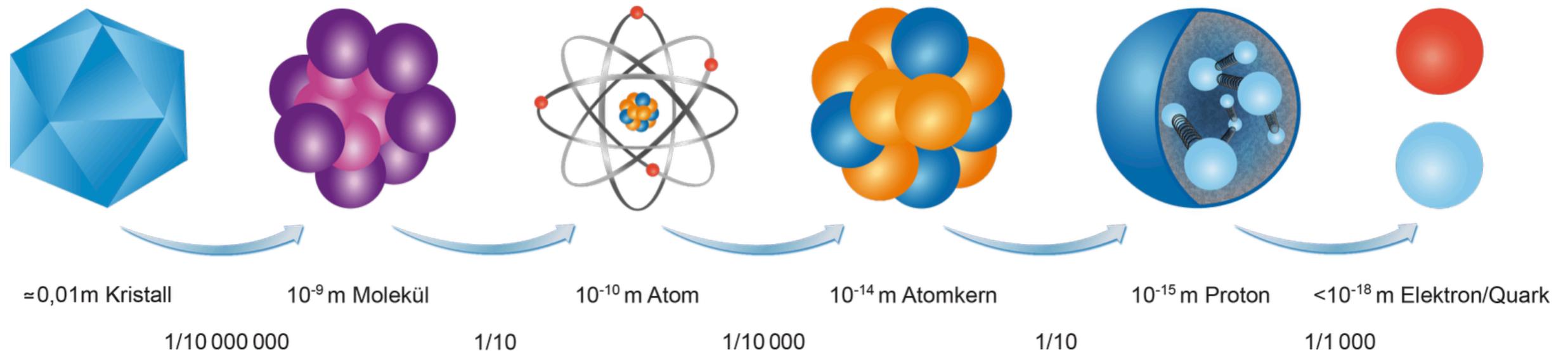
Precision Measurements at the Large Hadron Collider: Exploring the Foundations of Particle Physics

The experiments at the Large Hadron Collider (LHC) continue to confirm the Standard Model (SM) of particle physics with impressive precision, and no conclusive evidence for new physics at the TeV scale has yet been observed. In this context, precision measurements of electroweak observables provide a powerful and complementary approach to exploring physics beyond the SM.

The LHC experiments have delivered a broad and highly precise program of electroweak measurements, probing the internal consistency of the SM through fundamental quantities such as the W - and Z -boson masses, the effective weak mixing angle, and related electroweak parameters. More than forty years after their discovery, the W and Z bosons remain key laboratories for testing the SM, where even small deviations from predicted relations could point to new phenomena.

This talk will review recent high-impact ATLAS results in electroweak precision physics, highlighting both experimental and theoretical challenges and their relevance in the ongoing LHC physics program. Prospects for the High-Luminosity LHC, as well as the role of future collider projects, will also be discussed.

What is everything made of ?



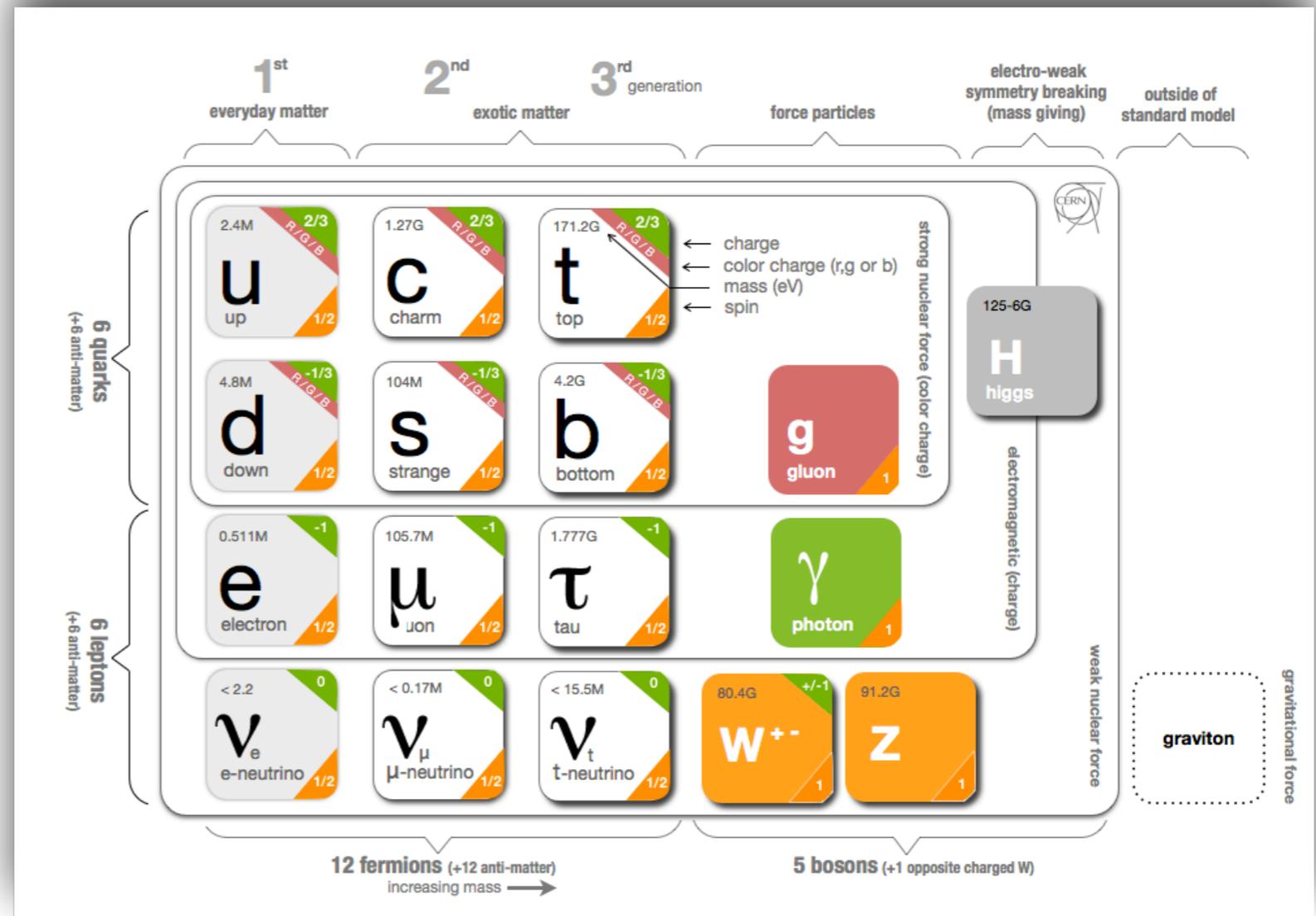
It's all made of a handful of particles and forces

Particle physics studies the elementary **building blocks** of matter

- **Particles** interact via forces caused by fields
- **Forces** are being carried by special particles called "**force mediators**" (**boson**)

The theory of everything: the Standard Model

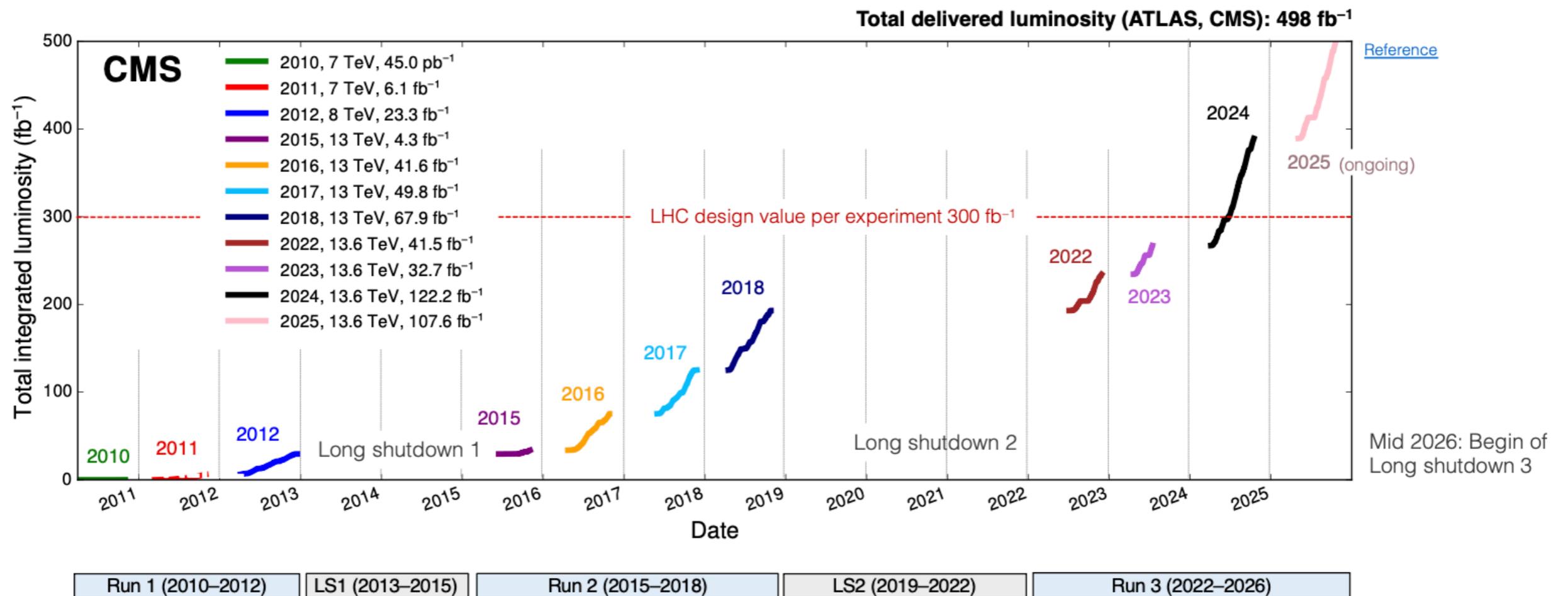
$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\
 & + i\bar{\psi} \not{D} \psi \\
 & + \chi_i y_{ij} \chi_j \phi + h.c. \\
 & + |D_\mu \phi|^2 - V(\phi)
 \end{aligned}$$



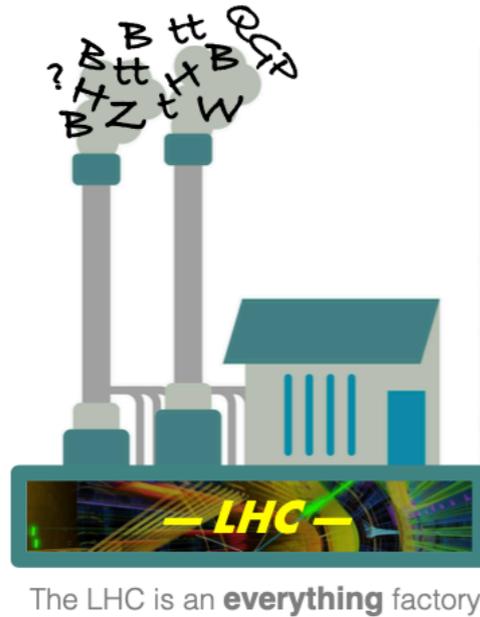
LHC a discovery machine at the energy frontier

- The **Large Hadron Collider (LHC)** is the world's largest and most powerful particle accelerator at date @ CERN in Geneva
- it was build to reproduce the universe condition after the big-bang to help us understanding and study the fundamental component of **matter and their interactions**

Superb LHC performance in 2024 and 2025 — on track for a strong Run-3 finish



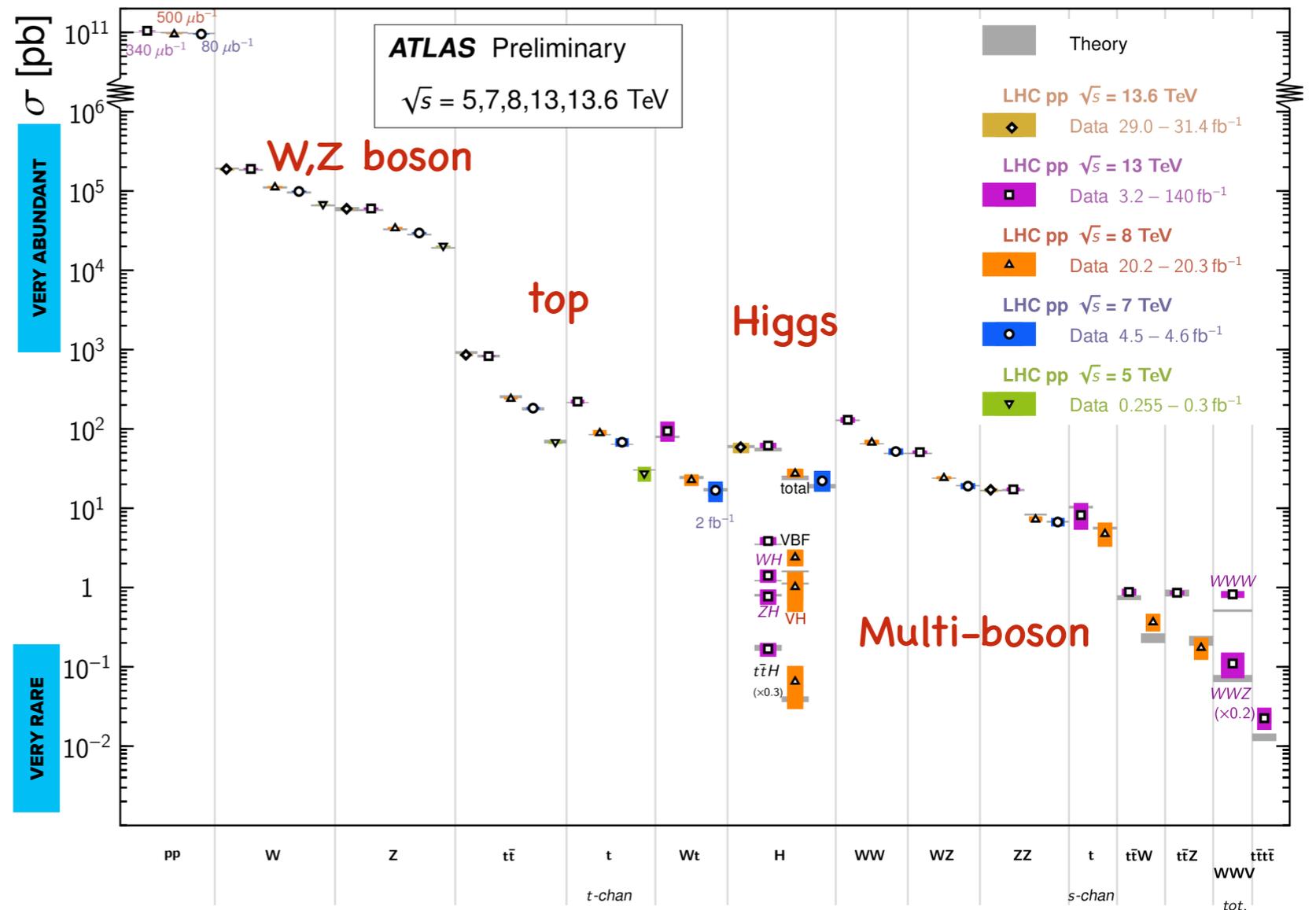
The LHC physics program



LHC experiments got the richest hadron collision data sample ever recorded with production rates varying across an incredible 10 orders of magnitude!

Standard Model Total Production Cross Section Measurements

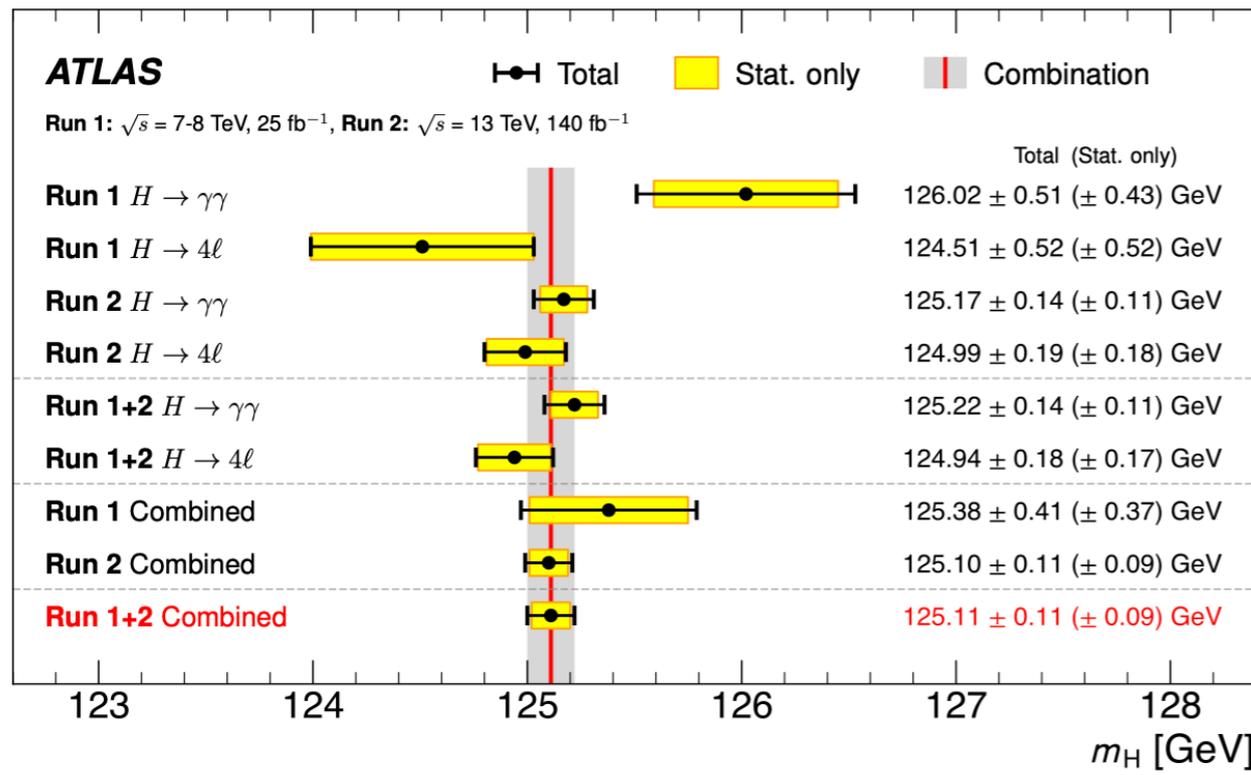
Status: June 2024



Precision objects enable precision measurements

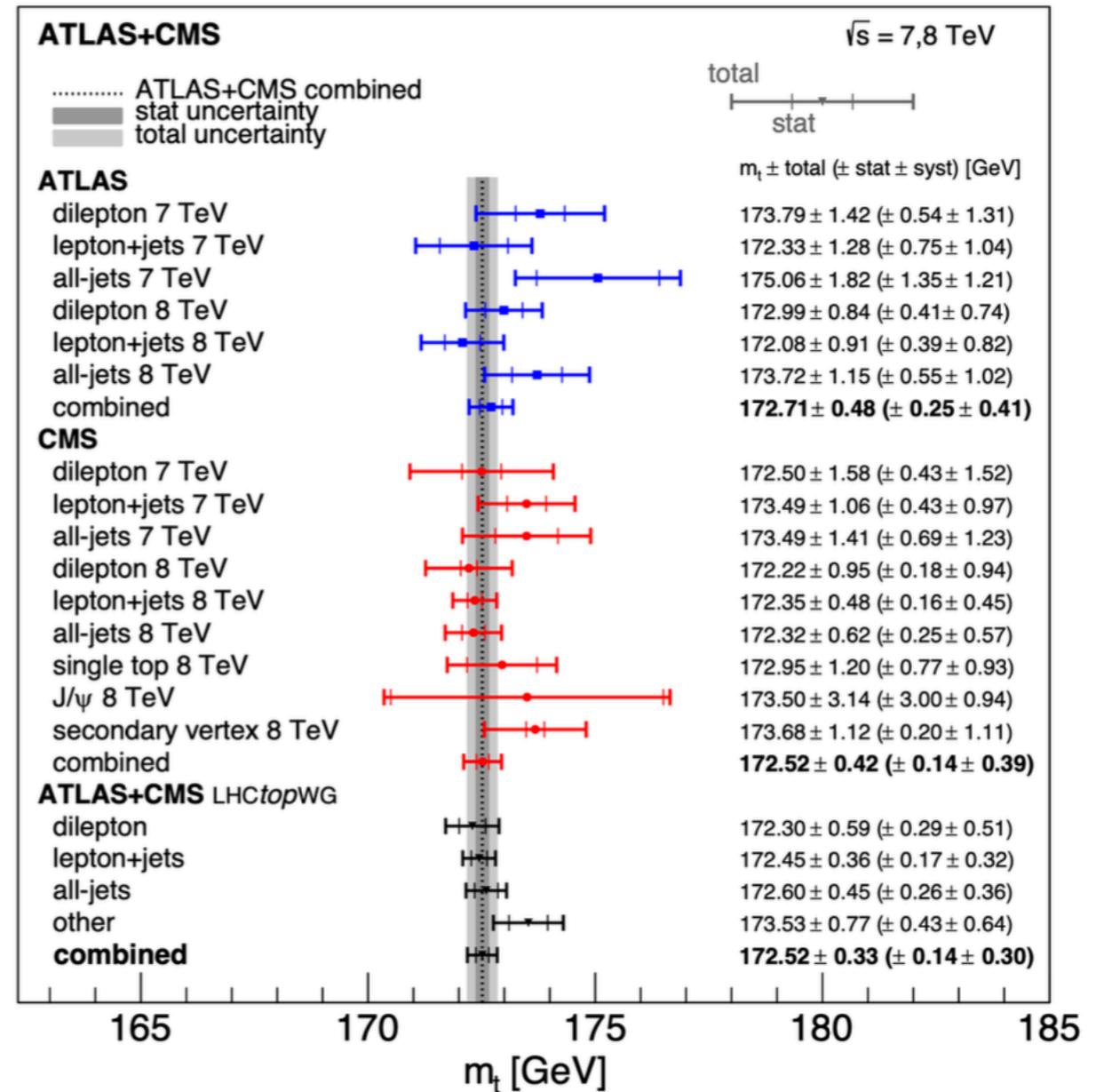


[arXiv:2308.07216](https://arxiv.org/abs/2308.07216), [arXiv:2308.04775](https://arxiv.org/abs/2308.04775), [arXiv:2309.05471](https://arxiv.org/abs/2309.05471)



most precise Higgs mass measurement to date (0.1%)

[arXiv:2402.08713](https://arxiv.org/abs/2402.08713)

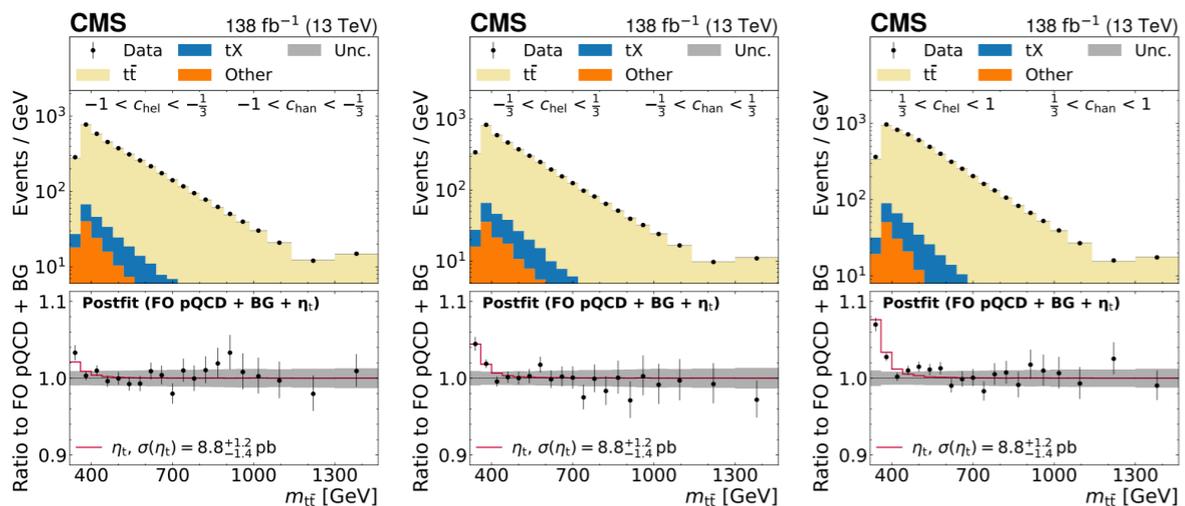
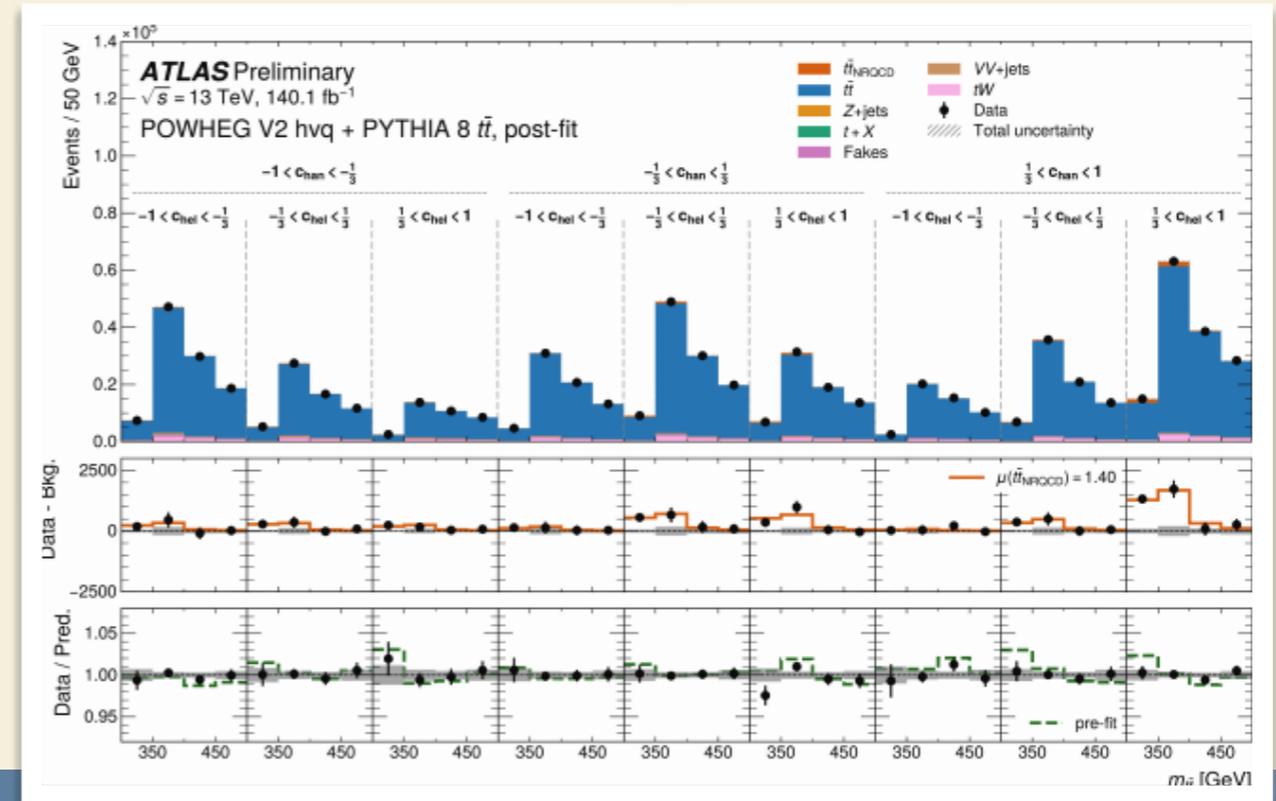
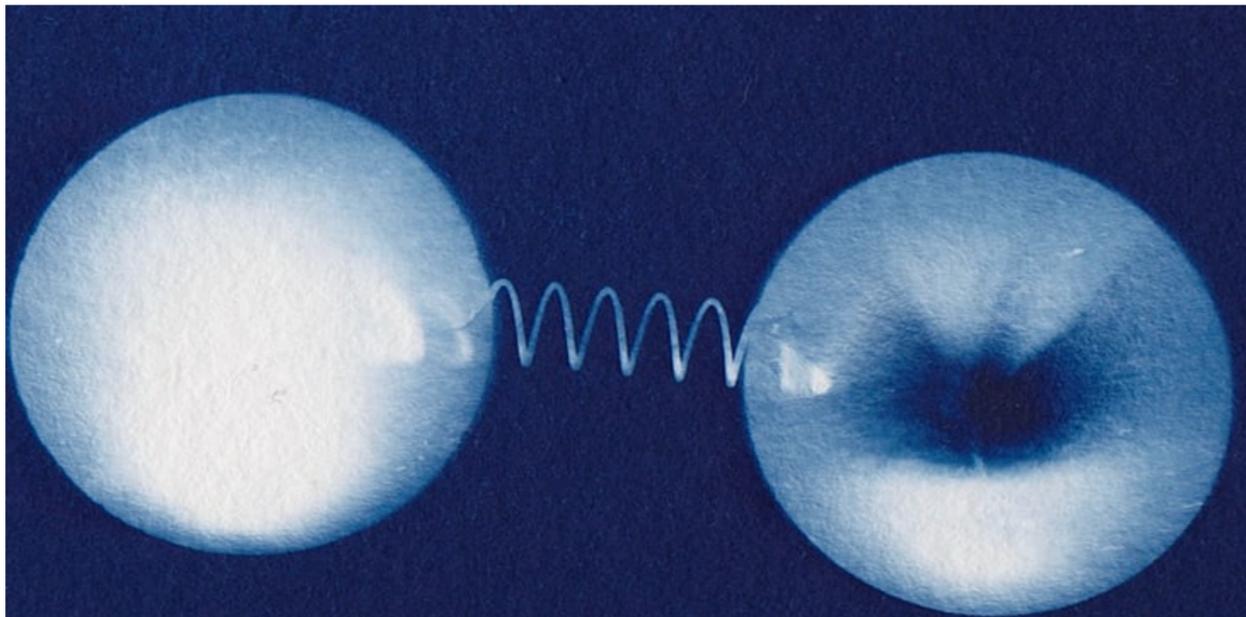


high-precision top mass measurements (0.2%)

New observed state

Non-relativistic QCD predicts highly compact, colour-singlet quasi-bound pseudoscalar $t\bar{t}$ states (negligible self-annihilation, top decays before)

Suddenly Visible: New Particle Challenges Long-Held Assumptions



[Updates](#) > [Press Statement](#) > Elusive romance of top-quark pairs observed at the LHC

Press Statement

Tags:
EPS 2025,
top quark,
physics results

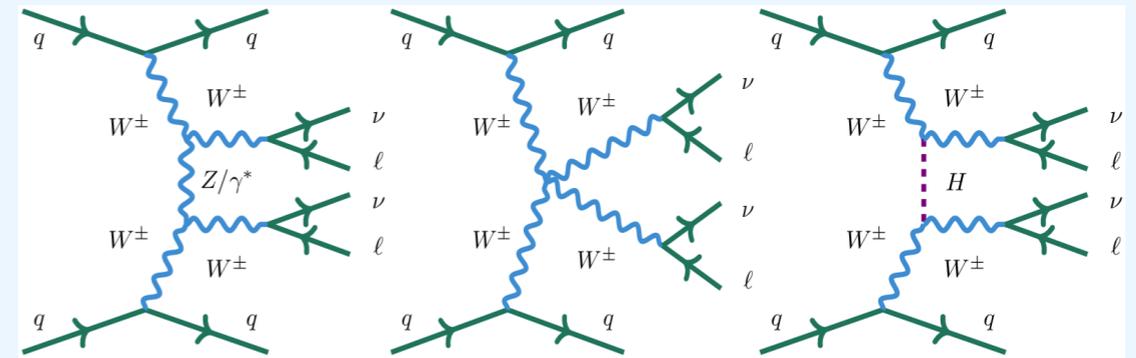
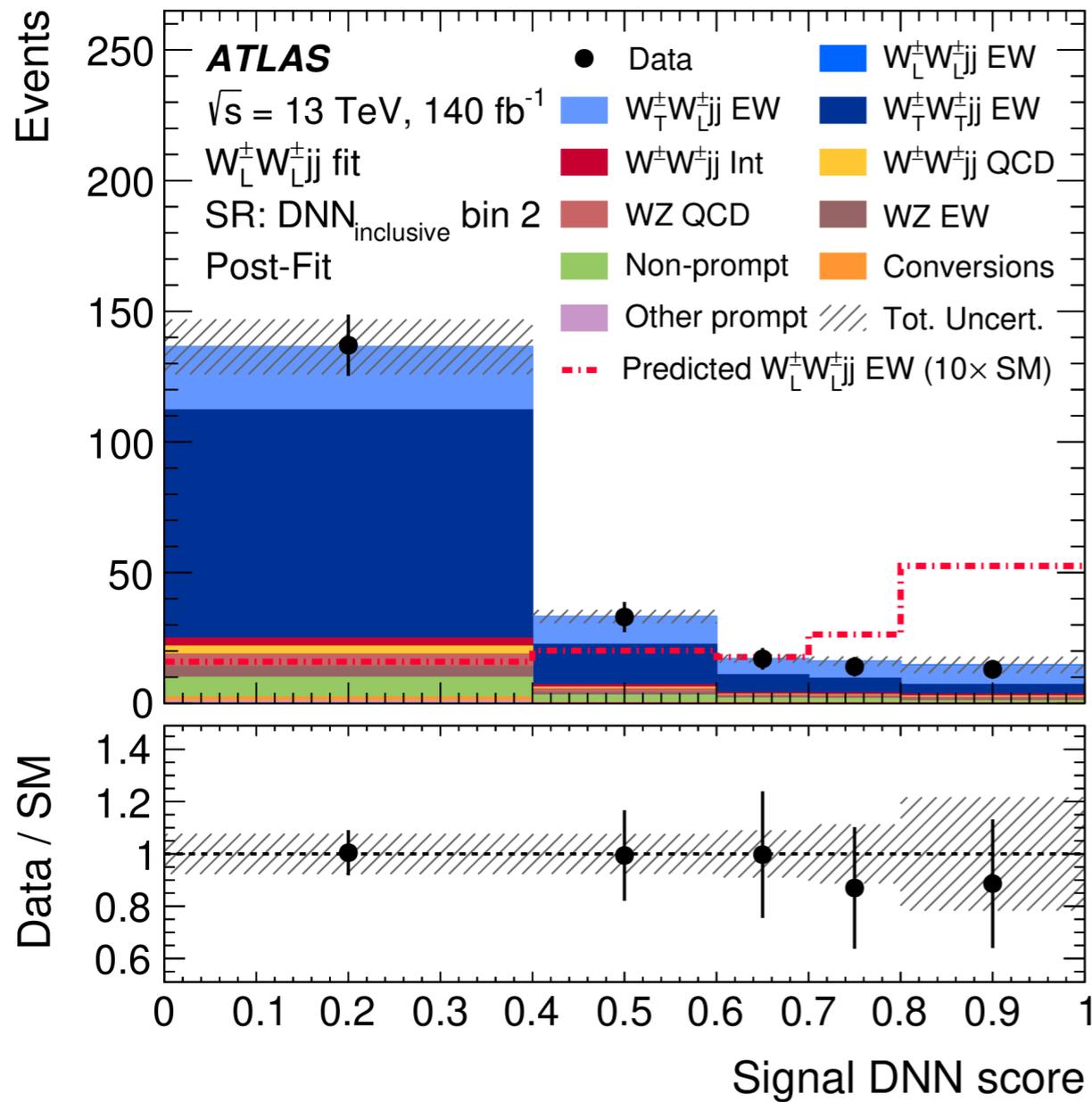
Elusive romance of top-quark pairs observed at the LHC

8 July 2025 | By CERN

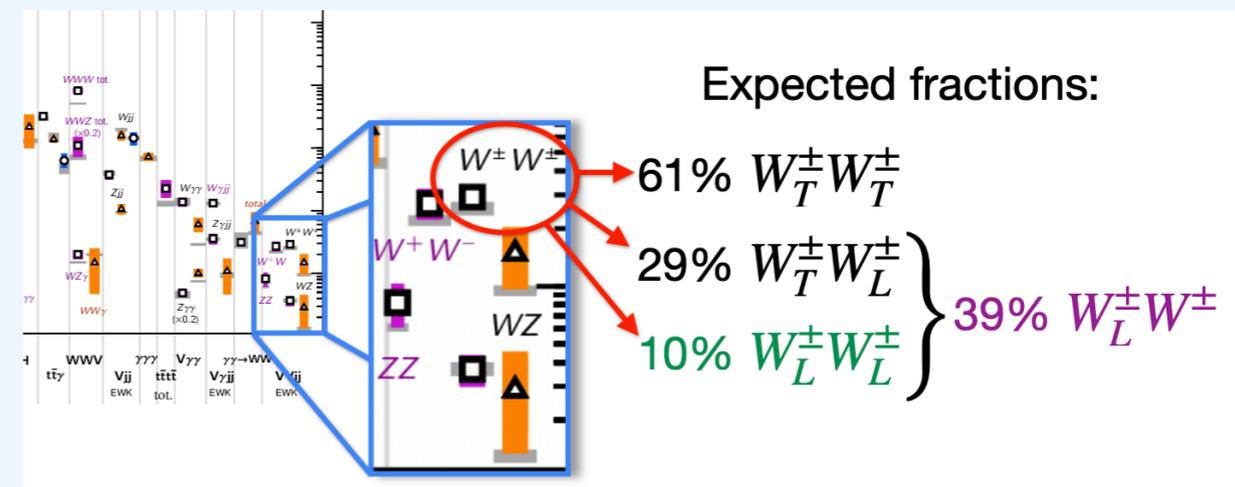
The CMS and ATLAS experiments at CERN's Large Hadron Collider have observed an unforeseen feature in the behaviour of top quarks that suggests that these heaviest of all elementary particles form a fleeting union.



Measurement of Super Rare process - longitudinal polarised WW - scattering



- First evidence of production of polarised WW where at least one of the bosons is longitudinally polarised (observed significance is 3.3σ with a measured cross-section of $0.88 \pm 0.30 \text{ fb}$)
- Most stringent limits to date for the fiducial cross-section of longitudinally polarised WW [observed (expected) 95 % CL upper limit of 0.45 (0.70) fb]

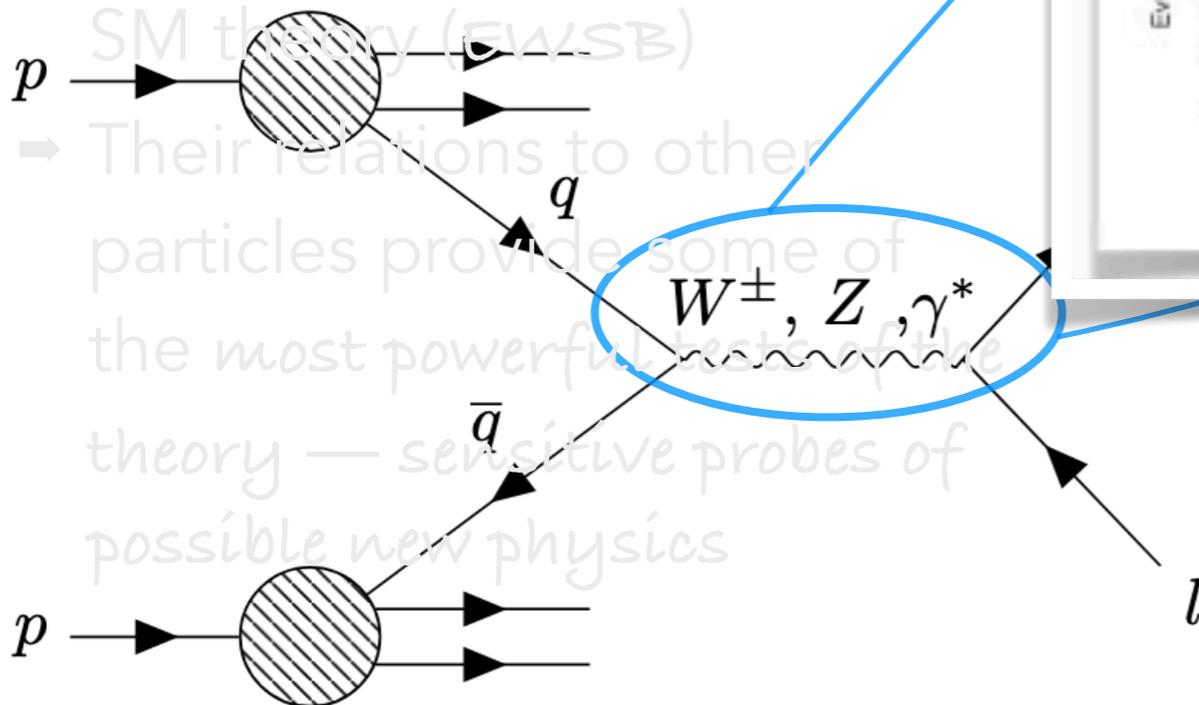


W,Z physics program at LHC

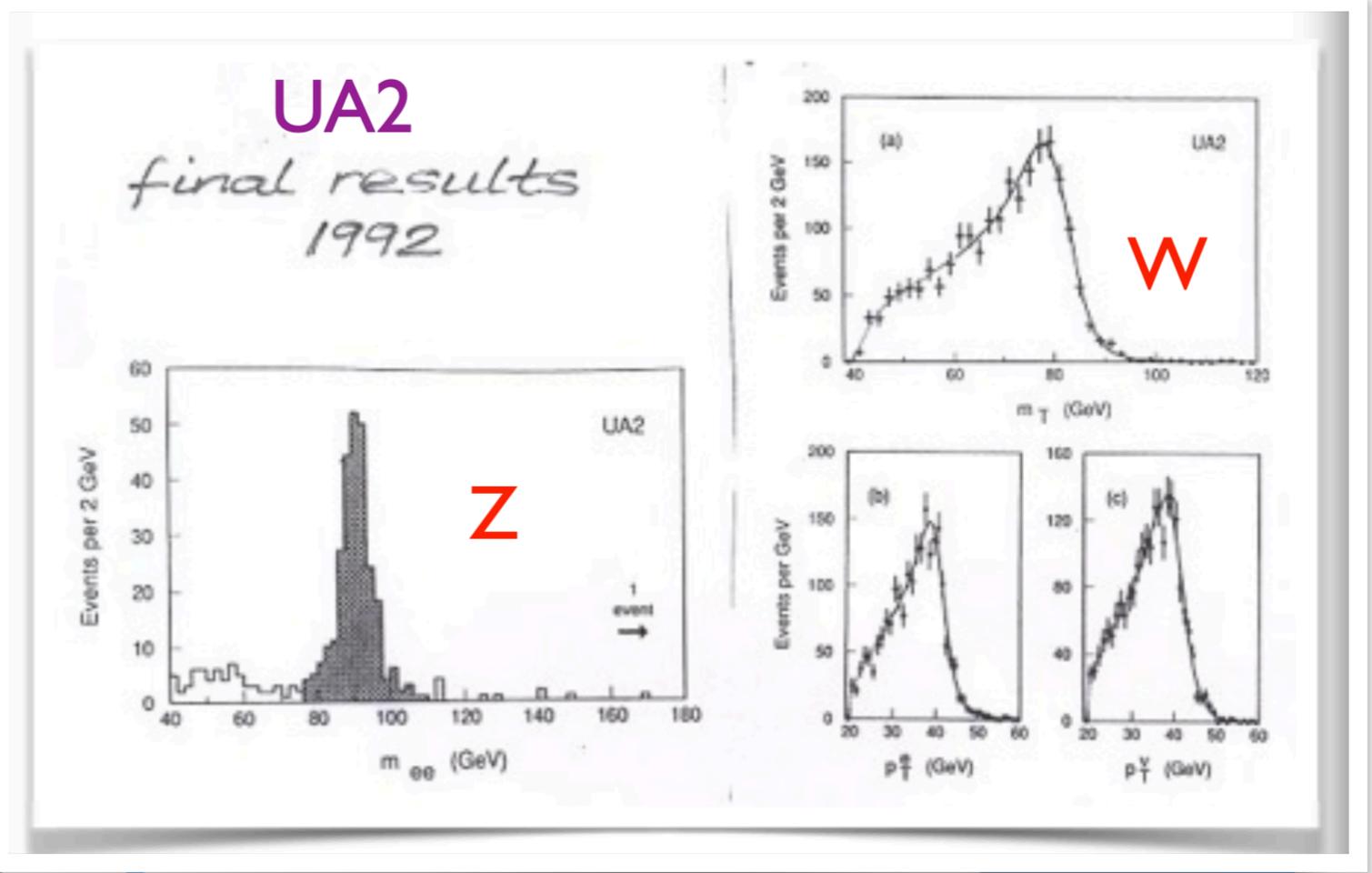
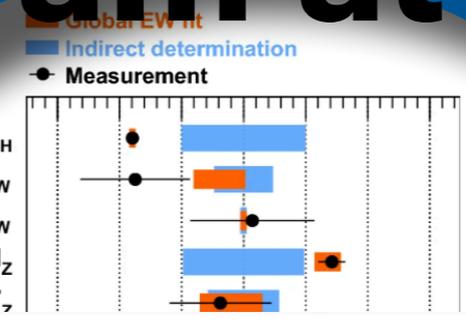
40 years after their discovery, the **W,Z bosons** are still at the heart of the LHC physics programme.

Why is this?

- W,Z properties are related to fundamental symmetries of SM theory (EWSB)
- Their relations to other particles provide some of the most powerful tests of the theory — sensitive probes of possible new physics



W^\pm, Z, γ^*



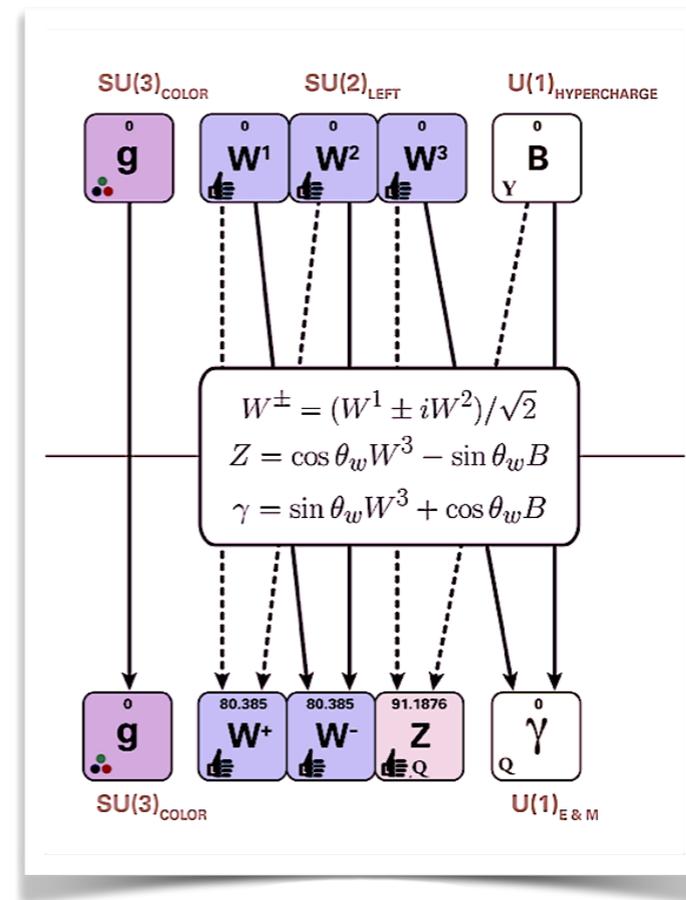
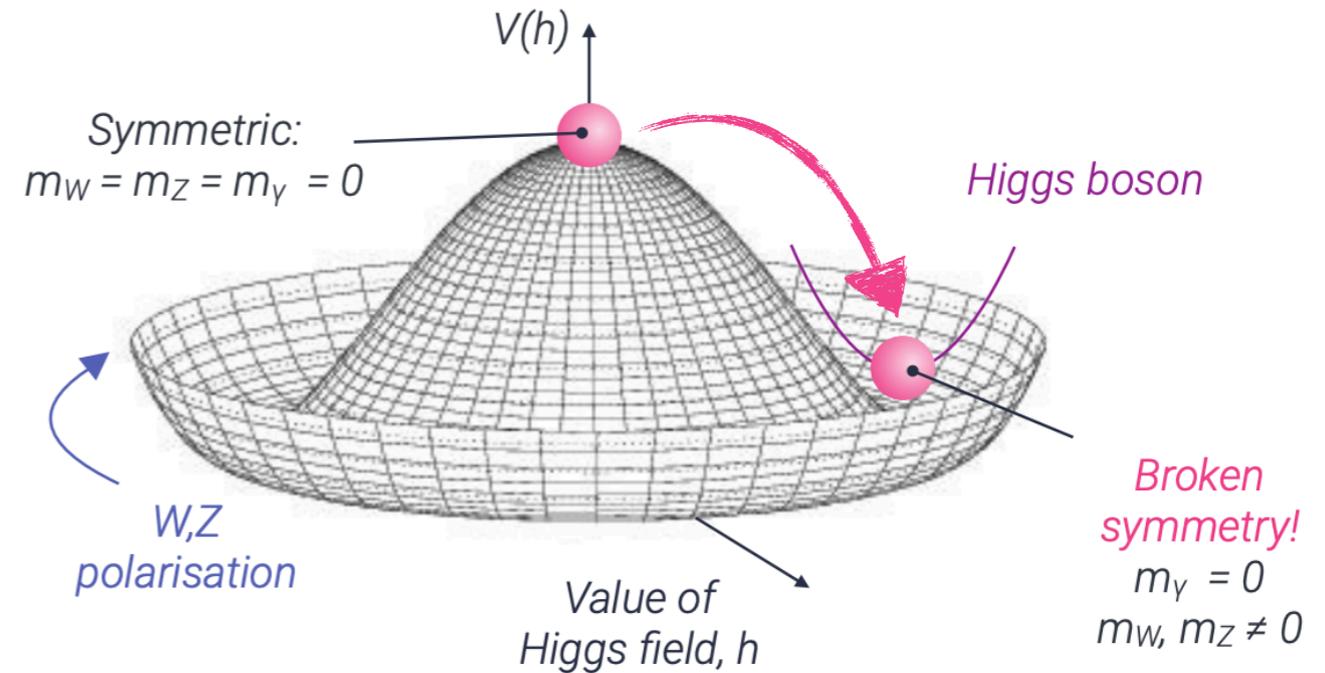
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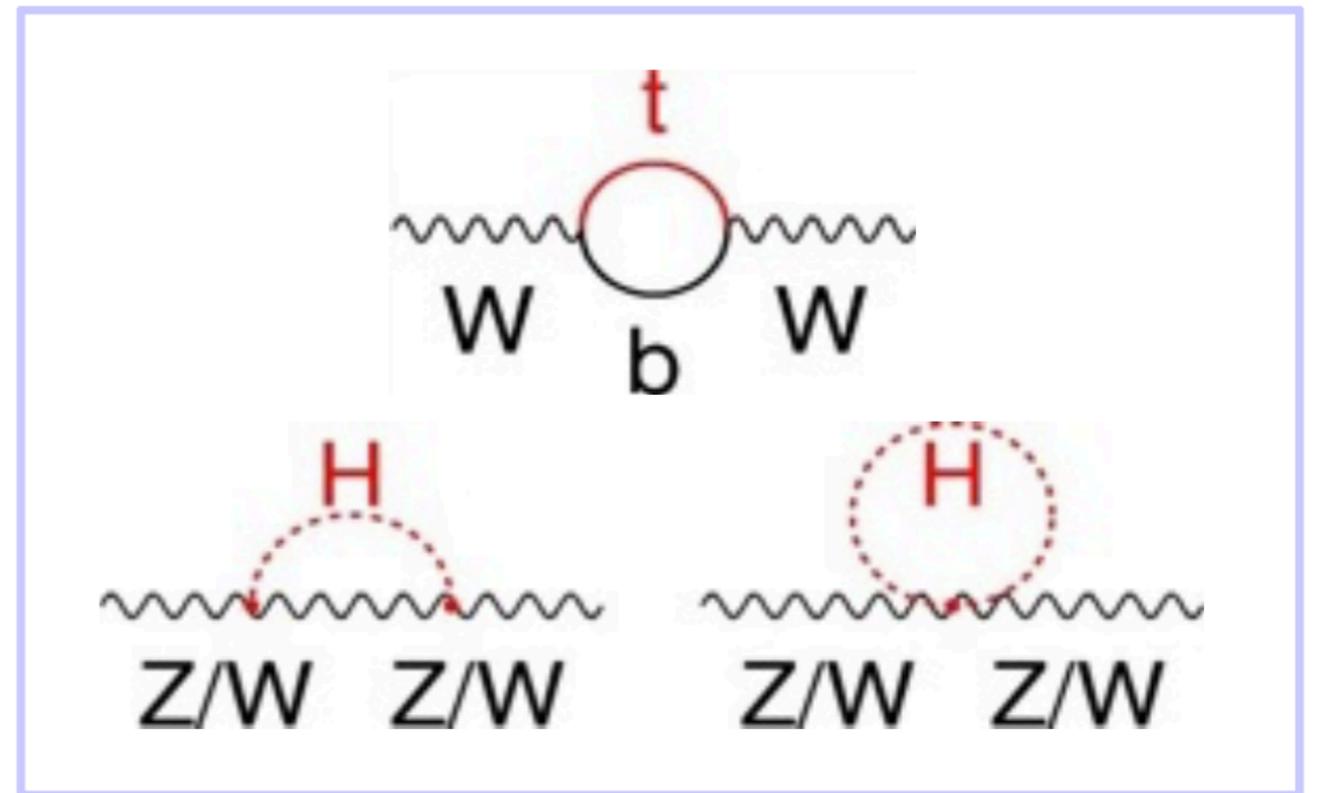
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m_t, m_W, m_H related !



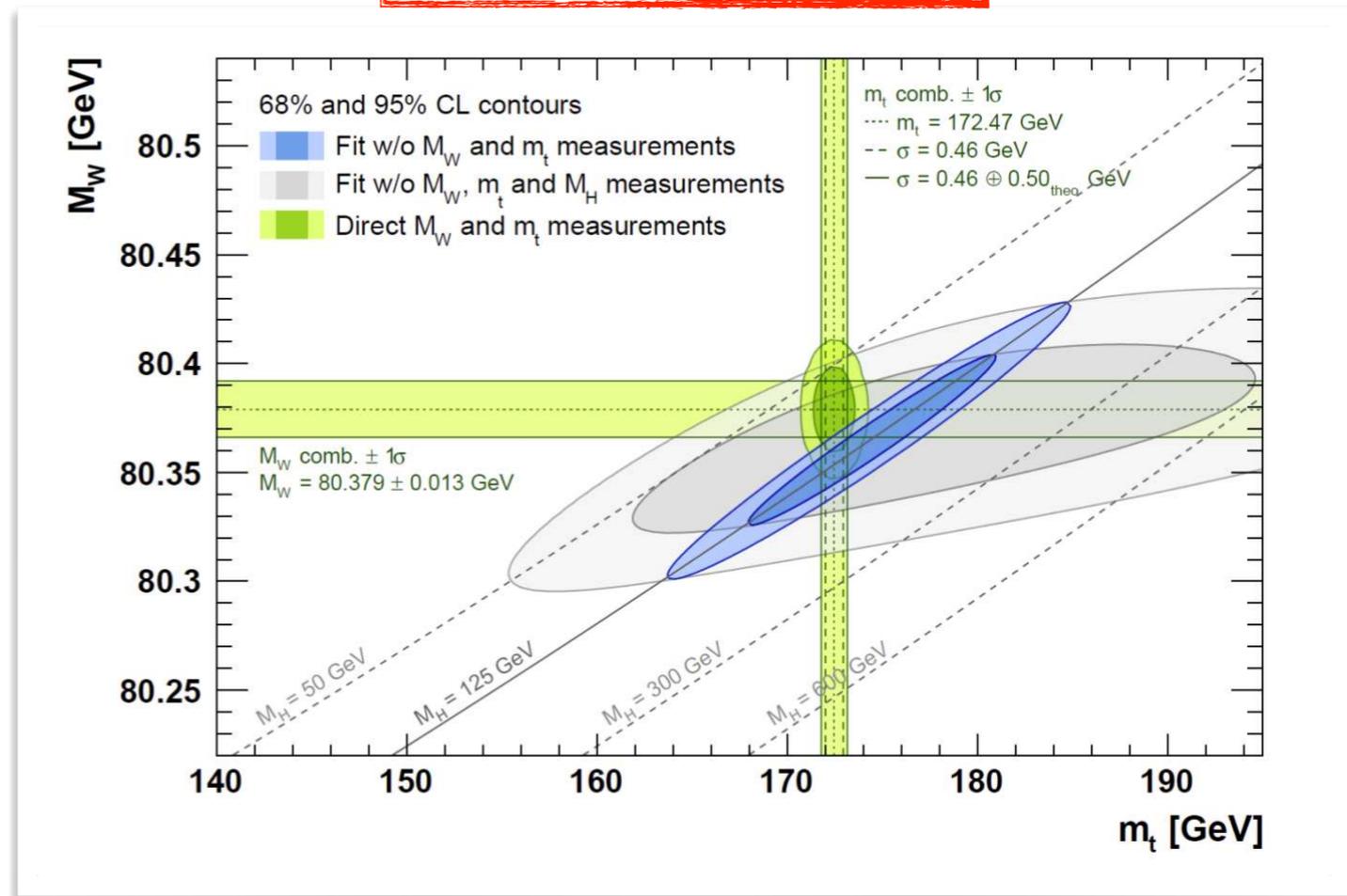
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W,Z properties

► The electroweak gauge sector of the Standard Model is constrained by three precisely measured parameters

REL. UNC.

$O(10^{-10})$

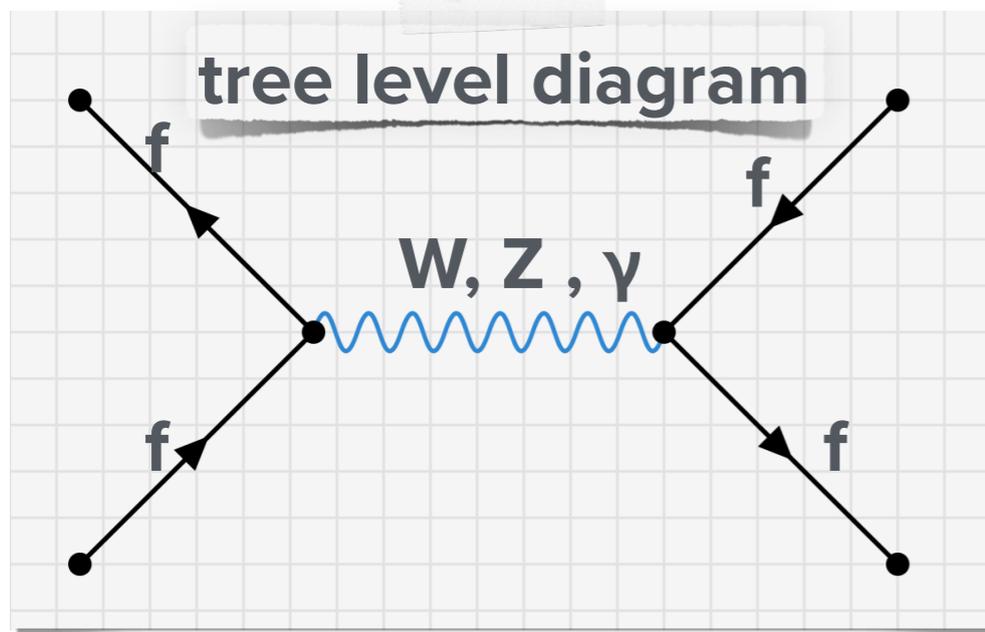
$O(10^{-7})$

$O(10^{-5})$

$$\begin{aligned}\alpha &= 1/137.035999139(31) \\ G_F &= 1.1663787(6) \times 10^{-5} \text{ GeV}^{-2} \\ m_Z &= 91.1876(21) \text{ GeV}\end{aligned}$$

**PROPERTIES OF THE W,Z BOSONS
CAN BE EXPRESSED AS:**

$$\begin{aligned}m_W^2 &= \frac{\pi\alpha}{\sqrt{2}G_F \left(1 - \frac{m_W^2}{m_Z^2}\right)} \\ \sin^2 \theta_W &= 1 - \frac{m_W^2}{m_Z^2} \\ \Gamma_W &= \frac{3G_F m_W^3}{2\sqrt{2}\pi}\end{aligned}$$



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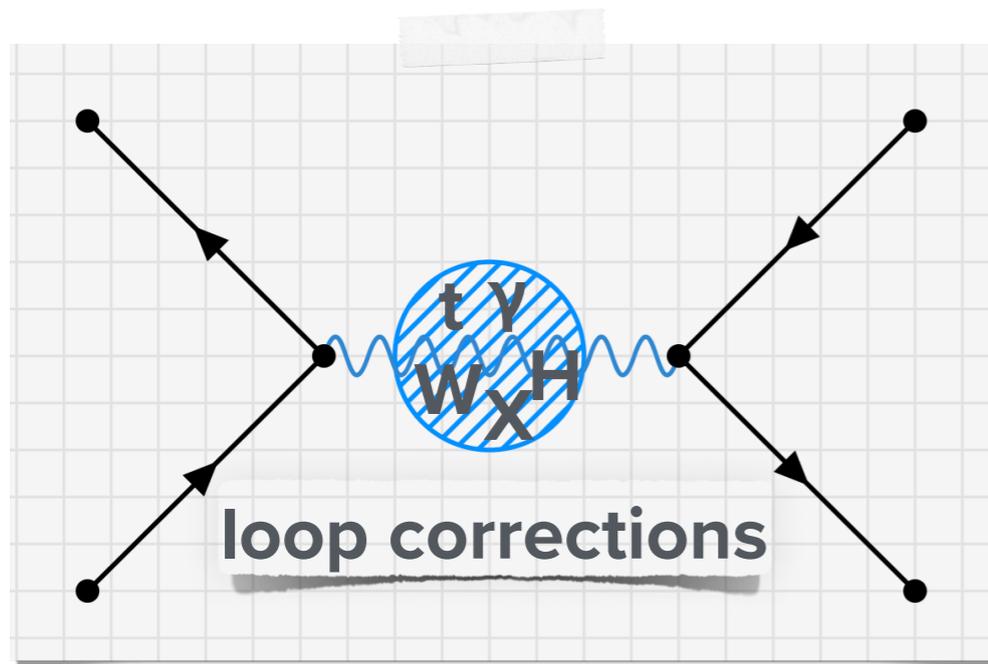
$O(10^{-10})$

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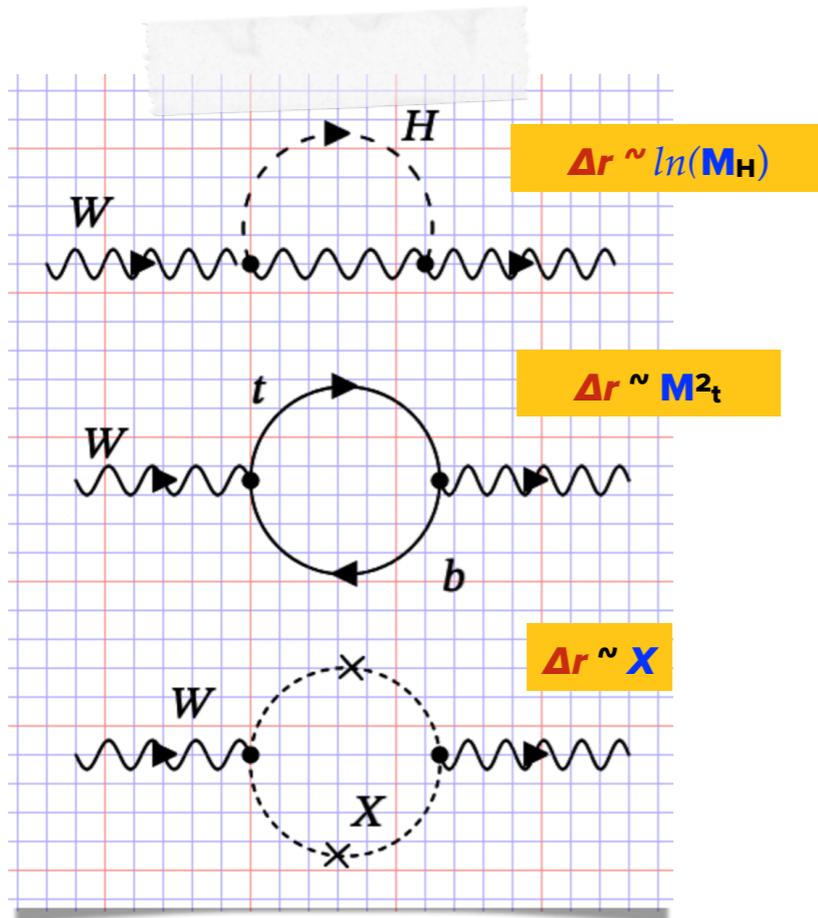
**PROPERTIES OF THE W,Z BOSONS
CAN BE EXPRESSED AS:**

$$\begin{aligned}m_W^2 &= \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2)} \underline{(1 - \Delta r)} \\ \sin_{\text{eff}}^2 \theta_W &= \left(1 - \frac{m_W^2}{m_Z^2}\right) \underline{\kappa} \\ \Gamma_W &= \frac{3G_F m_W^3}{2\sqrt{2}\pi} \underline{\rho}\end{aligned}$$



Higher order corrections modify these relations, and determine sensitivity to other particle masses and couplings

Loop corrections in m_W



$$= \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2) (1 - \Delta r)}$$



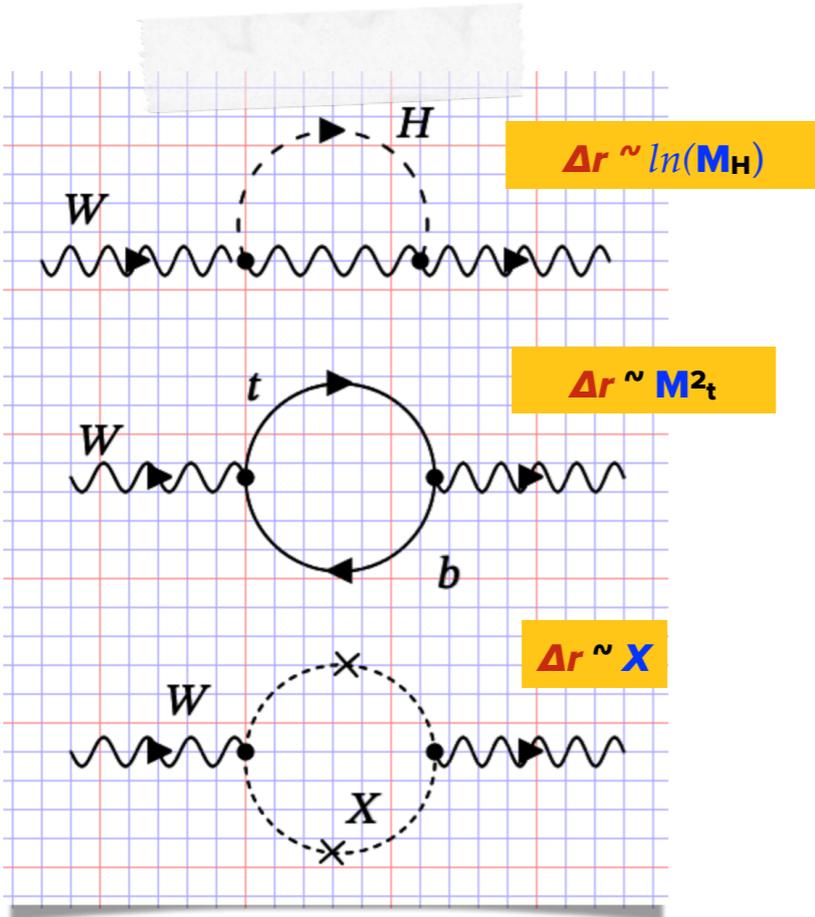
In SM, Δr correction on m_W reflects loop corrections and depends on m_t^2 and $\ln(m_H)$ but can potentially also hide contributions from **new physics**

- ▶ SM relation between m_t , m_W , m_H is the most popular way to test the predictive power of global fits in high-energy physics.
 - Historically has been used to predict m_t and put constraint on the m_H before they were discovered!

Predictivity of the SM

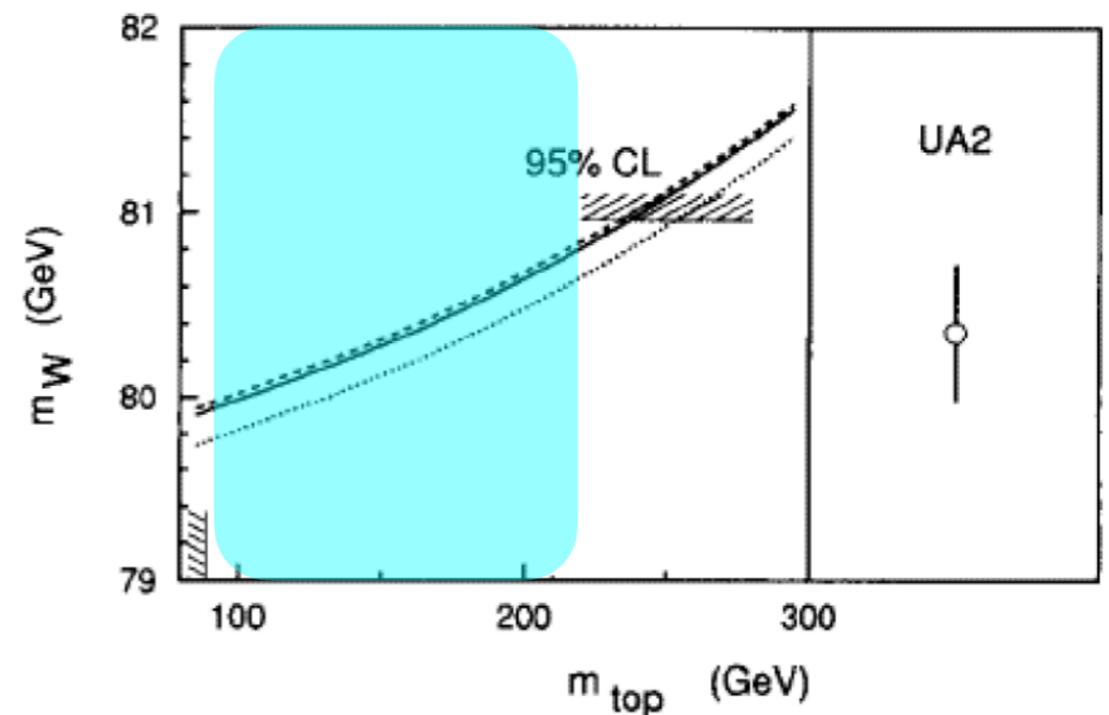


$$= \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2) (1 - \Delta r)}$$



In SM, Δr correction on m_W reflects loop corrections and depends on m_t^2 and $\ln(m_H)$ but can potentially also hide contributions from **new physics**

UA2 m_W measurement in 1983 Provide first stringent limits on the m_{top} 10 years before the first observation

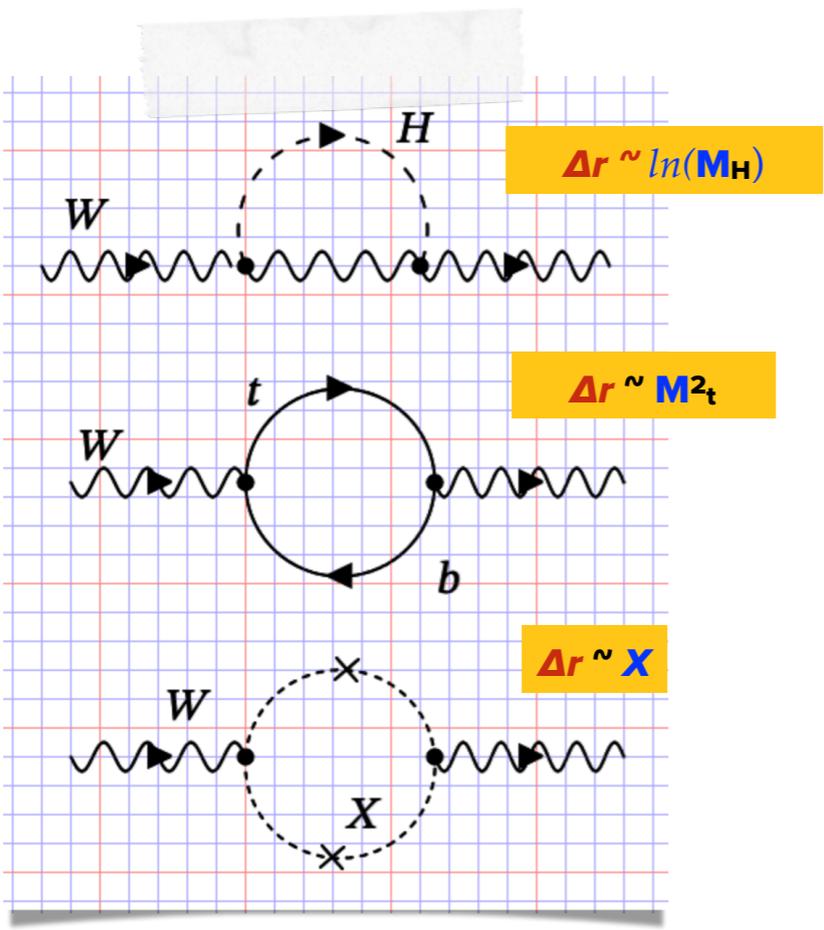


The Discovery of the W and Z Particles @ UA1, UA2

Predictivity of the SM

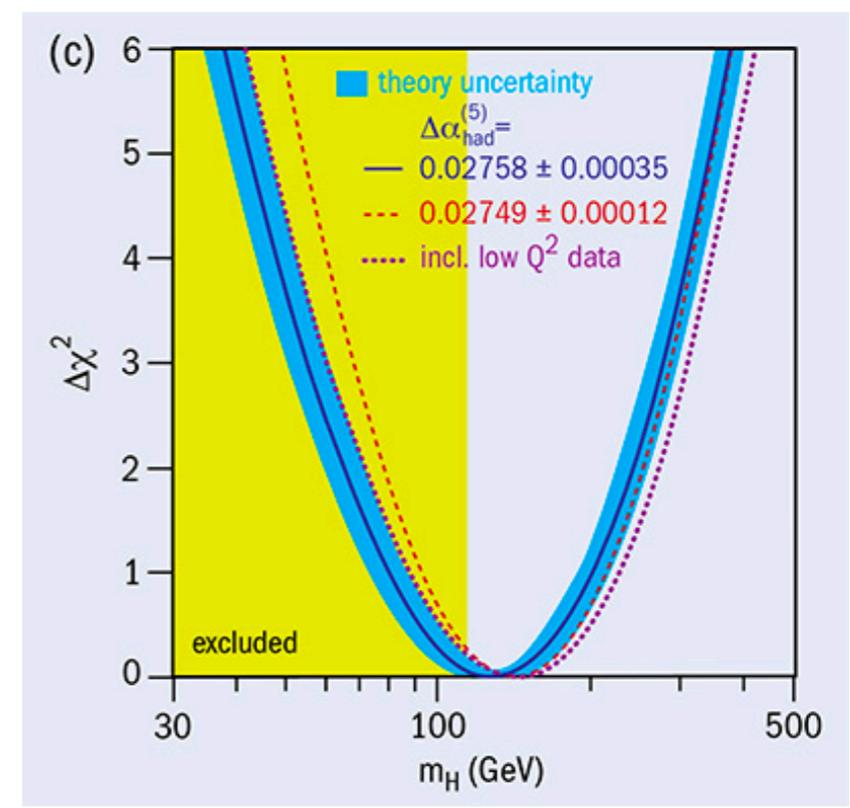


$$= \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2)} (1 - \Delta r)$$



In SM, Δr correction on m_W reflects loop corrections and depends on m_t^2 and $\ln(m_H)$ but can potentially also hide contributions from **new physics**

IN 2005 the legacy LEP results on m_W m_Z have been used to constrain the HIGGS boson mass (m_H) almost a decade before its discovery

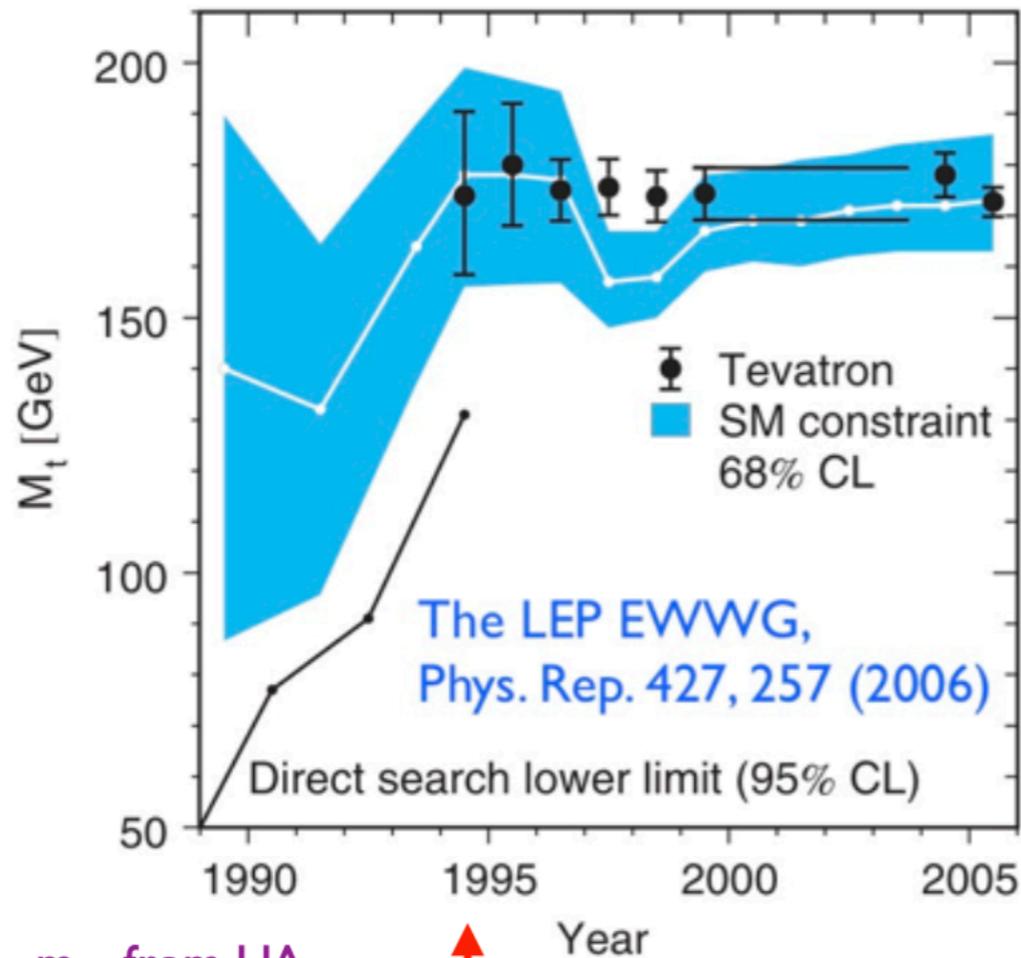


LEP's electroweak final results

Predictive Power of the SM early 2000



The Top Quark

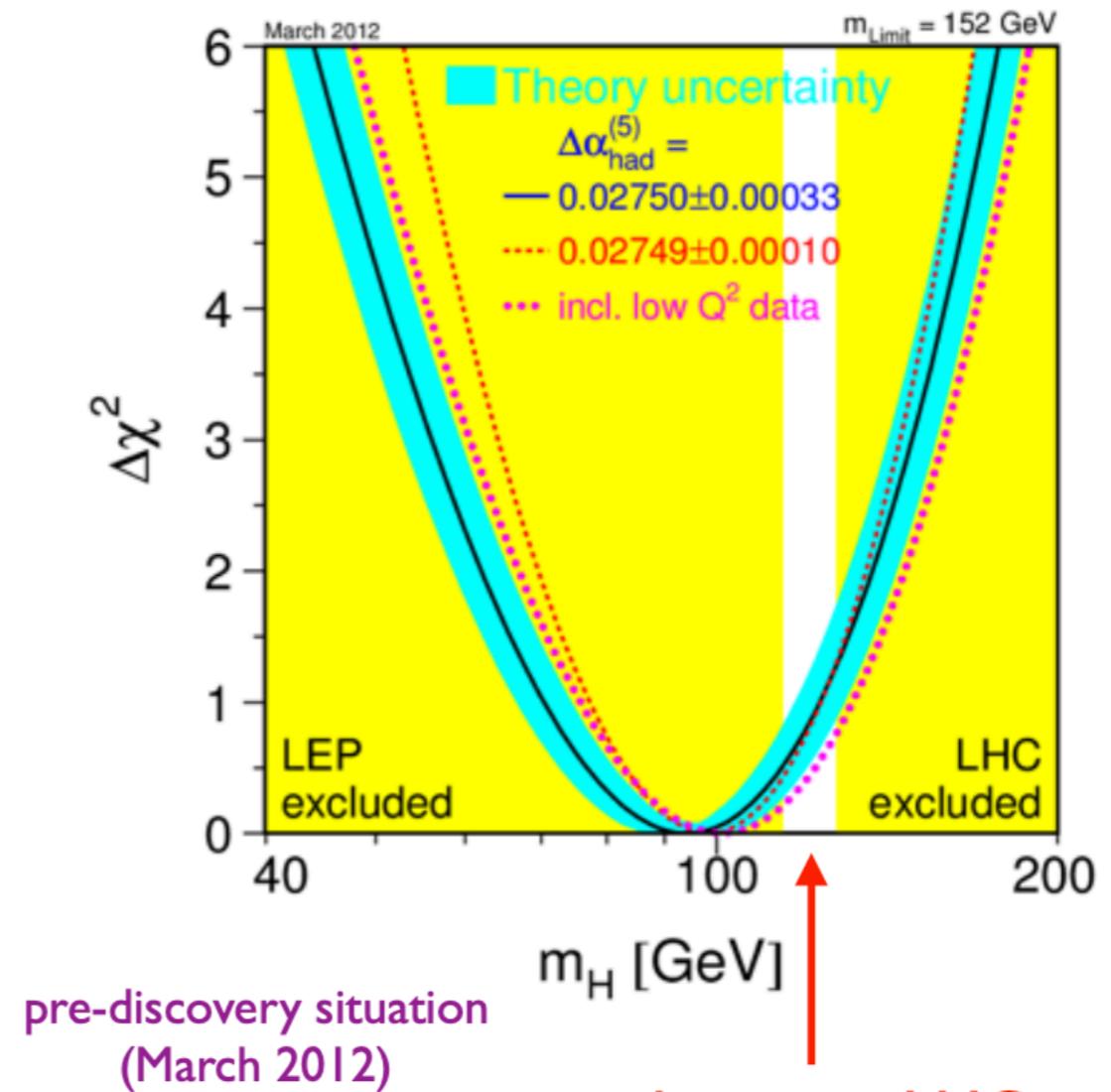


m_W from UA
 + precision EW
 from LEP-I

discovery
 Tevatron
 1994

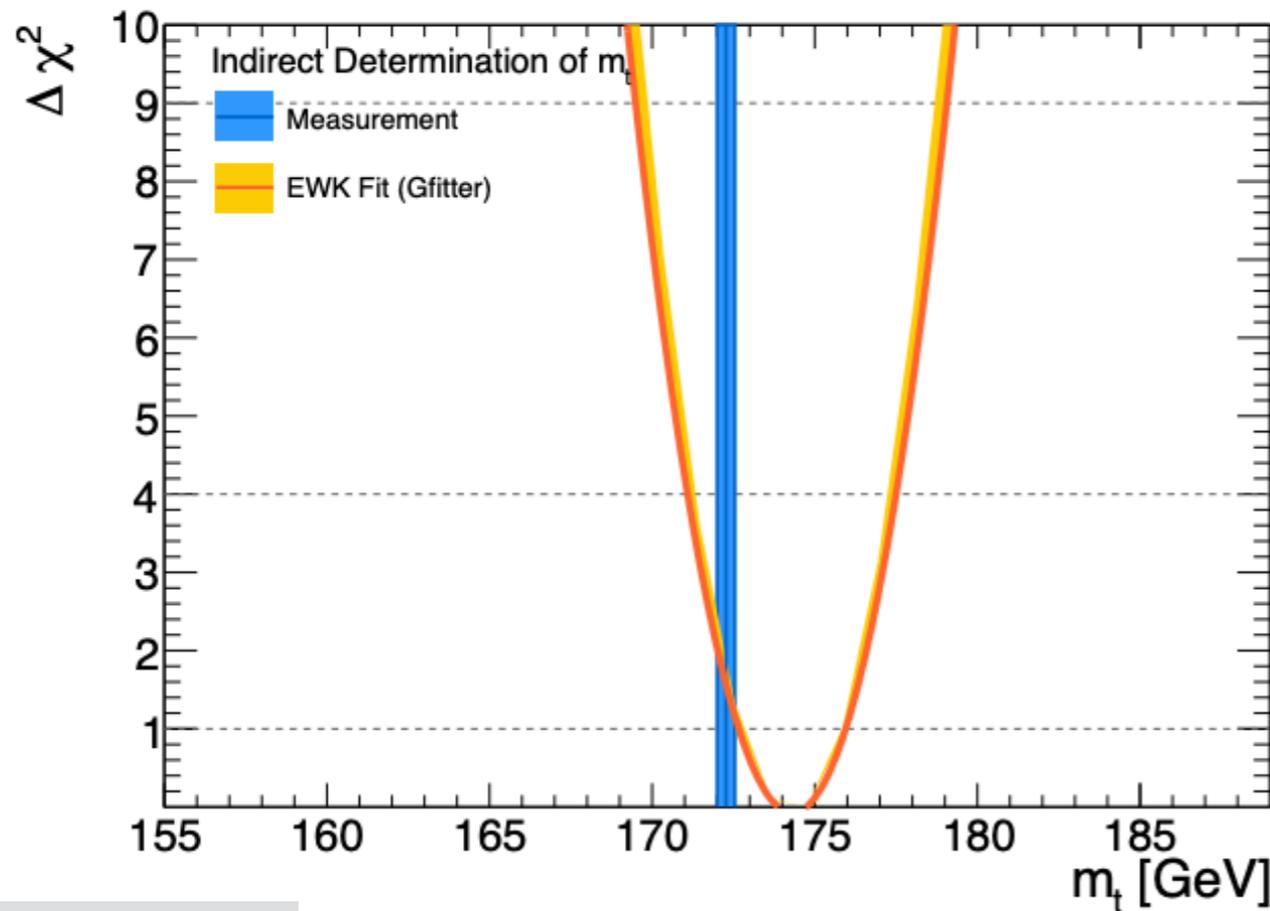
W mass
 from LEP-II

The Higgs Boson

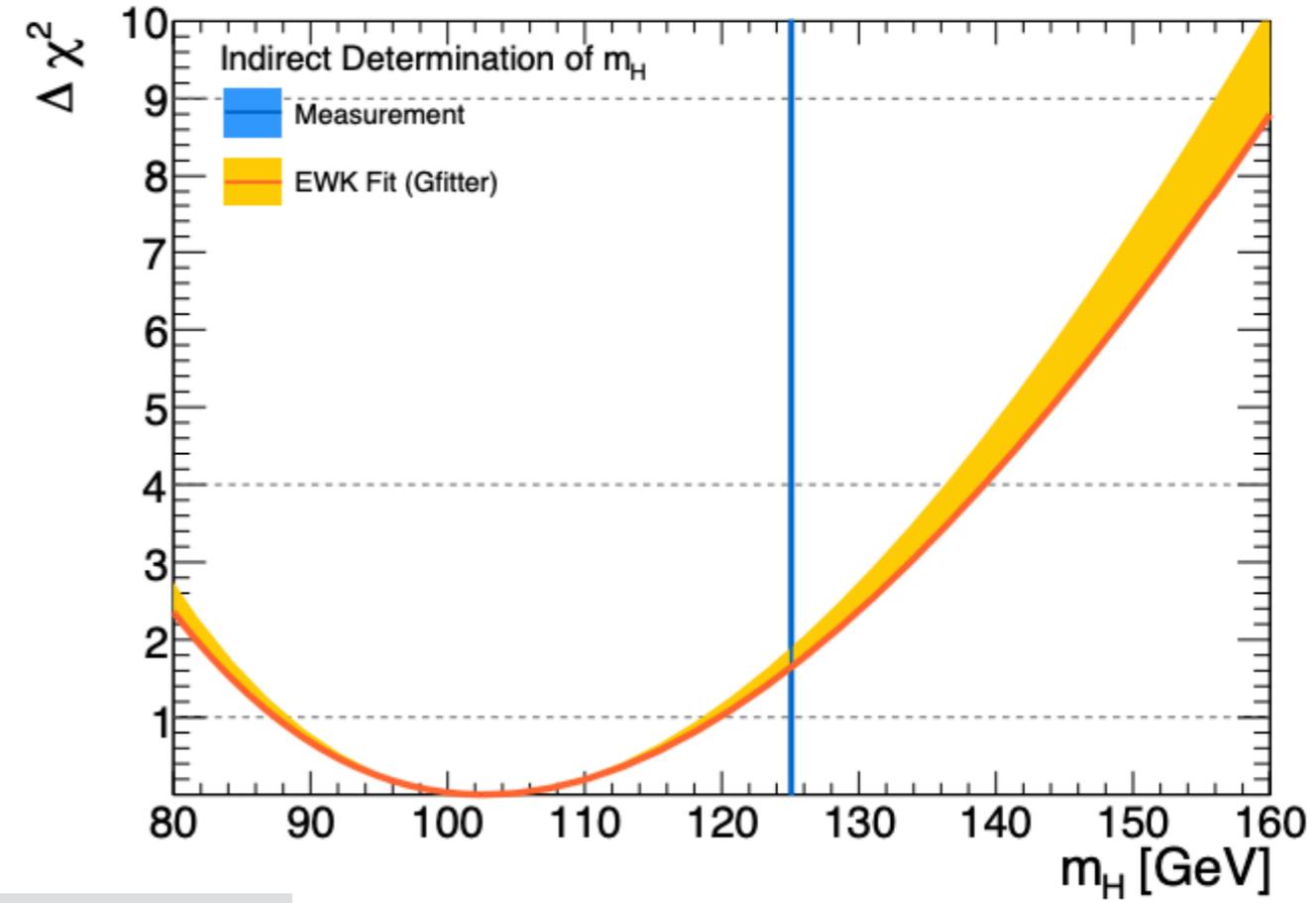


discovery LHC
 2012

right now...



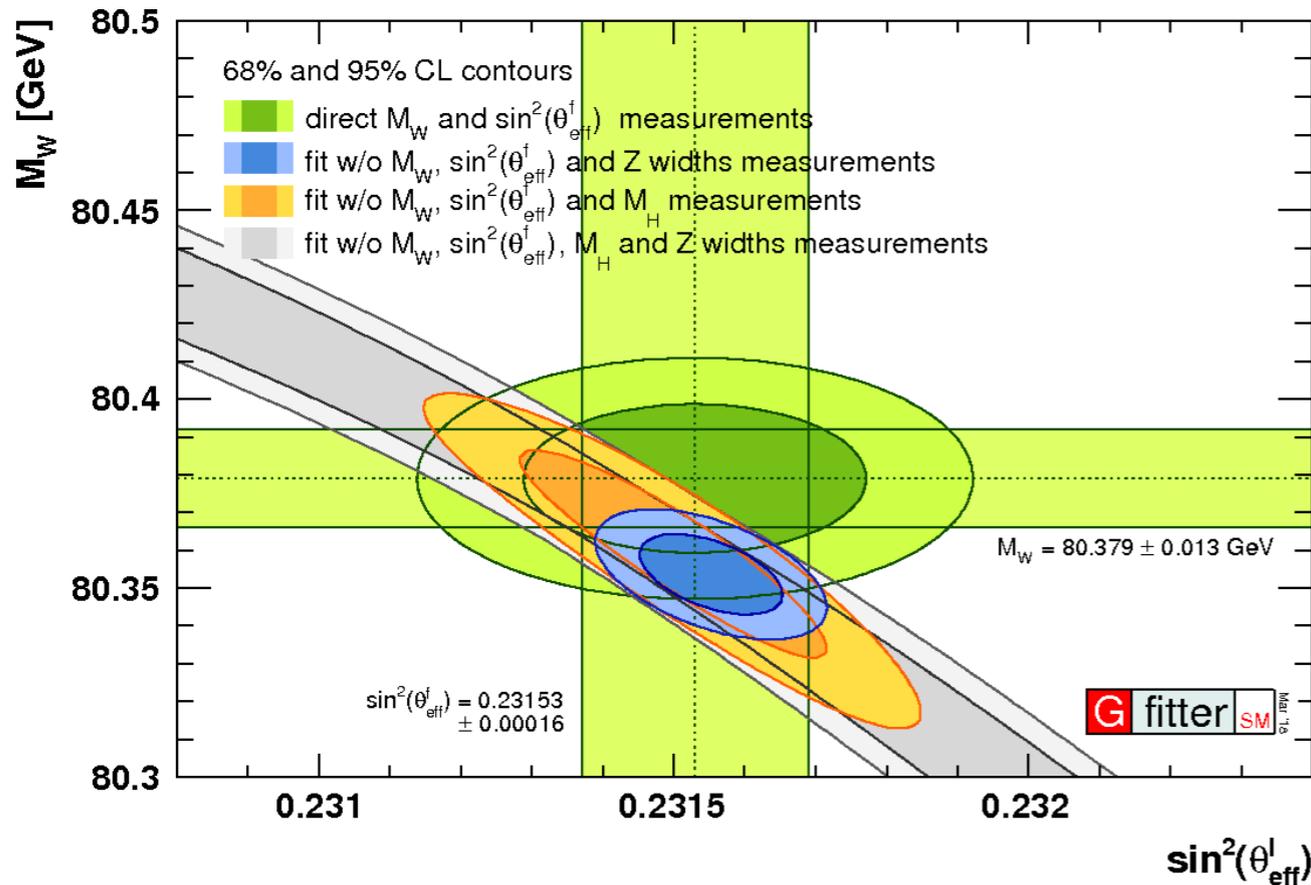
credit to M. Schott



credit to M. Schott

m_t and m_H are now so well-measured ($\delta m_t \sim 0.3$ GeV; $\delta m_H \sim 0.1$ GeV) that higher precision has minimal impact on the indirect determination of the others parameters

The custodial symmetry



<https://arxiv.org/pdf/hep-ph/0302058>

- The custodial symmetry protects this relation from large radiative corrections. All corrections to the ρ parameter are therefore proportional to terms that break the custodial symmetry (though radiative correction)

$$\rho_0 \equiv \frac{M_W^2}{M_Z^2 \hat{c}_Z^2 \hat{\rho}}, \quad \rho_0 = 1.00031 \pm 0.00019,$$

PDG, LEP legacy

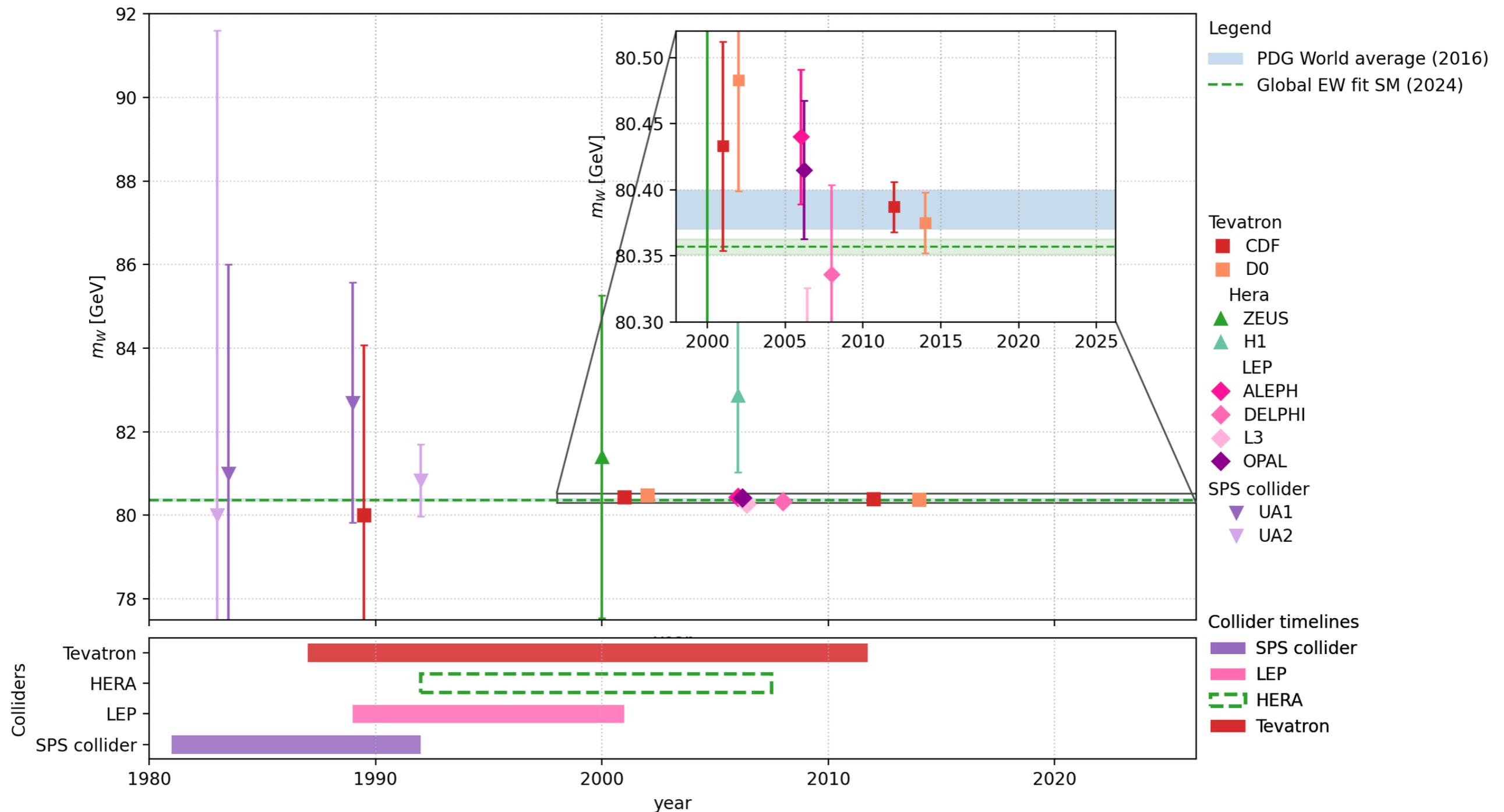
$$\rho \equiv \frac{M_W^2}{M_Z^2 \cos^2 \theta} = 1.$$

ADDITIONAL SYMMETRY WHICH BOUND THE INDIRECT DETERMINATION OF M_W AND $\sin^2 \theta_W$
 → EW FIT DETERMINATION OF M_W AND $\sin^2 \theta_W$ MORE PRECISE THAN THE EXPERIMENTAL MEASUREMENT

45 years of measurement

This is not the case for the W-boson mass

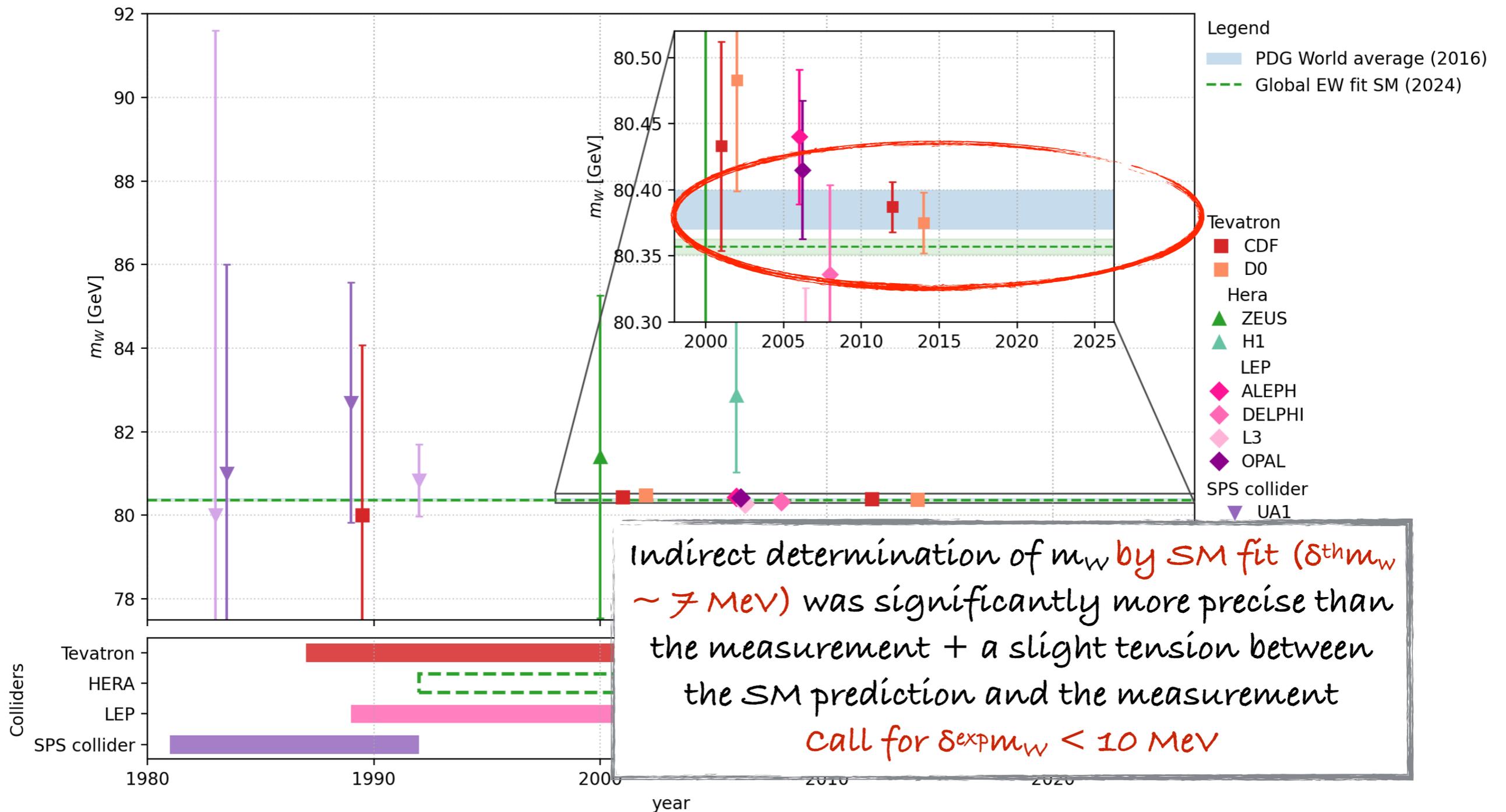
Situation of m_W measurements 10 years ago



45 years of measurement

This is not the case for the W-boson mass

Situation of m_W measurements 10 years ago



45 years of measurement



March 2017

Life and Physics
Physics

This article is more than 8 years old

From gravity to the Higgs we're still waiting for new physics

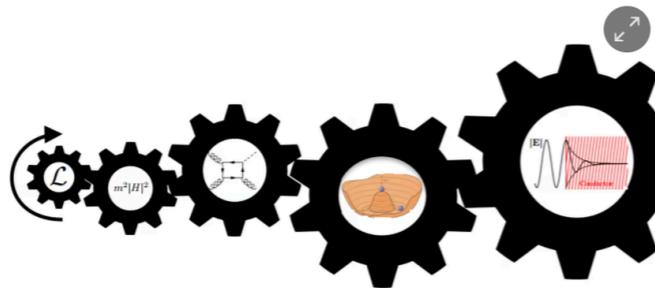
Annual physics jamboree Rencontres de Moriond has a history of revealing exciting results from colliders, and this year new theories and evidence abound

Ben Allnach

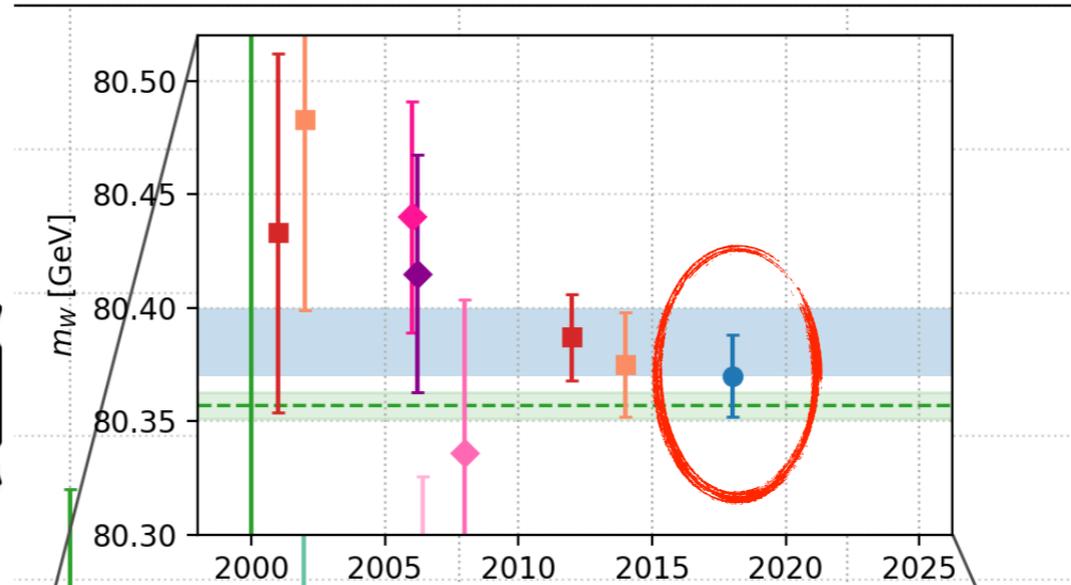
Fri 24 Mar 2017 14:11 CET

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Prefer the Guardian on Google



A new theoretical idea getting quite a bit of attention is A Clockwork Theory, invented by



Legend

PDG World average (2016)

Global EW fit SM (2024)

LHC
ATLAS

Tevatron

CDF

D0

Hera

ZEUS

H1

LEP

ALEPH

DELPHI

L3

OPAL

SPS collider

UA1

UA2

Collider timelines

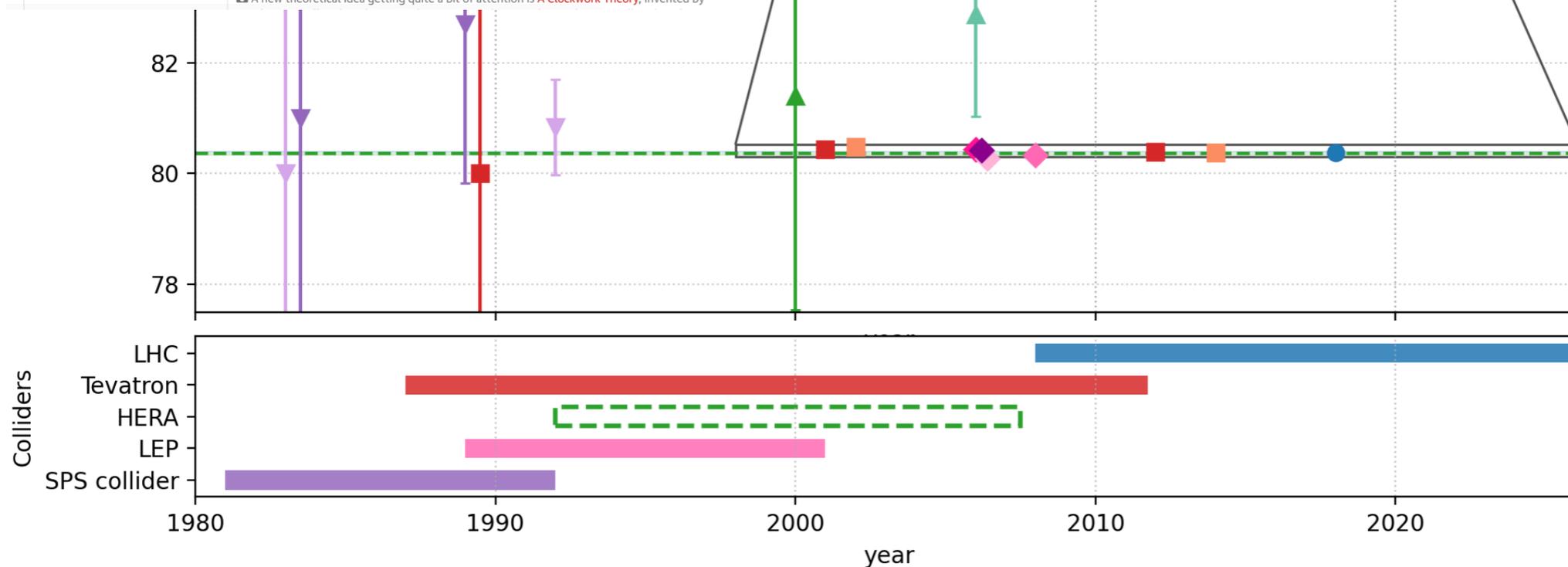
SPS collider

LEP

HERA

Tevatron

LHC



Colliders

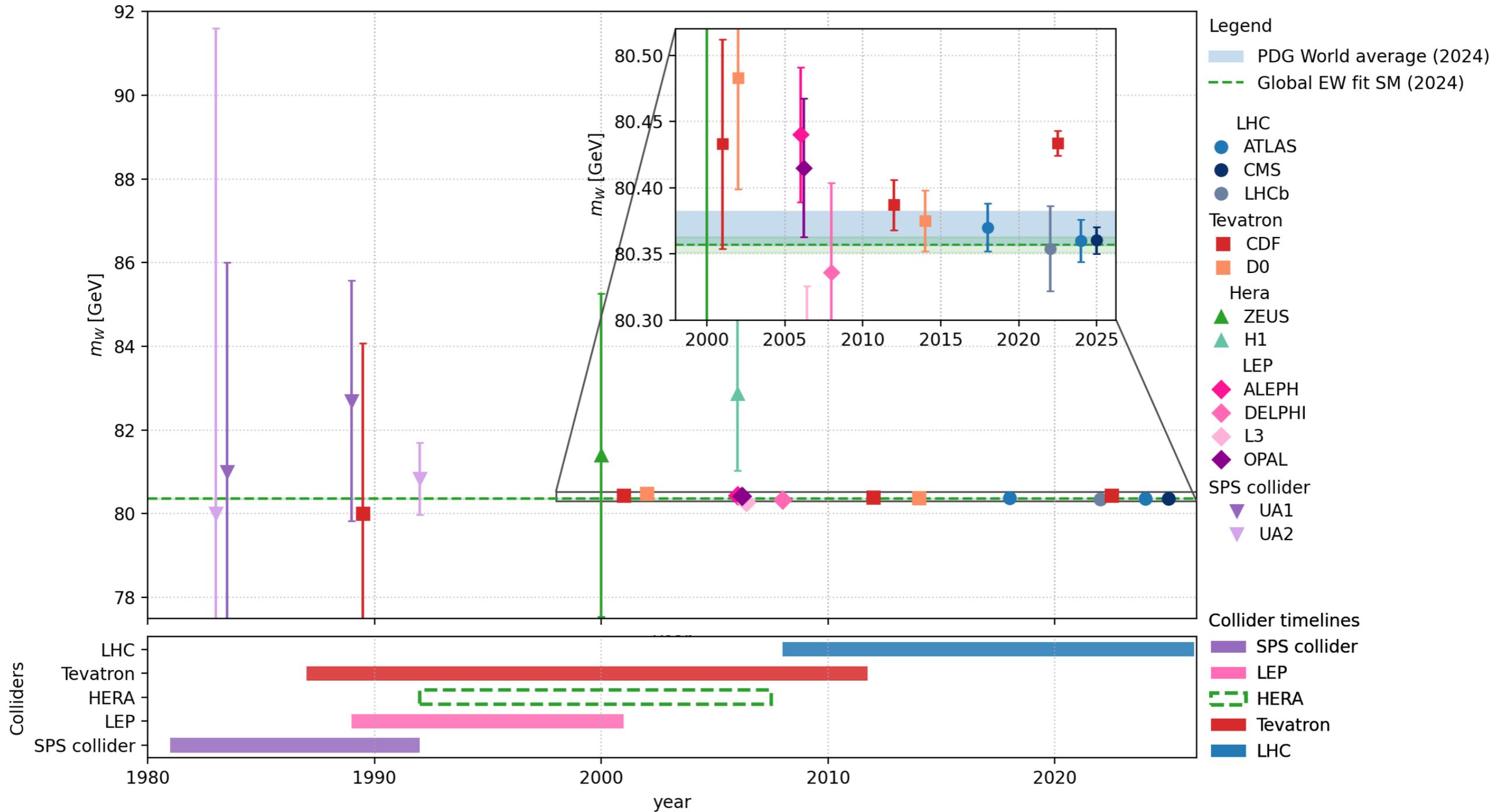
LHC
Tevatron
HERA
LEP
SPS collider

1980 1990 2000 2010 2020

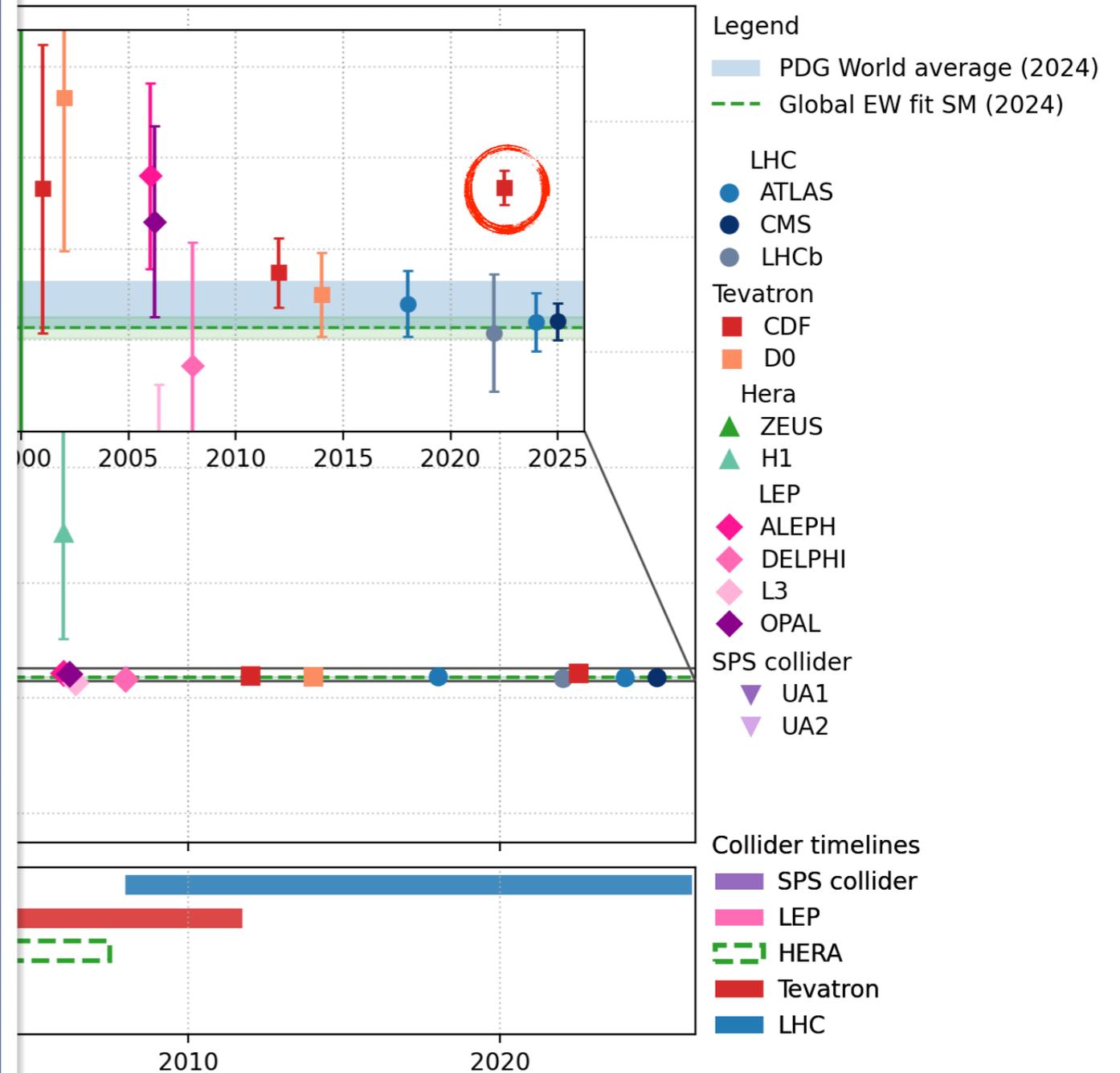
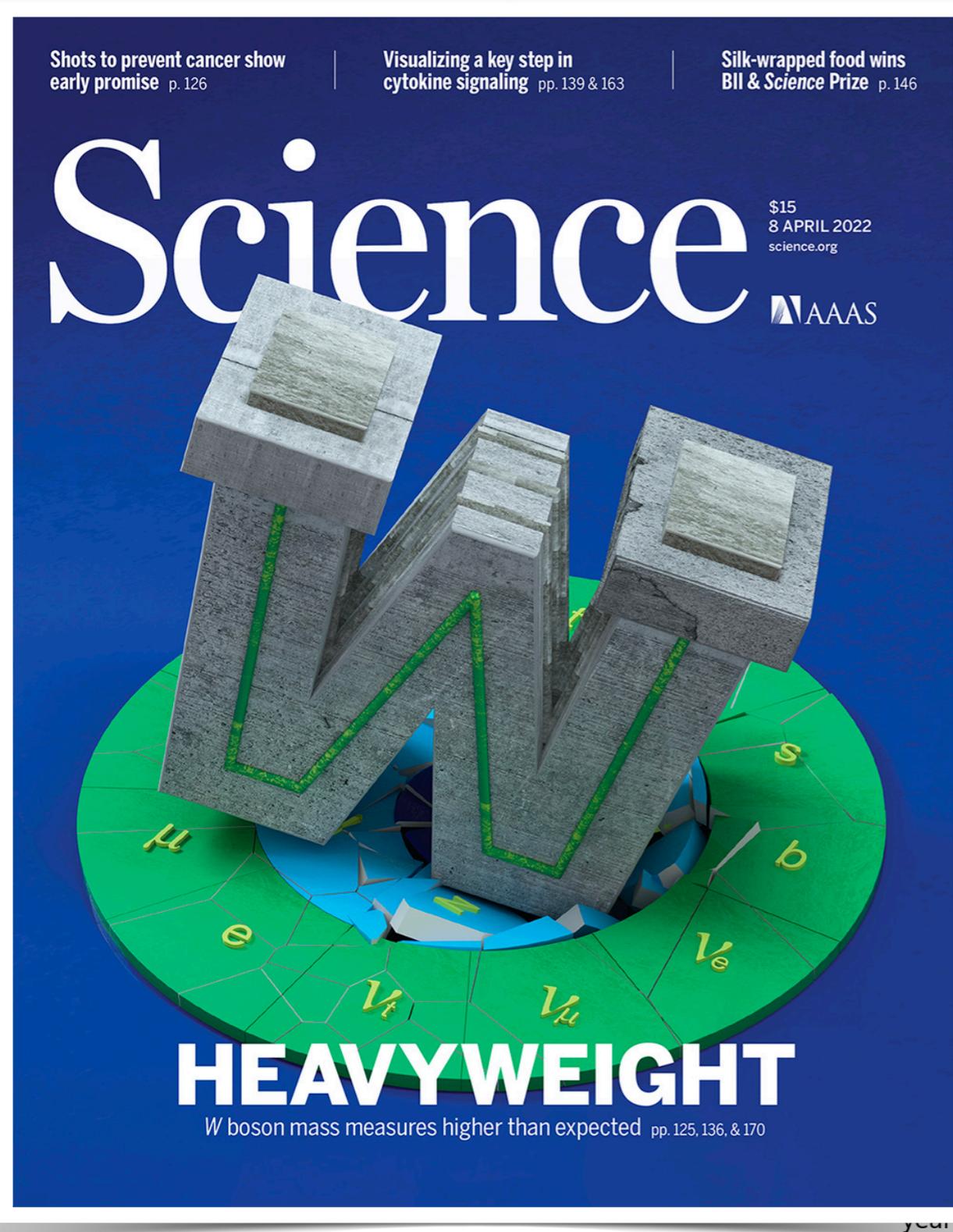
year

Much better predicted than measured

Situation of m_W measurements today



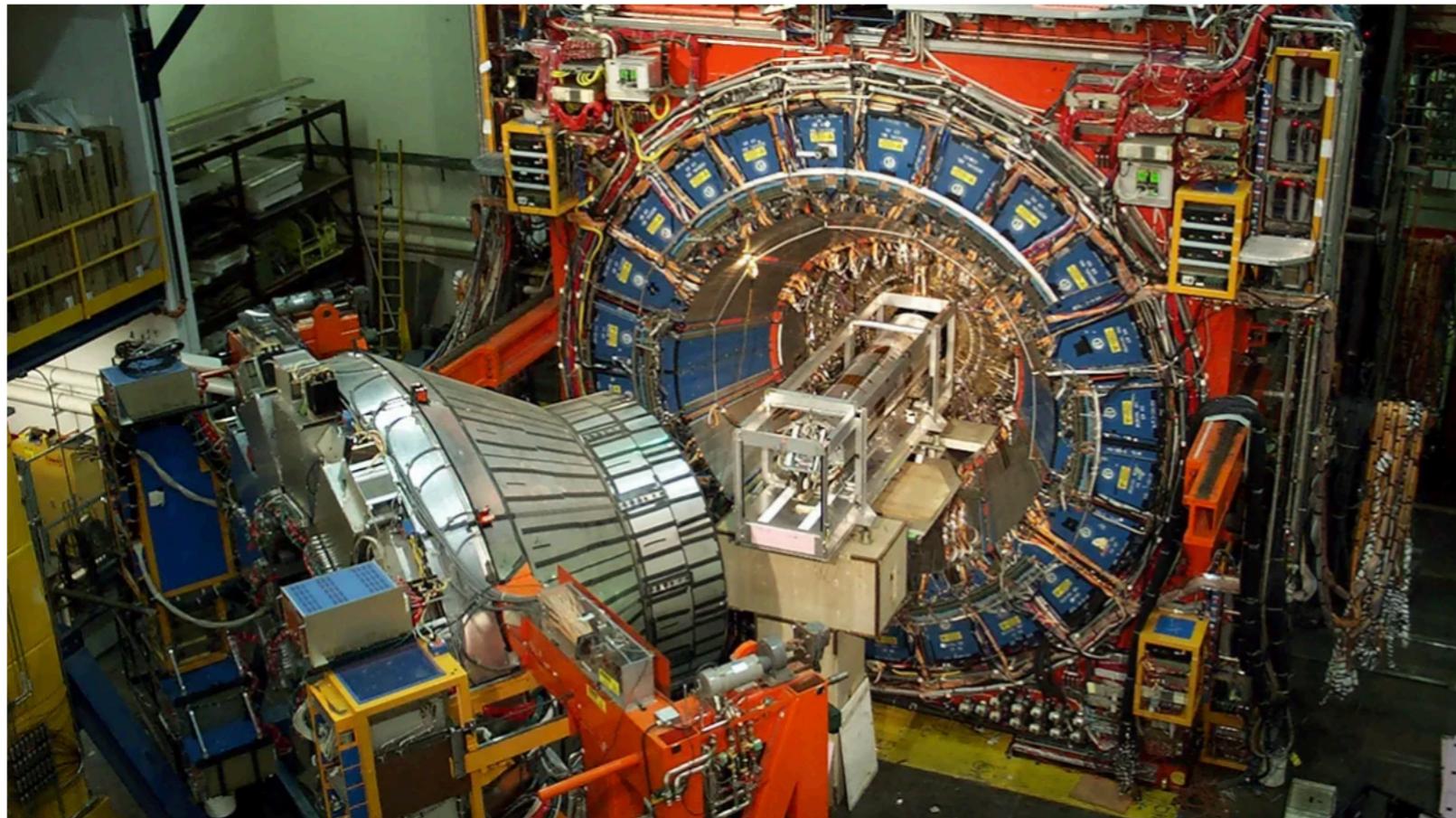
Much better predicted than measured



Surprise W boson measurement could rewrite particle physics

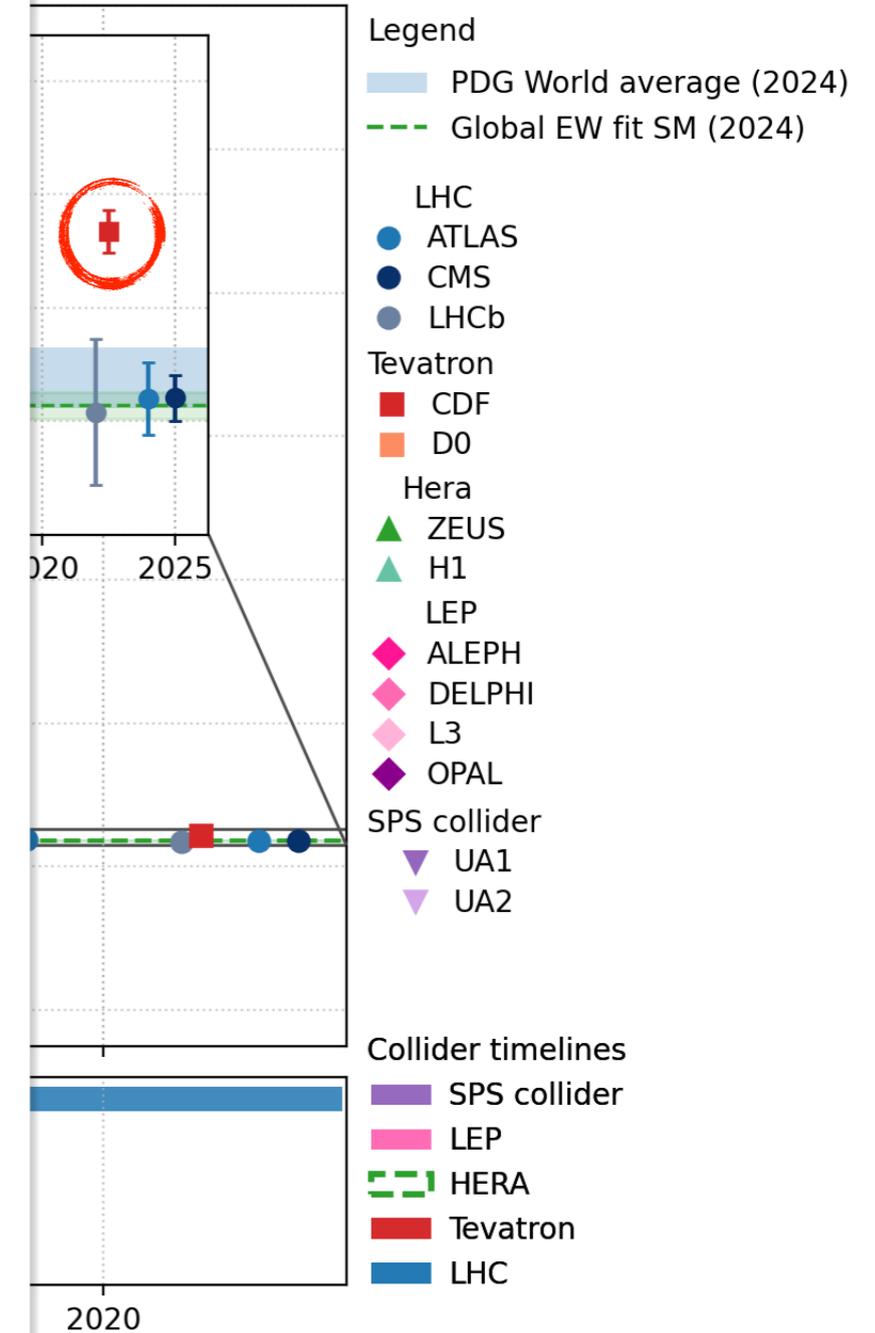
News By Tereza Pultarova published April 8, 2022

A subatomic particle called the W boson may be heavier than expected, a surprising finding that might lead to a shake-up of physics' grand model of how the world works on the microscale.



Physicists used the Tevatron collider at Fermilab to estimate the mass of the W boson. (Image credit: Fermilab)

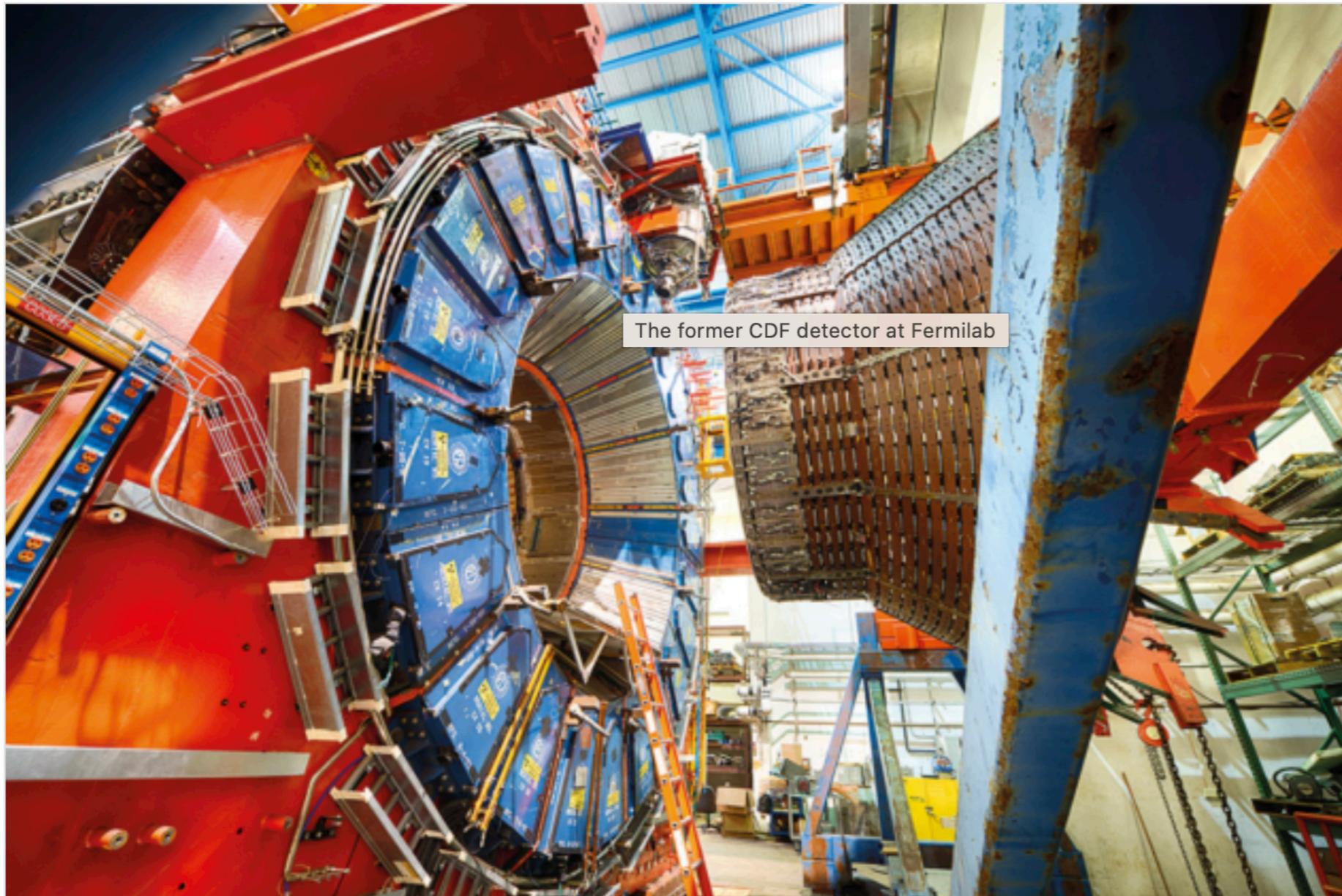
n measured



The W boson's midlife crisis

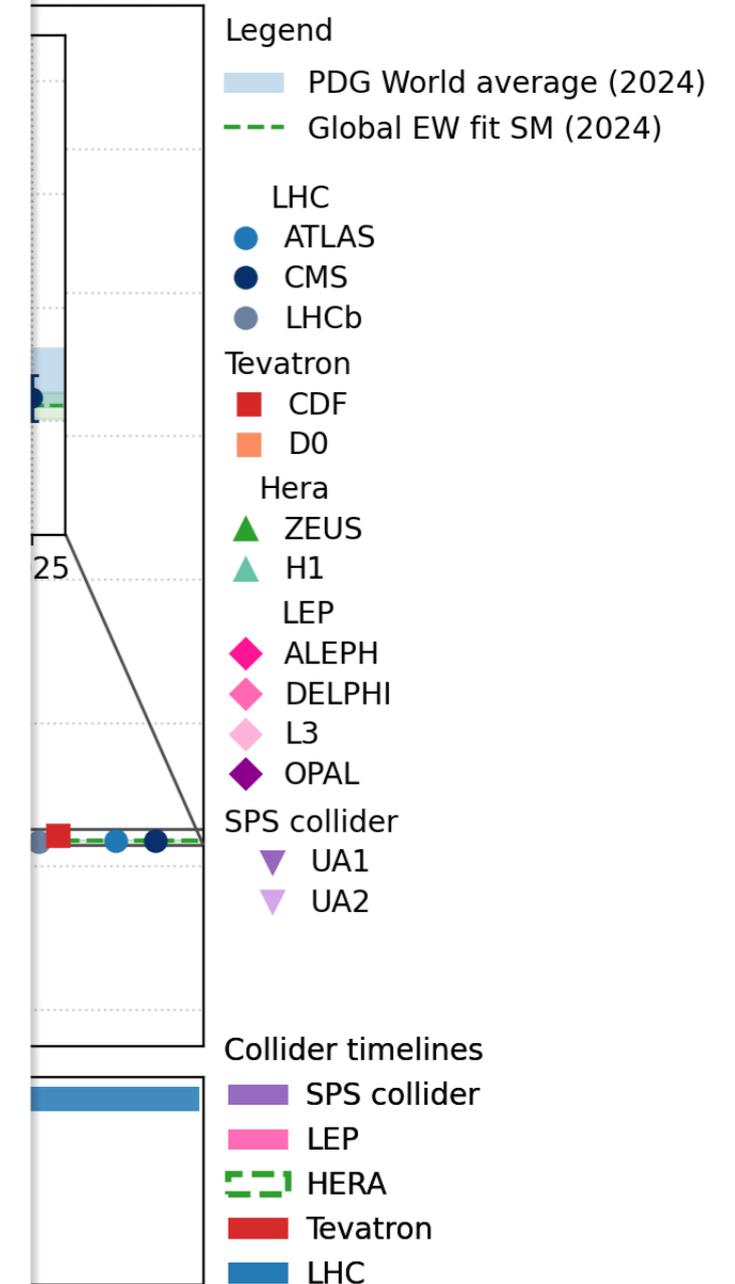
24 August 2023

Forty years after its discovery, the W boson continues to intrigue. Chris Hays describes recent progress in understanding a surprisingly high measurement of its mass using data from the former CDF experiment.

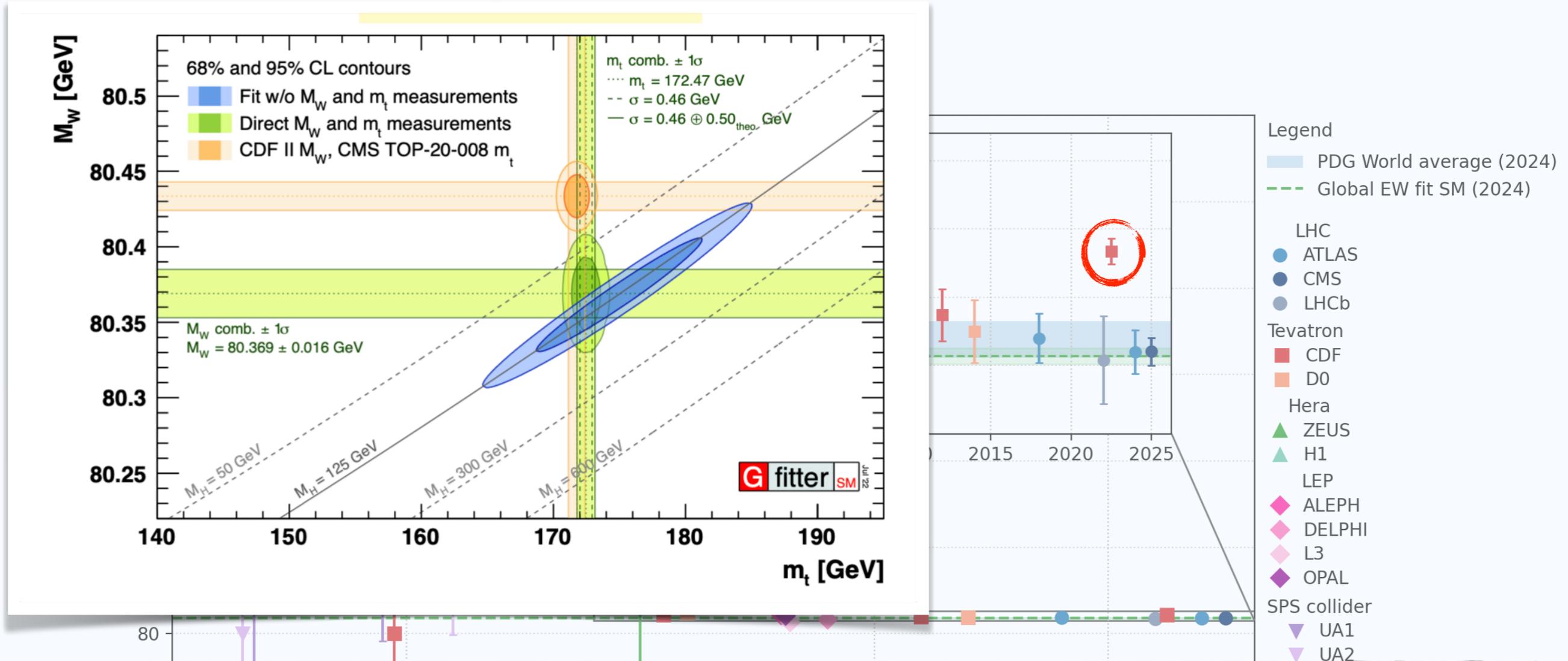


Massive The former CDF detector at Fermilab, data from which point towards an unexpectedly high value of the

measured

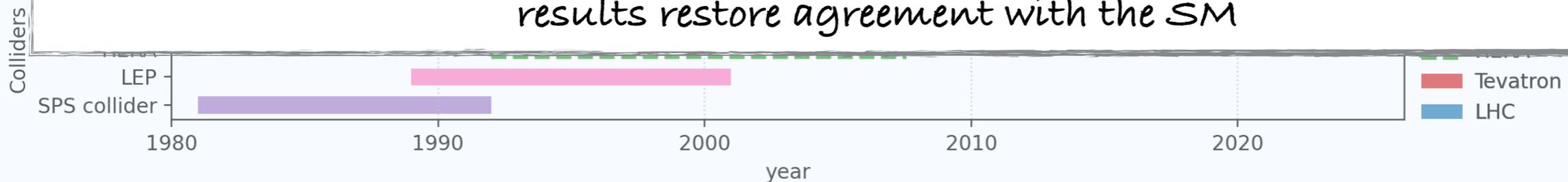


Midlife crisis



Ultra-precise, surprisingly heavy.

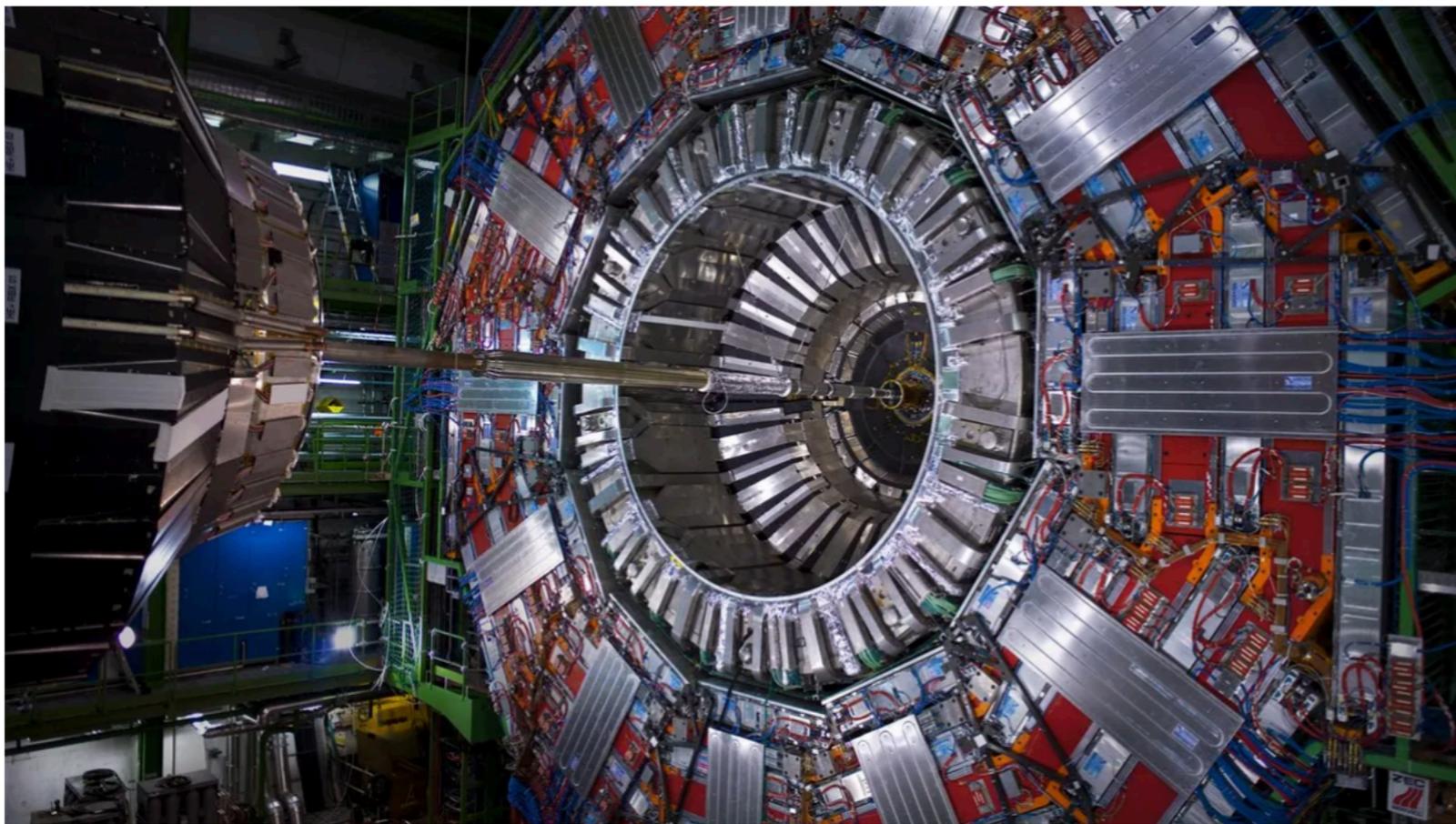
The CDF m_w result stands in tension with the Standard Model ... Latest ATLAS, CMS results restore agreement with the SM



The W boson caused a particle mystery — but scientists have cracked the case

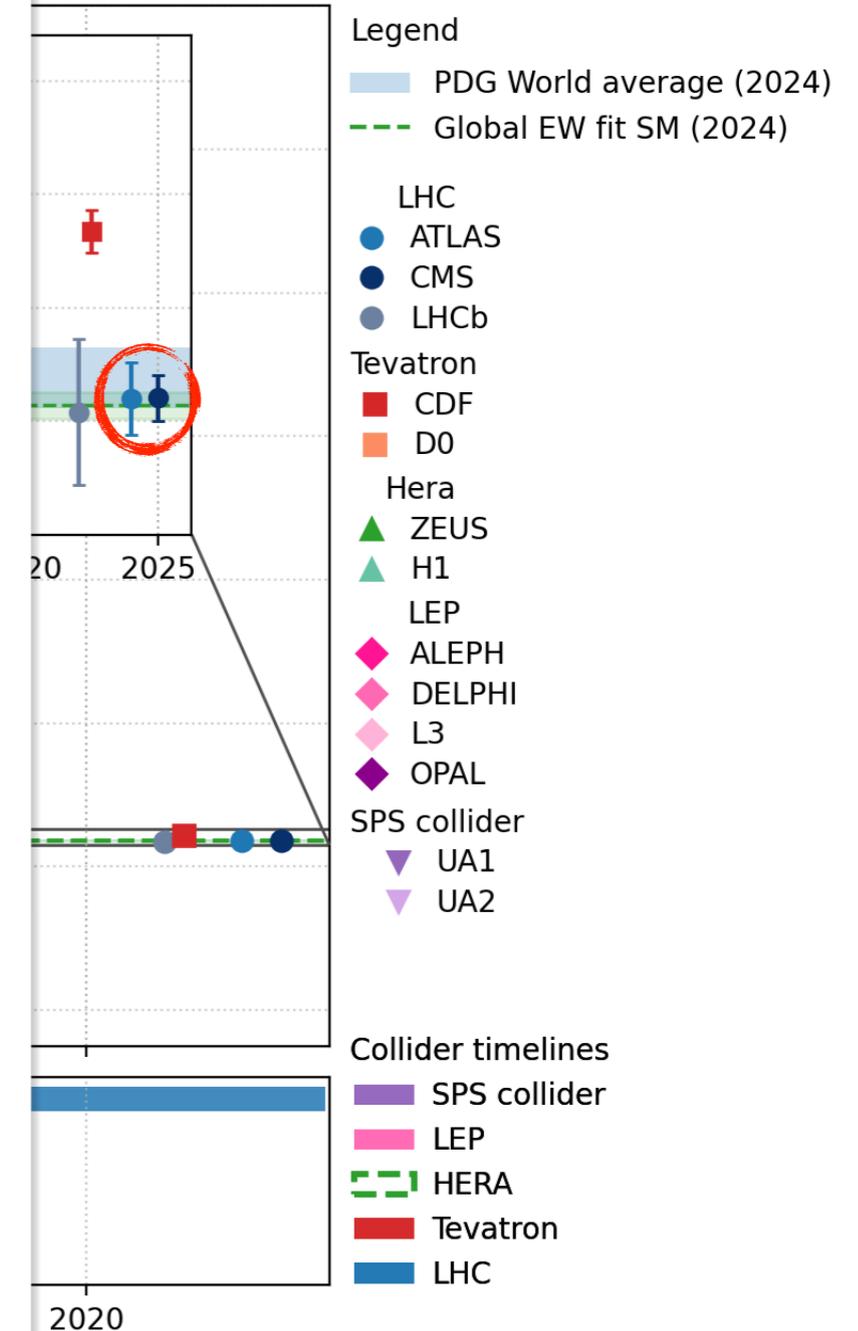
News By Keith Cooper published September 26, 2024

Large Hadron Collider has ended W boson fever. "We have to search for new physics elsewhere," one researcher says.



The giant Compact Muon Solenoid experiment at the LHC. The different rings of detectors, arranged a bit like an onion, measure different particles. (Image credit: CERN/Maximilien Brice)

W boson mass measured



year

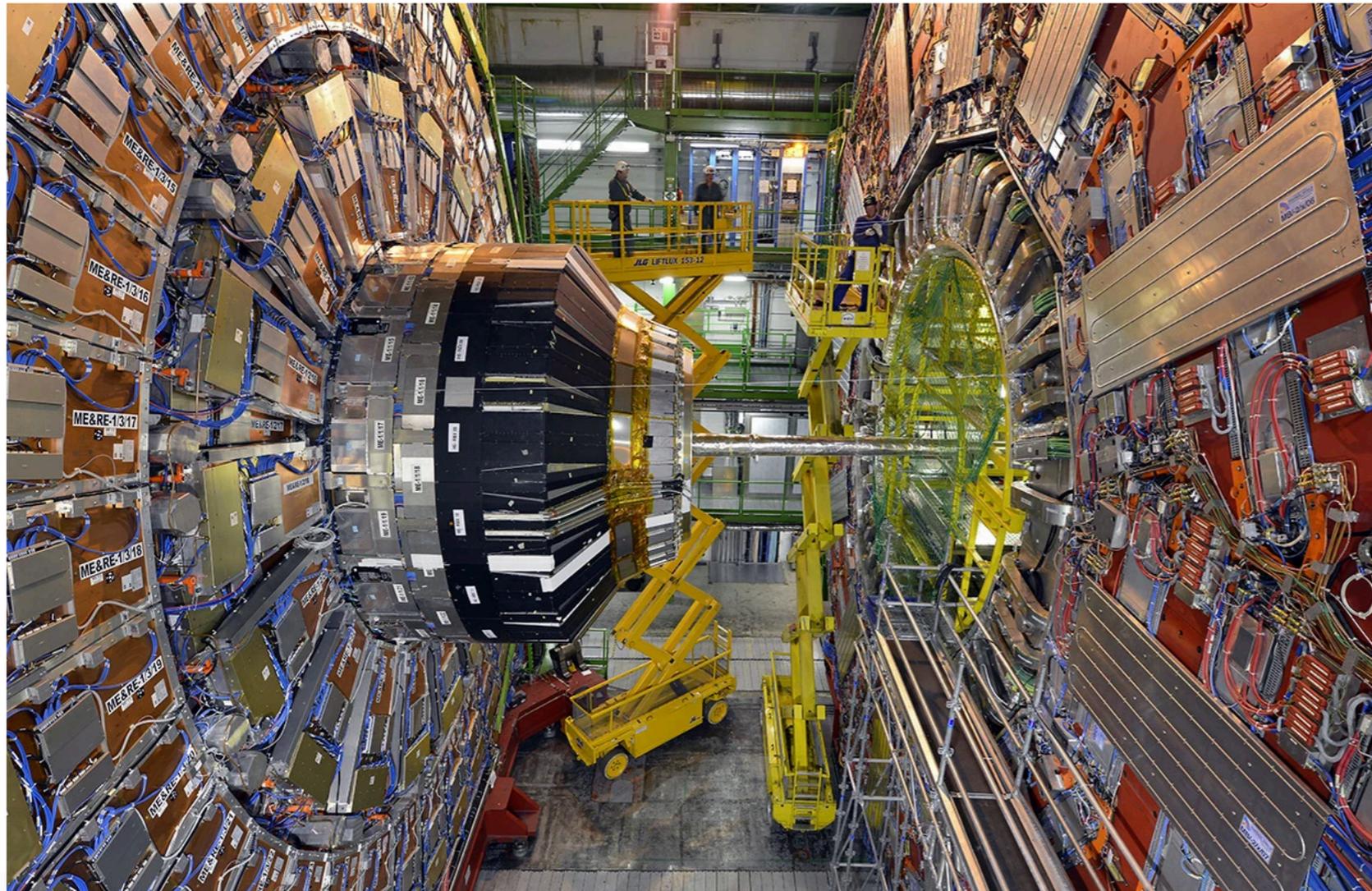
nature > news > article

NEWS | 17 September 2024

'The standard model is not dead': ultra-precise particle measurement thrills physicists

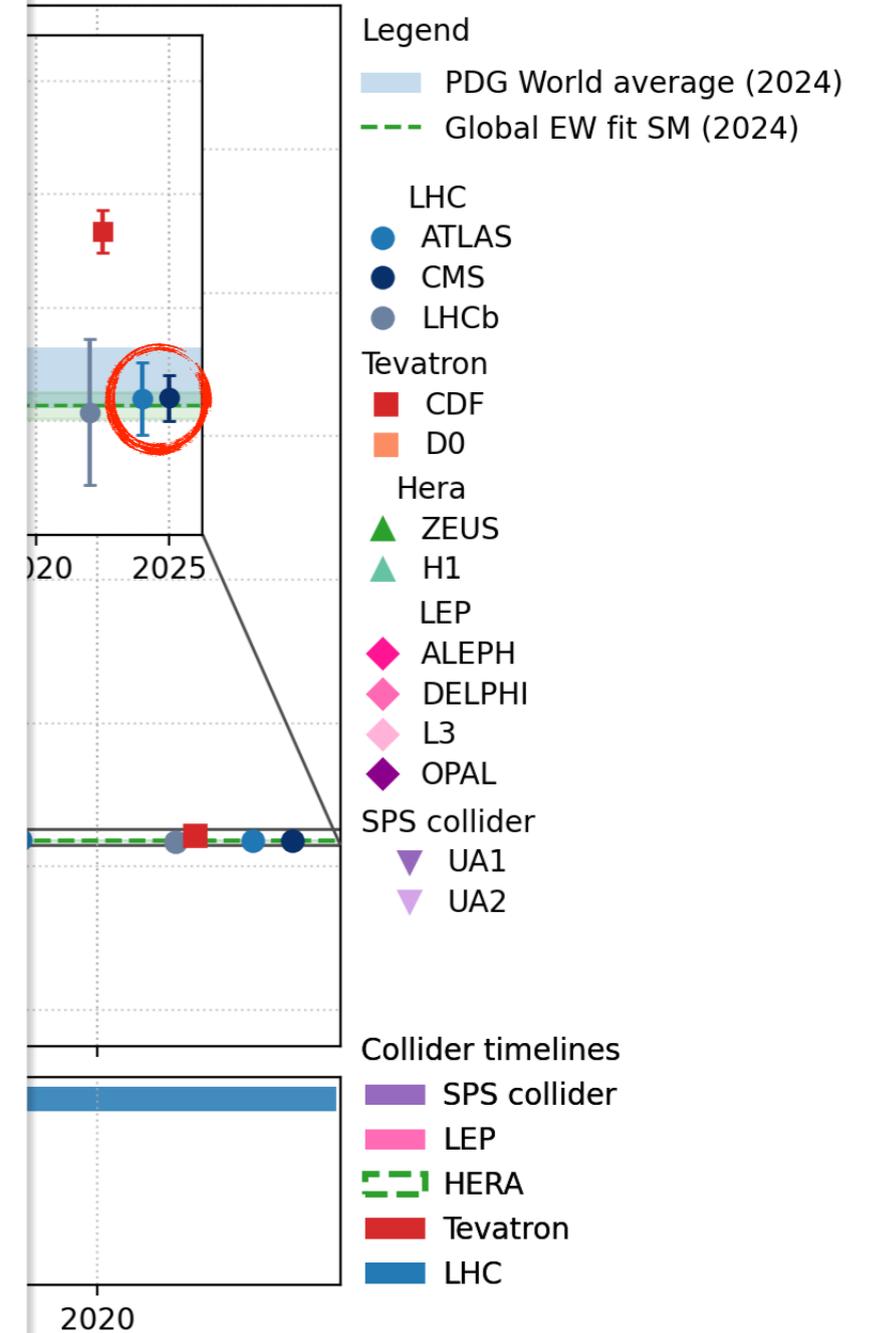
CERN's calculation of the *W* boson's mass agrees with theory, contradicting a previous anomaly that had raised the possibility of new physics.

By Elizabeth Gibney

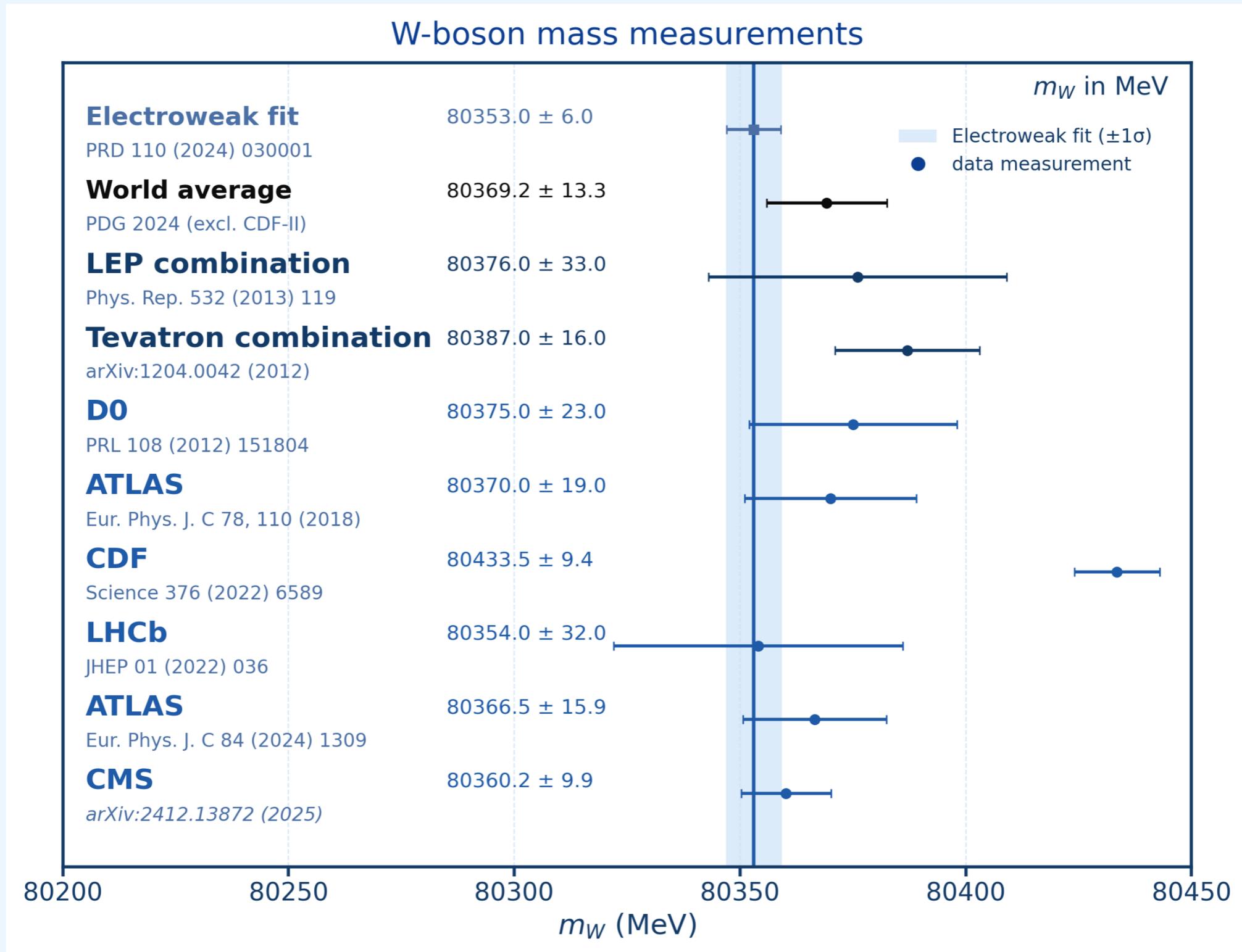


relement

icted then measured

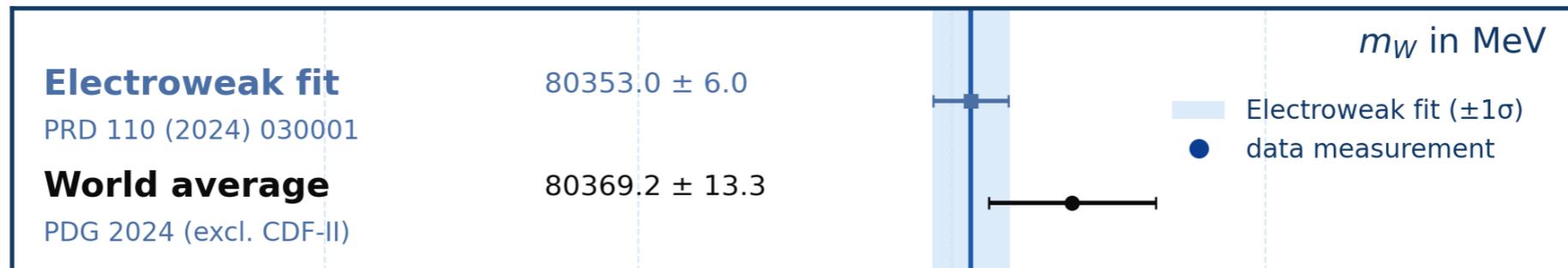


The W mass measurement at LHC



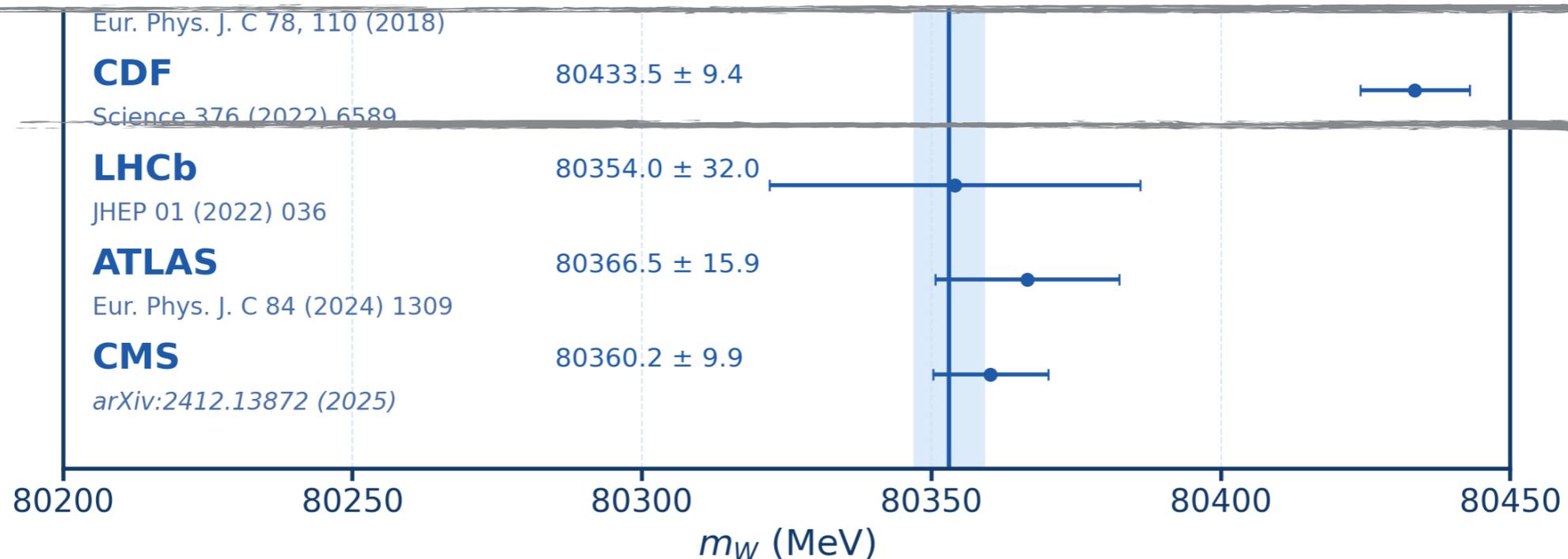
The W mass measurement at LHC

W-boson mass measurements



Spectacular !

Excluding recent CDF measurement all the LHC measurements are very consistent with each other and on-spot with the SM expectations with precision $\sim 0(10\text{MeV})$



The W Boson mass at LHC

The W-boson mass is one of the most challenging measurements in high-energy physics.

- *At the start of the LHC era, today's precision seemed unattainable.*
 - ATLAS, CMS, and LHCb aim for $\delta m_W(10 \text{ MeV})$ → **demanding extreme mastery of detector performance and systematics**
 - Its ultimate precision was limited by our **understanding of QCD.**

Ten years of LHC data have transformed the field:

- ✓ From discovery to precision → Detector control at the sub-‰ level using complementary methods and conditions
- ✓ Huge progress on theory methodologies in the past few years

THE W BOSON PUZZLE

CERN's CMS experiment has made a highly precise measurement of the W boson's mass. The result is in line with the prediction made in the standard model of particle physics.

Experiments

Tevatron I (DO and CDF, 2004)

DO II (2012)

LEP (ALEPH, DELPHI, L3, OPAL, 2013)

ATLAS (2018)

LHCb (2022)

CDF II (2022)

CMS (2024)

Standard-model prediction (2018)

80,200 80,300 80,400 80,500
Mass (MeV) ©nature

What are the challenges of the current W boson mass analyses @LHC ?

W mass analysis check-list

How to measure the mass of the **W**

Produce W-boson candidate

Select W-boson candidate

Observable sensitive to m_W

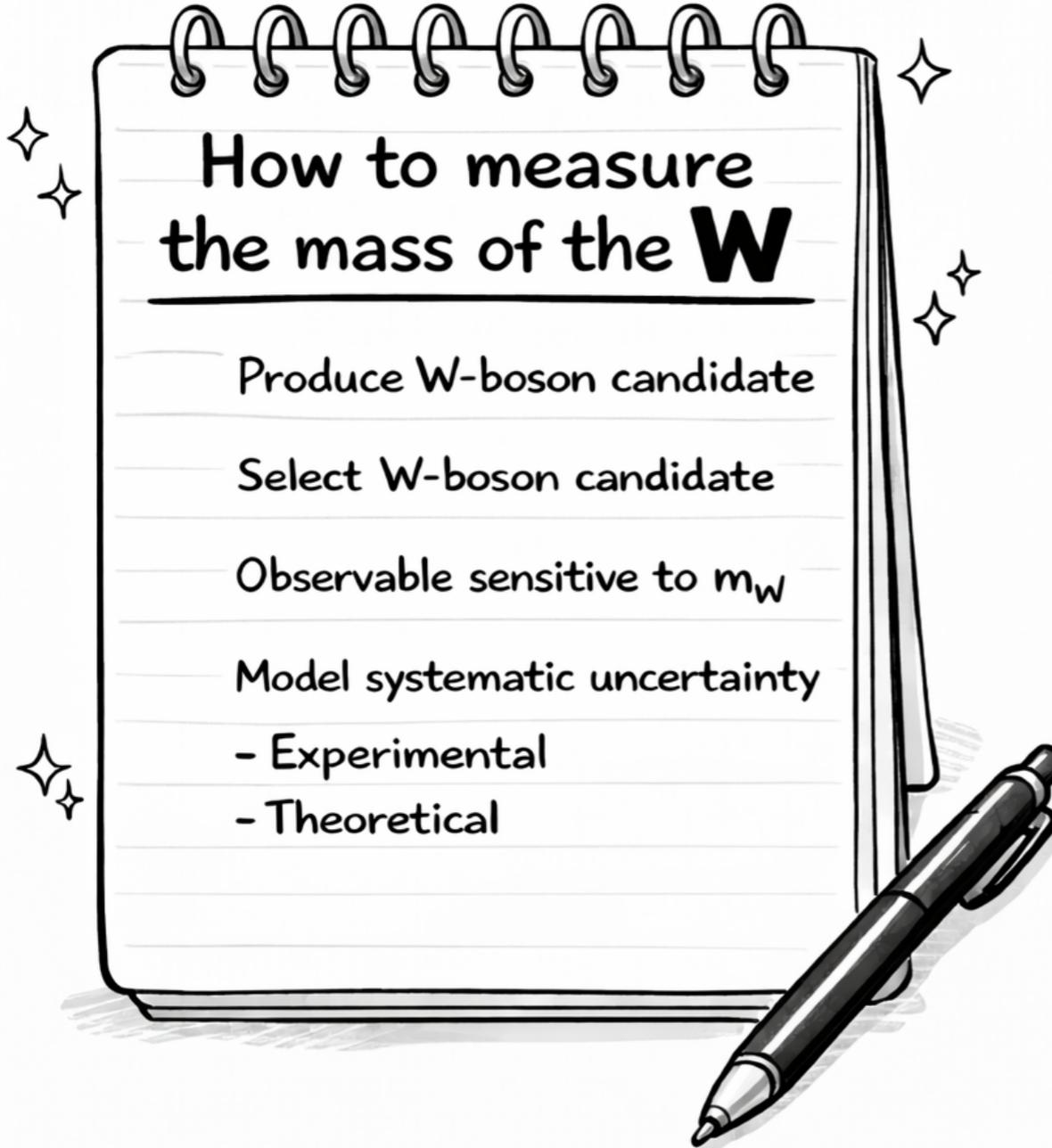
Model systematic uncertainty

- Experimental

- Theoretical

- ▶ High-performance [software & computing](#): huge data-flow and complexity of the fit ($> 10^3$ bins + 10^4 NP)
- ▶ Super-precise [detector calibration](#) and response control
- ▶ Robust [physics modelling](#): Percent-level theoretical precision \rightarrow Careful treatment of many uncertainty sources
- ▶ Extensive program of [ancillary measurements](#)

W mass analysis check-list



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Produce W-boson candidate

Select W-boson candidate

Observable sensitive to m_W

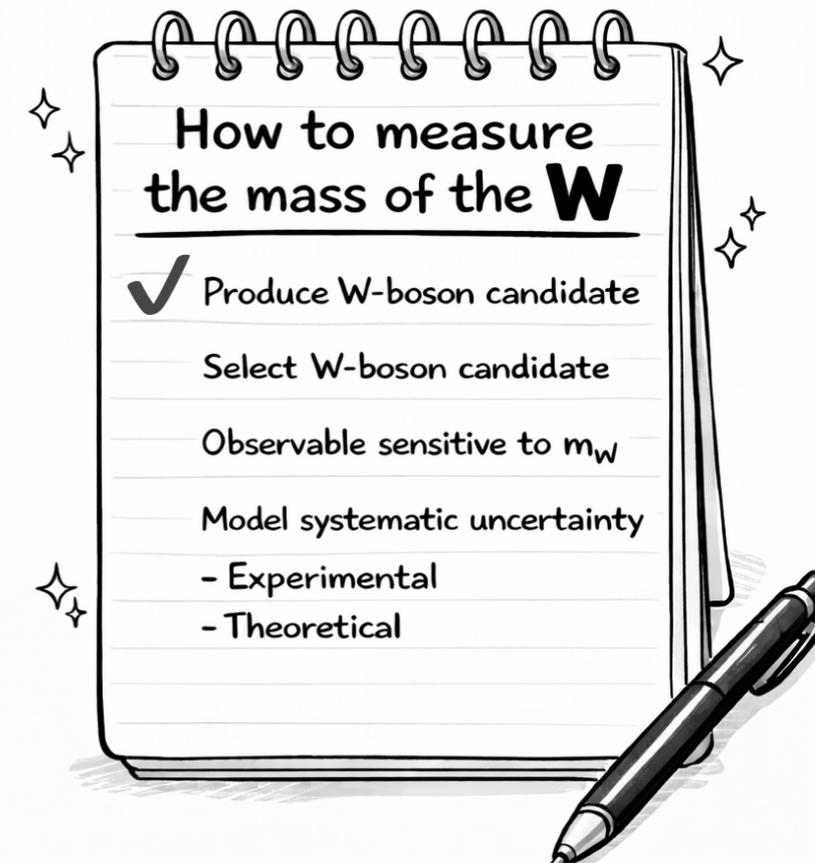
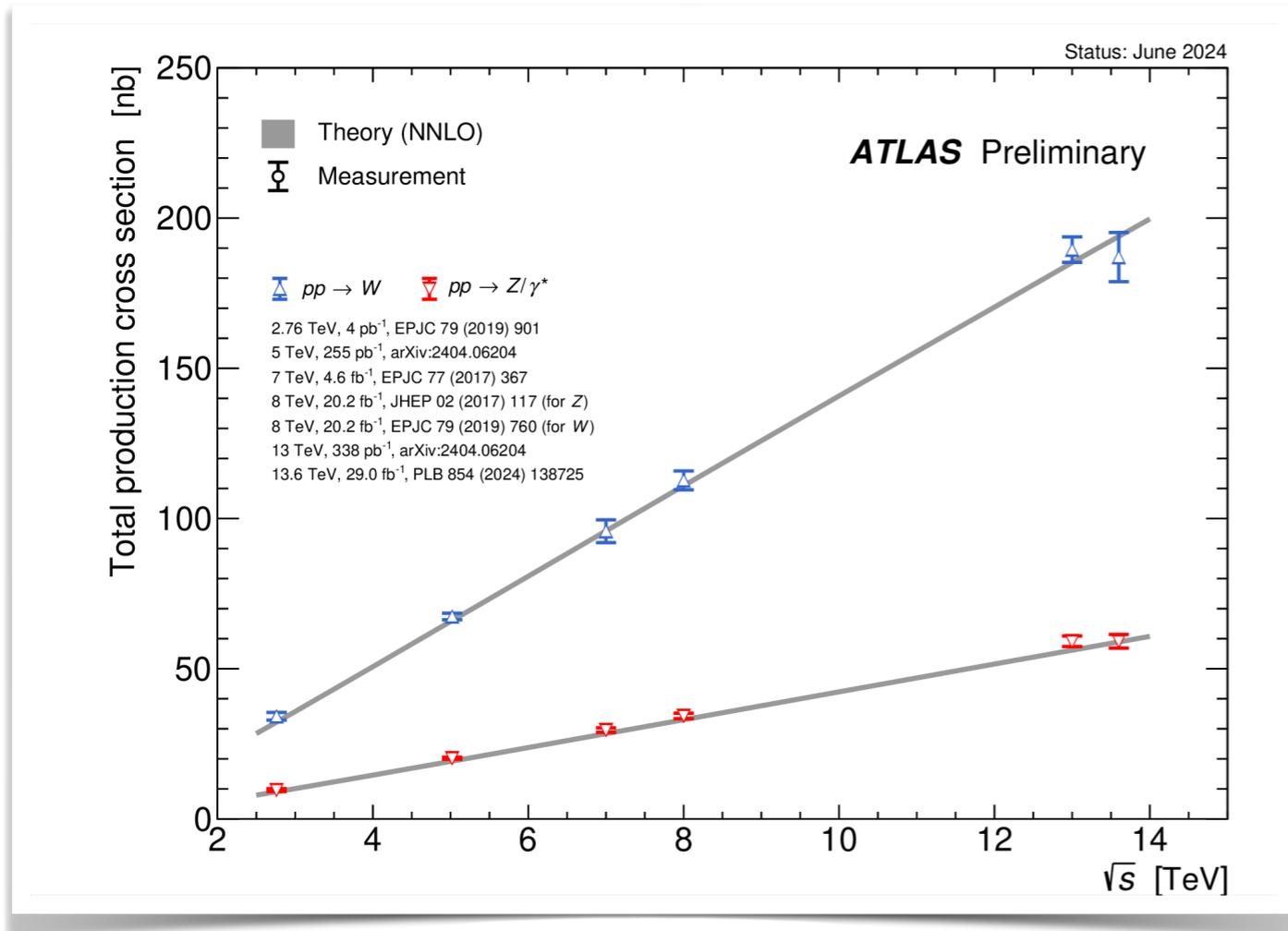
Model systematic uncertainty

- Experimental

- Theoretical

- ▶ High-performance software & computing: huge data-flow and complexity of the fit ($> 10^3$ bins + 10^4 NP) → **W boson prod. is $\approx O(1000)$ x greater than Higgs production @LHC**
- ▶ Super-precise detector calibration and response control → **Often 1 order of magnitude better precision than std. analysis**
- ▶ Robust physics modelling: Percent-level theoretical precision → **Data precision challenge the progress of the theory community**
- ▶ Extensive program of ancillary measurements → **Do you believe on what they predict ? 10-20 year in the past nobody would never believe it.**

Produce W candidate



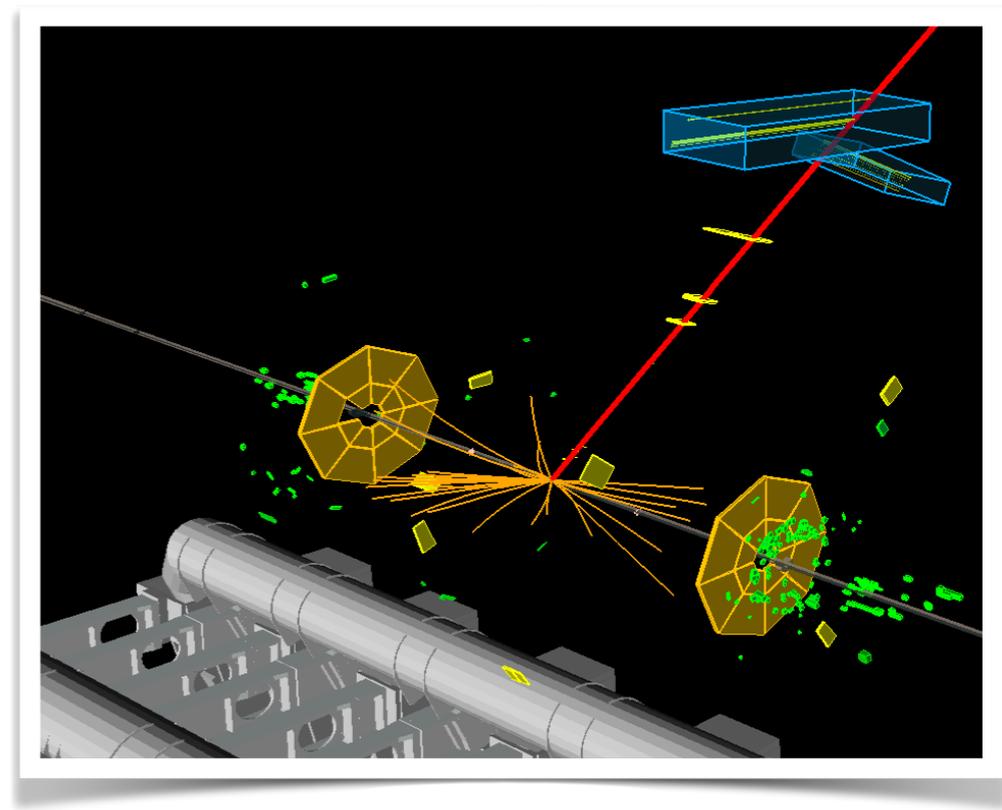
$$\text{BR}(Z \rightarrow e^+e^-) \simeq \text{BR}(Z \rightarrow \mu^+\mu^-) \simeq 3.37\%$$

$$\text{BR}(W \rightarrow e\nu) \simeq \text{BR}(W \rightarrow \mu\nu) \simeq 10.8\%$$

$$\frac{dN}{dt} = \mathcal{L}_{\text{inst}} \times \sigma$$

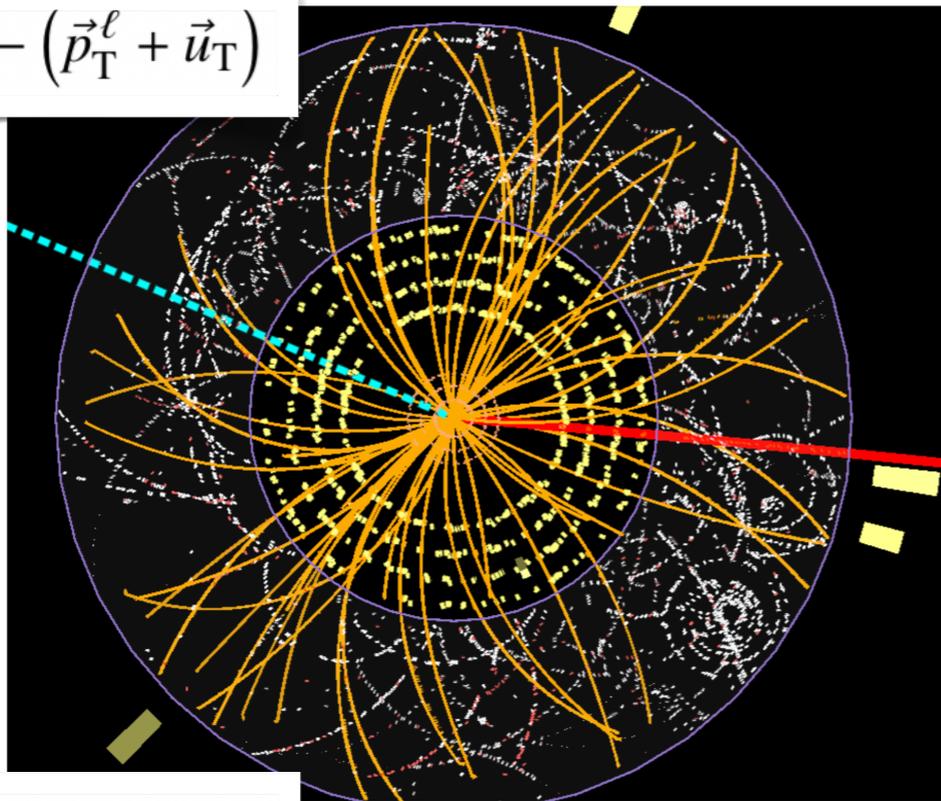
Event produced per fb⁻¹ (total, $\sigma \times \text{BR}$)

| \sqrt{s} | $W \rightarrow \ell\nu$ ($\ell = e/\mu$) events/fb ⁻¹ | $Z \rightarrow \ell\ell$ ($\ell = e/\mu$) events/fb ⁻¹ |
|------------|--------------------------------------------------------------------|---------------------------------------------------------------------|
| 5 TeV | 7.3×10^6 | 0.68×10^6 |
| 7 TeV | 10.7×10^6 | 1.0×10^6 |
| 13 TeV | 20.5×10^6 | 2.03×10^6 |
| | ≈ 115 events/second | ≈ 11 events/second |



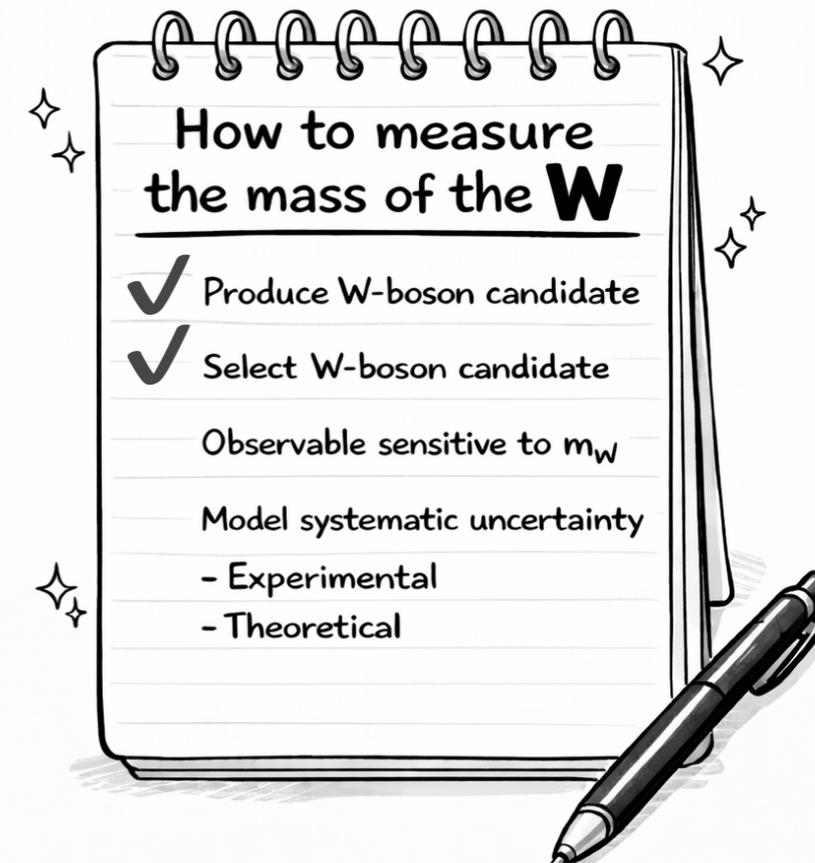
Select W candidate

$$\vec{p}_T^{\text{miss}} = -(\vec{p}_T^\ell + \vec{u}_T)$$



$$\vec{p}_T^\ell$$

$$\vec{u}_T = \sum_i \vec{E}_{T,i}$$



| selected events | CMS | ATLAS | LHCb |
|------------------------|-------------------------------------|----------------------------------|-----------------------------|
| Dataset | 17 fb ⁻¹ @13TeV $\mu=30$ | 5 fb ⁻¹ @7TeV $\mu=9$ | 1.7 fb ⁻¹ @13TeV |
| $W \rightarrow \mu\nu$ | 117 M | 7.8 M | 2.4 M |
| $W \rightarrow e\nu$ | X | 5.9 M | X |
| $Z \rightarrow \mu\mu$ | 7.5 M | 1.2 M | 0.2 M |
| $Z \rightarrow ee$ | X | 0.6 M | X |

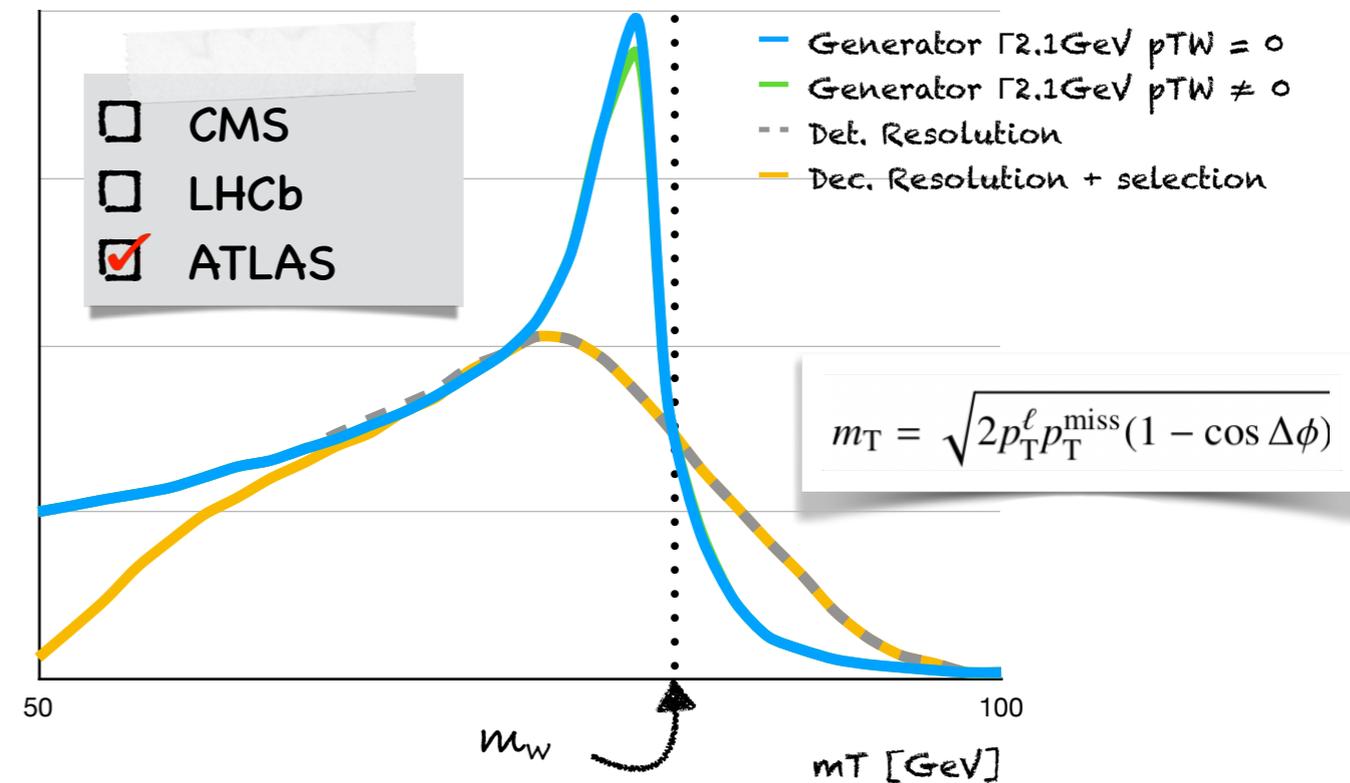
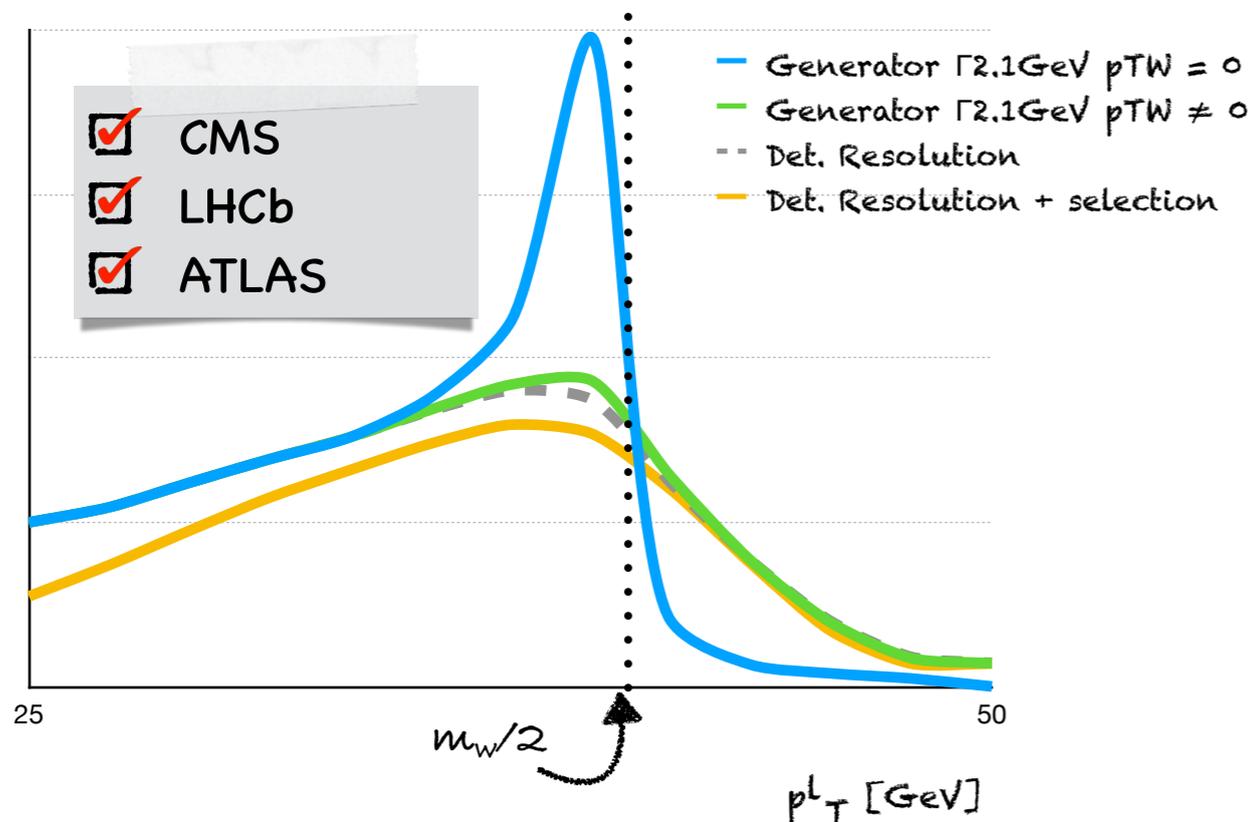
Observables sensitive to m_W

p_T^ℓ and m_T observable are *complementarity* against:

- Pile-up dependence,
- experimental systematic,
- Modelling effects

How to measure the mass of the **W**

- ✓ Produce W-boson candidate
- ✓ Select W-boson candidate
- ✓ Observable sensitive to m_W
- Model systematic uncertainty
 - Experimental
 - Theoretical



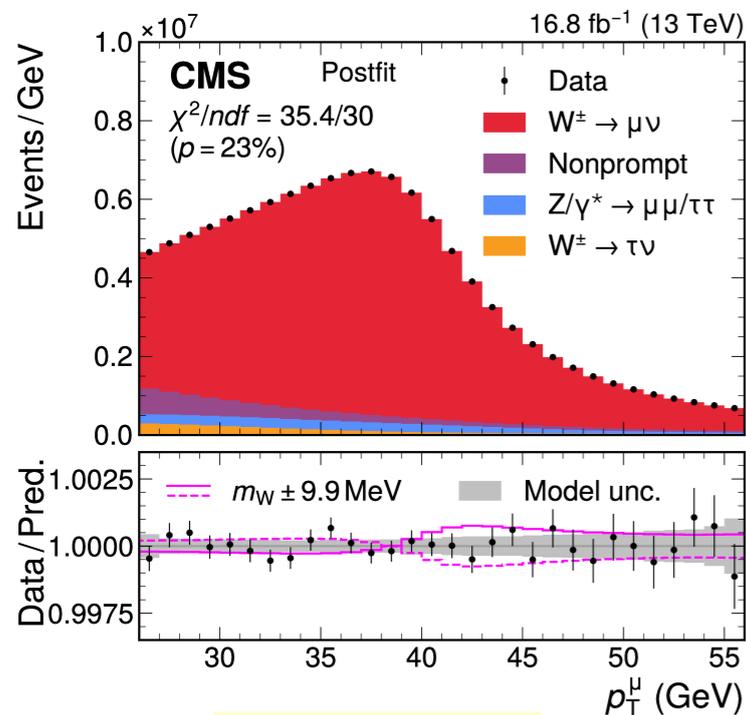
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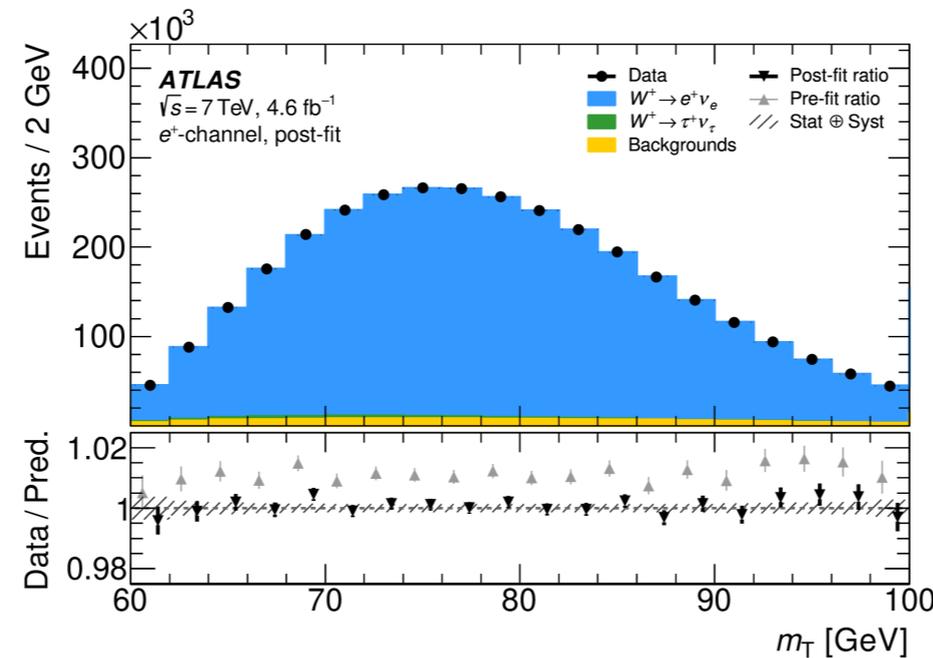
- Pile-up dependence,
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How to measure the mass of the **W**

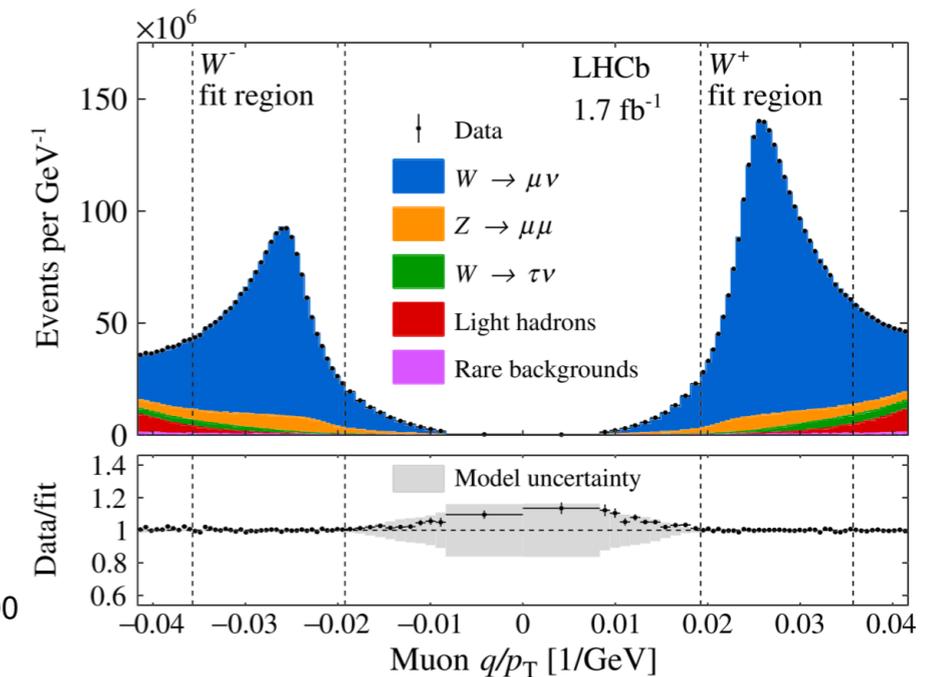
- ✓ Produce W-boson candidate
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- Model systematic uncertainty
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 - Theoretical



arXiv:2412.13872



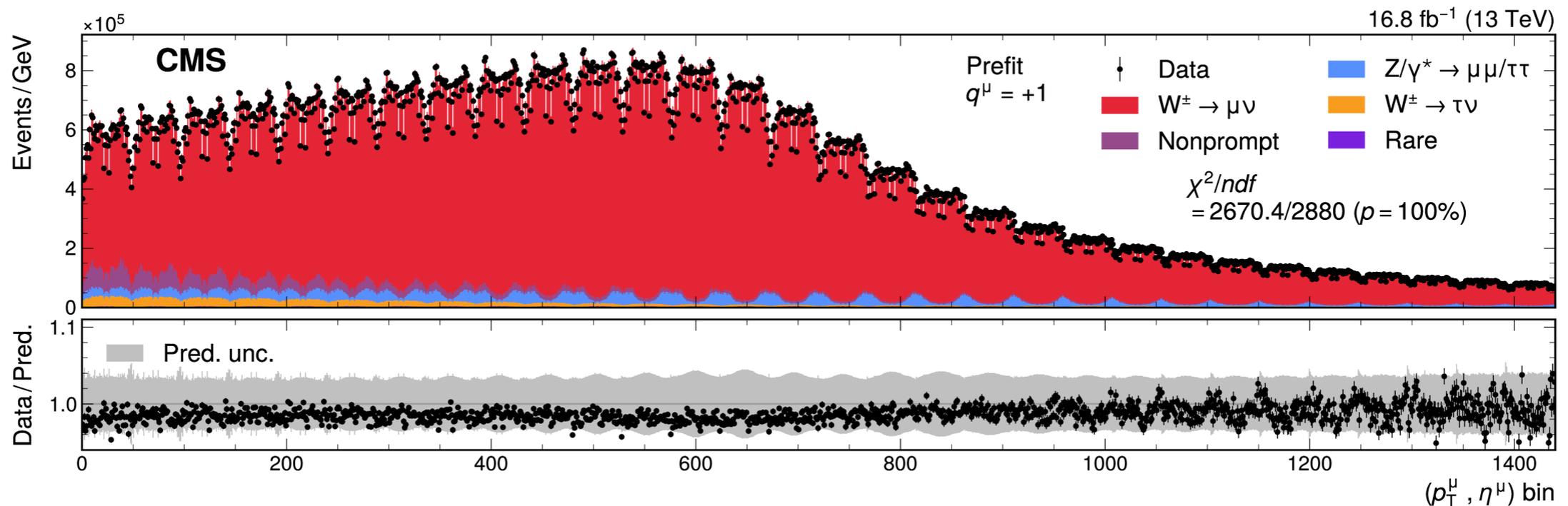
Eur. Phys. J. C 84 (2024) 1309



JHEP 01 (2022) 036

Event category

→ Events are split in several categories to maximise the sensitivity to the m_W and to Model and Experimental sys ($q_{\mu,e}, \eta_{\mu,e}, p_{T\mu,e}, m_{T\mu,e}$)



| Decay channel | $W \rightarrow e\nu$ | $W \rightarrow \mu\nu$ |
|-------------------------|----------------------------------|----------------------------------------------|
| Kinematic distributions | p_T^ℓ, m_T | p_T^ℓ, m_T |
| Charge categories | W^+, W^- | W^+, W^- |
| $ \eta_e $ categories | [0, 0.6], [0.6, 1.2], [1.8, 2.4] | [0, 0.8], [0.8, 1.4], [1.4, 2.0], [2.0, 2.4] |

Software challenges



in CMS 13TeV data ~120M of W-events

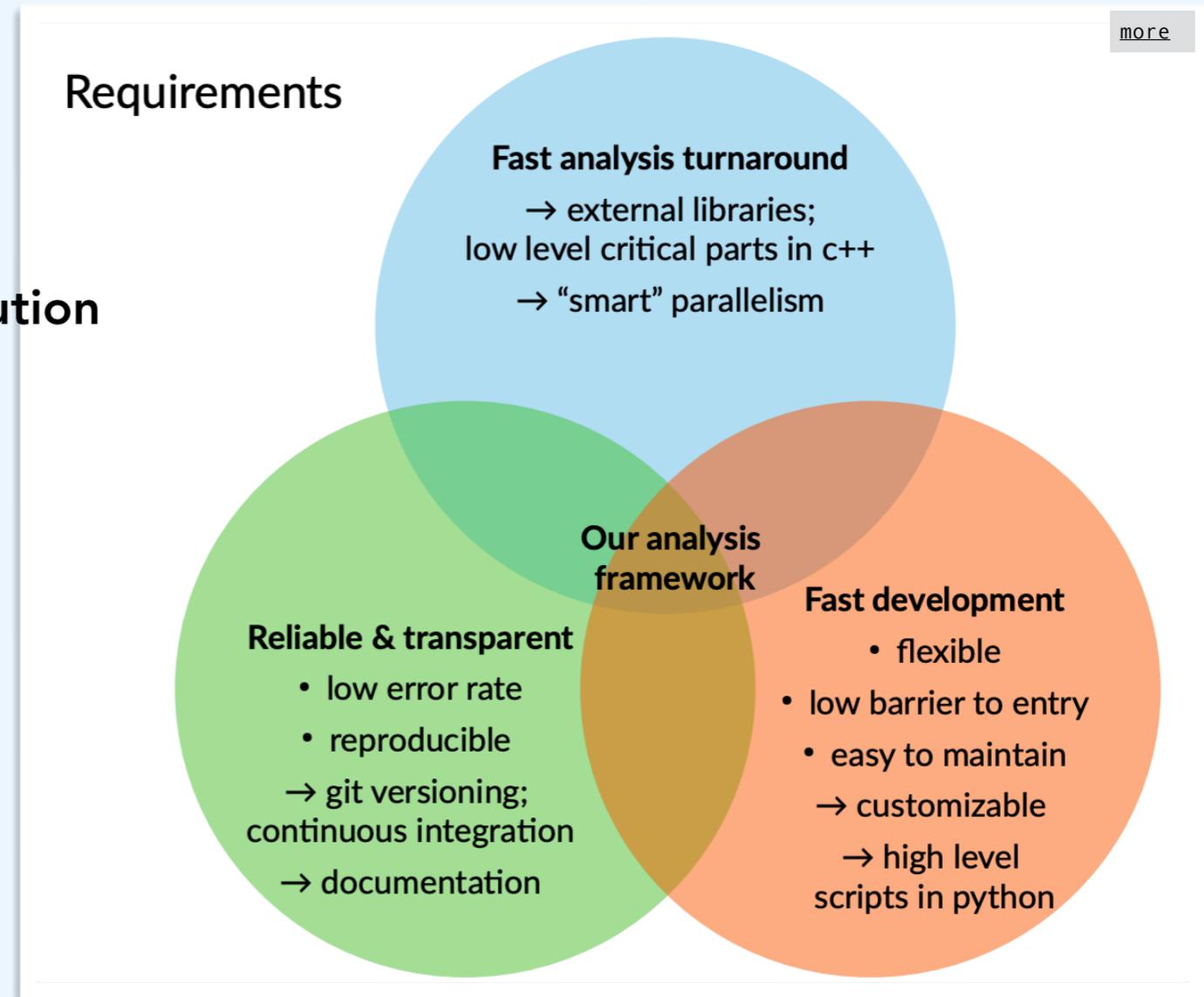
- ➔ Extract mass from fit to $(q\mu, \eta\mu, pT\mu)$ distribution
~2000 bins and 4000 nuisance parameters
- ➔ Major computational challenge

Increasing amount of data opens new opportunities

- Software must stay ahead to exploit data potential
- RDataFrame as efficient and flexible framework
- Optimisation of low-level critical parts [histogram implementation]
- Single high-performance node with fast SSDs and 100 Gbit/s networking for efficient I/O. [Future multi-core CPUs (e.g. EPYC Turin) will further improve scalability.]

Collaboration & Reliability

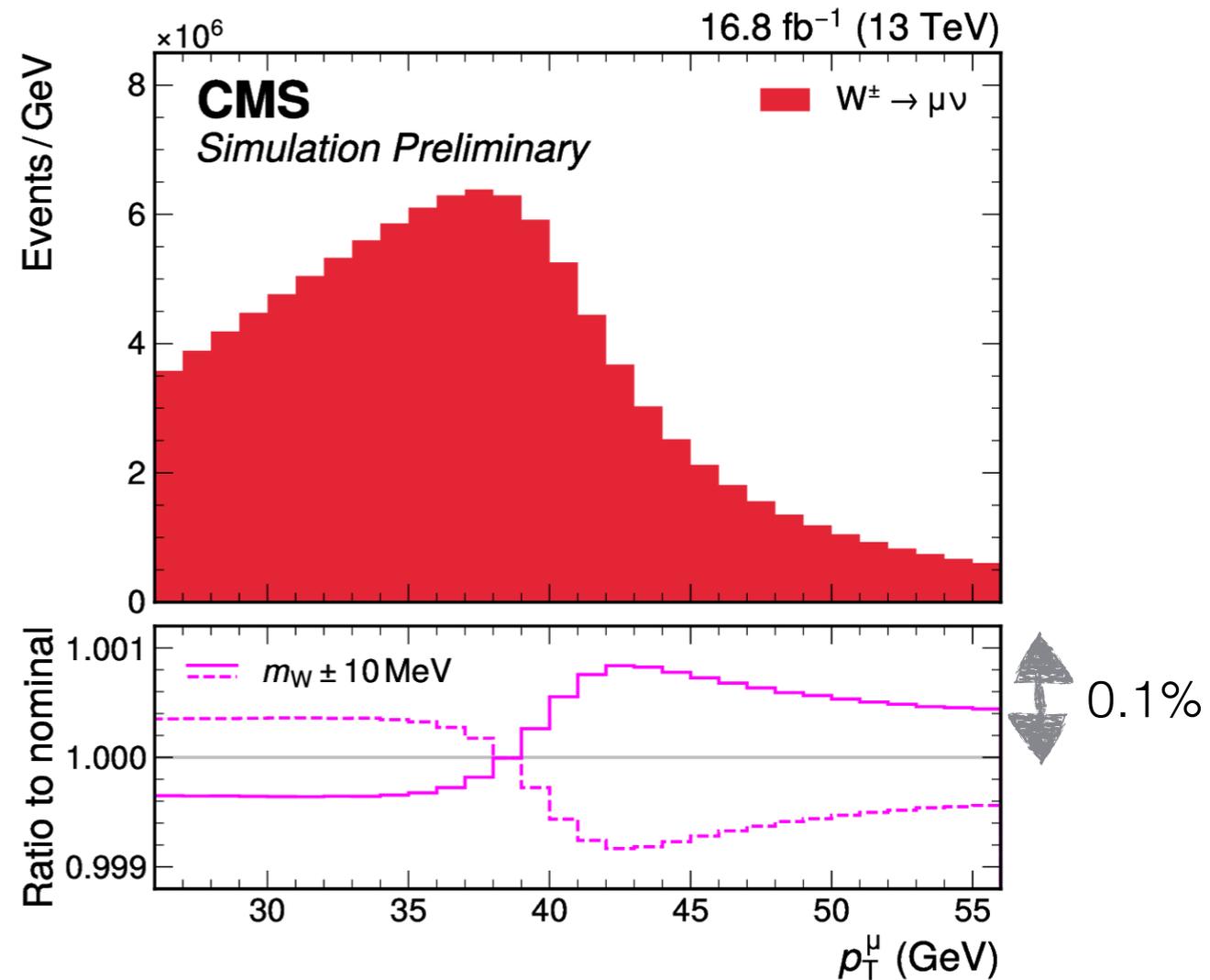
- GitHub CI/CD pipeline extremely useful
 - Early bug detection
 - Easy rollback of changes
 - Stable implementation across configurations



The precision we need

General measurement strategy: produce models ("templates") of the final state distributions for different W -mass hypotheses to compare to **data**

10 MeV precision in m_W need *per mille* precision!

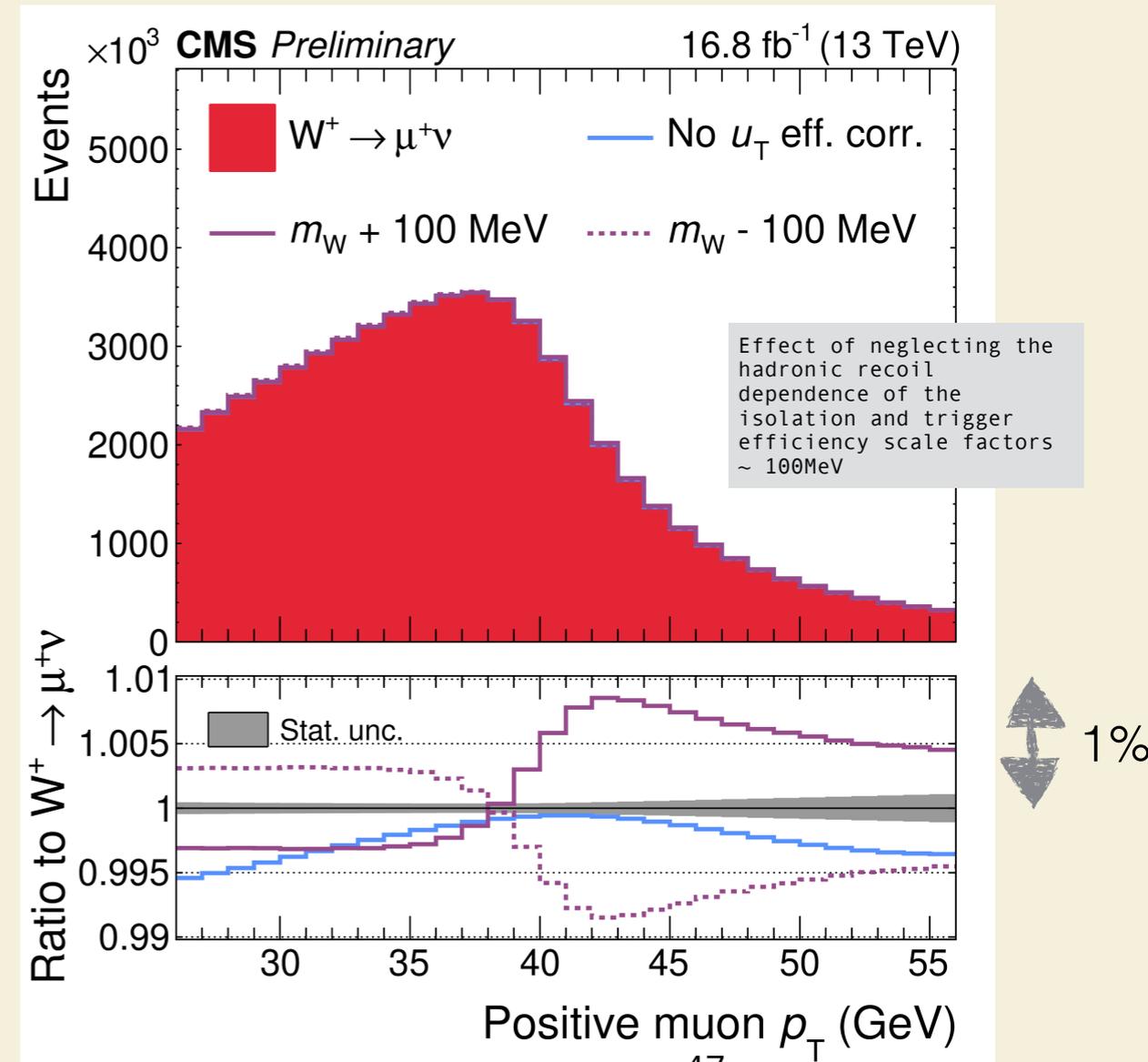
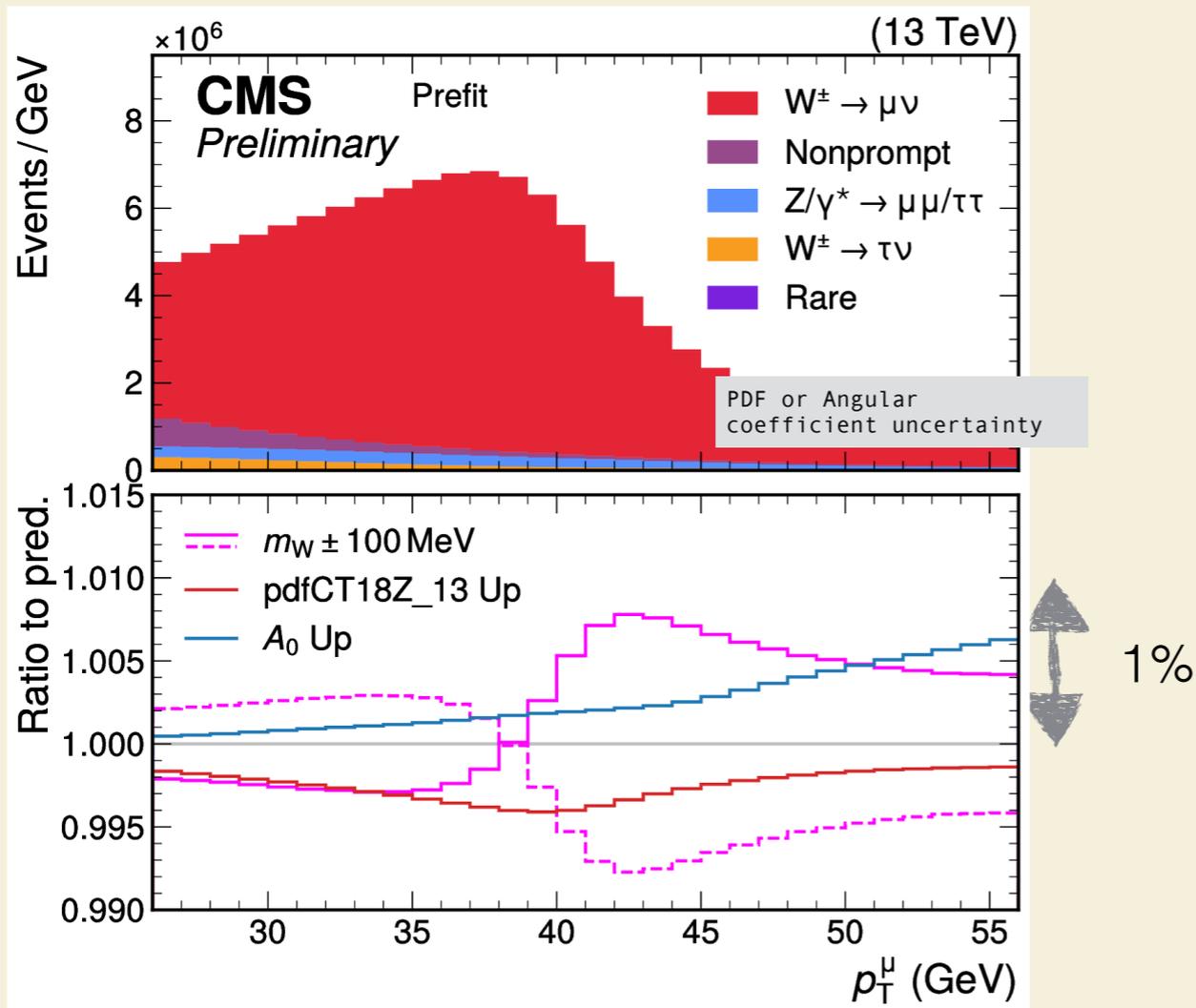
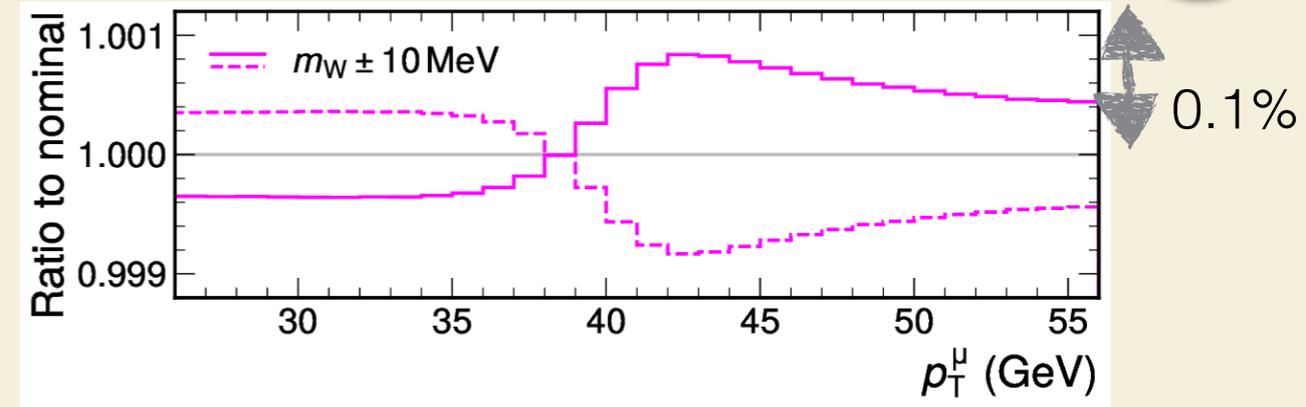


| | CMS | ATLAS | LHCb |
|------------|------------------------------------------------|--------------------------------------------------|---------------------------------------------------------------------------------------|
| Dataset | 17 fb ⁻¹ @13TeV $\mu=30$ (10% 2016) | 5 fb ⁻¹ @7TeV $\mu=9$ | 1.7 fb ⁻¹ @13TeV (no pileup) 2016 only |
| Channels | only muons | electron & muons | only muons $2.2 < \eta^\mu < 4.4$ |
| Observable | only p_T lepton | p_T, m_T | q/p_T |
| Modelling | TNP (theoretical nuisance parameters) | $Z \leftrightarrow W$ extrapolation of the model | simultaneous fit to $Z \rightarrow \mu\mu$ events binned in $\phi^* \approx p_T/M$ |

The precision we need

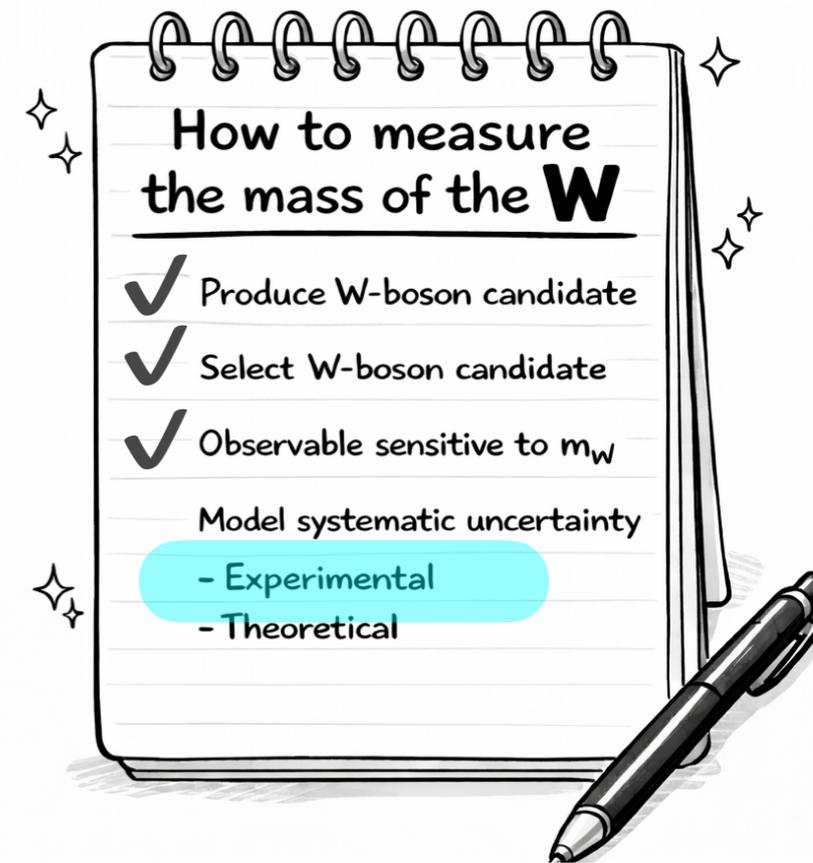


10 MeV precision in m_W need per mille precision in the observable



Experimental precision

- ▶ The m_W measurement is the culmination of an extensive program of **performance measurements** :
- ▶ **Lepton**:
 - ▶ Highly granular and precise estimation of lepton reconstruction/ID/Trigger **efficiency**
 - ▶ Calibration of **absolute p_T scale** (electron $\delta E_T \sim 10^{-4} \Rightarrow \delta m_W \sim 8$ MeV)
 - ▶ **> x10 better than typical ATLAS/CMS/LHcb analysis**
- ▶ **Calibration of the hadronic-Recoil - p_T^{miss}**
 - ▶ challenge of the pile-up \rightarrow % precision required
- ▶ Accurate estimation of **backgrounds**
 - ▶ primarily heavy flavour decays and jets mis-ID'd leptons

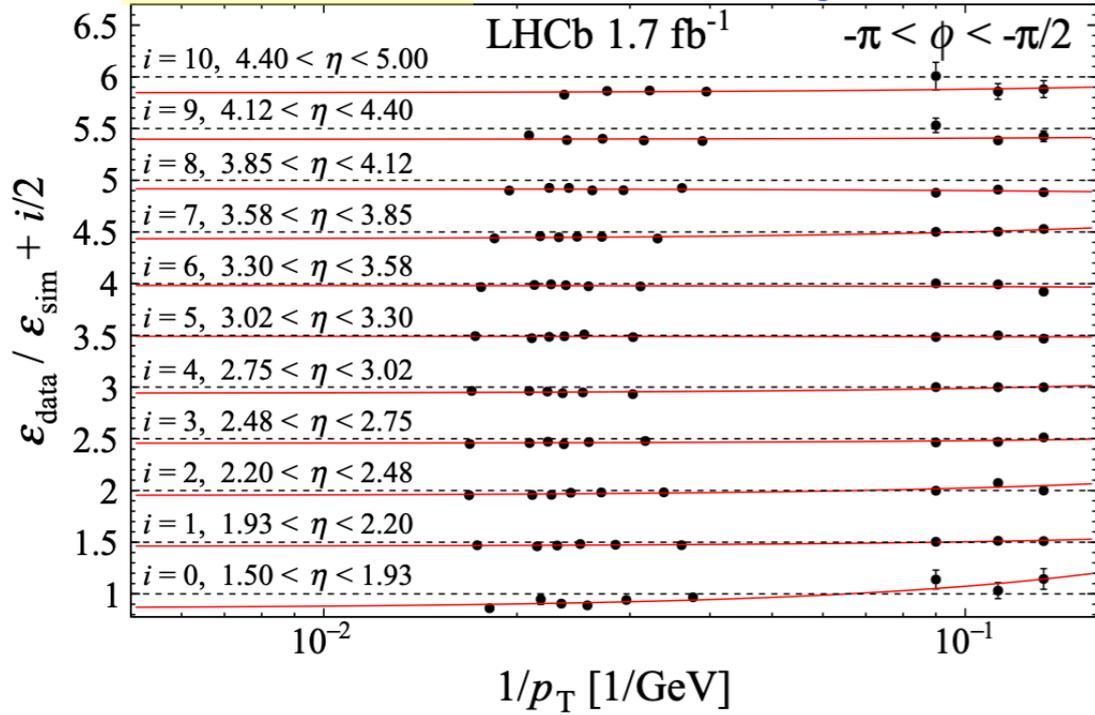


| | CMS | ATLAS | LHCb |
|----------------------|----------------------------------------|----------------------------------|----------------------------------------|
| Dataset | 17 fb ⁻¹ @13TeV $\mu=30$ | 5 fb ⁻¹ @7TeV $\mu=9$ | 1.7 fb ⁻¹ @13TeV |
| muon performance | Z to validate calibration (J/ψ, Y(1S)) | Z samples for calibration | Z to validate calibration (J/ψ, Y(1S)) |
| electron performance | X | Z samples for calibration | X |
| hadronic recoil | X | Z samples for calibration | X |

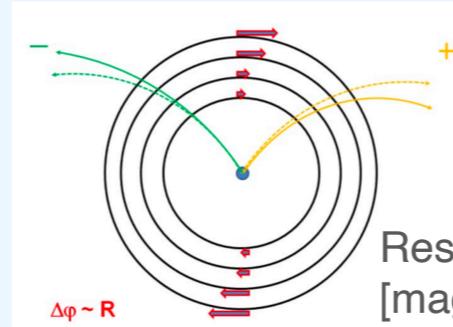
Lepton performances



JHEP 01 (2022) 036 → Uncertainty in m_W 6 MeV

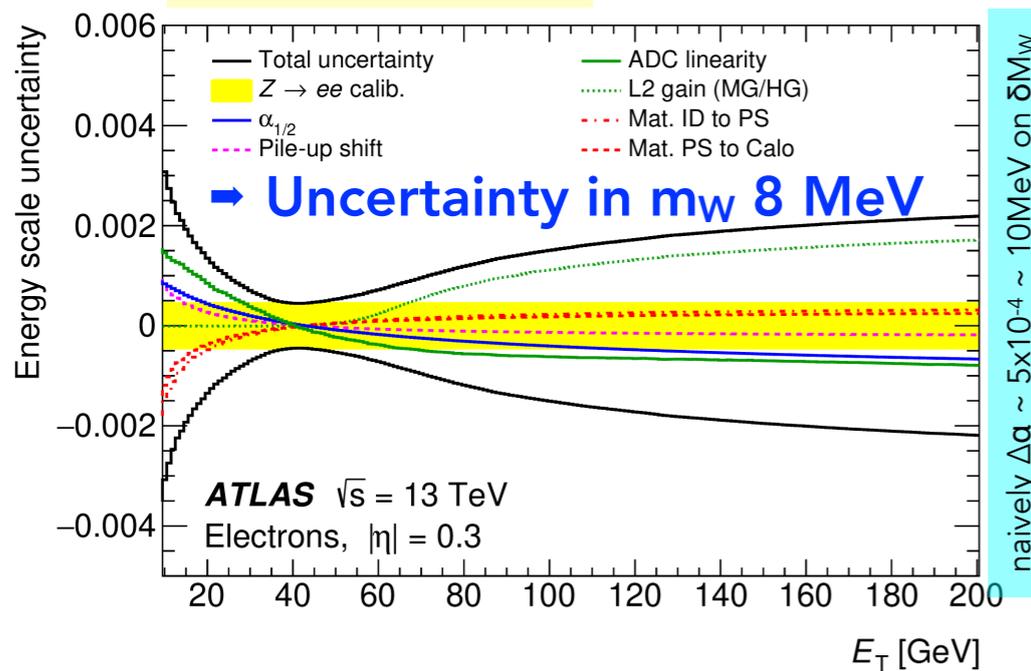


Outstanding experimental precision reached

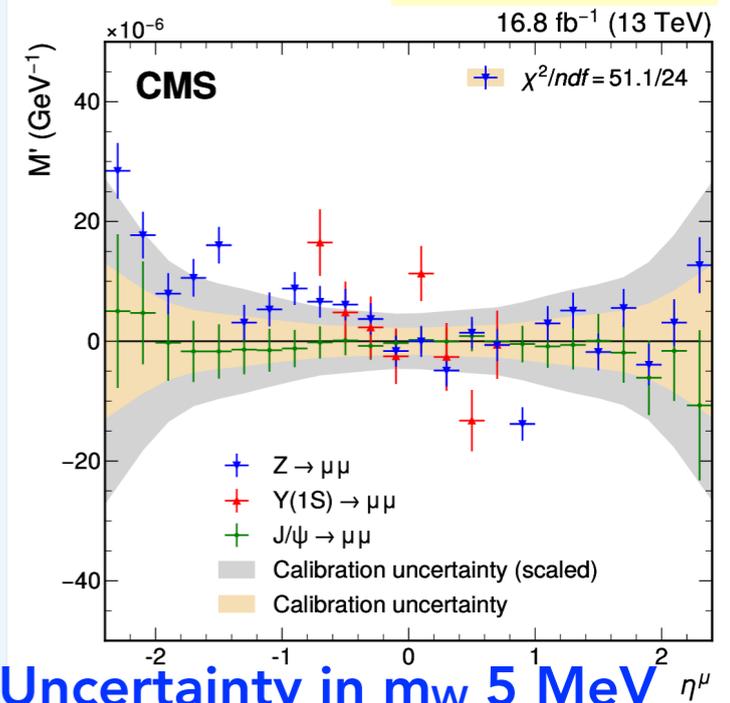
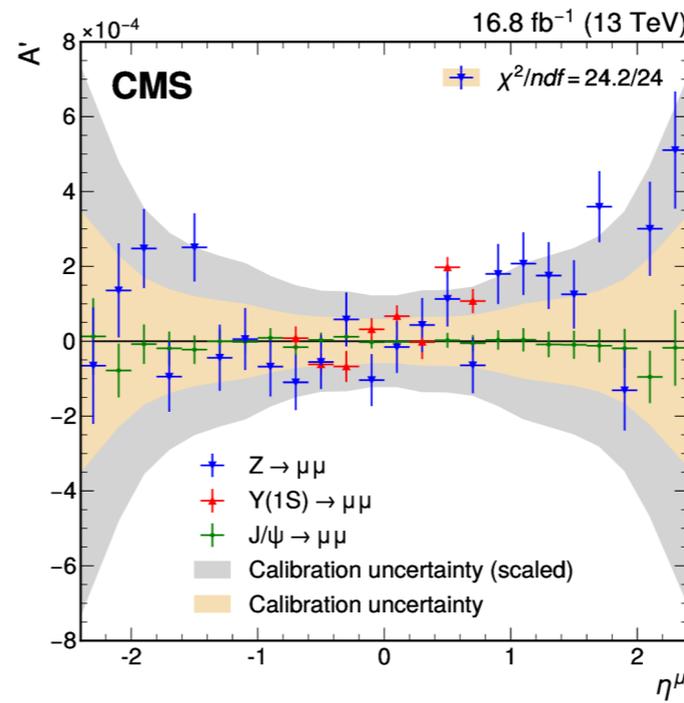


Residual scale differences for charge-independent A' [magnetic-field-like difference], and charge-dependent M' comparison [misalignment-like term]

JINST 19 (2024) P02009



arXiv:2412.13872



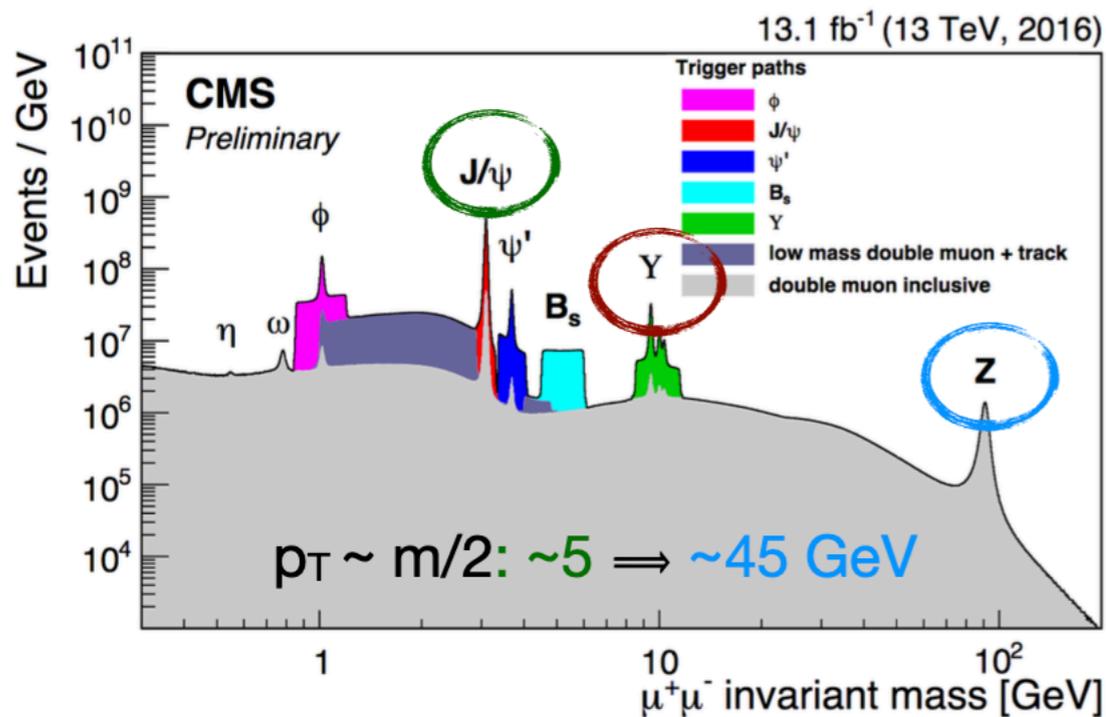
→ Uncertainty in m_W 5 MeV

calibration challenges - muon scale



$$k_{corr} = Ak + qM + \frac{k}{1 + ek}$$

$$\delta k/k \approx \underline{A} + \underline{qM/k} - \underline{ek}$$



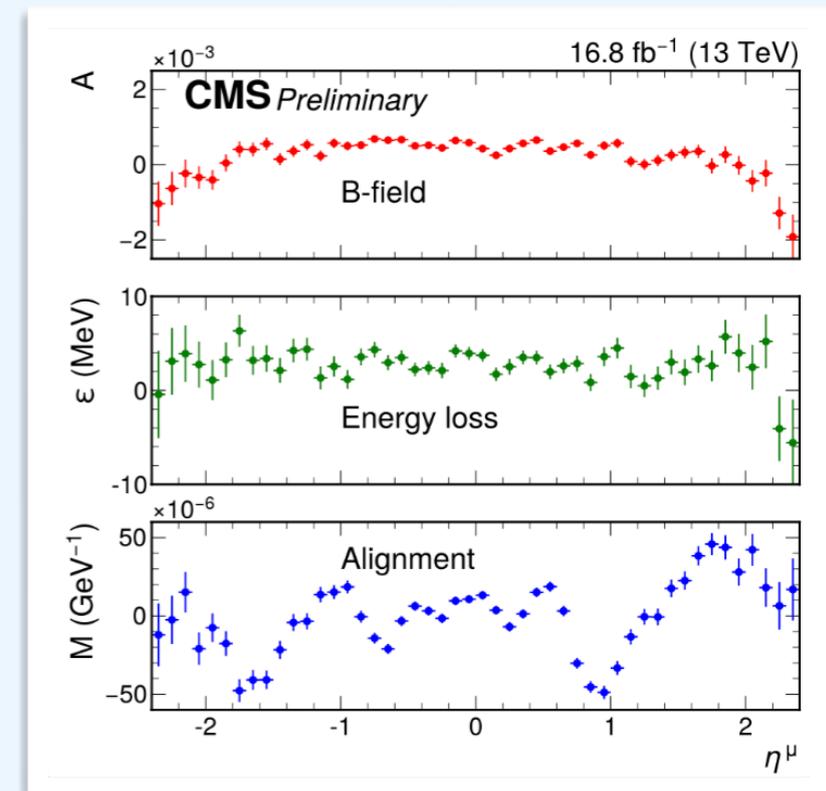
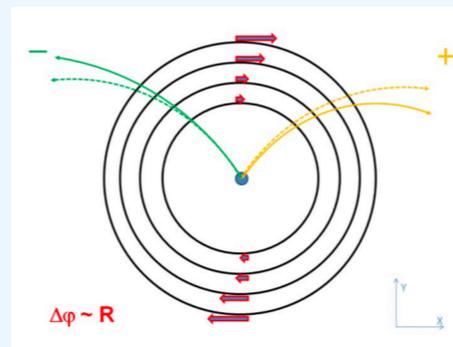
Calibration from quarkonia and extrapolation to W/Z momentum range requires precise control over momentum dependence of the calibration.

Canonical expression for curvature bias $\delta k/k$
Parameterize by small differences in

B-field

Alignment

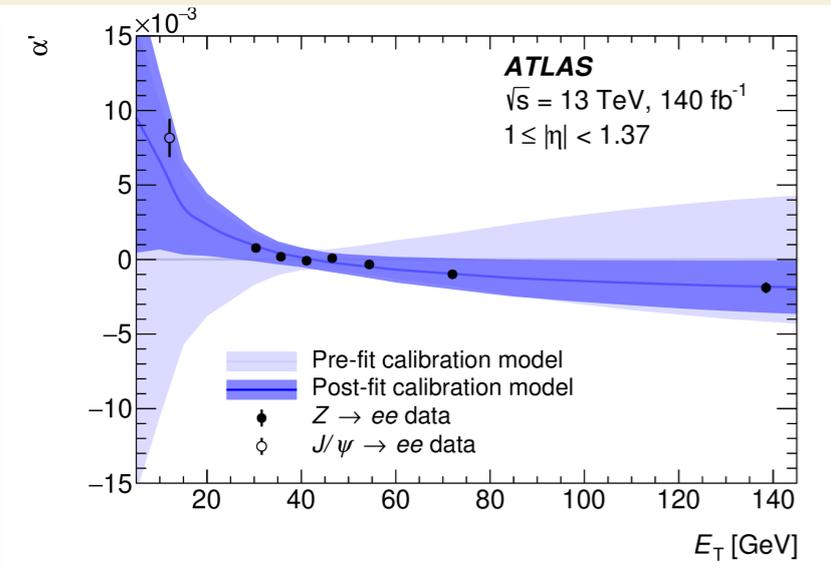
Energy loss (material)



→ Uncertainty in m_W **4.8 MeV**

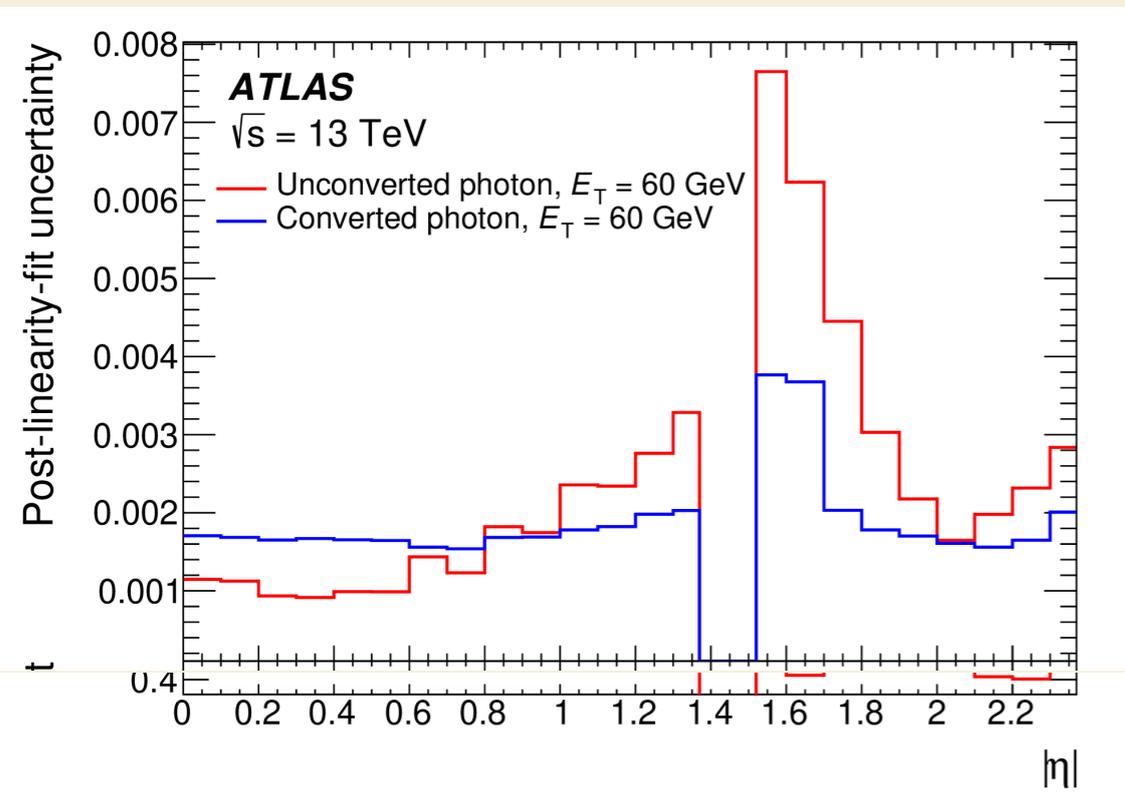
→ final precision scale for Z mass **5×10^{-5}**

e/γ performances

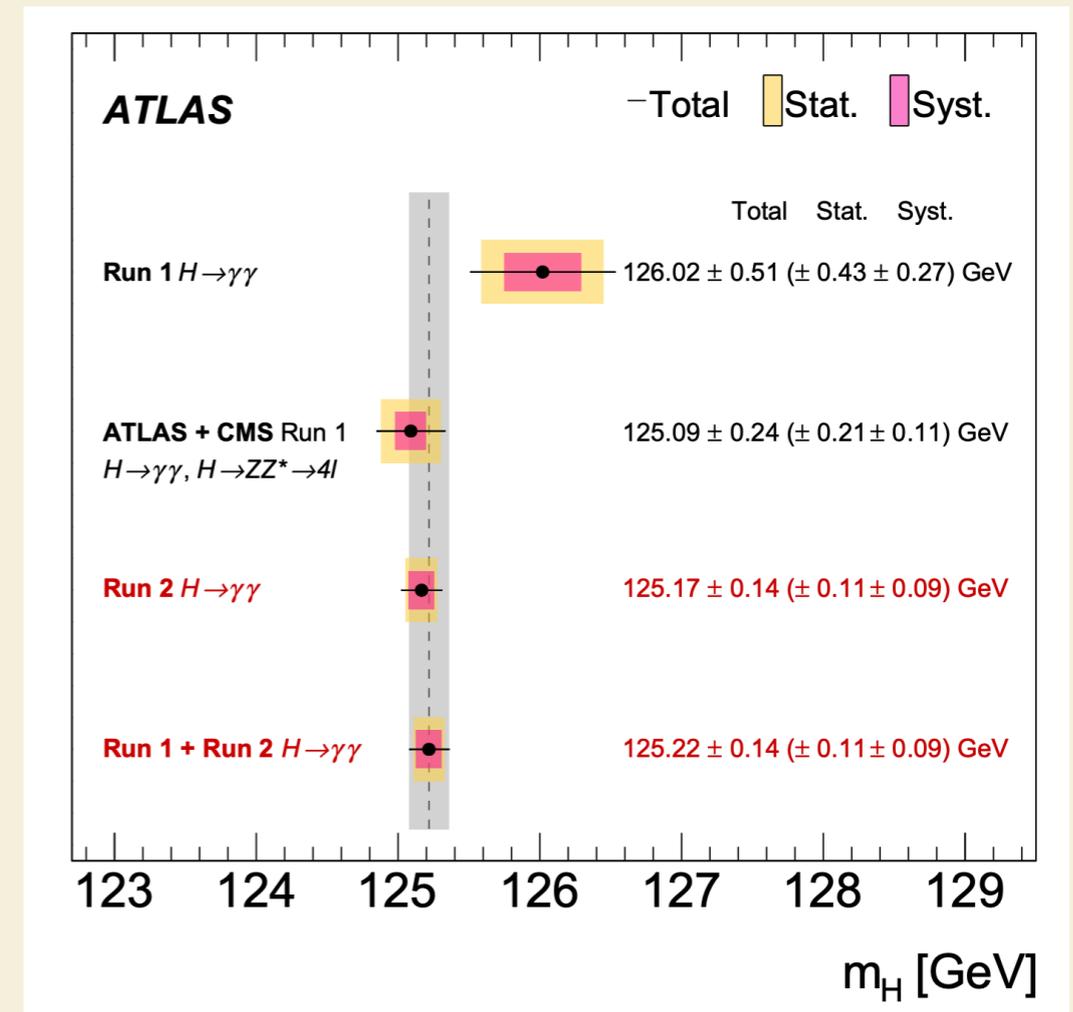


Detailed photon energy calibration enabled most precise Higgs mass measurement to date (90 MeV (0.07%) systematic uncertainty in $H \rightarrow \gamma\gamma$)

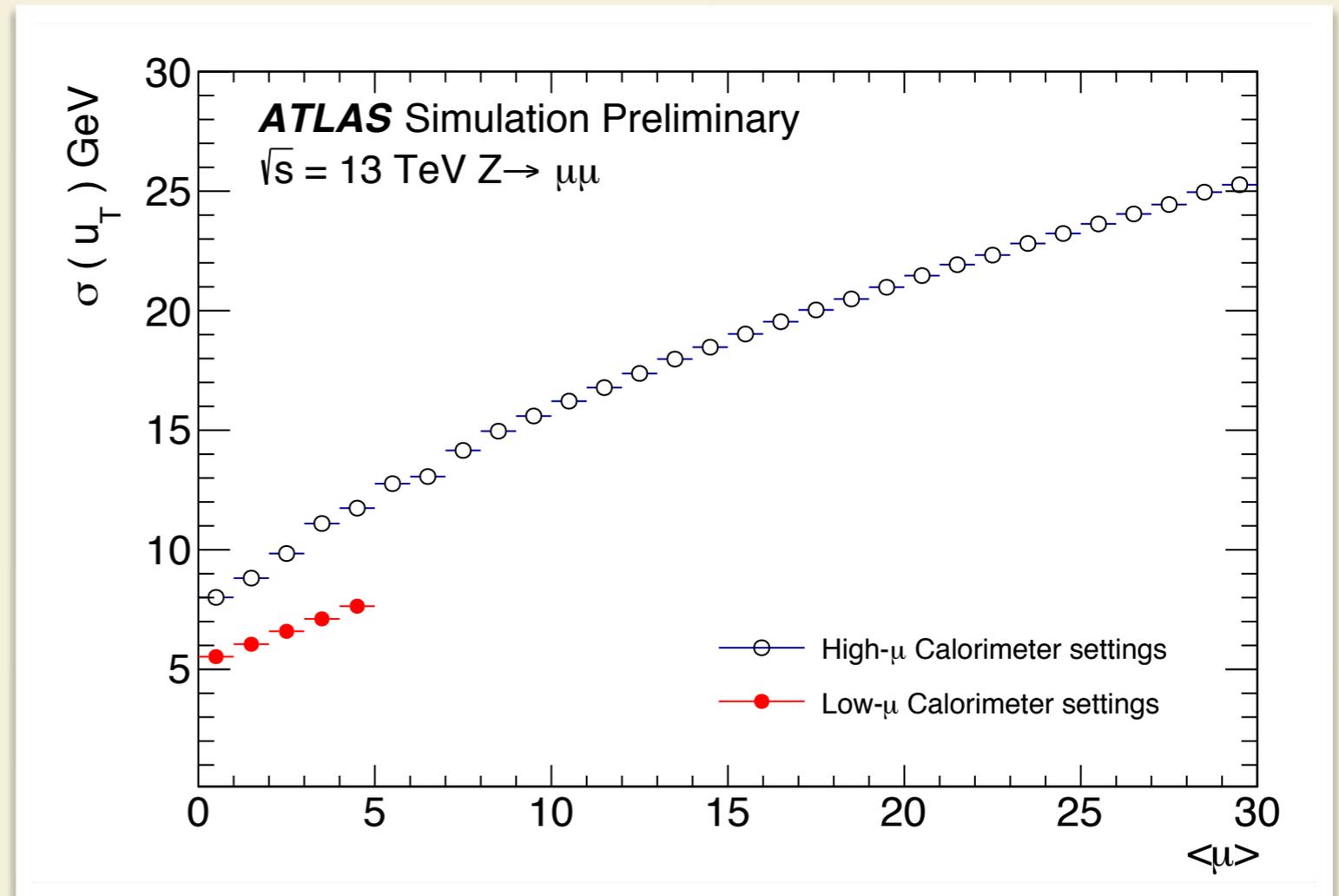
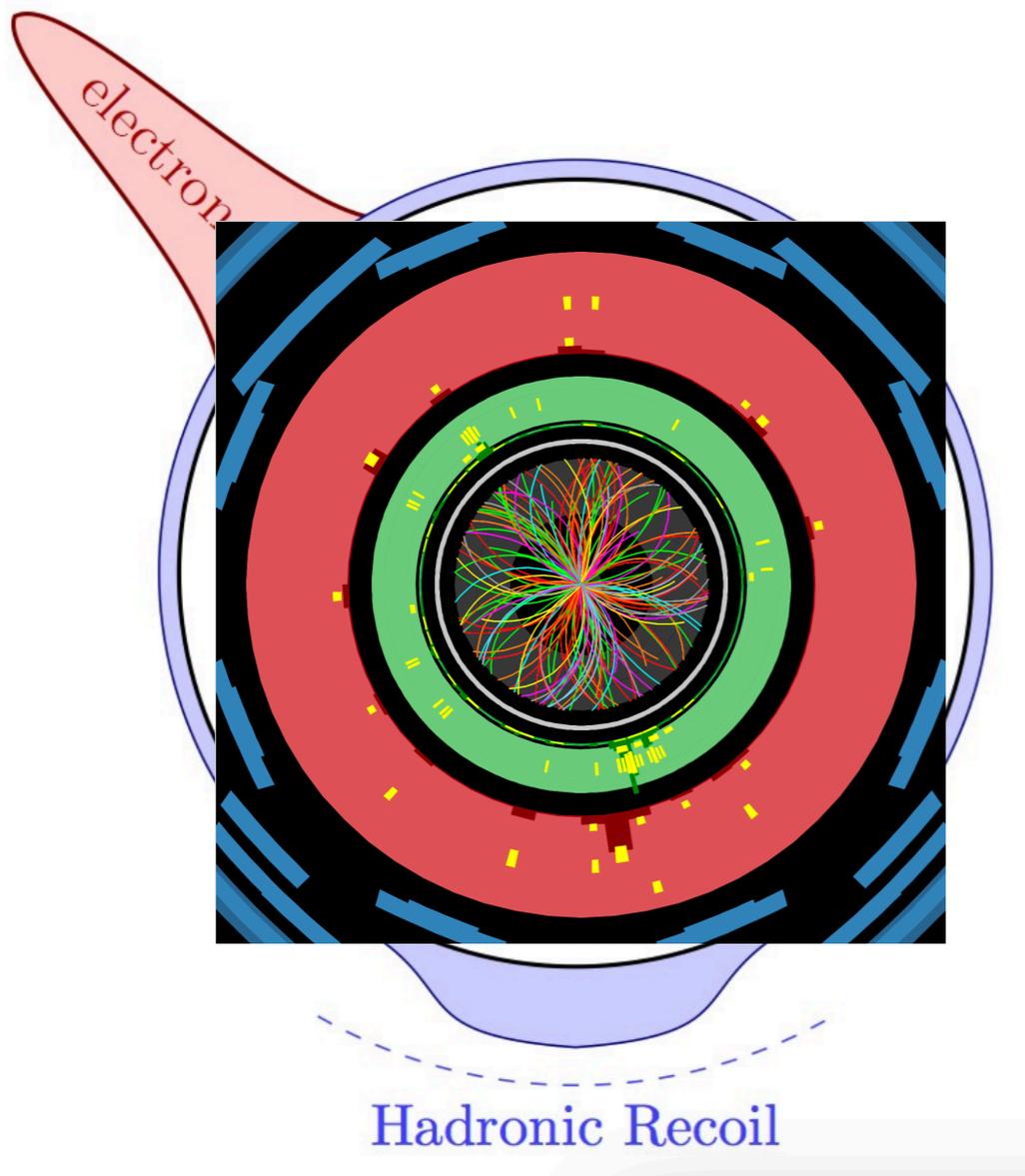
Phys. Lett. B 847 (2023) 138315



JINST 19 (2024) P02009



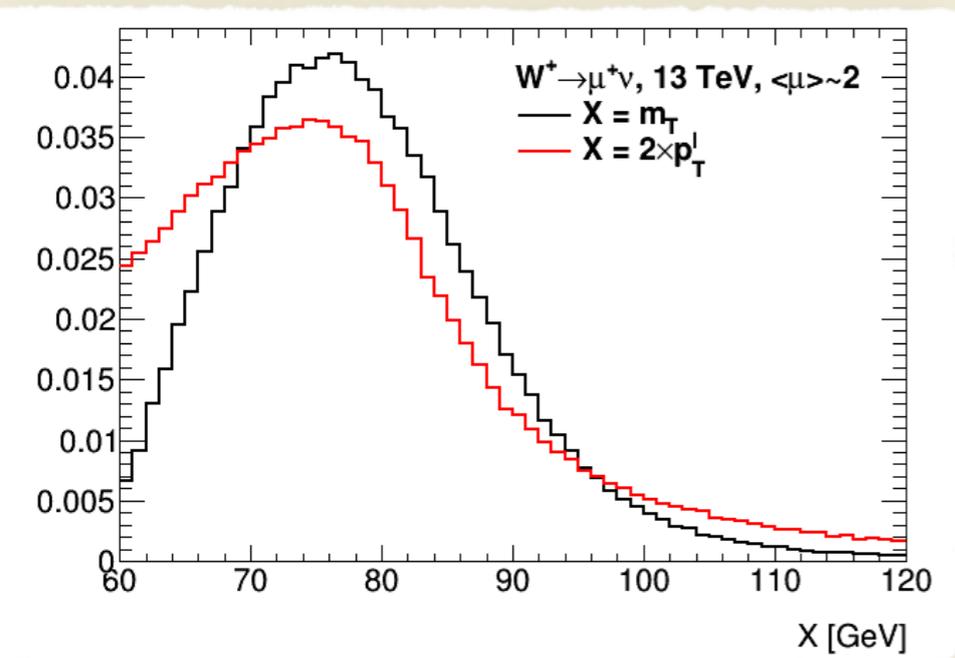
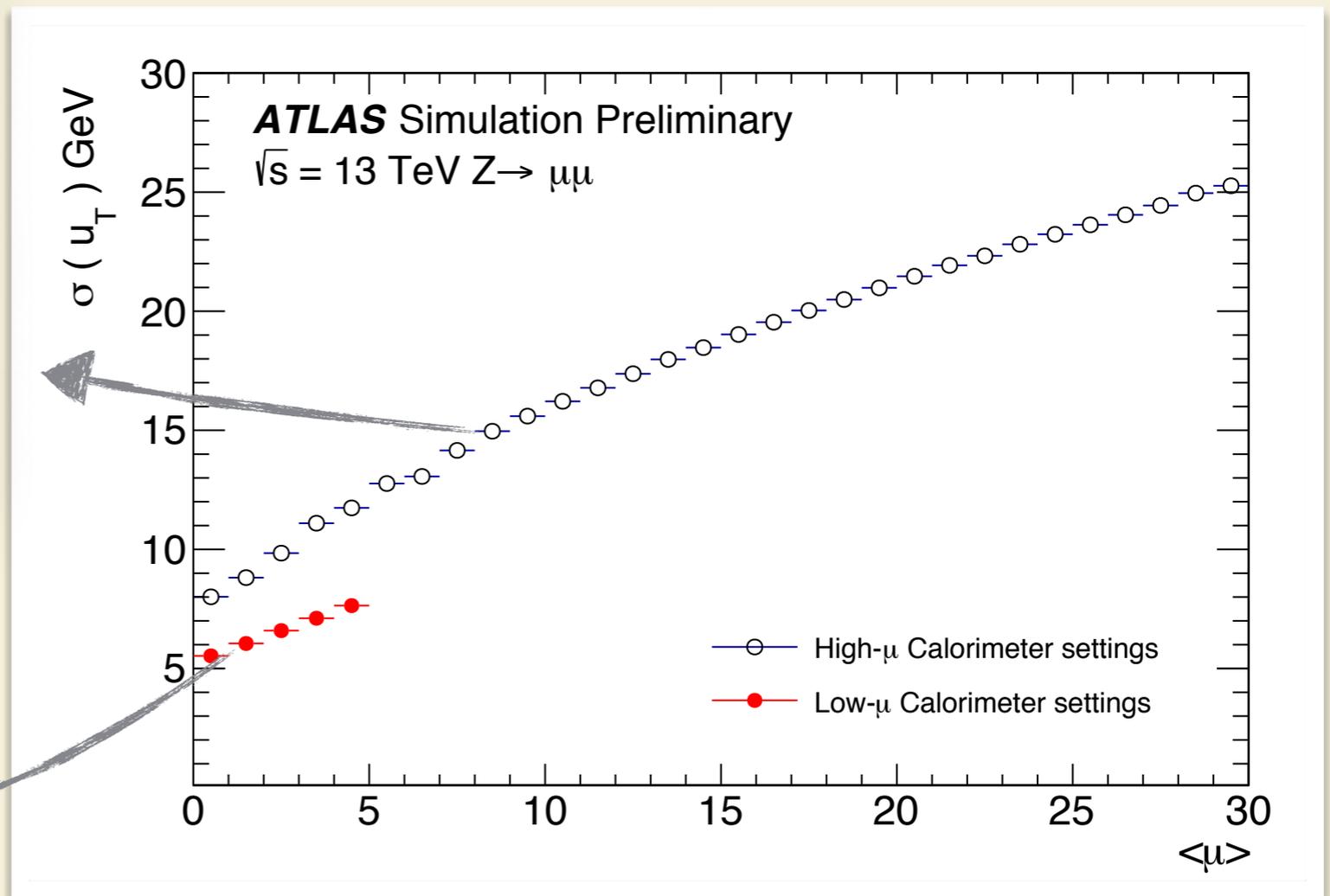
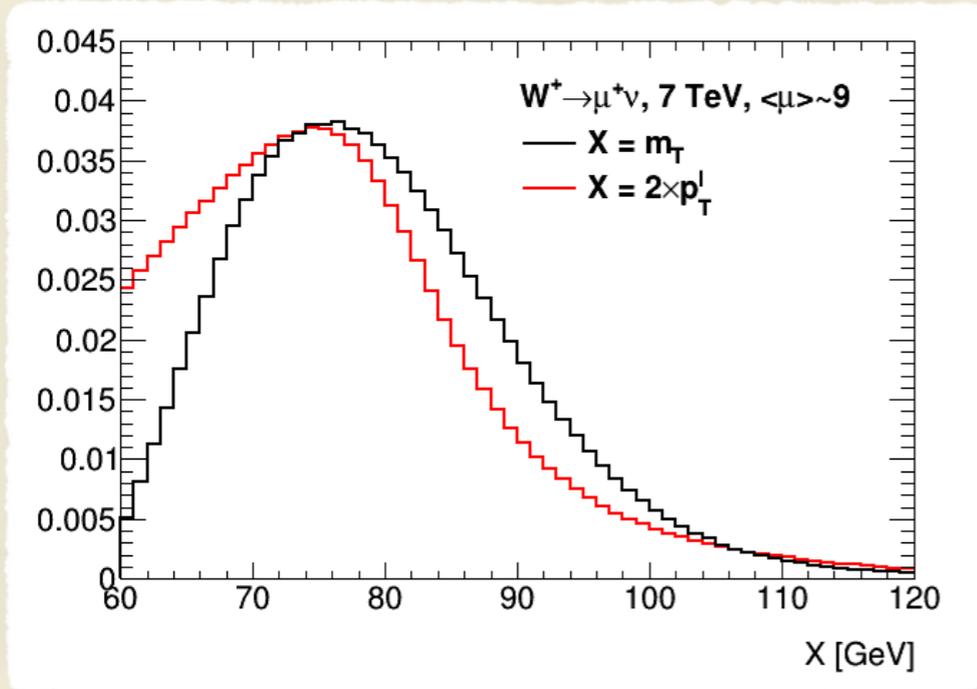
W mass sensitivity and pileUp



$$\vec{u}_T = \sum_i \vec{E}_{T,i}$$

- ▶ **u_T resolution** strongly depends on ΣE_T (~ total event activity)
 - ▶ At low p_T^W , underlying event & **pileup** $\langle \mu \rangle$ contribute to deterioration of the recoil resolution → **therefore to the statistical sensitivity to m_W**

W mass sensitivity and pileUp



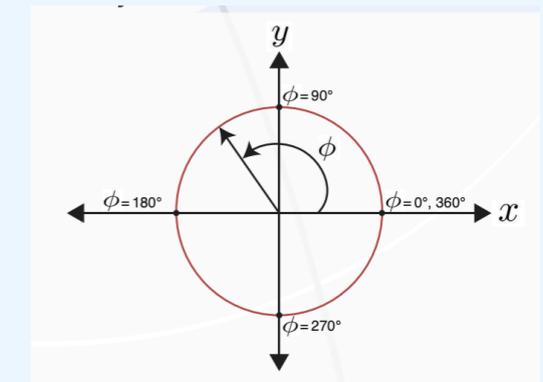
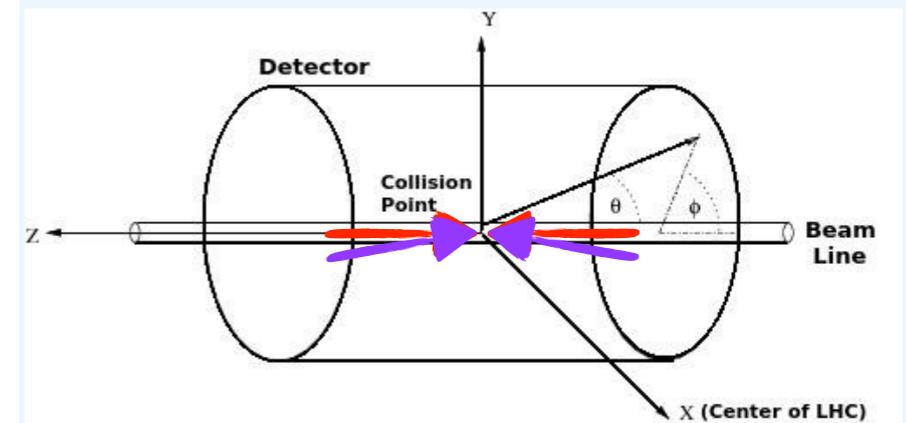
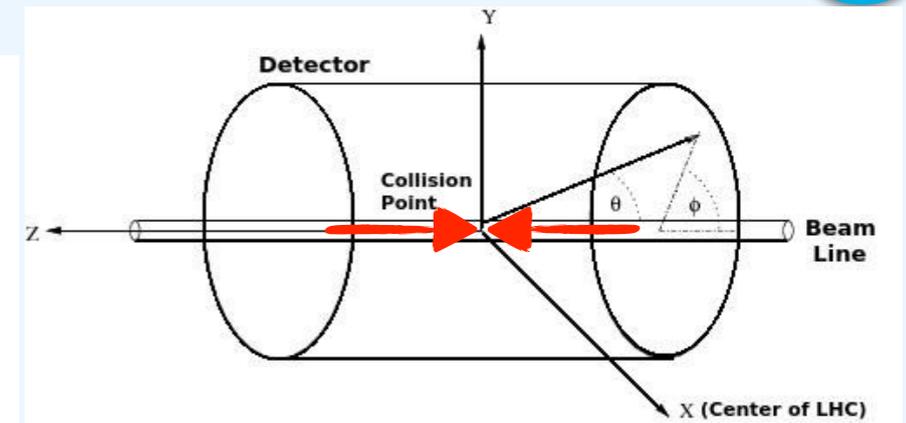
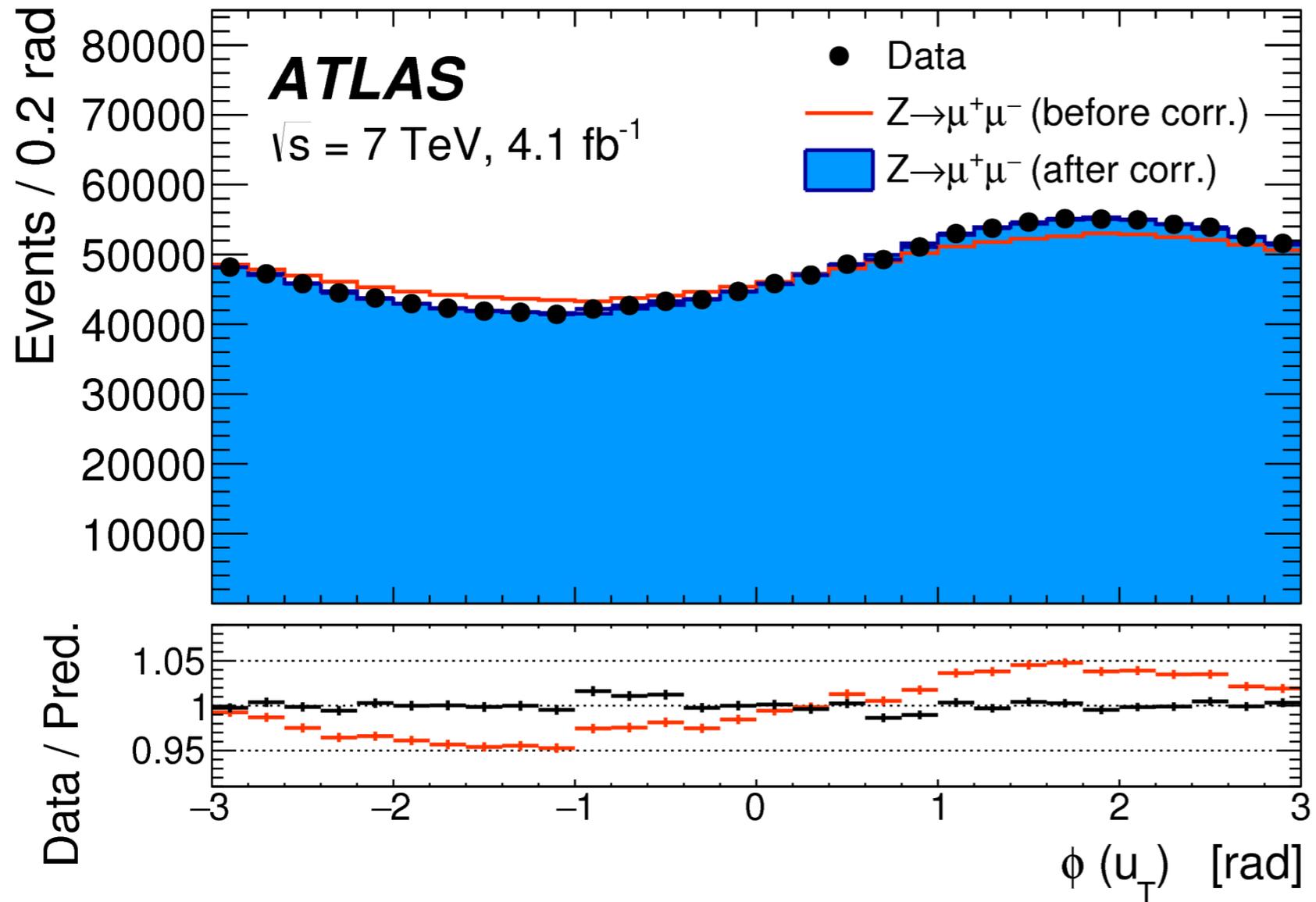
2.5 x better $\sigma(u_T)$
 7 TeV vs 5 TeV
 $\langle \mu \rangle = 9$ vs $\langle \mu \rangle = 2$

u_T resolution strongly depends on ΣE_T (~ total event activity)

- At low p_T^W , underlying event & pileup $\langle \mu \rangle$ contribute to deterioration of the recoil resolution → therefore to the statistical sensitivity to m_W

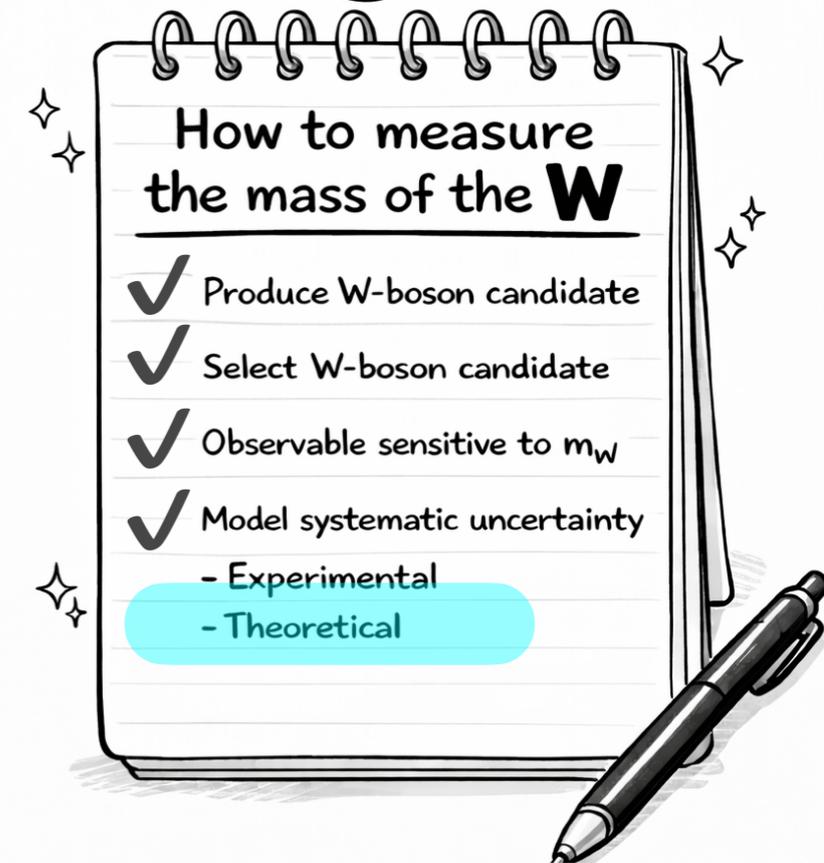
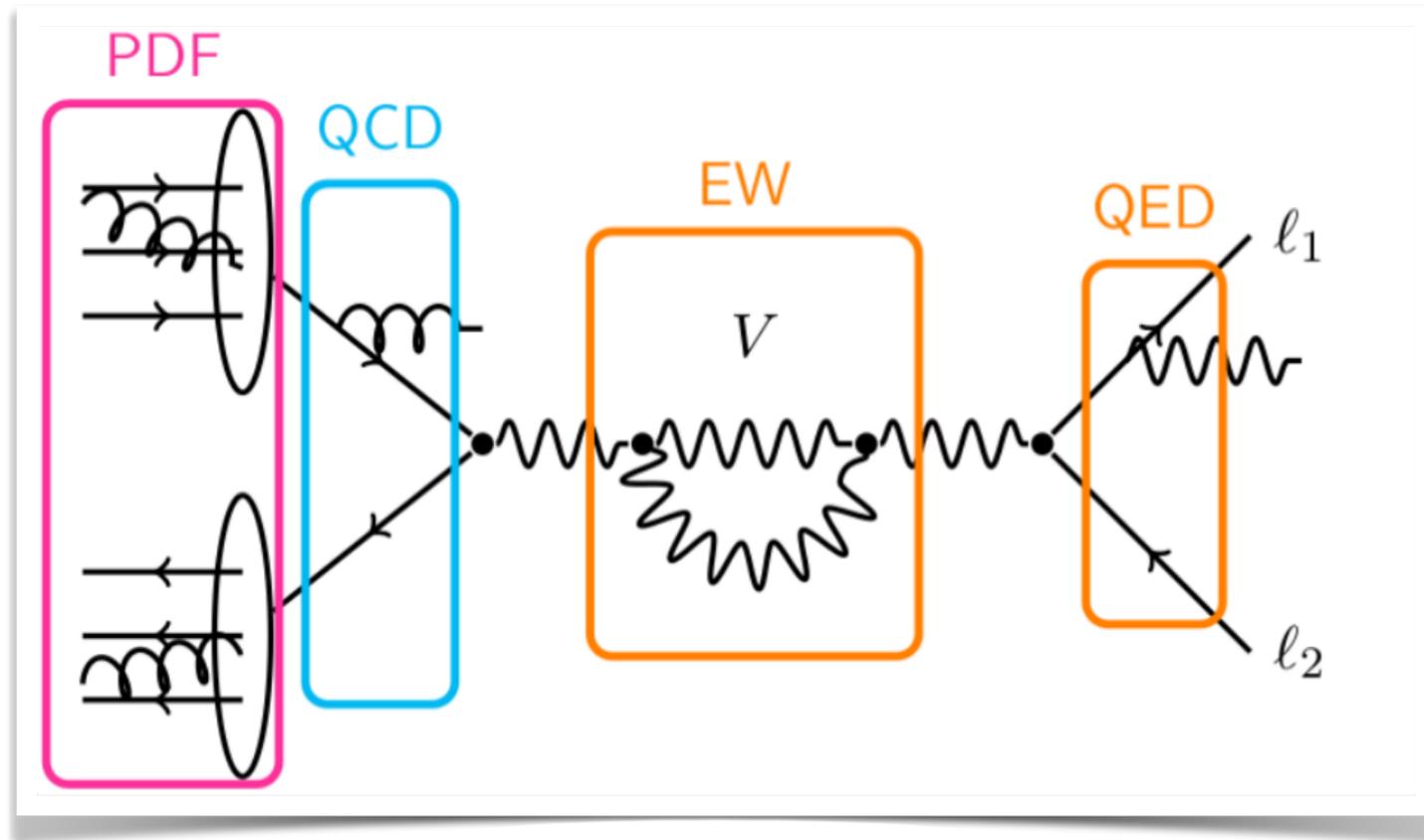


bonus: perfect knowledge of our detectors ?



In the ideal case of beams coinciding with the z-axis, the physical transverse momentum of W and Z bosons is uniformly distributed in ϕ . However, an offset of the interaction point with respect to the detector centre in the transverse plane, the non-zero crossing angle between the proton beams, and ϕ -dependent response of the calorimeters generate anisotropies in the reconstructed recoil distribution.

The W physics modelling



$\delta m_W < 10$ MeV precisions required $\sim 0.1-0.2\%$ control on the kinematics of the W production, sub-percent accuracy of predictions for PDF ; p_T^W modelling and W polarisation (A_i) is extreme challenge for QCD theory!

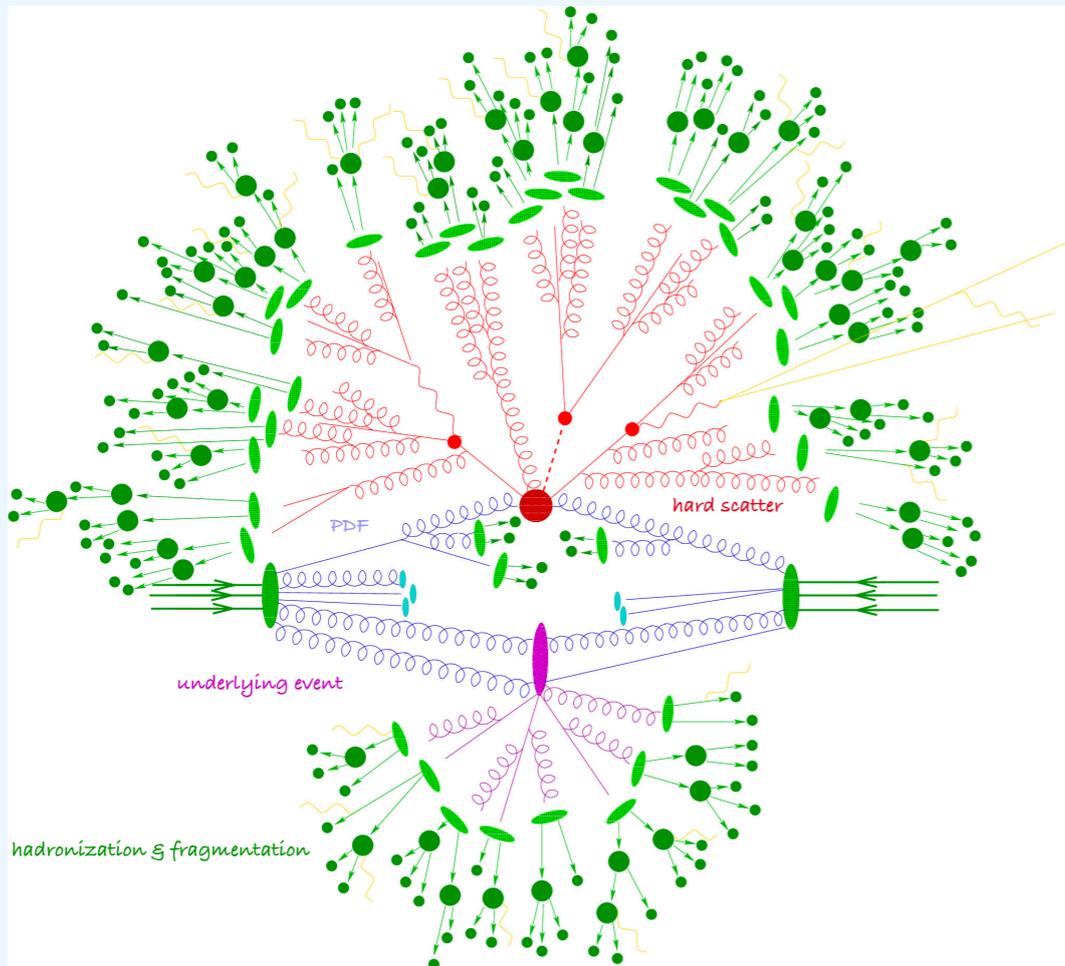


Theory advancement

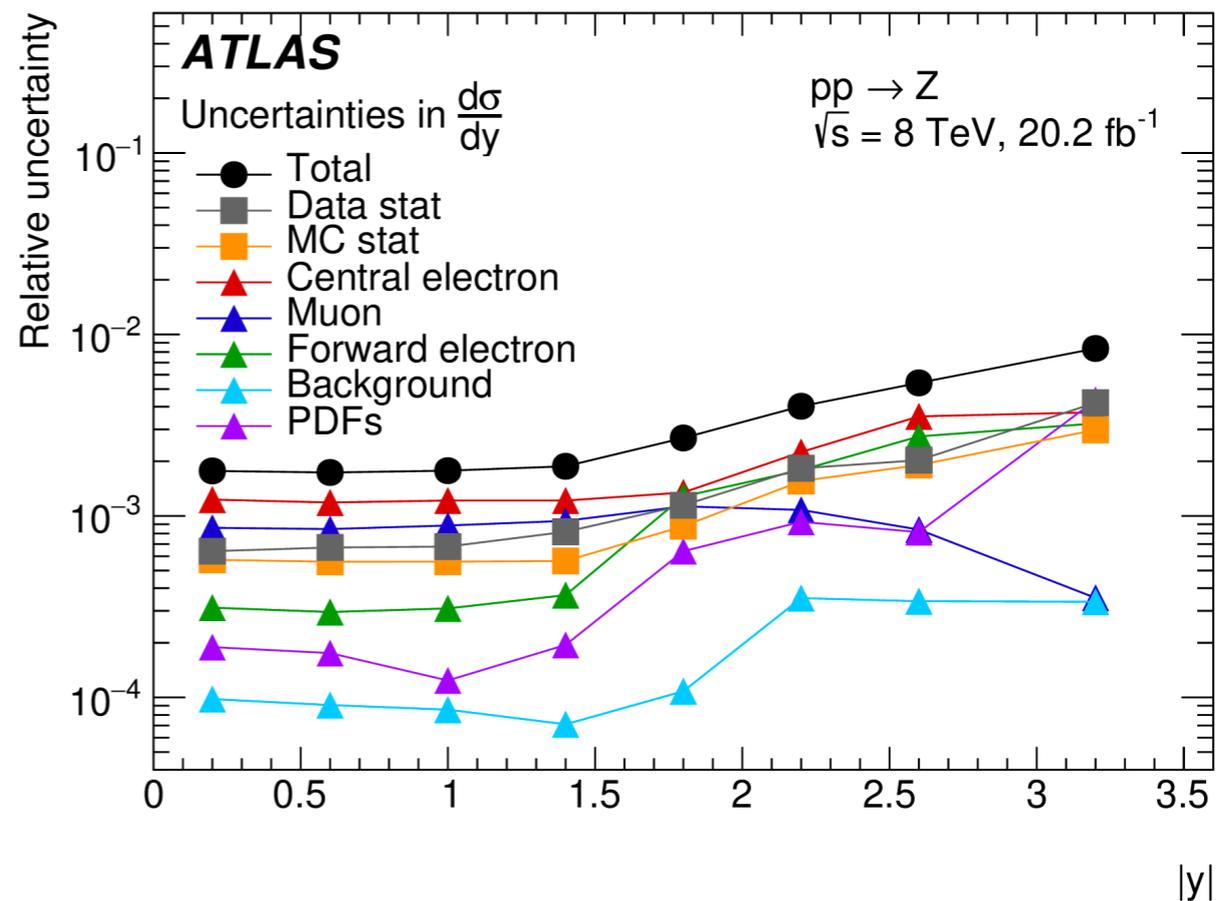


Tremendous progress in theory in the past 10 years !

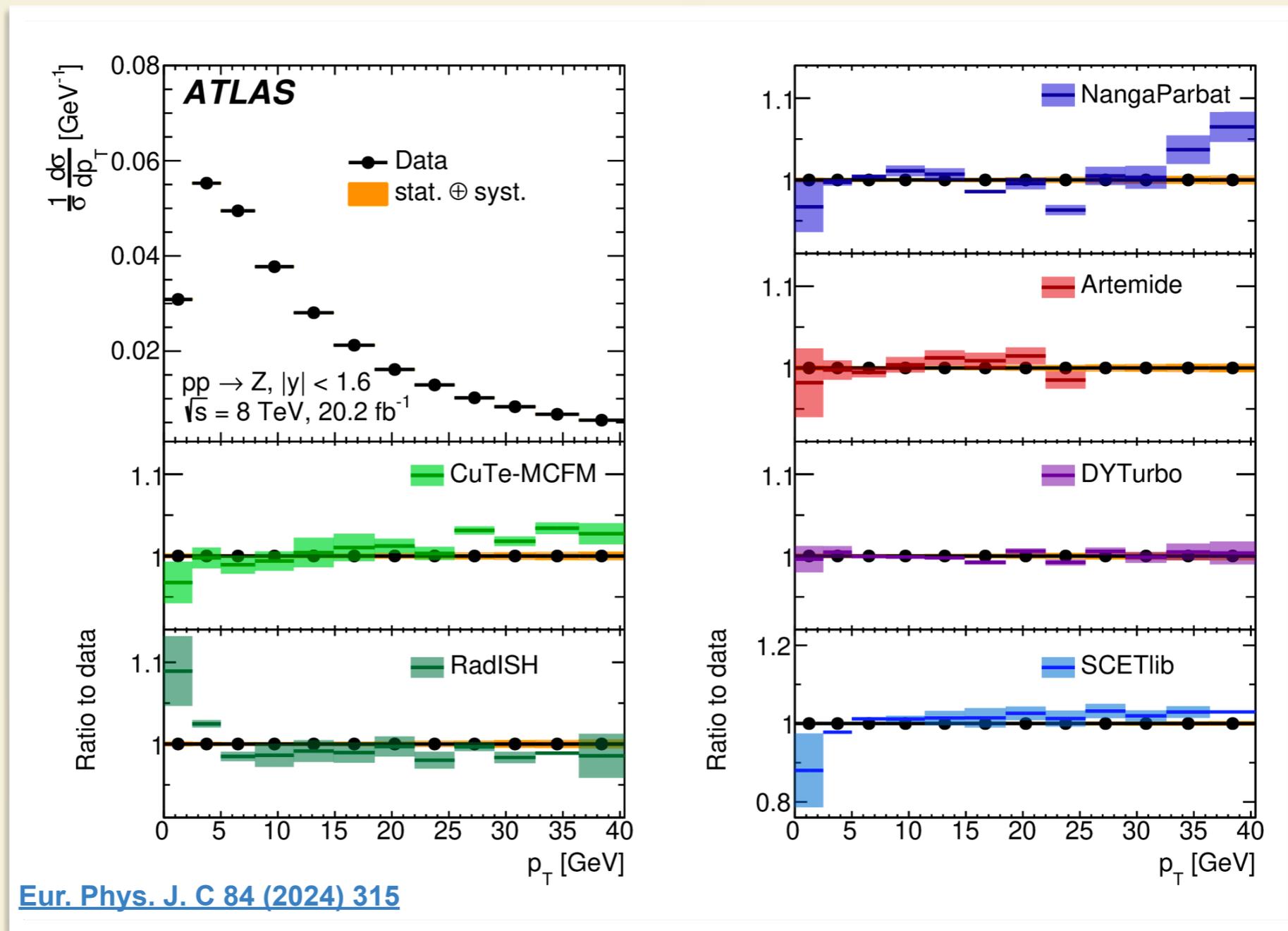
At the level of precision achieved by LHC experiments, pushing the theory frontier for all contributors to our predictions essential



differential x-section measurement of Z boson production
 % accuracy in the central $|y^Z|$ region below %
 uncertainties up to $|y^Z| < 3.6$

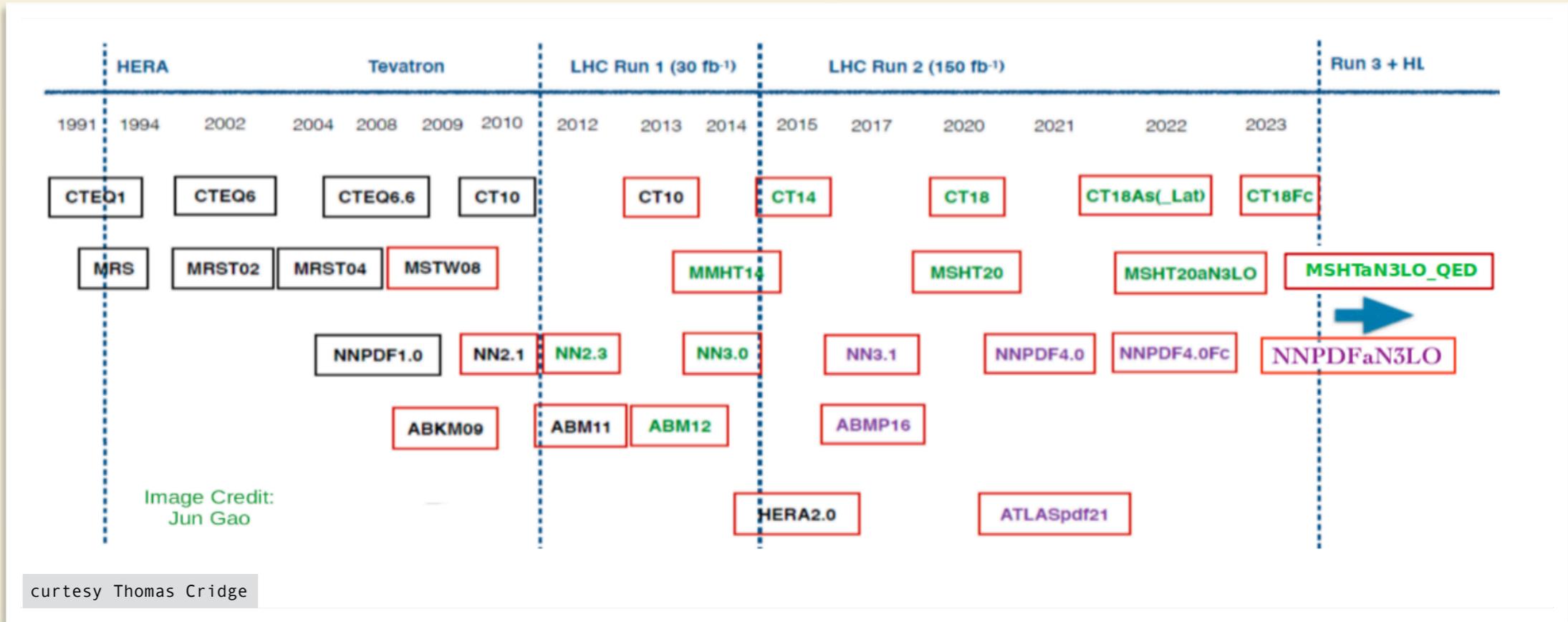


NNLO outdated \rightarrow N3LO + resummation

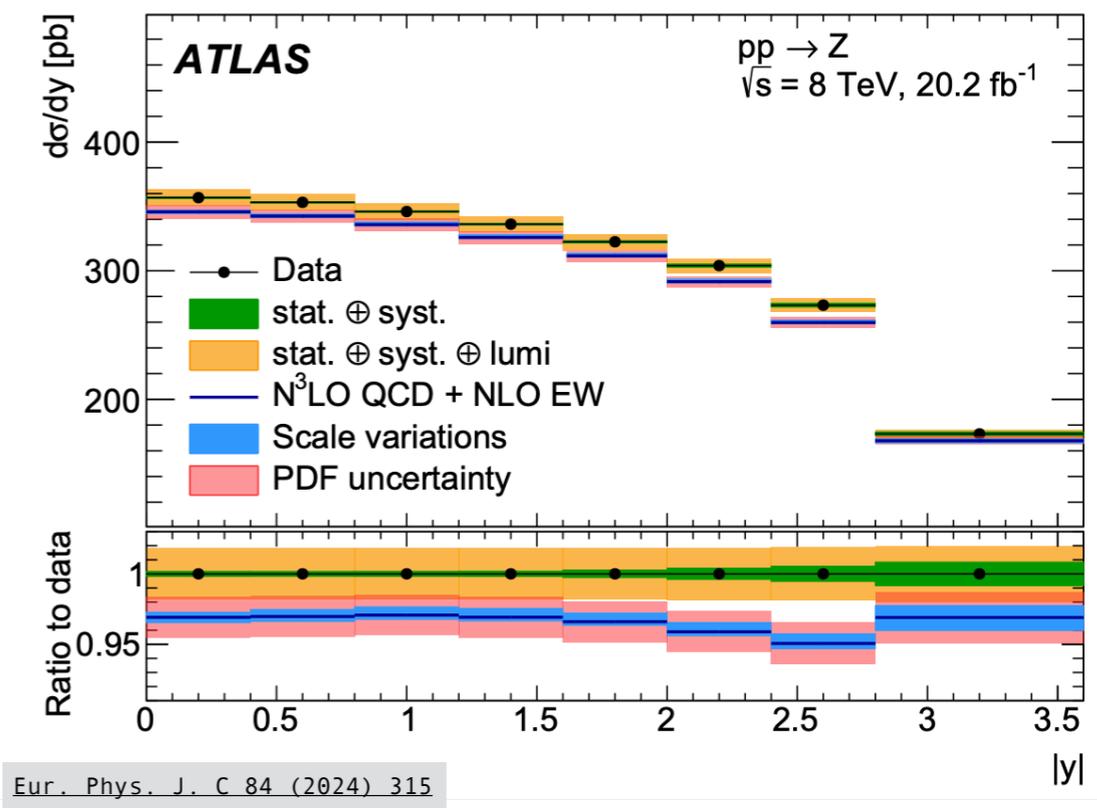
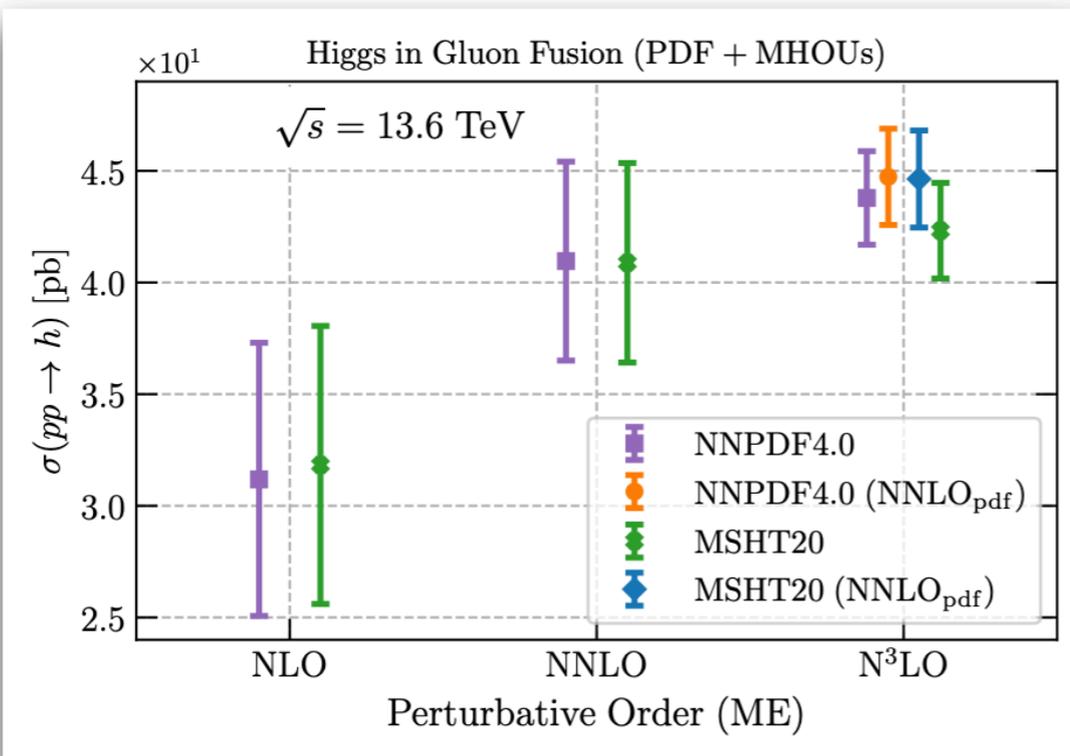


The Z-boson normalised $d\sigma/dp_T$ measurement compared with different state-of-the-art QCD perturbative calculations based on q_T resummation @ approximate N^4LL accuracy.

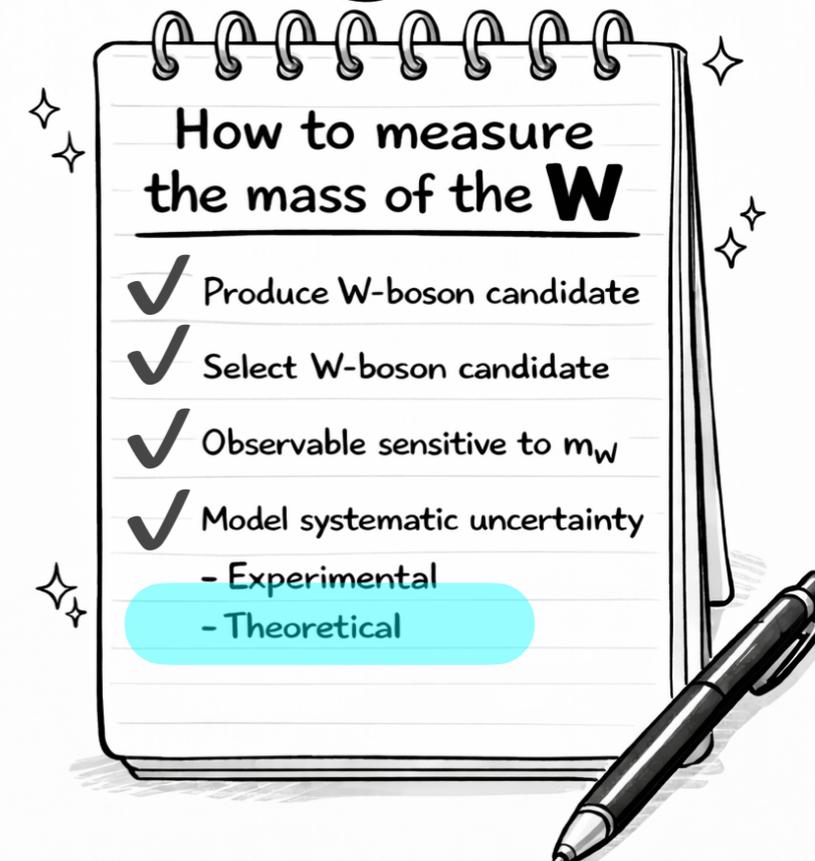
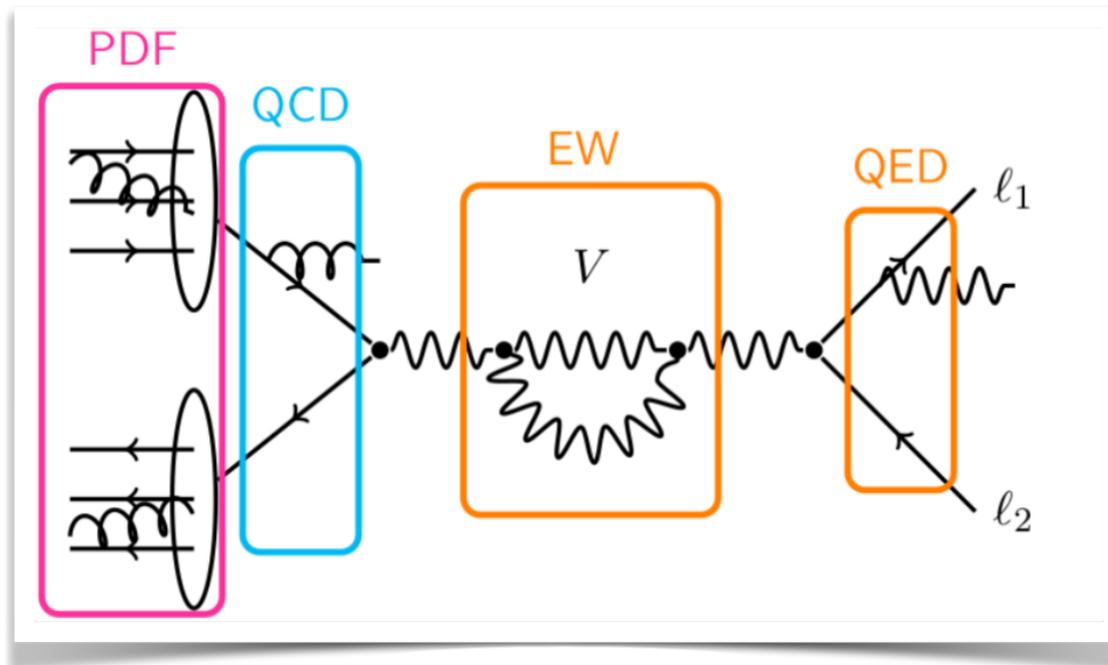
NNLO outdated → N3LO in PDF



<https://nnpdf.mi.infn.it/nnpdf4-0-n3lo/>



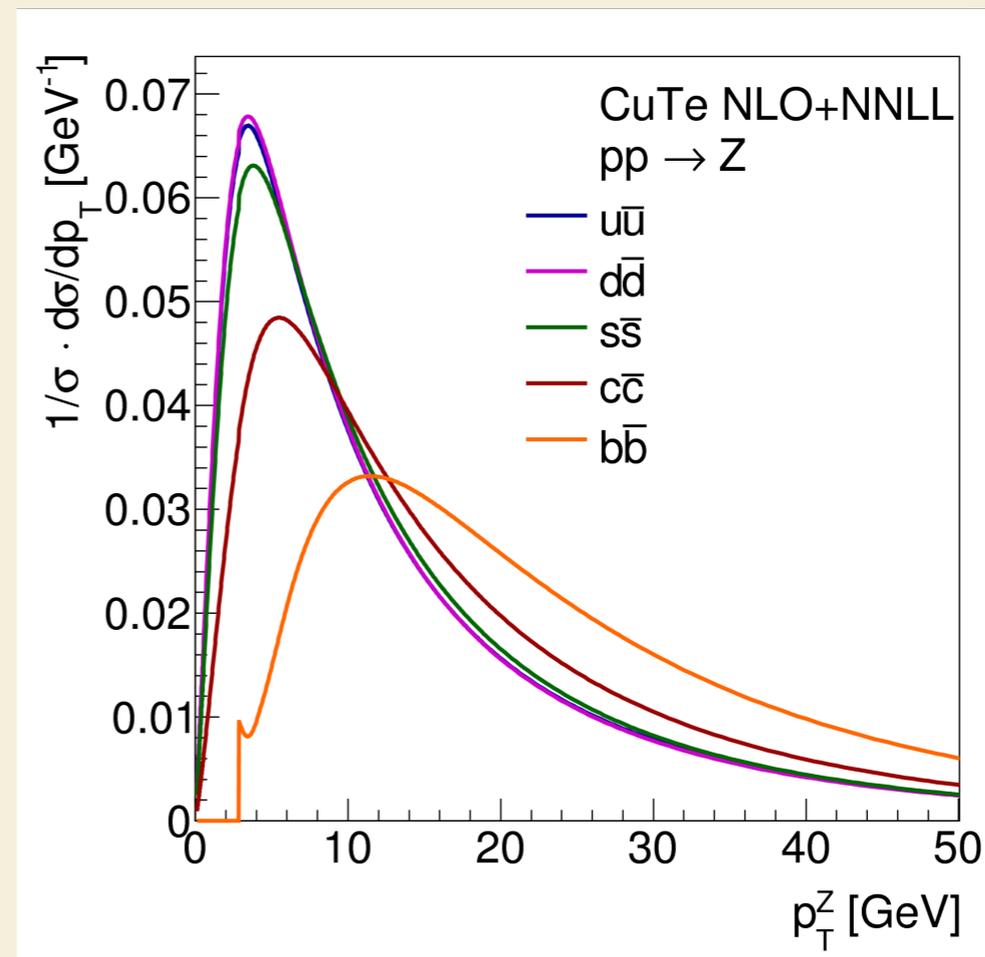
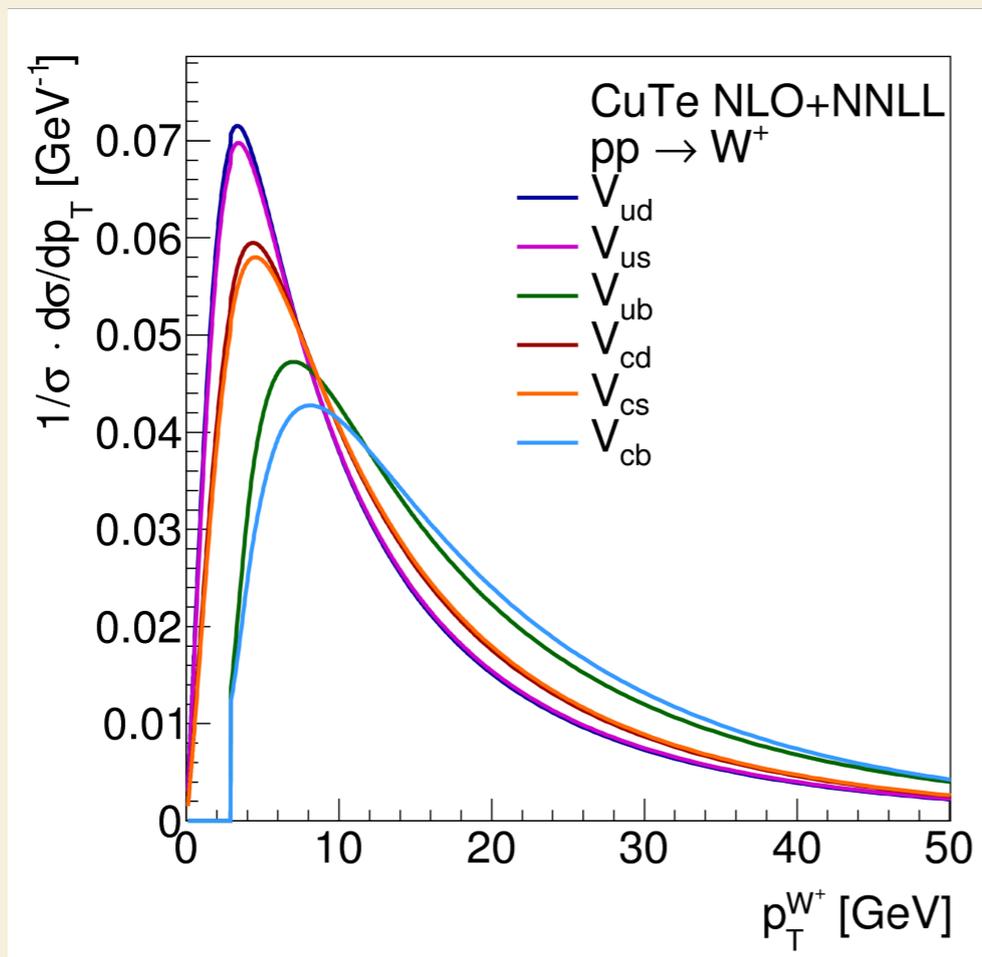
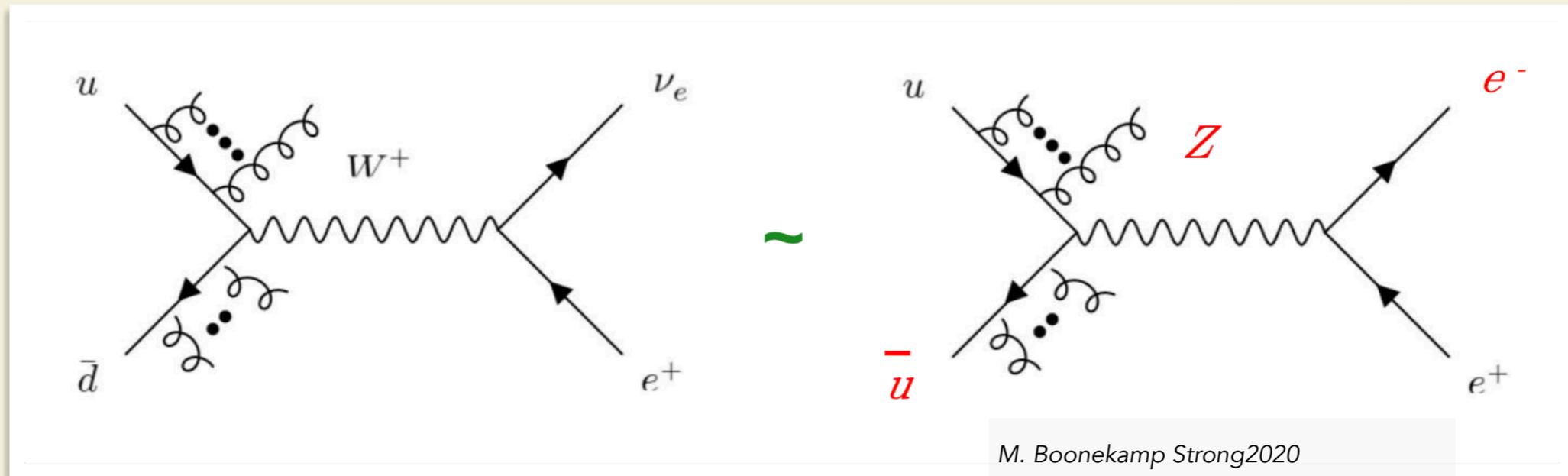
The W physics modelling



- ▶ @LHC W mass physics modelling is described using a **composite model** :
- ▶ Start from the NLO/NNLO generators + LL parton-shower (Pythia8) and apply corrections to reach the state of the art accuracy.
 - ▶ Using an useful decomposition: **factorising** the dynamic of the boson production and the kinematic of the boson decay.

$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T)}{dp_T} \right] \left[(1 + \cos^2\theta) + \sum_{i=0}^7 A_i(p_T, y, m) P_i(\cos\theta, \phi) \right]$$

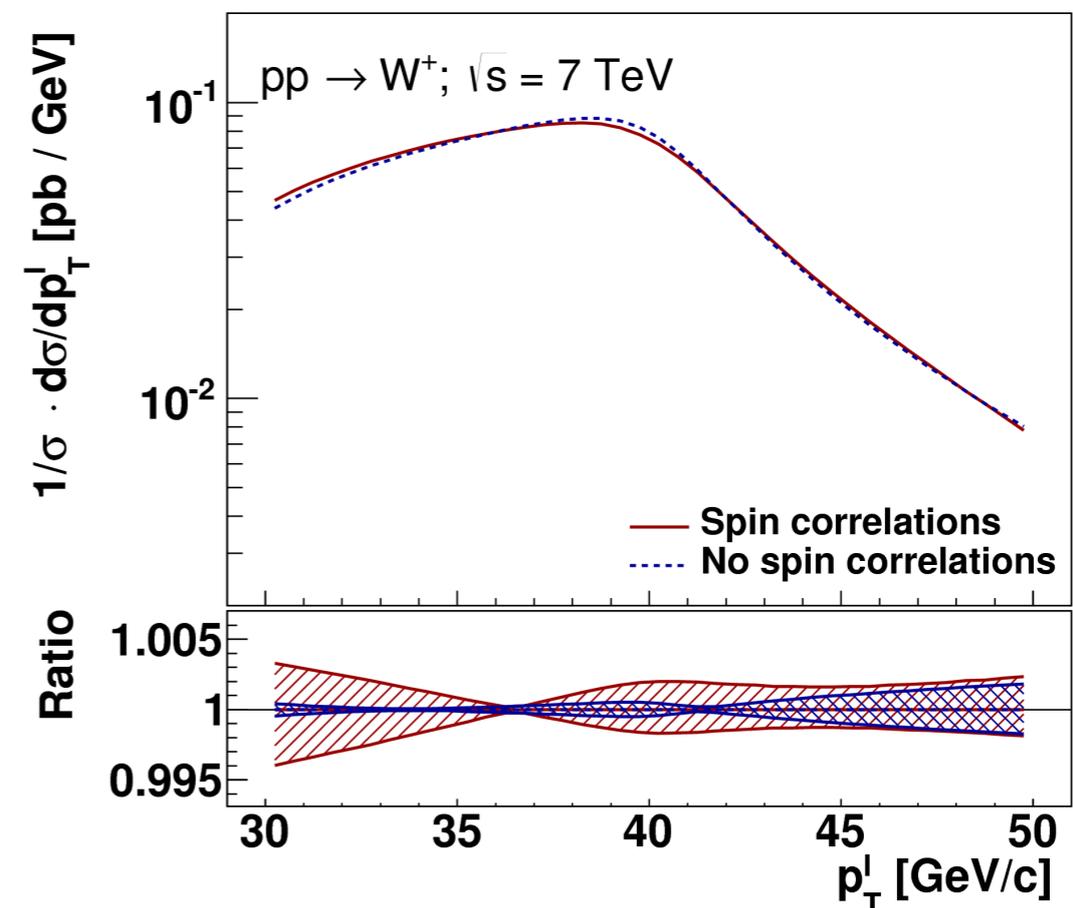
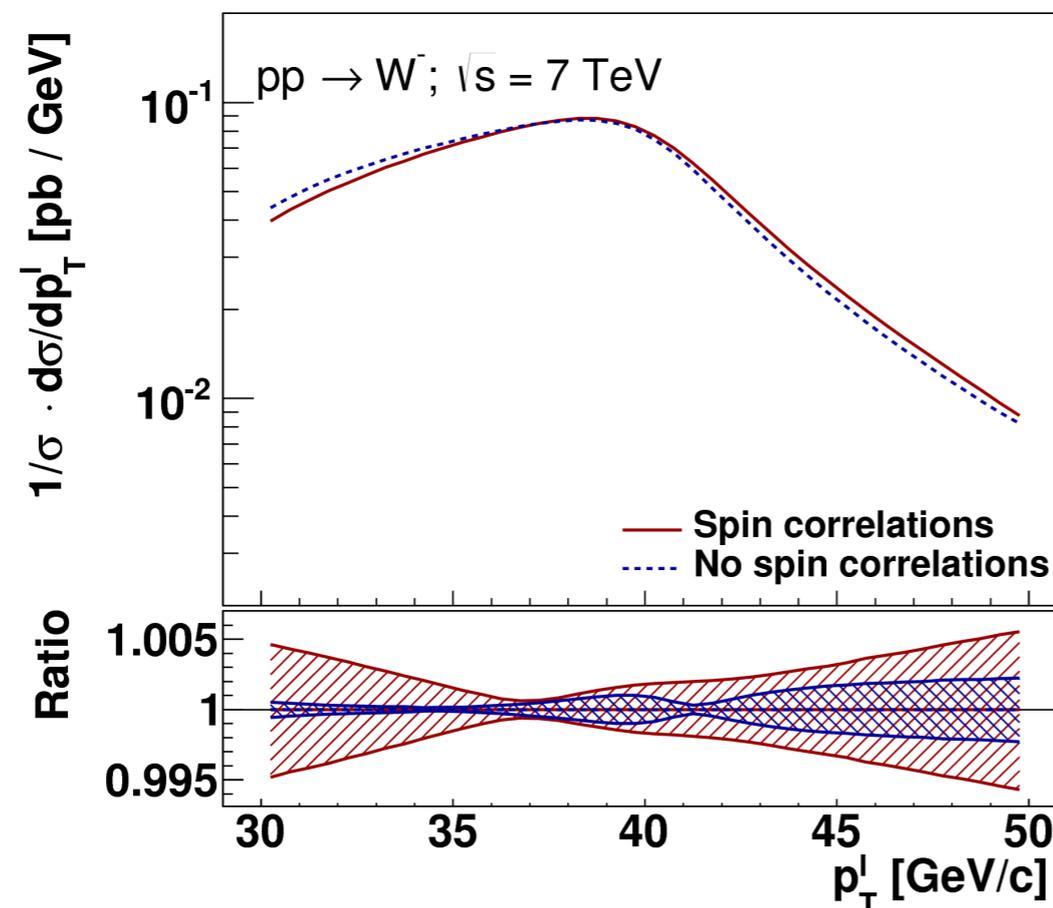
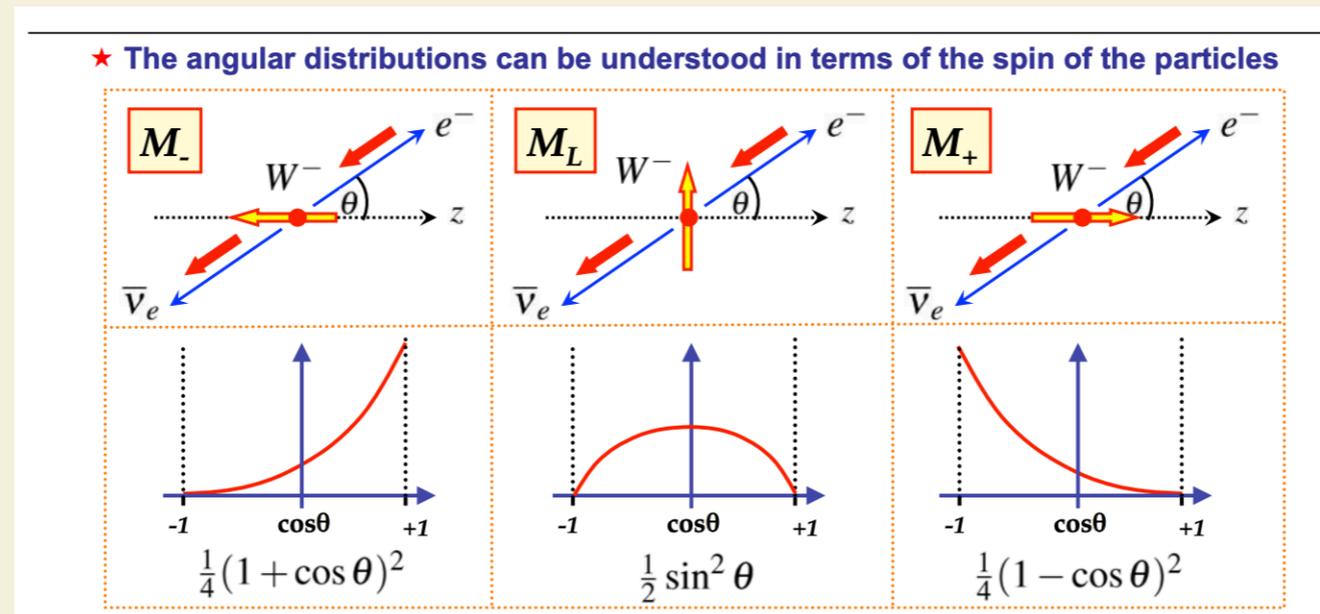
QCD it is not identical for W and Z boson



[More Info](#)



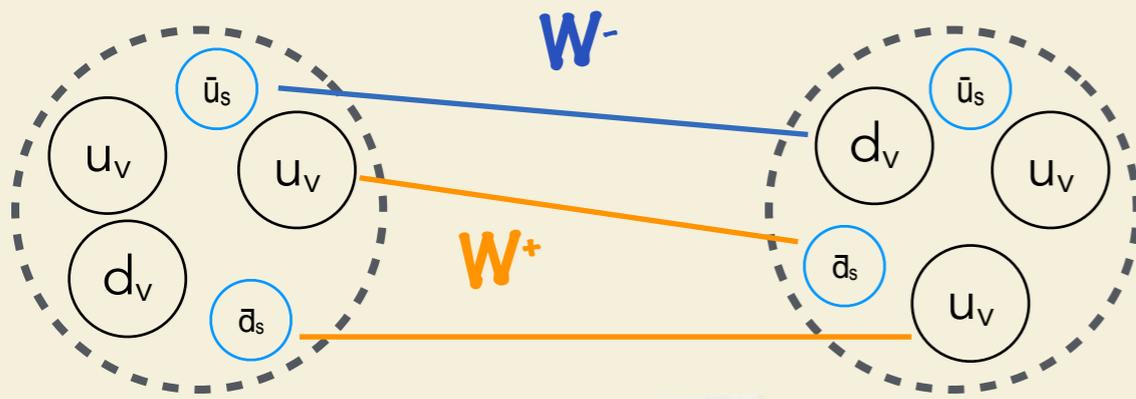
Spin correlation



[More Info](#)

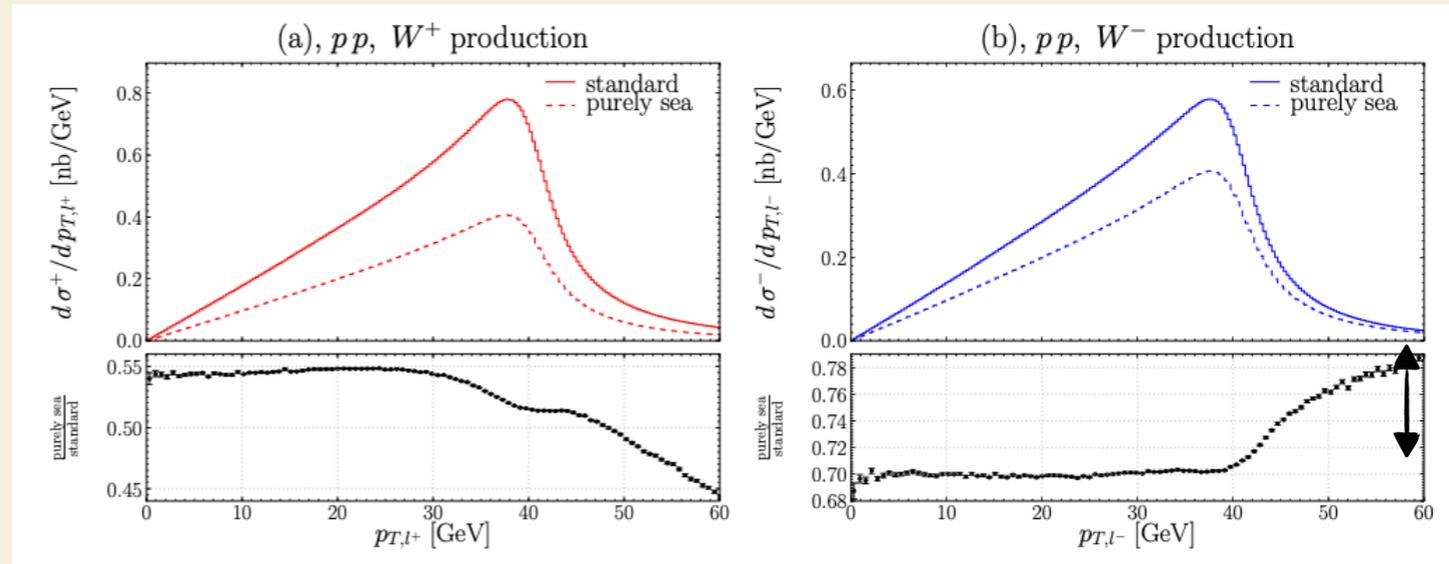


PDF



In pp collision: different cross section for W^+ and W^- and different dynamics.

Eur. Phys. J. C 69 (2010) 379-397



- ▶ Difference between u,d valence and the sea distributions determine the W-boson rapidity distributions → affects acceptance and fiducial volume
- ▶ kinematic distributions & signal yields in the different categories have additional constraining power on the PDFs unc. (*in situ constraint*)

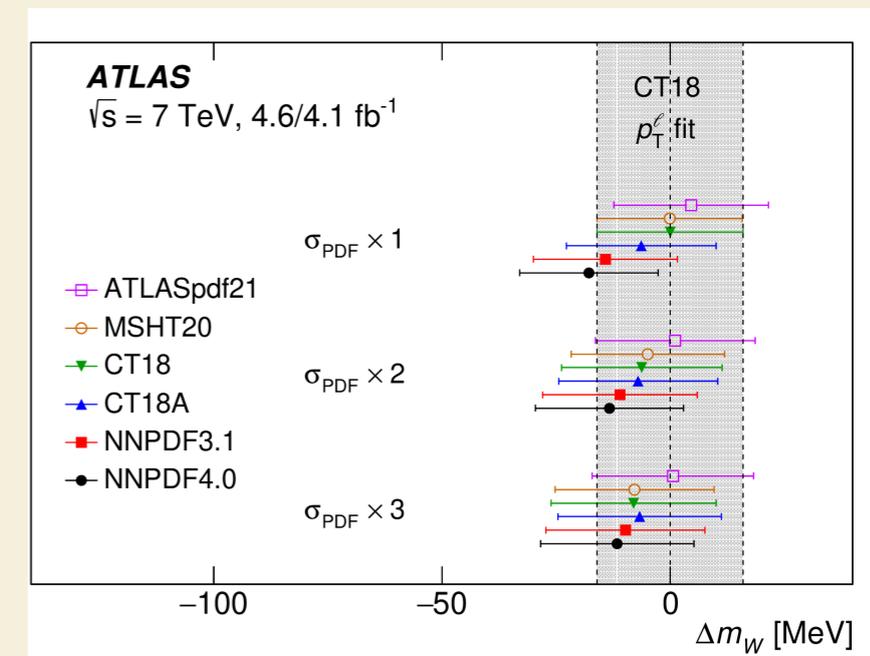
▶ Profiling of PDF uncertainty:

▶ **reduction** of Δm_W PDFs envelope

▶ **reduction** impact of PDF uncertainties

(previous measurement $\delta_{(PDF)} m_W = 9-10$ MeV)

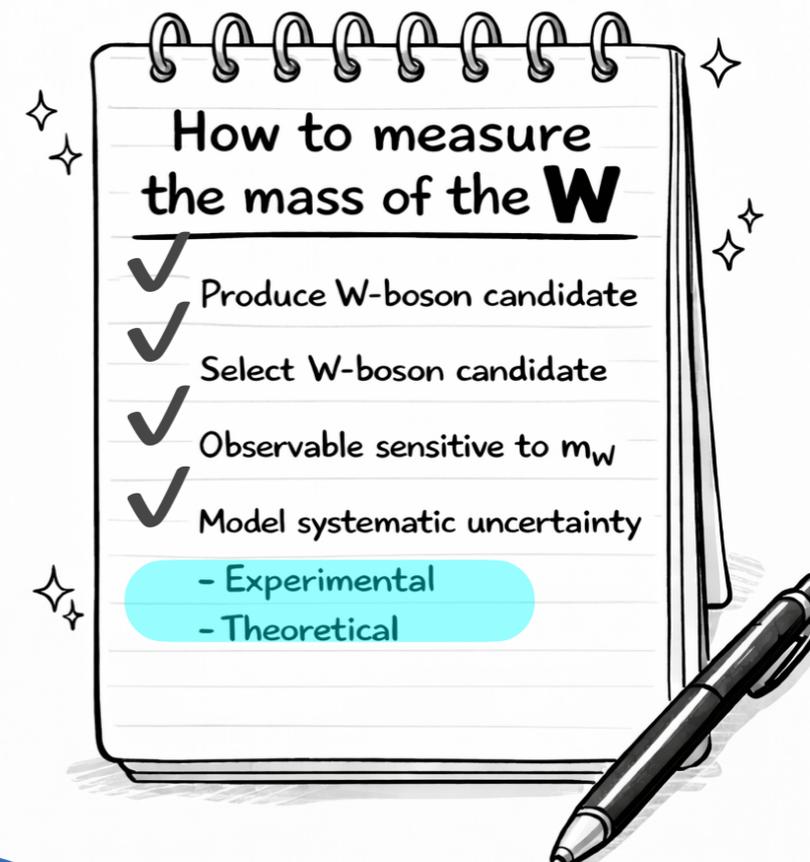
▶ **CT18 PDF set baseline:** $\delta_{(PDF)} m_W = 7.7$ MeV [ATLAS], 4.4 MeV [CMS]



The W physics modelling

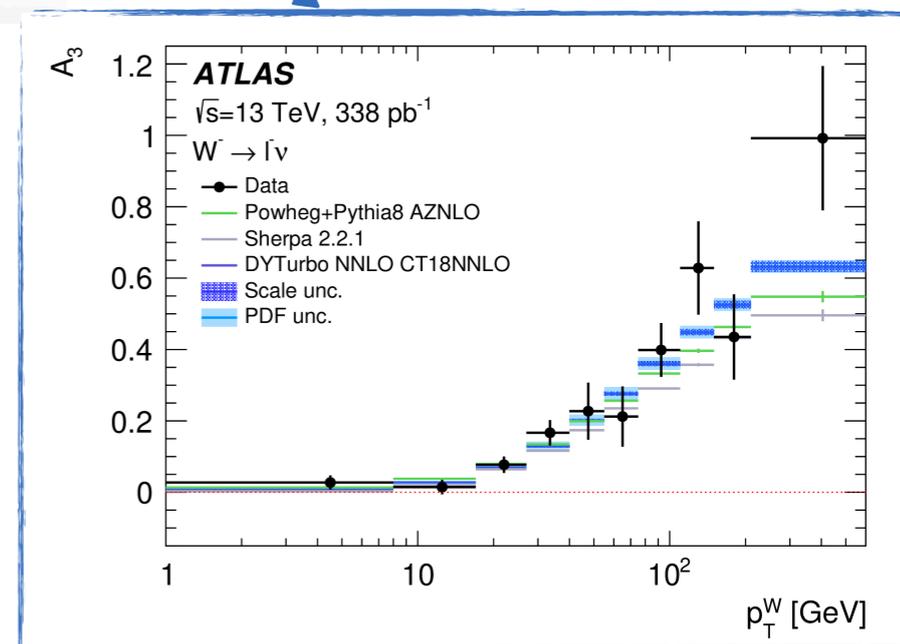
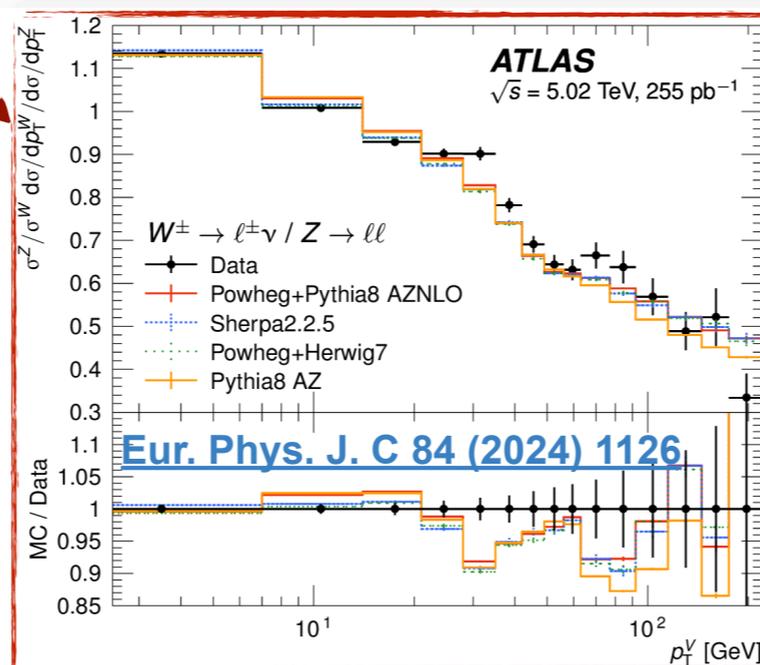
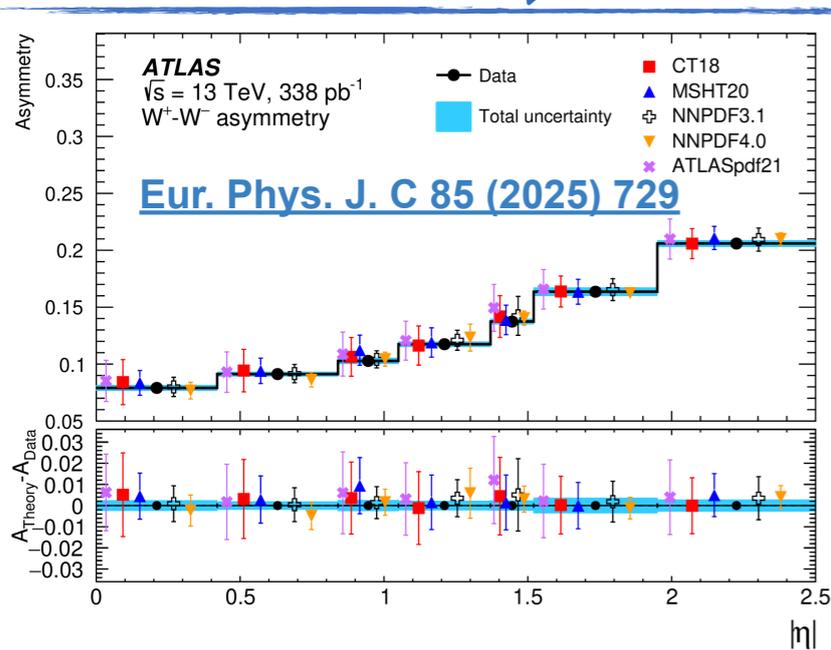
ATLAS/LHCb

- ▶ start Powheg+Pythia8 [NLO+LL (PS)] and apply corrections \Rightarrow NNLO pQCD accuracy
- Use ancillary measurements of Drell-Yan processes to validate (and tune) the model and assess systematic uncertainties.



$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T)}{dp_T} \right] \left[(1 + \cos^2\theta) + \sum_{i=0}^7 A_i(p_T, y, m) P_i(\cos\theta, \phi) \right]$$

e-print [arXiv:2509.13759](https://arxiv.org/abs/2509.13759)



Incredible set of new extremely precise measurement of W boson production

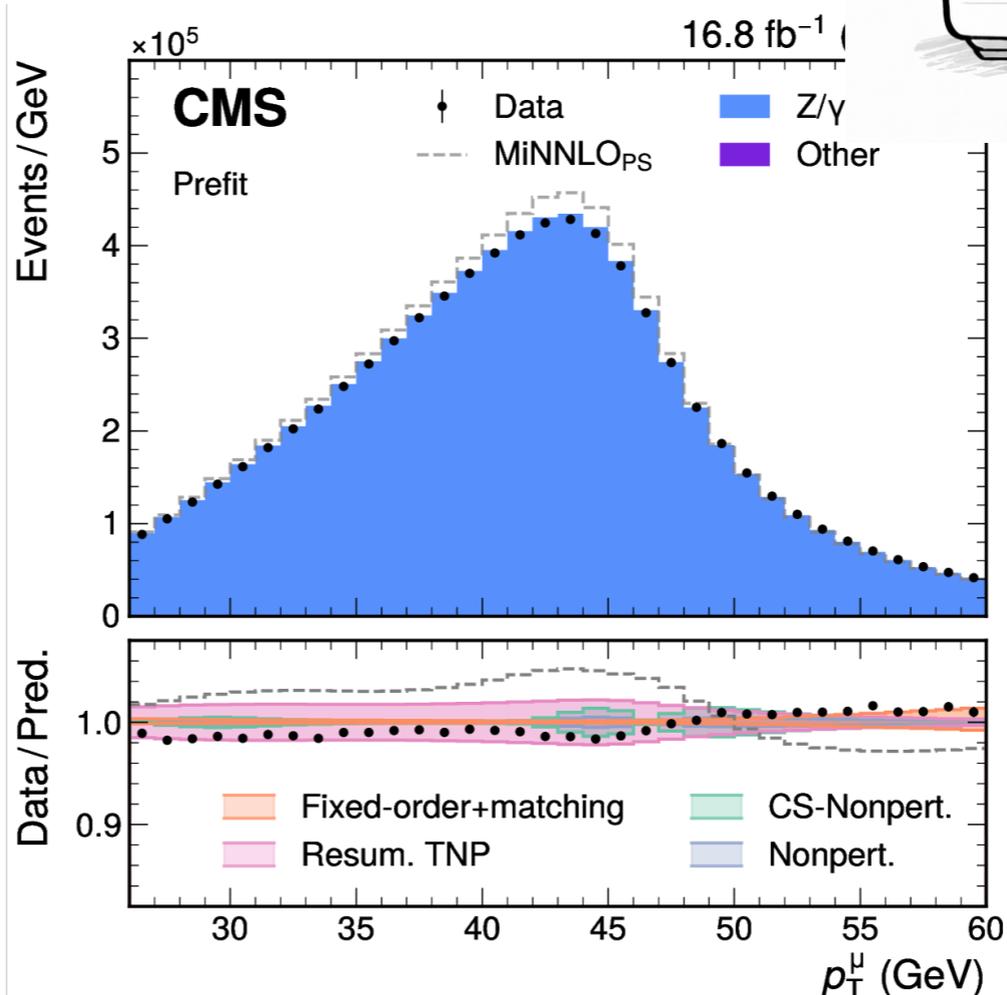
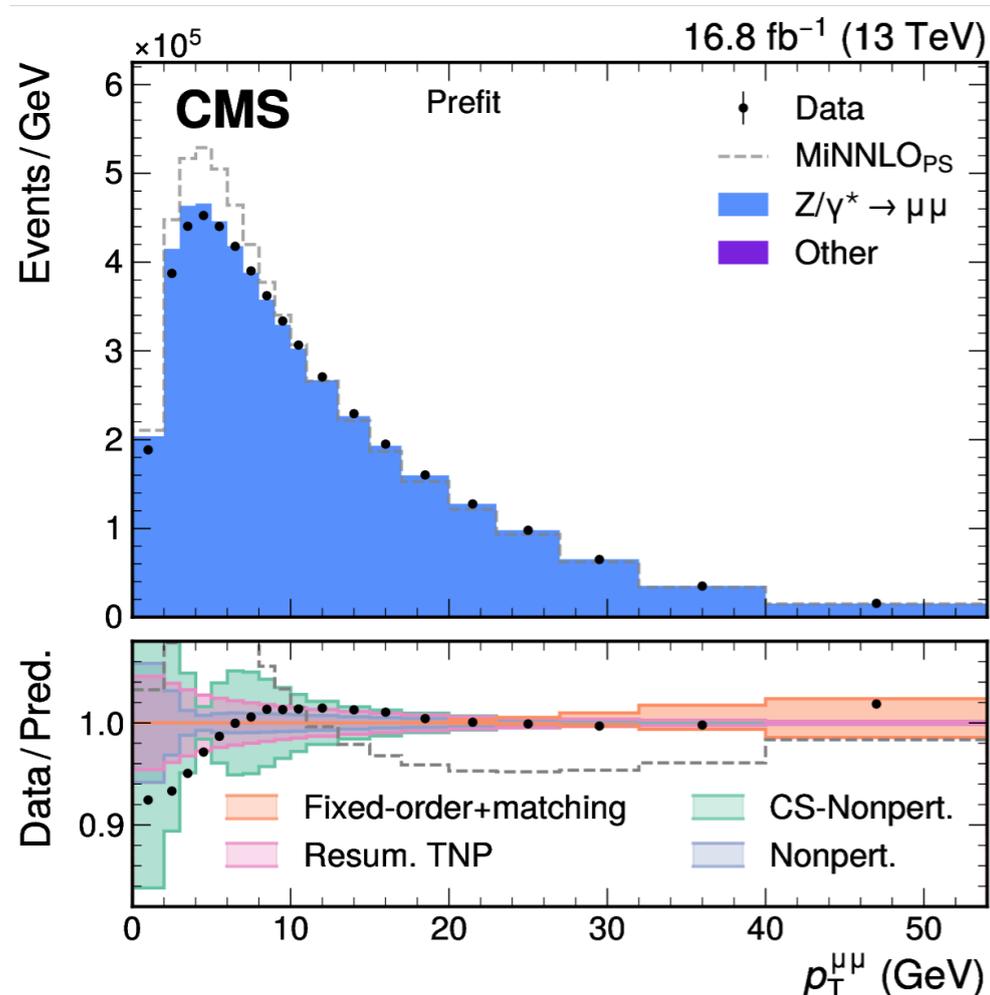
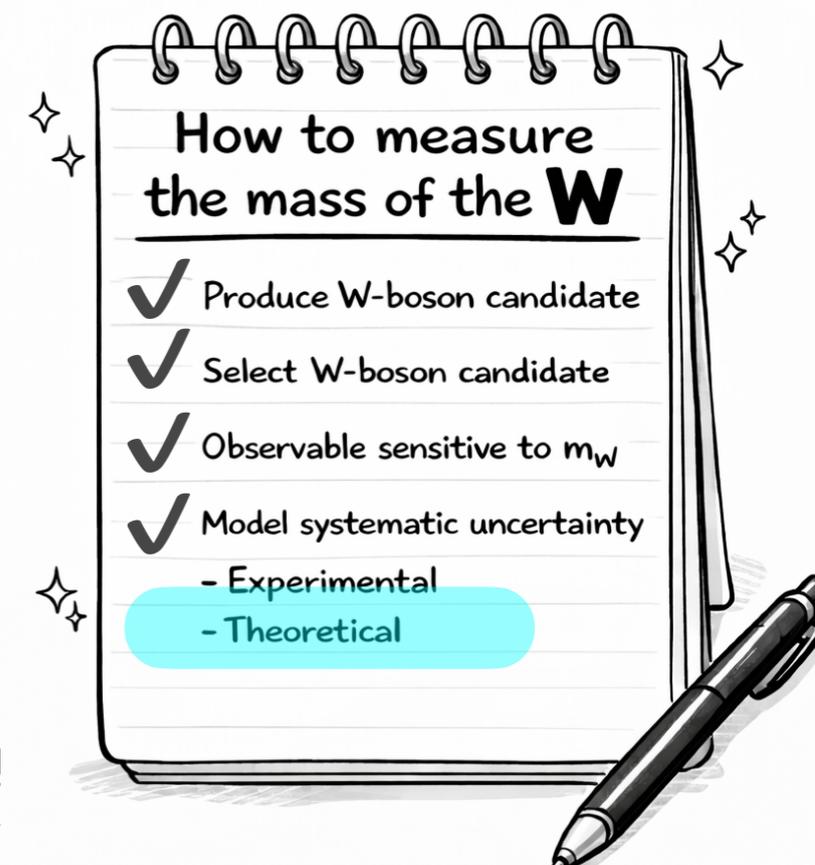


The W physics modelling

CMS strategy

Fully simulated MC samples with MiNNLO_{PS}+Pythia8 $O(\alpha_s^2)$ accuracy

- ▶ p_T^W not directly measured but same procedure applied on W →
Validate with Z boson measurements

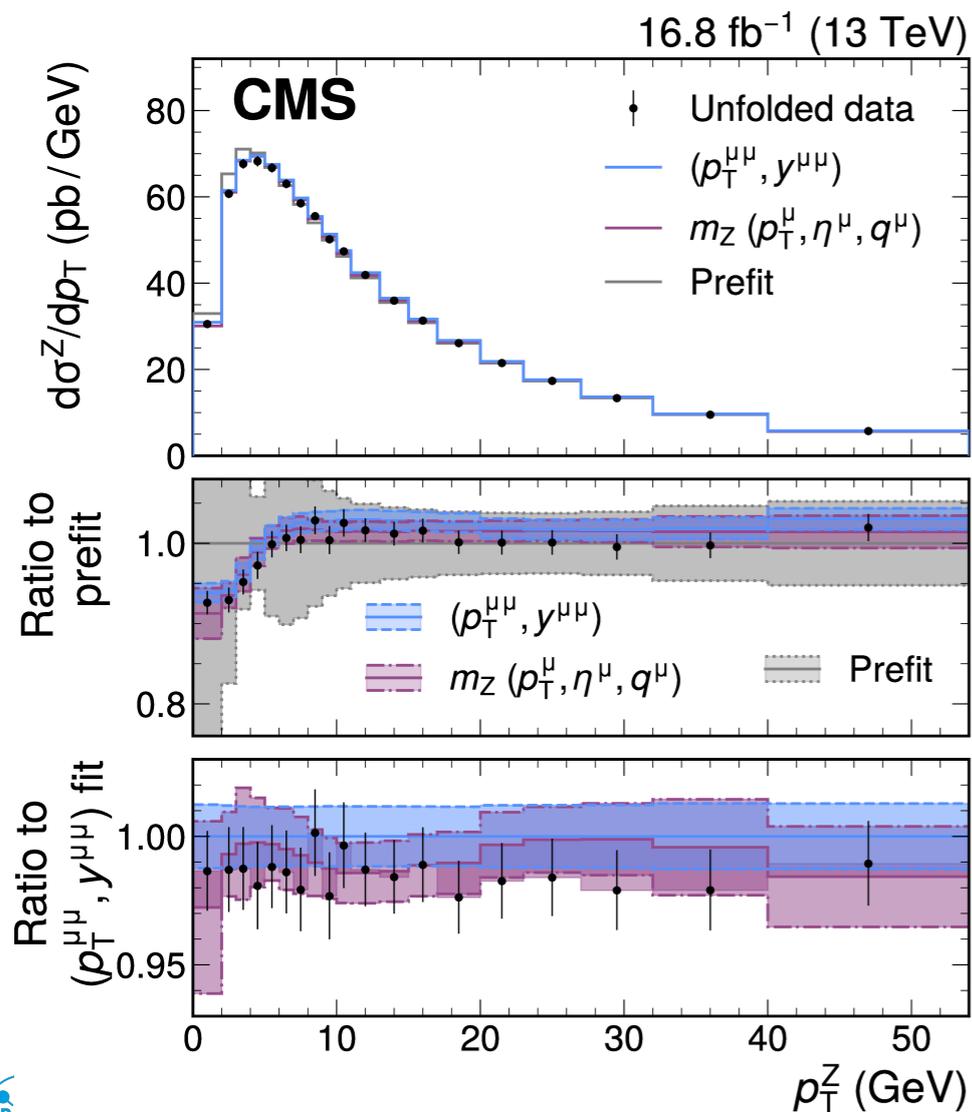
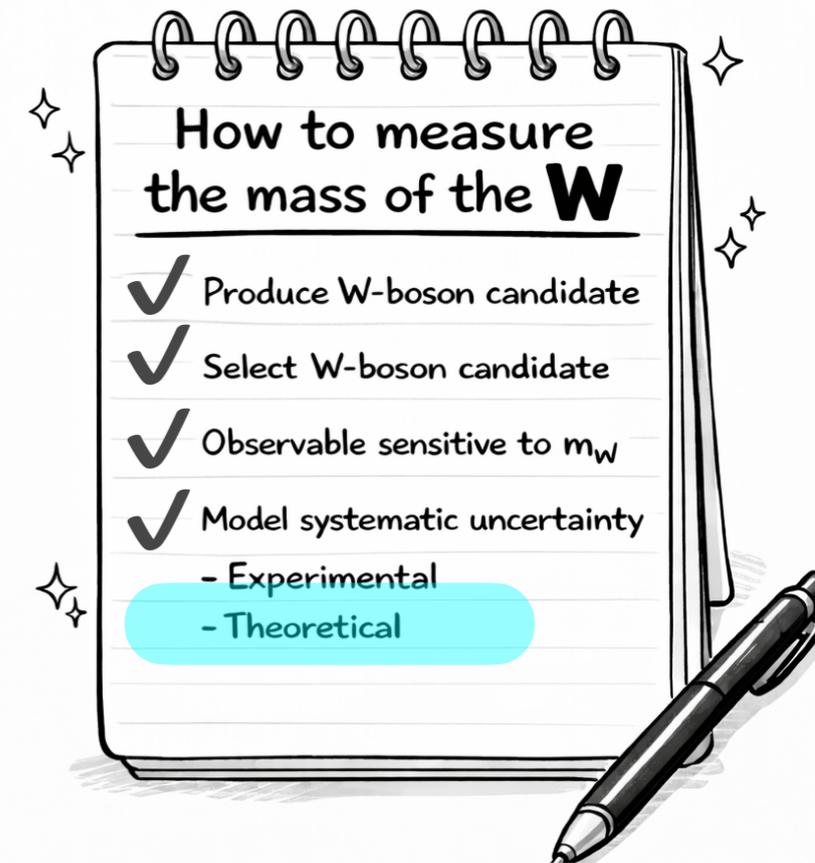


The W physics modelling

CMS strategy

Fully simulated MC samples with MiNNLOPS+Pythia8 $O(\alpha_s^2)$ accuracy

- p_T^W not directly measured but same procedure applied on W → **Validate with Z boson measurements**

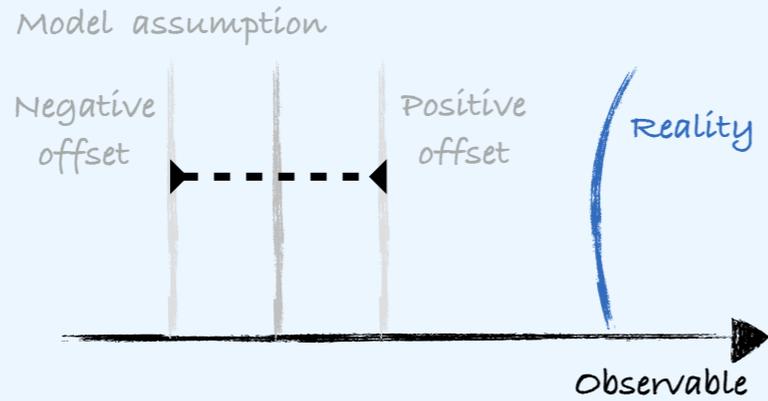


Rely on theory [SCETLIB prediction matched to fixed order DYTurbo prediction (N3LL + NNLO)] and on the *constraining power of the very high statistic of the data samples*

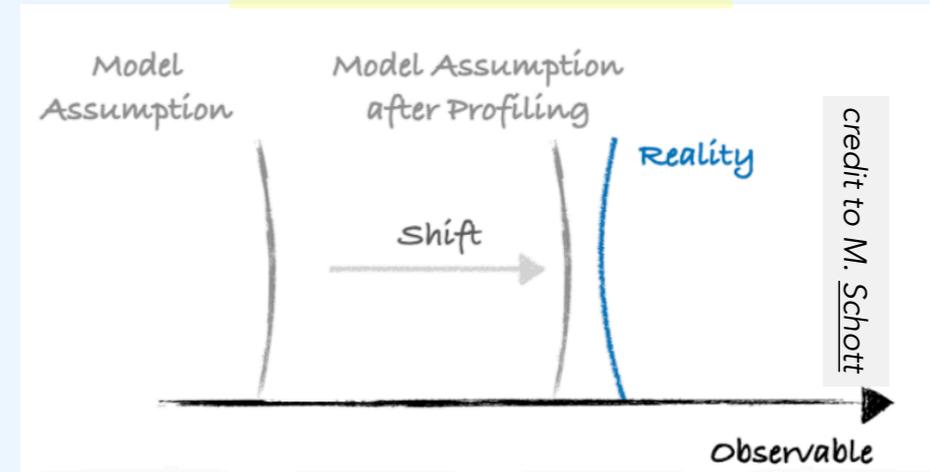
A quantitative example



χ^2 offset fit

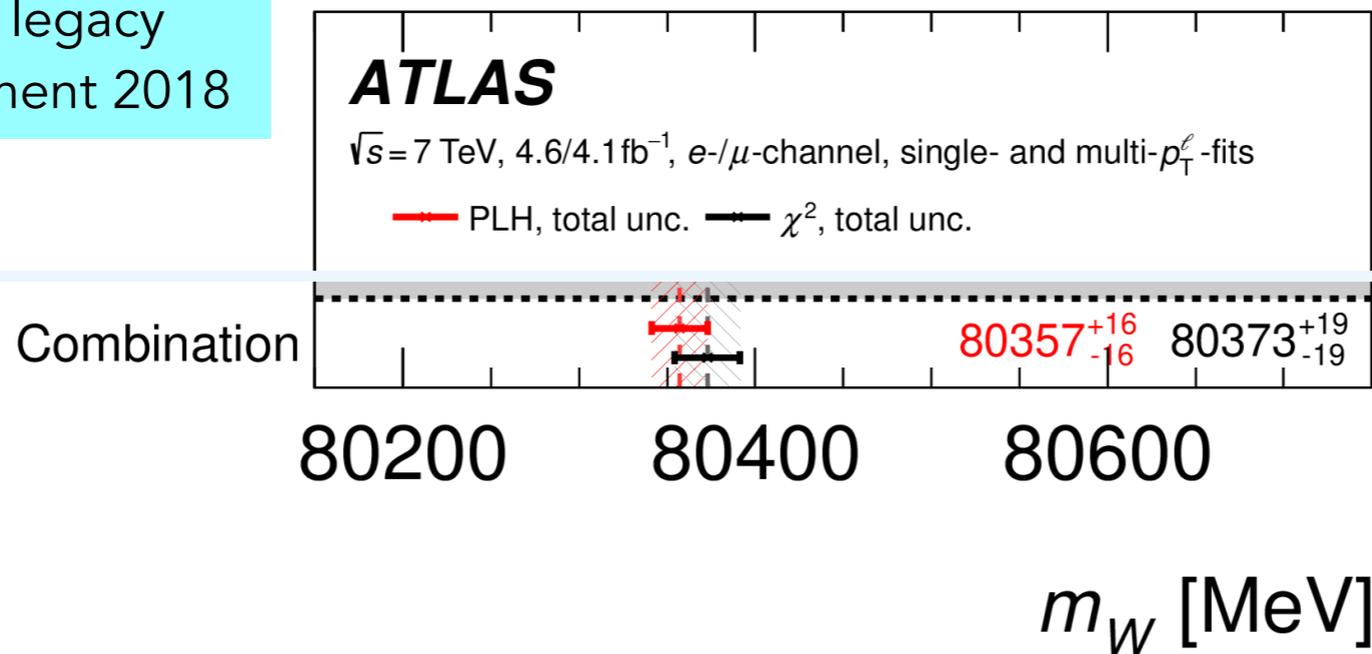


Profiled Likelihood fit



ATLAS legacy measurement 2018

ATLAS improved measurement 2024

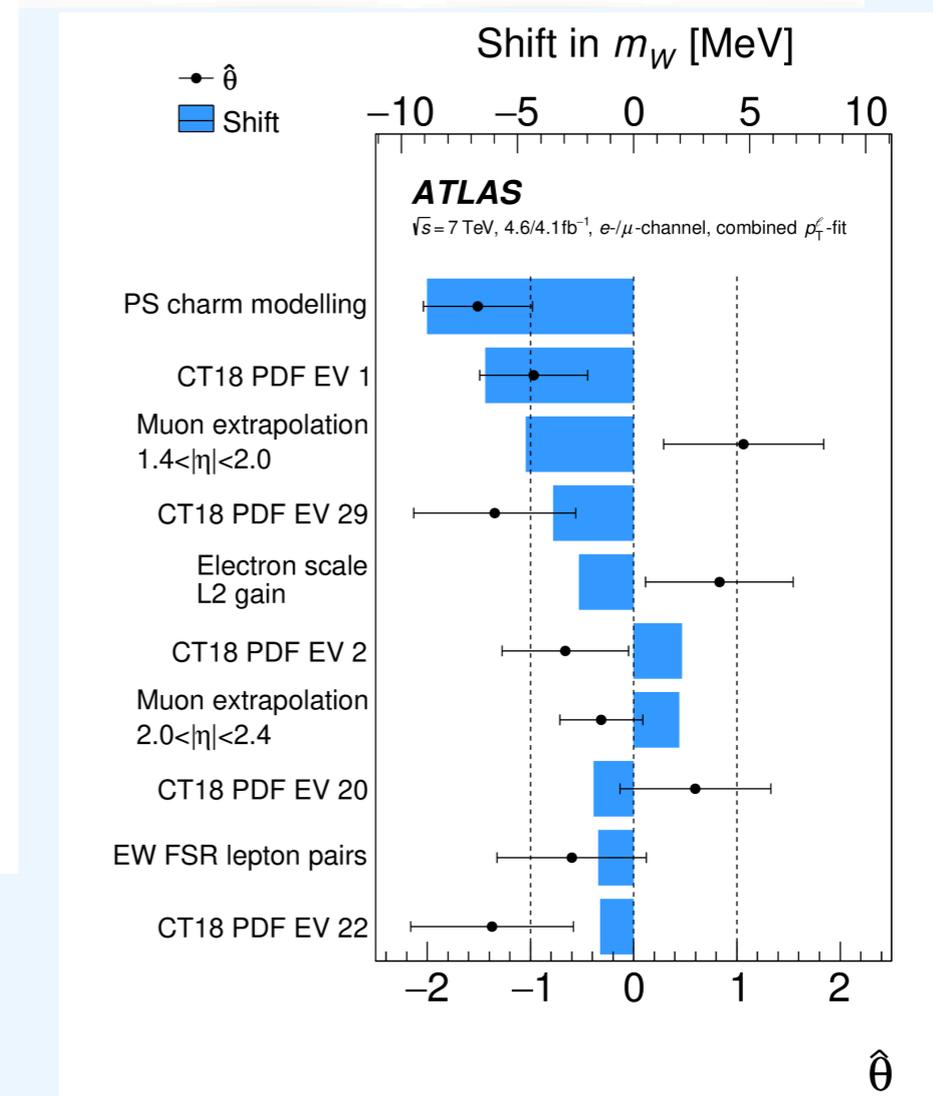
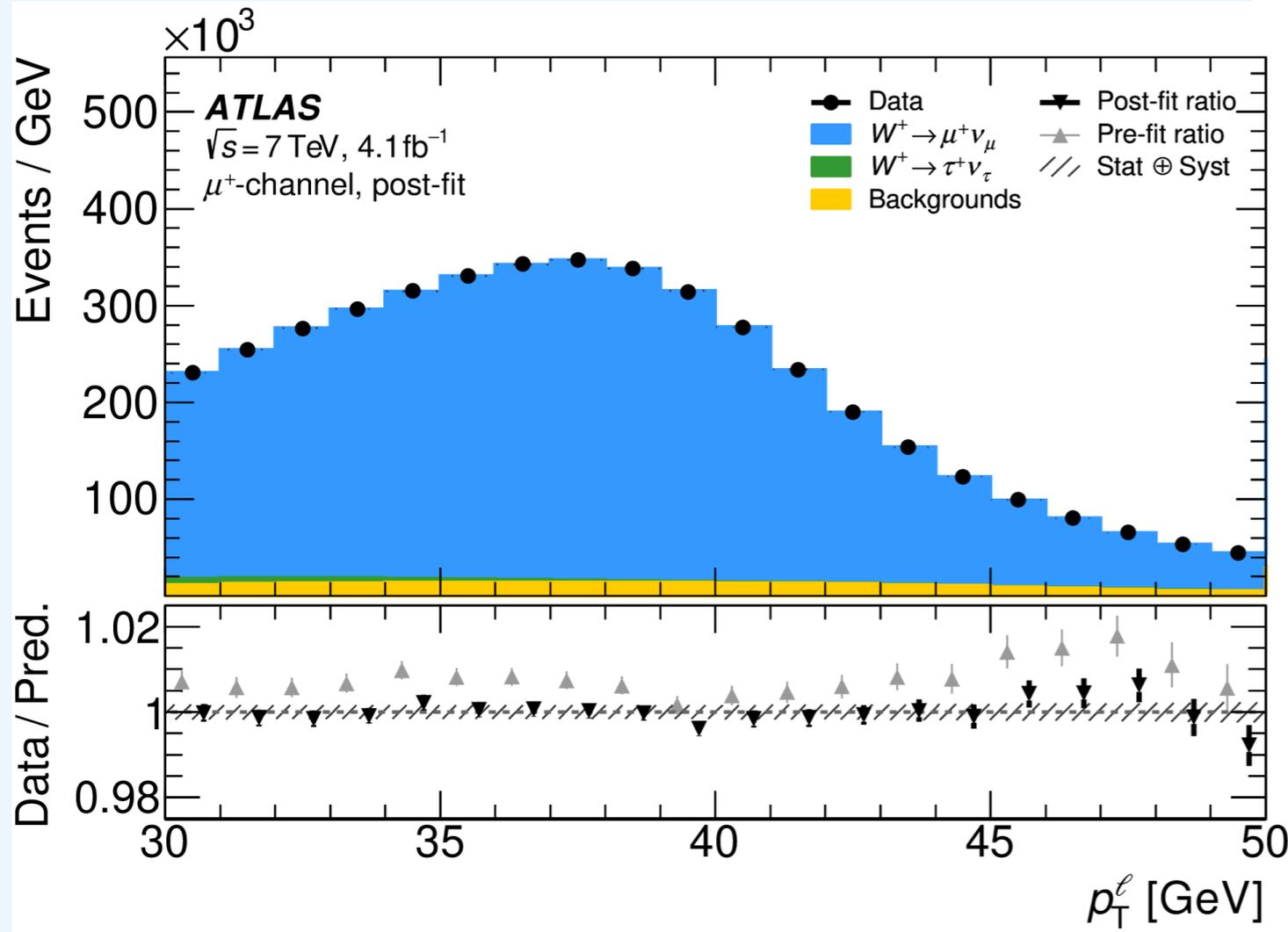
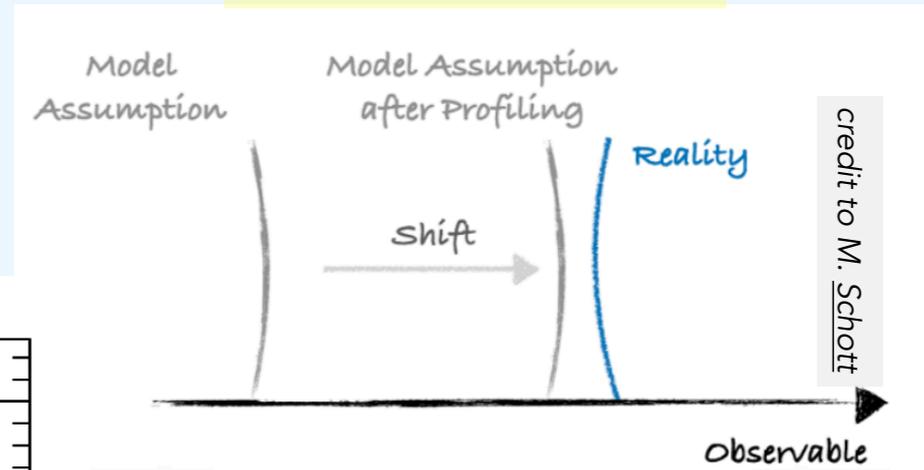


PLH allows simultaneous determination of POI together with NP taking account correlation in each category
 expected allowed shift $m_W \pm 16$ (± 23) MeV for p_T^l (m_T)

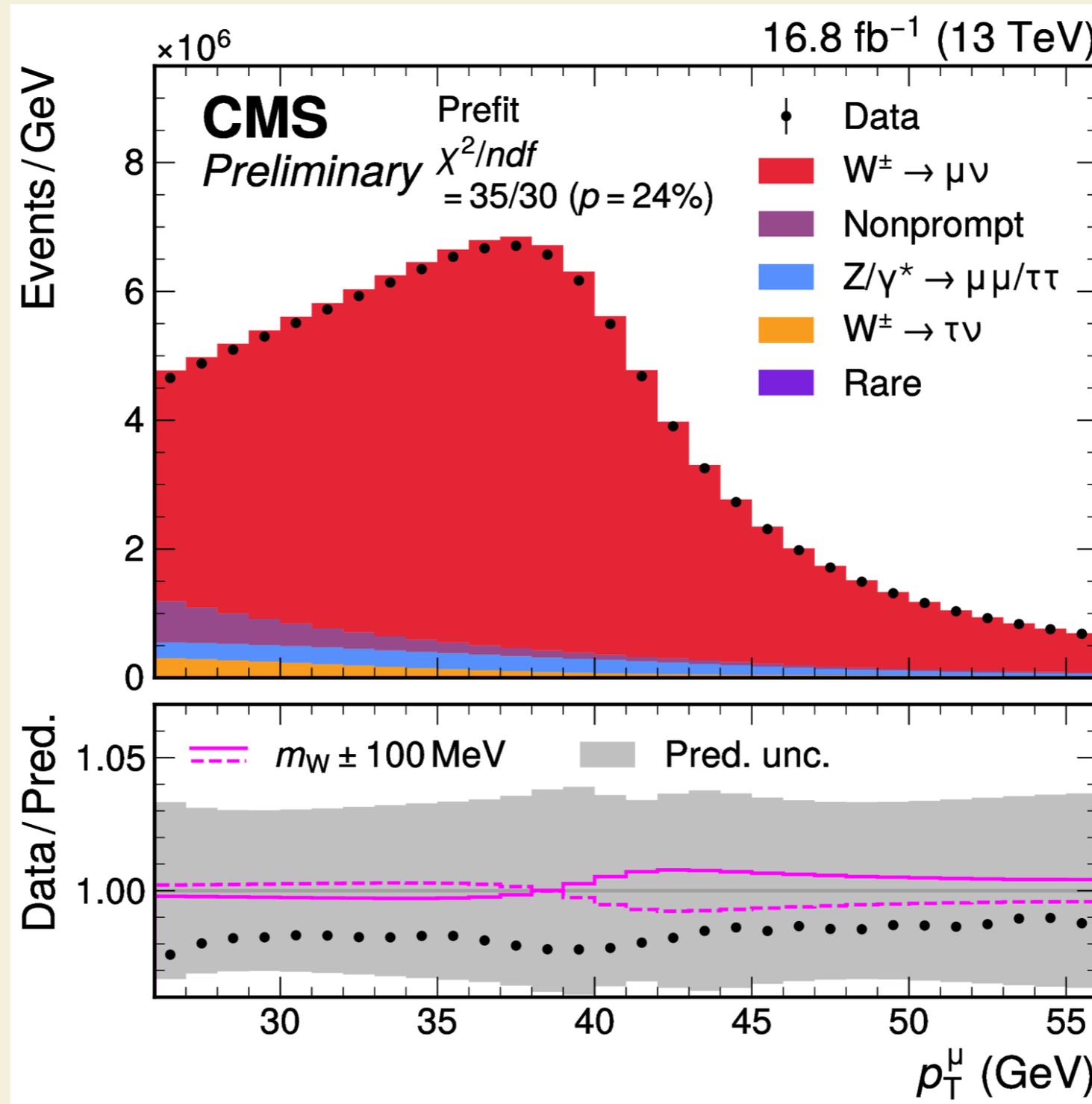
A quantitative example



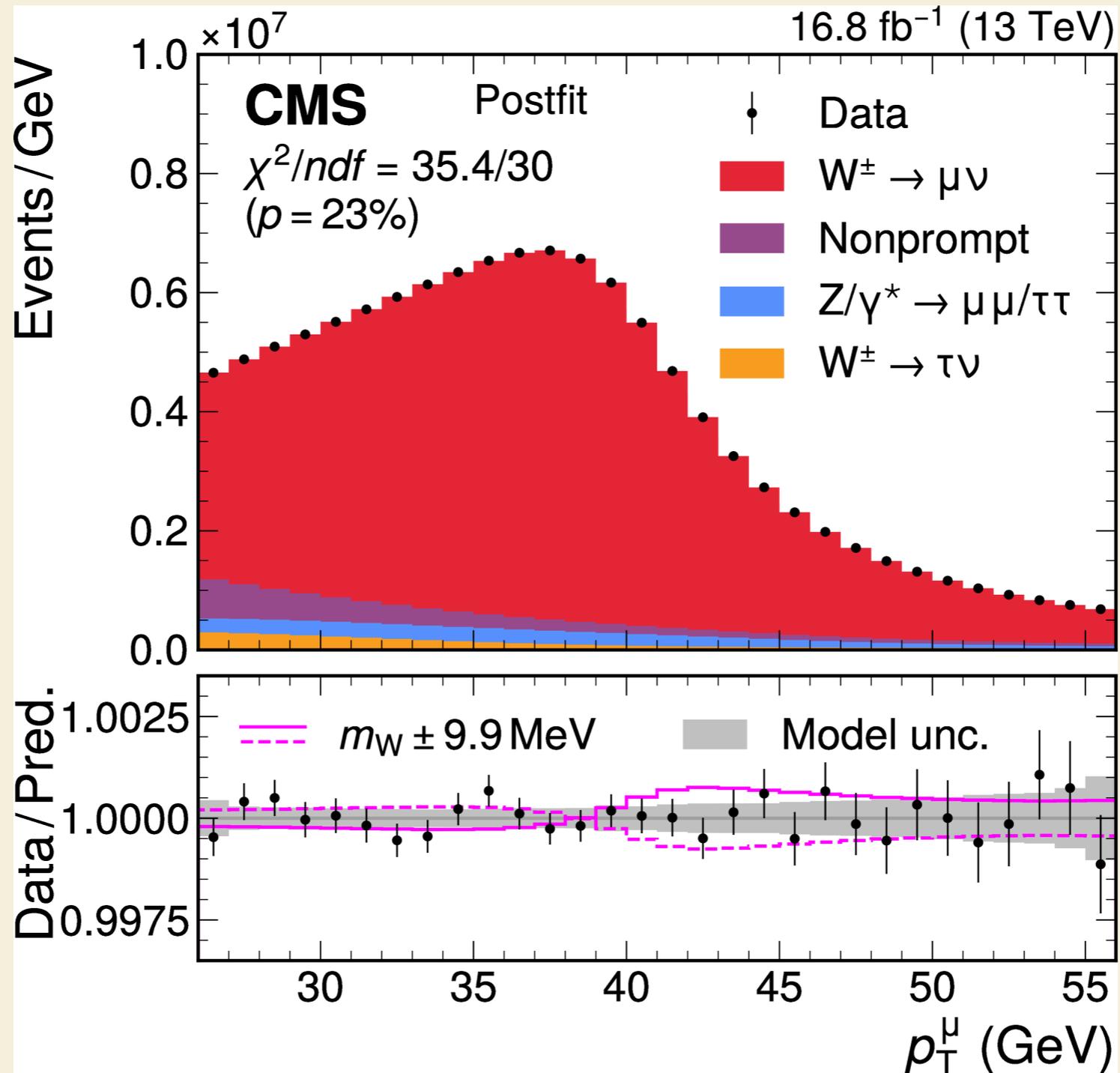
Profiled Likelihood fit



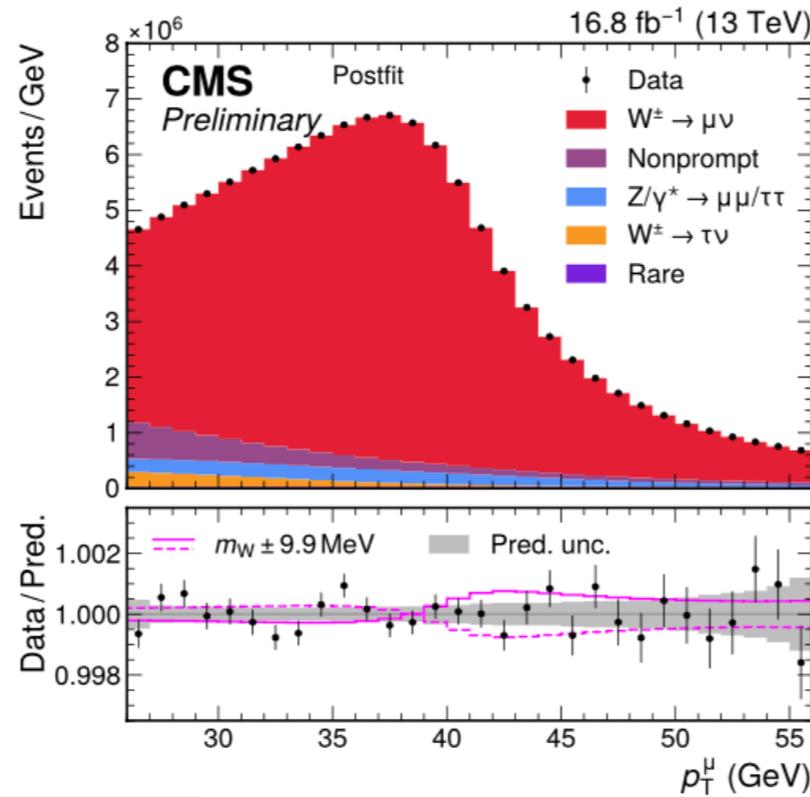
A quantitative example



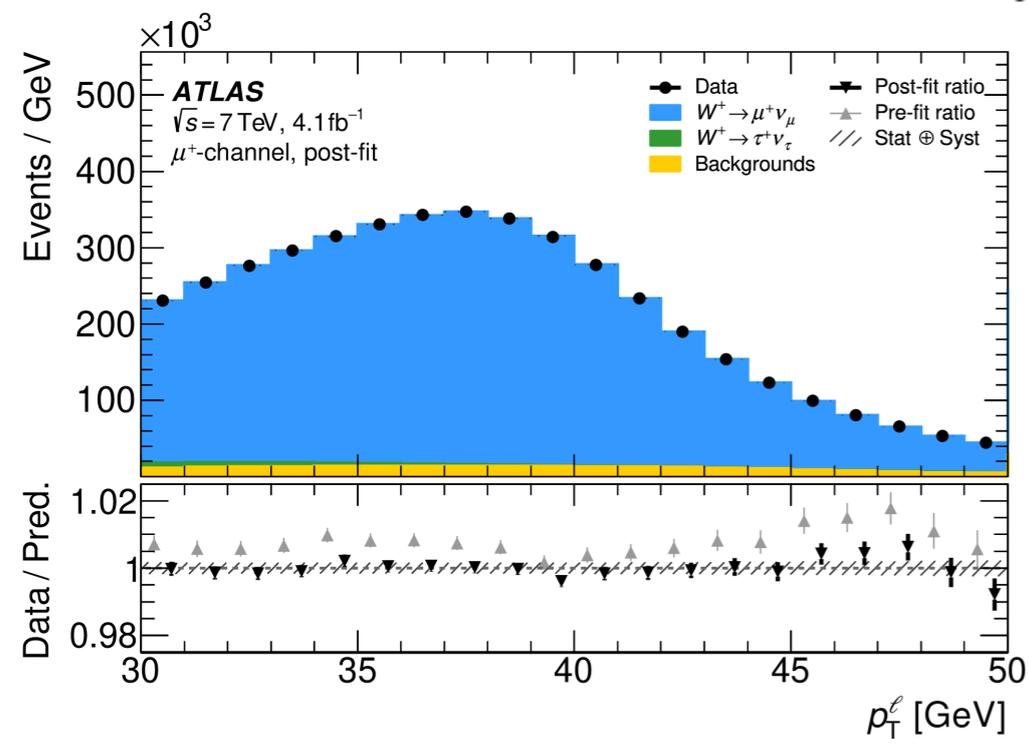
A quantitative example



Uncertainty decomposition



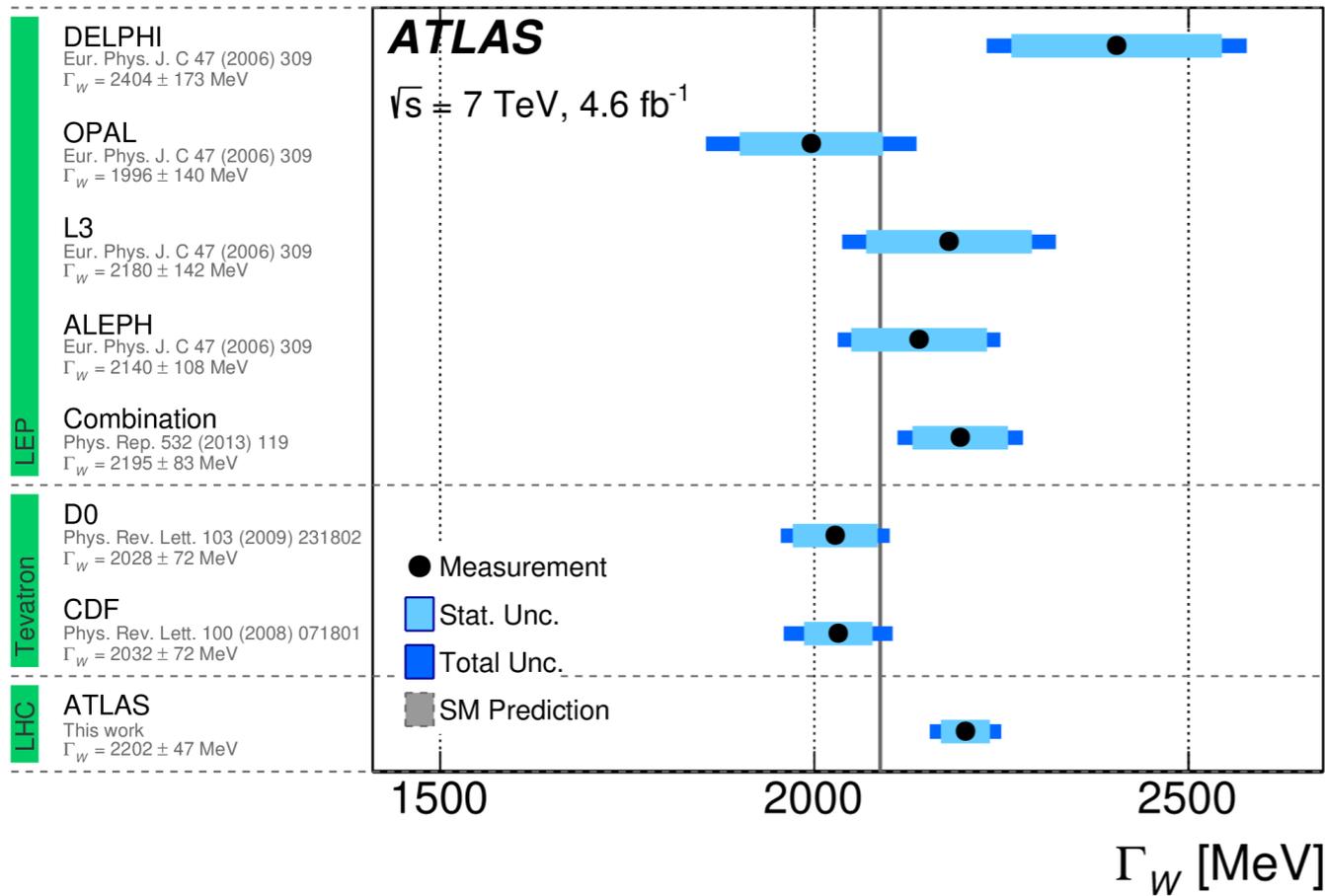
| Source of uncertainty | Impact (MeV) | |
|--------------------------|--------------|------------|
| | Nominal | Global |
| Muon momentum scale | 4.8 | 4.4 |
| Muon reco. efficiency | 3.0 | 2.3 |
| W and Z angular coeffs. | 3.3 | 3.0 |
| Higher-order EW | 2.0 | 1.9 |
| p_T^V modeling | 2.0 | 0.8 |
| PDF | 4.4 | 2.8 |
| Nonprompt background | 3.2 | 1.7 |
| Integrated luminosity | 0.1 | 0.1 |
| MC sample size | 1.5 | 3.8 |
| Data sample size | 2.4 | 6.0 |
| Total uncertainty | 9.9 | 9.9 |



| | [MeV] | Total | Stat. | Syst. | PDF | A_i | Backg. | EW | e | μ | u_T | Lumi | Γ_W | PS |
|----------|-------|-------|-------|-------|------|-------|--------|-----|-----|-------|-------|------|------------|-----|
| p_T^l | | 16.2 | 11.1 | 11.8 | 4.9 | 3.5 | 1.7 | 5.6 | 5.9 | 5.4 | 0.9 | 1.1 | 0.1 | 1.5 |
| m_T | | 24.4 | 11.4 | 21.6 | 11.7 | 4.7 | 4.1 | 4.9 | 6.7 | 6.0 | 11.4 | 2.5 | 0.2 | 7.0 |
| Combined | | 15.9 | 9.8 | 12.5 | 5.7 | 3.7 | 2.0 | 5.4 | 6.0 | 5.4 | 2.3 | 1.3 | 0.1 | 2.3 |

Bonus: W width measurement

Overview of Γ_W measurements



$$\Gamma_W = 2202 \pm 47 \text{ MeV}$$

First LHC measurement of W width also the most precise one!
 m_T observable has best sensitivity to width Γ_W
 Mass of the W treated as NP
 $m_W^{\text{SM}} = 80355 \pm 6 \text{ MeV}$
 the measurement agrees with the SM expectation of $\Gamma_W^{\text{SM}} = 2088 \pm 1 \text{ MeV}$ within 2.4σ

| Unc. [MeV] | Total | Stat. | Syst. | PDF | A_i | Backg. | EW | e | μ | u_T | Lumi | m_W | PS |
|------------|-------|-------|-------|-----|-------|--------|----|-----|-------|-------|------|-------|----|
| p_T^ℓ | 72 | 27 | 66 | 21 | 14 | 10 | 5 | 13 | 12 | 12 | 10 | 6 | 55 |
| m_T | 48 | 36 | 32 | 5 | 7 | 10 | 3 | 13 | 9 | 18 | 9 | 6 | 12 |
| Combined | 47 | 32 | 34 | 7 | 8 | 9 | 3 | 13 | 9 | 17 | 9 | 6 | 18 |

Bonus: The Z mass



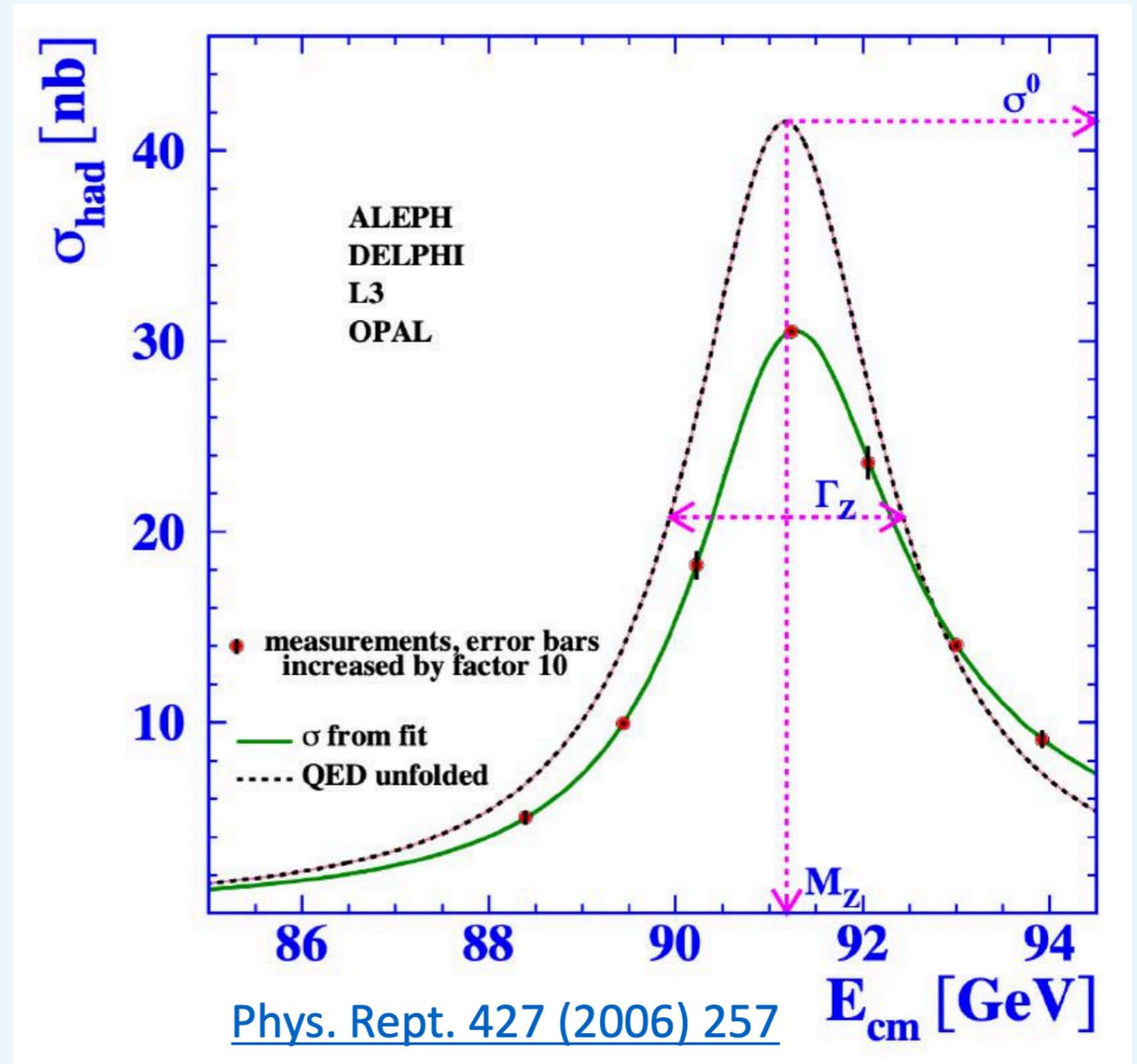
Large Electron Positron collider LEP (1989 – 2000 @ CERN)

- e^+e^- collider, tuned to Z resonance ~ 17 million Z bosons
 - Access via energy scan

The LEP legacy

$$m_Z = 91187.6 \pm 2.1 \text{ MeV}$$

- uncertainty dominated by Beam-energy calibration.



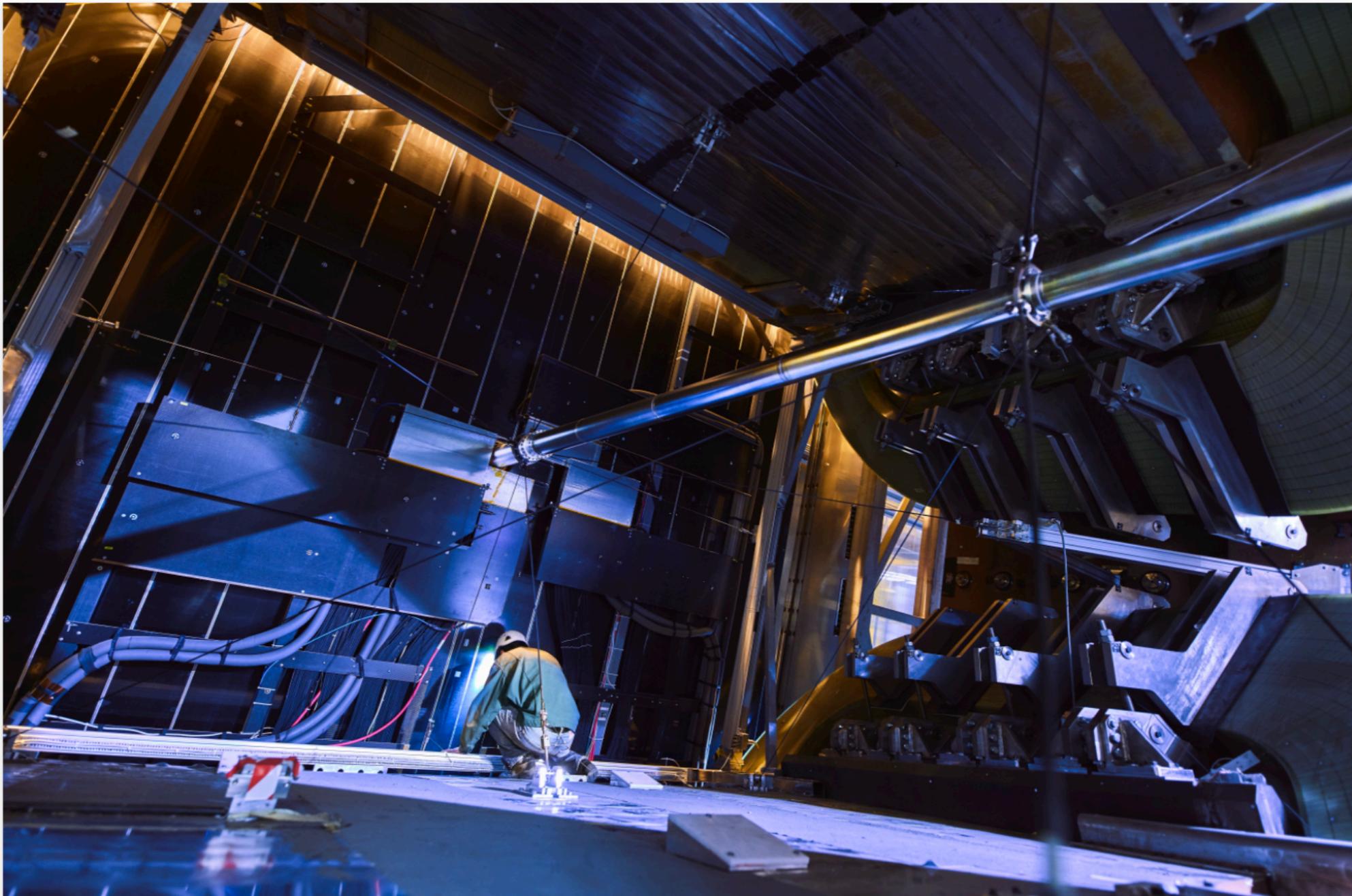
Reminder Indirect measurement $m_Z = 91201.7 \pm 8.9 \text{ MeV}$ [Phys. Rev D. 106.033003]

LHCb weighs up the Z

New measurement of the mass of the Z boson showcases the Large Hadron Collider's growing role in precision physics

6 JUNE, 2025 | By [Ana Lopes](#)

Recent [LHCb measurements](#) (2025)

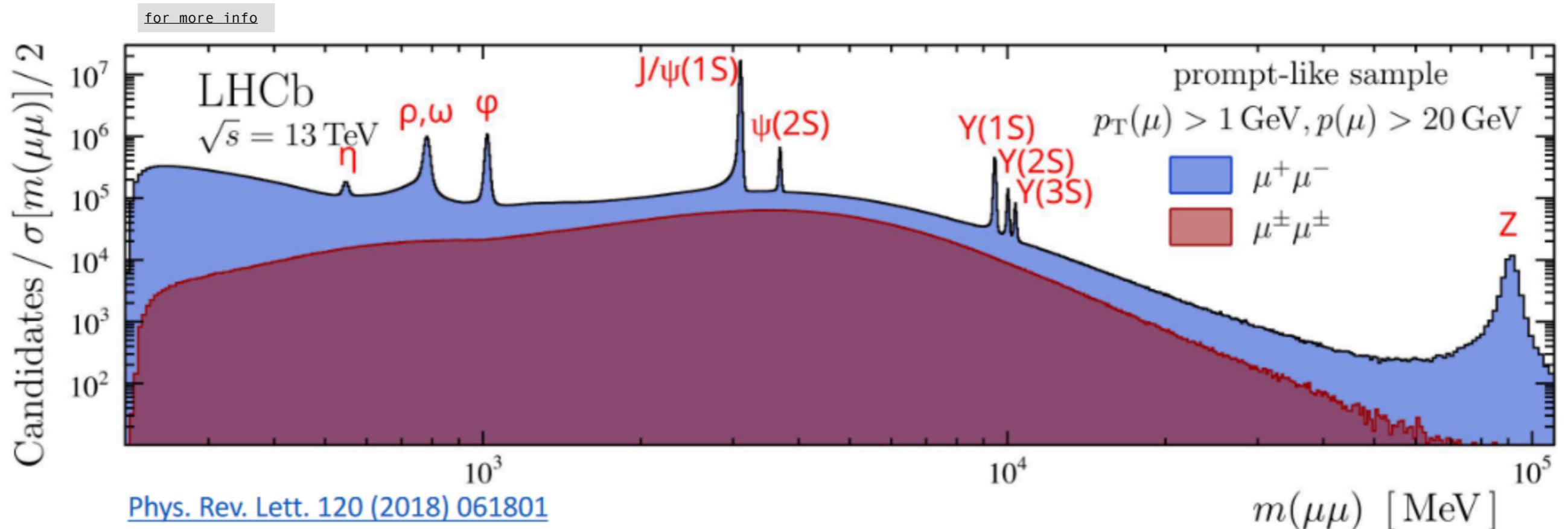


The LHCb detector in 2018. (Image: CERN)

Di-muon mass spectrum

- ▶ At Hadron collider the mass of the Z is extracted from final state kinematics.
- ▶ The di-muon mass spectrum become the key observable

| @13TeV 1.7 fb ⁻¹ | LHCb Candidates |
|---------------------------------------|-------------------|
| $\Upsilon(1S) \rightarrow \mu^+\mu^-$ | 190×10^3 |
| $J/\psi \rightarrow \mu^+\mu^-$ | 48×10^3 |
| $Z \rightarrow \mu^+\mu^-$ | 170×10^3 |

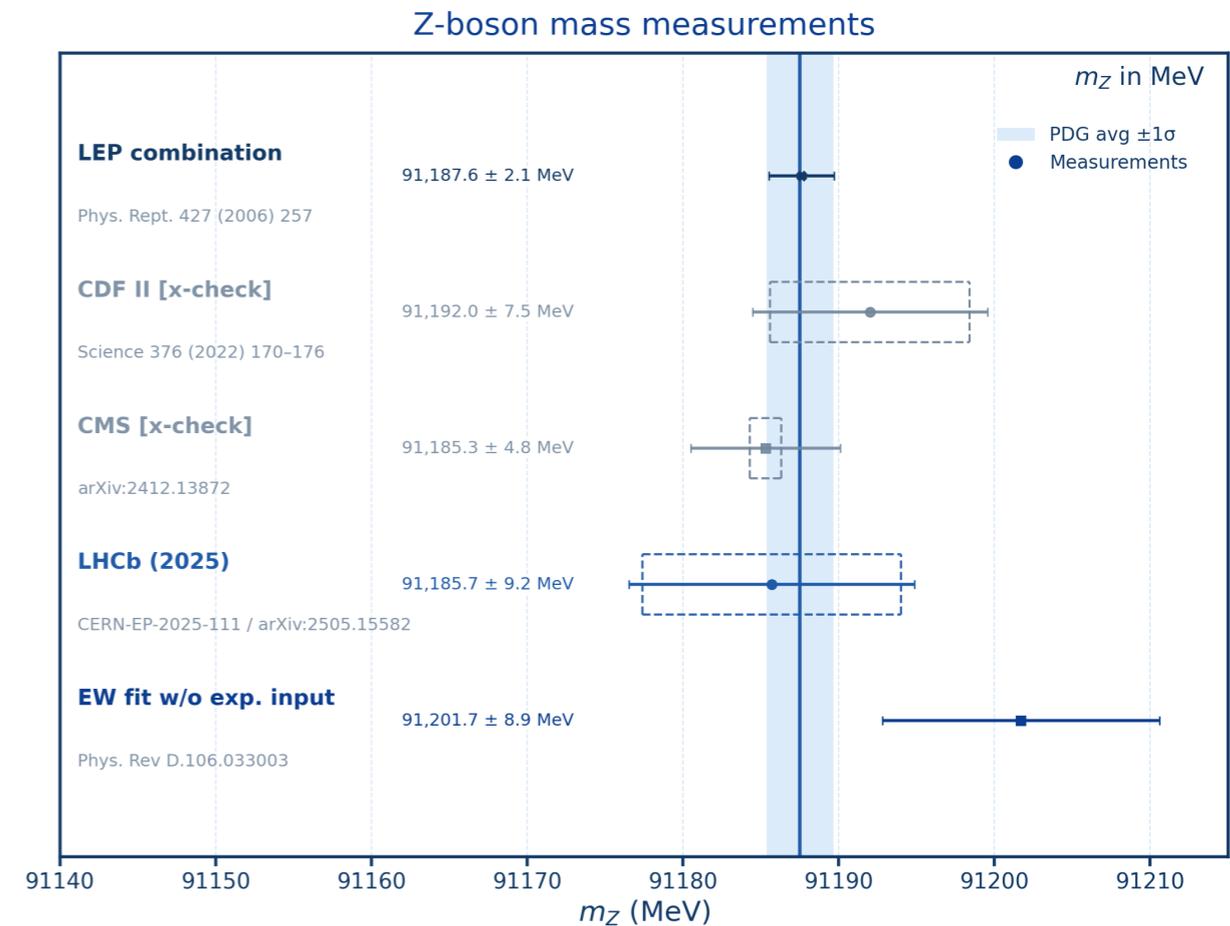
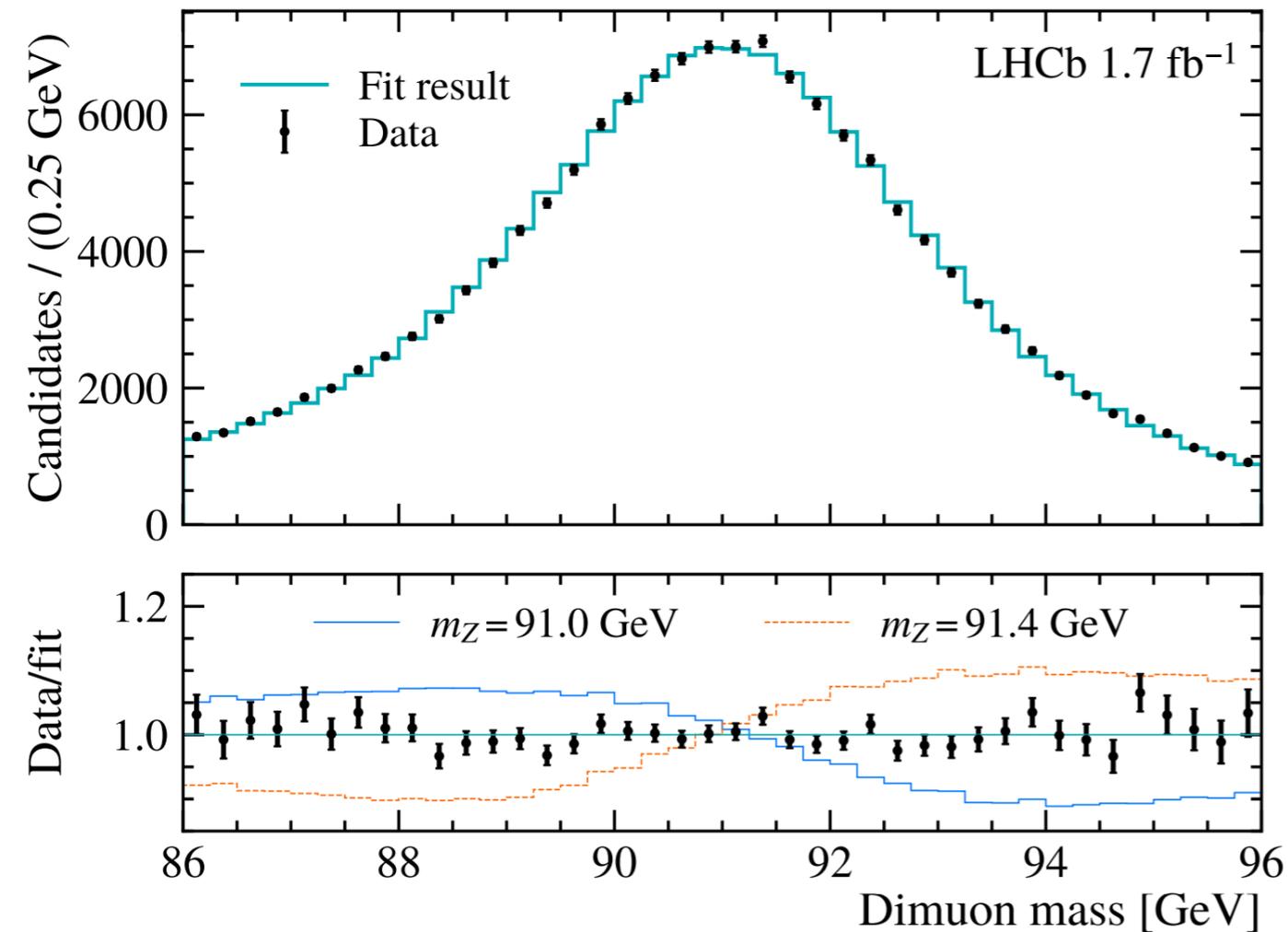


Standard muon momentum calibration for LHCb achieves a relative uncertainty of 3×10^{-4}

For the Z mass analysis muon momentum calibration uncertainty reached 4×10^{-5} (dominated by the detector material description in the simulation) $\Rightarrow \delta m_Z = 3.6 \text{ MeV}$

LHCb m_Z measurement

Rev. Lett. 135 (2025) 161802



The resulting measurement of the Z-boson mass is $m_Z = 91185.7 \pm 8.3$ (stat) ± 3.9 (sys) MeV

... to summarise

➔ **The m_W measurement is the culmination of an extensive precision physics program**

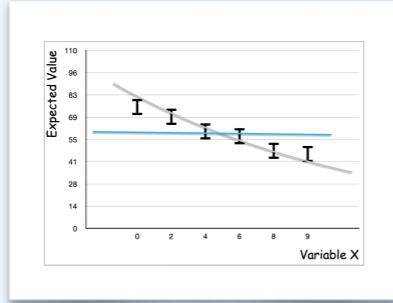
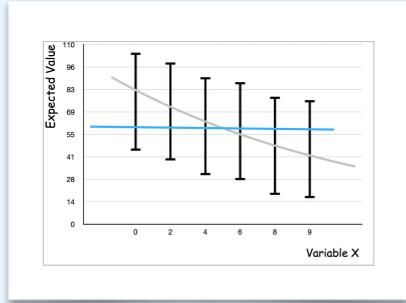
- ▶ LHC experiments are reaching unprecedented precisions on the measurement of fundamental parameter of the SM
- ▶ Individual experiments now approach — or even surpass — the precision of the combined LEP, SLD, and Tevatron electroweak results.

What Makes It Possible ?

- ▶ Incredible understanding of detector response across energies and pileup conditions.
- ▶ The measurement relies on extremely complex, multi-differential analyses.
 - ▶ almost ∞ data statistic is used to test and constrain state of the art prediction:
 - ▶ PDF uncertainties
 - ▶ p_T^W modelling

Backup

Precision Experiments: Revealing New Frontiers



★ Ruling Out Theories

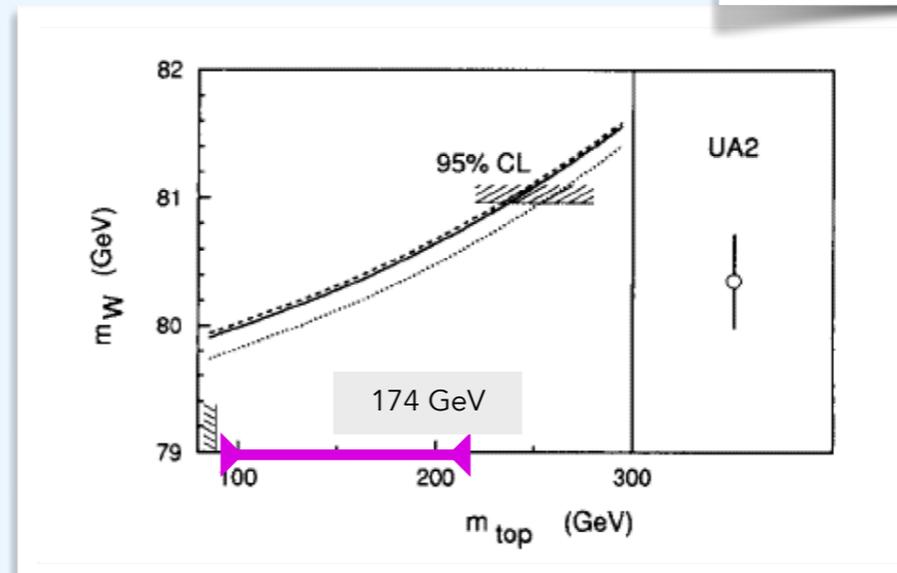
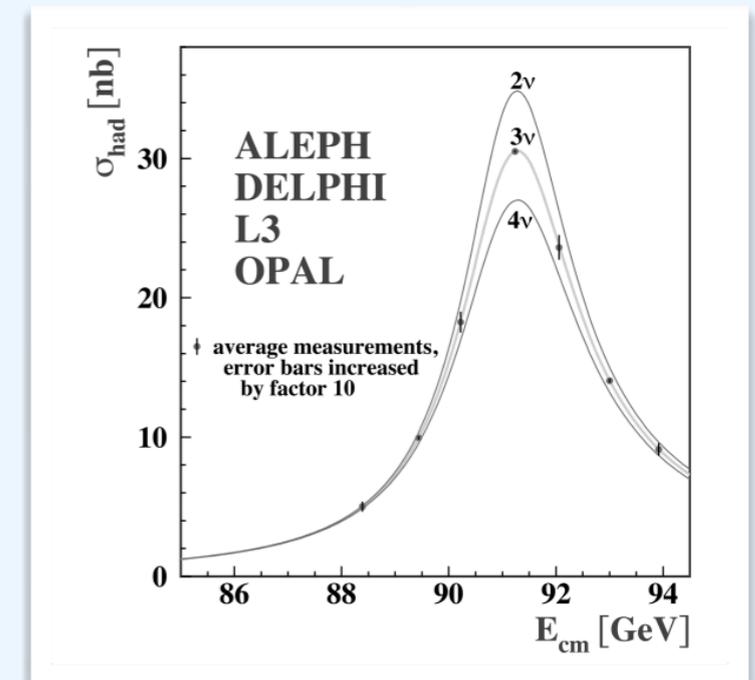
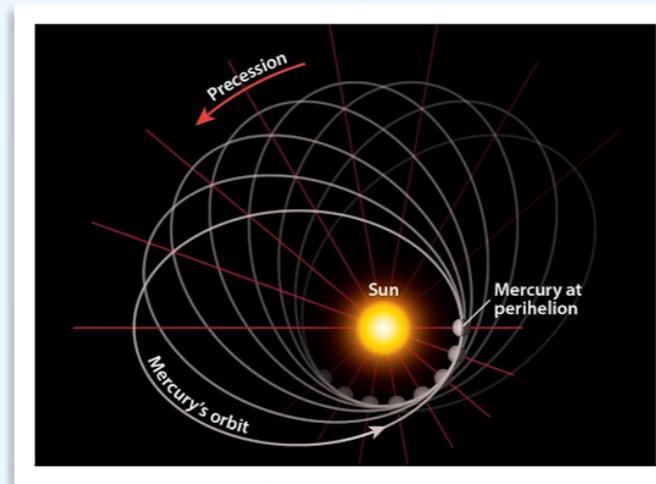
(1860') Mercury's precession measured at 1.56° per century—Newtonian physics explained most of it but missed 0.01194° . This gap led to the triumph of **General Relativity!**

★ Confirming Theories

Precision measurements of the (1990') confirmed the existence of **3 families of neutrinos (3%)**, pushing the boundaries of established facts of the SM.

★ Paving the Way for Discoveries

First precise measurement of the **W boson mass** in the 1990s paved the way for the discovery of the **top quark**.



LHC experimental data

Now — after an outstanding Run 2 — the LHC experiments have in their hands the richest hadron collision data sample ever recorded

| Particle | Produced in 140 fb^{-1} pp at $\sqrt{s} = 13 \text{ TeV}$ |
|--------------|---------------------------------------------------------------------|
| Higgs boson | 7.8 million |
| Top quark | 275 million (115 million $t\bar{t}$) |
| Z boson | 8 billion ($\rightarrow \ell\ell$, 270 million per flavour) |
| W boson | 26 billion ($\rightarrow \ell\nu$, 2.8 billion per flavour) |
| Bottom quark | ~ 160 trillion (significantly reduced by acceptance) |

credit to A. Hoecker



The LHC is an **everything** factory

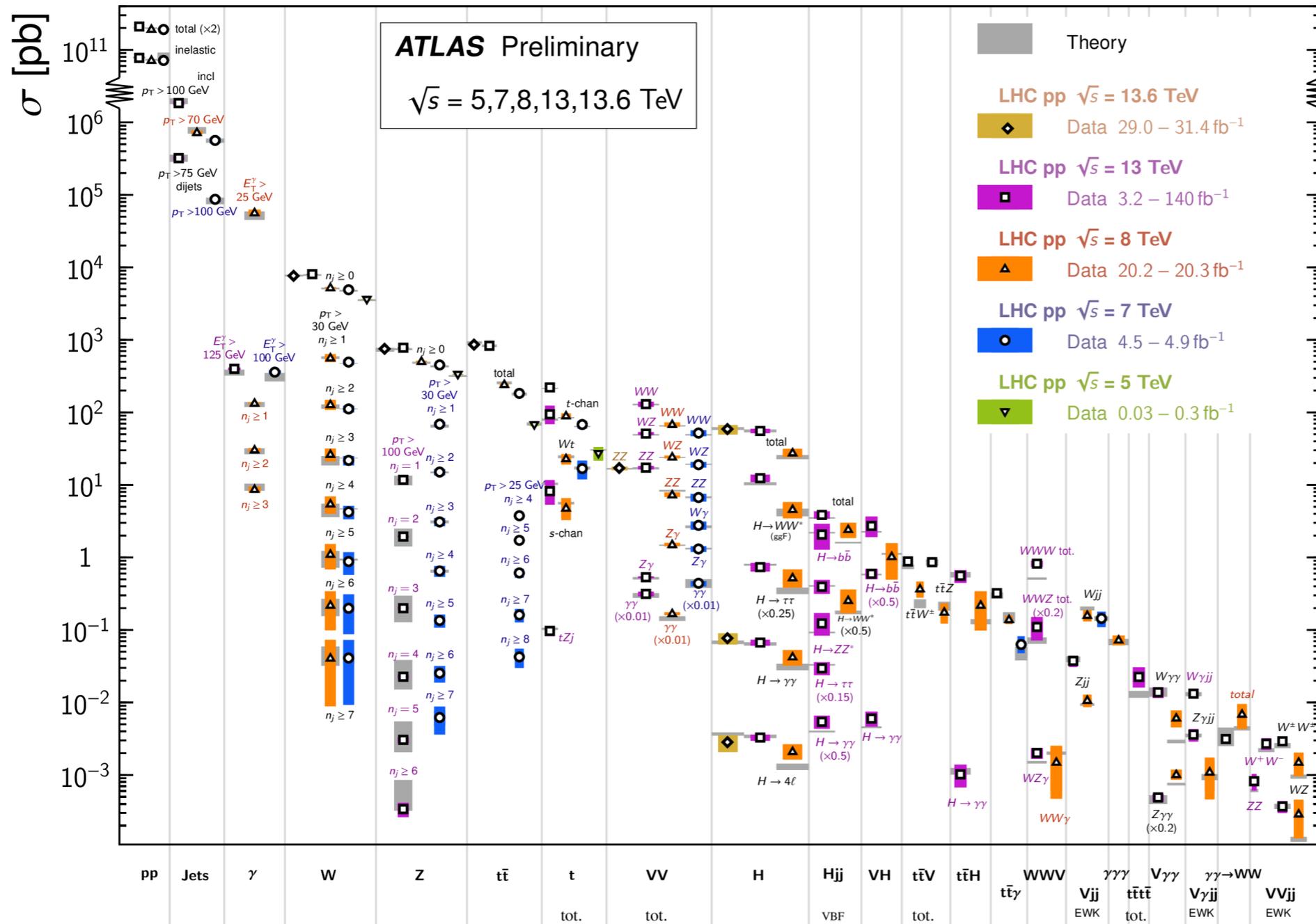
Vast and reach program at High energy frontier.

- ▶ *Probing with high-precision Standard Model processes self consistency of the SM*
- ▶ *detecting very rare processes*
- ▶ *exploring new physics via direct and indirect measurements*

The SM of particle physics @LHC

Status: June 2024

Standard Model Production Cross Section Measurements



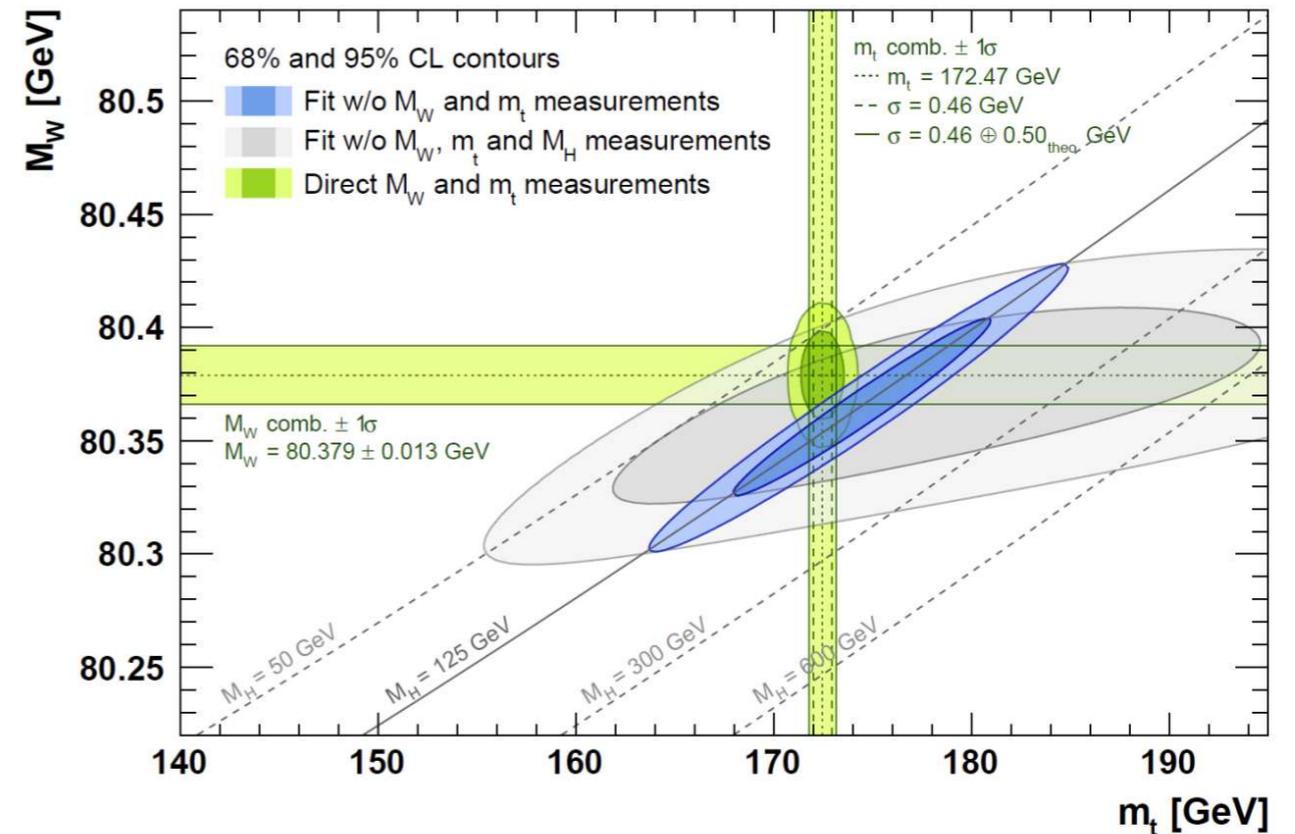
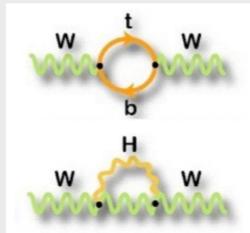
- ▶ Theory so far agrees with all measured cross sections across widely different processes
- ▶ and across centre-of-mass energies ...
- ▶ **Often data precision challenges the theory predictions...**

Can we consider now the LHC a "precision physics" machine ?

The EW sector: m_t , m_W and m_H

$$m_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2) (1 - \Delta r)}$$

In SM, Δr reflects loop corrections and depends on m_t^2 and $\ln(m_H)$

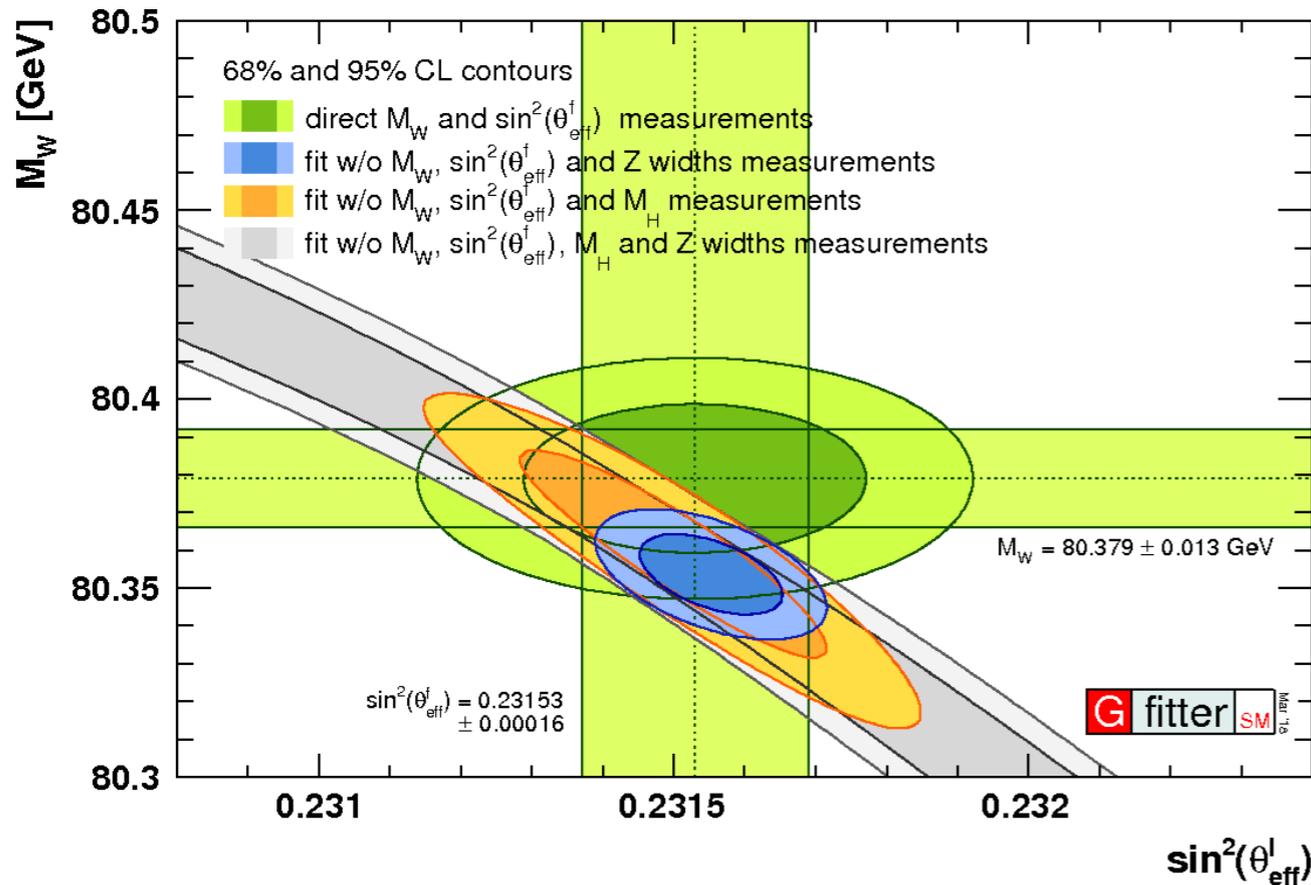


- m_t , m_W , m_H interrelation is the most popular way to test the predictive power of global fits in high-energy physics.
 - Historically, SM relation between fundamental parameters has been used to predict m_t and put constraint on the m_H before they were discovered!

m_t and m_H are now so well-measured ($\delta m_t \sim 0.5/0.4$ GeV; $\delta m_H \sim 0.2$ GeV) that higher precision has minimal impact on the indirect determination of the others, however m_W is more precisely determined by SM fit $\delta^{th} m_W \sim 7$ MeV ...

The custodial symmetry

<https://arxiv.org/pdf/hep-ph/0302058>



TEST OF THE CONSISTENCY OF THE EW SECTOR IN THE SM THROUGH PRECISION MEASUREMENTS OF ITS FUNDAMENTAL PARAMETERS IS ONE OF THE GOAL OF LHC PHYSICS PROGRAM.

- ▶ Indirect determination of both m_W and $\sin^2\theta_W$ more precise than the experimental measurement

$$\rho \equiv \frac{M_W^2}{M_Z^2 \cos^2 \theta} = 1.$$

- The custodial symmetry protects this relation from large radiative corrections. All corrections to the ρ parameter are therefore proportional to terms that break the custodial symmetry (though radiative correction $H, \text{top}_{\text{mass}}$)

$$\rho_0 \equiv \frac{M_W^2}{M_Z^2 \hat{c}_Z^2 \hat{\rho}},$$

PDG, LEP legacy

$$\rho_0 = 1.00031 \pm 0.00019,$$

EW radiative correction

Electroweak parameters

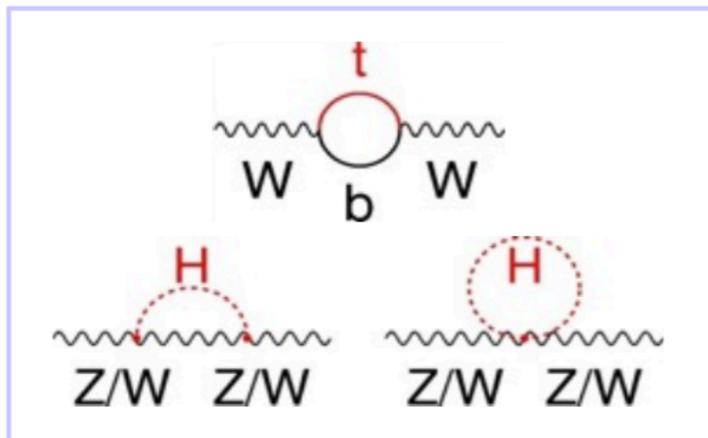
$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} (= 1) \quad s_W^2 \equiv 1 - \frac{m_W^2}{m_Z^2} (= \sin^2 \theta_W)$$

Physical quantities

$$\bar{\rho} = 1 + \Delta\rho$$

$$M_W^2 = m_W^2 (1 + \Delta r) \quad \text{and} \quad \sin^2 \theta_W^{\text{eff}} = s_W^2 (1 + \Delta\kappa)$$

$$\text{with} \quad \Delta r, \Delta\rho, \Delta\kappa = f(m_t^2, \ln(m_H), \dots)$$



$$\Delta\rho_t \simeq 0.01 \times [m_t / (175 \text{ GeV})]^2$$

$$\Delta\rho_H \simeq -0.0015 \times \log(m_H / M_W)$$

the electroweak radiative correction parameters are of the order of the percent and involve contributions from top quark and Higgs boson loops

The electroweak theory predicts relations between experimentally measurable quantities

Observables can be calculated in the SM in term of a **finite number of parameters** to be determined experimentally (**coupling constants**, **masses** of fermions, **CKM** and **M_H**)

Update of the Global EW Fit (2026)



- Update of the Global Electroweak Fit with Gfitter

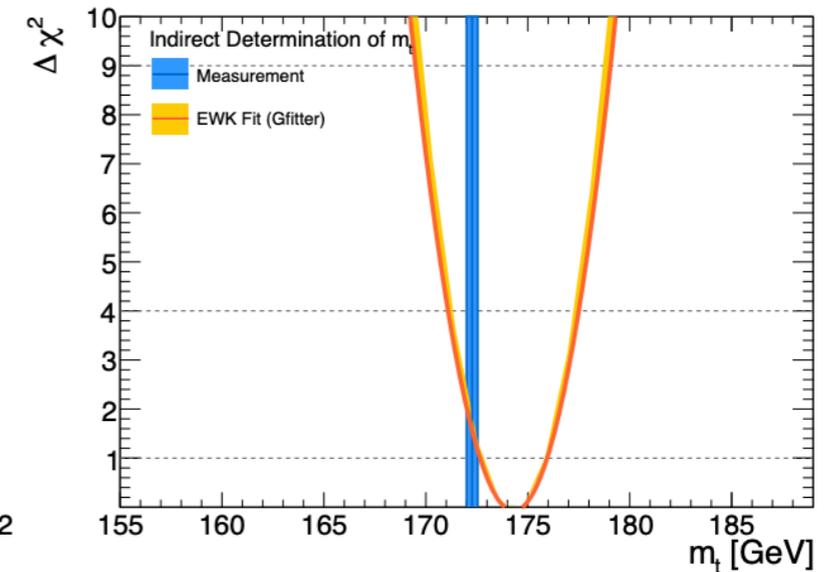
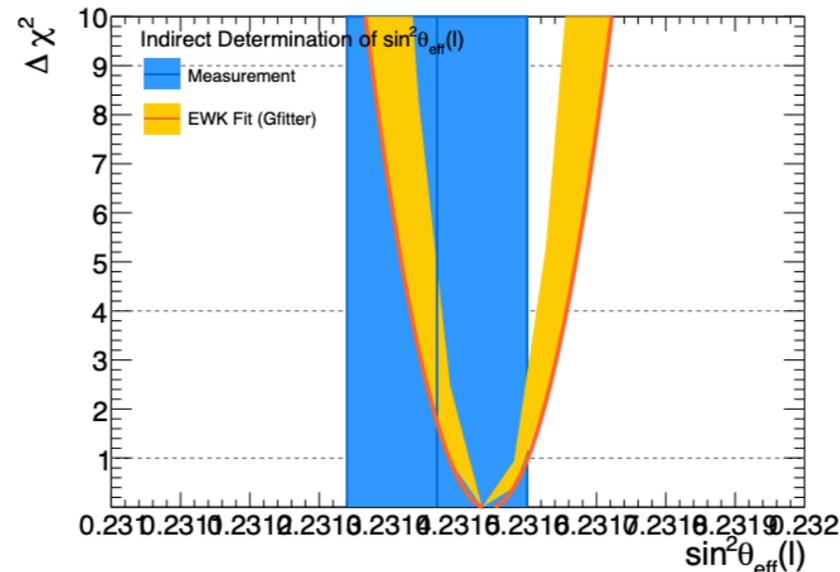
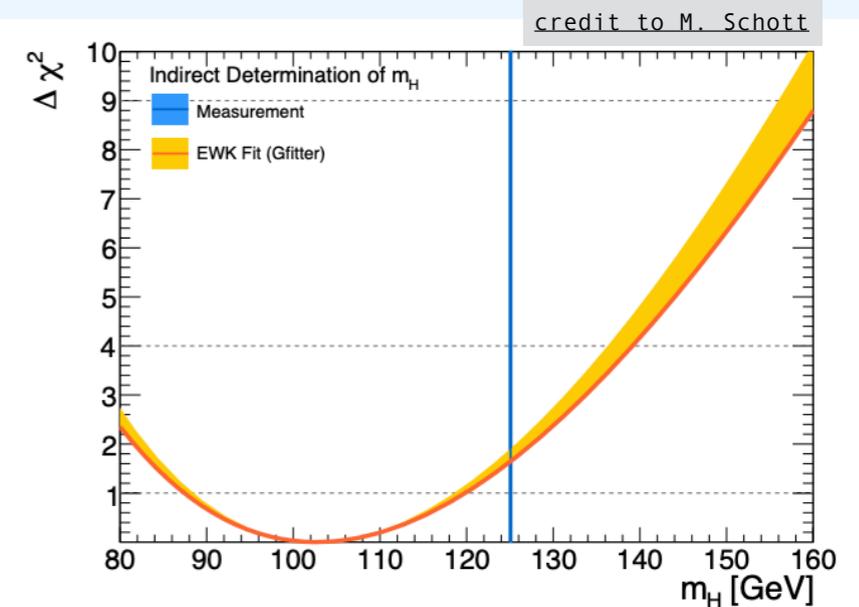
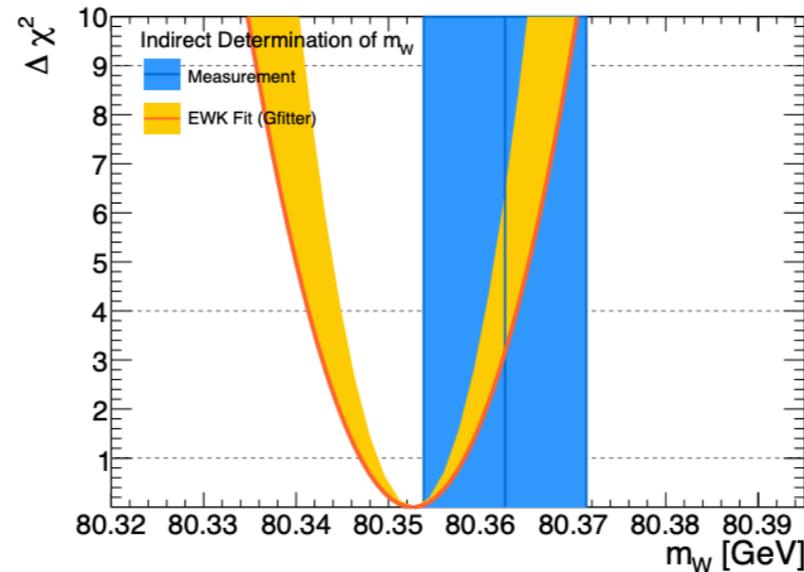
- <https://project-gfitter.web.cern.ch/>

- Indirect predictions for main observables

- $m_W = 80353 \pm 5.6$ MeV
- $m_Z = 91195 \pm 7$ MeV
- $m_T = 174.3 \pm 1.6$ GeV
- $m_H = 102.7 \pm 16$ GeV
- $\sin^2\theta_W = 0.231544 \pm 0.000056$

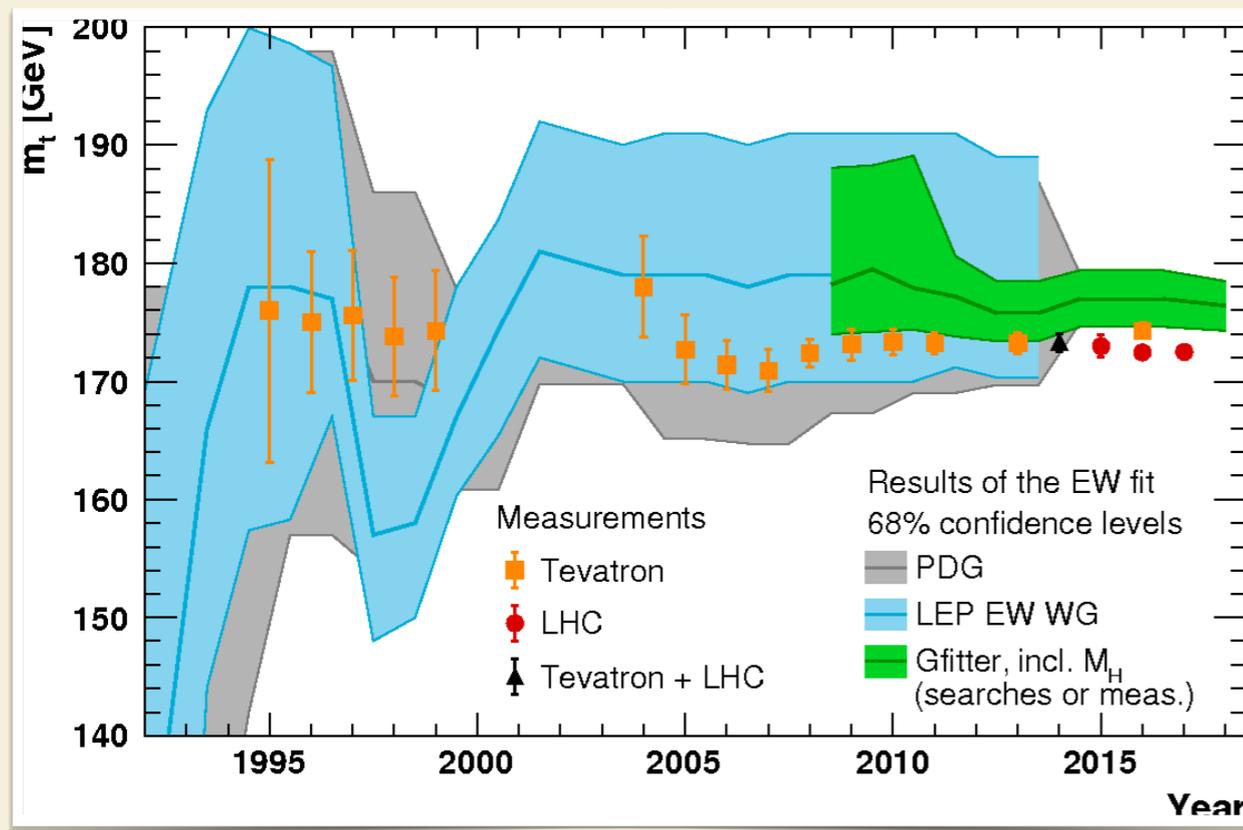
- Overall consistency of the SM Global Electroweak Fit

- $\chi^2/\text{ndf} = 17.1/14$ (p-value 0.25)

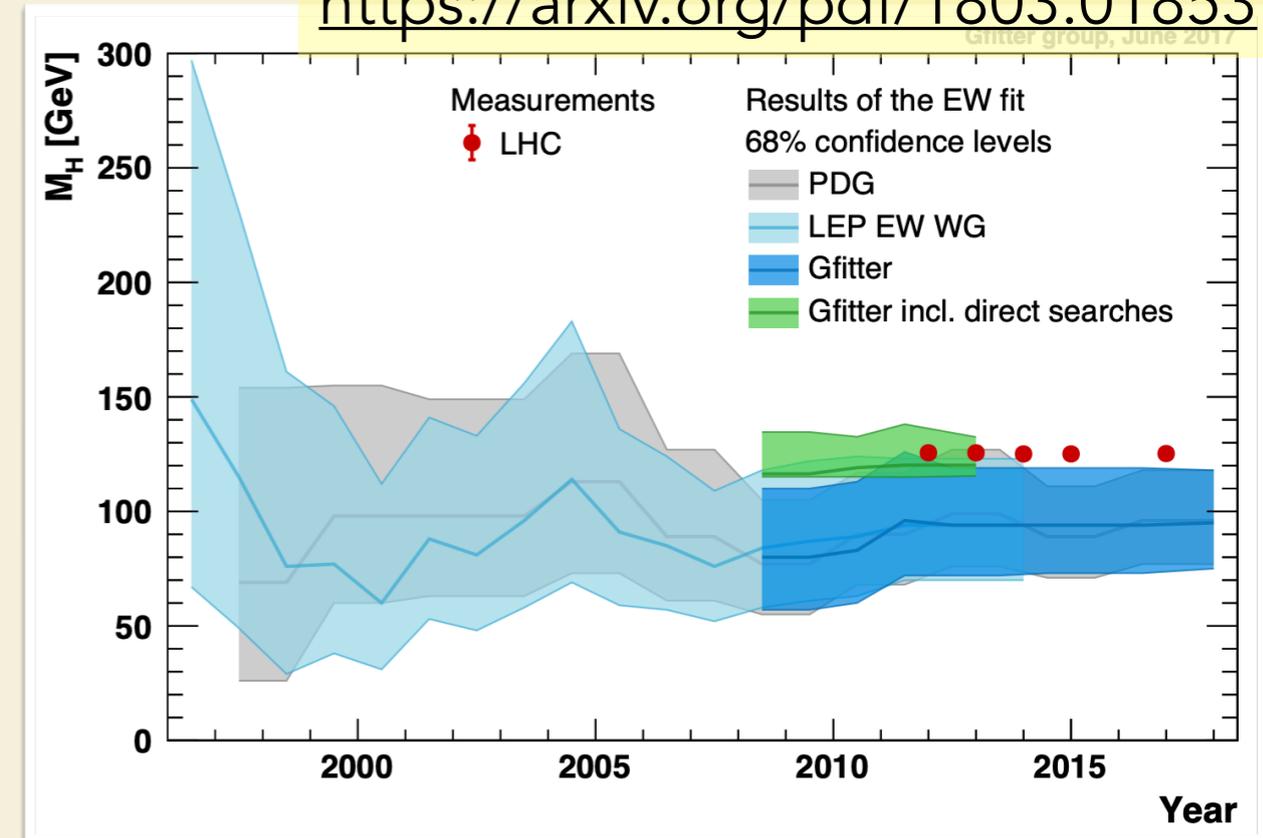


credit to M. Schott

right now...

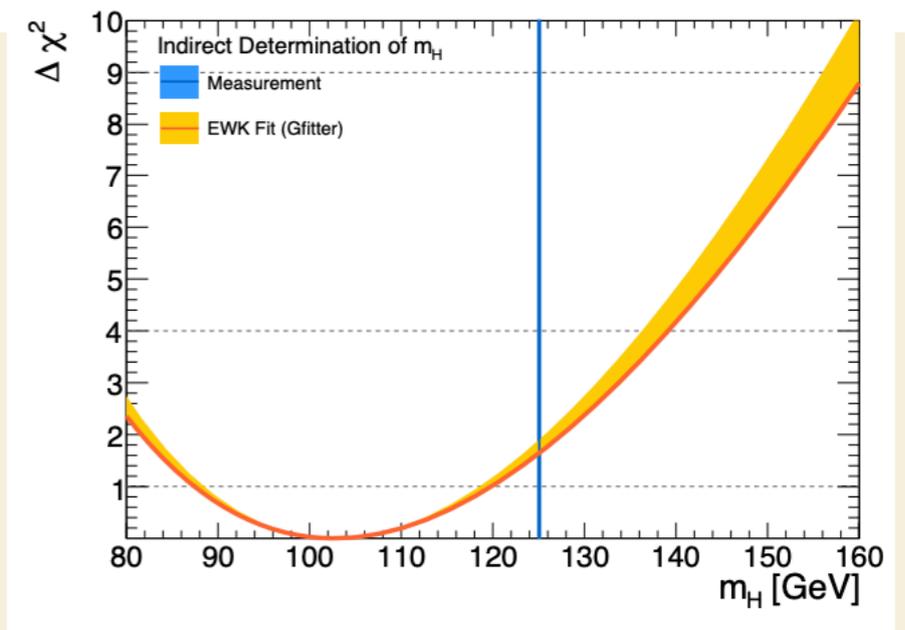
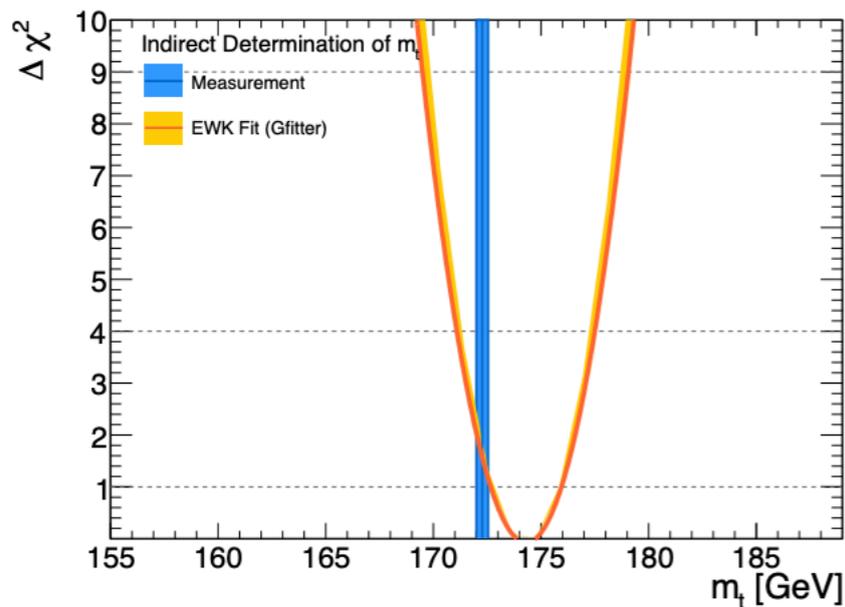
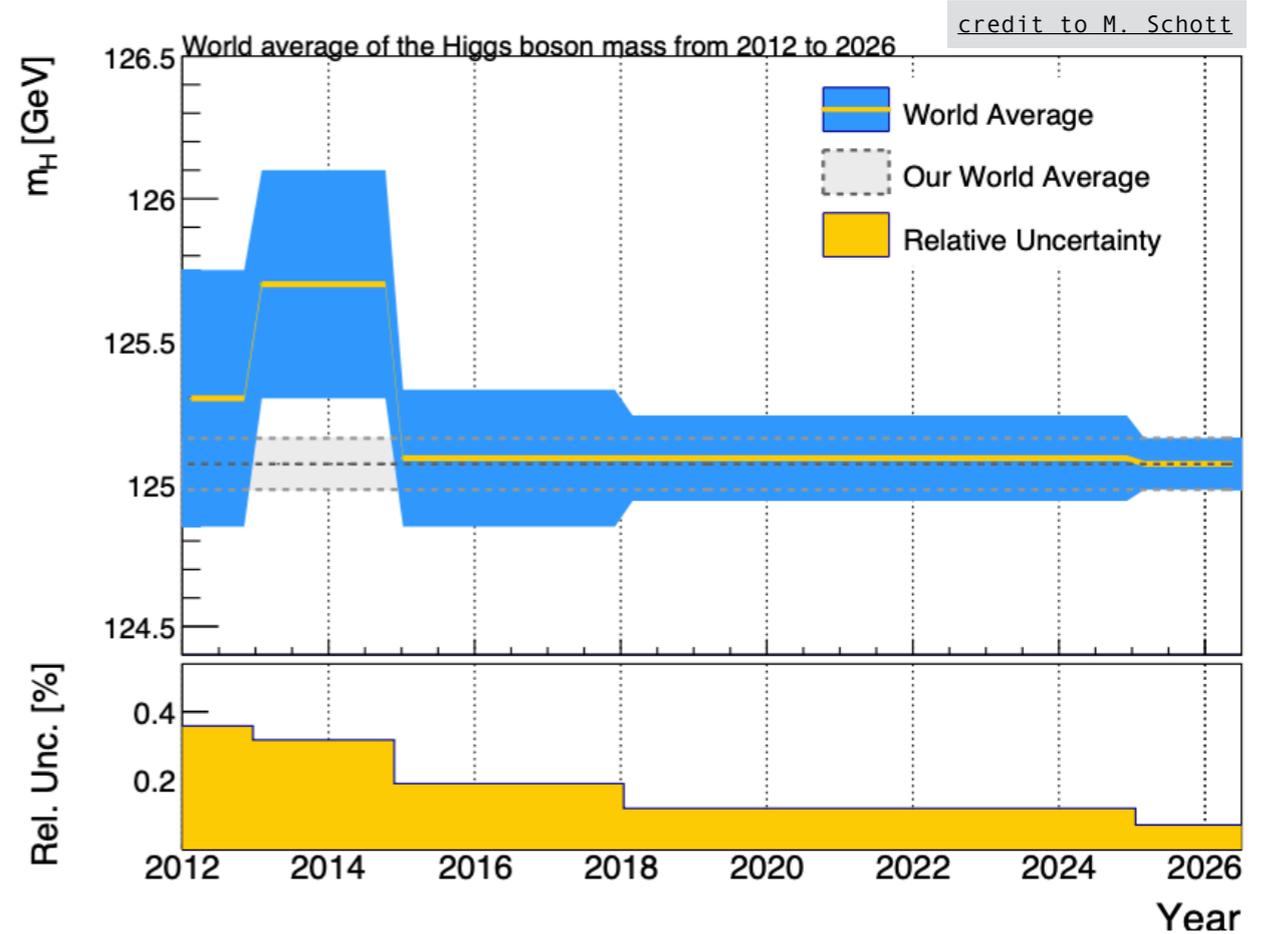
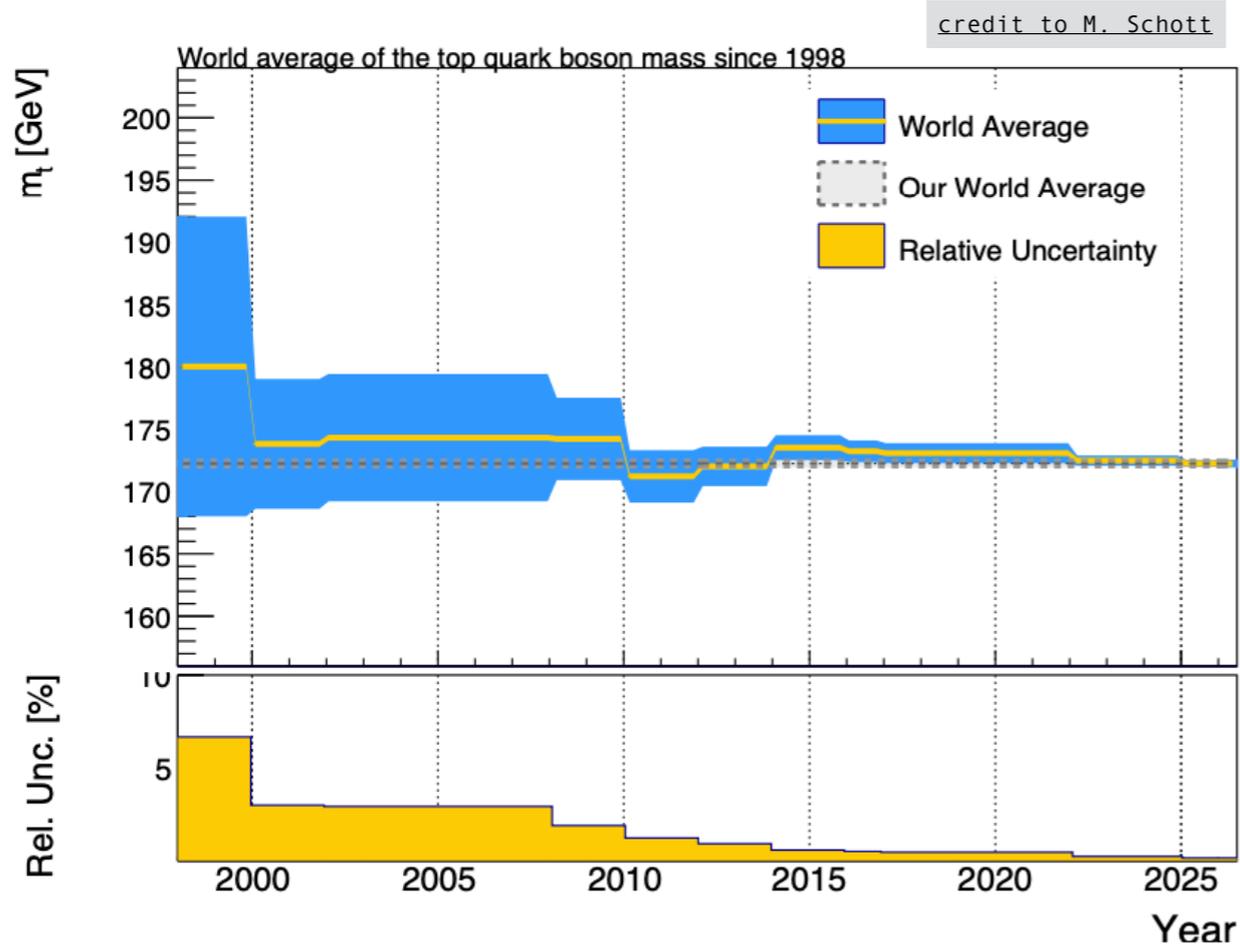


<https://arxiv.org/pdf/1803.01853>

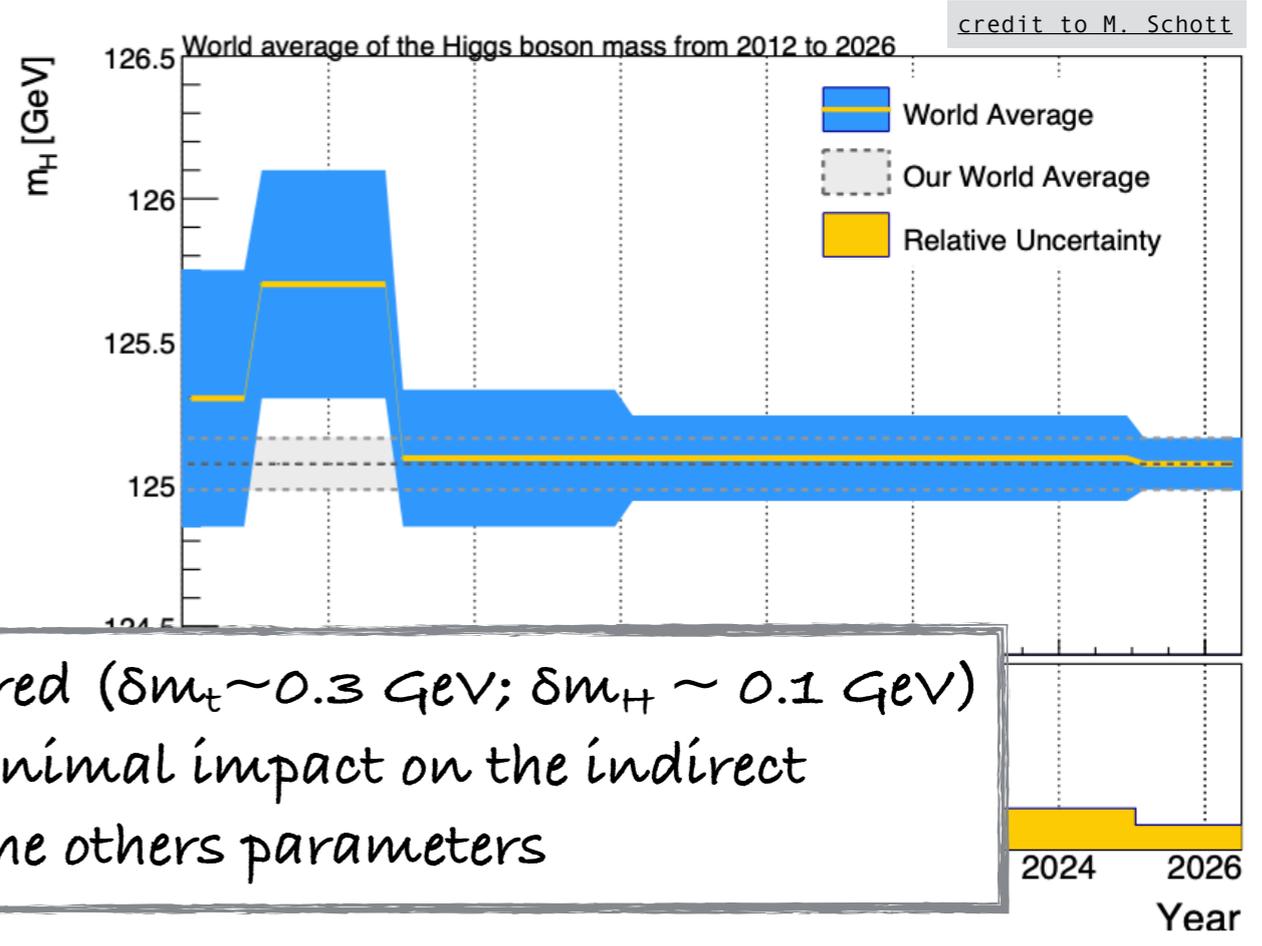
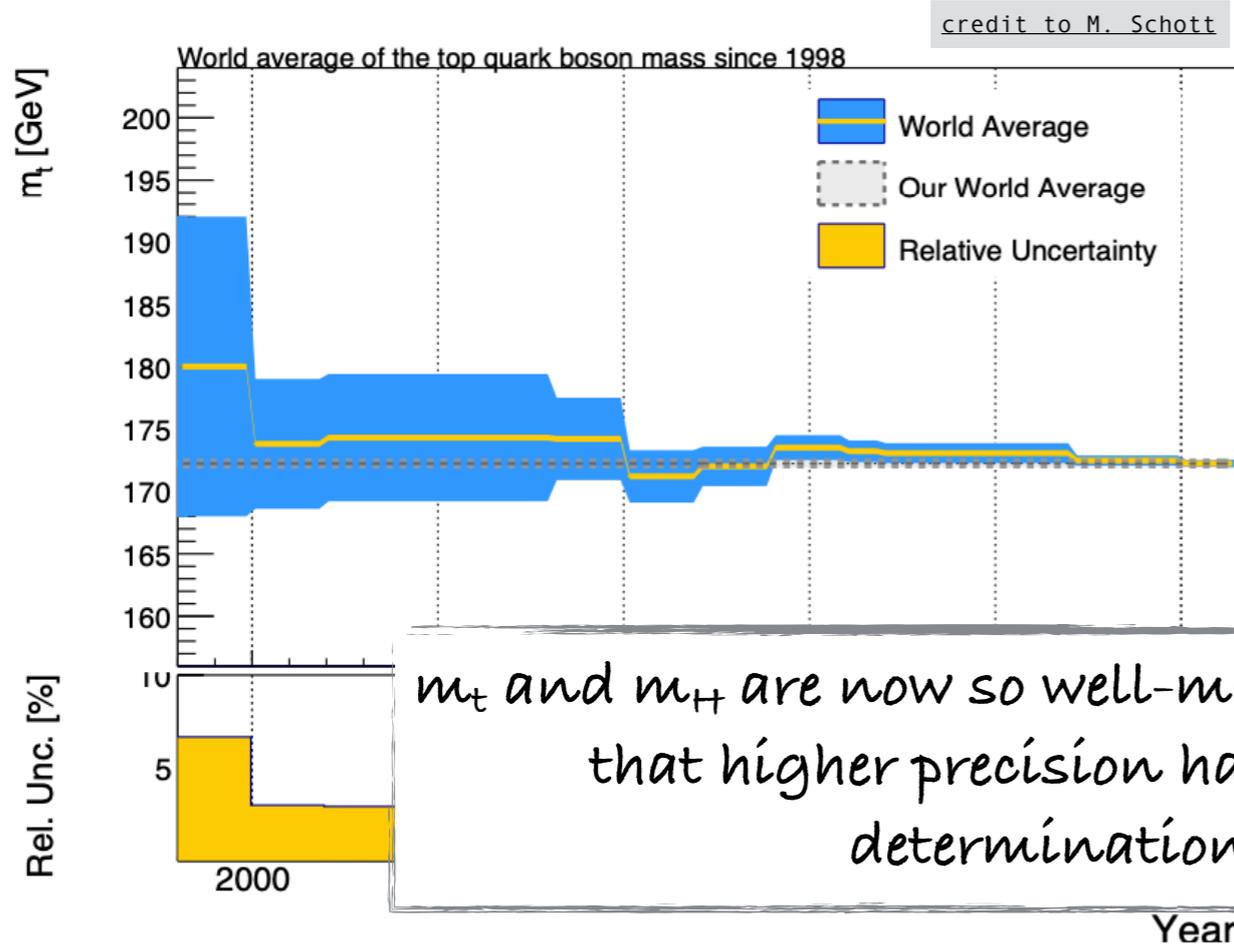


m_t and m_H are now so well-measured ($\delta m_t \sim 0.3$ GeV; $\delta m_H \sim 0.1$ GeV) that higher precision has minimal impact on the indirect determination of the others parameters

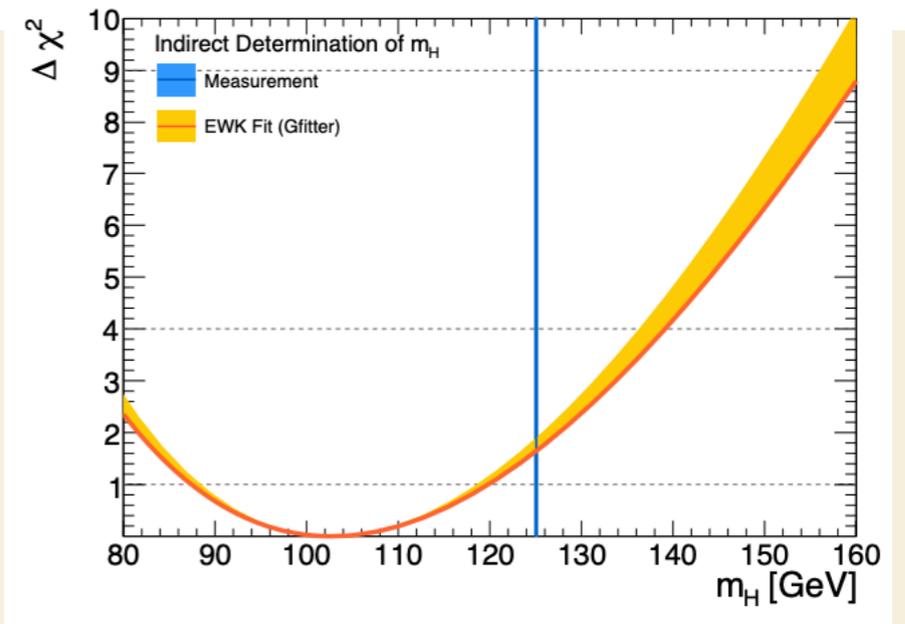
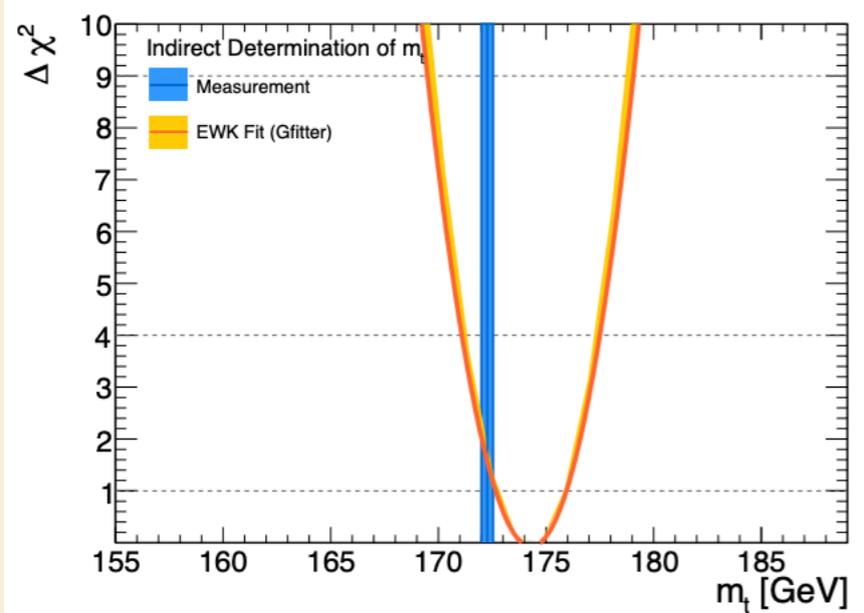
Predictive Power of the SM today



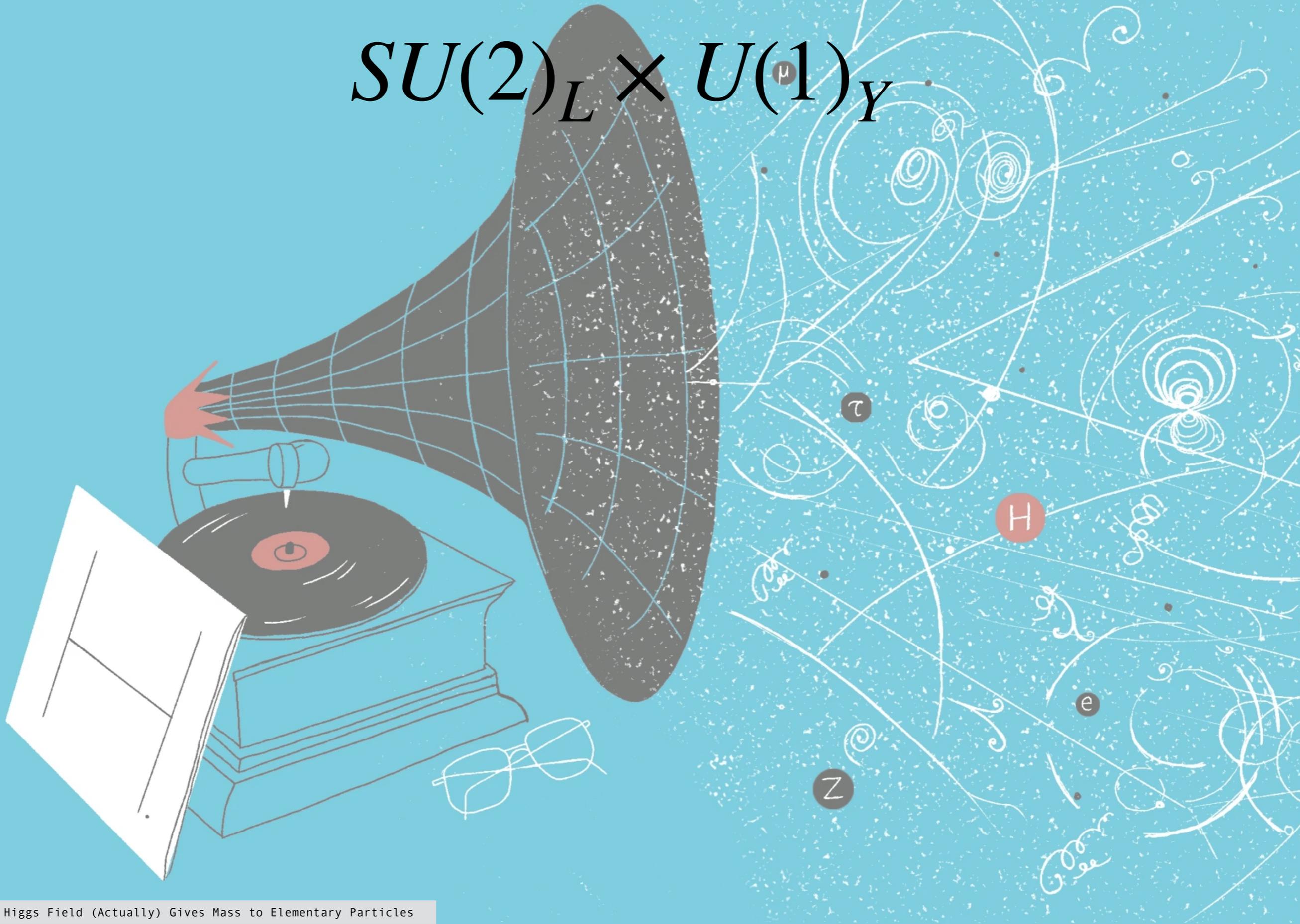
Predictive Power of the SM today



m_t and m_H are now so well-measured ($\delta m_t \sim 0.3$ GeV; $\delta m_H \sim 0.1$ GeV) that higher precision has minimal impact on the indirect determination of the others parameters



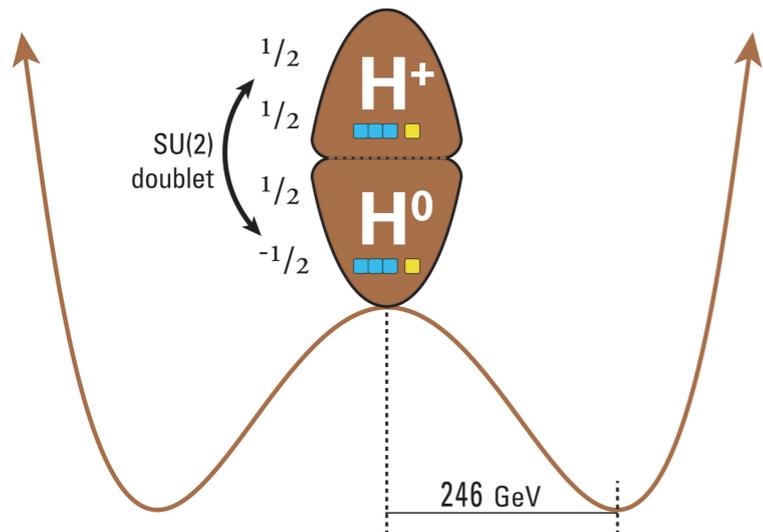
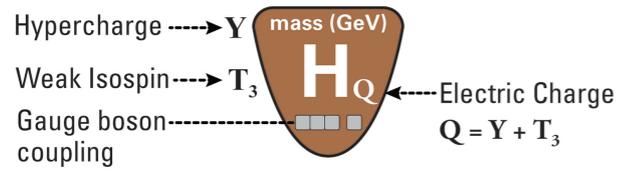
$$SU(2)_L \times U(1)_Y$$



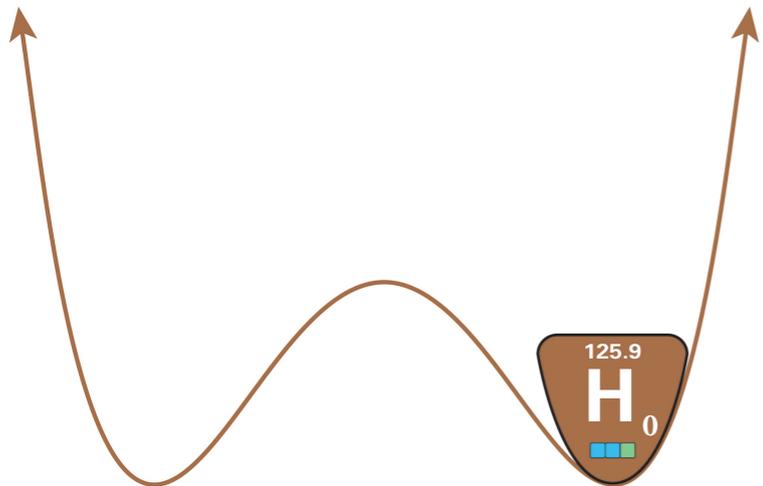
How the Higgs Field (Actually) Gives Mass to Elementary Particles

The Standard Model of Particle Physics

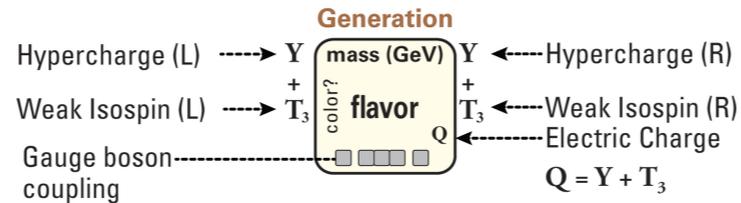
Spin 0 (Higgs Boson)



Unbroken Symmetry
Broken Symmetry



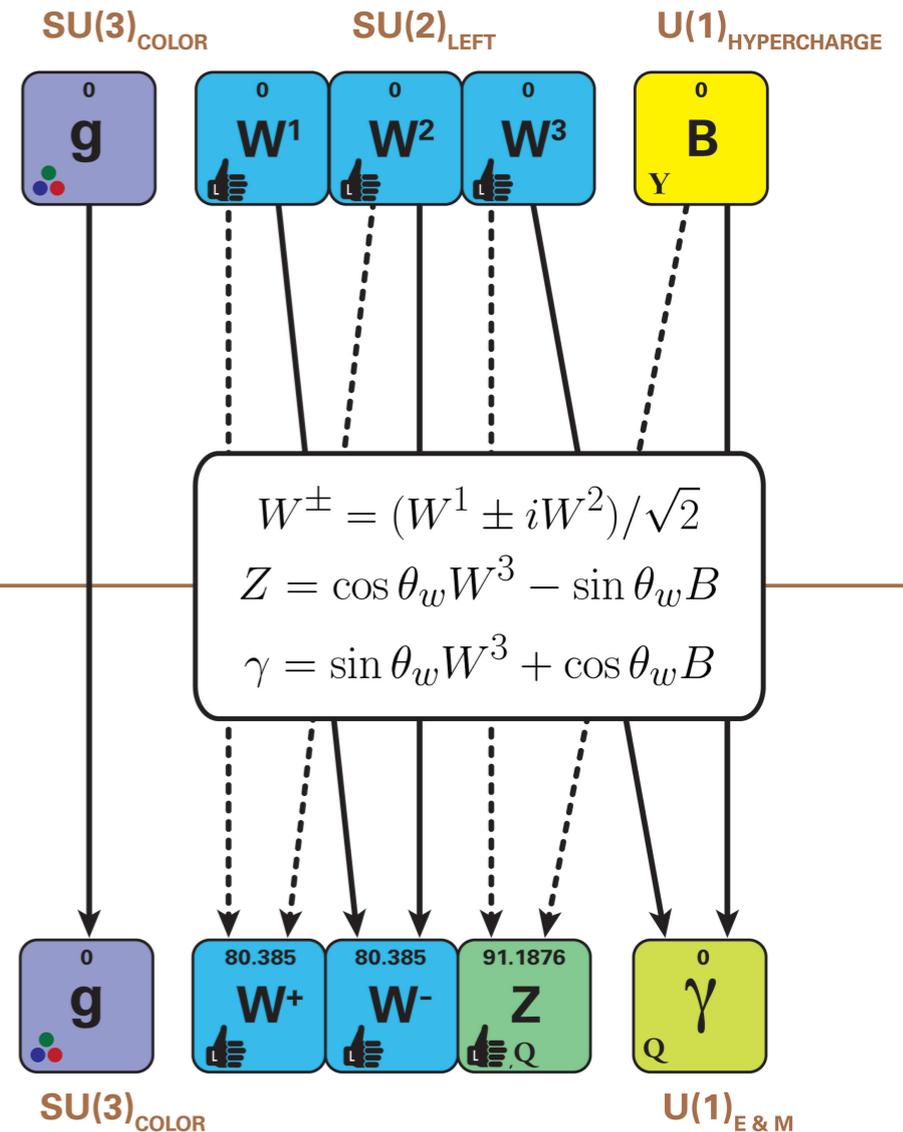
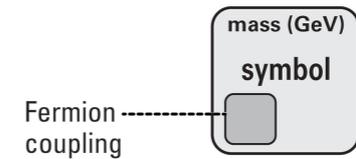
Spin 1/2 (Fermions)



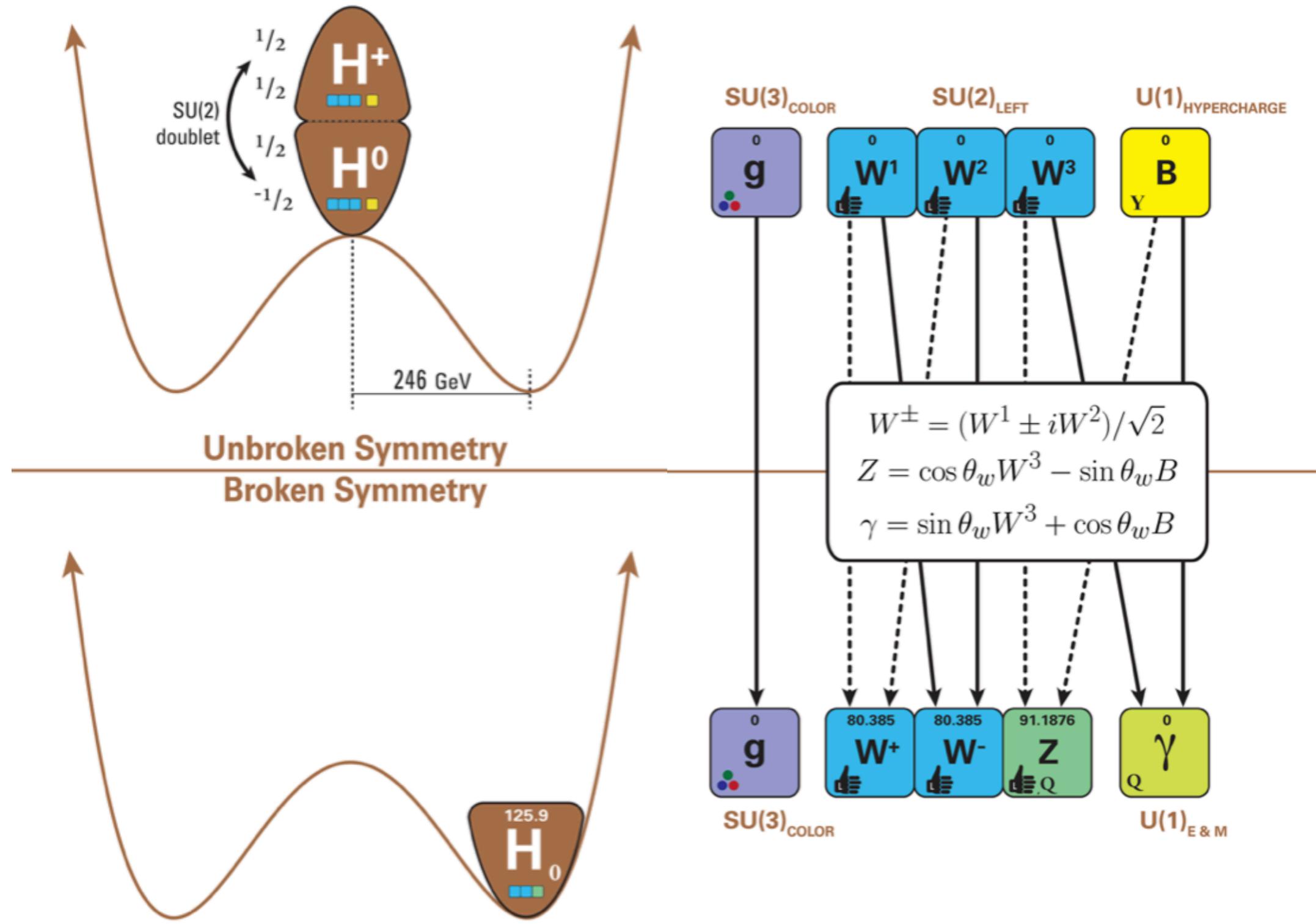
| | 1 st | 2 nd | 3 rd | |
|---------------------------|---------------------------|-----------------------------|------------------------------|--------------------------|
| Left handed SU(2) doublet | $1/6$ | $1/6$ | $1/6$ | $2/3$ |
| | $1/2$ | $1/2$ | $1/2$ | 0 |
| | u | c | t | Quarks |
| | $1/6$ | $1/6$ | $1/6$ | |
| | $-1/2$ | $-1/2$ | $-1/2$ | |
| | Left handed SU(2) doublet | $-1/2$ | $-1/2$ | $-1/2$ |
| $1/2$ | | $1/2$ | $1/2$ | 0 |
| ν_e | | ν_μ | ν_τ | Leptons |
| $-1/2$ | | $-1/2$ | $-1/2$ | |
| $-1/2$ | | $-1/2$ | $-1/2$ | |
| | | e | μ | τ |

| | 1 st | 2 nd | 3 rd |
|---------------------------|-----------------------------|------------------------------|-----------------|
| 0.0023 | 1.275 | 173.07 | |
| u | c | t | |
| $2/3$ | $2/3$ | $2/3$ | |
| 0.0048 | 0.095 | 4.18 | |
| d | s | b | |
| $-1/3$ | $-1/3$ | $-1/3$ | |
| m_1 M_1 | m_2 M_2 | m_3 M_3 | |
| ν_e | ν_μ | ν_τ | |
| 0 | 0 | 0 | |
| 0.000511 | 0.105658 | 1.77682 | |
| e | μ | τ | |
| -1 | -1 | -1 | |

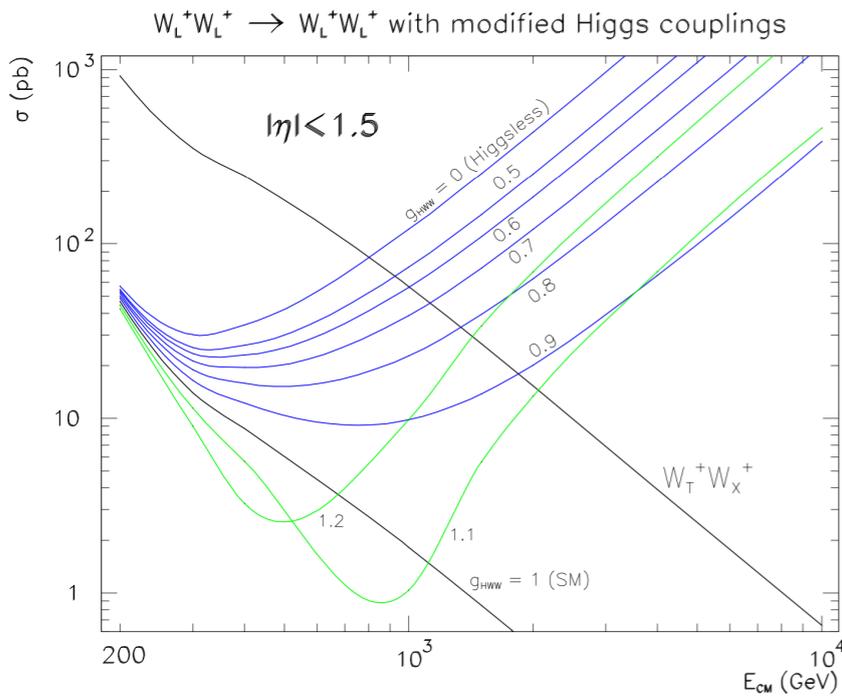
Spin 1 (Gauge Bosons)



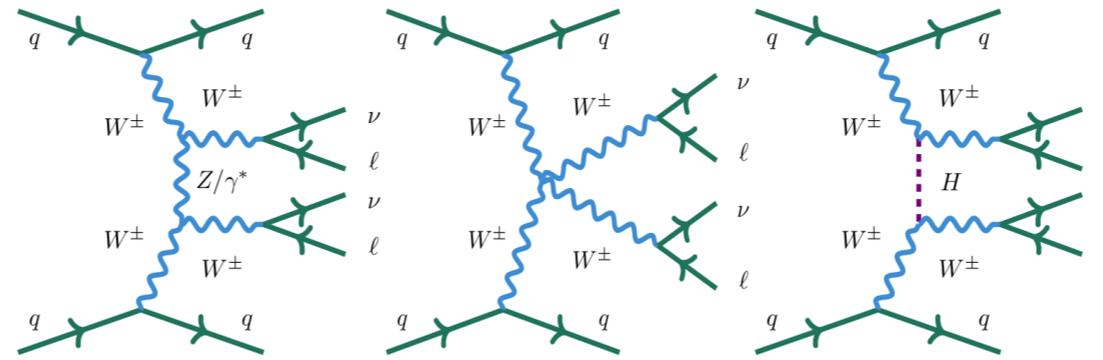
$SU(2)_L \times U(1)_Y$



longitudinal polarised WW - scattering



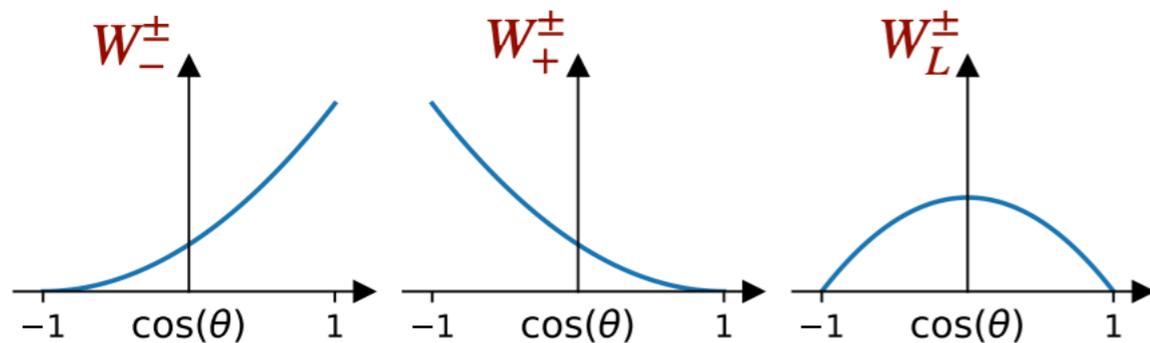
<https://arxiv.org/pdf/1412.8367>



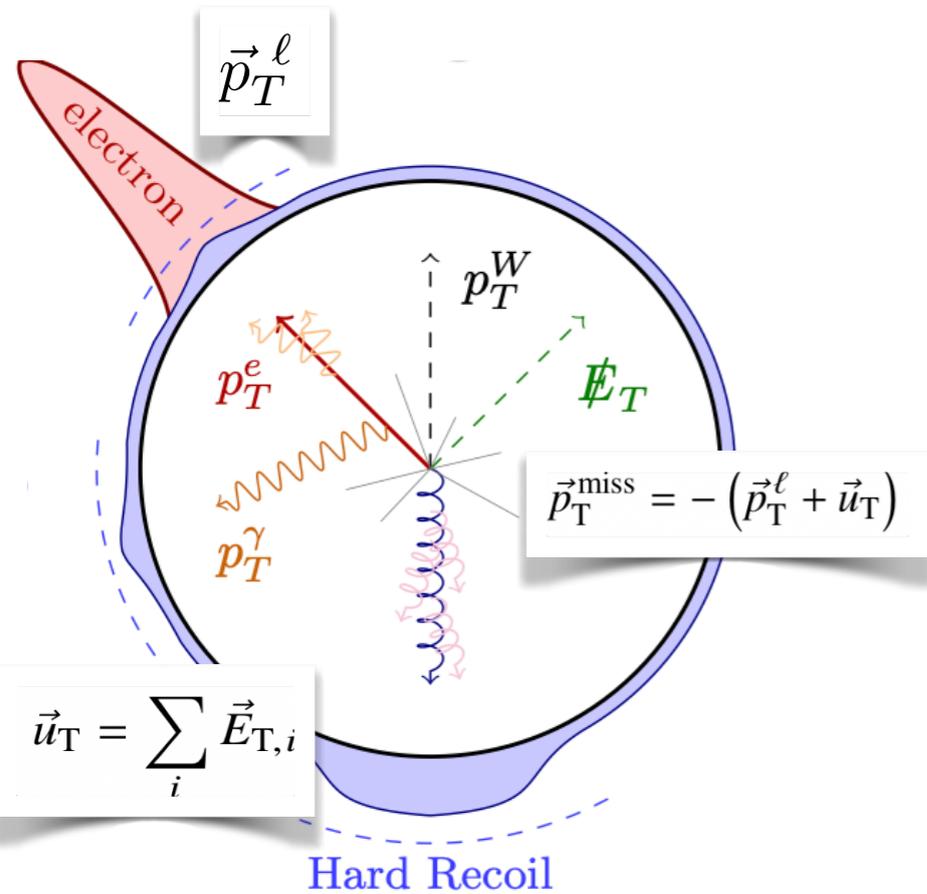
Higgs mechanism (eg. EW symmetry breaking) result in longitudinal polarised vector bosons:

$W_L^\pm W_L^\pm \rightarrow W_L^\pm W_L^\pm$ scatter would violate unitarity if Higgs coupling deviates from SM prediction

➔ is a unique opportunity to probe electroweak symmetry-breaking

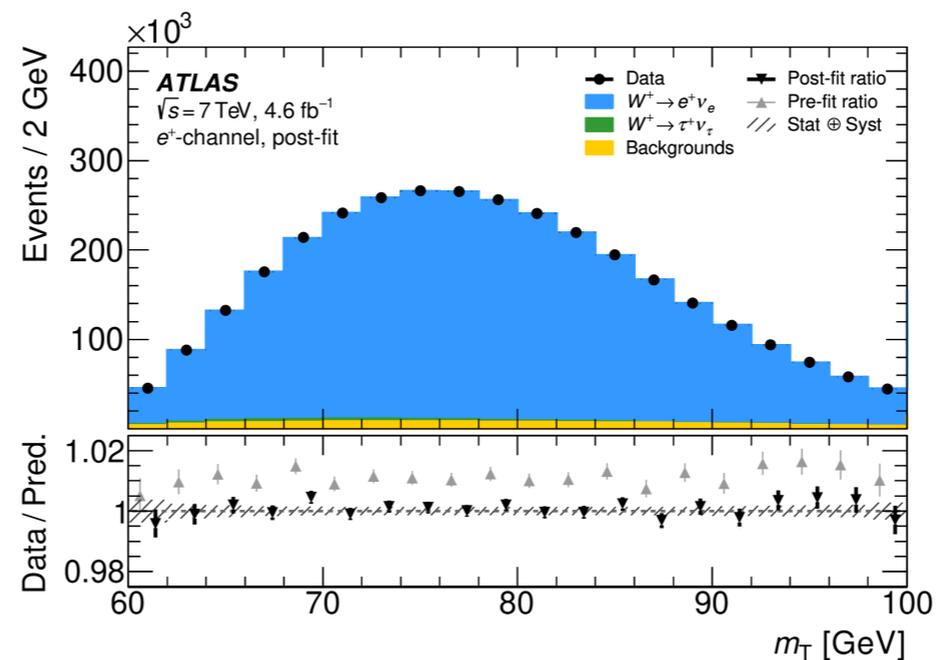
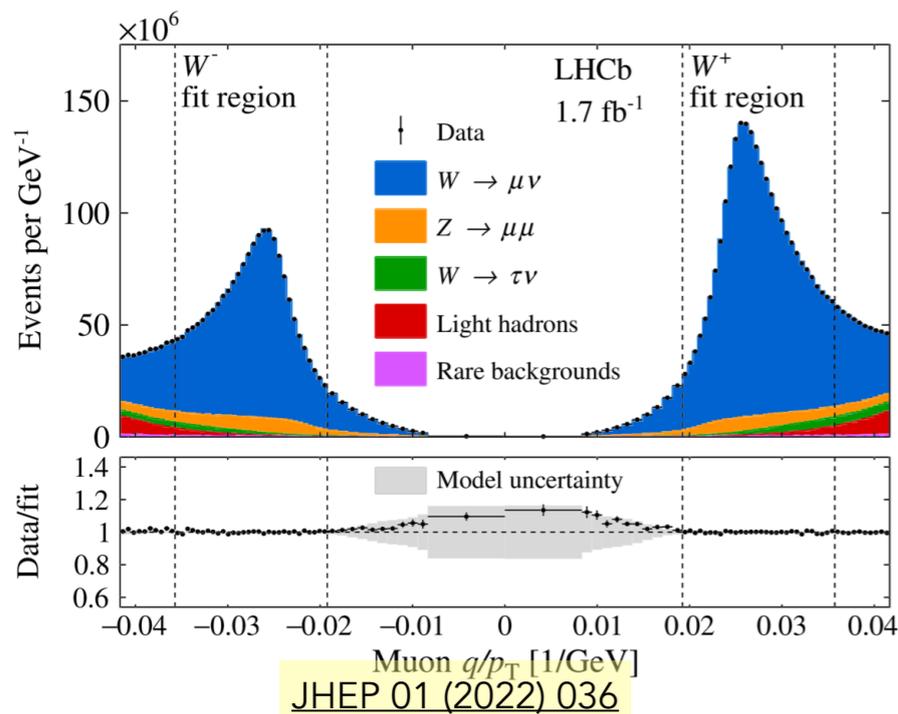


The W Boson mass at LHC

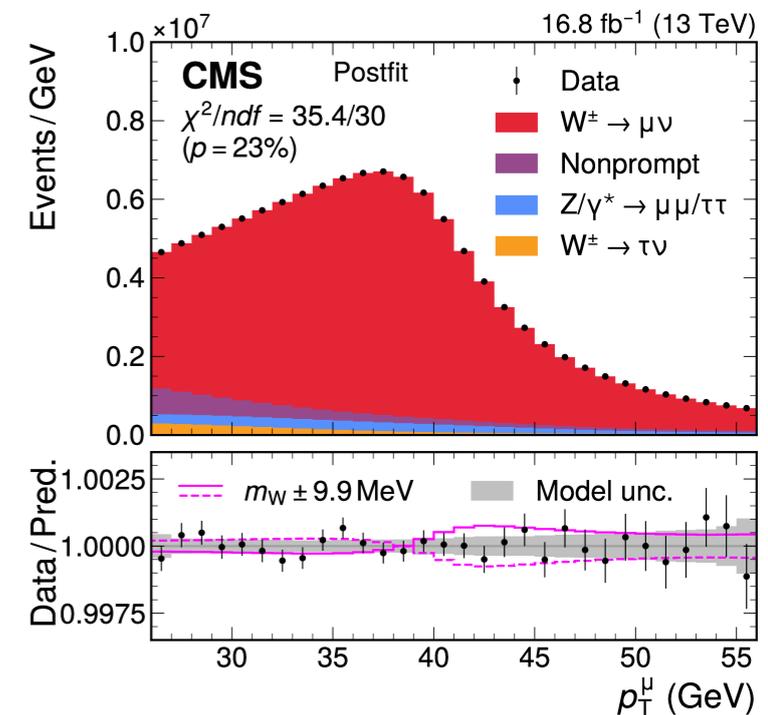


W boson signature: Incomplete kinematics (missing neutrino) no invariant mass: rely on measured quantities (p_{\perp} , u_{\perp}) and exploit momentum conservation in the transverse plane (p_{\perp}^{miss} , m_{\perp})

$$m_{\perp} = \sqrt{2p_T^\ell p_T^{\text{miss}} (1 - \cos \Delta\phi)}$$

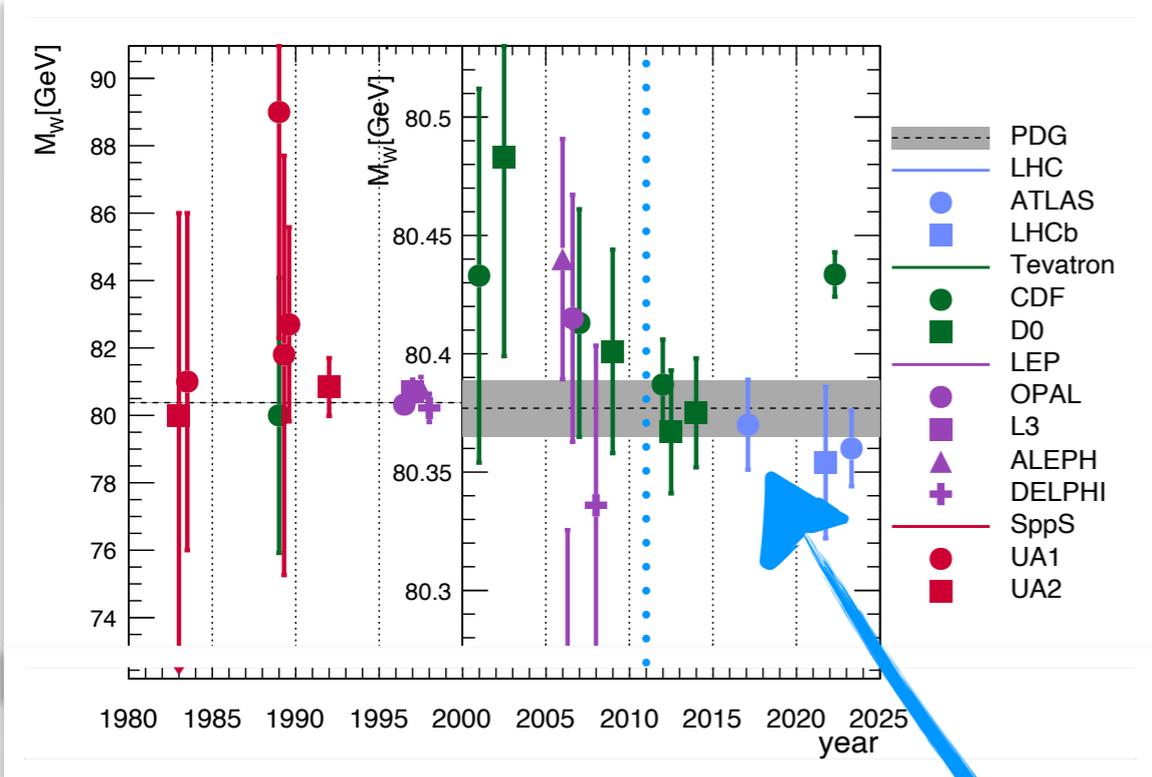


Eur. Phys. J. C 84 (2024) 1309



arXiv:2412.13872

The road map of the first **LHC** m_W measurement



2008 Eur.Phys.J.C 57

ATLAS Potential on m_W

2014 JHEP 09 (2014) 145

Z Boson Transverse Momentum at 7 TeV

2016 Eur. Phys. J. C 77 (2017) 367

W and Z Boson Production at 7 TeV

2016 JHEP 08 (2016) 159

Z Boson Angular Coefficients

2017 Eur.Phys.J.C 78 (2018)

First Measurement of m_W

2018 Start of the m_W

Re-analysis Efforts

2019 A. Dürder

PhD Theses

2020 L. Adam

PhD Thesis

2022: P. König

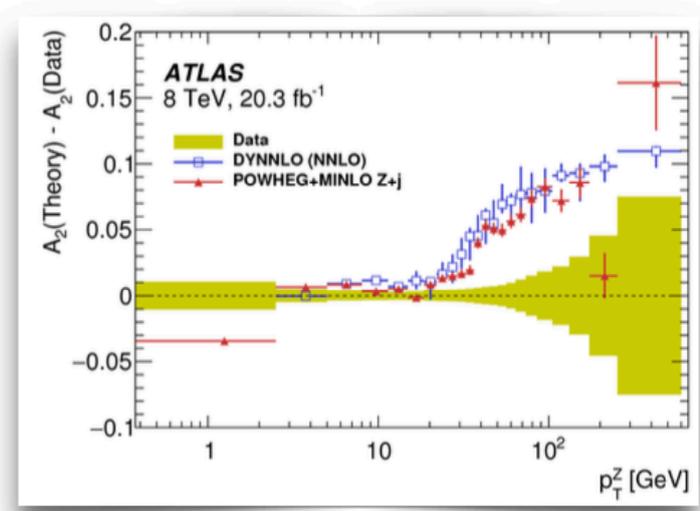
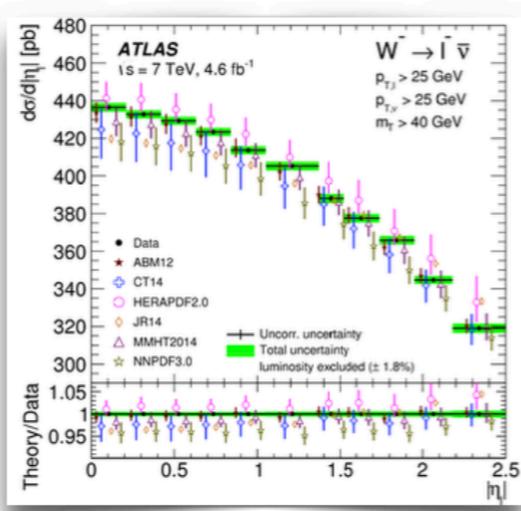
PhD Thesis

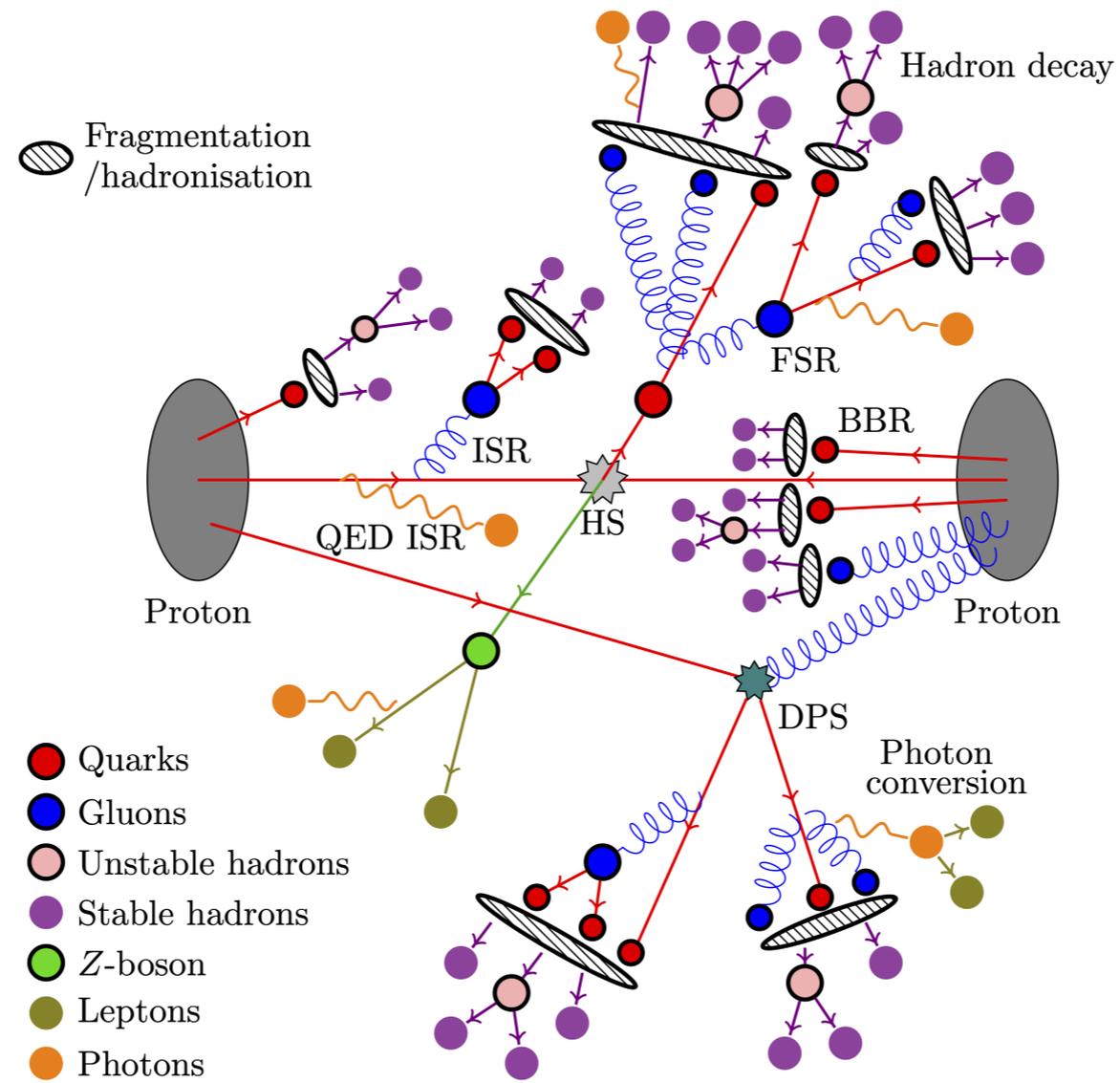
2023 This Work

Reanalysis of m_W

2012 Start of the m_W

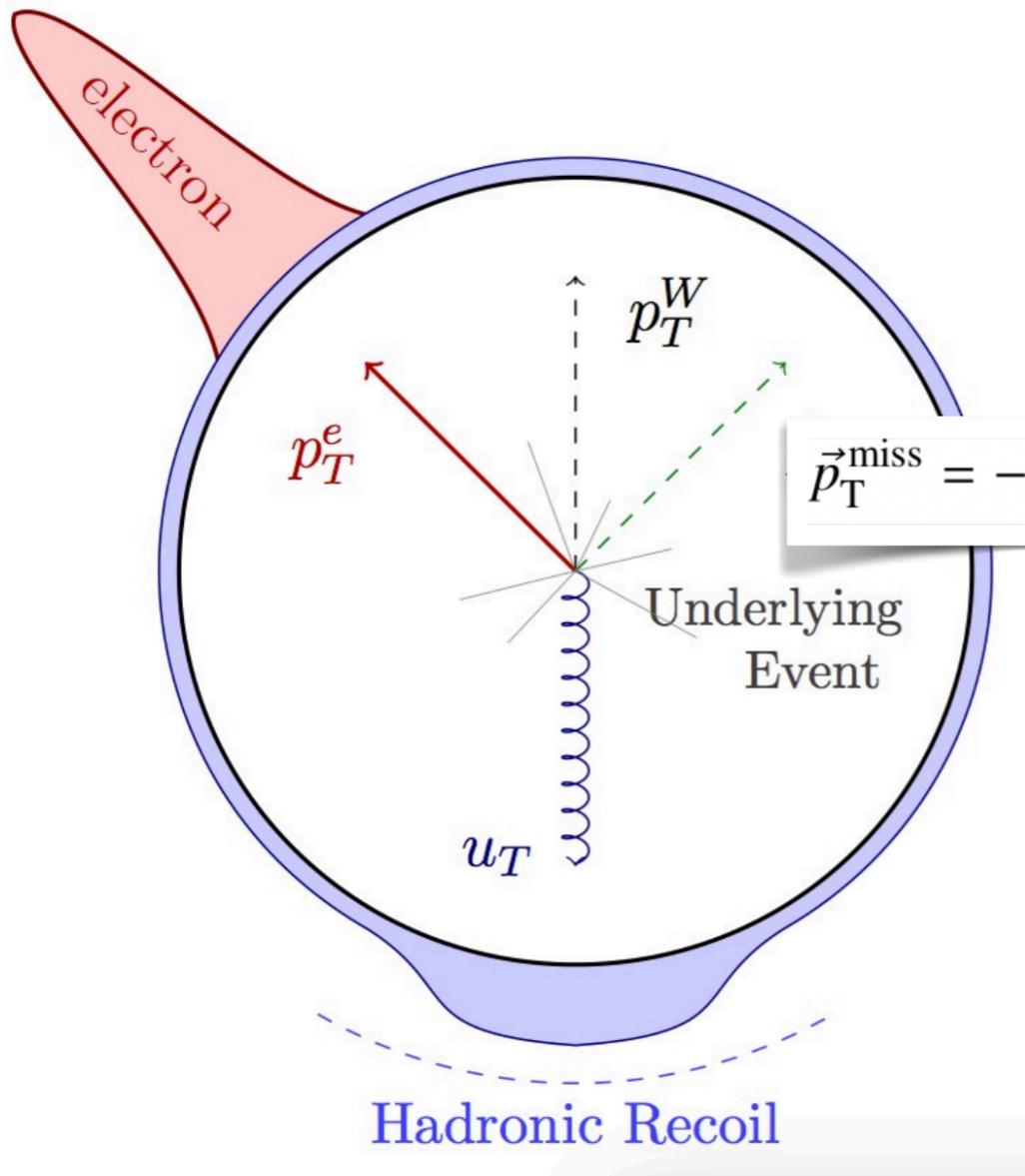
analysis Efforts





Hadronic recoil

Experimental challenge: W boson signature



Incomplete kinematics (missing **neutrino**):

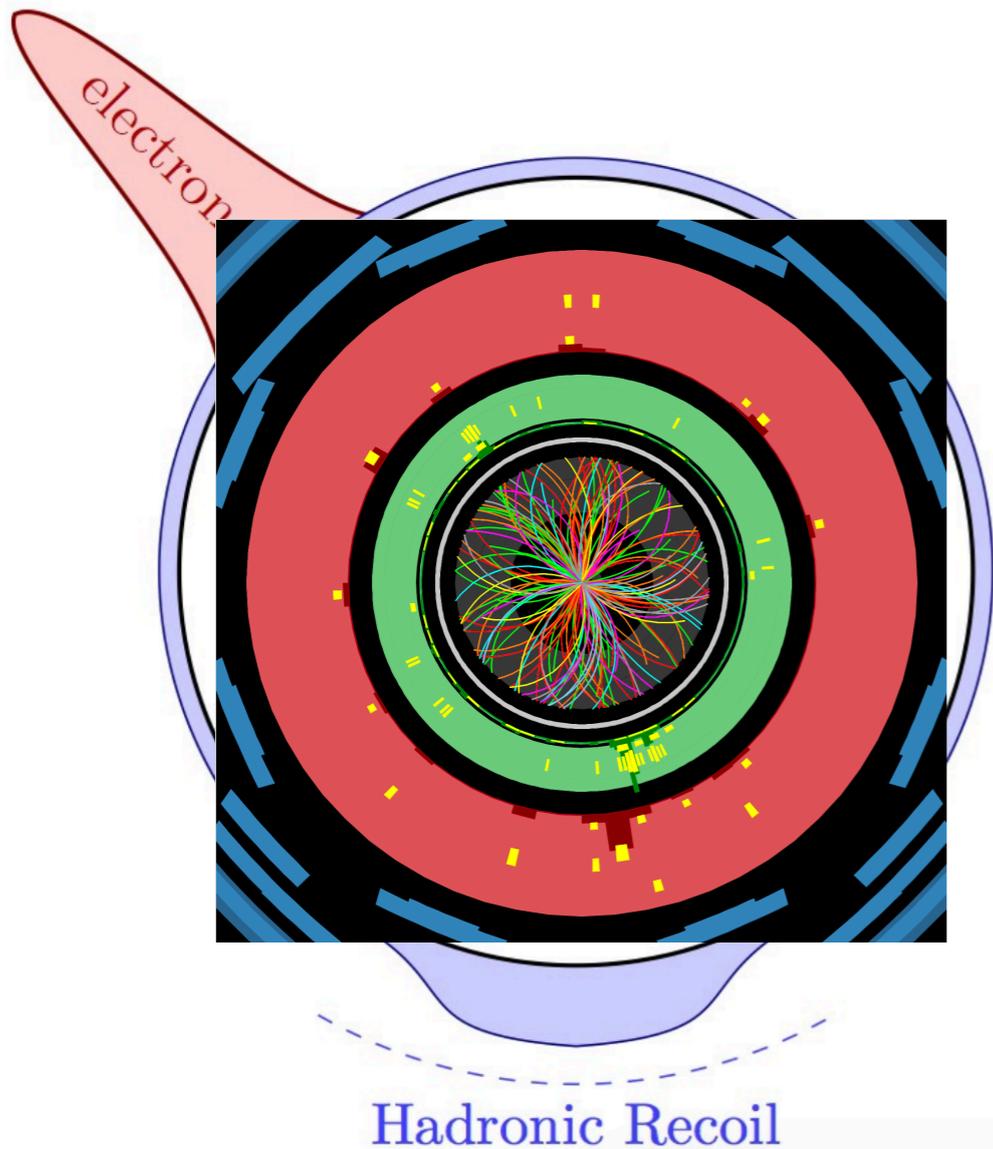
- no invariant mass
- measured quantities
 - Prompt and isolated **lepton** (e or μ)
 - **Hadronic-Recoil** (u_T): sum of "everything else" reconstructed in the calorimeters;
- exploit momentum conservation in the transverse plane to reconstruct p_T^{miss} and transverse mass (m_T)

+ Pileup ...

$$\vec{u}_T = \sum_i \vec{E}_{T,i}$$

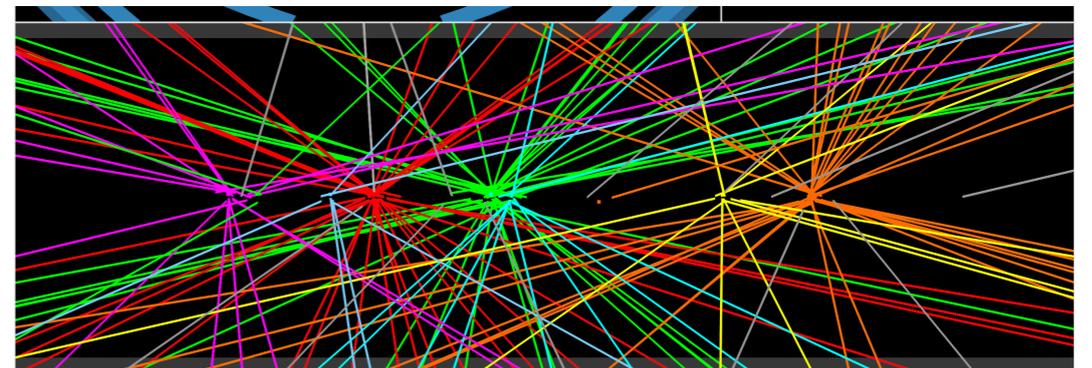
$$m_T = \sqrt{2p_T^\ell p_T^{\text{miss}} (1 - \cos \Delta\phi)}$$

W boson signature

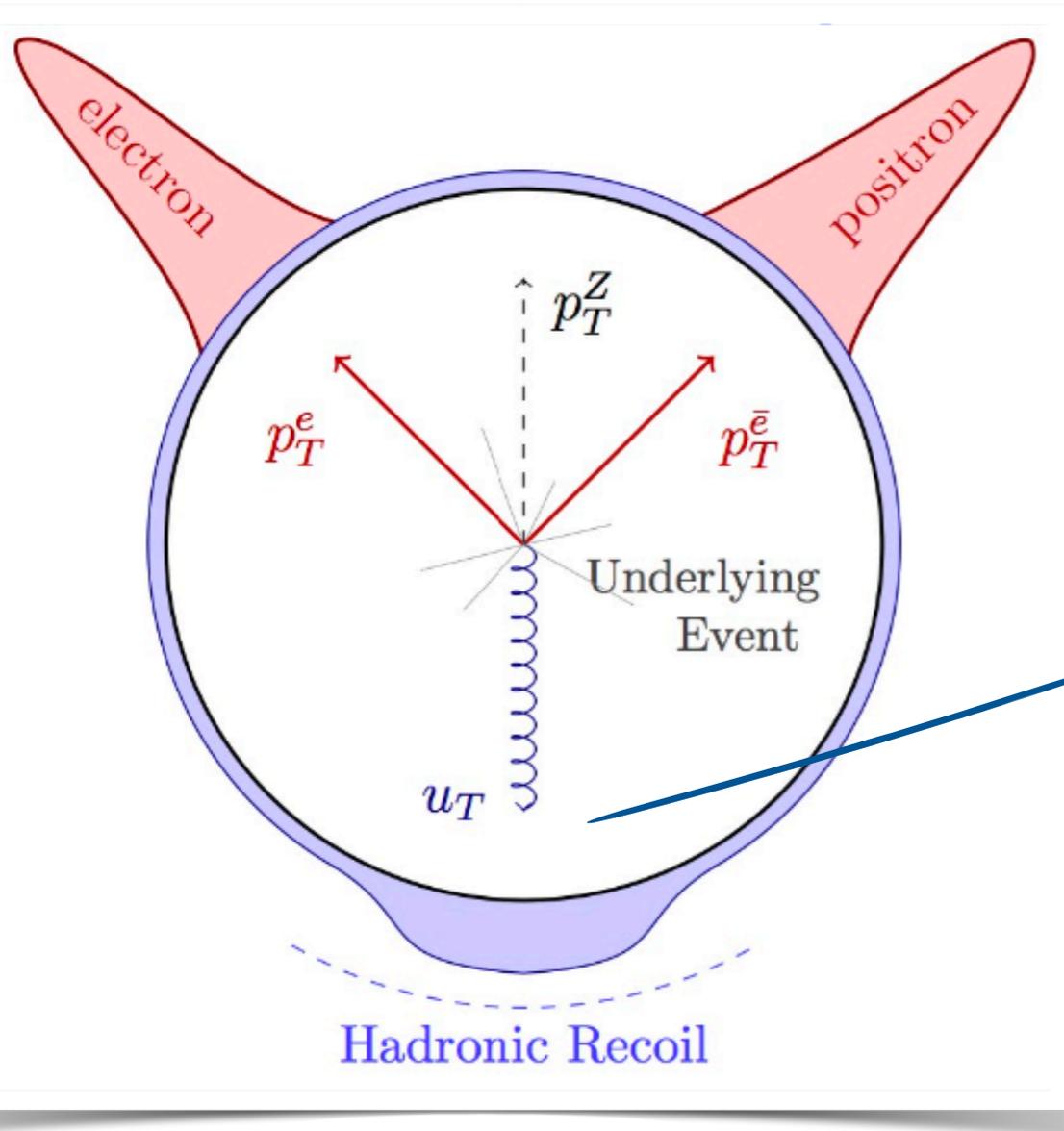


- Incomplete kinematics (missing **neutrino**):
- no invariant mass
 - measured quantities
 - Prompt and isolated **lepton** (e or μ)
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- + Pileup ...**

$$\vec{u}_T = \sum_i \vec{E}_{T,i}$$



Hadronic recoil calibration with Z events

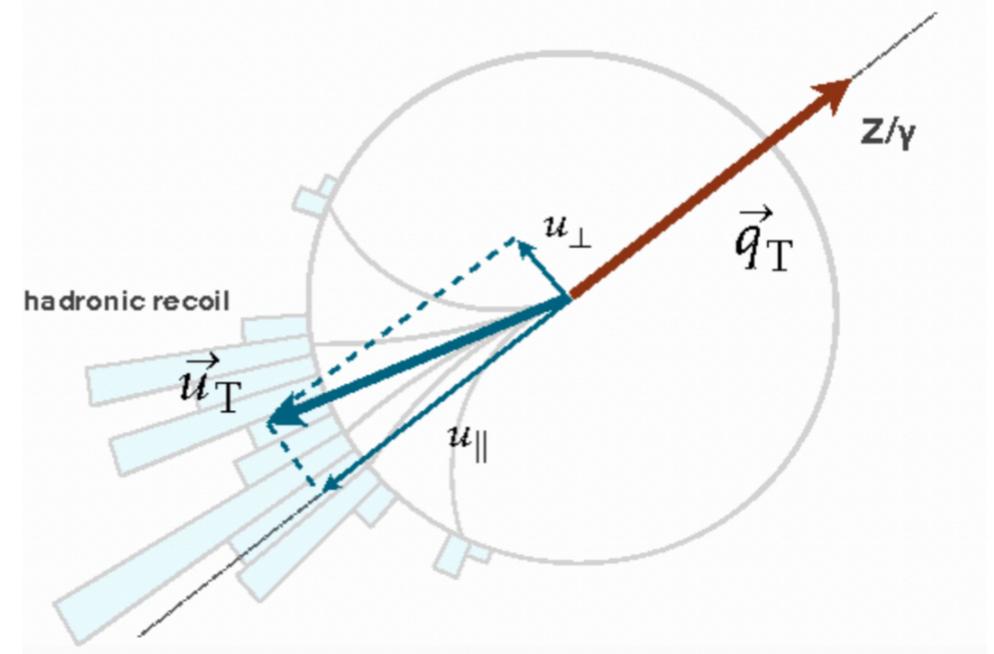


In Z-events

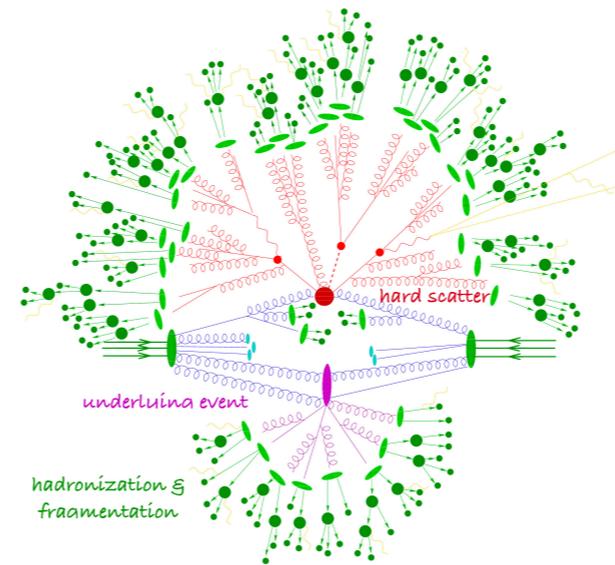
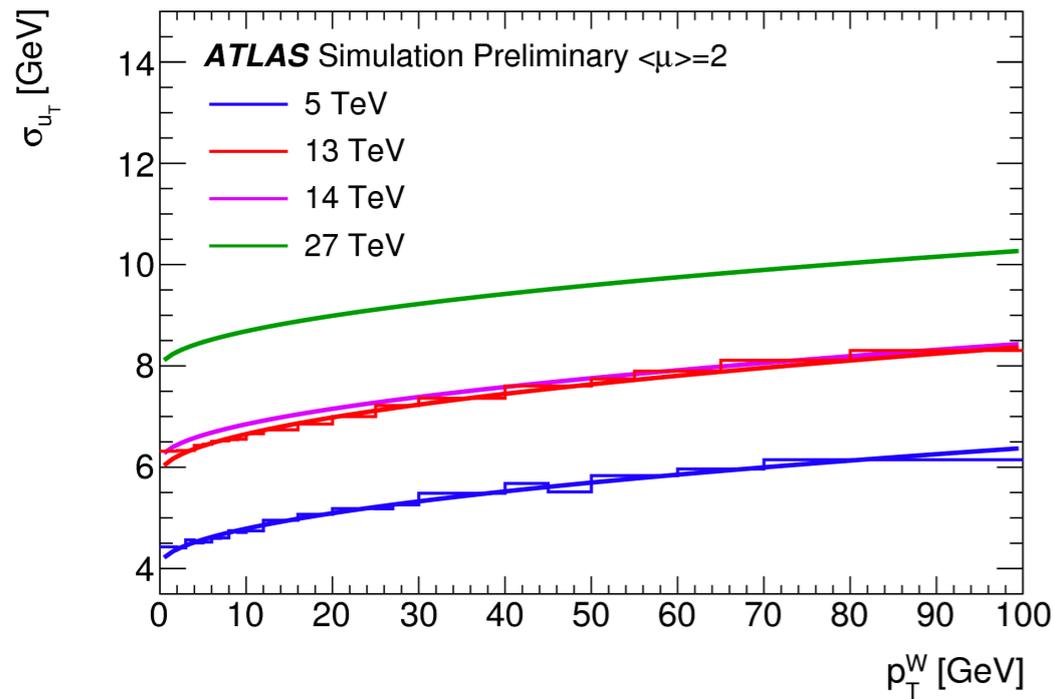
- exploit momentum conservation in the transverse plane to measure in data the u_T response using the p_T^Z balance in Z events

$$p_T^Z = p_T^{ll} = -u_T$$

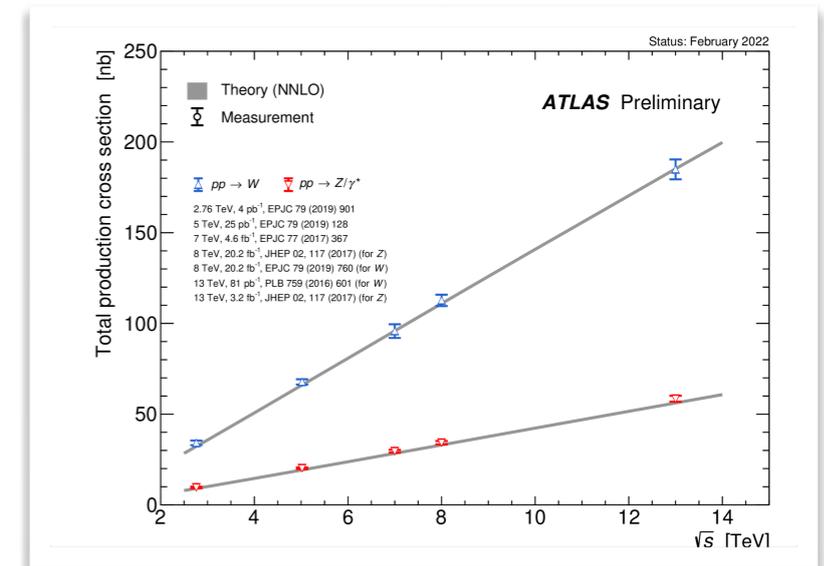
u_T scale and resolution are characterise by the \parallel and \perp projection of the recoil into the p_T^Z axis



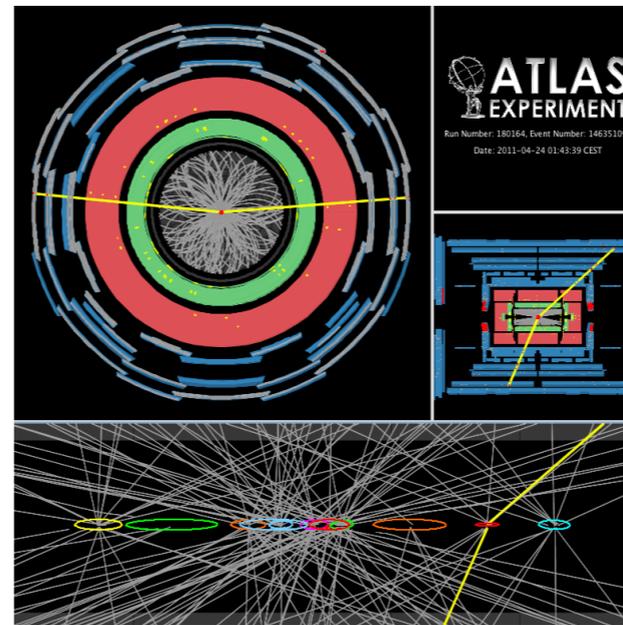
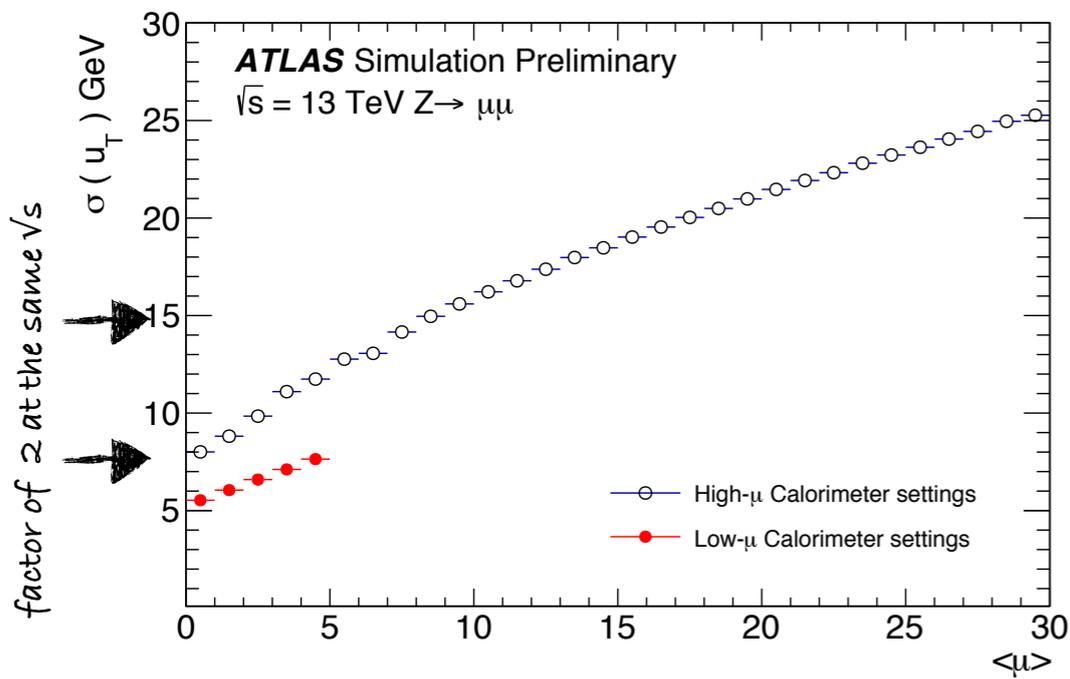
Underlying event and Pileup contribution to the recoil



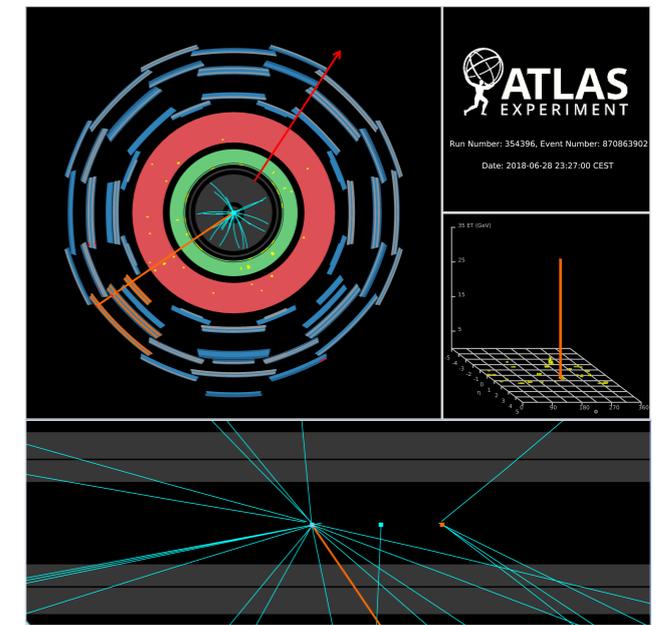
underlying events grows with \sqrt{s}



X-section grows with \sqrt{s}



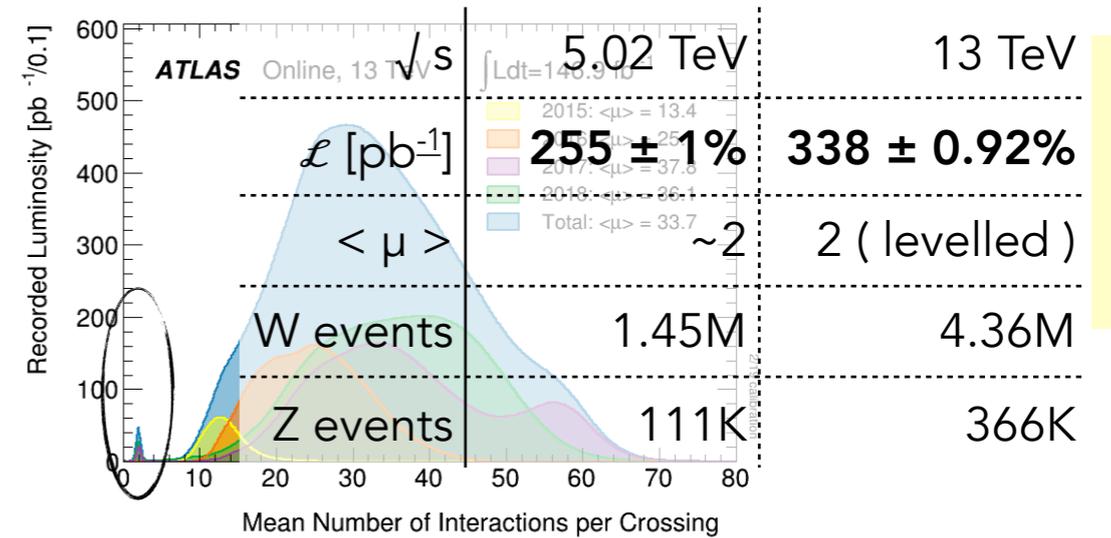
9 additional reconstructed vertices



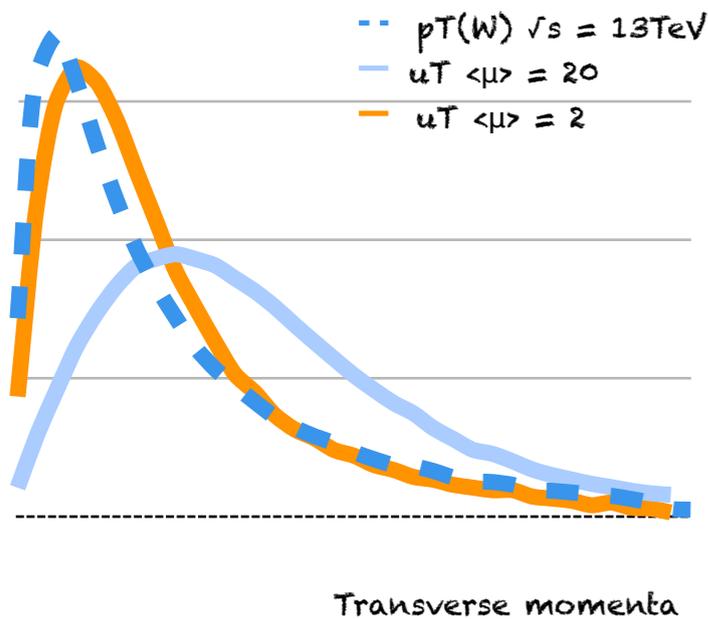
2 additional reconstructed vertices

Low- μ dataset

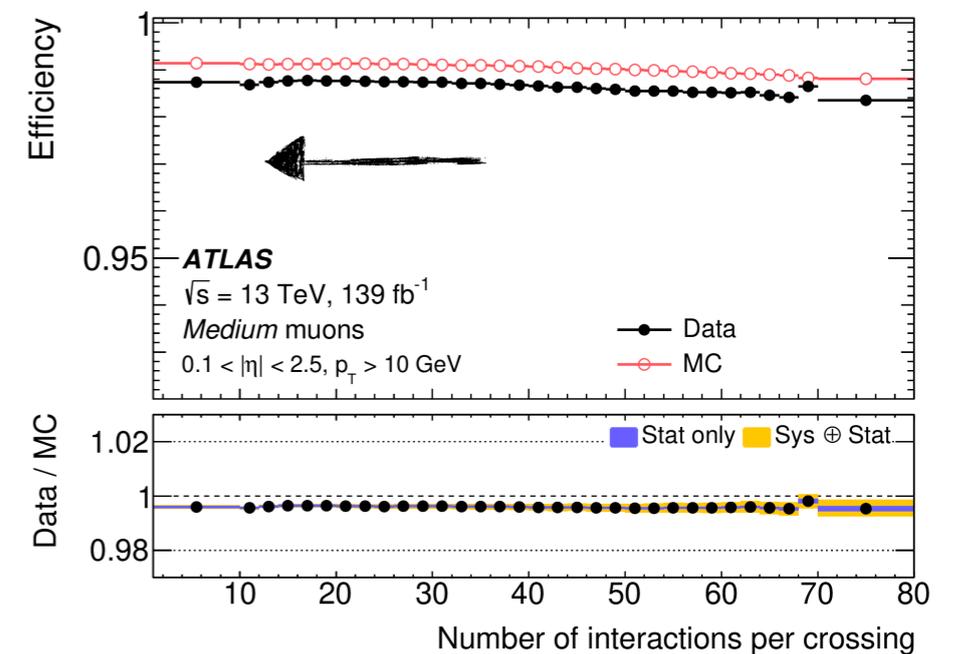
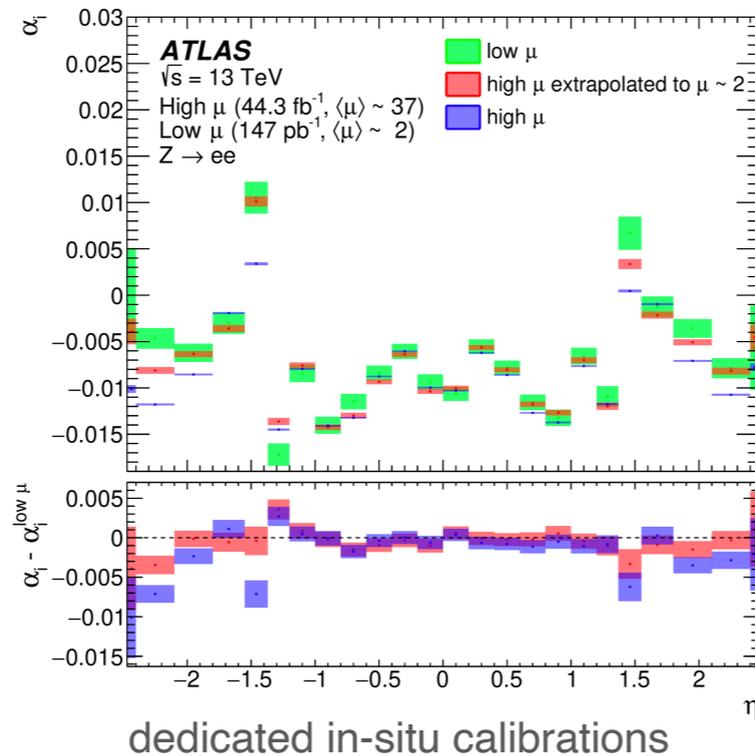
In Run-2 ATLAS collected $\sim 500 \text{ pb}^{-1}$ at $\langle \mu \rangle \sim 2$
fantastic opportunity for W precision physics!



Run2-luminosity



- **Unique** recoil resolution
- Benefit from *super precise* luminosity uncertainty
- **Dedicated** set of detector calibration and performances



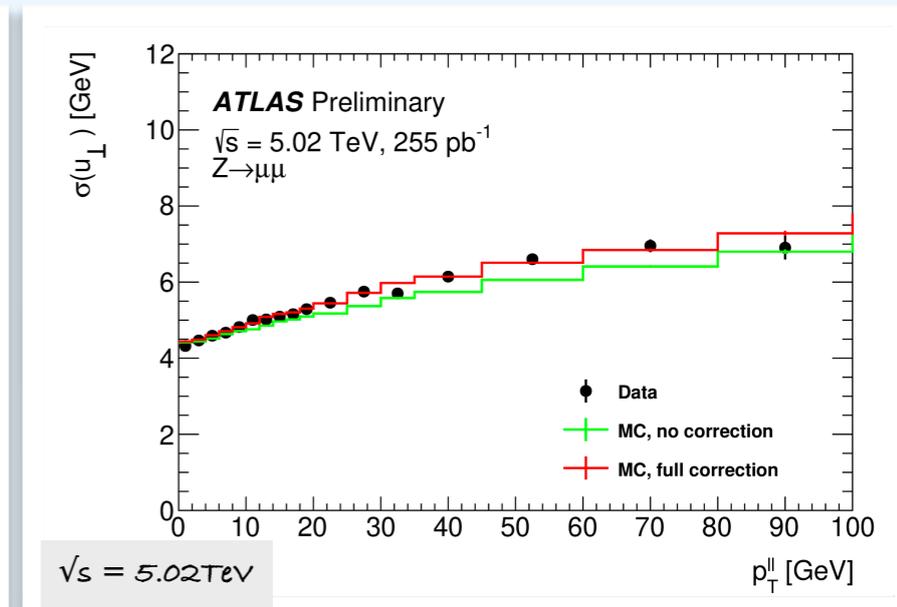
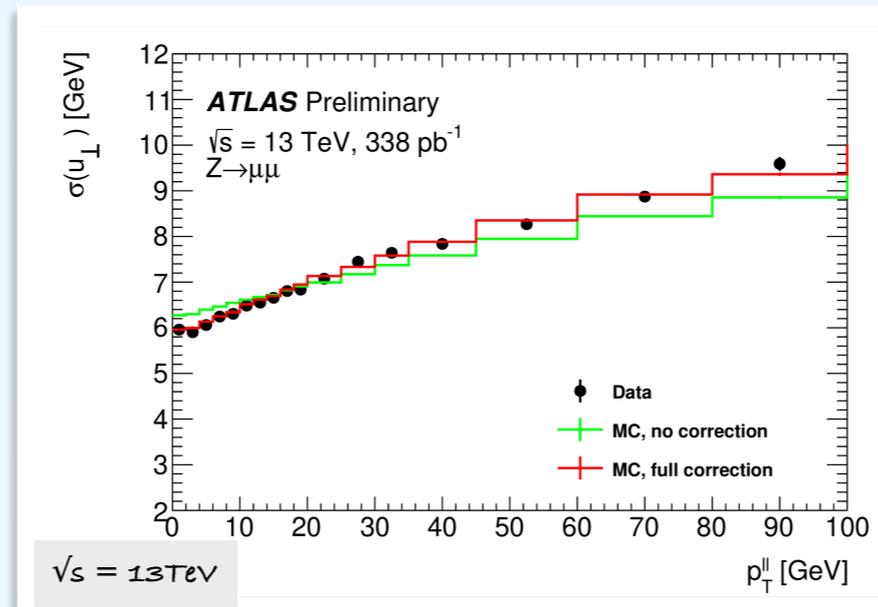
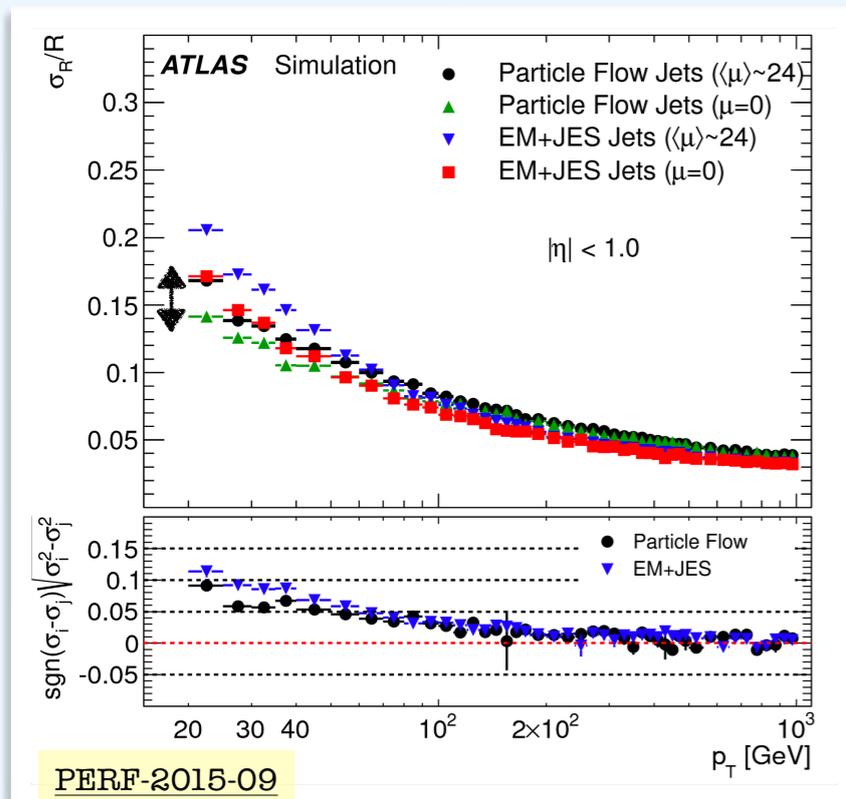
wherever possible extrapolated high- μ to low- μ conditions

leptons performance accuracy limited by the Z sample statistic

Hadronic recoil performances



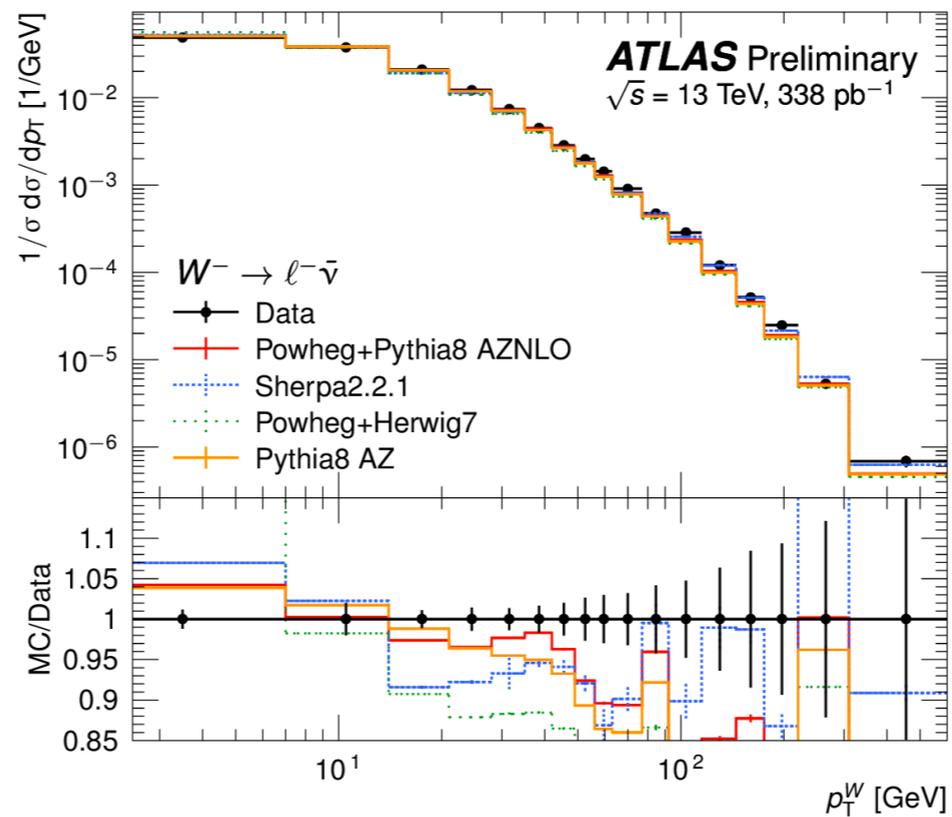
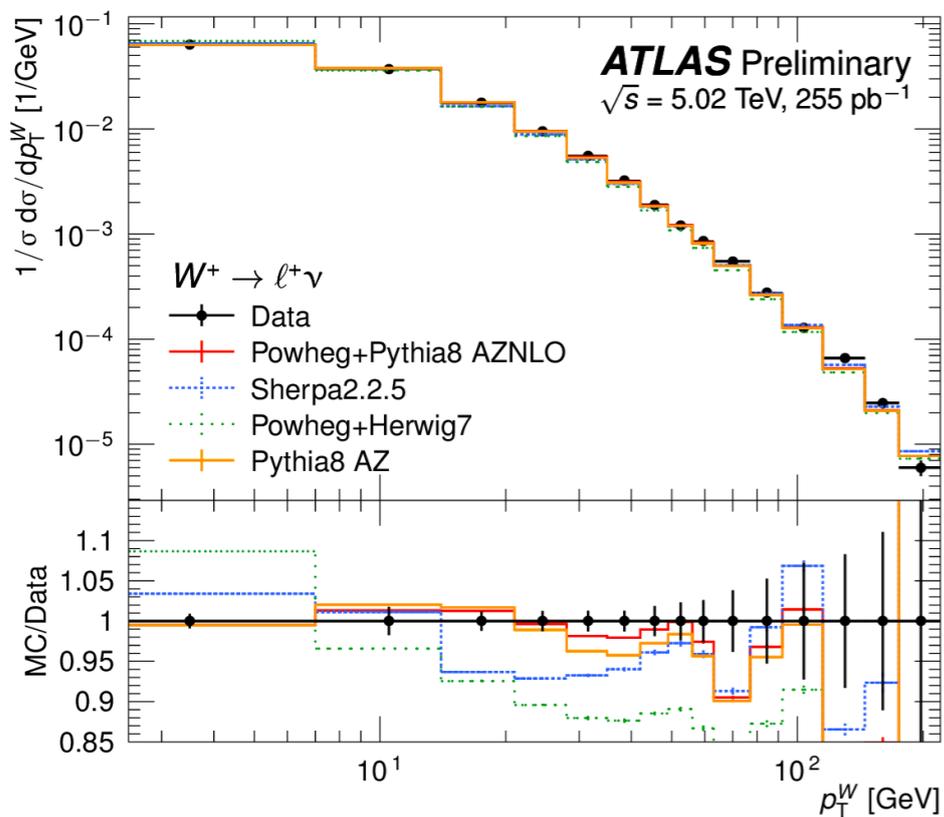
A) Particle flow objects (PFOs) for recoil reconstruction up to 5% improvement in resolution



B) in-situ in $Z \rightarrow \ell\ell$ events used to **Calibrate** the recoil response:

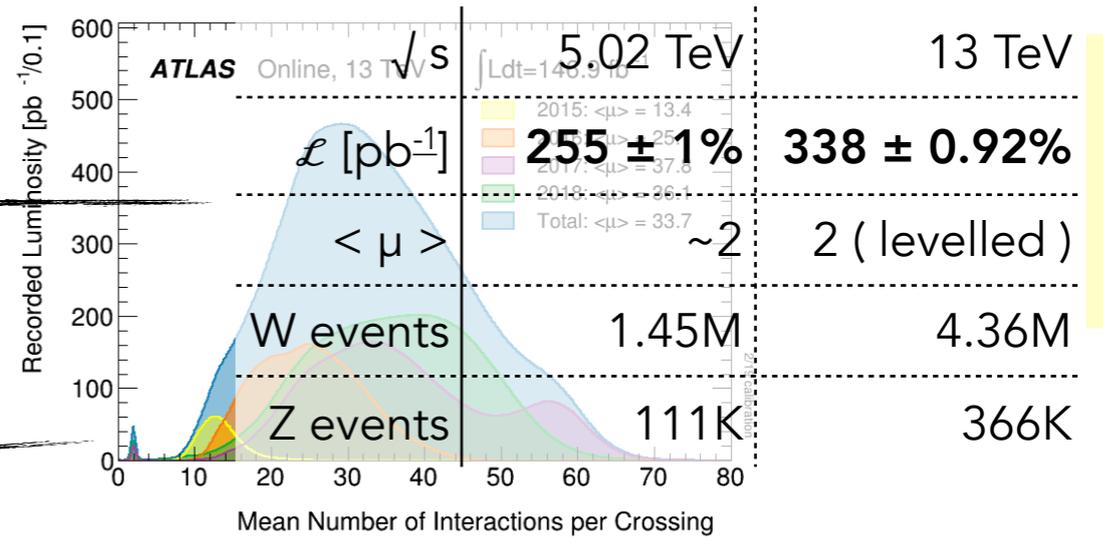
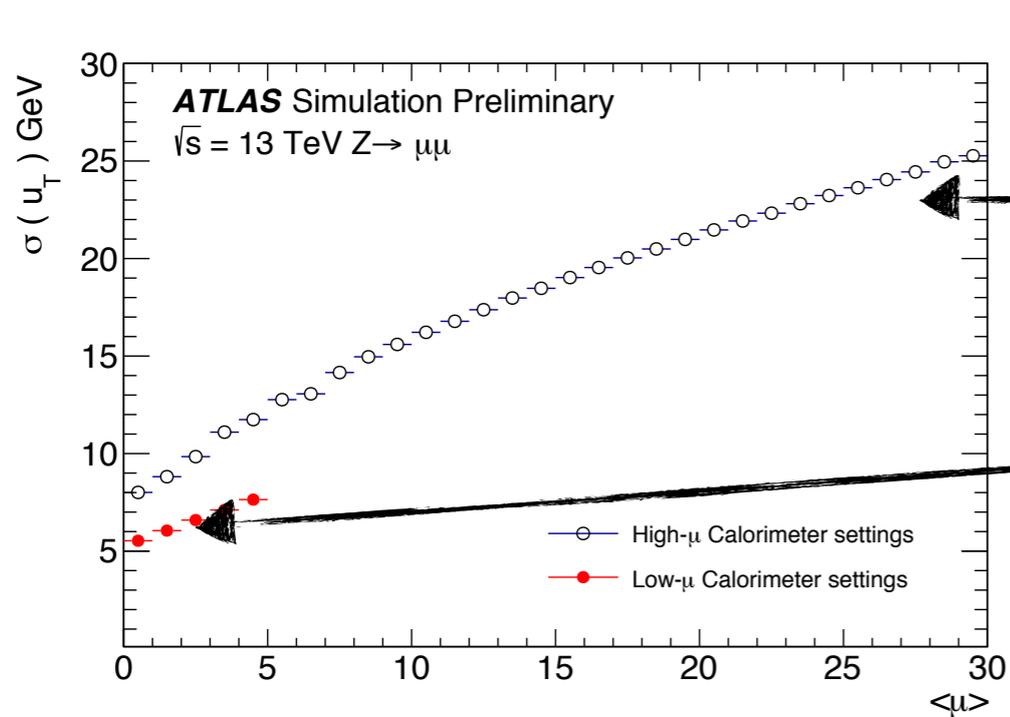
- ▶ Modelling of underlying activity from data
- ▶ Correcting response non-uniformity in the calorimeter (beam displacement, beam-crossing angle, azimuthal angle)
- ▶ Equalising response and resolution differences between data/MC
- ▶ Correcting for residual non-Gaussian tails in the response

Hadronic-recoil uncertainties have sub-percent level impact on $p_T^W < 50 \text{ GeV}$ (@ 5TeV limited stat of the Z samples is the dominant source)



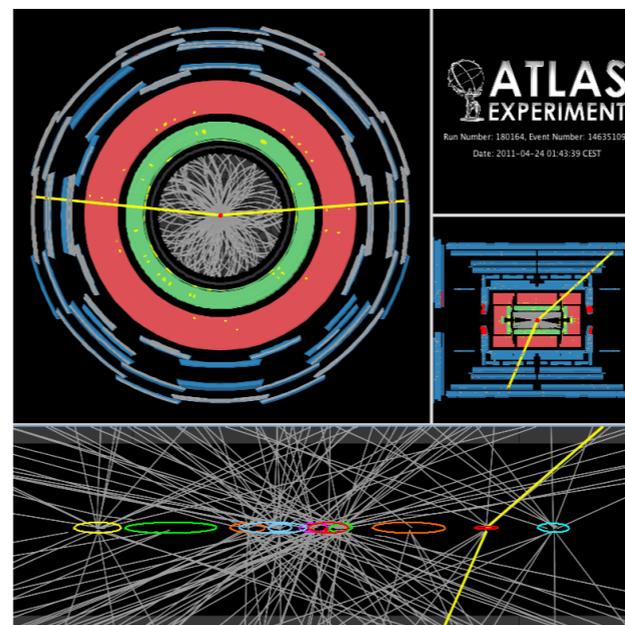
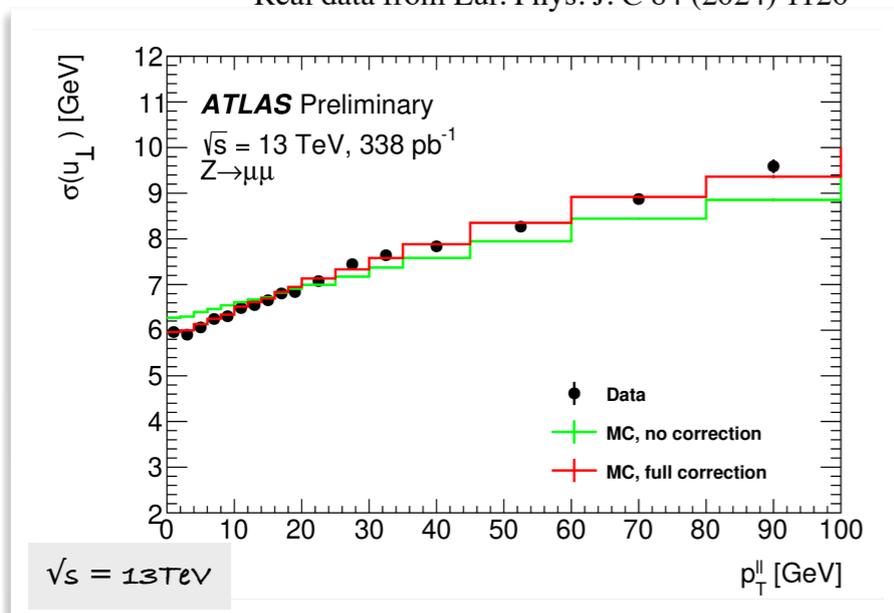
The p_T^W measurement

Low mu

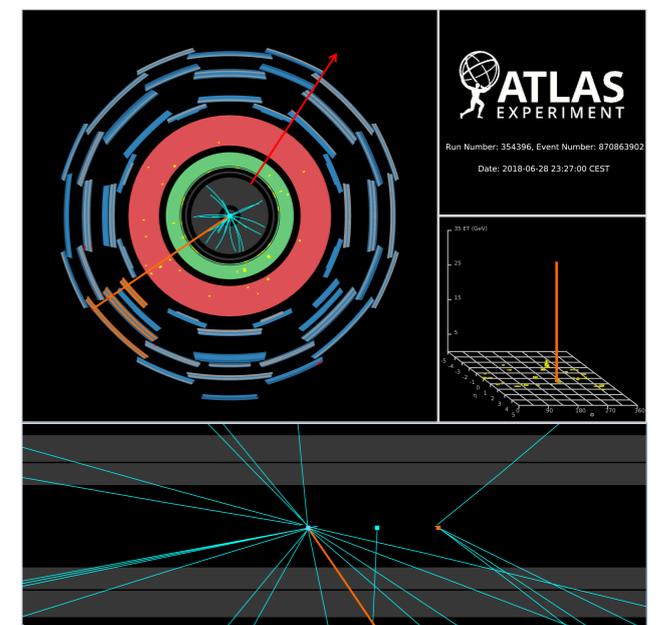


Run2-luminosity

Real data from Eur. Phys. J. C 84 (2024) 1126



9 additional reconstructed vertices



2 additional reconstructed vertices

W_{p_T} measurements

Detector level distributions unfolded at particle level in fiducial volume:

lepton $p_T > 25$ GeV
 lepton $|\eta| < 2.5$
 W : $p_T > 25$ GeV ; $m_T > 50$ GeV
 Z : $66 < m_{\ell\ell} < 116$ GeV

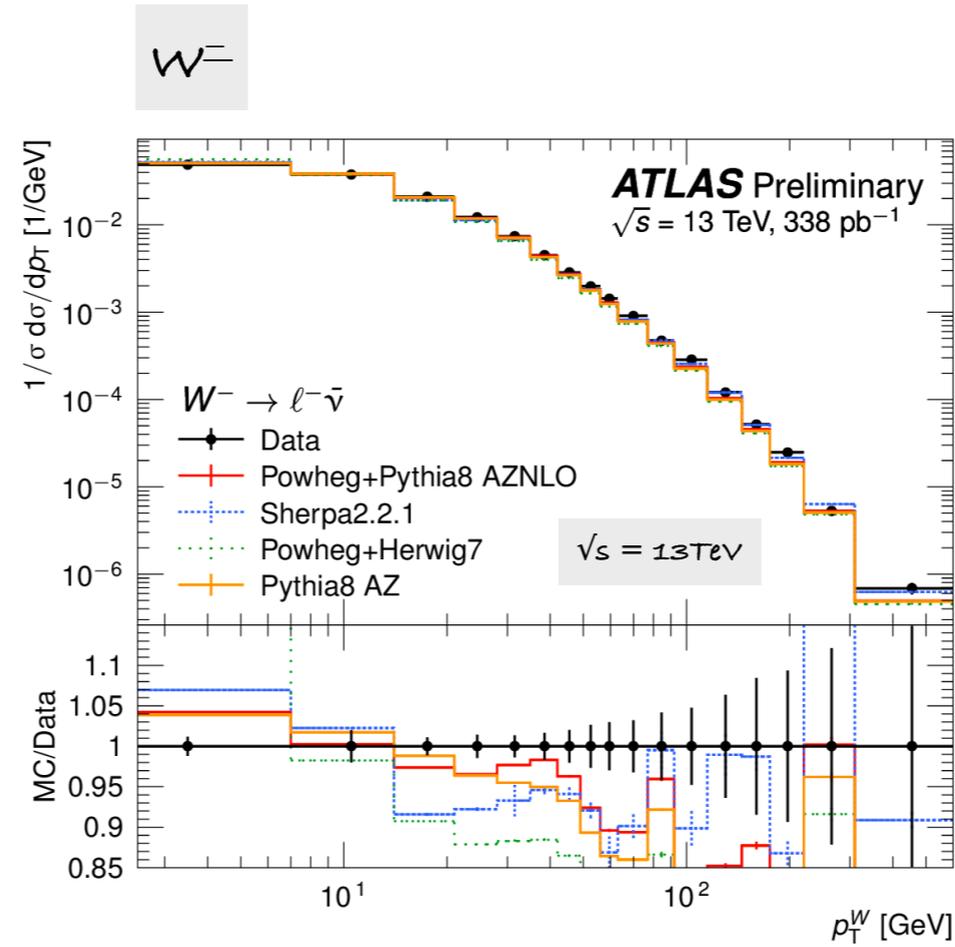
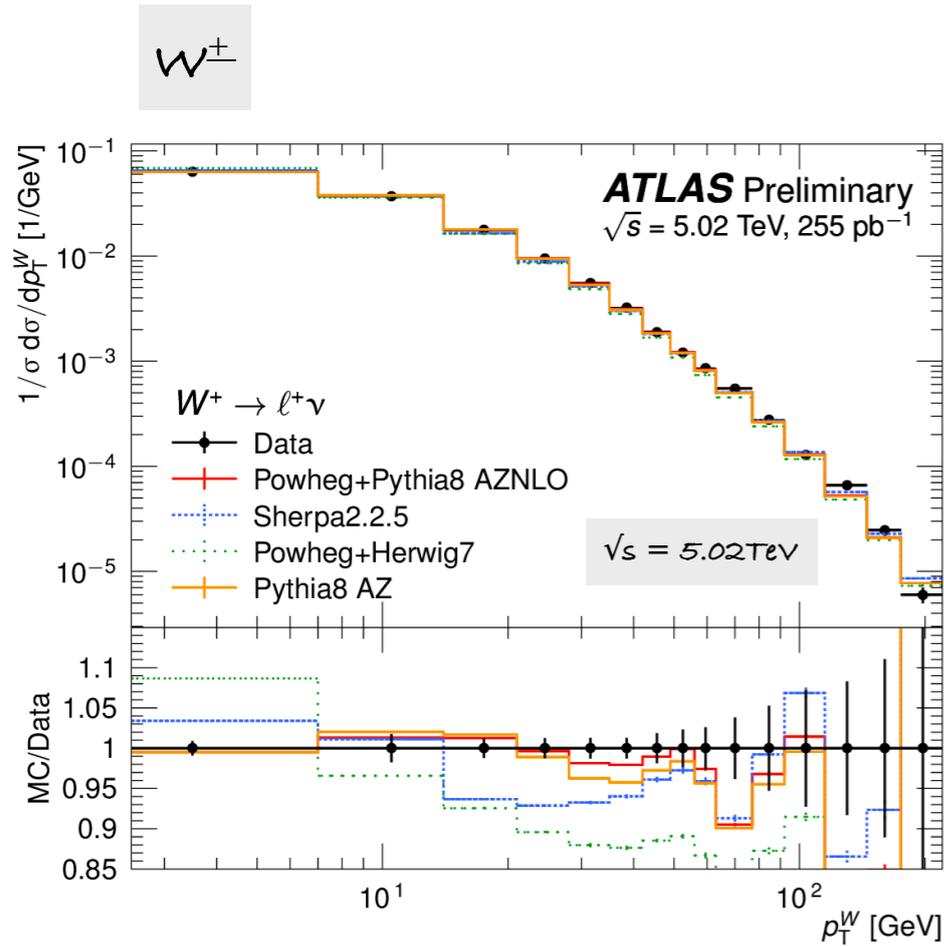
- ▶ **Bayesian unfolding** of $u_T(W)$; p_T^{Z} (Z) , separately for e/ μ channels
 - ▶ Bin width/iterations **optimise to reduce uncertainty of unfolding prior bias**
 - ▶ 9 (25) iterations, 7 GeV bin at low p_T^W at 5.02 (13) TeV
 - ▶ 2 iterations, 2 GeV bin width at low p_T^Z
- ▶ electron and muon channels combined with BLUE, all giving good χ^2

Most precise integrated fiducial measurement of the W^\pm and Z boson @ 5.02 and 13 TeV:

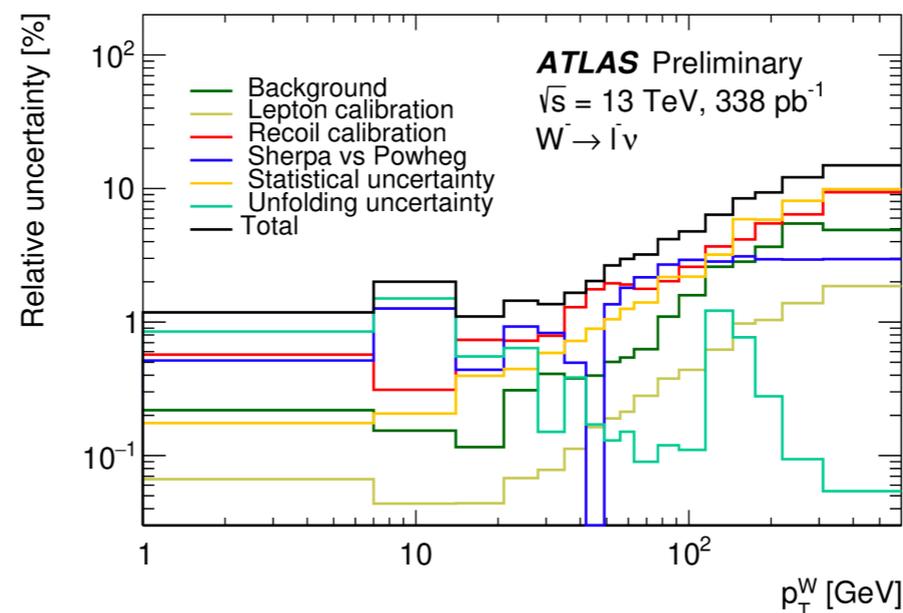
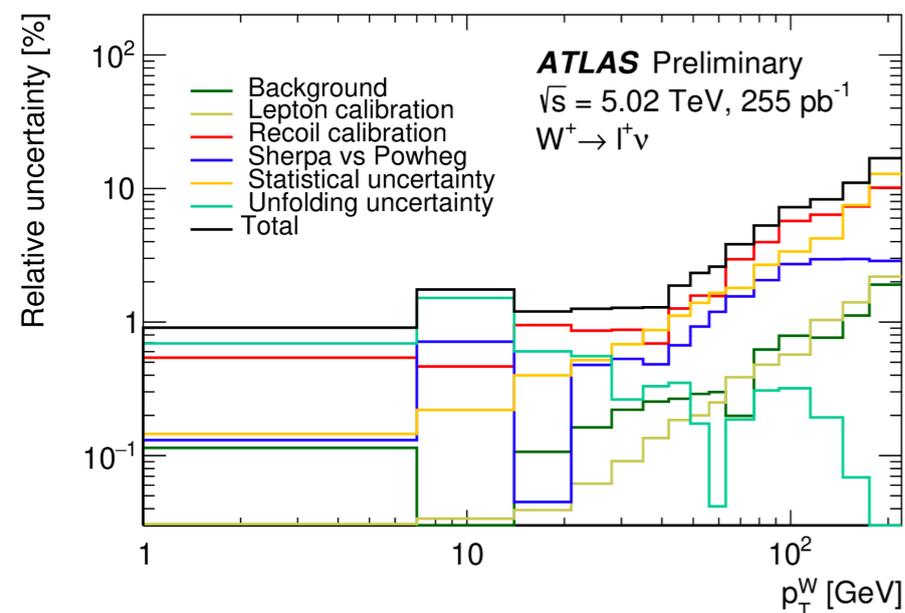
| Process | Cross section at $\sqrt{s} = 5.02$ TeV [pb] | Cross section at $\sqrt{s} = 13$ TeV [pb] |
|--------------------------|------------------------------------------------------------|------------------------------------------------------------|
| $W^- \rightarrow l\nu$ | 1385 ± 2 (stat.) ± 5 (sys.) ± 15 (lumi.) | 3486 ± 3 (stat.) ± 18 (sys.) ± 34 (lumi.) |
| $W^+ \rightarrow l\nu$ | 2228 ± 3 (stat.) ± 8 (sys.) ± 23 (lumi.) | 4571 ± 3 (stat.) ± 21 (sys.) ± 44 (lumi.) |
| $Z \rightarrow \ell\ell$ | 333.0 ± 1.2 (stat.) ± 2.2 (sys.) ± 3.3 (lumi.) | 780.3 ± 2.6 (stat.) ± 7.1 (sys.) ± 7.1 (lumi.) |

experimental accuracy 0.4 - 0.5 % with 1% lumi
 factor of 2 (3.5) better than previous W X-section at 5.02 (13 TeV)
 good agreement with DYTURBO [NNLO+NNLL] prediction with 3 different PDF sets

W^\pm and W^\pm transverse momentum measurement

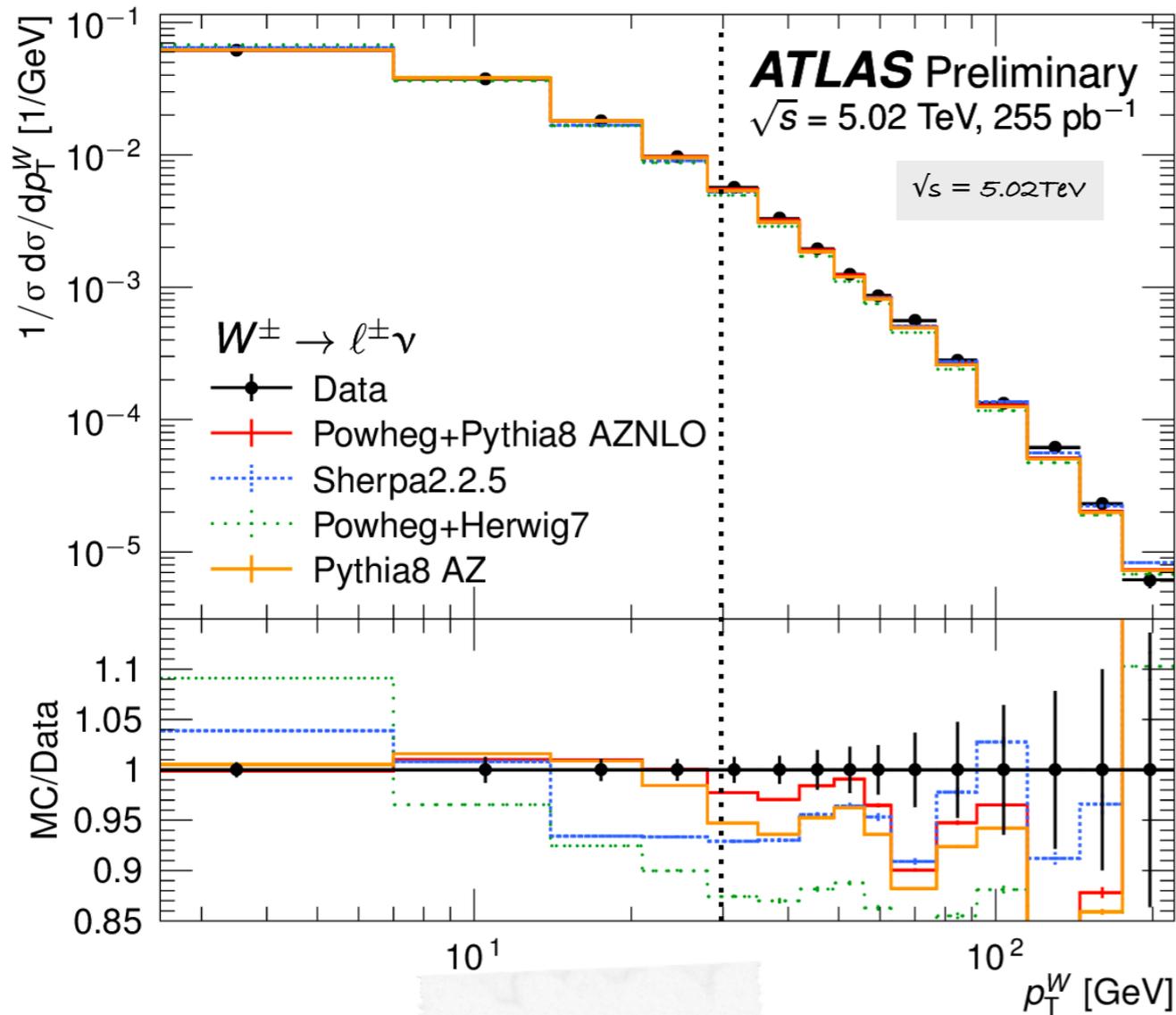


► Normalised differential distributions in data are compared to several predictions

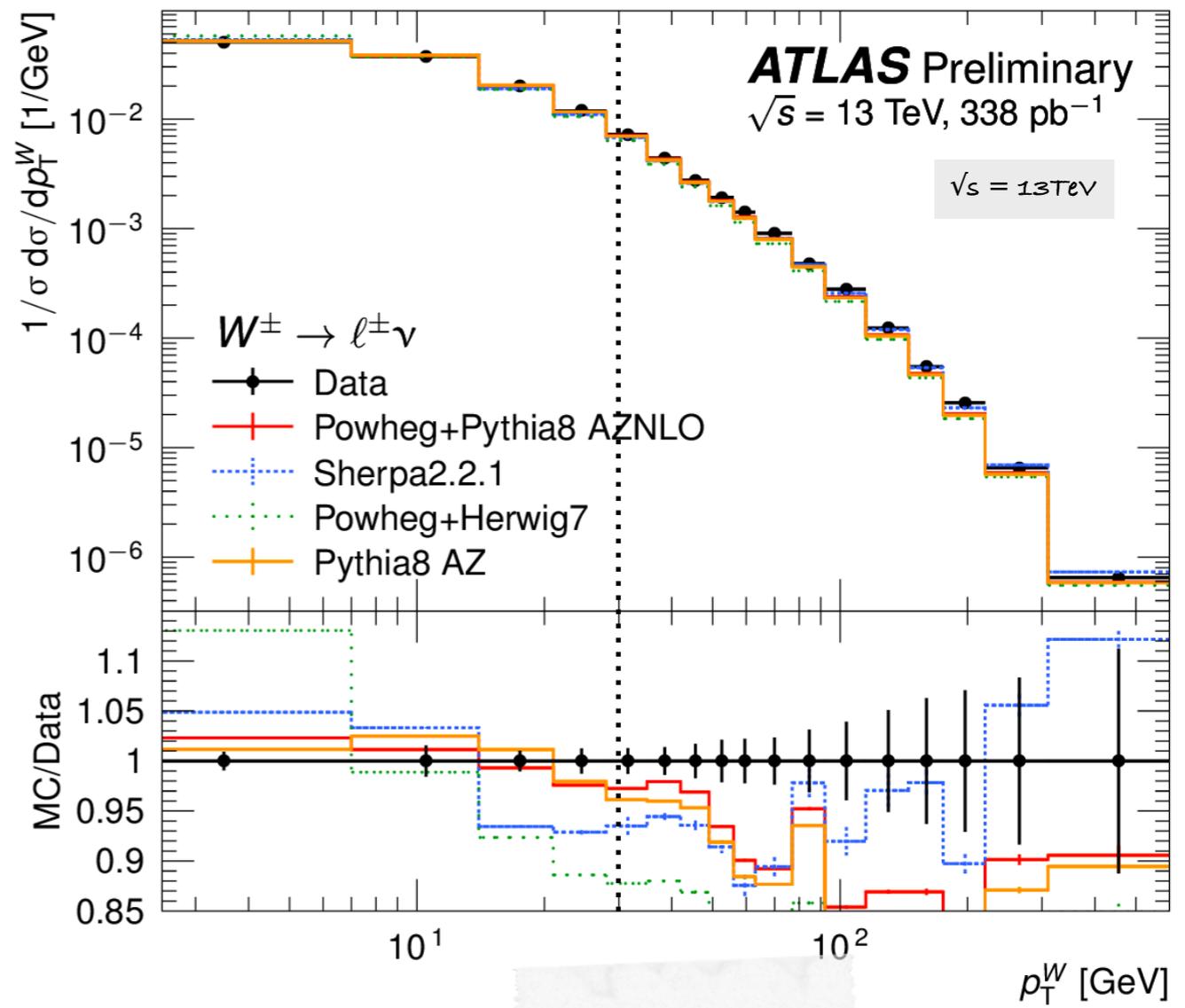


overall data precision:
 $\sim 1\%$ at low p_T ,
 $\sim 10\%$ towards the end of the spectrum.

Validation of the m_W physic modelling

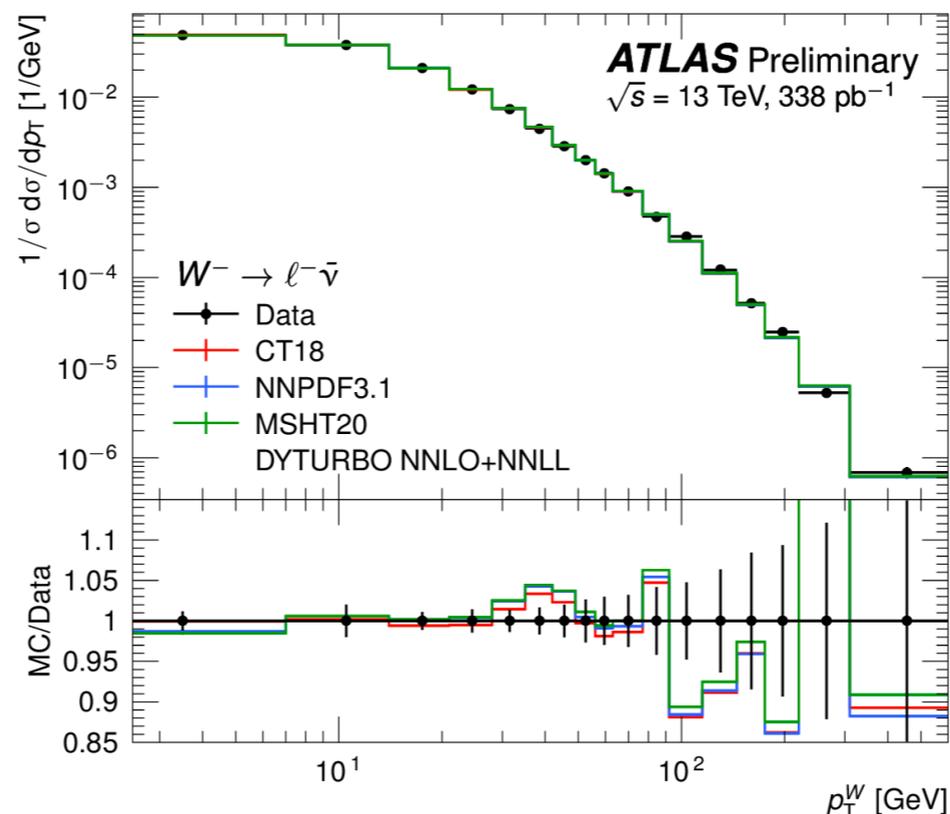
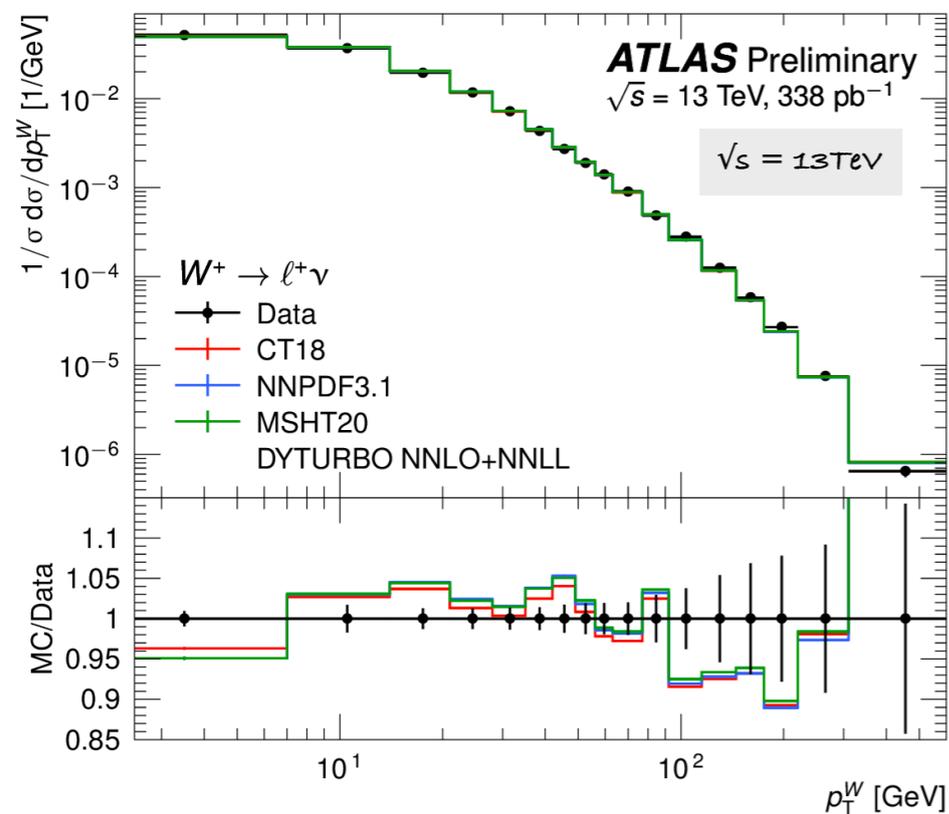
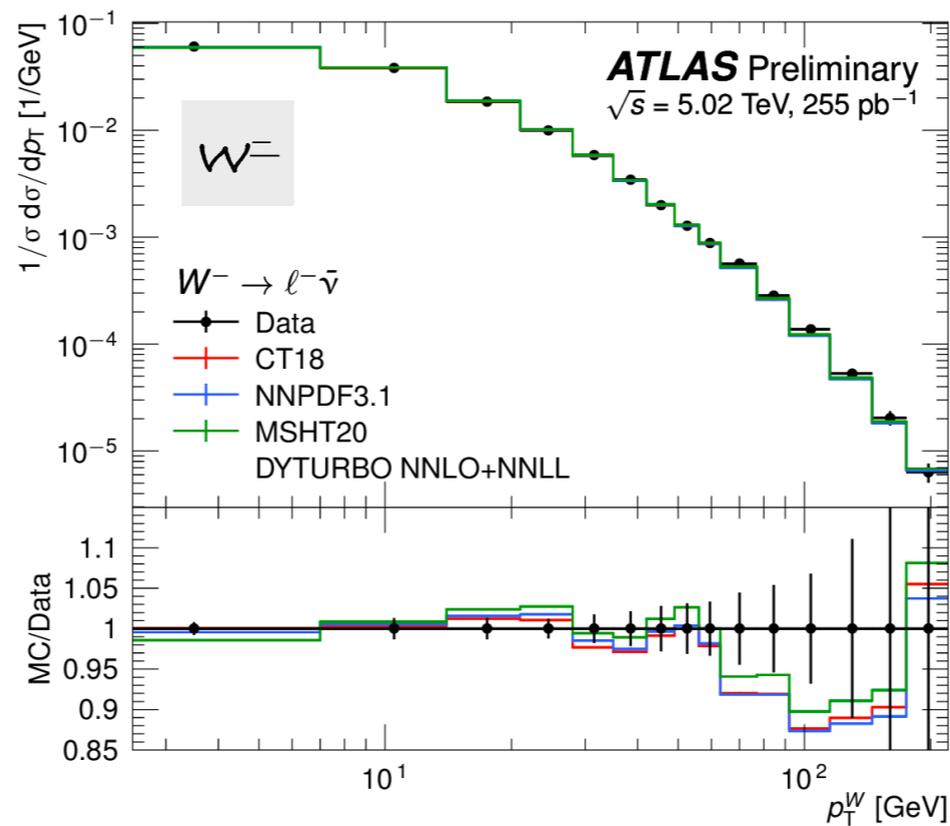
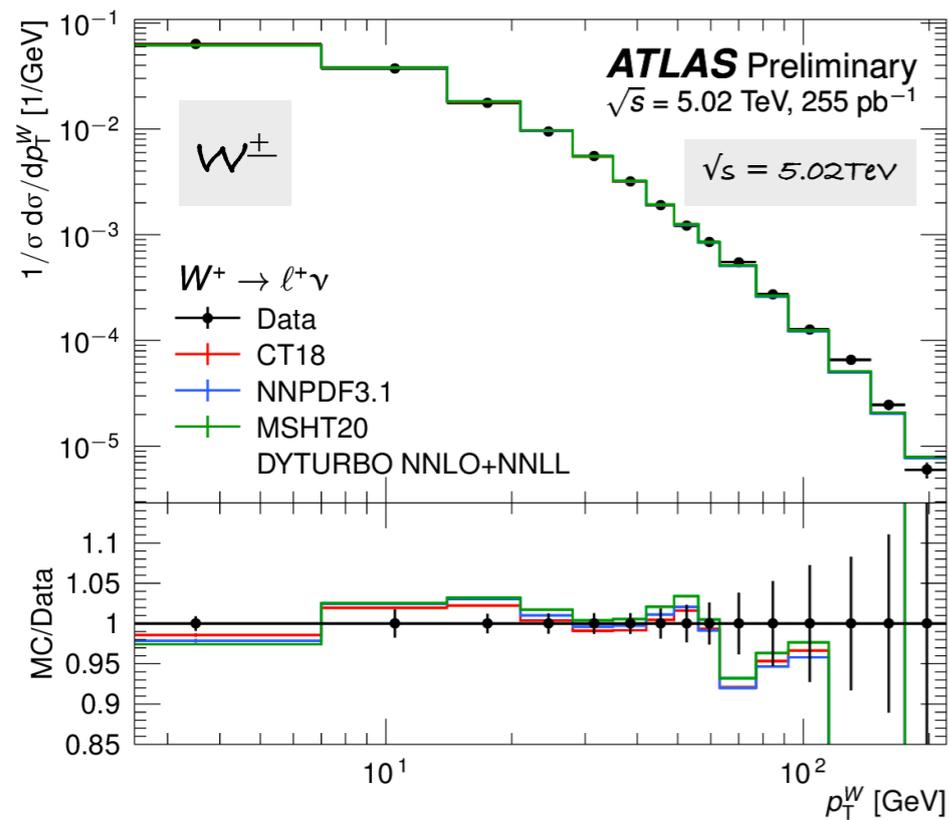


*W mass p_T^W physics modelling
 [Powheg+Pythia 8 AZNLO ;
 Pythia 8 AZ] describe well the
 data in the low- p_T region @5TeV*



*W mass p_T^W physics modelling
 [Powheg+Pythia 8 AZNLO ; Pythia
 8 AZ] a bit worst agreement @13TeV
 => PS retuning needed.*

W^\pm and W^- transverse momentum measurement

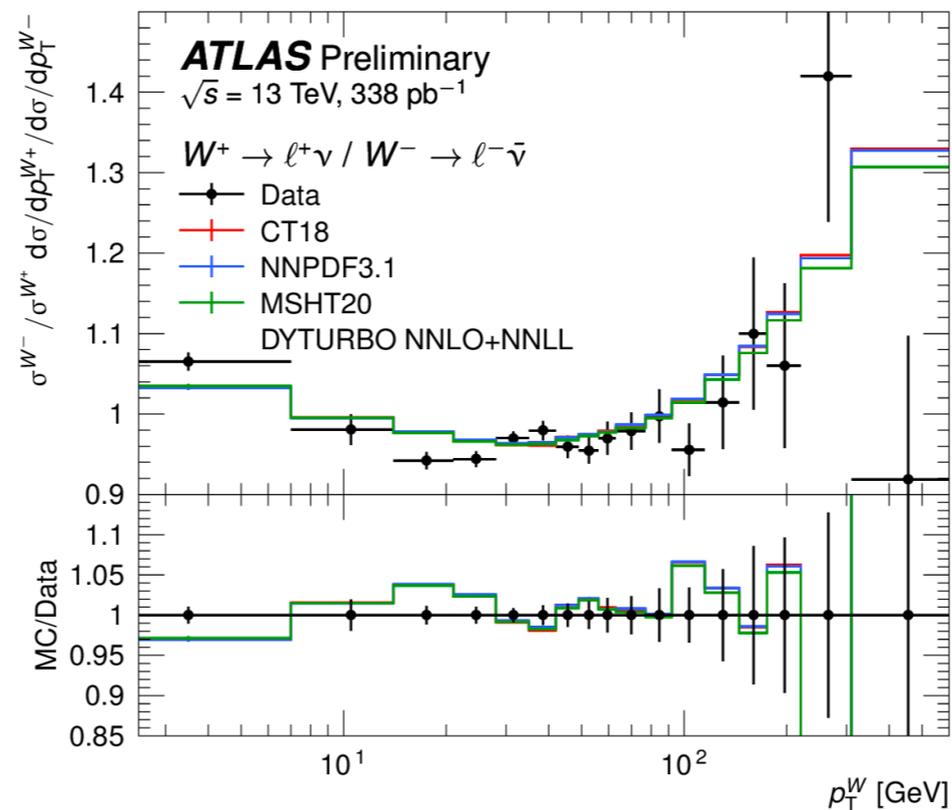
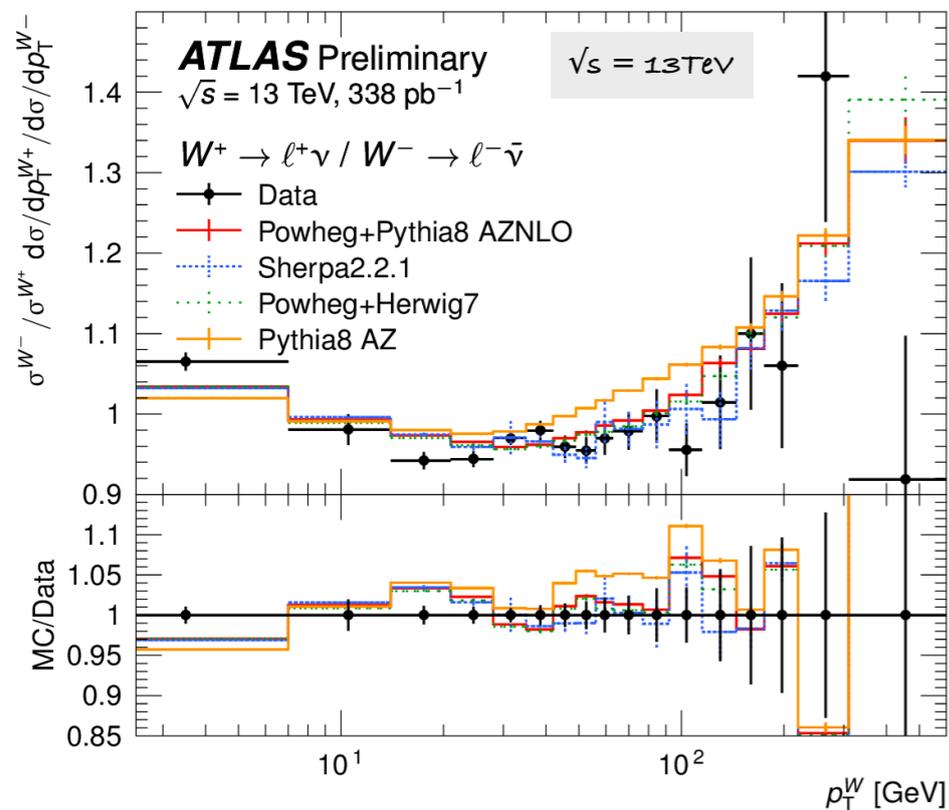
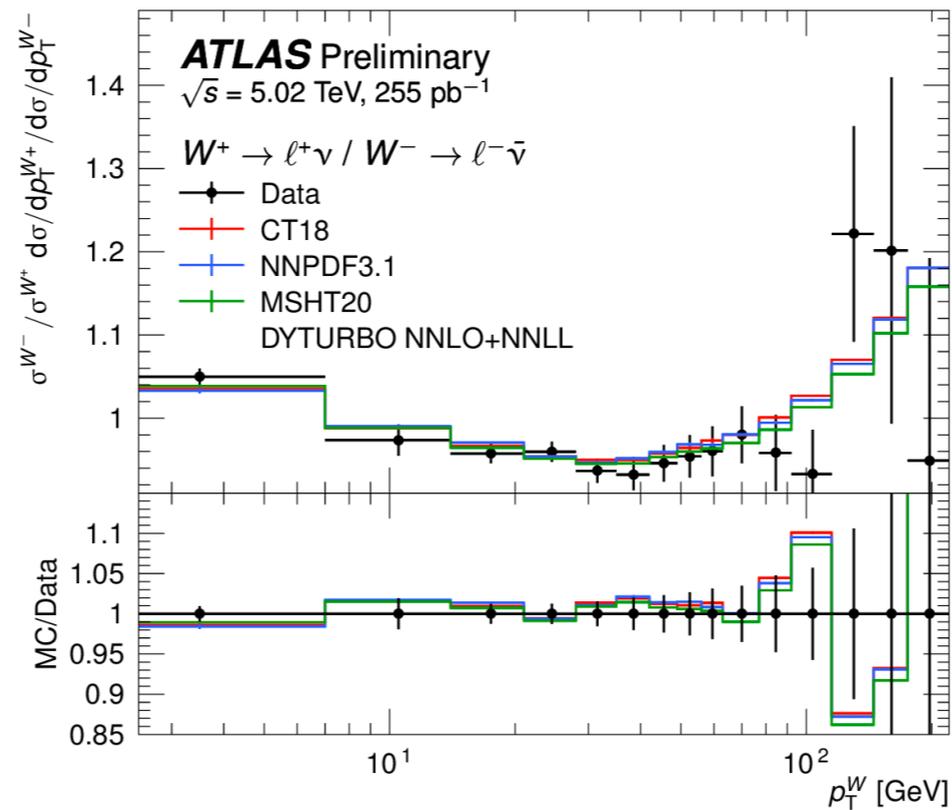
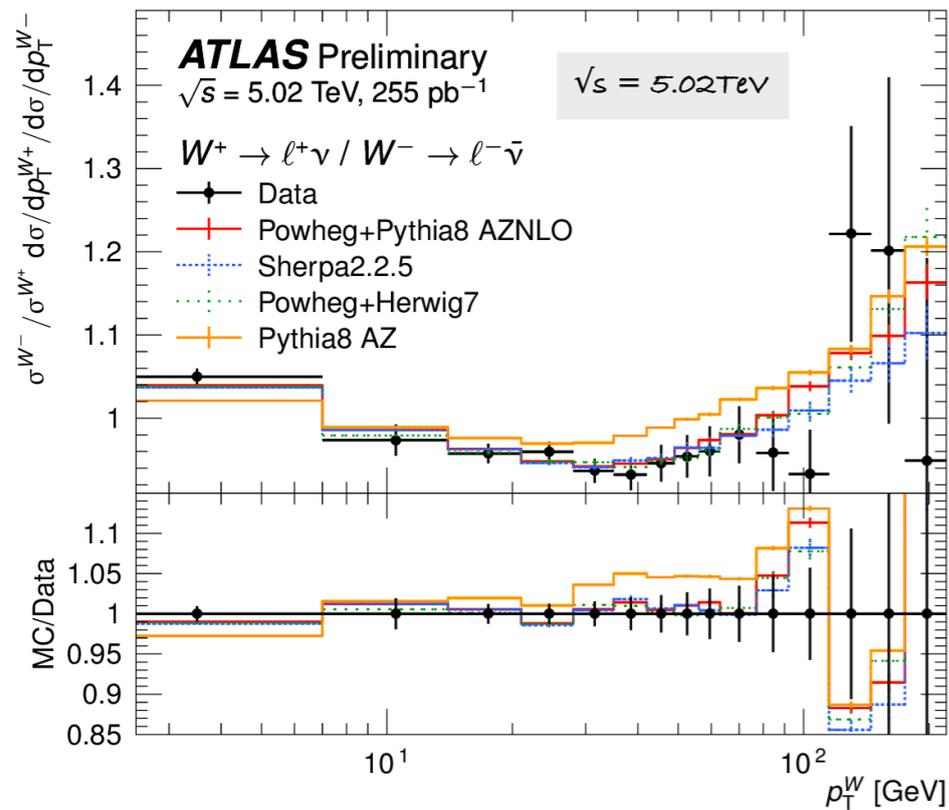


► Data distributions are compared with DYTURBO predictions [NNLO + NNLL]

► Effect of PDF estimate comparing 3 recent PDF sets

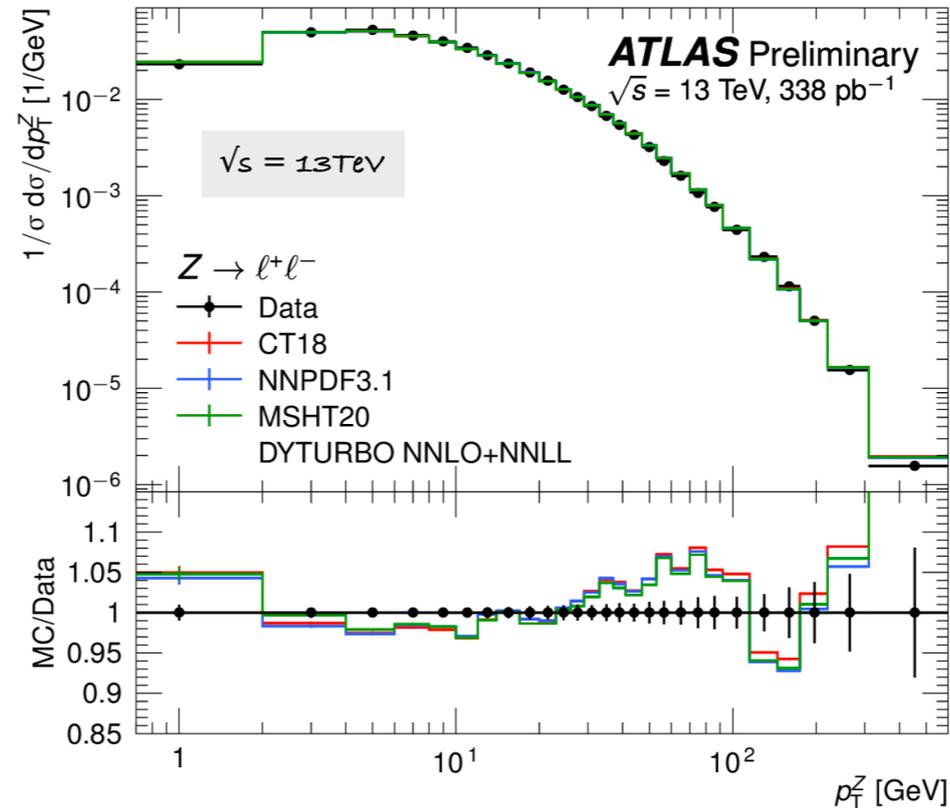
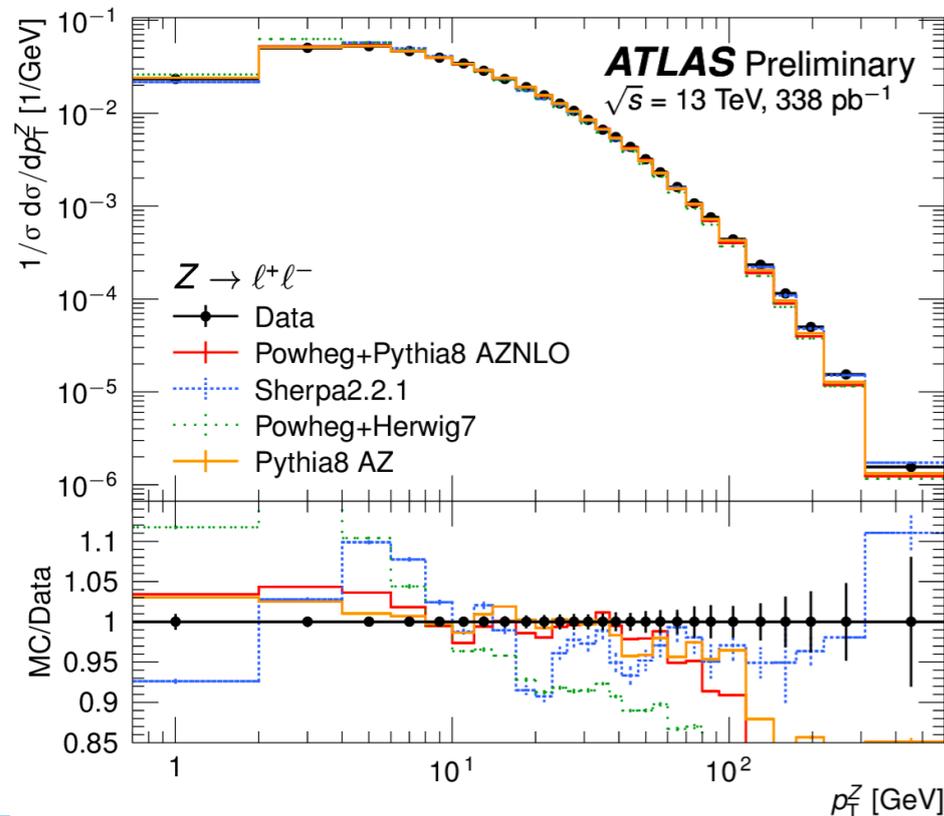
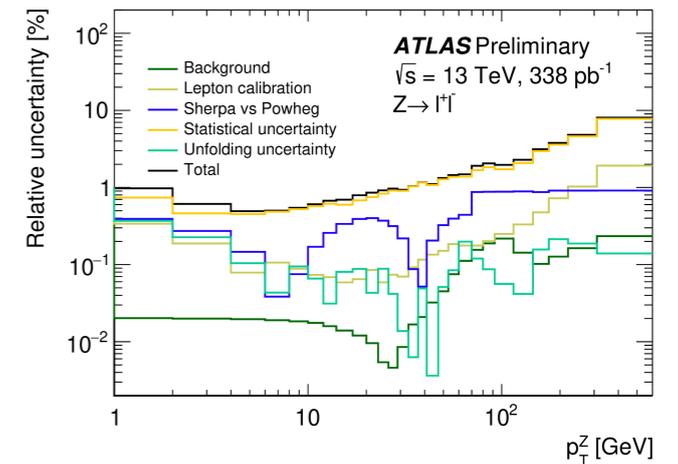
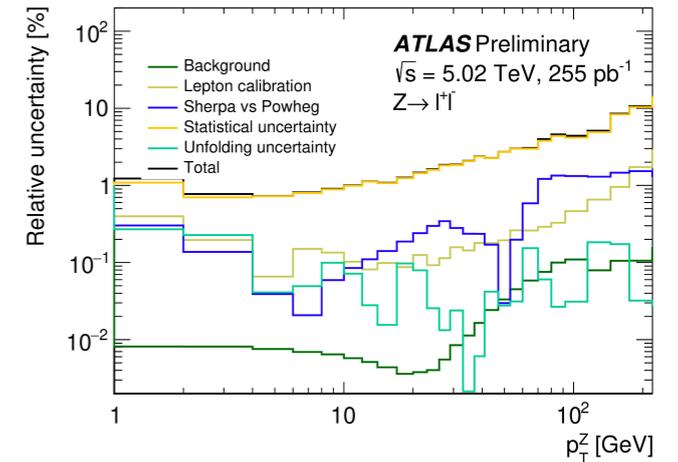
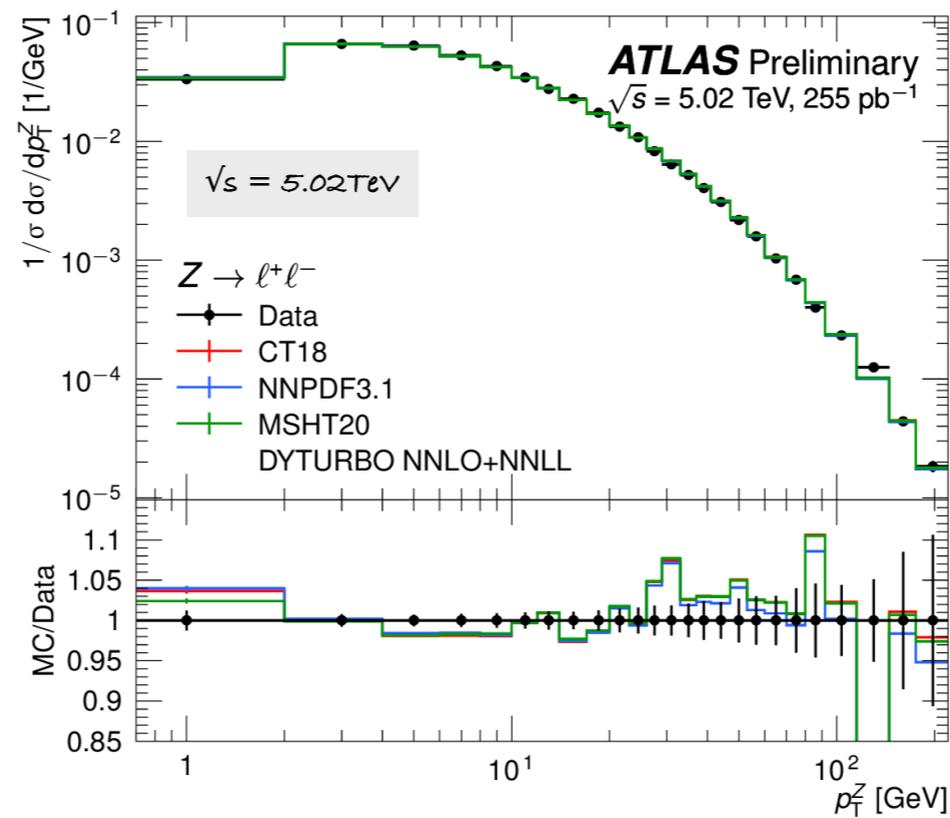
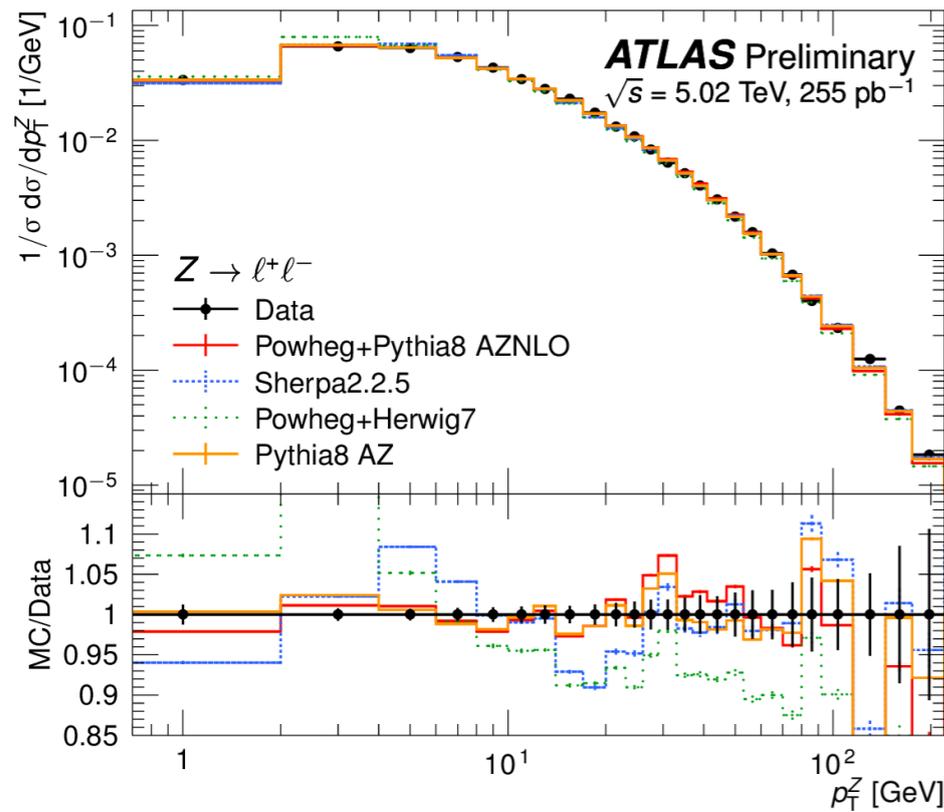
reasonable good agreement in the whole spectra
→ showing the improvements on analytic resummation programs!

W^\pm / W^\mp ratio



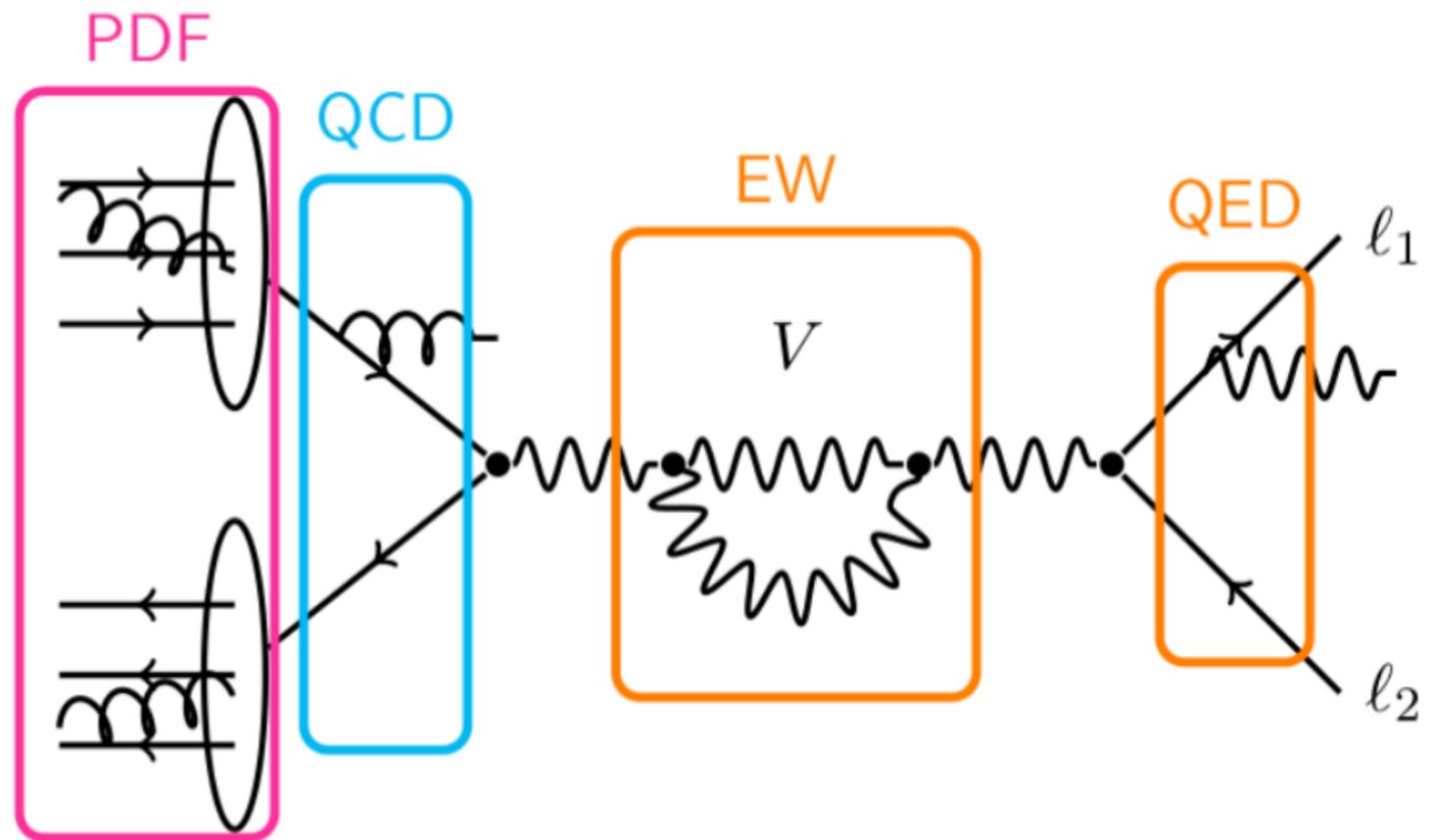
The W^+ / W^- ratio is expected to be relatively insensitive to universal resummation effects, but the low- p_T range is sensitive to the different initial quark flavours. Exp precision $\sim 1\%$

Z transverse momentum differential measurement



The comparison to MC sample/resummed predictions shows a variety of deficiencies most of which are common for all vector bosons. The agreement is better at $\sqrt{s} = 5.02 \text{ TeV}$

Physics Modelling



reminder limiting factor in the legacy 2018 first mW ATLAS publication

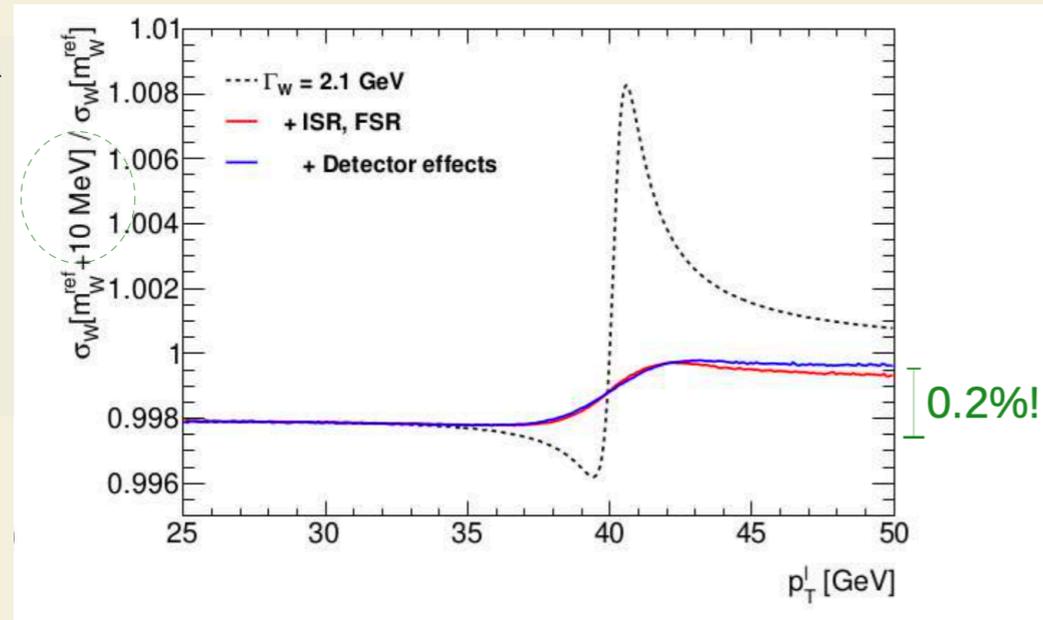


$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T)}{dp_T} \right] \left[(1 + \cos^2\theta) + \sum_{i=0}^7 A_i(p_T, y, m) P_i(\cos\theta, \phi) \right]$$

Complexity of the physics modelling



credit to M. Boonekamp



- ▶ < 10 MeV precisions required ~0.1-0.2% control on the kinematics of the W production
- ▶ sub-percent accuracy of predictions for PDF ; p_T^W modelling and W polarisation (A_i) is extreme challenge for QCD theory!

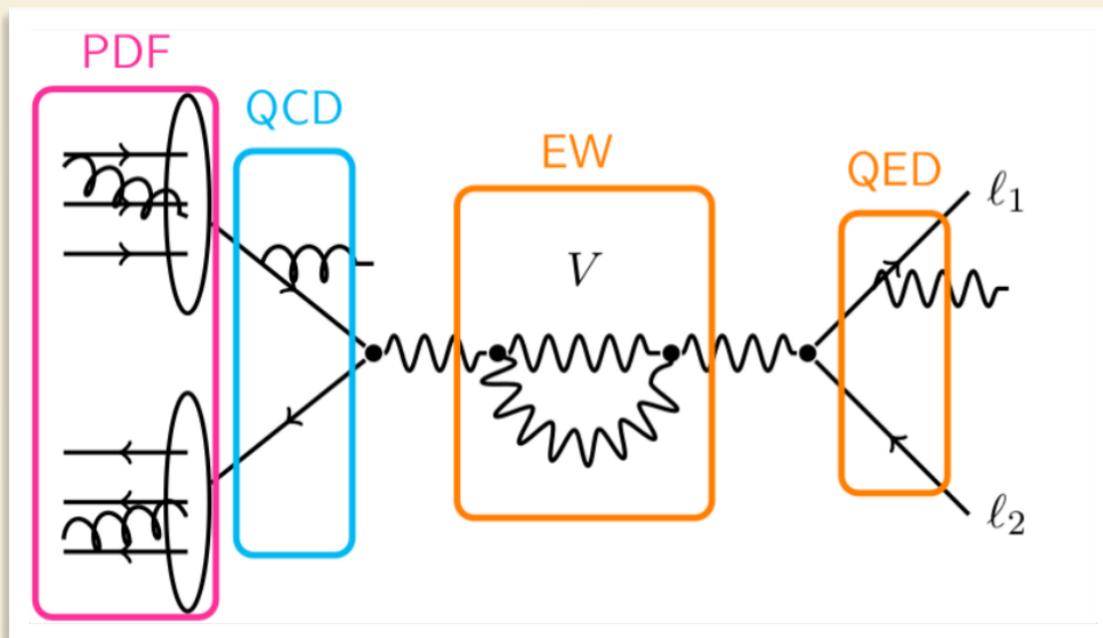


- ▶ @LHC W mass physics modelling is described using a **composite model** :
- ▶ Start from the NLO/NNLO generators + LL parton-shower (Powheg+Pythia8) and apply corrections to reach the state of the art accuracy.
 - ▶ The Drell-Yan cross-section can be decomposed by **factorising** the dynamic of the boson production and the kinematic of the boson decay.

$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T)}{dp_T} \right] \left[(1 + \cos^2\theta) + \sum_{i=0}^7 A_i(p_T, y, m) P_i(\cos\theta, \phi) \right]$$

Use **ancillary measurements** of Drell-Yan processes to validate (and tune) the model and assess systematic uncertainties.

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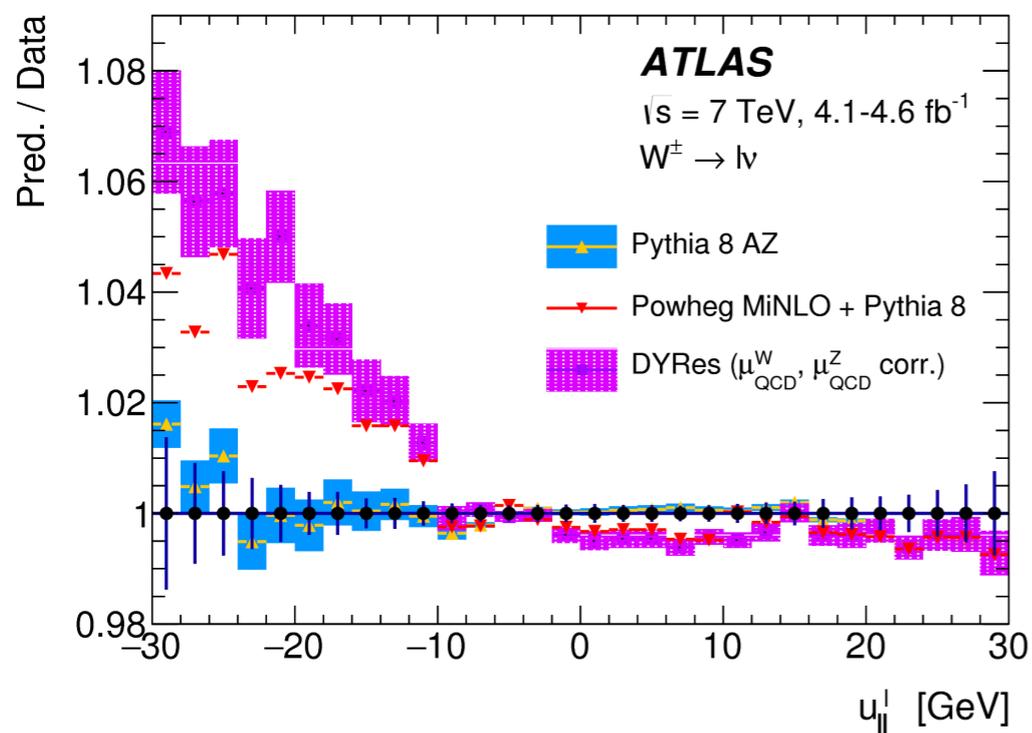
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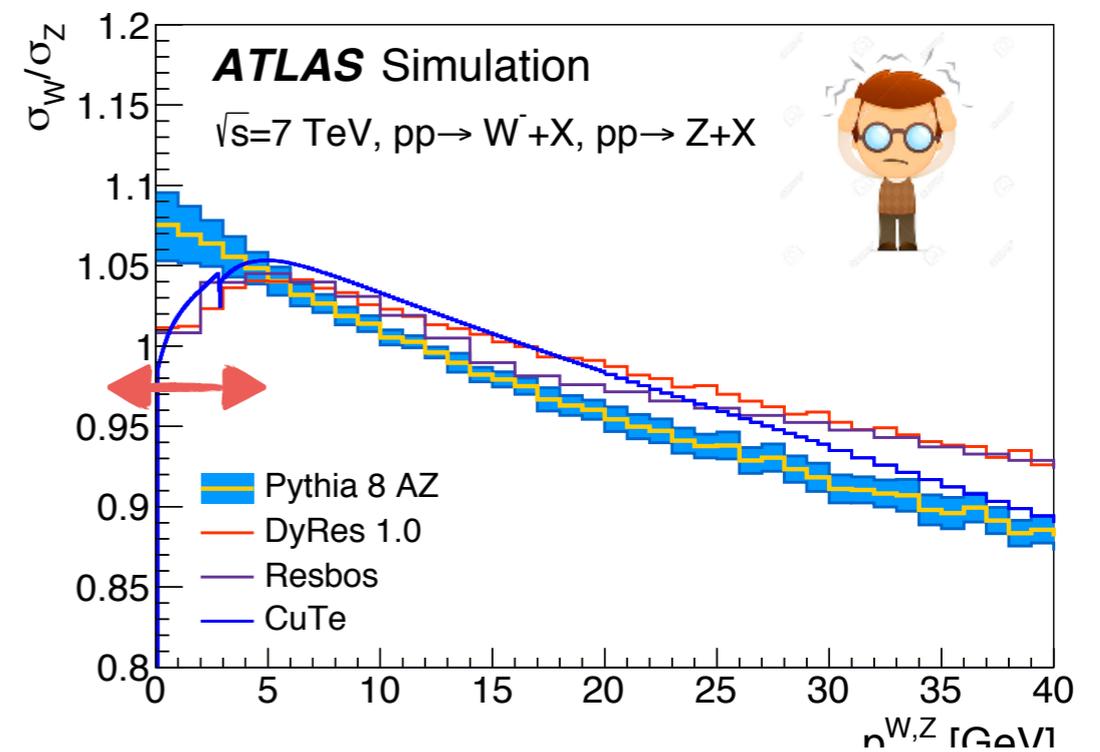
The p_T^W modelling

- ▶ p_T^W modelling is a challenge for QCD theory (resummation, heavy flavour, multiple scale, no pQCD)
 - ▶ Experimentally very precise p_T^Z measurement (W limited by recoil resolution)
- ▶ Approach: adjust model parameters using Z events → extrapolate to W production

$$R_{W/Z}(p_T) = \left(\frac{1}{\sigma_W} \cdot \frac{d\sigma_W(p_T)}{dp_T} \right) \left(\frac{1}{\sigma_Z} \cdot \frac{d\sigma_Z(p_T)}{dp_T} \right)^{-1}$$



@time of the first measurement: analytic resummed predictions were **strongly disfavoured** by the recoil distribution in data.



+

@time of the first measurement: low p_T^Z W/Z ratio very different between analytic resummed predictions and PS model tuned with Z data

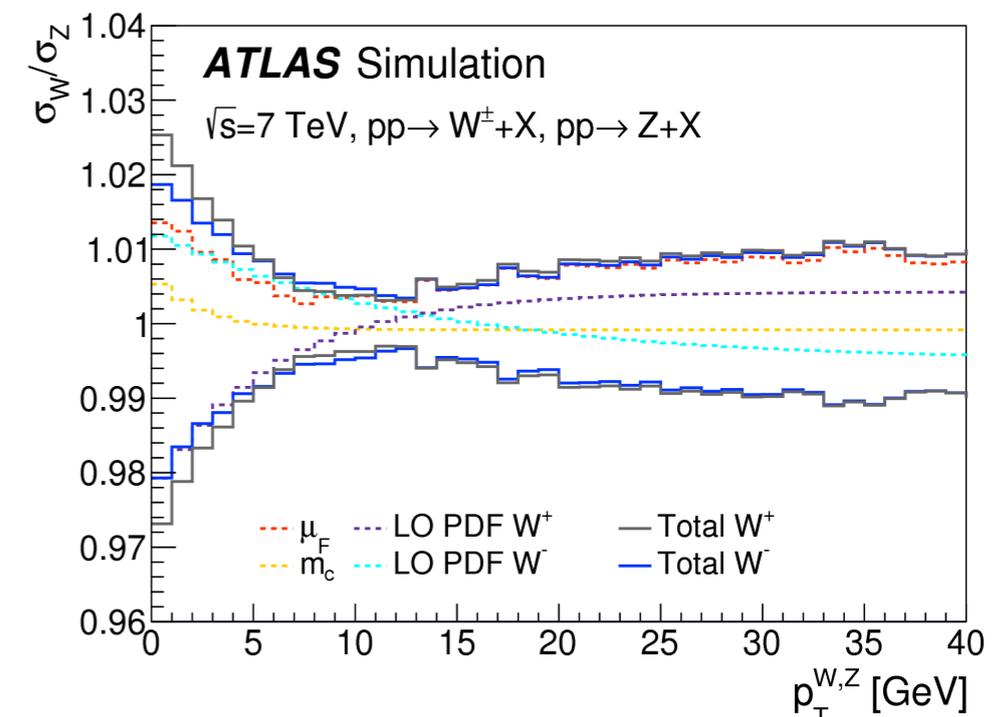
Addressing the difficulties of p_T^W modelling

- ▶ p_T^W modelling is a challenge for QCD theory (resummation, heavy flavour, multiple scale, no pQCD)
 - ▶ Experimentally very precise p_T^Z measurement (W limited by recoil resolution)
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ATLAS m_W $d\sigma/dp_T$ modelling uses Pythia parton shower

- ▶ PS parameters tune on **7TeV p_T^Z data** (AZ tune)
- ▶ Fairly good modelling of the W-data, **but hard to improve on uncertainties** (mostly related to model limitations)





CMS modelling strategy

“agnostic” approach eg. rely on constraining power of the DATA

- **Overall strategy:** construct the best possible theoretical model for the W and constrain in-situ directly with the W data

- Z data is “only” used for validation

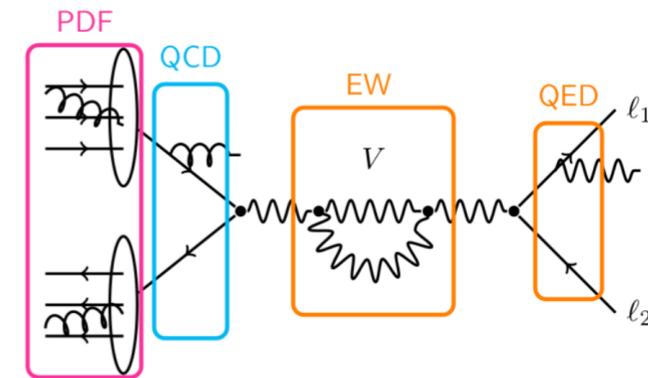
- **Nominal Theory uncertainties:**

- Perturbative QCD

- PDFs

- Additional non-perturbative QCD (e.g. transverse momentum of partons within proton)

- Electroweak effects



similar decomposition as ATLAS

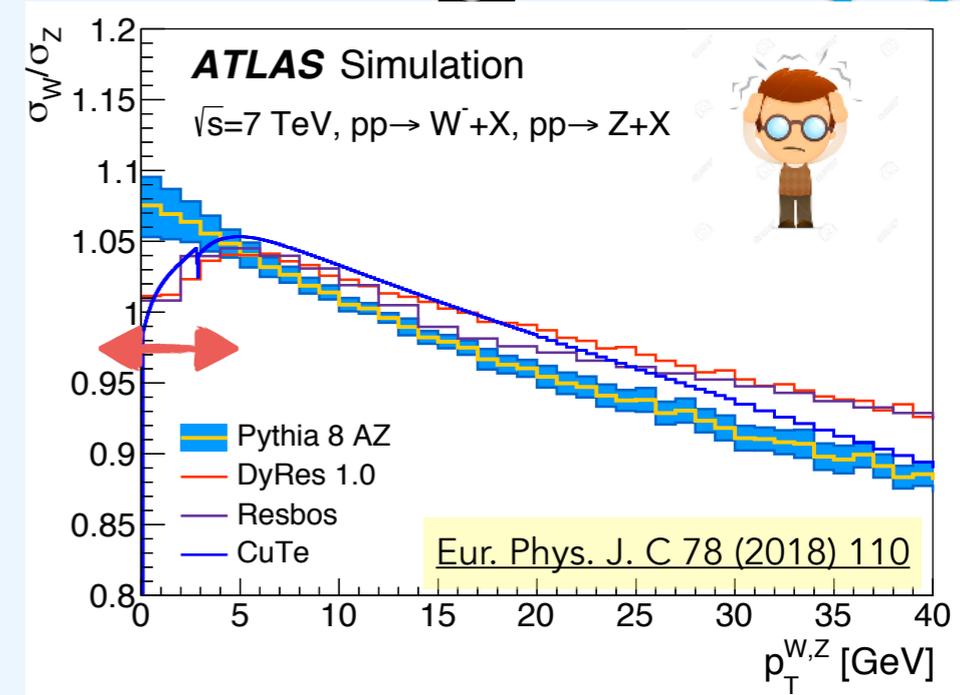
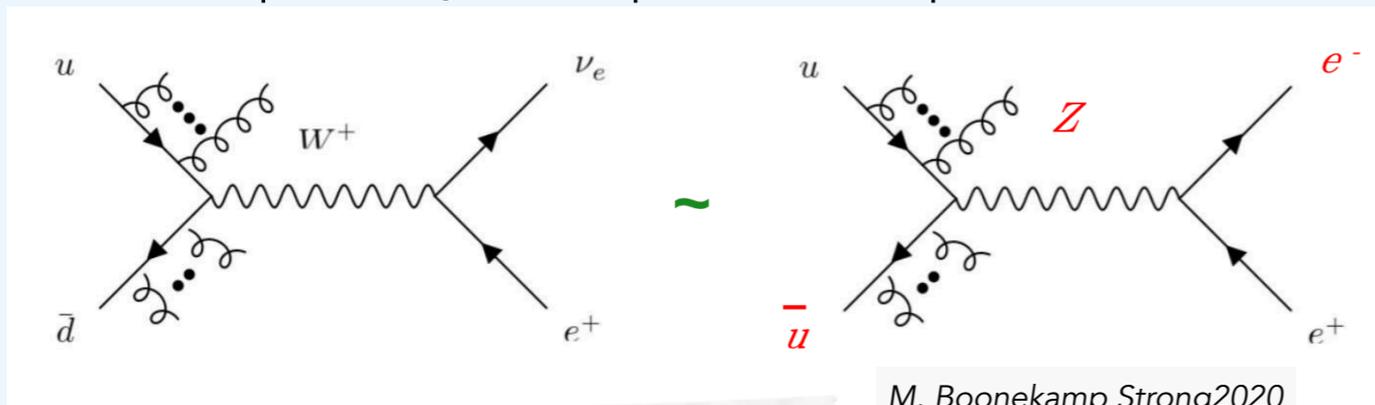
- **In addition:** Helicity cross section fit is used as a cross-check which augments or replaces the theory uncertainties by directly varying the different components of the angular decomposition

- Reduced theory/model-dependence at the cost of increased statistical uncertainty

W mass: p_T^W modelling



- ▶ QCD Initial state radiation involves large corrections (perturbative and non-perturbative).
 - ▶ Experimental measurement limited by the resolution of the recoil...
- ▶ Approach: adjust model parameters using Z events (can be measured precisely) extrapolate to W production

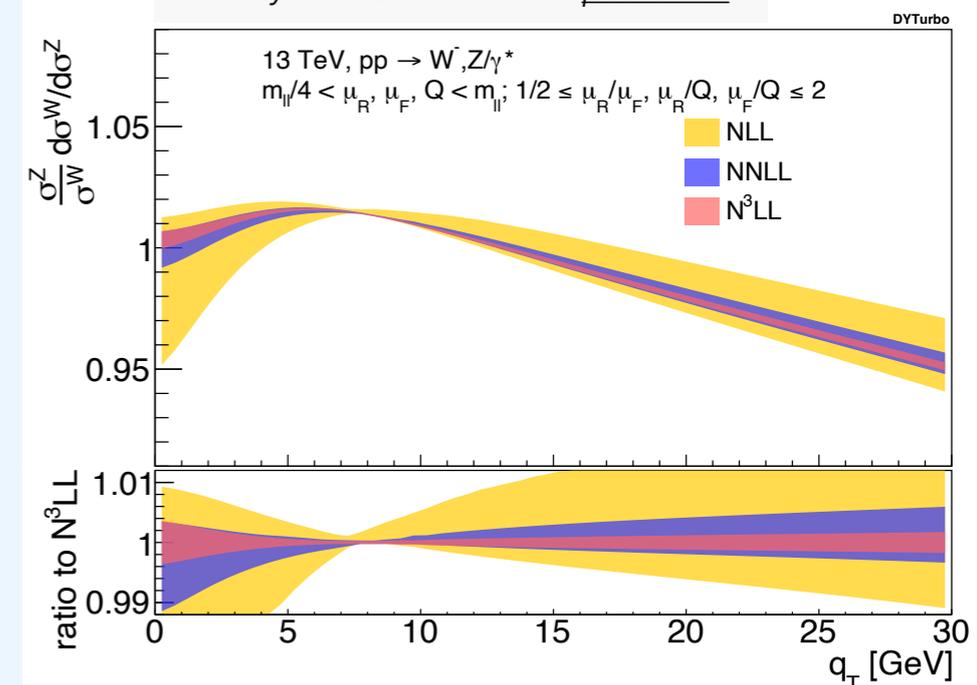


current days several improvements done on analytic resummation programs (improved treatment of HFI production, higher orders etc)

NEW era of analytic resummation models

able to predict/be flexible enough to fit W/Z p_T ratio in data or exploiting constraining power of data providing TNP [theory nuisance parameter] for the fit

courtesy of S. Camarda from public talk

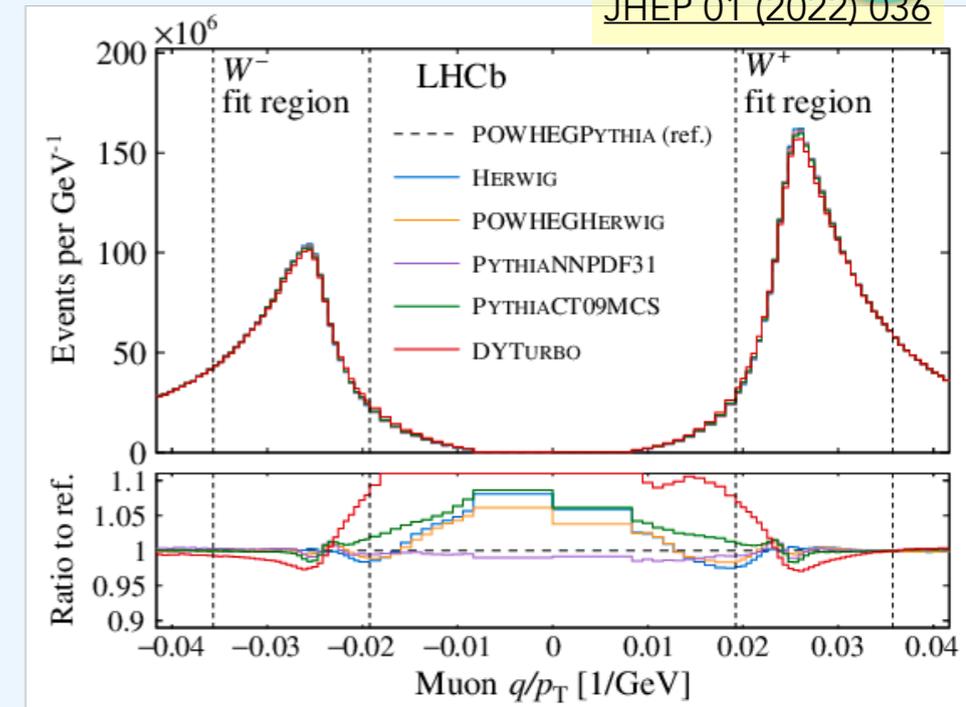
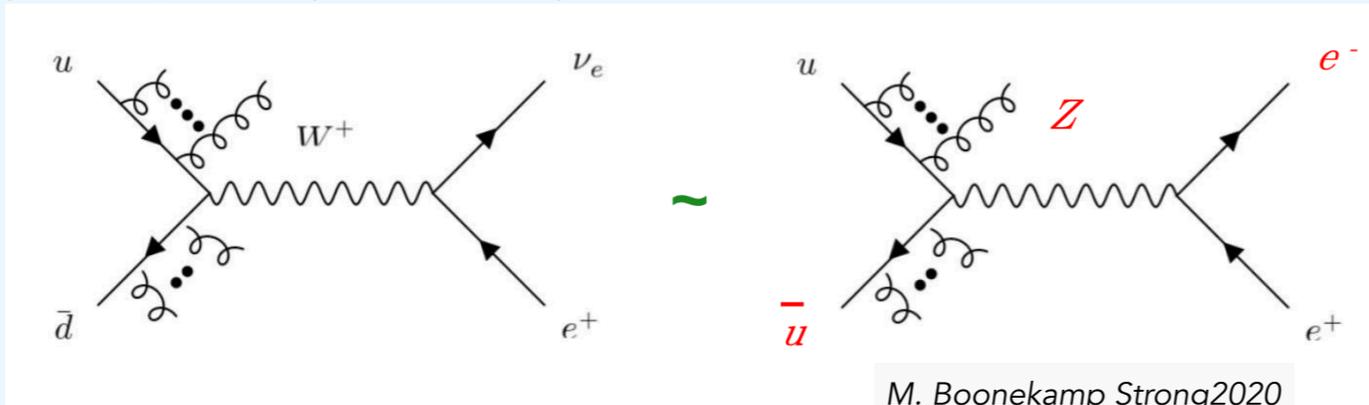


W mass: p_{\perp}^W modelling



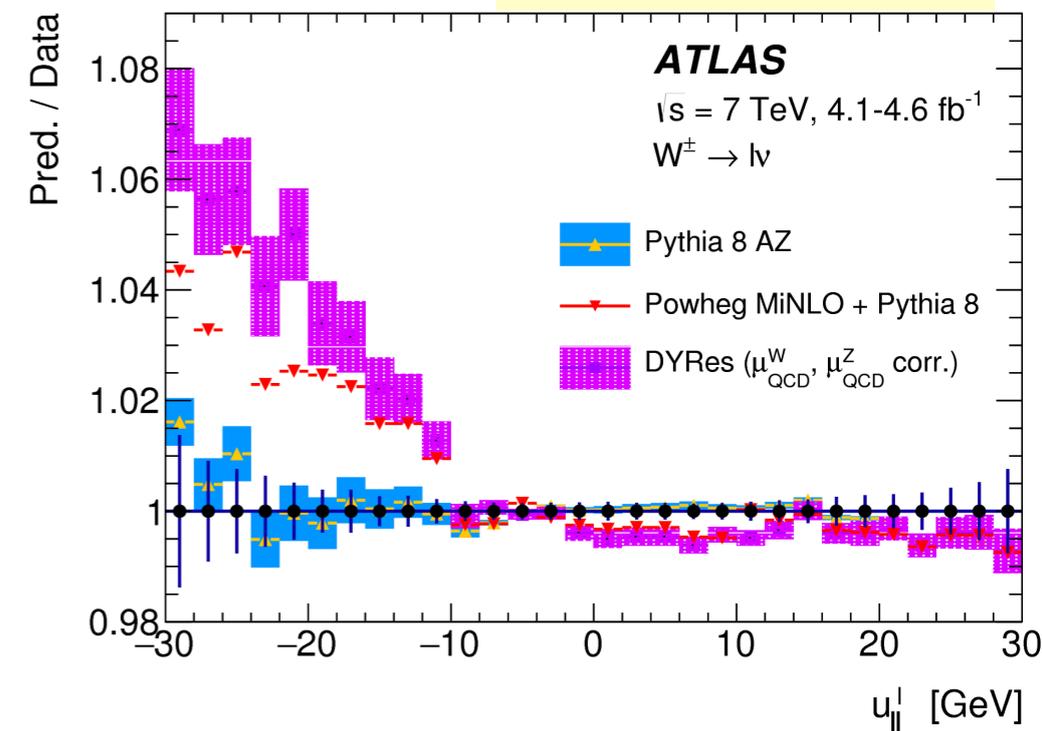
JHEP 01 (2022) 036

- QCD Initial state radiation involves large corrections (perturbative and non-perturbative).
 - Experimental measurement limited by the resolution of the recoil...
- Approach: adjust model parameters using Z events (can be measured precisely) extrapolate to W production



- Current m_W physics modelling uses Pythia parton shower for $d\sigma/dp_{\perp}$
 - p_{\perp}^Z data are used to tune the parameters of the model (AZ tune)
- Fairly good modelling of the W-data, **but hard to improve on uncertainties**, which are mostly related to theory limitations :
 - Based on parton shower which is only (N)LL accurate
 - Limited to LO PDFs
 - No scale variations (meaningless at LL)
 - No handles on heavy-flavour initiated production
- at the time of the measurement analytic resummed predictions (Resbos, Cute, and DyRes) are **strongly disfavoured** by the recoil distribution in data.

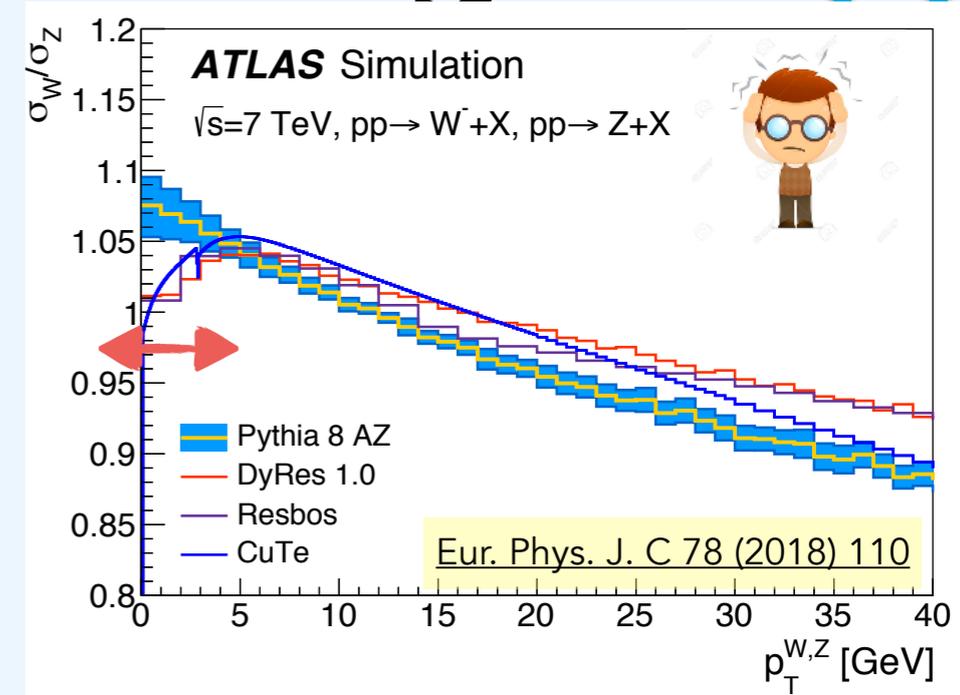
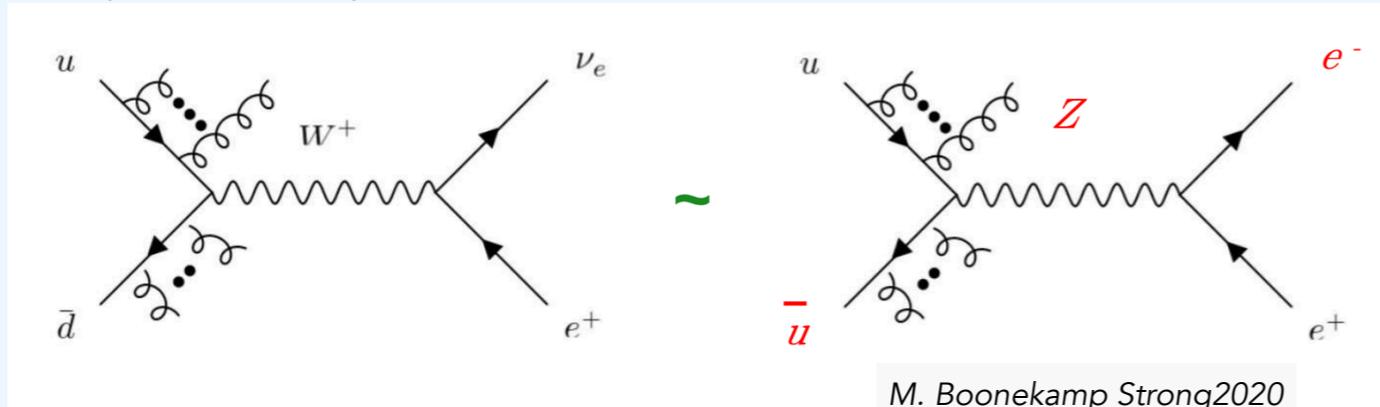
Eur. Phys. J. C 78 (2018) 110



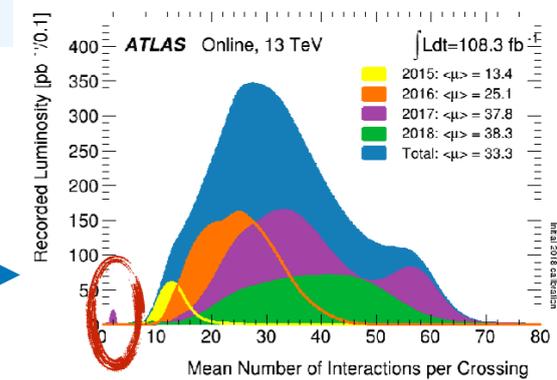
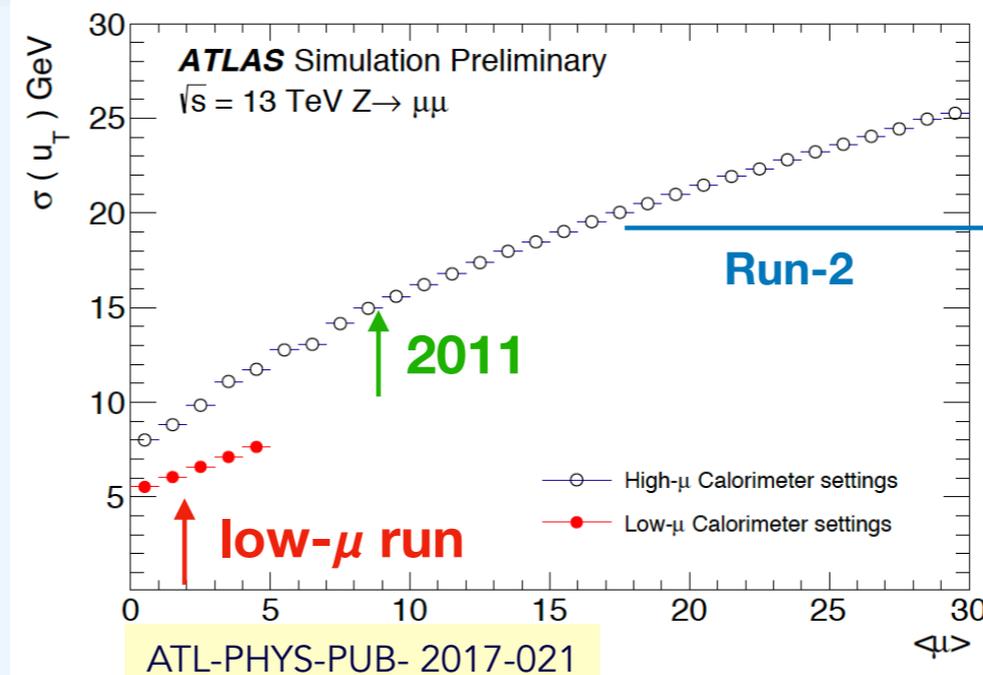
W mass: p_T^W modelling



- ▶ QCD Initial state radiation involves large corrections (perturbative and non-perturbative).
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A **measurement** able to resolve $W p_T$ in bins of 5 GeV with **1% uncertainty** would provide a direct probe of the $W/Z p_T$ ratio and a crucial experimental input to understand this issue.



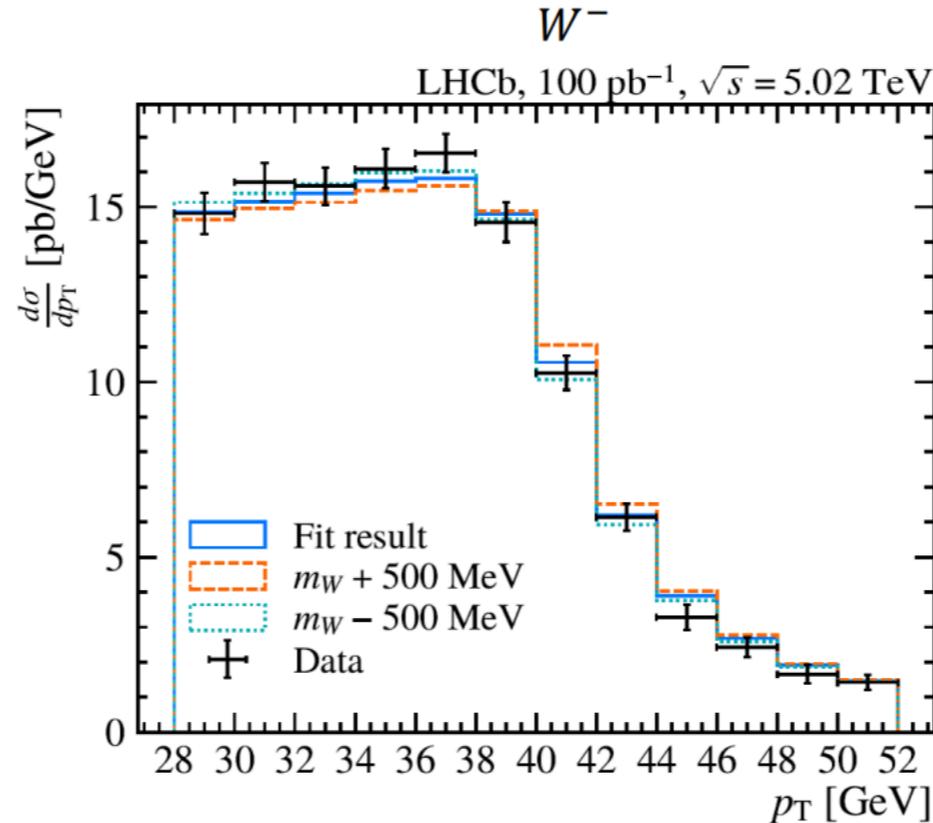
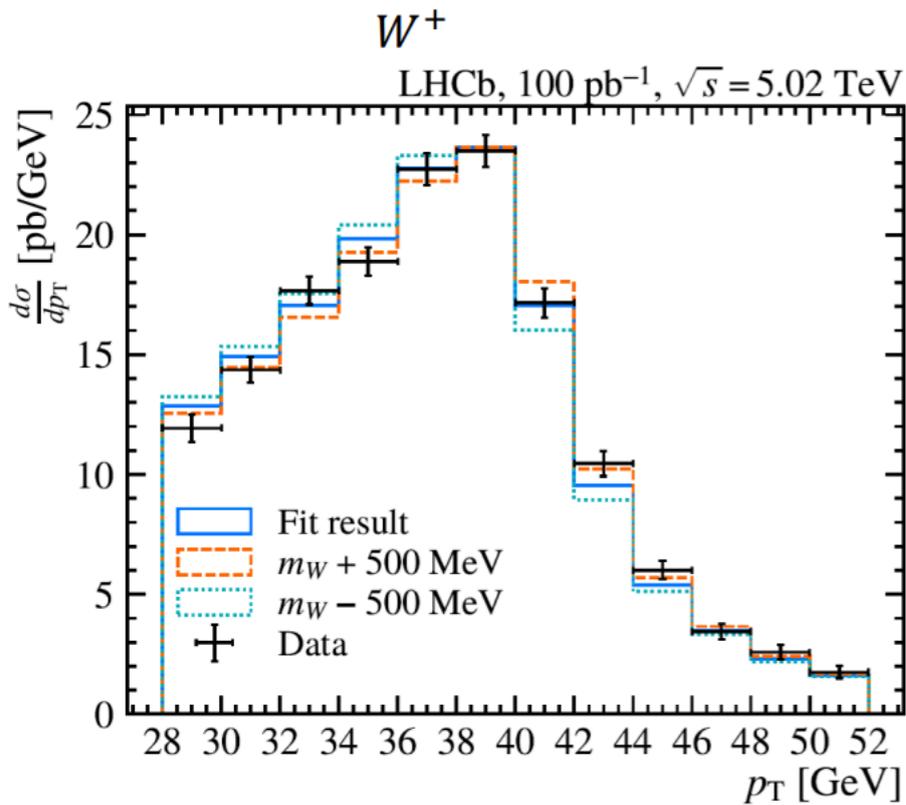
Both ATLAS and CMS collected $\sim 500(200)$ pb^{-1} of data with low- μ ! **fantastic opportunity** for W precision physics!

- ▶ NB In order to resolve $W p_T$ at 5 GeV we need to achieve a experimental resolution of the Hadronic recoil of the same order.

proof of principle - LHCb

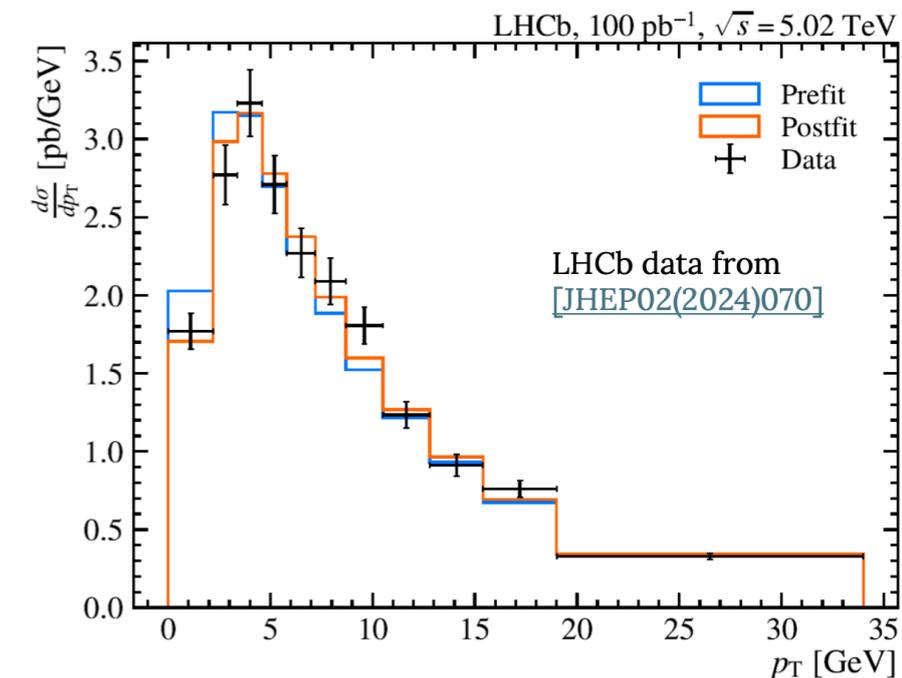


[arXiv:2509.18817]



LHcb extract the differential cross-section of W boson decays as a function of the muon p_T

- Can later fit the W boson mass (model-independent way)
- Ensures long-term reusability of the cross-section measurement for evolving models
- More power to the community (particularly theorists)



Z boson auxiliary measurement crucial the to constrain QCD modelling (α_s and g parameters)

proof of principle - LHCb



The final m_W result is a simple average of the results from using the 3 PDF sets:

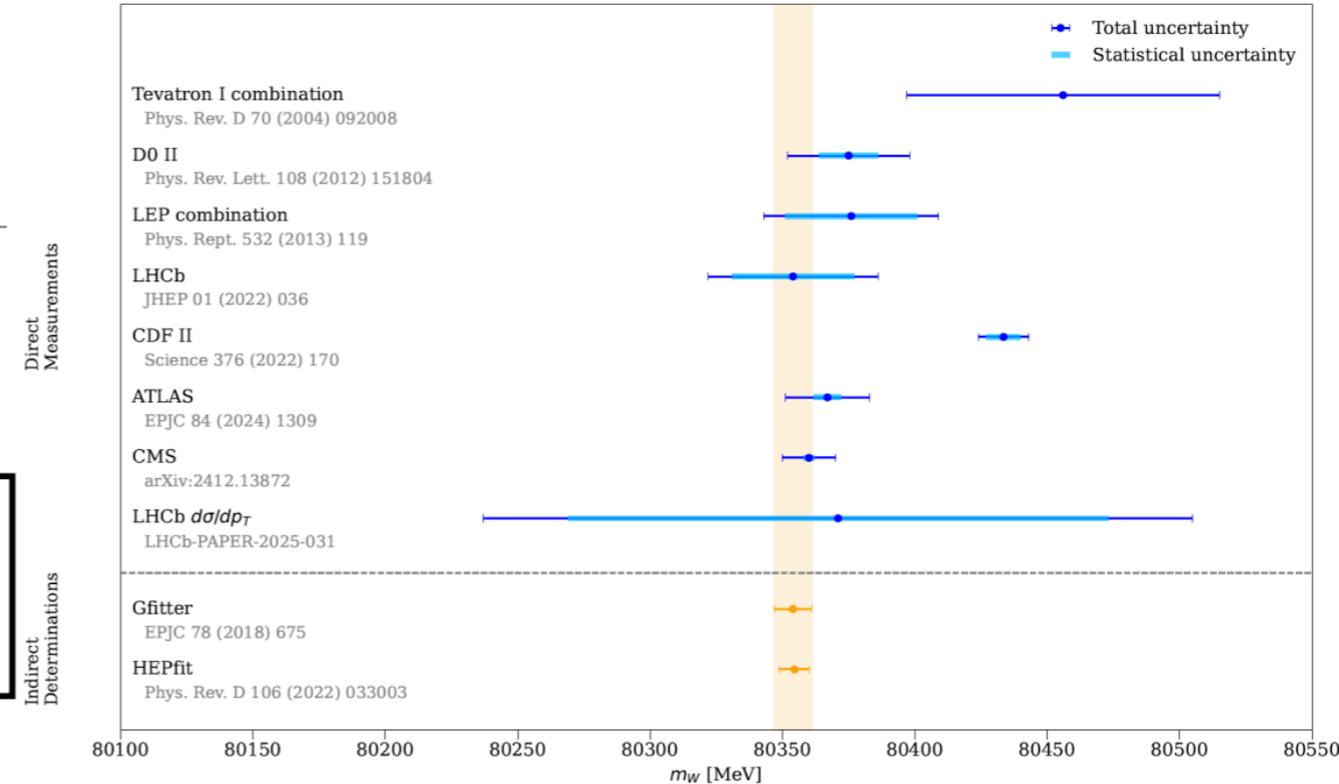
| PDF set | χ^2/ndf | m_W | σ_{theory} | σ_{PDF} |
|----------|---------------------|---------------------|--------------------------|-----------------------|
| NNPDF3.1 | 25.6/21 | 80366 ± 130 MeV | 25 MeV | 28 MeV |
| MSHT20 | 27.2/21 | 80380 ± 129 MeV | 25 MeV | 15 MeV |
| CT18 | 23.9/21 | 80362 ± 130 MeV | 25 MeV | 23 MeV |

$$m_W = 80371 \pm 130_{\text{stat+syst}} \pm 32_{\text{theo}*}$$

(~100 MeV stat)

- **Submitted to JHEP**
- **Now onto full Run 2 analysis!**
(at $\sqrt{s} = 13$ TeV)

*The theory uncertainty is the combination of the PDF members uncertainty and other variations (namely, varying α_s + QED FSR radiation + the 7-point variation of the DYTurbo QCD scale factors)

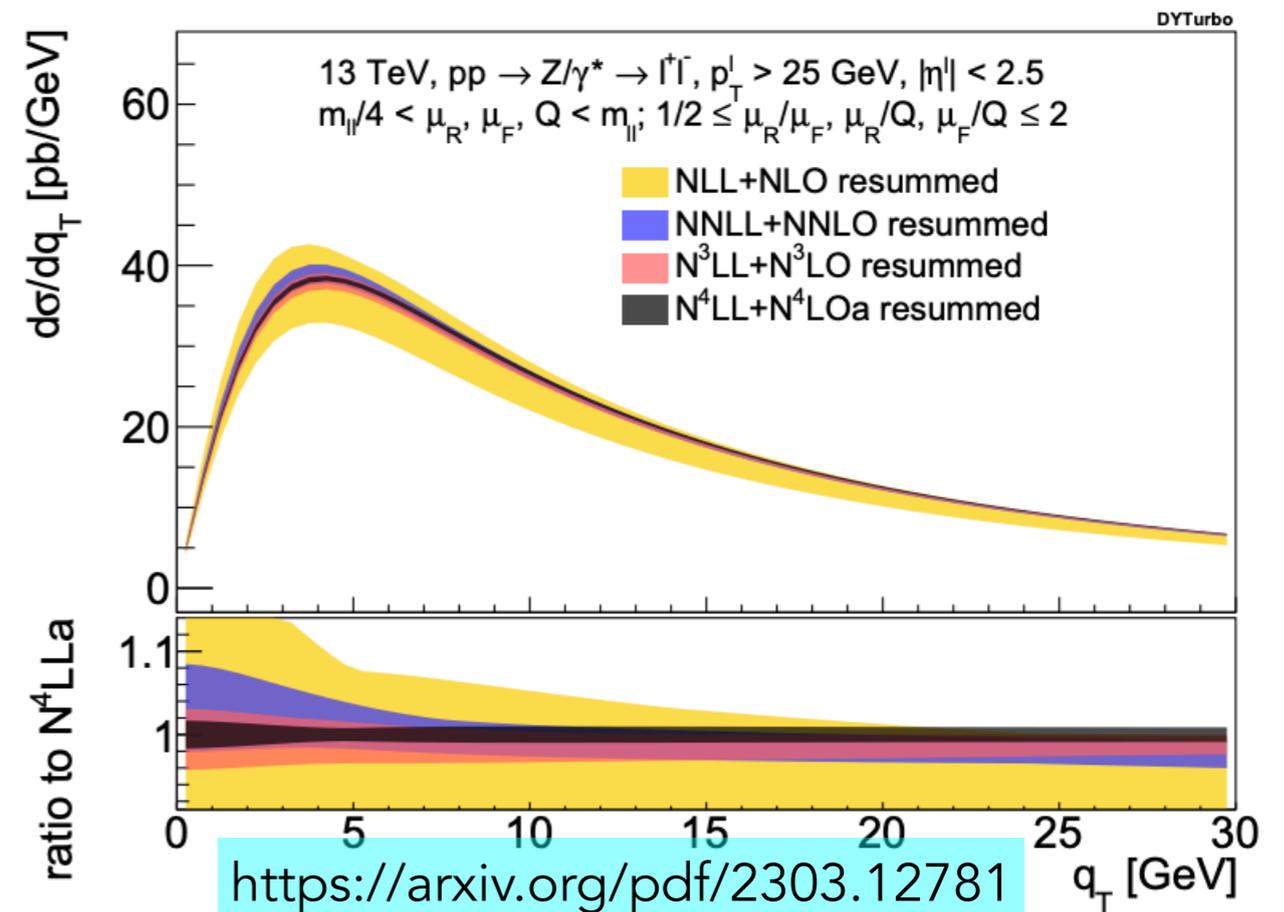
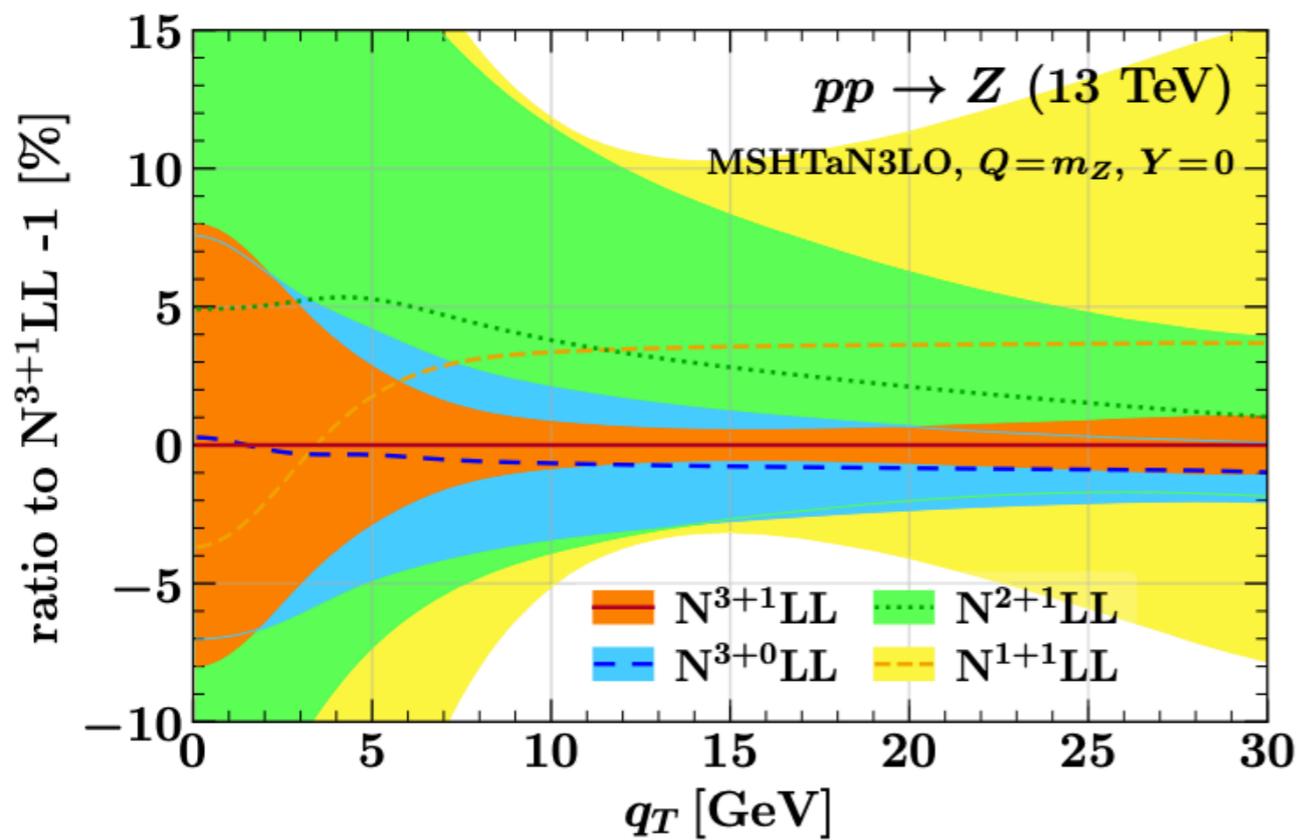


Theory advancement

Tremendous progress in theory in the past 10 years !

At the **level of precision achieved by LHC experiments**, pushing the **theory frontier for all contributors to our predictions essential**

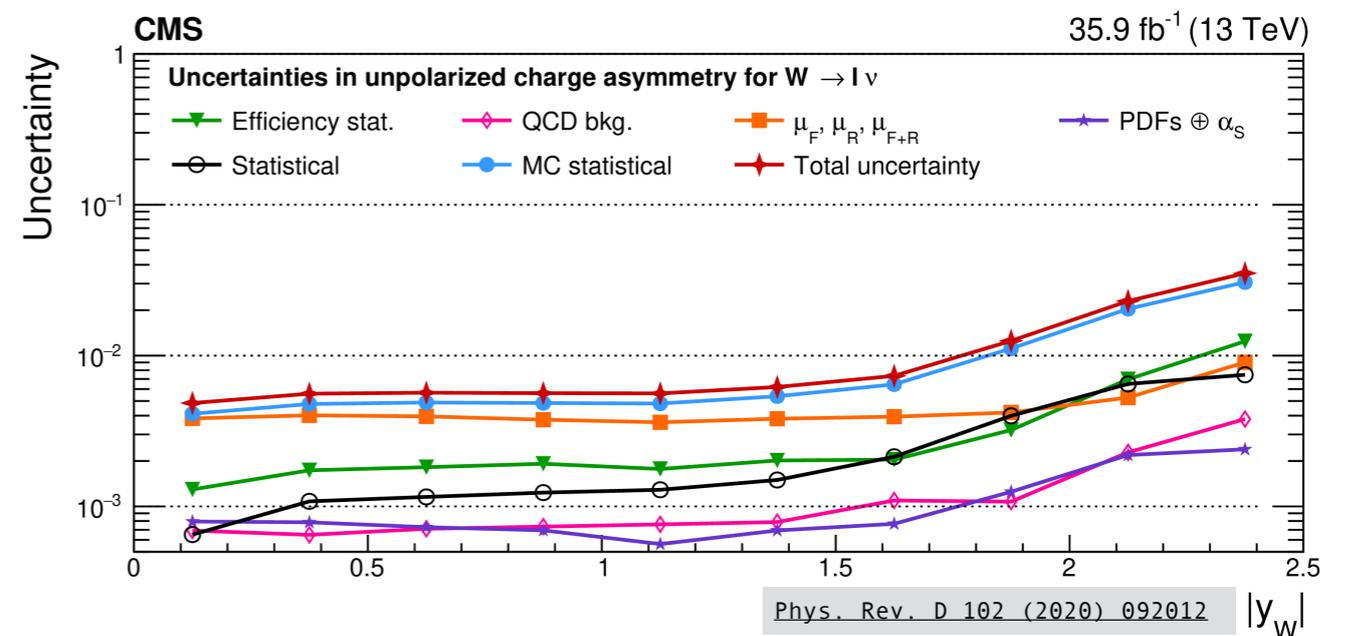
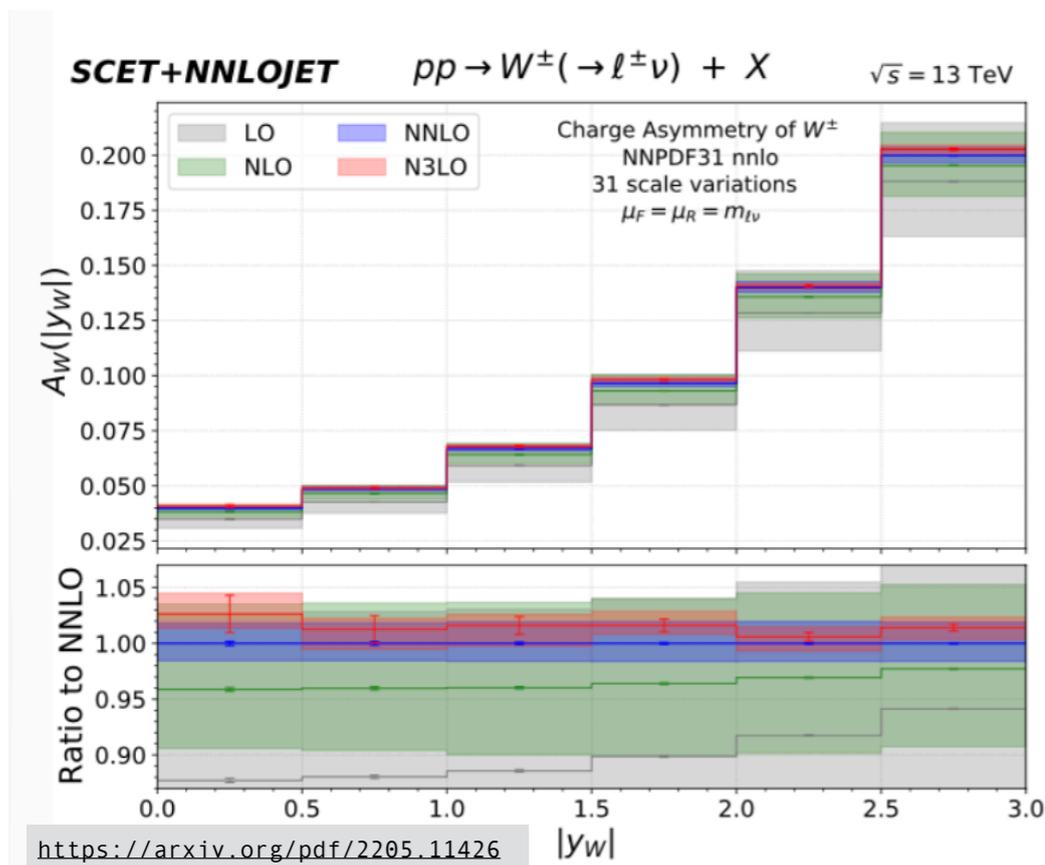
<https://arxiv.org/pdf/2411.18606>



NNLO outdated → N3LO

Tremendous progress in theory in the past 5~10 years !

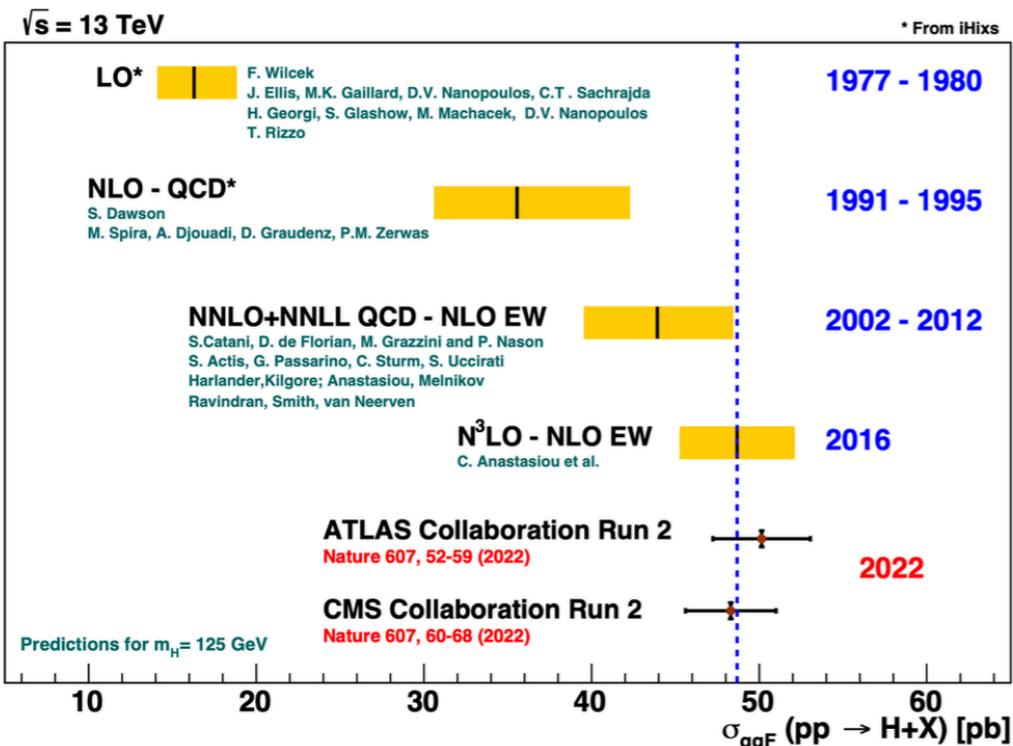
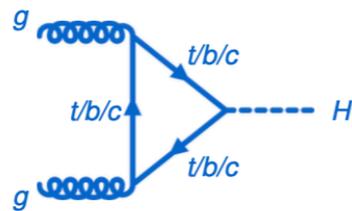
At the **level of precision achieved by LHC experiments**, pushing the **theory frontier for all contributors to our predictions essential** theory & model uncertainties already now **limiting factor** for many LHC analyses



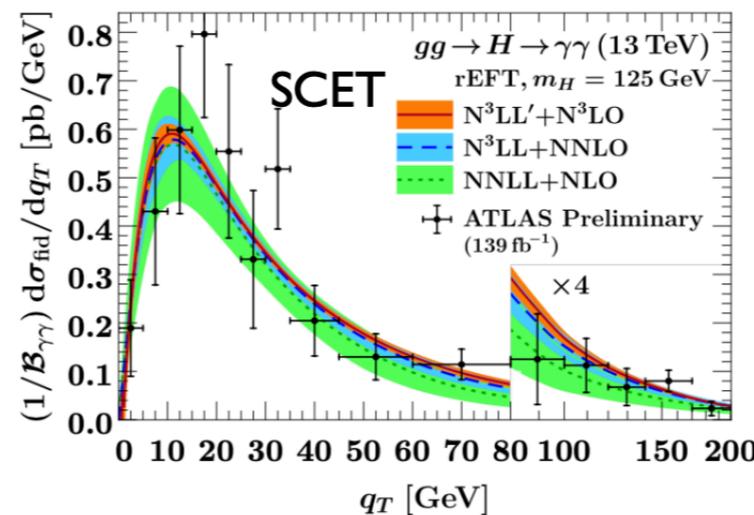
NNLO outdated → N3LO

Tremendous progress in theory in the past 10 years !

Interpretation relies on theory:
calculations of Higgs boson production
via gluon fusion versus time

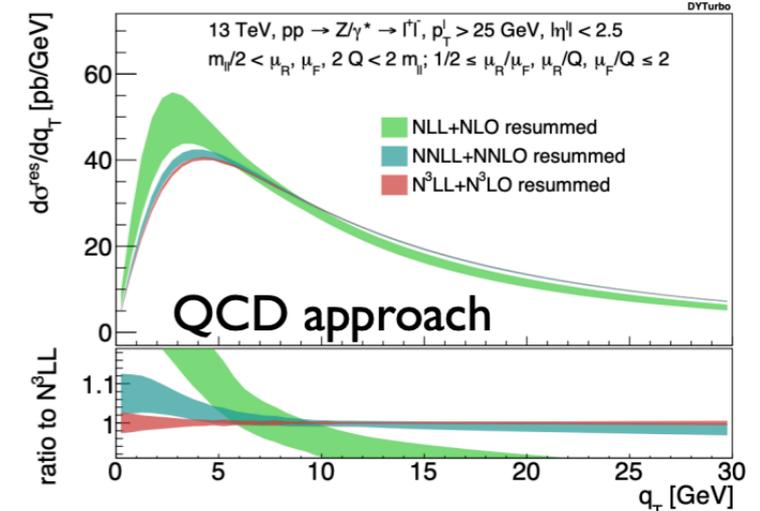


At the level of precision achieved by LHC experiments, pushing the theory frontier for all contributors to our predictions essential



Billis, Denhadi, Ebert, Michel, Tackmann (2021)

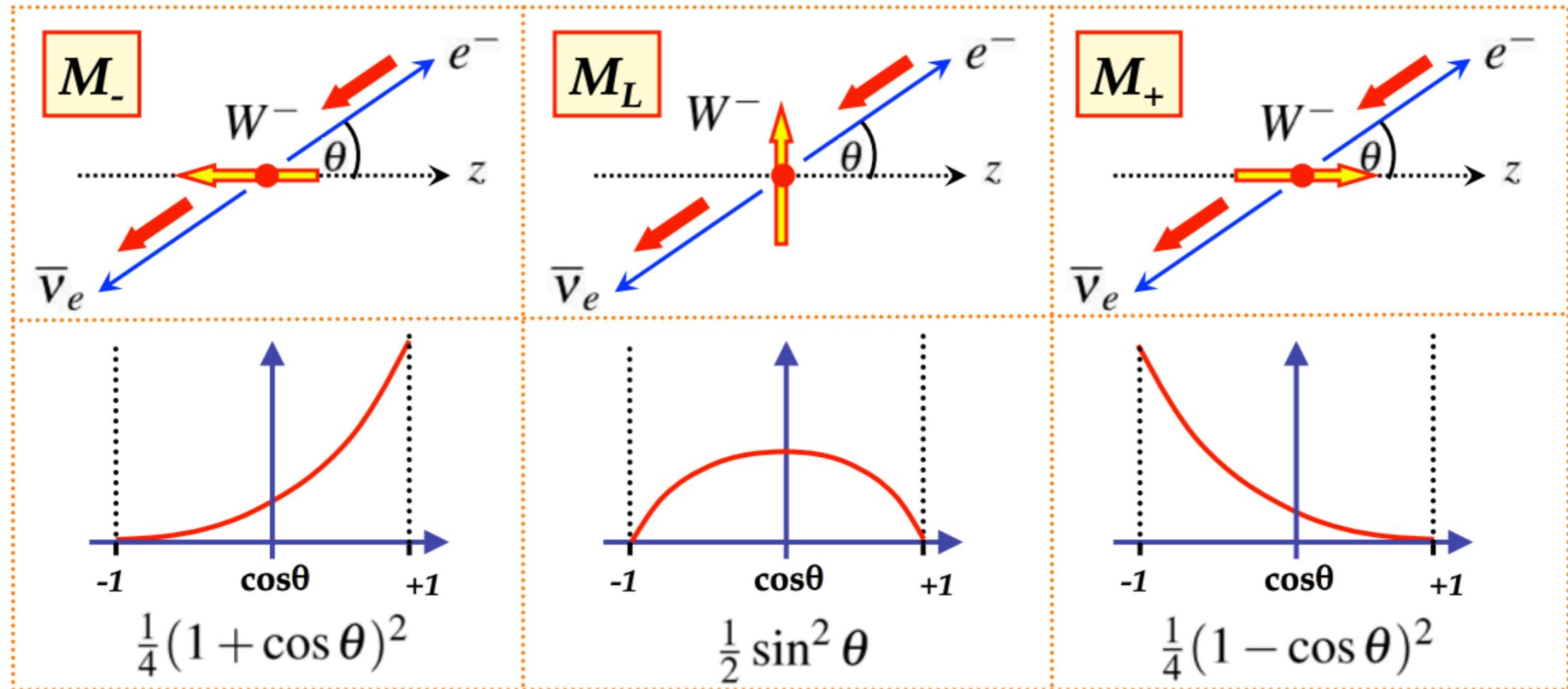
N3LL' resummation + N3LO



Camarda, Cieri, Ferrera (2021)

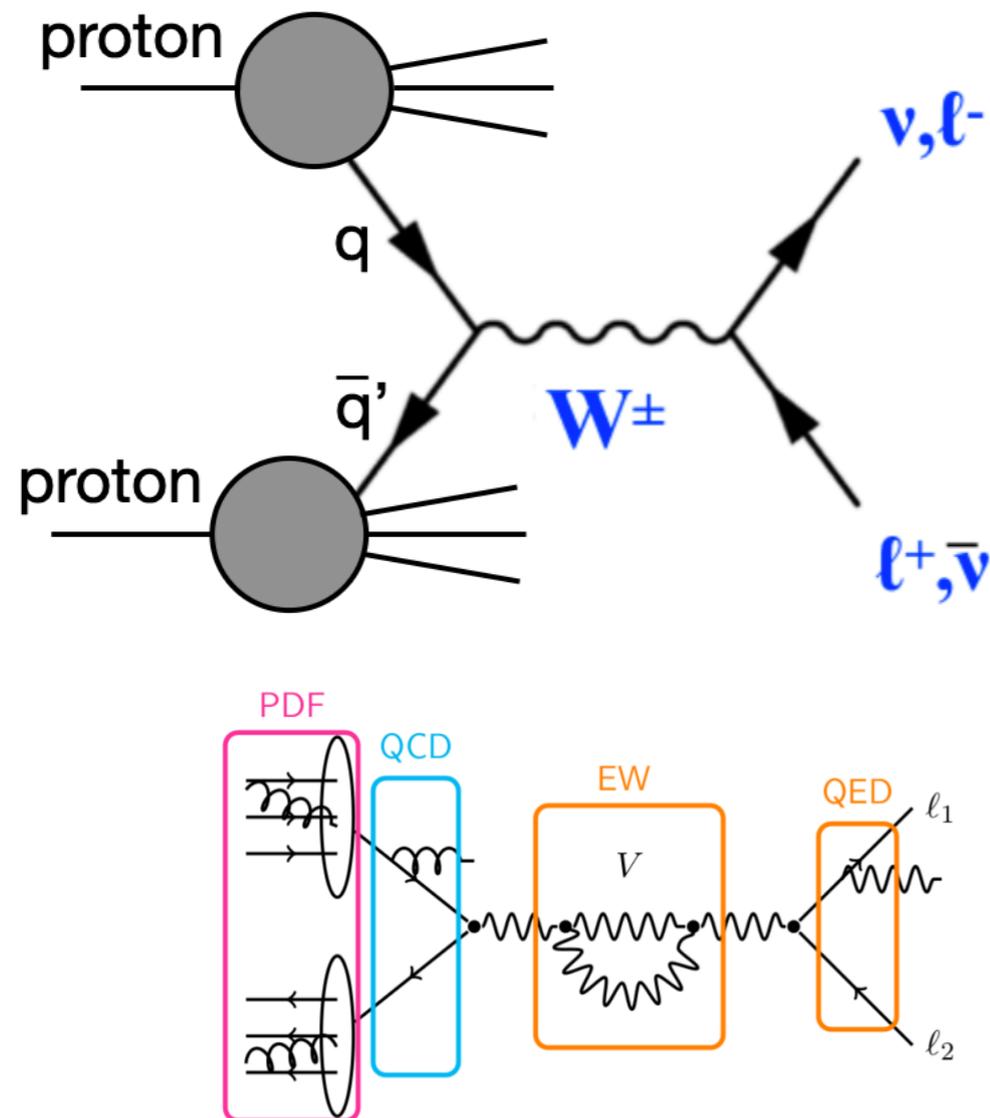
N3LL resummation + N3LO

★ The angular distributions can be understood in terms of the spin of the particles



W - Polarisation

W production at LHC



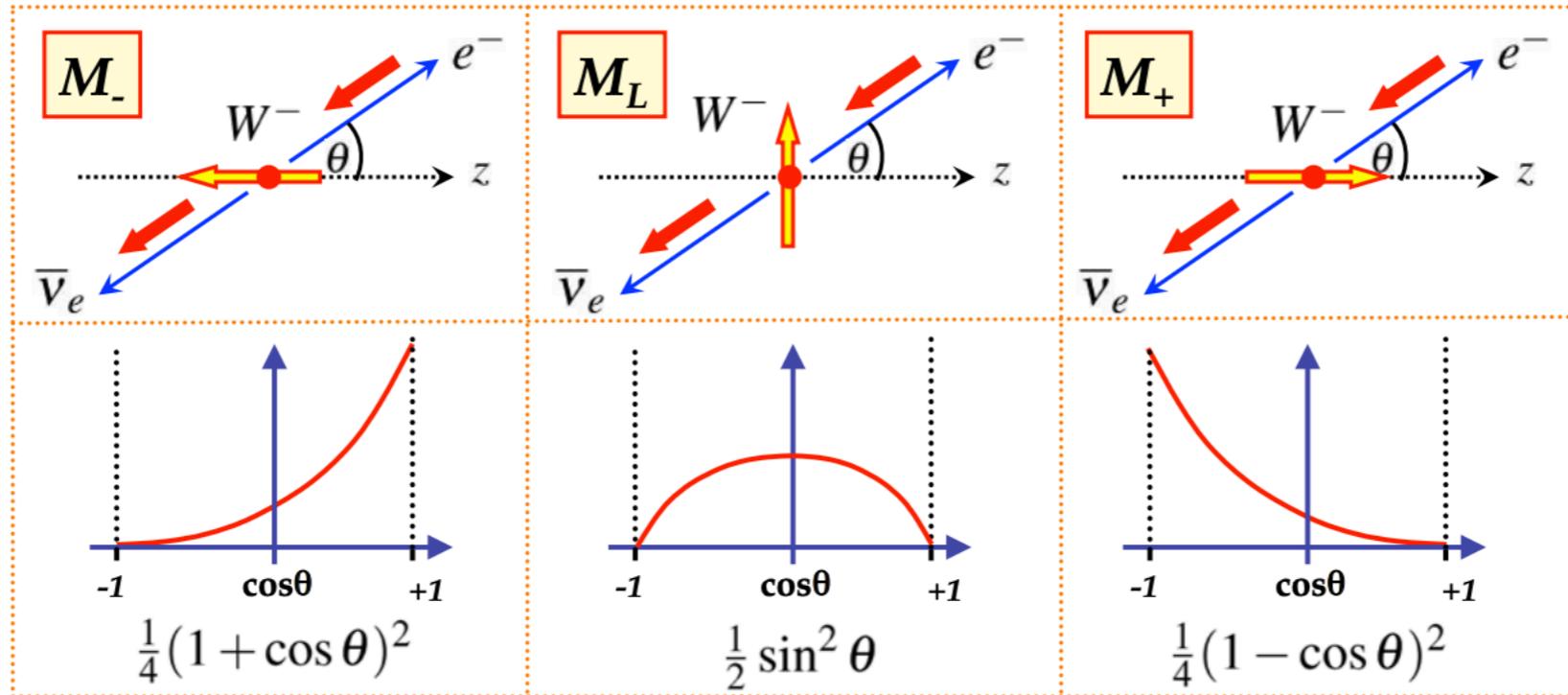
Measuring the polarisation of particles is crucial for understanding their production mechanisms.

- At hadron colliders, W bosons with small transverse momentum are mainly produced by $u\bar{d} \rightarrow W^+$ and $d\bar{u} \rightarrow W^-$ eg. leading order electroweak processes and decay governed by V-A structure of weak interaction $\sim (A4)$
 - production depends on quark kinematics \rightarrow parton distribution functions (PDFs)
 - interesting at LHC (pp): anti-quark must be a sea quark
 - we will see: lepton kinematics carry information about the PDFs!
- At high transverse momenta the production mechanism are :
 - $u\bar{d} \rightarrow W^+g, g\bar{d} \rightarrow W^+\bar{u}$ or $ug \rightarrow W^+d$
 - higher QCD order are needed and full Helicity decomposition is needed (because of the vector nature of the gluon)

$$\frac{d\sigma}{dp_1 dp_2} = \left[\frac{d\sigma(m)}{dm} \right] \left[\frac{d\sigma(y)}{dy} \right] \left[\frac{d\sigma(p_T)}{dp_T} \right] \left[(1 + \cos^2\theta) + \sum_{i=0}^7 A_i(p_T, y, m) P_i(\cos\theta, \phi) \right]$$

reminder polarisation

★ The angular distributions can be understood in terms of the spin of the particles



- W decays: governed by V-A couplings
→ angular distributions of W decay products: not random, but correlated with W

$$\frac{dN}{d \cos \theta_{W,l}^*} \propto (1 + \text{sgn}(h_l \times h_W) \cos \theta_{l,W}^*)^2 = (1 \pm \cos \theta_{l,W}^*)^2 \quad \text{@ leading order!}$$

- sign determined by product of W boson and lepton helicities
- W helicity depends on the incoming quarks:
 - 1) leading x quark/anti-quark determines the (longitudinal) W boost direction
 - 2) $W(-)$ spin direction is fixed to direction of motion of incoming anti-quark

Vector boson polarisation



| Feature | W | Z |
|-----------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------|---------------------------------------------------------|
| No Longitudinal polarisation at LO Purely transverse V [J [±]] | $A_0 \sim$ longitudinal fraction | $A_0 \sim$ longitudinal fraction |
| Coupling structure | Pure V–A | Vector + axial |
| Parity violation | Maximal (V–A) | Partial (V+A mix) |
| Forward–backward asymmetry | $A_4 \rightarrow$ parity violation sensitive to PDF [different for W ⁺ W ⁻] | $A_4 \rightarrow$ proportional to $\sin^2\theta_w$ |
| Lam–Tung holds at $O(\alpha_s)$ | $A_0 - A_2 \neq 0 \rightarrow$ higher-order QCD effects | $A_0 - A_2 \neq 0 \rightarrow$ higher-order QCD effects |

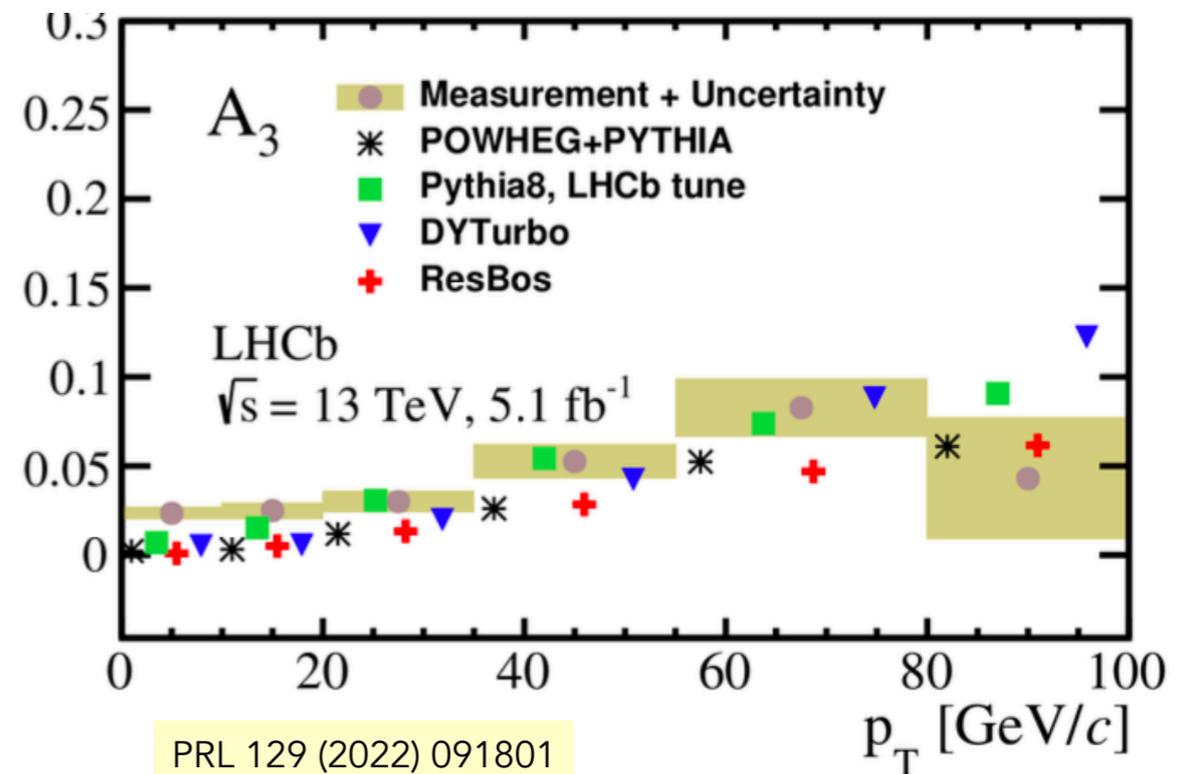
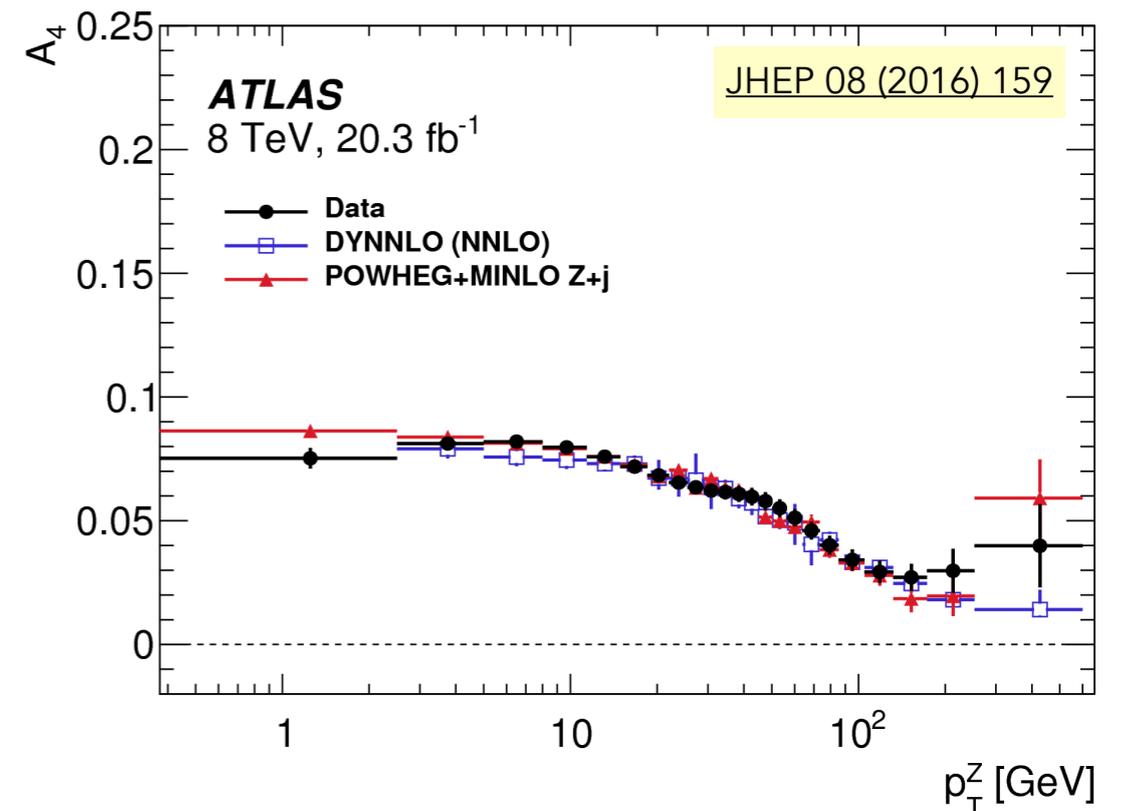
$p_T^V = 0 \rightarrow$ No orbital angular momentum \rightarrow Both W and Z are purely transverse

W mass: Angular coefficients

- ▶ The DY cross section can be reorganised by factorising the dynamic of the boson production, and the kinematic of the boson decay

$$\frac{d\sigma}{dpdq} = \frac{d^3\sigma}{dp_T dy dm} \sum_i A_i(y, p_T, m) P_i(\cos\theta, \phi)$$

- ▶ Current m_W physics modelling has the angular coefficients (A_i) modelled with fixed order perturbative QCD at NNLO
- ▶ A_i predictions are validated by comparisons to the Z measurement
 - ▶ **Suboptimal for A_4 : fixed order prediction down to low p_T ?**
 - ▶ Nowadays A_4 can be predicted including resummation effects
 - ▶ LHCb m_W measurement accounts for A_3 data/ prediction discrepancy [cf. Recent LHCb measurement of A_i in $Z \rightarrow ll$]



The analysis motivation

Measure W angular coefficients in 340 pb⁻¹ @ 13TeV ATLAS low- μ data

- Precise measurements of DY production dynamics through the measurement of the angular distributions → connected with the W **polarisation**
 - Stringent **test of QCD and physics modelling for m_W**
- **NEW** measurement never exploited before in W events!
- Analysis strategy follow the Moments Method from Eur. Phys. J. C 84 (2024) 315 + Dedicated set of lepton&hadronic recoil performances correction from the WpT/ZpT measurement and **low mu-W** mass effort (more info)
 - For the first time extraction of the W-boson angular coefficient ($A^0 - A^4$) & at the same full phasespace differential cross-section vs p_T^W
 - **More challenging** wrt Z boson (JHEP08(2016)159) due to the missing neutrino and the poor MET resolution (**ambiguity sign of $\cos\theta$ solved using m_W kinematic constraint requirement**)
 - Benefit from new techniques / **low- μ environment** to have O(5) better hadronic recoil reconstruction

A convenient decomposition

A convenient way of expressing the radiation-inclusive DY cross section is through the factorisation of the production dynamic and the decay kinematic properties of the dilepton system.

$$\frac{d^3\sigma^{U+L}}{dp_T dy dm} \left(1 + \cos^2\theta + \sum_{i=0}^7 A_i(y, p_T, m) P_i(\cos\theta, \phi) \right)$$

The unpolarised cross sections do not depend on lepton variables, they are defined in "full-lepton phase space", only by cuts (or bins) in p_T, y, m of the boson

Measuring the angular coefficients correspond to building a synthetic "quantized" representation of the $(\cos\theta, \phi)$ kinematic space decompose in helicity cross sections

Smart idea: Exploit the angular variables decomposition to perform a simultaneous p_T measurement of unpolarised full-lepton phase space cross sections + extraction of angular coefficients

- ▶ **Very powerful:** trade systematics for statistics
- ▶ **Very useful:** provides analytic extrapolation of lepton cuts and enables a rich interpretation programme

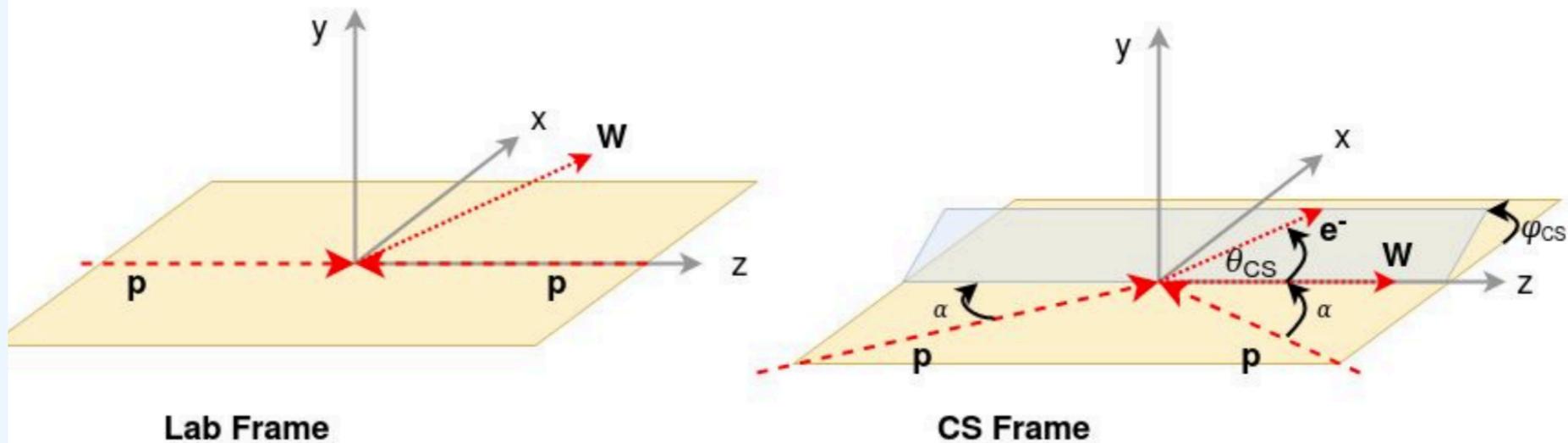
Angular coefficients



$$\frac{d\sigma}{dp_T^W dm^W dy^W d\cos\theta d\phi} = \frac{3}{16\pi} \frac{d\sigma^{U+L}}{dp_T^W dm^W dy^W} \left\{ \begin{aligned} & \left(1 + \cos^2\theta\right) + \frac{1}{2}A_0 \left(1 - 3\cos^2\theta\right) \\ & + A_1 \sin 2\theta \cos\phi + \frac{1}{2}A_2 \sin^2\theta \cos 2\phi \\ & + A_3 \sin\theta \cos\phi + A_4 \cos\theta + A_5 \sin^2\theta \sin 2\phi \\ & + A_6 \sin 2\theta \sin\phi + A_7 \sin\theta \sin\phi \end{aligned} \right\}.$$

Non-zero at LO
 Non-zero at NLO
 Non-zero at NNLO

Collins Soper Frame



Special W boson rest frame where angles are defined by lepton and proton kinematics.
 Both incoming partons share the same transverse momentum (ie. maximally symmetric)
 Define using “negative” lepton, so for W^+ case this is the neutrino

about the ambiguity in sign

→ Missing neutrino p_z information → results in a sign ambiguity in the determination of $\cos\theta$
 How to infer the Neutrino p_z information?

Solving for the Neutrino P_z :

- W mass constraint: quadratic equation

$$(p^\mu + q^\mu)^2 = m_W^2 \Rightarrow q_z(1,2) = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$E_T^{\vec{m}iss} = \vec{p}_T^\nu = -(\vec{u}_T + \vec{p}_T^\ell)$$

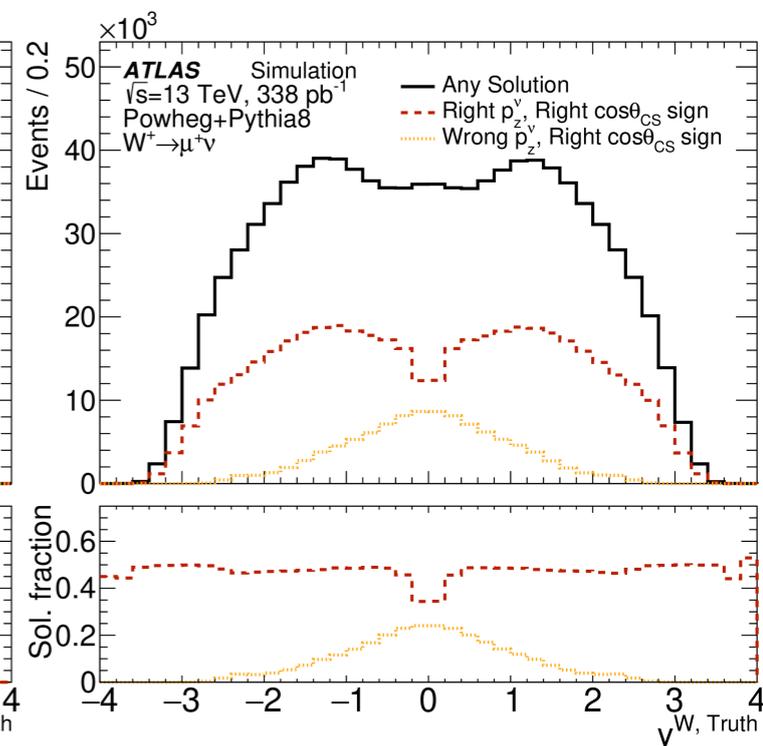
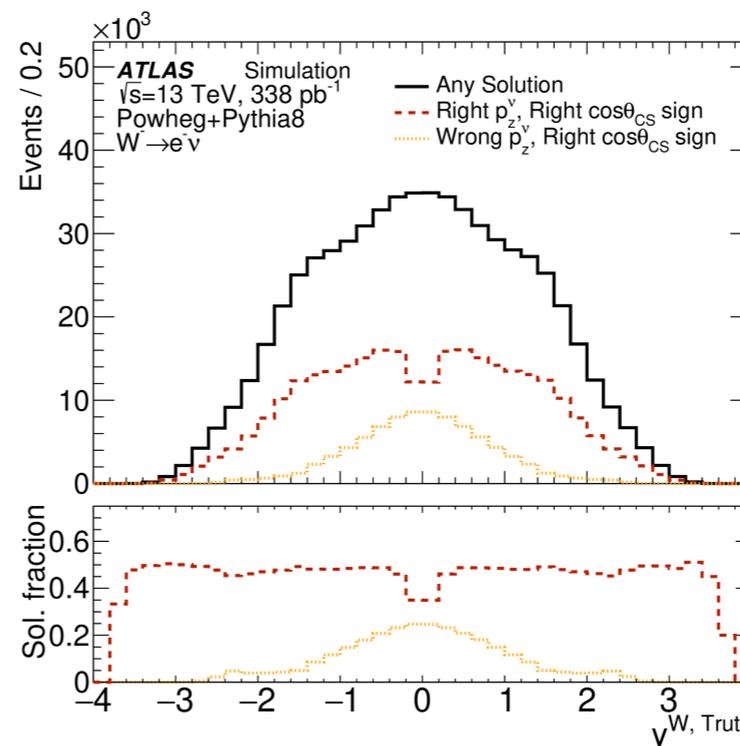
for $\Delta = (b^2 - 4ac)$:

- A. $\Delta = 0 \rightarrow 1$ solution
- B. $\Delta > 0 \rightarrow 2$ solutions
- C. $\Delta < 0 \rightarrow$ no real solution

NO solution $\Delta < 0$:

when we can not infer the neutrino p_z information we keep the sign ambiguity in $\cos\theta$ definition

NB. when $m_{T^{reco}} > m_W \Rightarrow \Delta < 0$ and this appears more often at high p_{TW} because of bad recoil resolution



about the ambiguity in sign

→ Missing neutrino p_z information → results in a sign ambiguity in the determination of $\cos\theta$
 How to infer the Neutrino p_z information?

2 solution $\Delta > 0$:

when we have 2 solution pick one at random

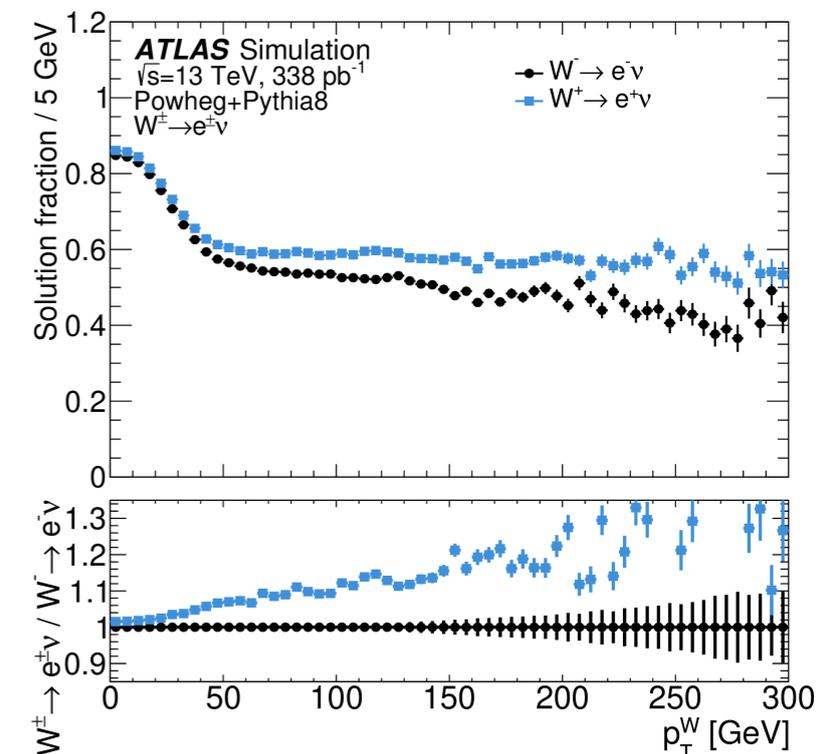
Choosing a solution at random can result in ambiguity in the sign of $\cos\theta_{cs}$, but with enough statistic we can overcome this to solve the sign ambiguity. There are 3 cases :

1. Both solutions change sign to $\cos\theta_{cs}$ and y_w (50% chance to get the right solution)
2. Only y_w have sign ambiguity the sign ambiguity of the 2 solutions in $\cos\theta_{cs}$ cancels
3. One solution is unphysical ($x_{Bjorken} > 1$)

$$\cos\theta = 2 \frac{(l^+ \bar{l}^- - l^- \bar{l}^+) \cdot \text{sign}(y_{\ell\ell})}{m_{\ell\ell} \sqrt{m_{\ell\ell}^2 + \vec{p}_T^2}}$$

$l^\pm = E \pm p_z$ for the lepton/neutrino
 $\bar{l}^\pm = E \pm p_z$ for the antilepton/antineutrino

$$y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right)$$



Likelihood FIT

Likelihood Fit

$$\begin{aligned}
 N_{\text{exp}}^n(A, \sigma, \theta) &= \left\{ \sum_{j=0}^{N_{\text{bins}}^{pT^W}} \sigma_j \times L \left[T_{8,j}^n(\beta) + \sum_{i=0}^7 A_{ij} \times T_{ij}^n(\beta) \right] \right\} \times \gamma^n + \sum_B^{\text{bkgds}} T_B^n(\beta) \\
 \mathcal{L}(A, \sigma, \theta | N_{\text{obs}}) &= \prod_n^{N_{\text{bins}}} \left\{ P(N_{\text{obs}} | N_{\text{exp}}^n(A, \sigma, \theta)) \right. \\
 &\quad \left. P(N_{\text{eff}}^n | \gamma^n N_{\text{eff}}^n) \right\} \times \prod_m^M G(0 | \beta^m, 1)
 \end{aligned}$$

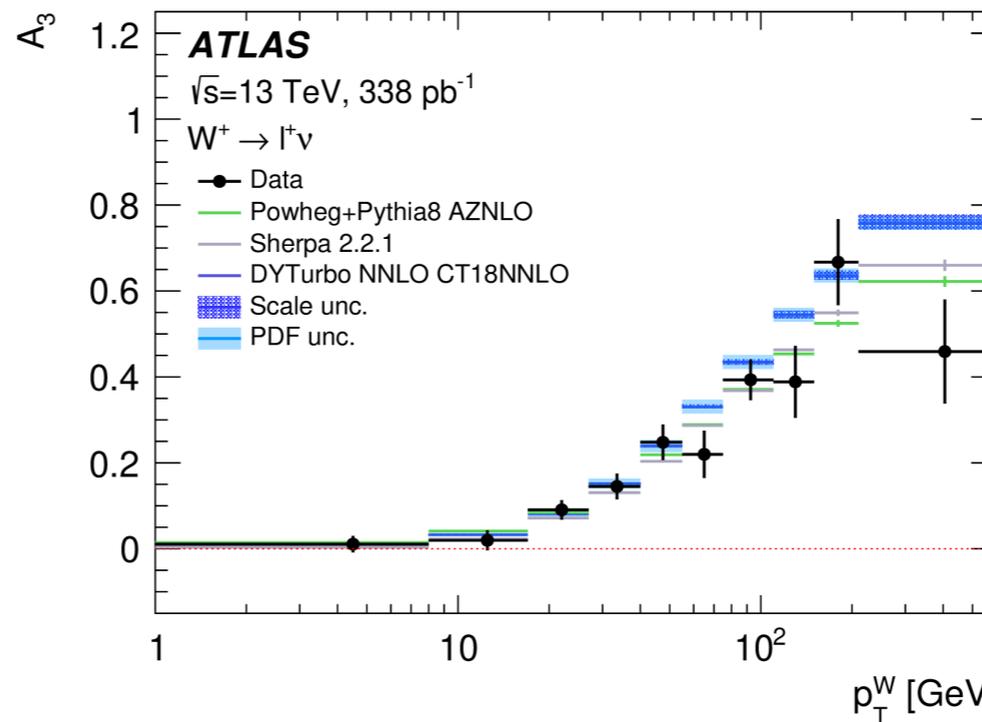
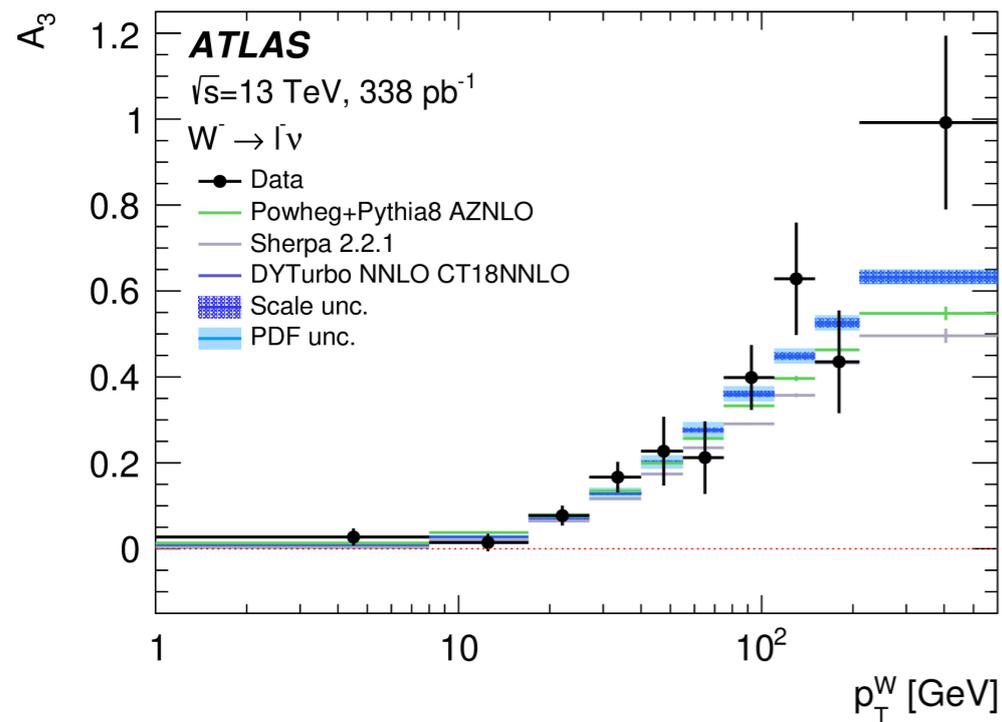
Labels in the diagram:

- Cross-section parameters**: points to σ_j
- Ai parameters**: points to A_{ij}
- Polynomial Templates**: points to $T_{ij}^n(\beta)$
- Bkgd Templates**: points to $T_B^n(\beta)$
- Expected Events**: points to $N_{\text{exp}}^n(A, \sigma, \theta)$
- Observed Events**: points to N_{obs}
- MC Stat**: points to $P(N_{\text{eff}}^n | \gamma^n N_{\text{eff}}^n)$
- Syst NPs**: points to $G(0 | \beta^m, 1)$

Product of all Poisson probabilities for each p_T^W , $\cos\theta_{\text{CS}}$, ϕ_{CS} bin and NP constraints

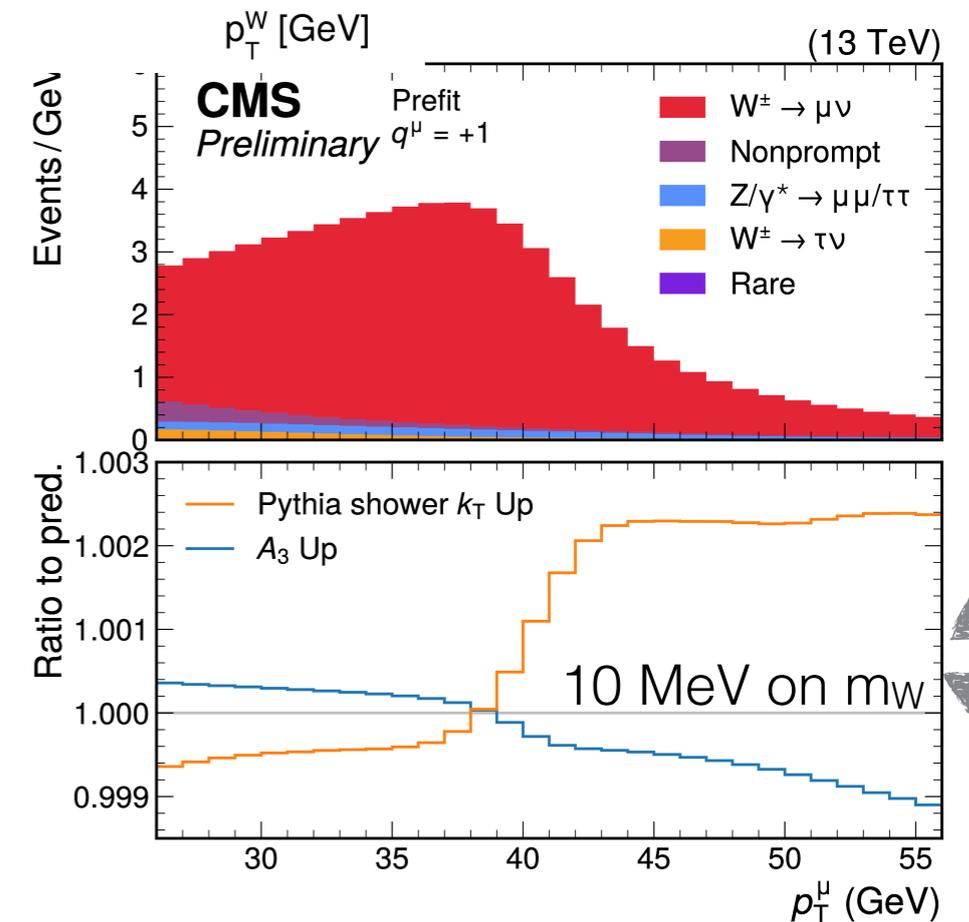
Minimized using binned NLL to calculate first and second derivatives to calculate Hessian, $H = \nabla^2(-\ln L)$ to find a solution for $\nabla(-\ln L) = 0$

First measurement of full set of angular coefficient in W production



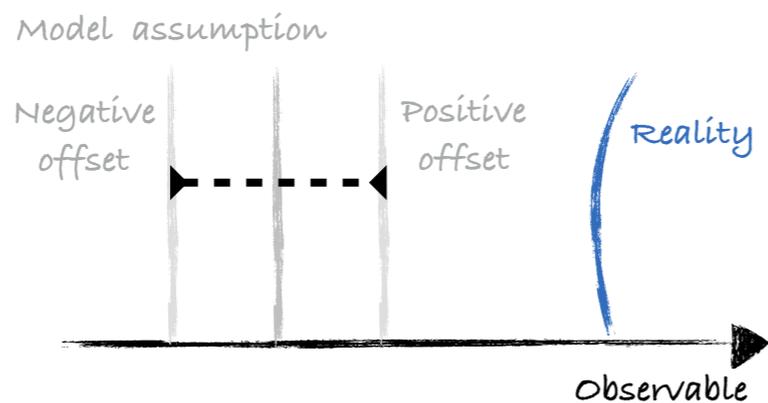
e-print [arXiv:2509.13759](https://arxiv.org/abs/2509.13759)

- For the first time extraction of the full set of W-boson angular coefficient (A_0 - A_7)
- First direct measurement of A_0 and A_4 vs p_T^W
- Improvement for A_2 and A_3 Precision exceeds that of any previous measurement
- Measurement of p_T^W spectra in full phase space for W^+ and W^- at 13 TeV with %level accuracy

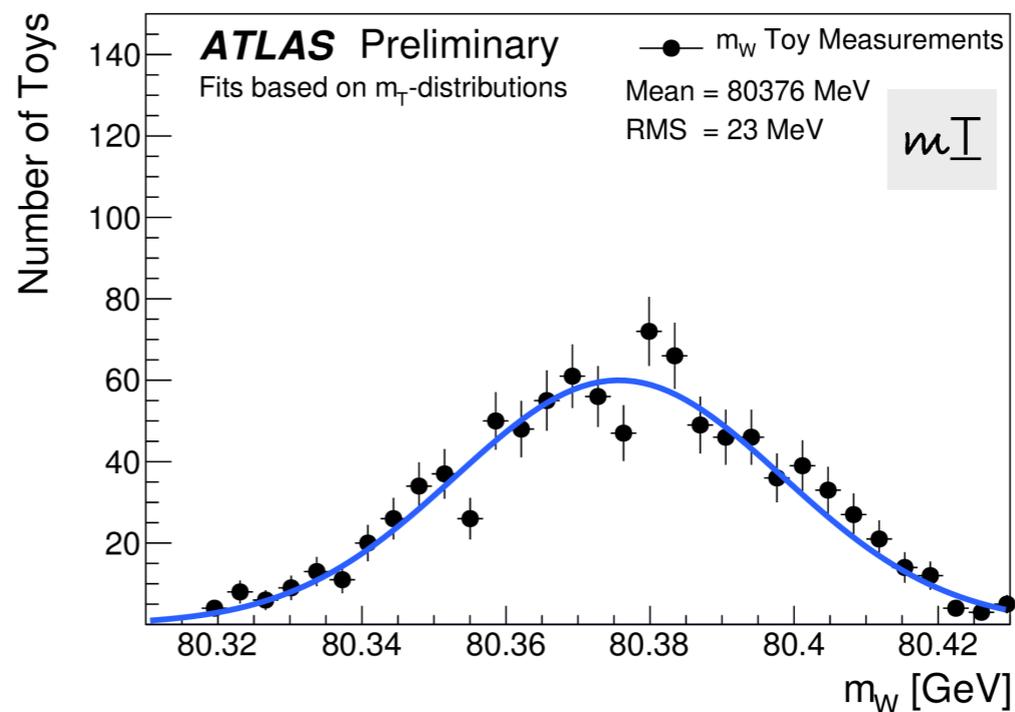
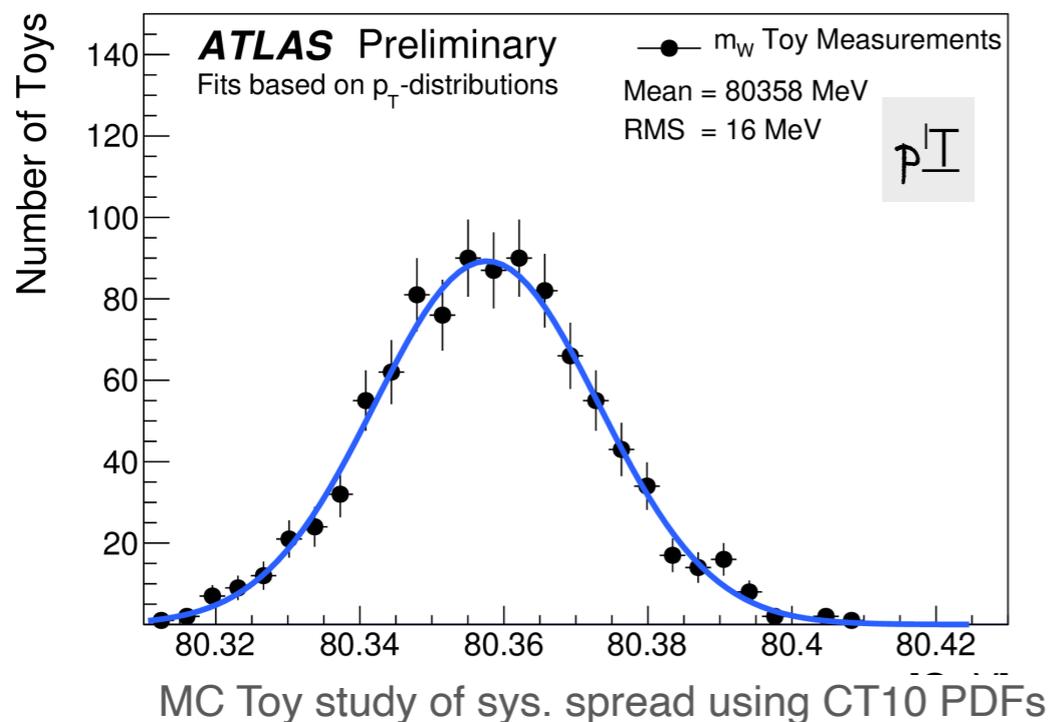
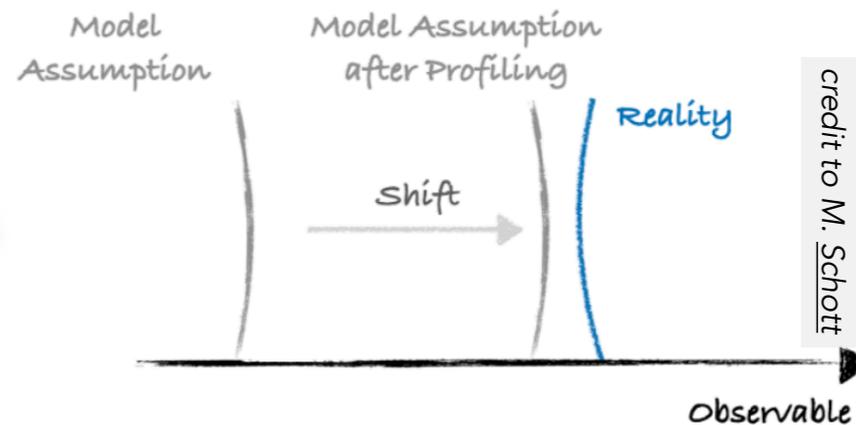


The improvement of the analysis

χ^2 offset fit

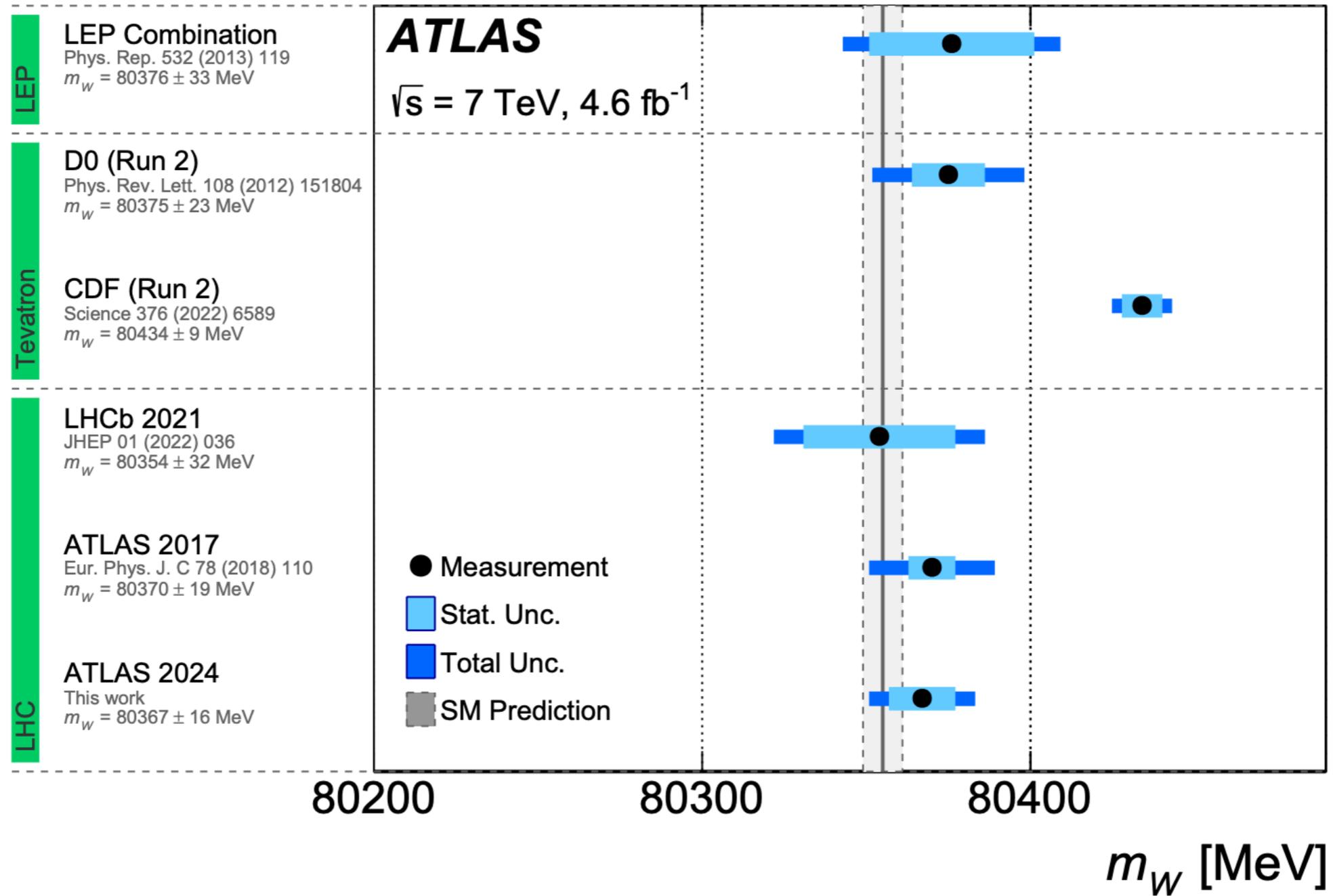


Profiled Likelihood fit



PLH allows simultaneous determination of POI together with NP taking account correlation in each category
 expected allowed shift $m_W \pm 16$ (± 23) MeV for p_T (m_T)

Overview of m_W measurements



W mass re-analysis

ATLAS W boson mass

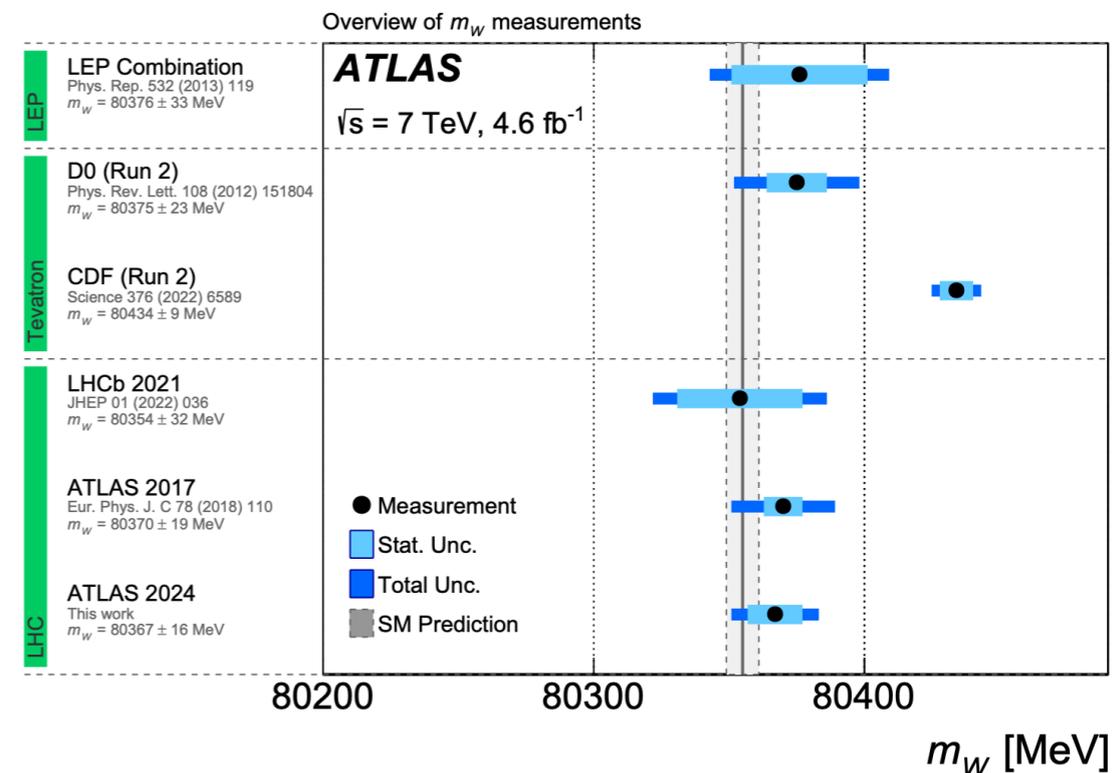
- ▶ p_T and m_T measurement are compatible at 1.2σ level
 - ▶ correlation between the 2 measurements $\rho = 0.63$

| Unc. [MeV] | Total | Stat. | Syst. | PDF | A_i | Backg. | EW | e | μ | u_T | Lumi | Γ_W | PS |
|-------------|-------|-------|-------|------|-------|--------|-----|-----|-------|-------|------|------------|-----|
| p_T^ℓ | 16.2 | 11.1 | 11.8 | 4.9 | 3.5 | 1.7 | 5.6 | 5.9 | 5.4 | 0.9 | 1.1 | 0.1 | 1.5 |
| m_T | 24.4 | 11.4 | 21.6 | 11.7 | 4.7 | 4.1 | 4.9 | 6.7 | 6.0 | 11.4 | 2.5 | 0.2 | 7.0 |
| Combined | 15.9 | 9.8 | 12.5 | 5.7 | 3.7 | 2.0 | 5.4 | 6.0 | 5.4 | 2.3 | 1.3 | 0.1 | 2.3 |

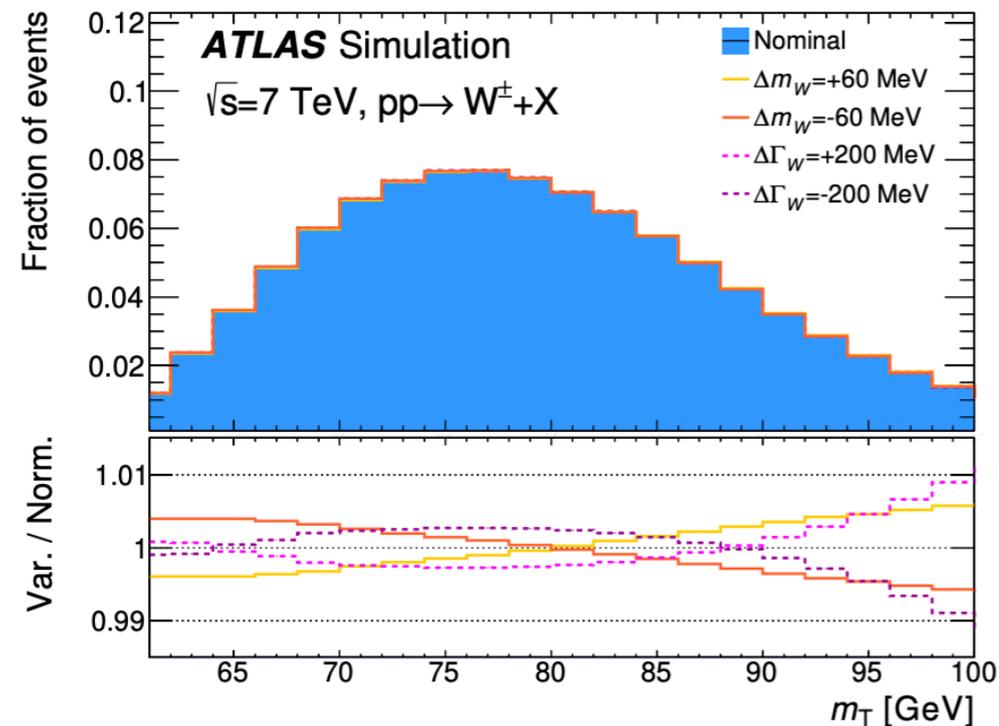
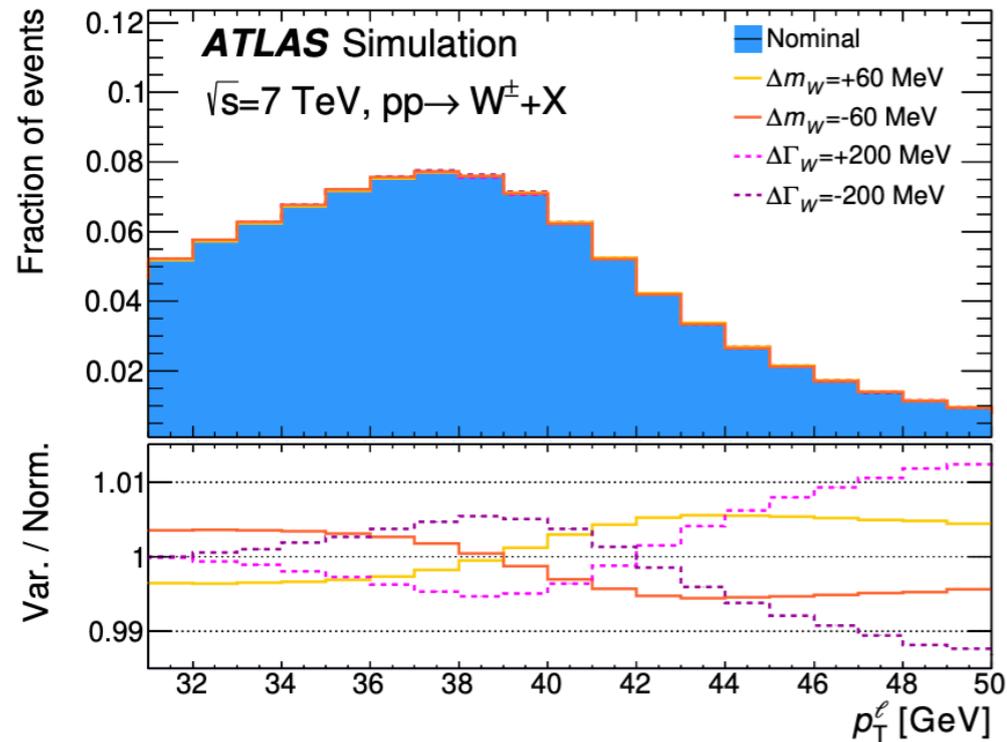
BLUE Combination for p_T and m_T results

- ▶ The p_T fit largely dominates the final result (95% weight

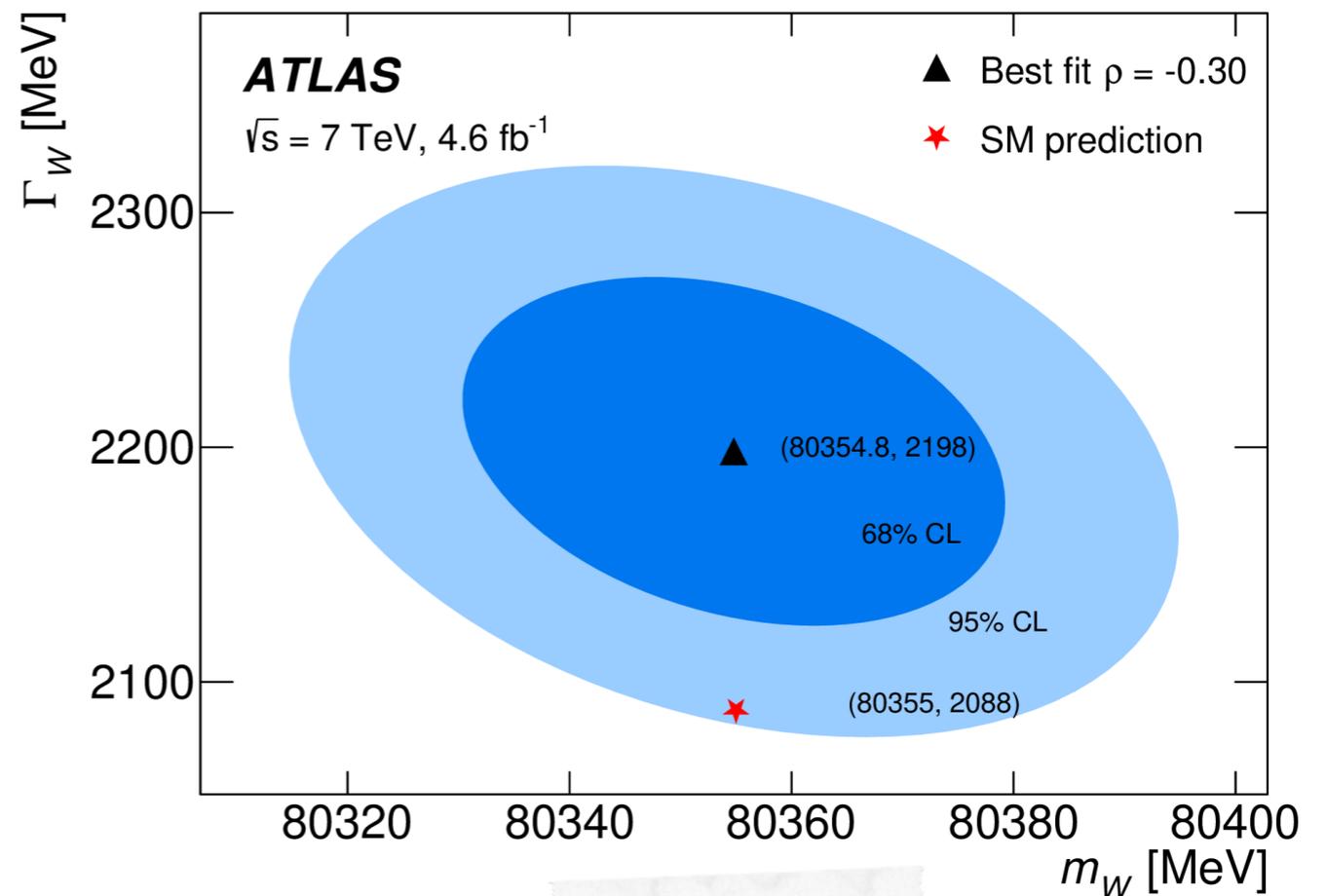
$$m_W = 80360 \pm 5(\text{stat.}) \pm 15(\text{syst.}) = 80360 \pm 16 \text{ MeV}$$



simultaneously extracting Mass and width



Contrary to m_W , the fitted value of Γ_W depends more strongly on the assumed value of the mass $\Delta \Gamma_W = -1.25 \Delta m_W$



For the CT18 PDF set, the combination yields values of $m_W = 80354.8 \pm 16.1$ MeV
 $\Gamma_W = 2198 \pm 49$ MeV,

Uncertainty decomposition



[arXiv:2307.04007](https://arxiv.org/abs/2307.04007)

Interpreting Uncertainties in Profile-Likelihood Fits

- The usual separation into “statistical” and “systematic” components can be misleading.
 - Statistical-only fits underestimate the true statistical uncertainty when systematics are included.
 - Systematic impacts overestimate the genuine systematic contribution.
 - Impact plots should not be used directly for combinations or interpretation fits.
- The Gaussian approximation [Global in the CMS decomposition] give a consistent split of uncertainties consistent with other method.

Example ATLAS :

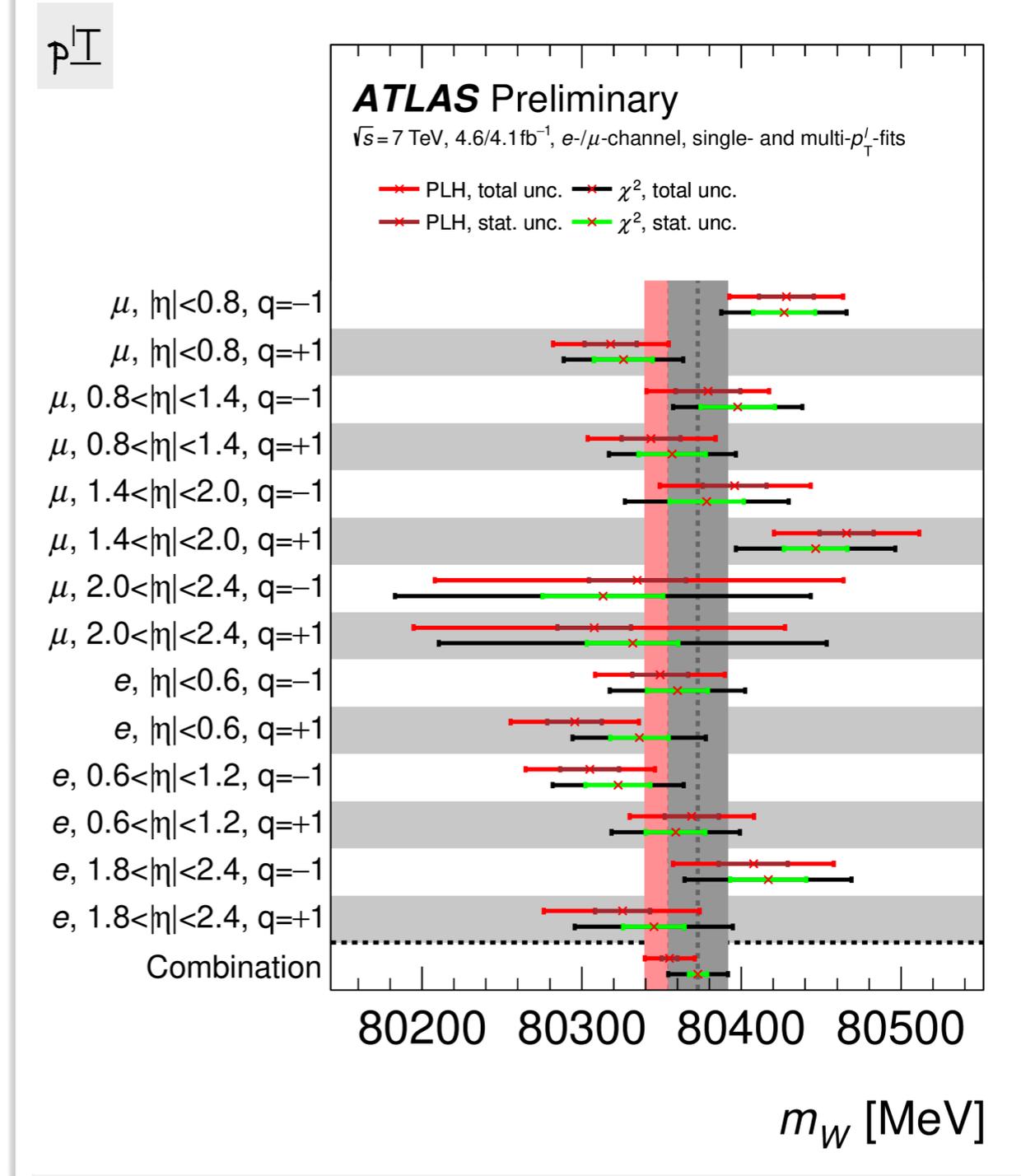
- The statistical uncertainty on final m_W analysis is ~ 10 MeV in the full profile-likelihood fit
 - Larger than the 6 MeV from statistical-only fits (with nuisance parameters fixed)
 - The genuine systematic uncertainty is ~ 13 MeV – smaller than conventional “impact” estimates.

Test consistency PLH fit

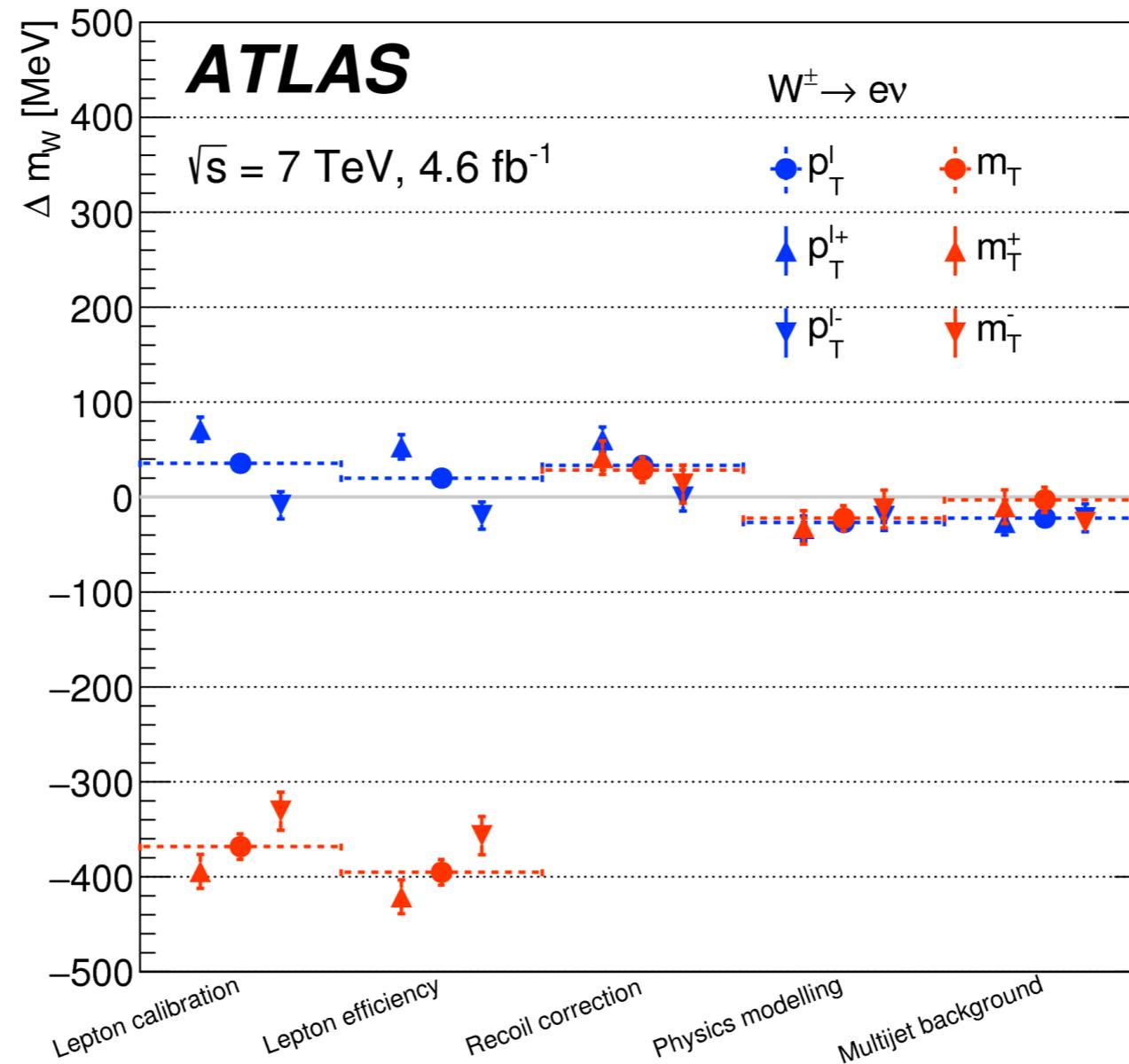
- ▶ PLH fit $m_W = 80355.1 \pm 15.6$ MeV (CT10nnlo PDF)
- ▶ $\Delta m_W = -14.4$ MeV ($m_W^{2017} = 80369.5 \pm 18.5$ MeV)
- ▶ Profiling of systematic uncertainties reduce δm_W by 15%

$\Delta(m_W)$ well within the expectation from Toys studies.

PLH fit validation using CT10 PDFs

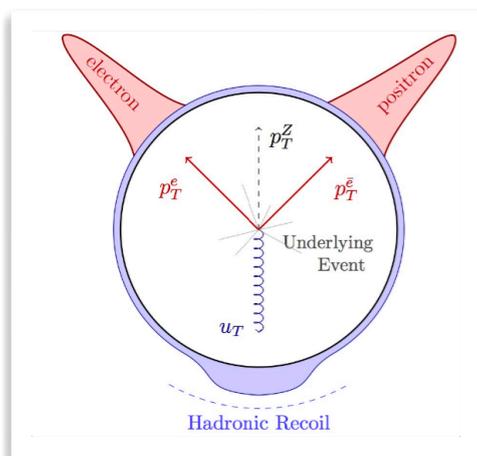
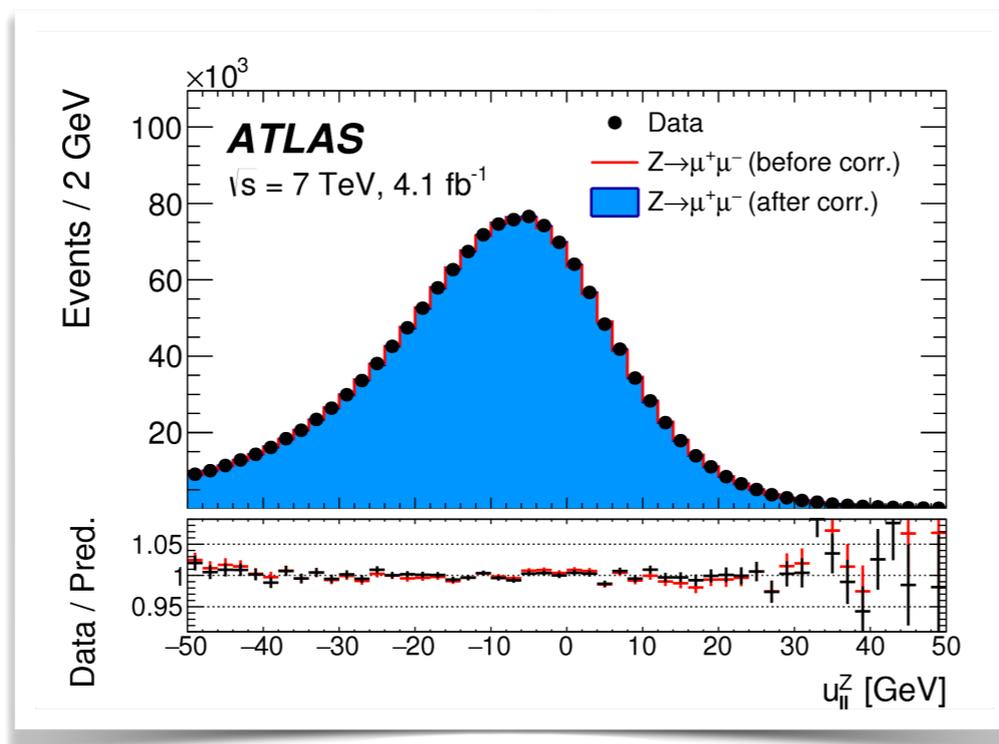
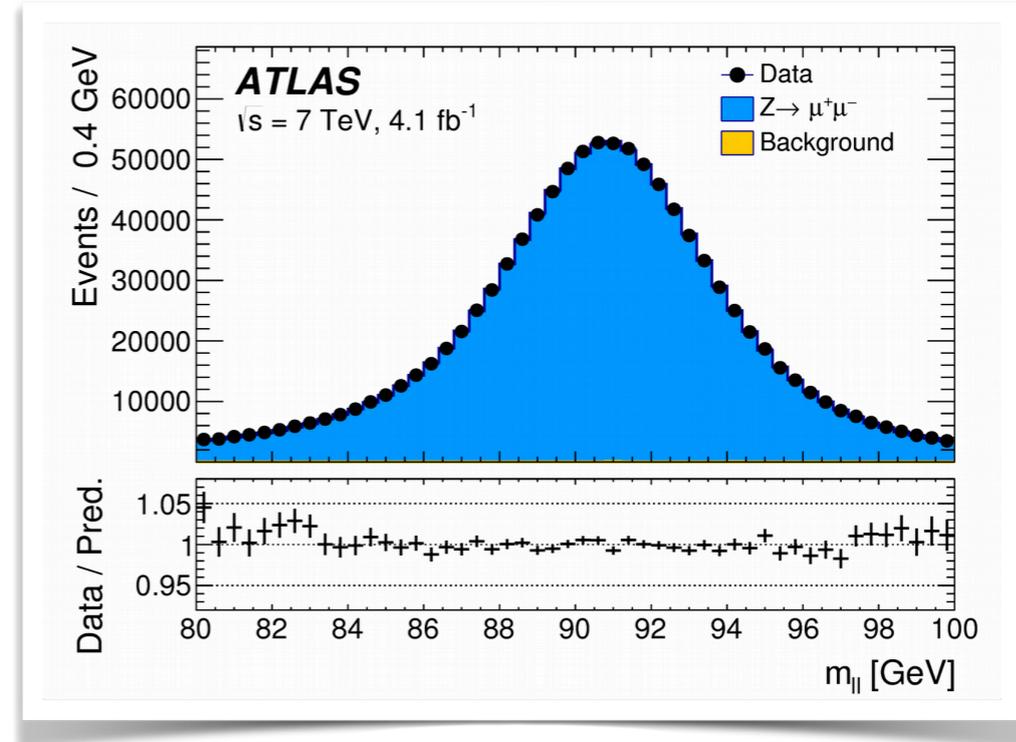
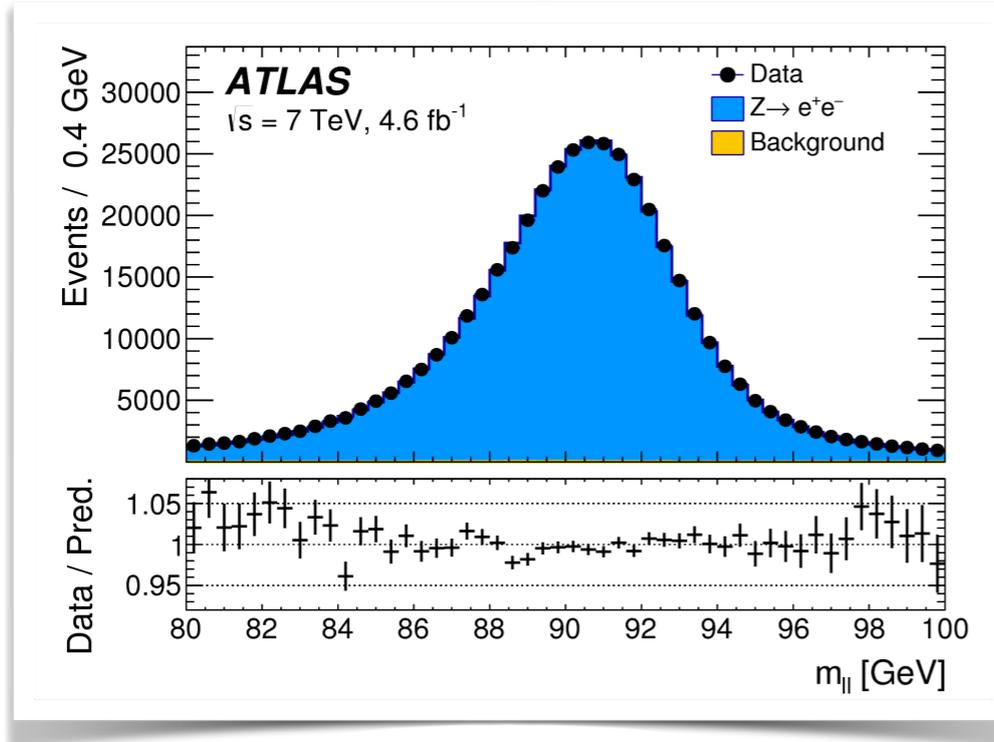


The precision we need



| | | | |
|------------|-----------------------------------------|----------------------------------|--------------------------------------------------------------------|
| Dataset | 17 fb ⁻¹ @ 13 TeV | | LHCb |
| Channels | | | 7 fb ⁻¹ @ 13 TeV (pileup) 2016 only |
| Observable | only p _T lepton | p _T , m _T | muons 2.2 < η ^μ < 4.4 |
| Modelling | TNP (theoretical nuisance parameters) | Z ↔ W extrapolation of the model | simultaneous fit to Z → μμ events binned in φ* ≈ p _T /M |

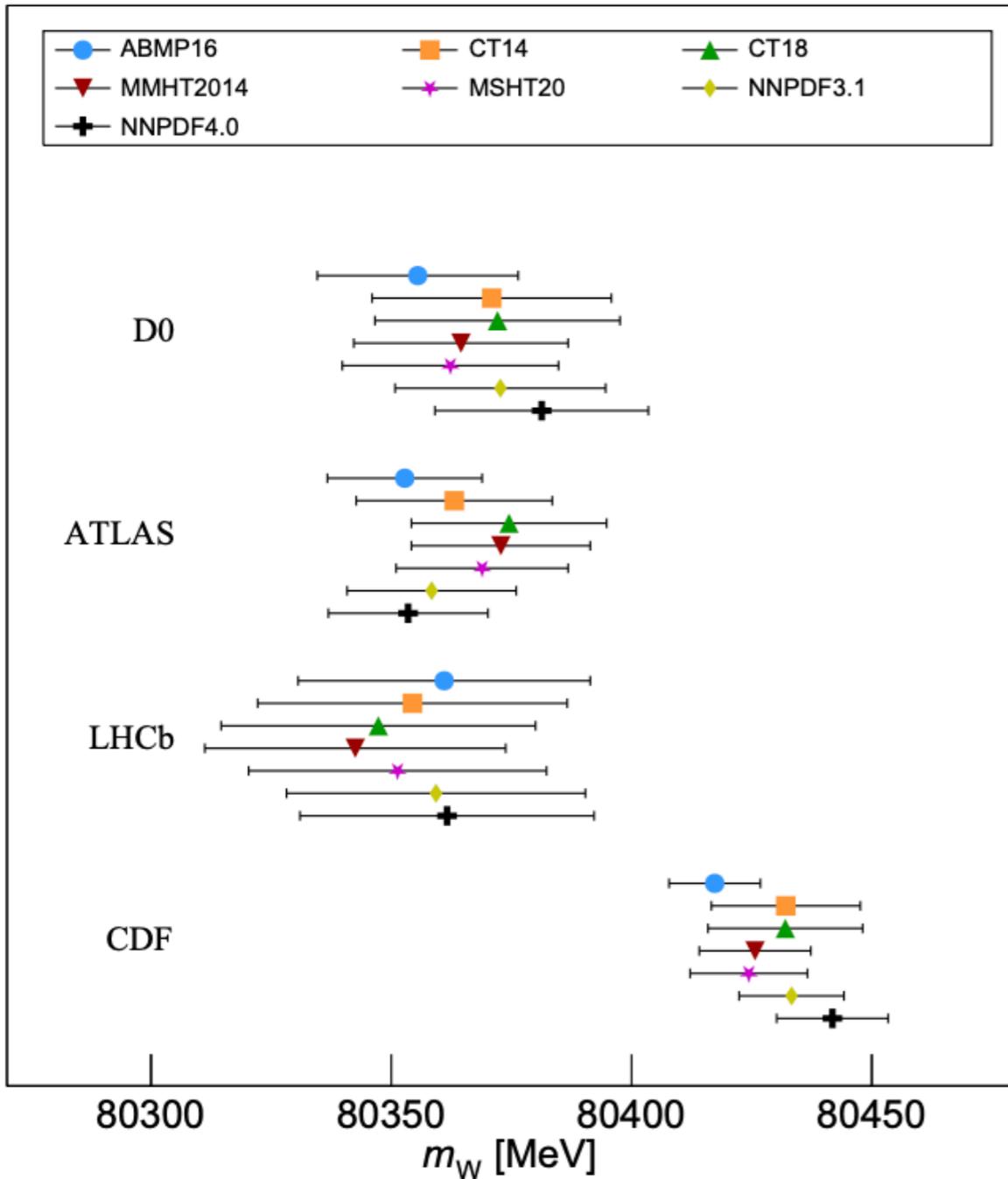
in ATLAS - Z samples



The response of u_{\perp} is measured in data using the p_{\perp}^Z balance in Z events

- Z boson events are used to derive detector calibrations.
- **Experimental precision :**
 - Lepton performances at sub-% level $\Rightarrow \delta m_W \sim 7-10 \text{ MeV}$
 - Hadronic Recoil calibration at % level $\Rightarrow \delta m_W \sim 12 \text{ MeV}$

often objects-calibration precision is trade of between clean environment and Z samples statistic [particularly true for low- μ]



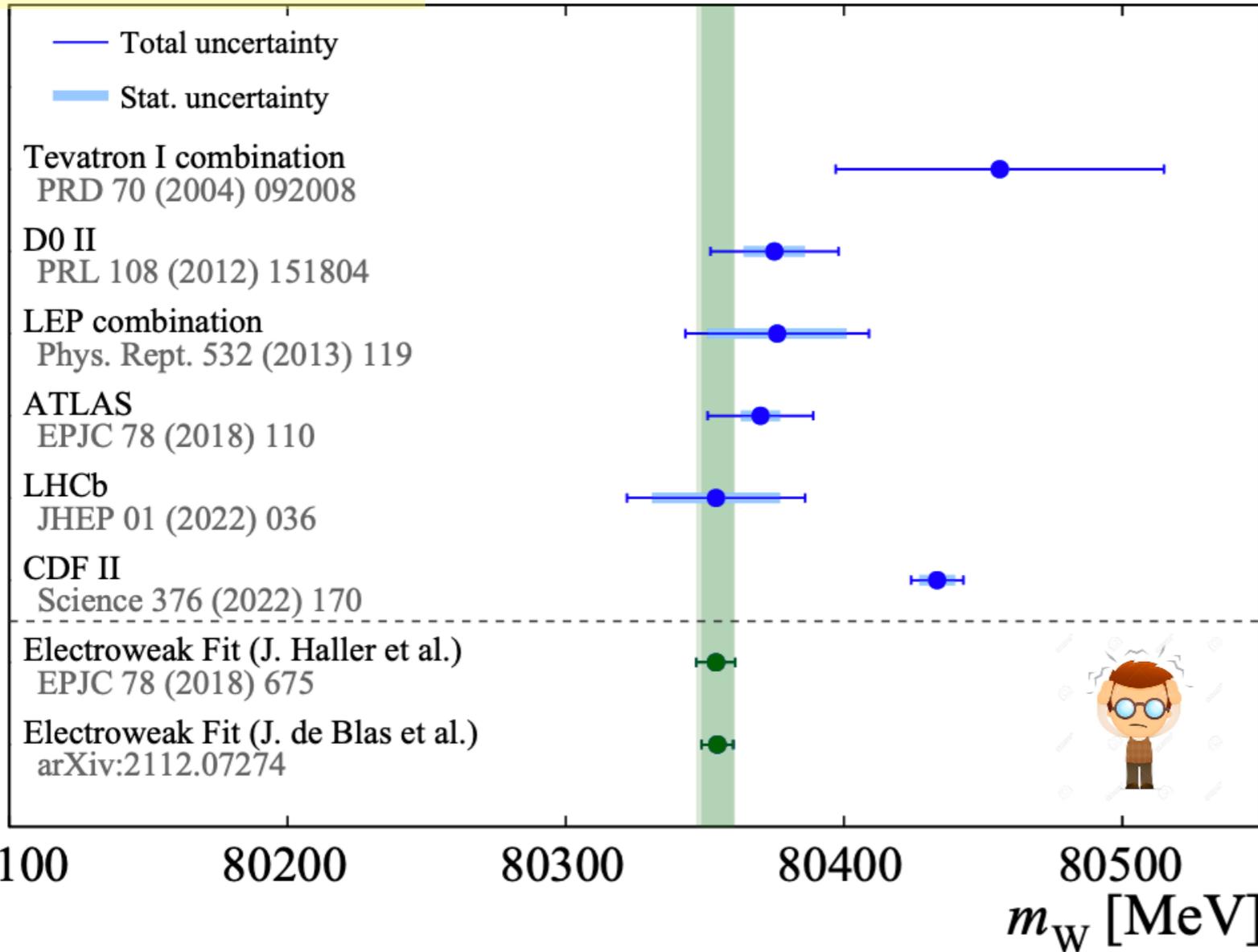
Eur. Phys. J. C (2024) 84: 451

LHC-EW WG

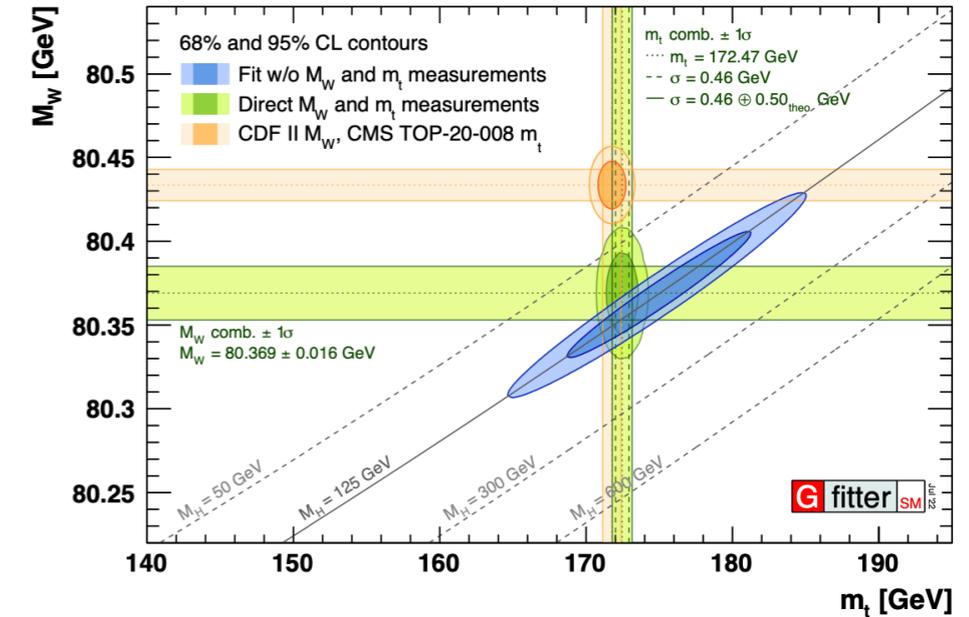
W mass combination

Tevatron/LHC W-mass combination

[LHCB-FIGURE-2022-003]



R.Kogler ICHEP2022



► Measuring m_W at the LHC (pp) is more challenging than at the Tevatron ($pp\text{-bar}$)

- PDF-induced polarisation uncertainty

- 2nd generation quarks

► 3(2) sigma tension between CDF and ATLAS(LHCb)

Tevatron/LHC W-mass combination

- ▶ Ongoing LHC/TeVatron Electroweak WG effort towards combination
 - ▶ Crucial to understand theoretical correlations between measurements: prime examples **PDFs** and lepton angular correlations (**Ai**)

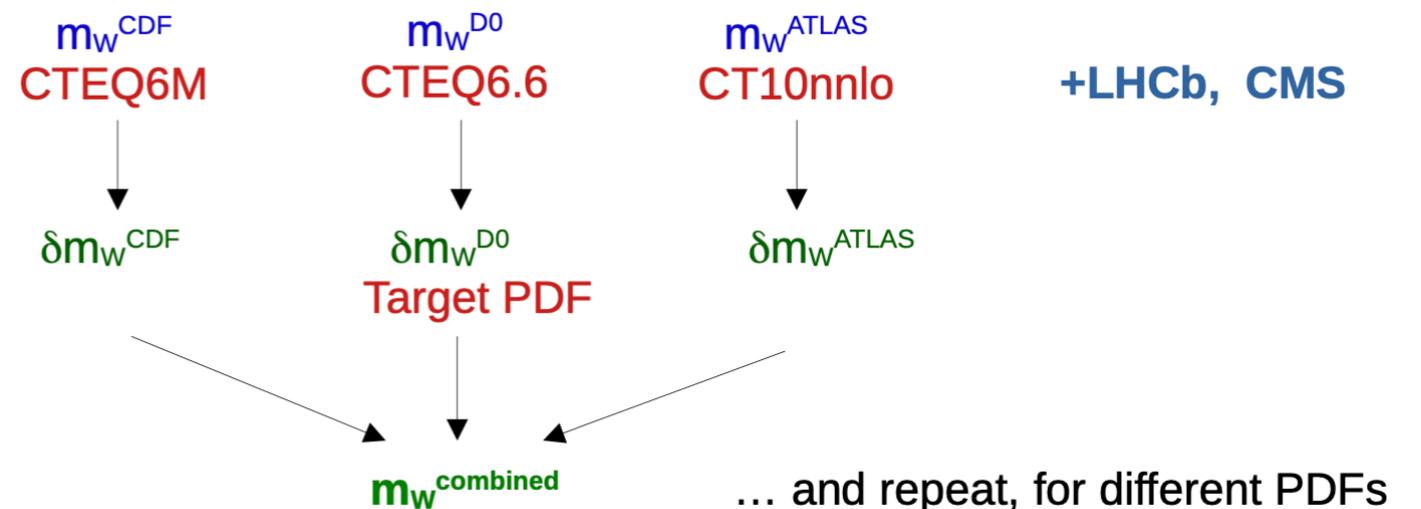
$$m_W^{new} = m_W^{ref} - \delta m_W^{QCD} - \delta m_W^{PDF}$$

published value
Improved predictions
PDF extrapolation

δm_W^{PDF} correction to reference PDF

δm_W^{QCD} correction to QCD modelling beyond quoted uncertainties

- ▶ **PDFs main source of correction and uncertainty correlations**
- ▶ Other sources very small (EW corrections) or mostly decorrelated (pT W/Z)
- ▶ Correction applied in a two-step procedure:
 1. Correct all measurements to a common PDF/QCD
 2. Combine them properly including correlations



Tevatron/LHC W-mass combination

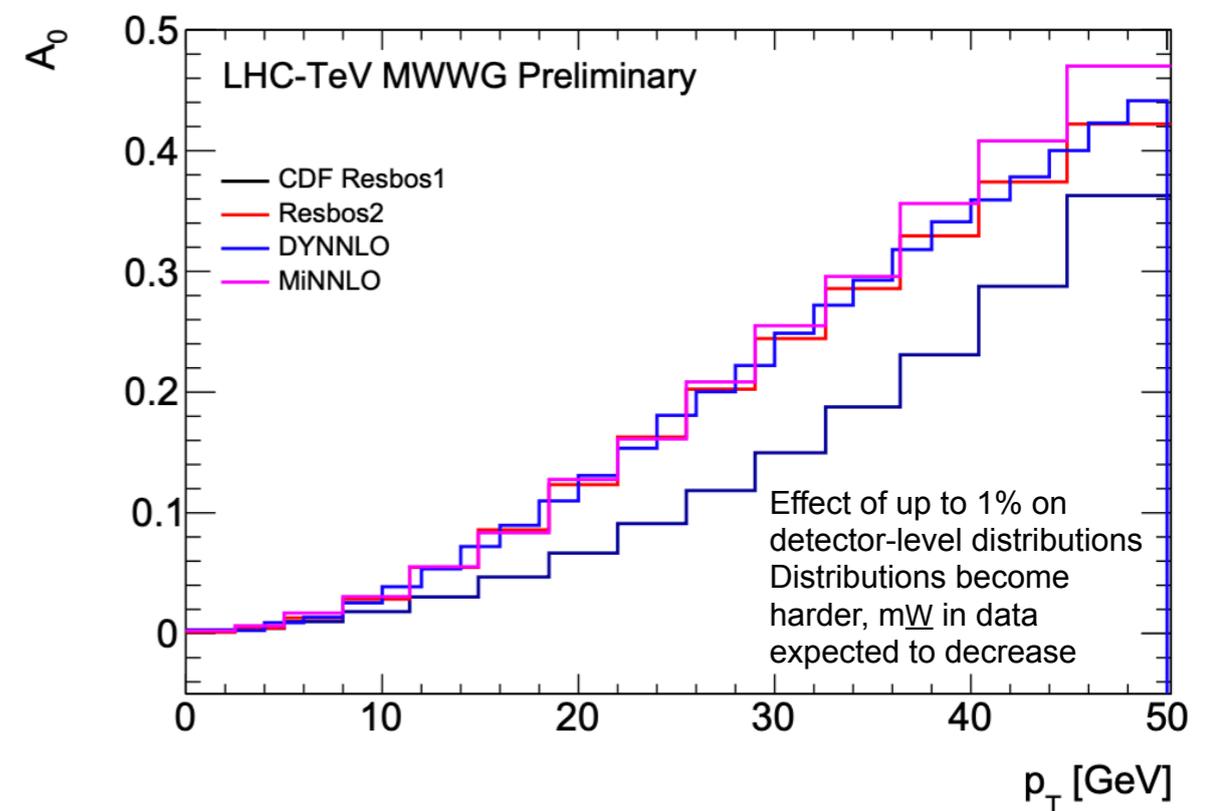
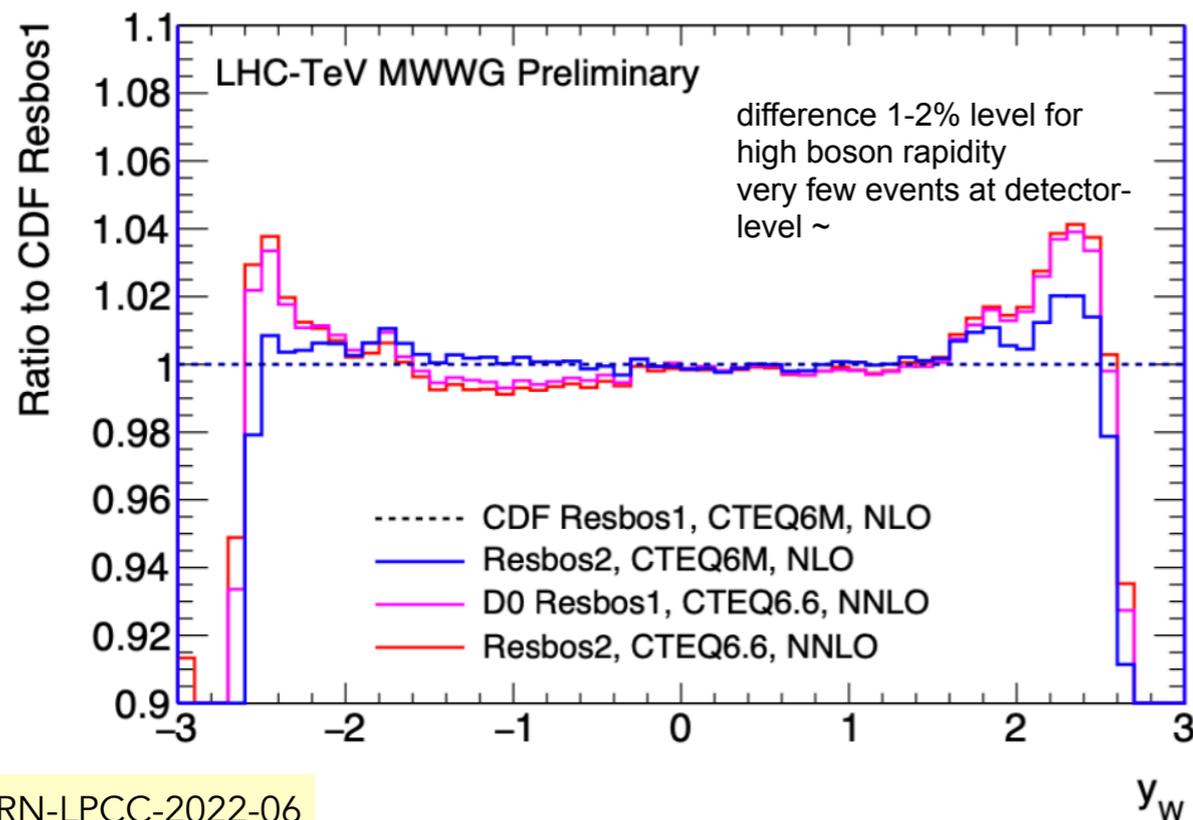
- ▶ Ongoing LHC/TeVatron Electroweak WG effort towards combination
 - ▶ Crucial to understand theoretical correlations between measurements: prime examples **PDFs** and lepton angular correlations (**A_i**)

$$m_W^{new} = m_W^{ref} - \delta m_W^{QCD} - \delta m_W^{PDF}$$

published value
Improved predictions
PDF extrapolation

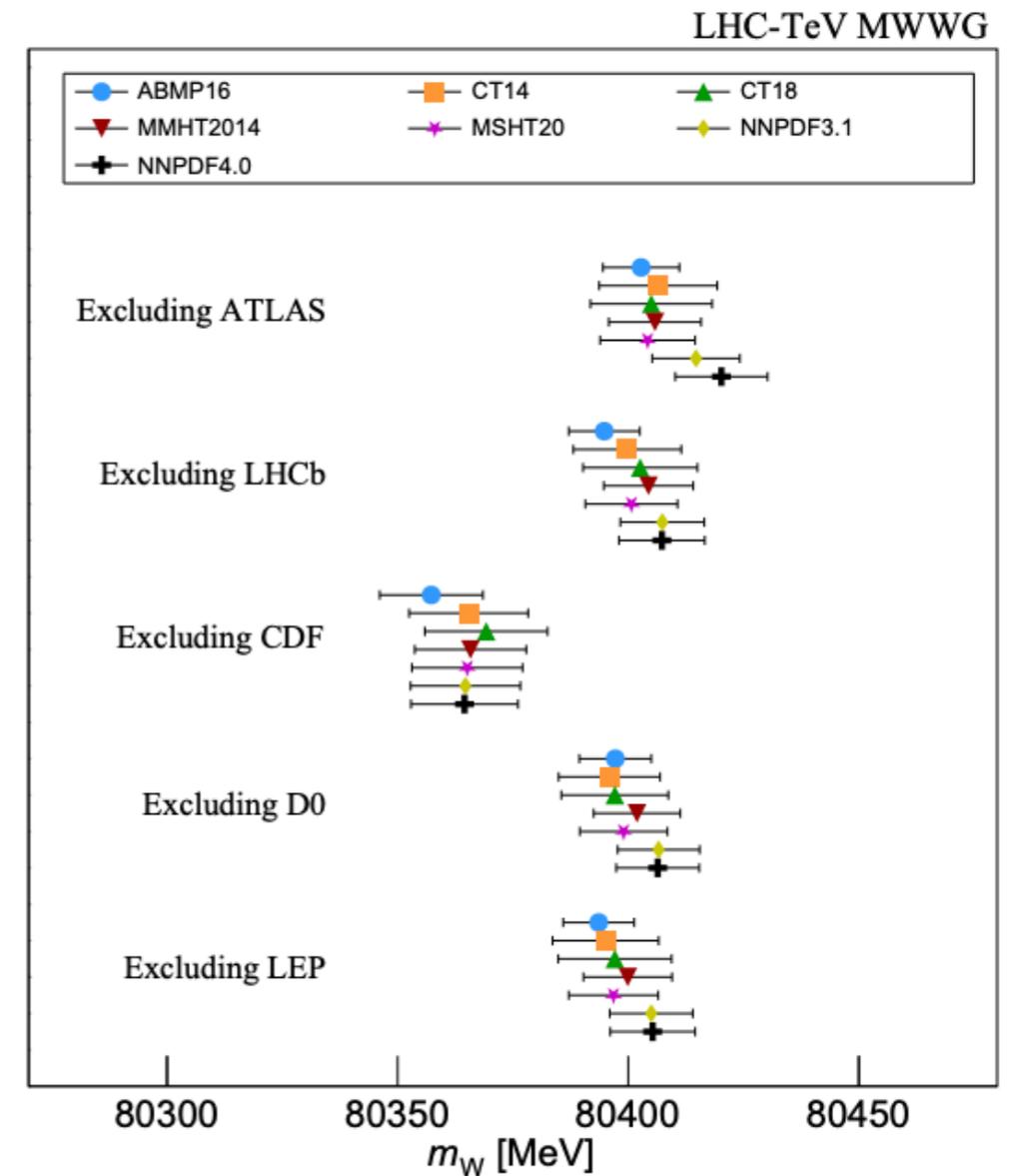
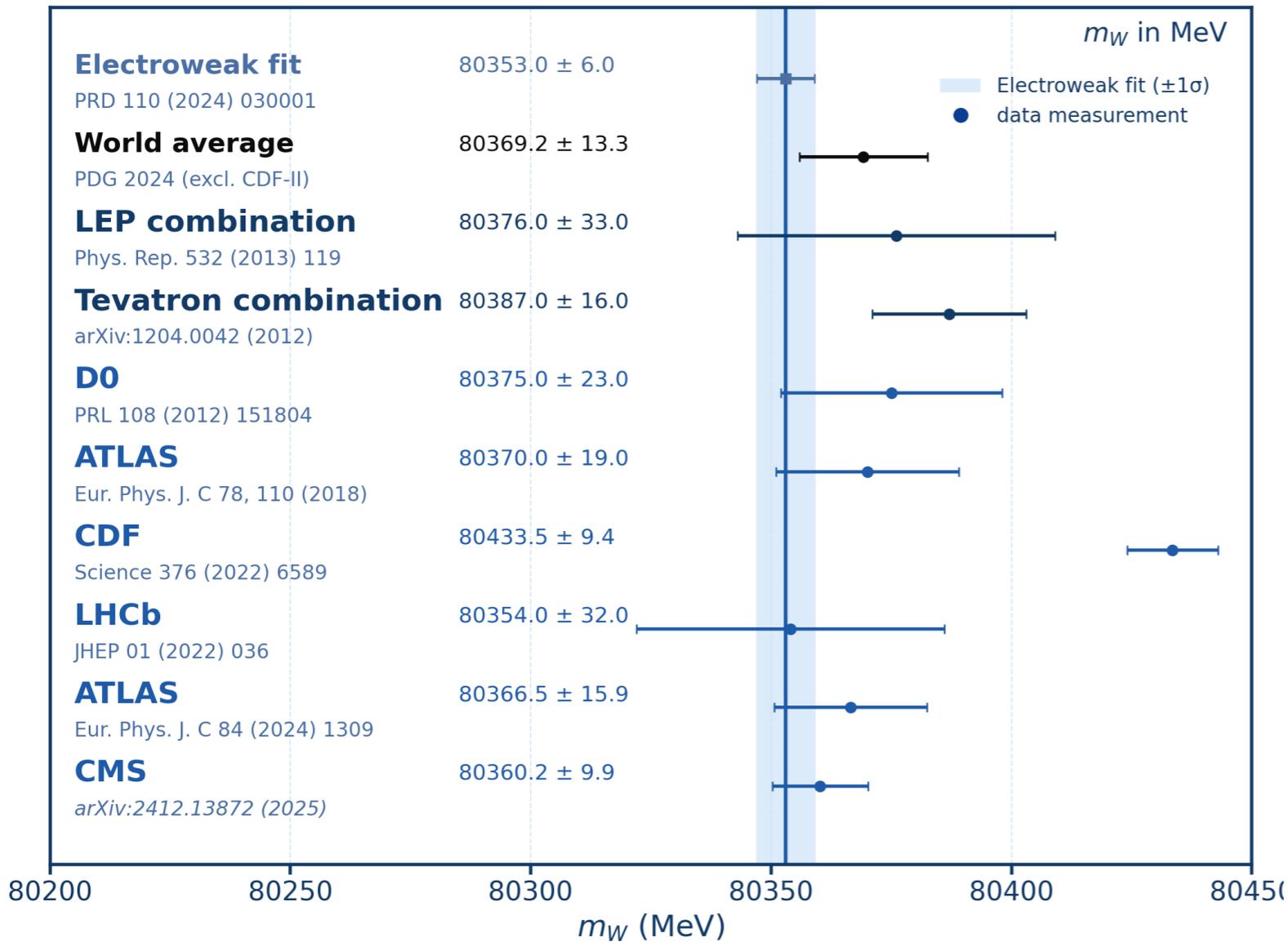
δm_W^{PDF} correction to reference PDF
 δm_W^{QCD} correction to QCD modelling beyond quoted uncertainties

- ▶ **Boson polarisation** in legacy Resbos different from Resbos2 and other codes: E.g. description of $W A_i$ in legacy Resbos codes not ideal, motivates of O(10 MeV) correction of Tevatron measurements



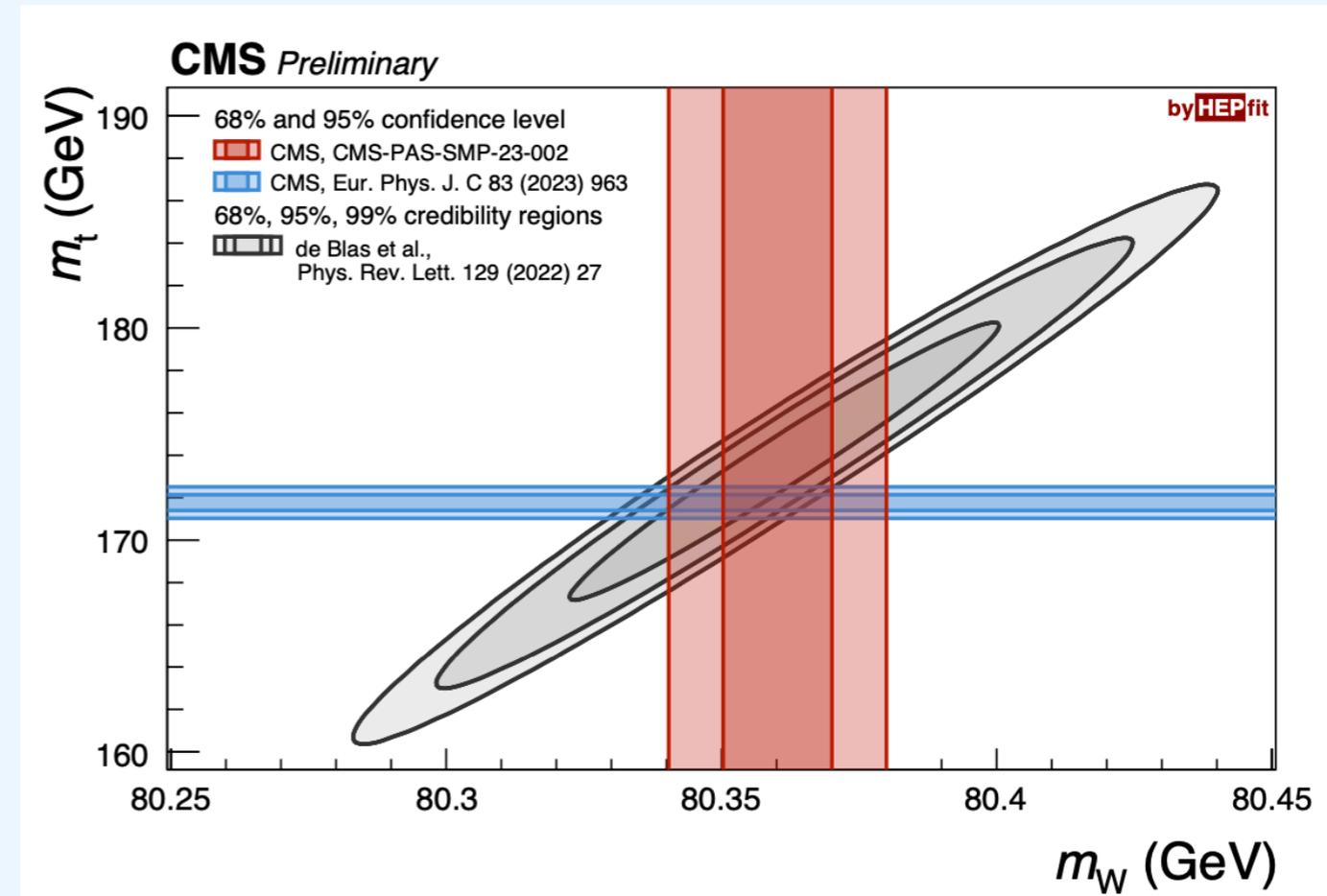
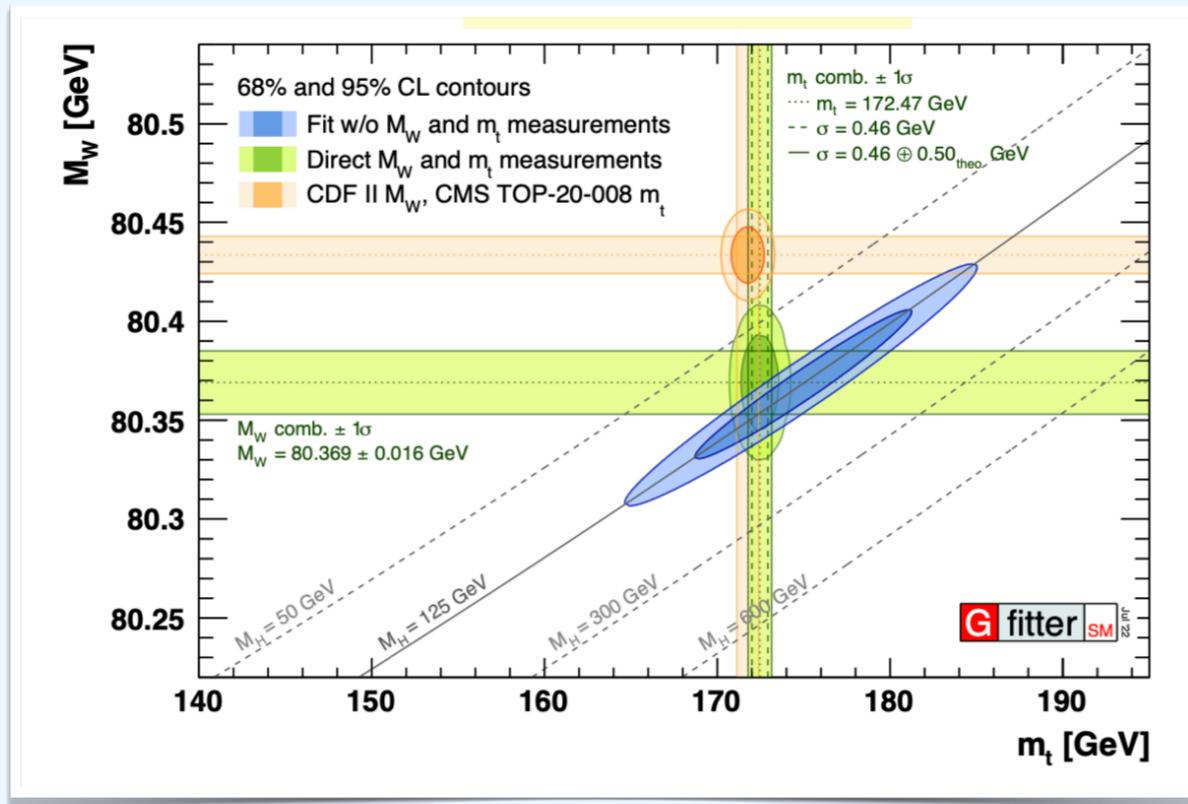
The W mass combination

W-boson mass measurements



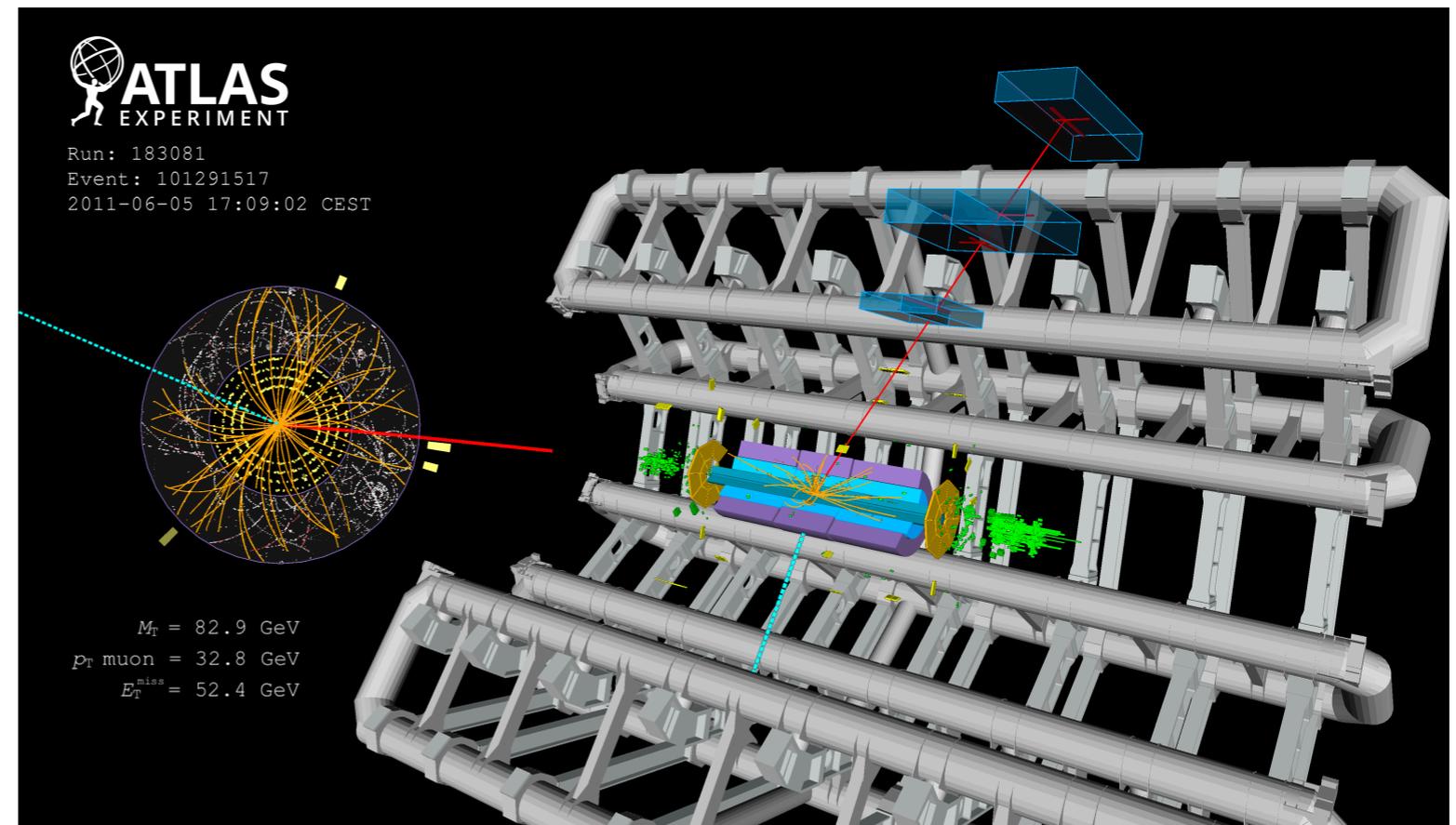
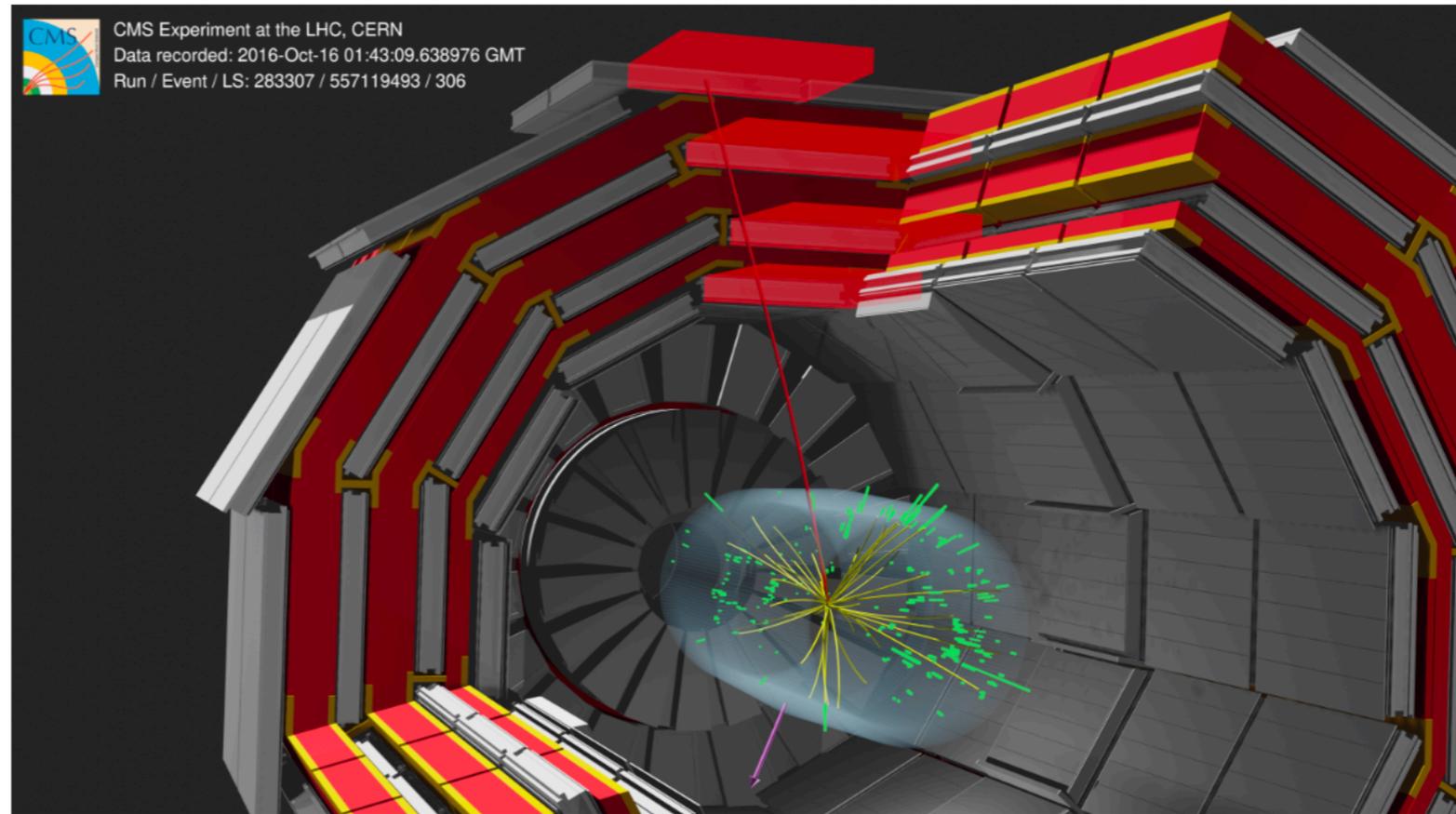
<https://arxiv.org/pdf/2308.09417>

SM is restored



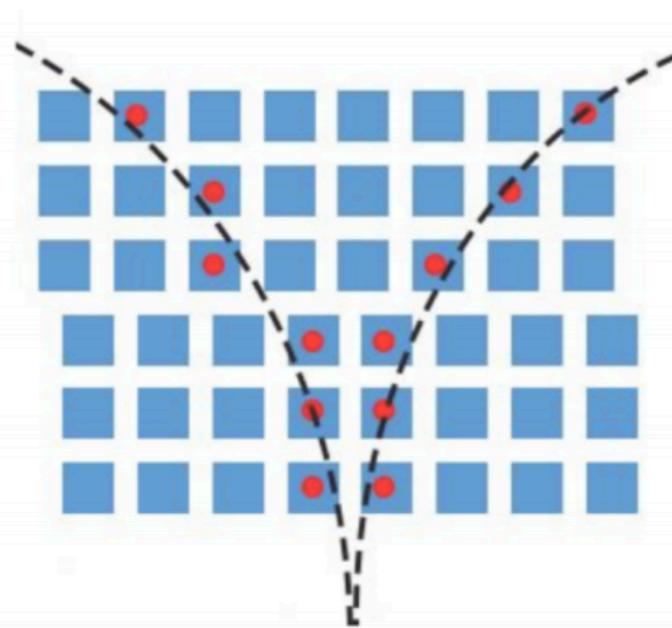
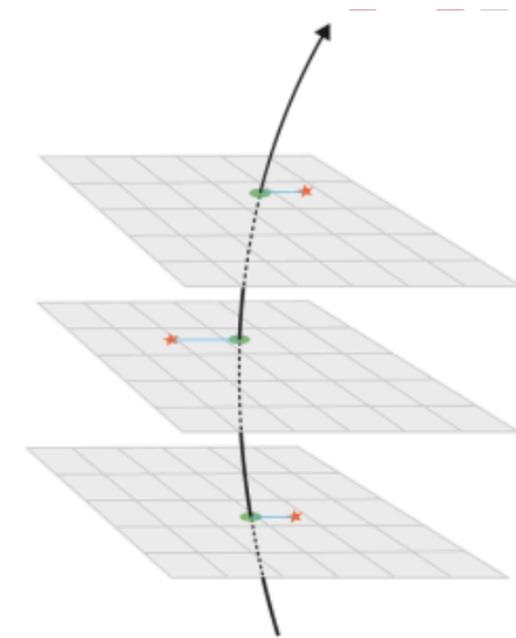
Ultra-precise. Surprisingly heavy.
 The CDF m_W result stands in tension with the Standard Model ... Latest ATLAS, CMS results restore agreement with the SM

Experimental challenges

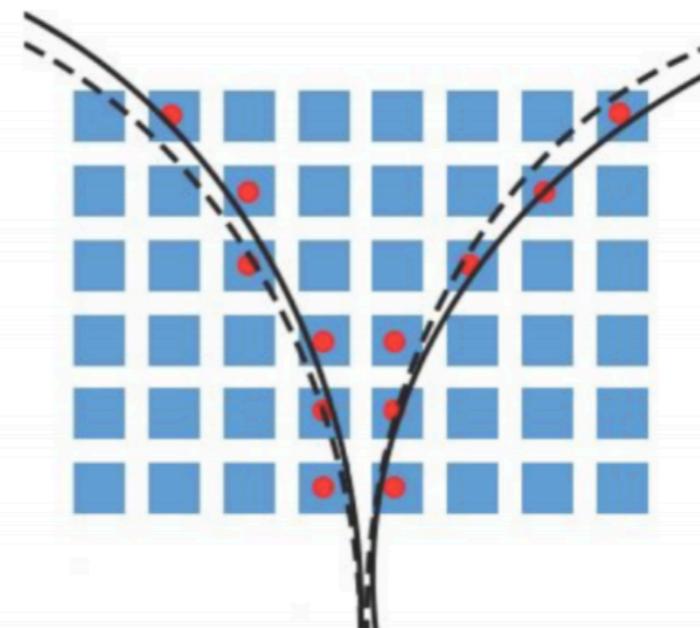


challenges of tracking calibration

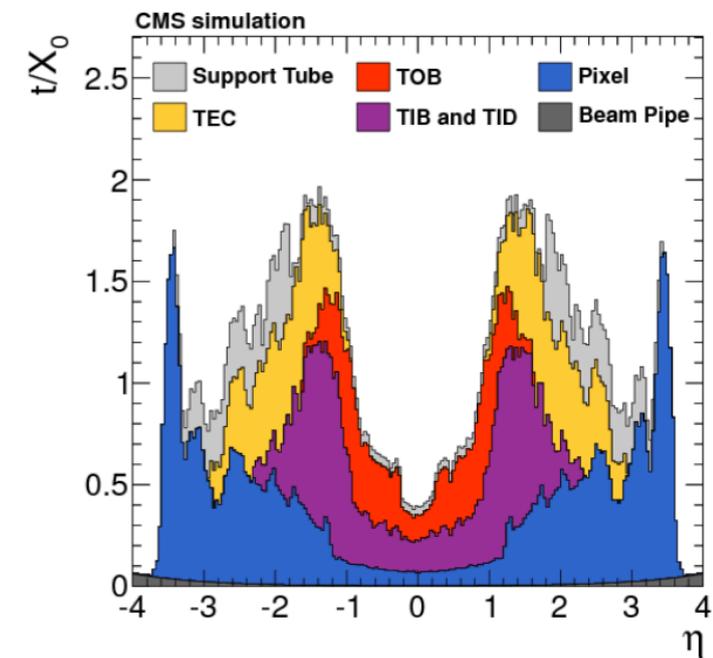
- Knowing location and quantity of material, and relative alignment of 12k tracker modules also crucial
 - Need to know material traversed—not just silicon, but electronics, cables, support structure...
 - ➔ **5 MeV of bias equivalent to $\sim\Delta 5$ mm of iron in the tracker volume**
- Relative shifts from gravity, opening of the detector, modify alignment
 - ➔ **5 MeV uncertainty is a ~ 0.4 μm misalignment**



If the tracker is misaligned and we don't know it...

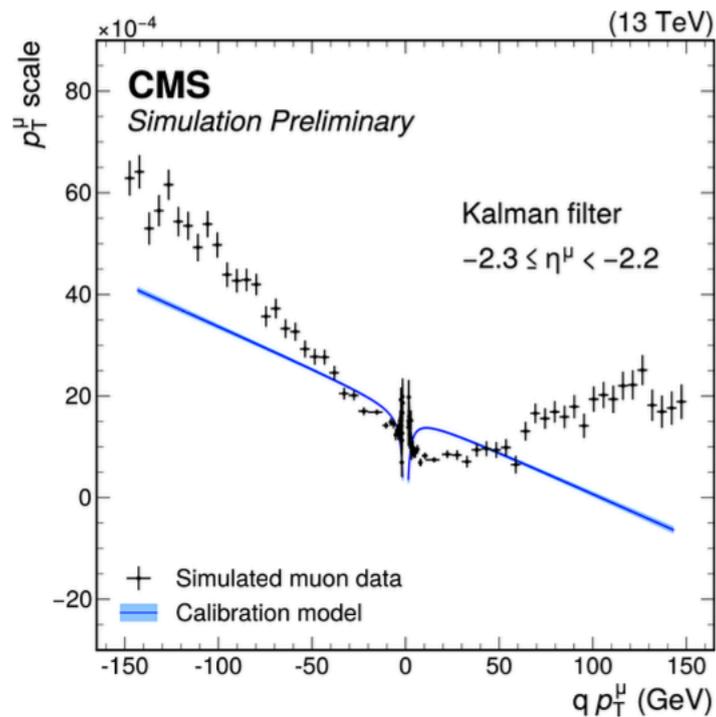
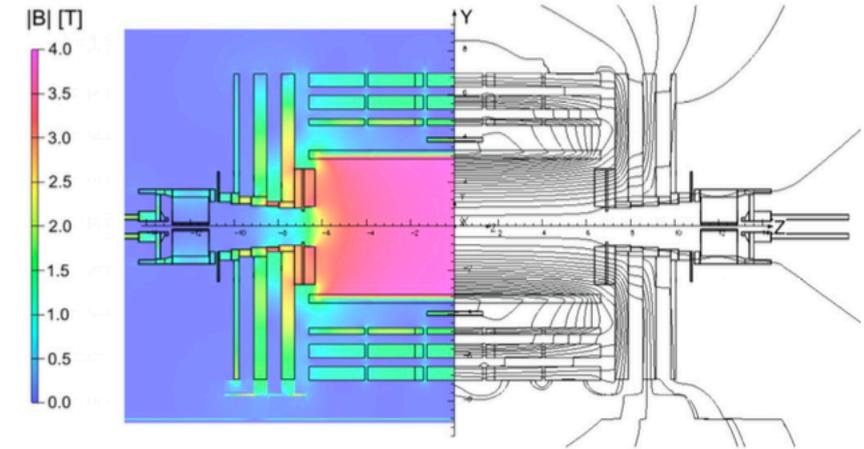


...the track will be reconstructed as if the tracker was aligned

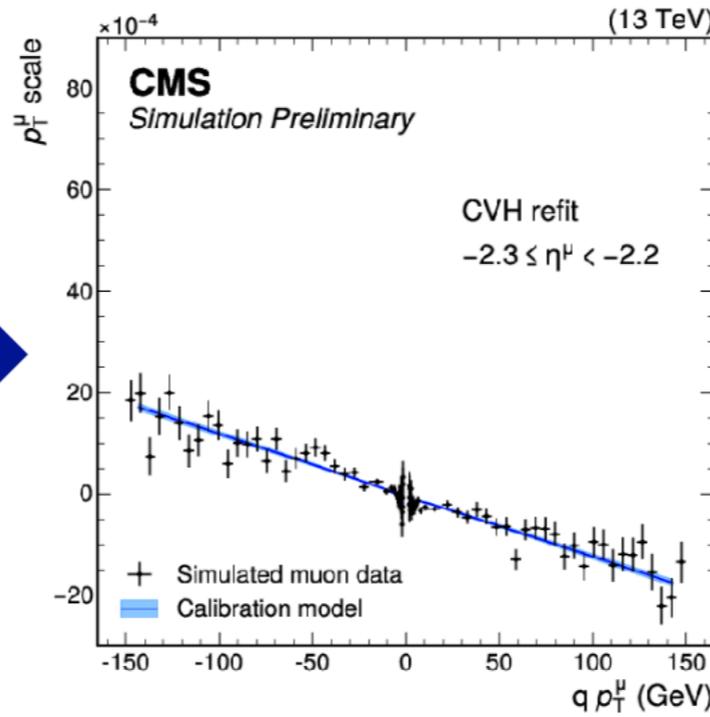
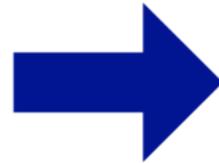


CMS

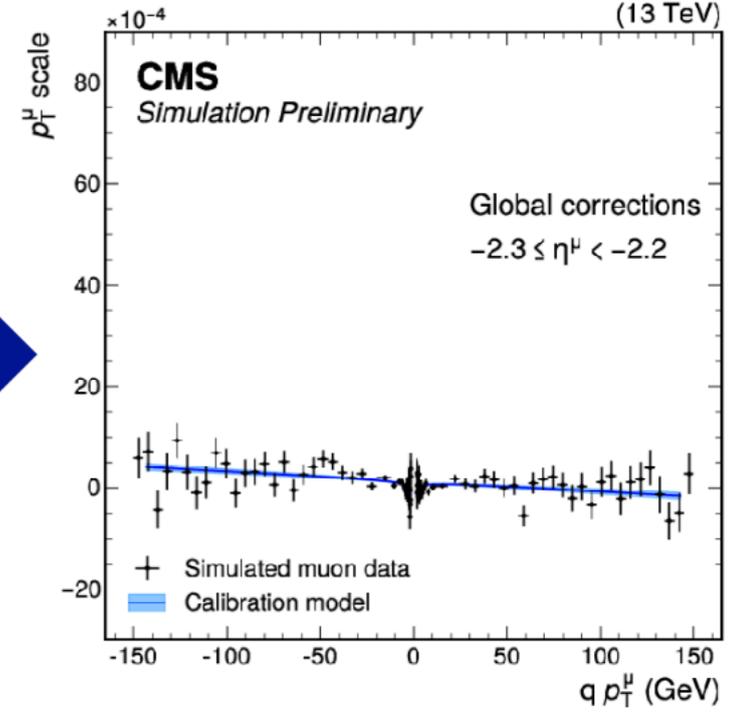
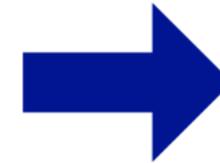
- Refit muon hits using custom “Continuous Variable Helix” fit
 - Model material in helix fit with Geant4+additional params for B-field
 - Increase Geant precision wrt standard CMS reco.
 - Use of high-precision B-field map (lower speed wrt standard reco.)
- ➔ Extract and apply per-module parameter corrections



CMS standard reco.



CVH refit

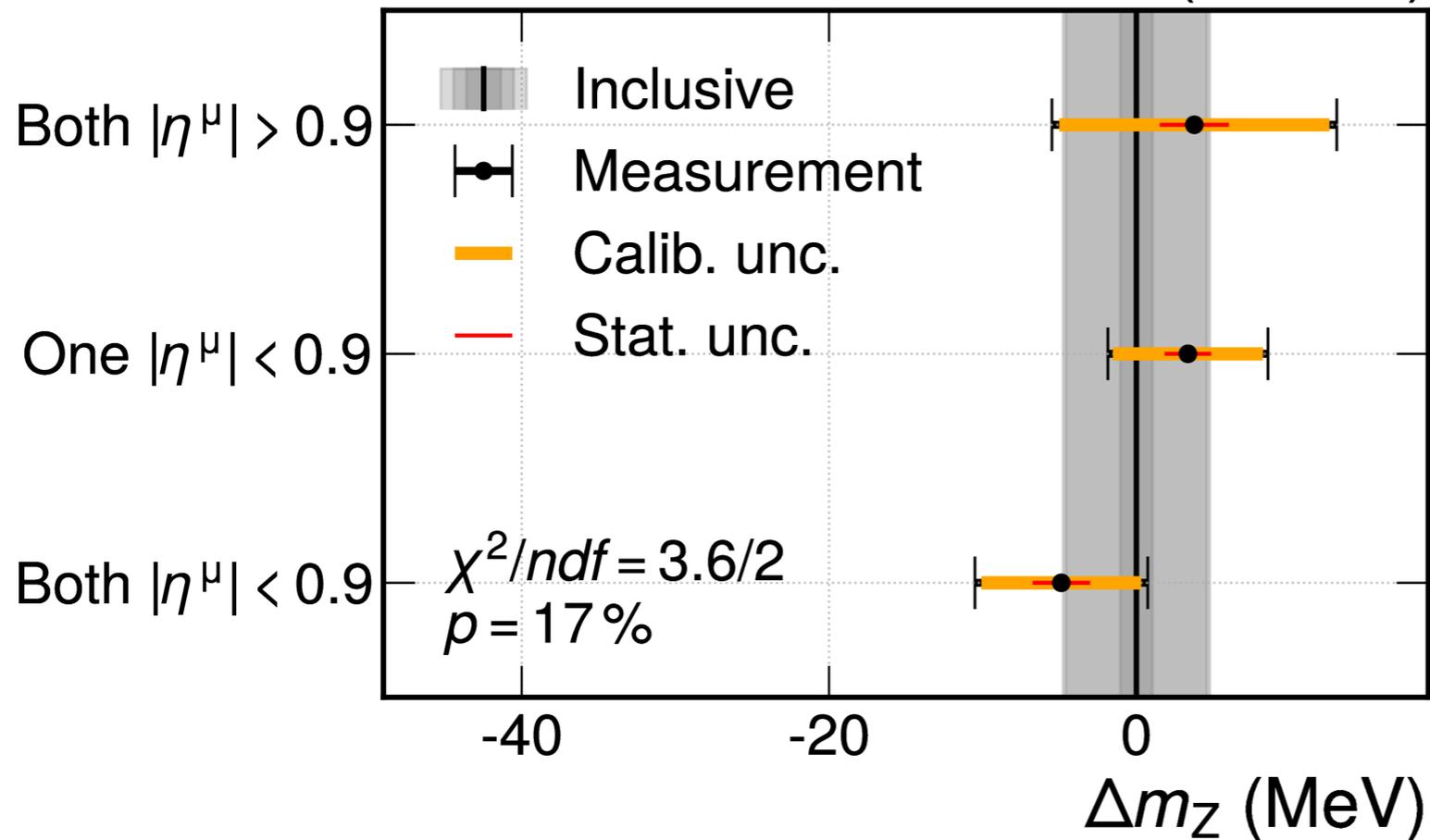


CVH refit+corr.

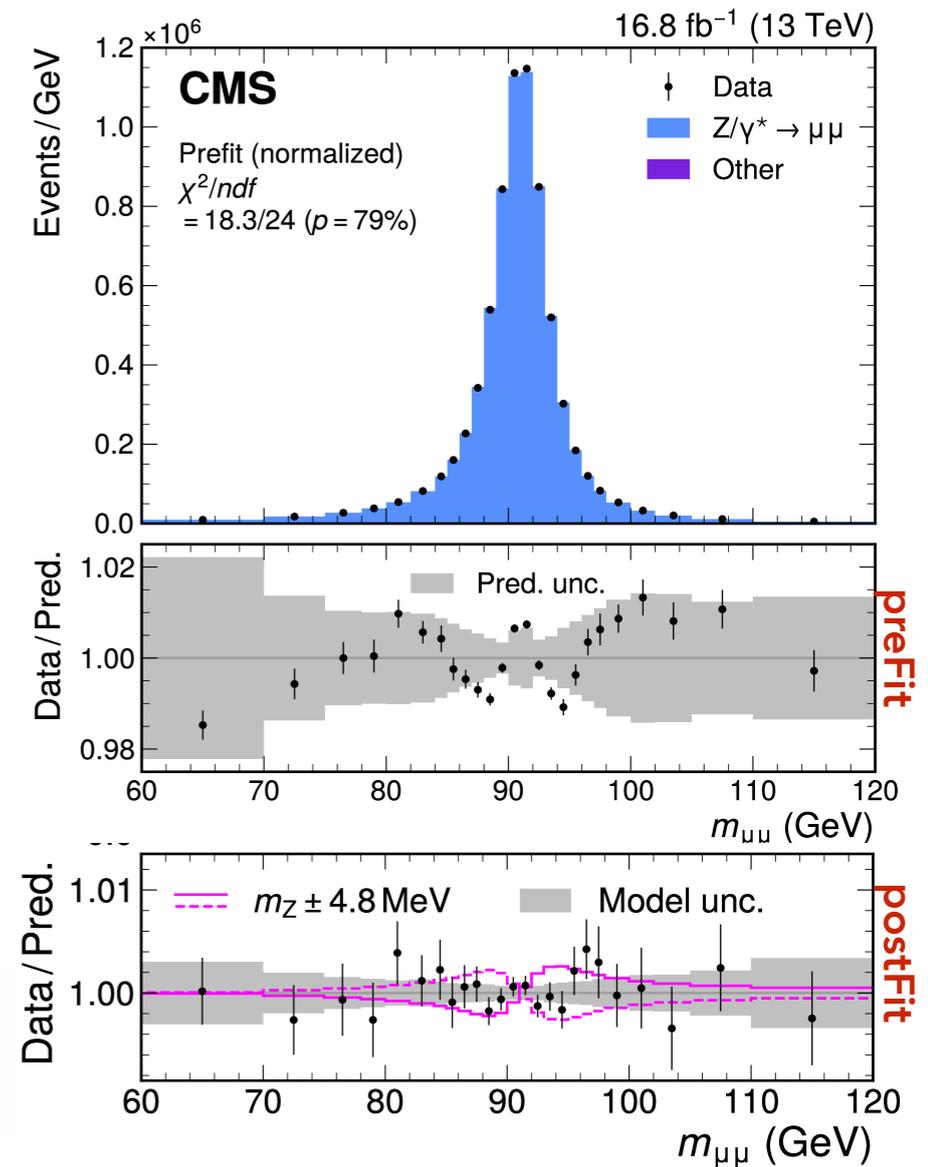
Z boson mass

Final validation of calibration uncertainties by extracting m_Z from the di-muon spectra \rightarrow 2D profile-likelihood fit in $m_{\mu\mu} \cdot \eta$
 Since J/ψ vs Z closure was used to tune calibration and enters the uncertainty model, not (yet) a fully independent measurement for inclusion in world average.

CMS 16.8 fb⁻¹ (13 TeV)



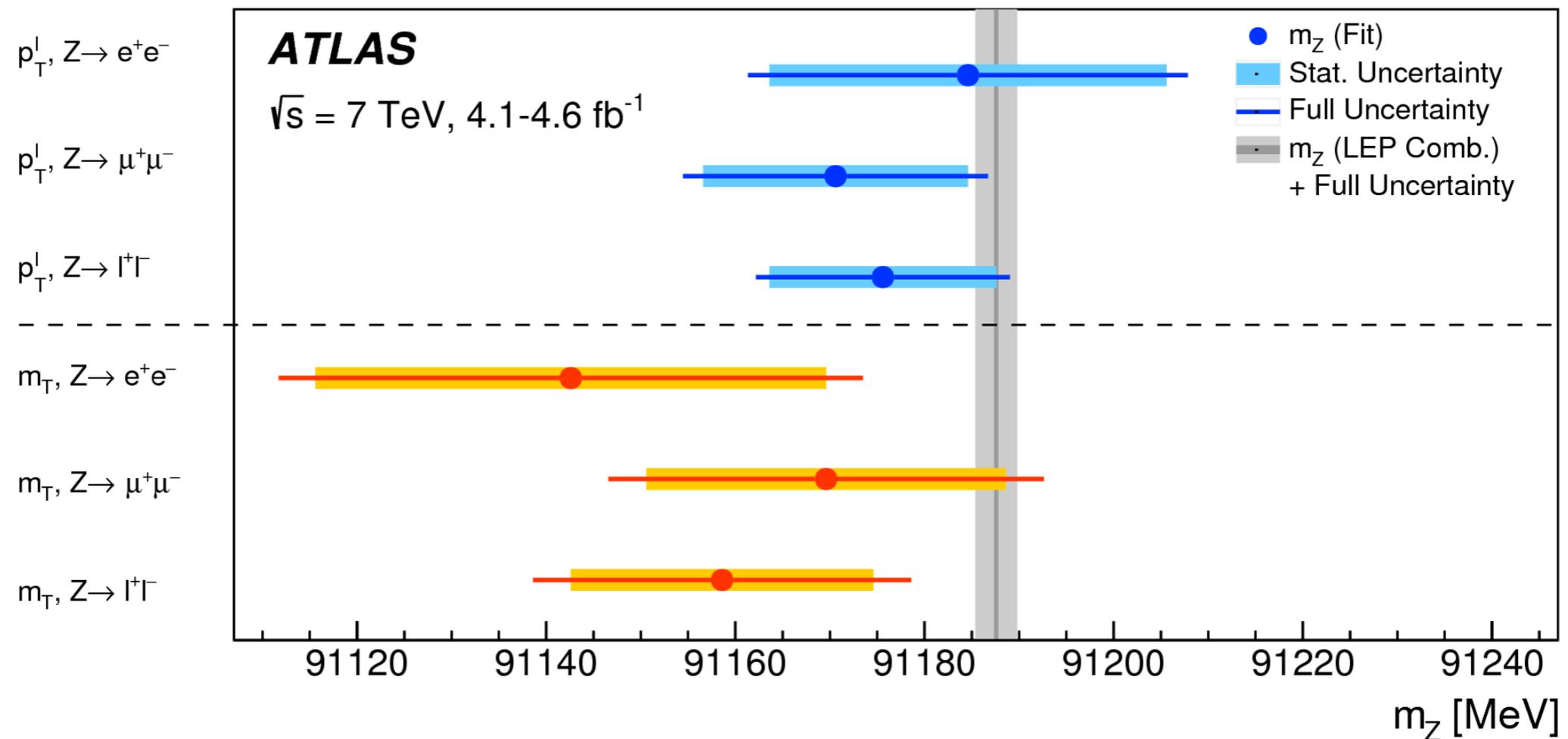
$$m_Z - m_Z^{\text{PDG}} = -2.2 \pm 4.8 \text{ MeV} = -2.2 \pm 1.0 \text{ (stat)} \pm 4.7 \text{ (syst) MeV}$$



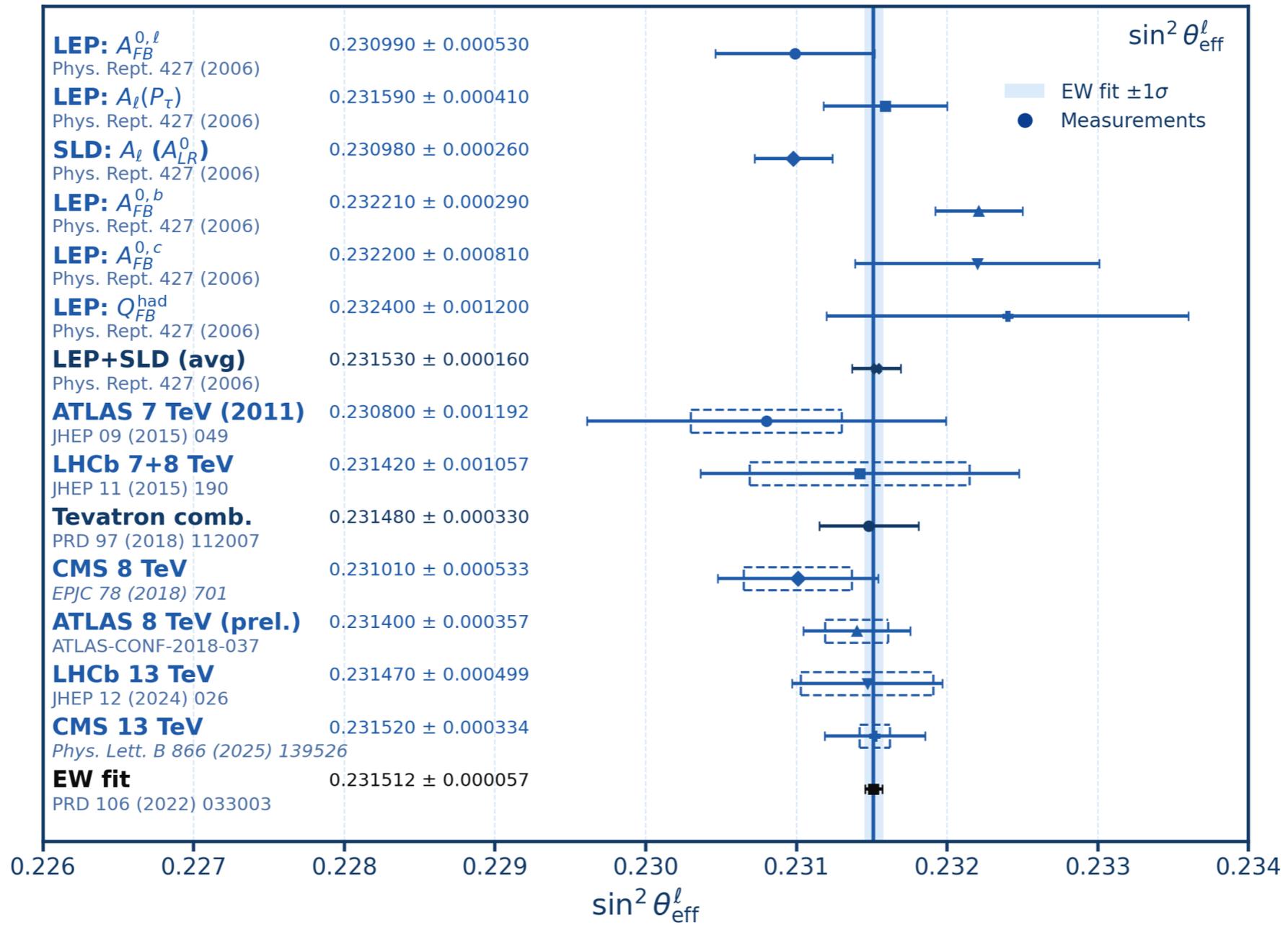
W-like sample with Z boson events

The measurement strategy is tested using Z-boson events to get a measurement of M_z .

- One of the charged leptons from Z-decay is treated as a neutrino
- The precision of this validation is limited by the Z-boson statistics, 10 times smaller than for W-boson



Summary of $\sin^2 \theta_{\text{eff}}^{\ell}$ determinations



weak mixing angle

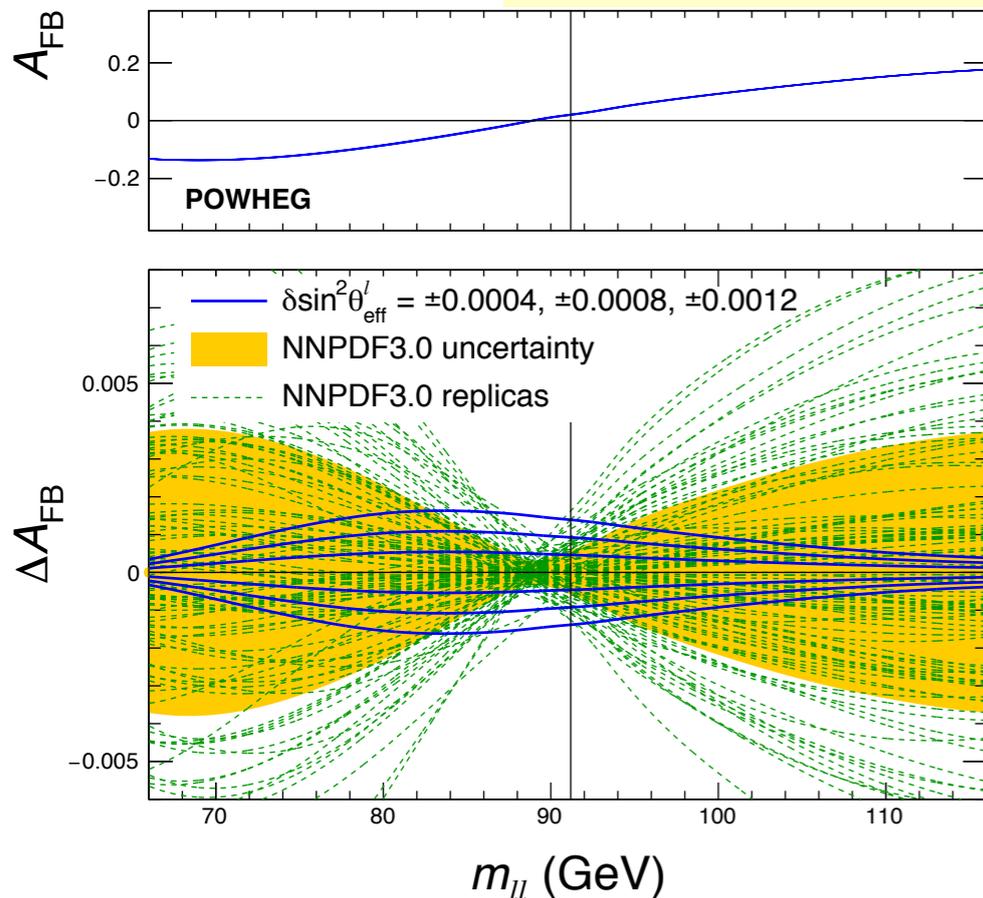
The weak mixing angle @LHC

$$\sin_{\text{eff}}^2 \theta_W = \left(1 - \frac{m_W^2}{m_Z^2} \right) \kappa$$

κ are EW loop corrections

- ▶ $\pm 20 \times 10^{-5}$ error in $\sin_{\text{eff}}^2 \theta_W$ corresponds to $\pm 10 \text{ MeV}$ error in m_W
 - another extremely powerful test of the EW sector of the SM.
 - another measurement quite challenging @LHC

Eur. Phys. J. C 78 (2018) 701

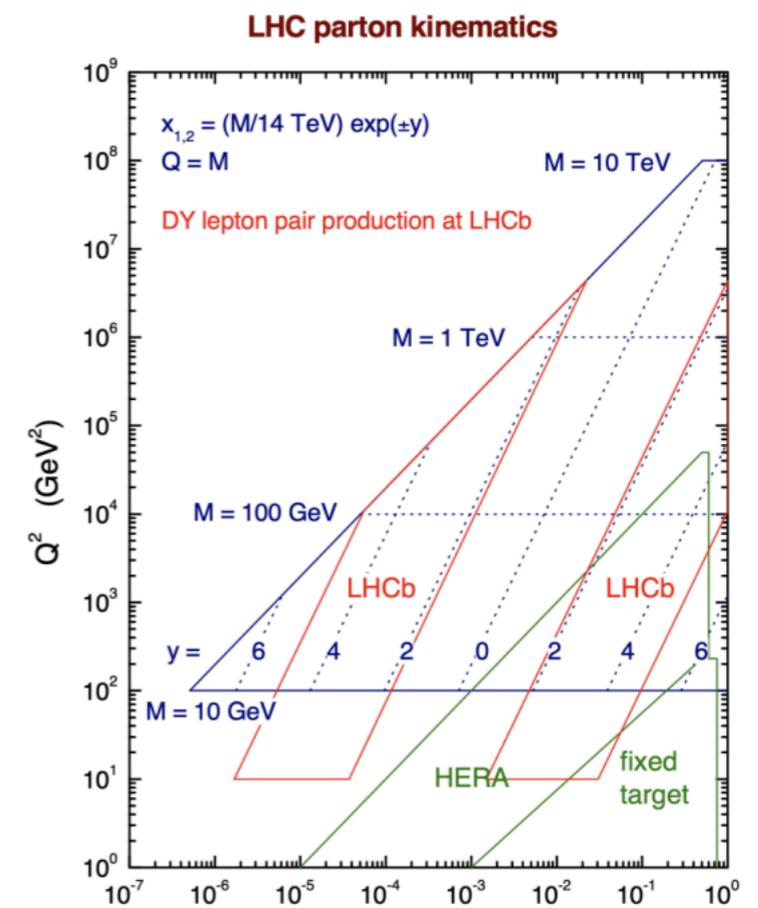
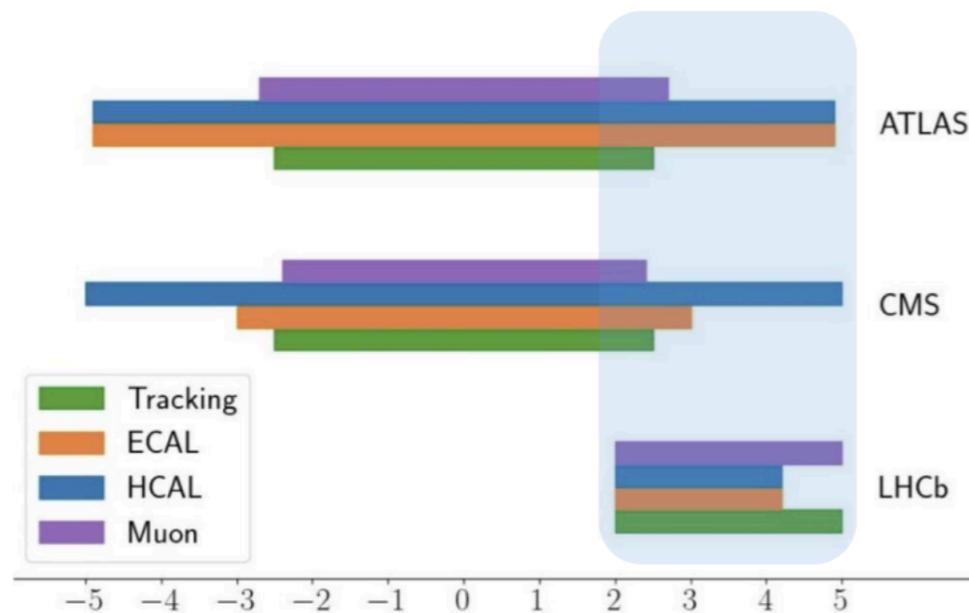


- ▶ $\sin_{\text{eff}}^2 \theta_W$ extracted from forward-background asymmetry in DY events: A_{FB}, A_4 (extraction is done in m_{ll}, y_{ll} bins)
- ▶ **Challenge:** strongly depends on PDF uncertainty.
 - At the **LHC** the colliding proton beams are FB symmetric → **the asymmetry vanishes at central rapidity, and grows as a function of rapidity**
 - Asymmetry largest at high y^Z where valence quark PDFs dominate at large x → ATLAS benefit from extending the acceptance of electron reconstruction for $|\eta| > 2.5$.
 - ▶ also depend on quark flavour, so on relative contributions of u and d PDFs

unique acceptance of LHCb

The x value of interacting partons is correlated with the boson rapidity Rapidity $y = \frac{1}{2} \ln \frac{x_1}{x_2}$

- Large rapidity: either very large x or very small x
- ATLAS/CMS and LHCb: complementary to each other



arXiv:0808.1847

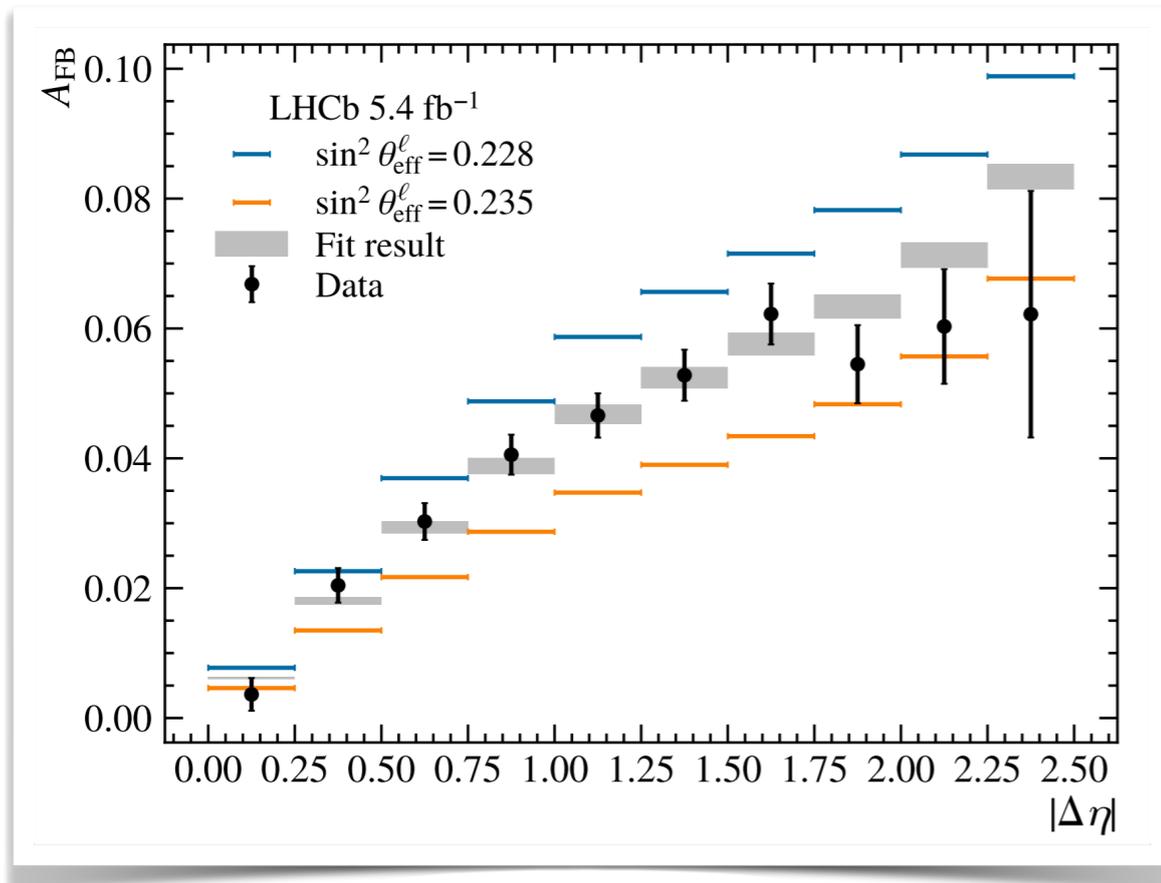
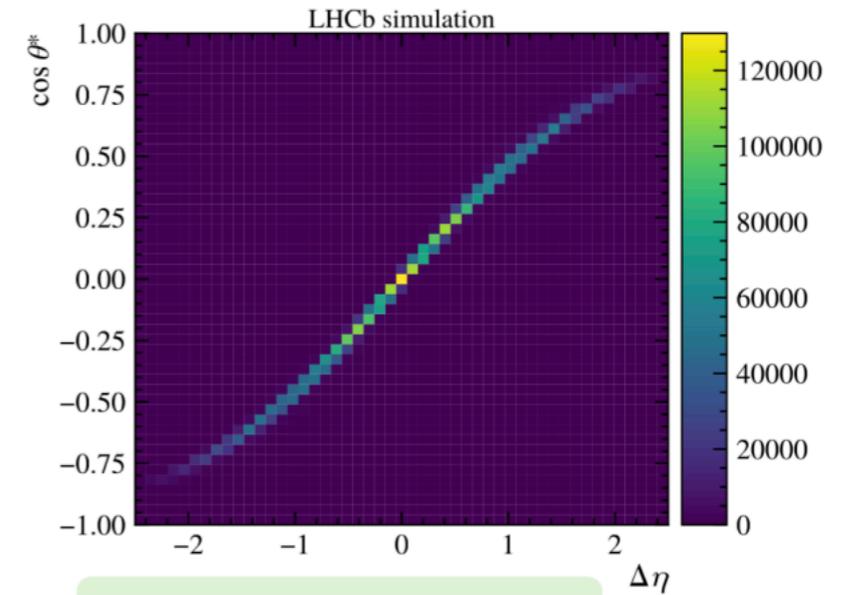
4

NB: PDF uncertainty are largely uncorrelated or anti-correlated between ATLAS-CMS and LHCb → highly beneficial for combination

LHCb

JHEP 13 (2024) 026

- small $|\cos\theta^*|$ mostly dilute the measurement
- $\cos\theta^* \sim \tanh(|\Delta\eta|/2)$, $\Delta\eta = \eta^- - \eta^+$
- Improves the precision of the $\sin^2\theta_{eff}^\ell$ measurement by **14%** in simulation



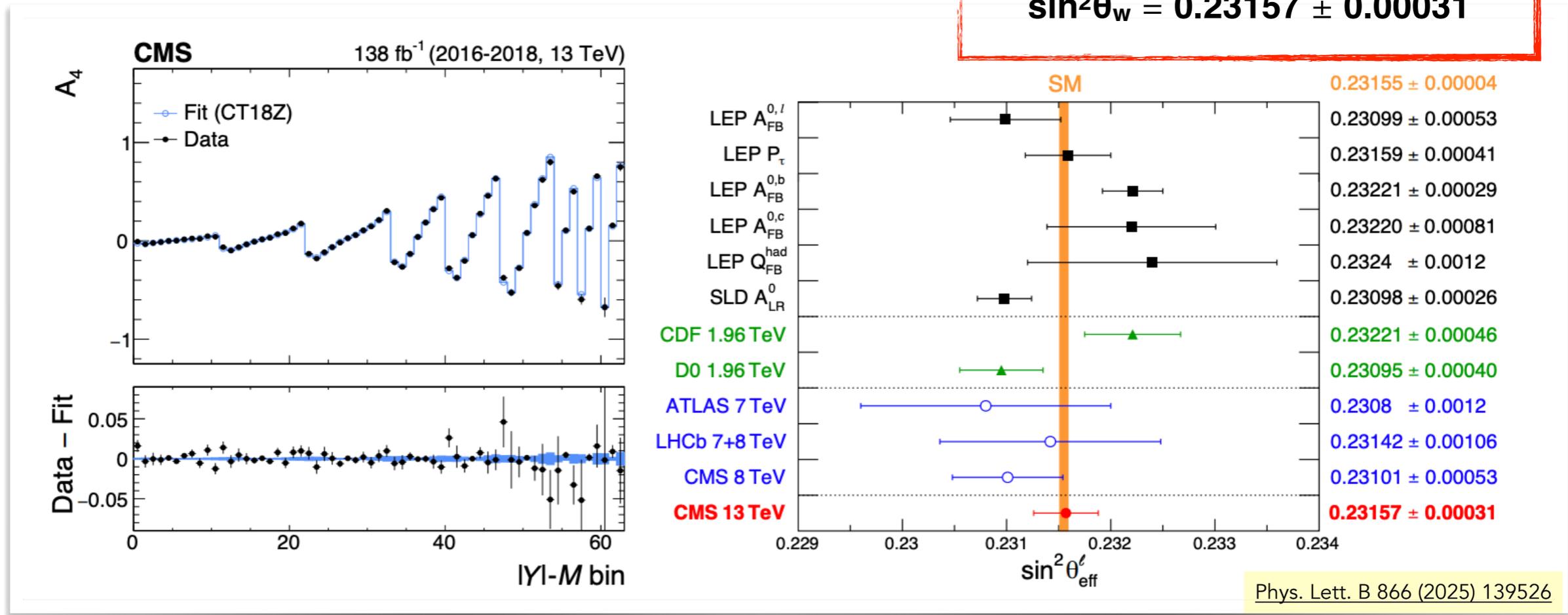
$$\sin^2\theta_{eff}^\ell = 0.23147 \pm 0.00044 \text{ (stat.)} \\ \pm 0.00005 \text{ (syst.)} \pm 0.00023 \text{ (theory)}$$

CMS

New analysis techniques, including **in-situ PDF profiling*** and categorisation statistical and systematic uncertainties are significantly reduced relative to previous CMS and ATLAS measurements.

Approaching precision of Tevatron combination

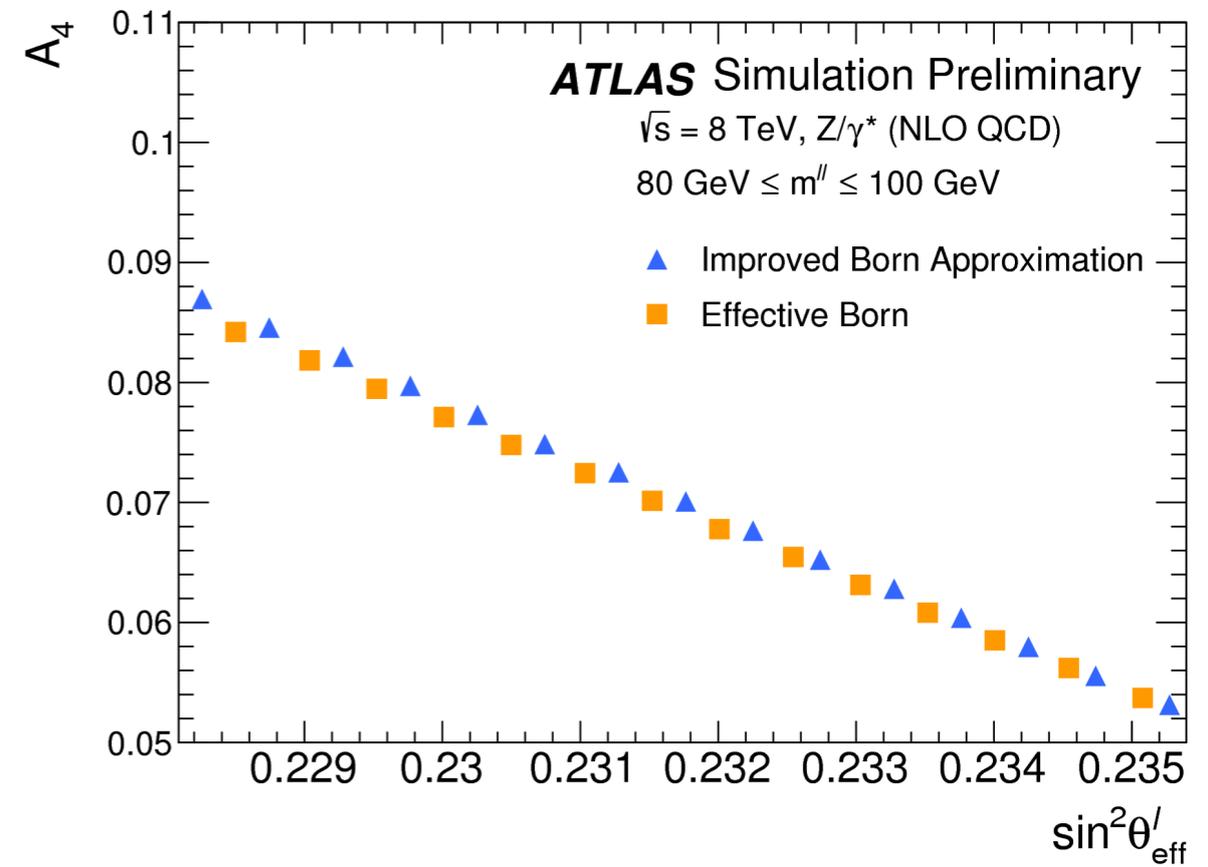
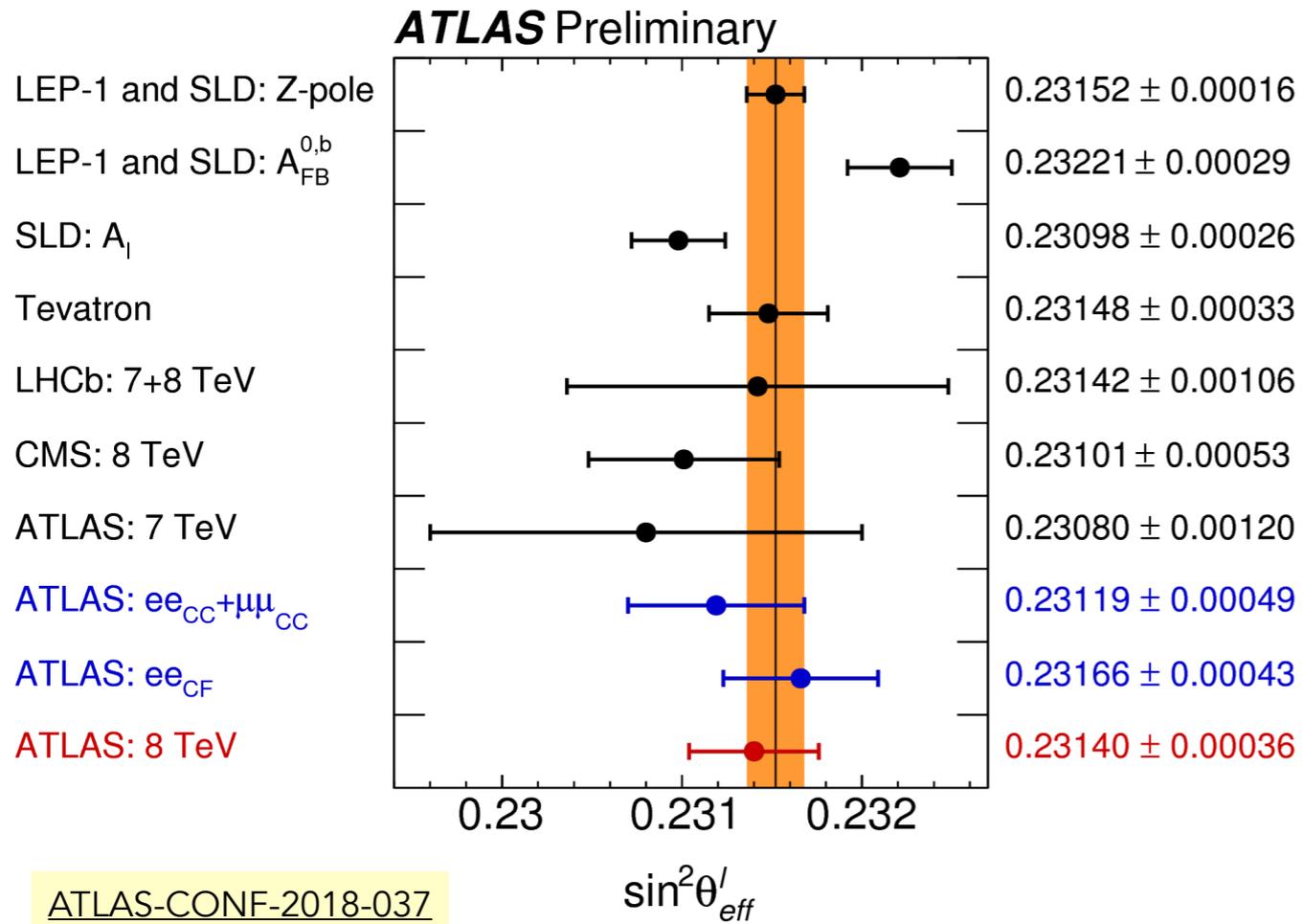
$$\sin^2\theta_w = 0.23157 \pm 0.00031$$



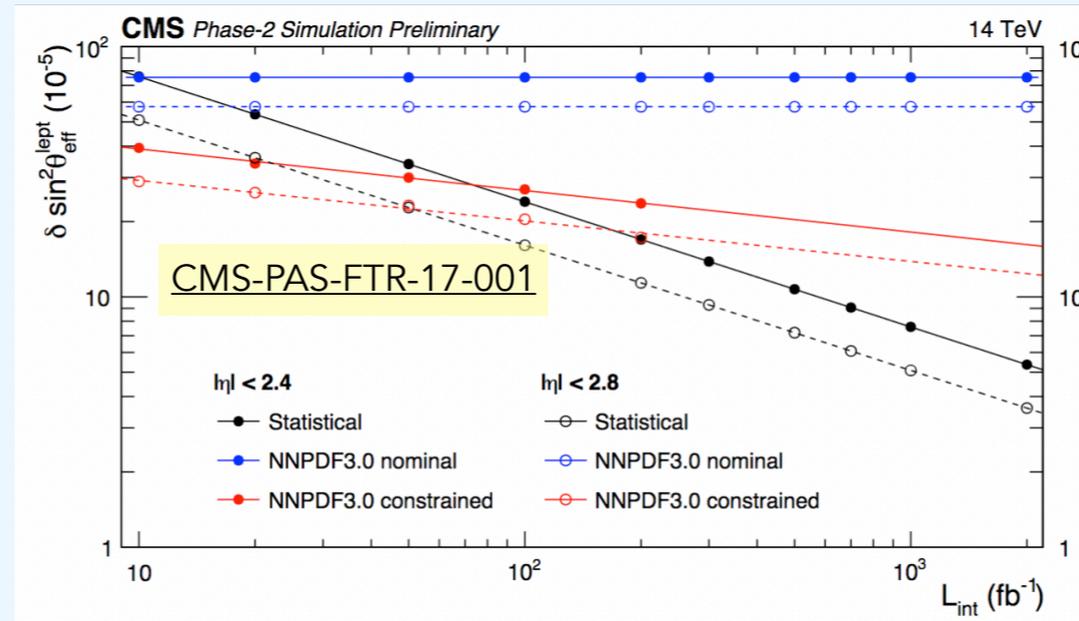
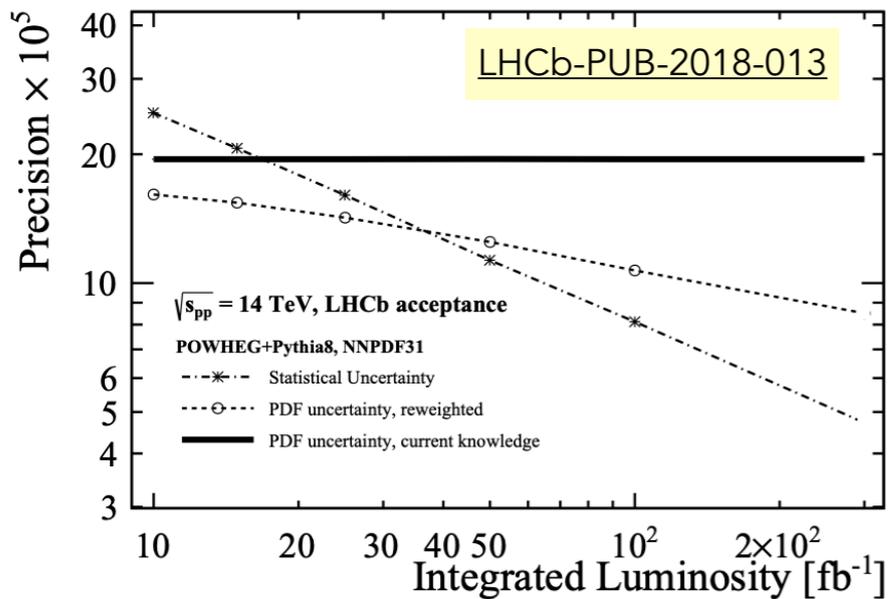
Phys. Lett. B 866 (2025) 139526

(*) PDF uncertainties are constrained in the interpretation exploiting their different dependence on m_{ll} , y_{ll}

ATLAS

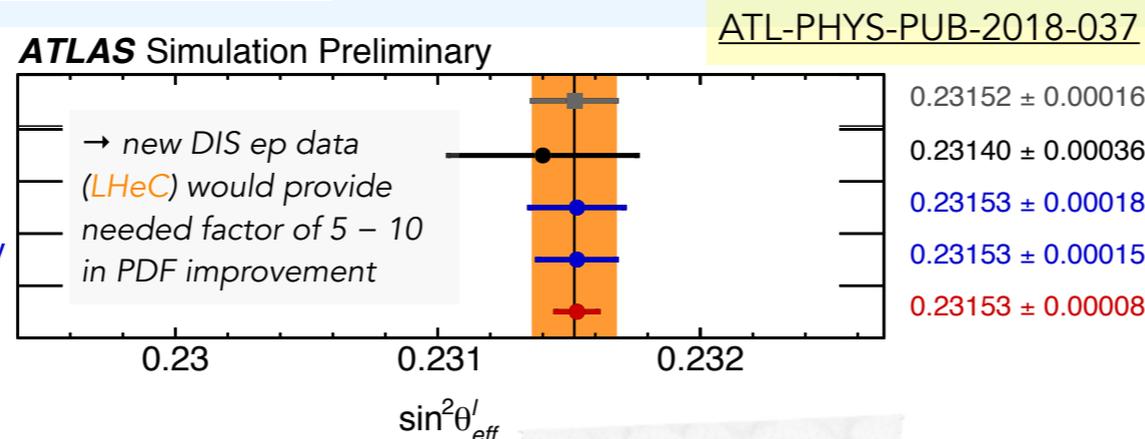


$\sin^2\theta_w$ prospects studies



- ▶ LHC experiments officially entered the **precision electroweak race**: current measurement limited by PDF uncertainty
- ▶ PDFs and their uncertainties can not any longer be treated as a black box, need similar or even bigger scrutiny, in terms of uncertainty decomposition and correlations, as exp. uncertainties.

LEP-1 and SLD: Z-pole average
ATLAS Preliminary: 8 TeV
HL-LHC ATLAS CT14: 14 TeV
HL-LHC ATLAS PDF4LHC15_{HL-LHC}: 14 TeV
HL-LHC ATLAS PDFLHeC: 14 TeV



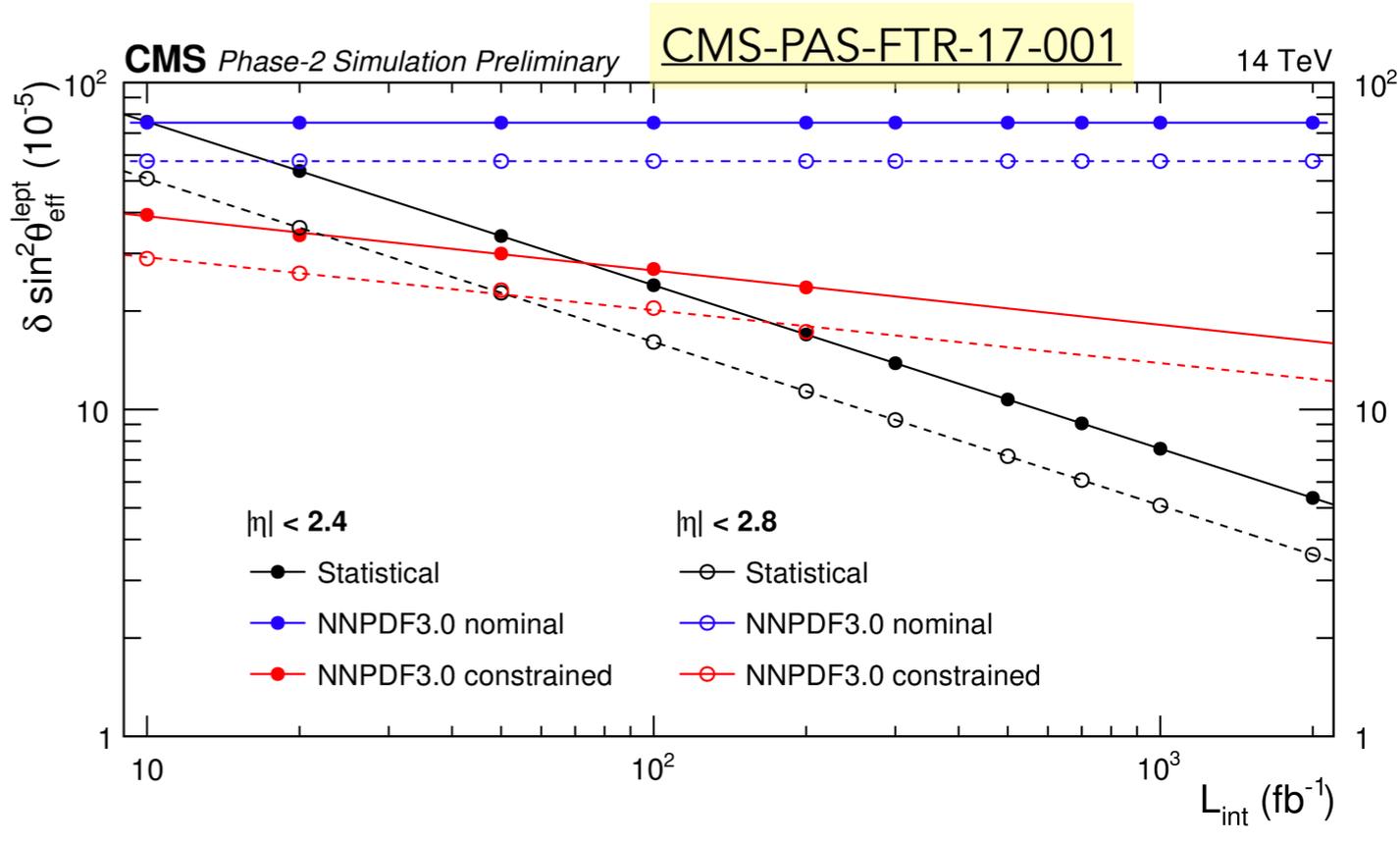
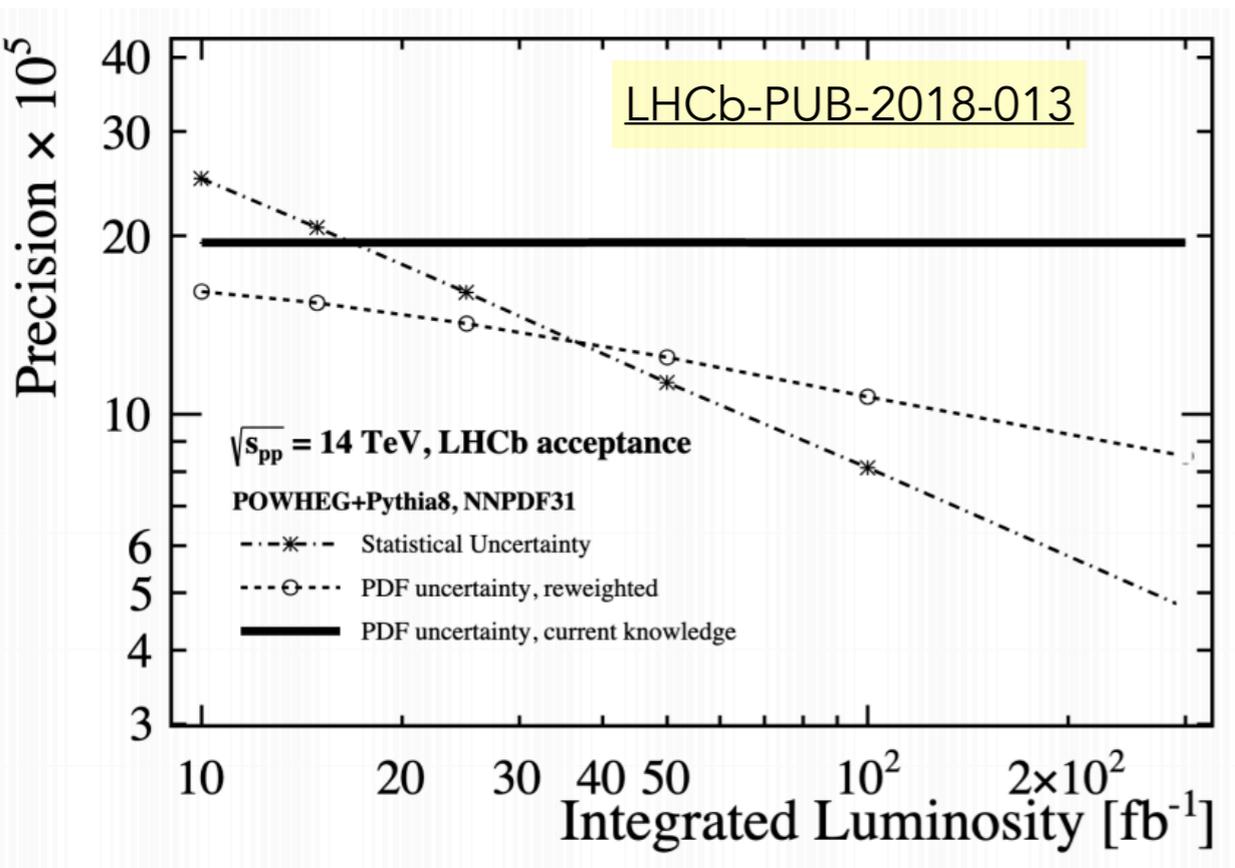
Towards LHC combination: Including **LHCb acceptance** (low dilution in forward region) offers a crucial handle by examining at precision a region where the PDF uncertainty is intrinsically small.

Work ongoing in **LHC-EW working group** and **PDF4LHC forum** to investigate:

- EW/QED NLO+h.o. accuracy corrections, benchmark NNLO and resummed calculations and uncertainties
- PDF differences and correlations

Weak mixing angle @HL-LHC

LHC experiments entered the precision electroweak race: New analysis techniques, including in-situ PDF profiling and event categorisation substantially reduced statistical and systematic uncertainties wrt previous LHC measurements.



Current and future measurement at pp collider limited by PDF uncertainty

$\sin^2\theta_w$ extraction with LHeC data

LEP-1 and SLD: Z-pole average

LEP-1 and SLD: $A_{FB}^{0,b}$

SLD: A_l

Tevatron

LHCb: 7+8 TeV

CMS: 8 TeV

ATLAS: 7 TeV

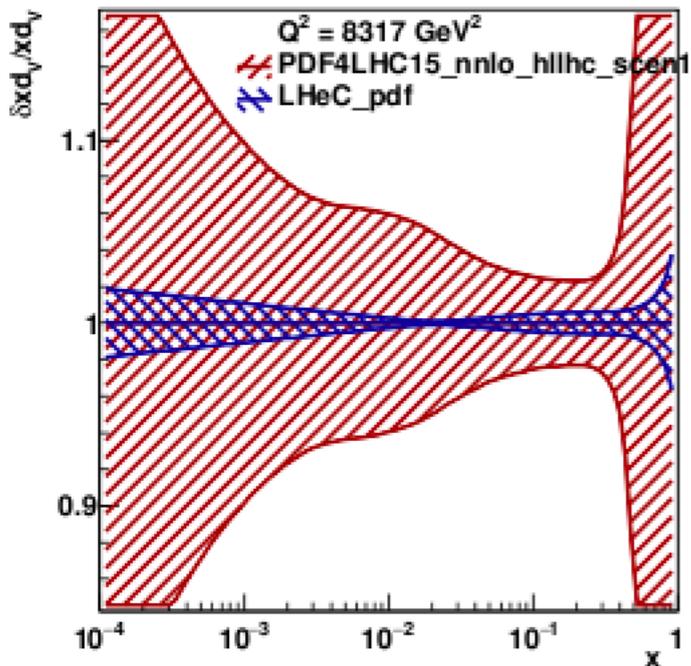
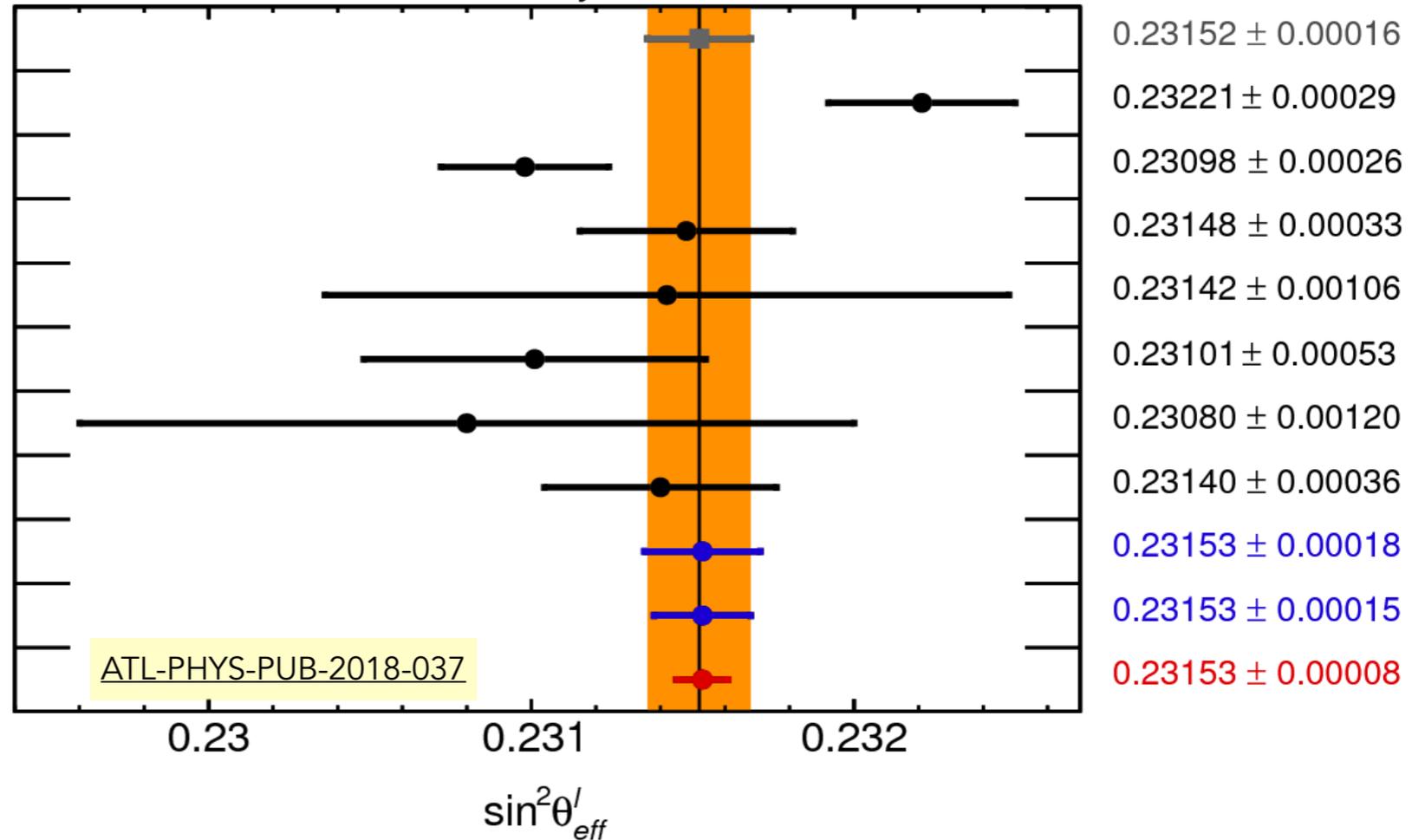
ATLAS Preliminary: 8 TeV

HL-LHC ATLAS CT14: 14 TeV

HL-LHC ATLAS PDF4LHC15_{HL-LHC}: 14 TeV

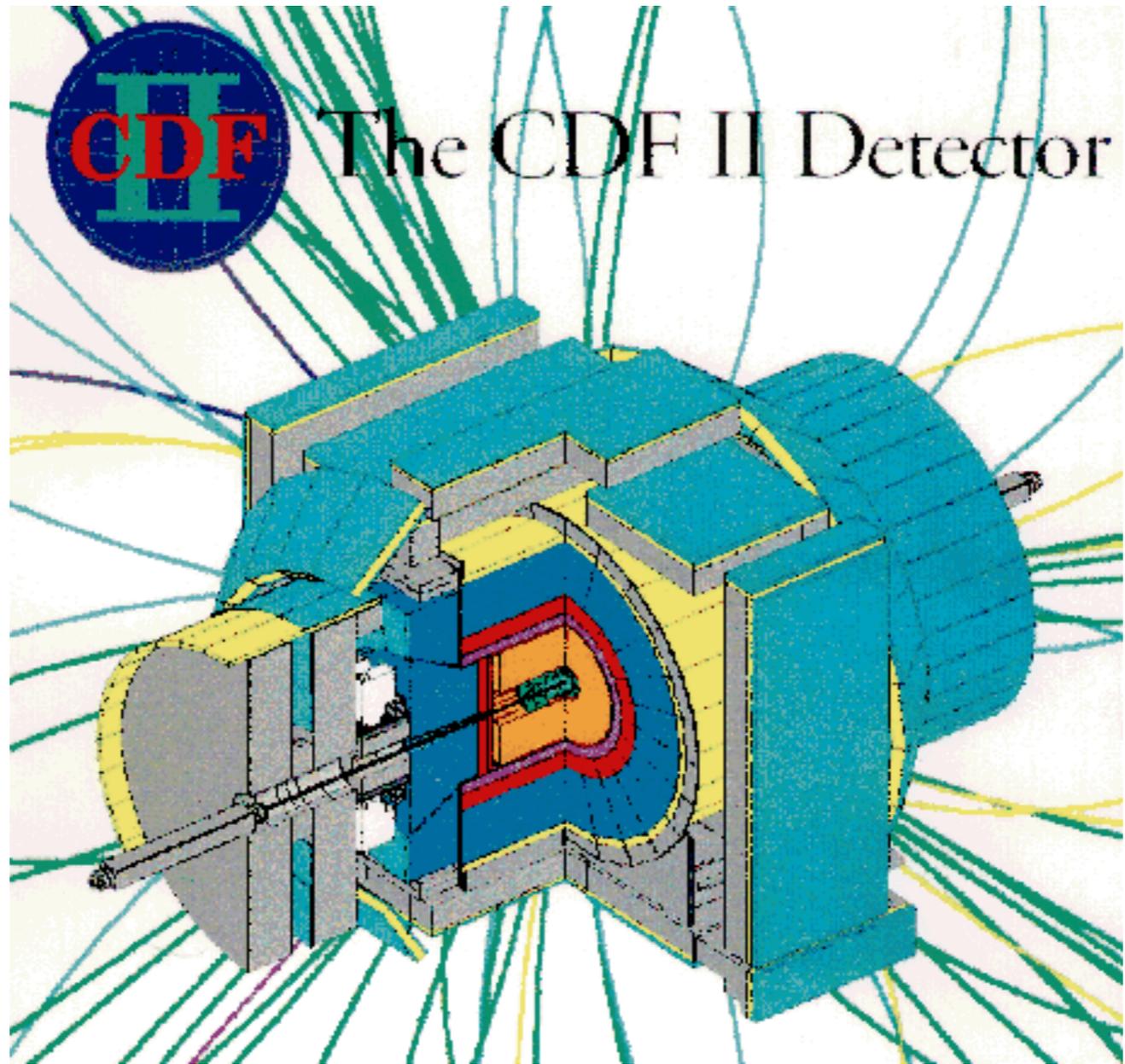
HL-LHC ATLAS PDFLHeC: 14 TeV

ATLAS Simulation Preliminary



The expected sensitivity of the $\sin^2\theta_{eff}$ measurements is improved by
~20% using HL-LHC data/PDF sets.

→ new DIS ep data (LHeC) would provide needed factor of 5 – 10
 in PDF improvement to **exceed LEP precision**

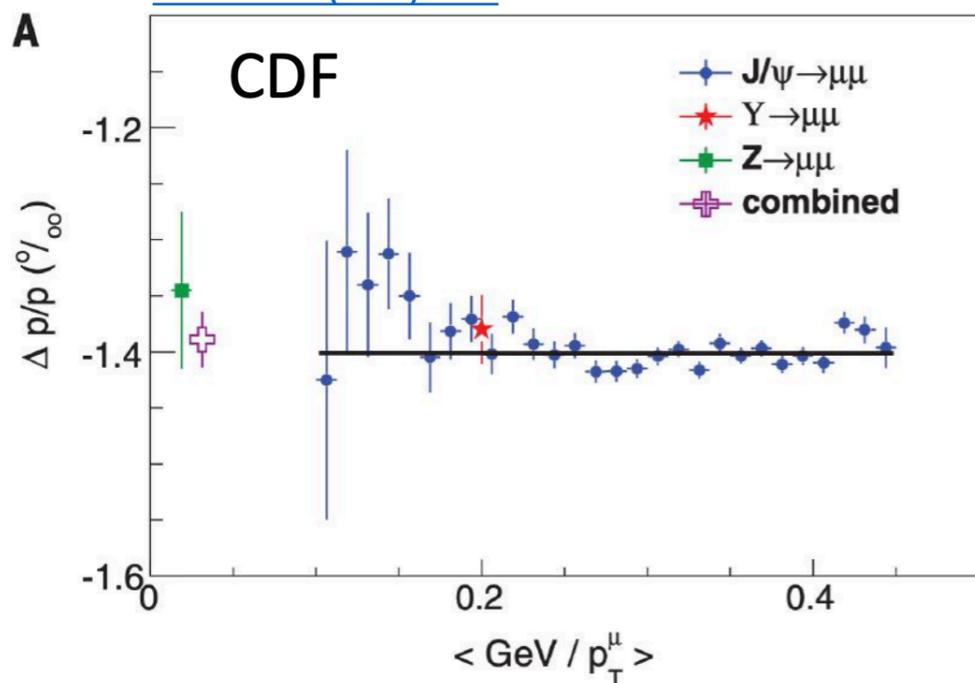


CDF II

Tevatron

CDF

Science 374 (2021) 6568



$$m_Z = 91192.3 \pm 7.1 \text{ MeV}$$

| Source | Uncertainty (MeV) |
|--------------------------|-------------------|
| Lepton energy scale | 3.0 |
| Lepton energy resolution | 1.2 |
| Recoil energy scale | 1.2 |
| Recoil energy resolution | 1.8 |
| Lepton efficiency | 0.4 |
| Lepton removal | 1.2 |
| Backgrounds | 3.3 |
| p_T^Z model | 1.8 |
| p_T^W/p_T^Z model | 1.3 |
| Parton distributions | 3.9 |
| QED radiation | 2.7 |
| W boson statistics | 6.4 |
| Total | 9.4 |

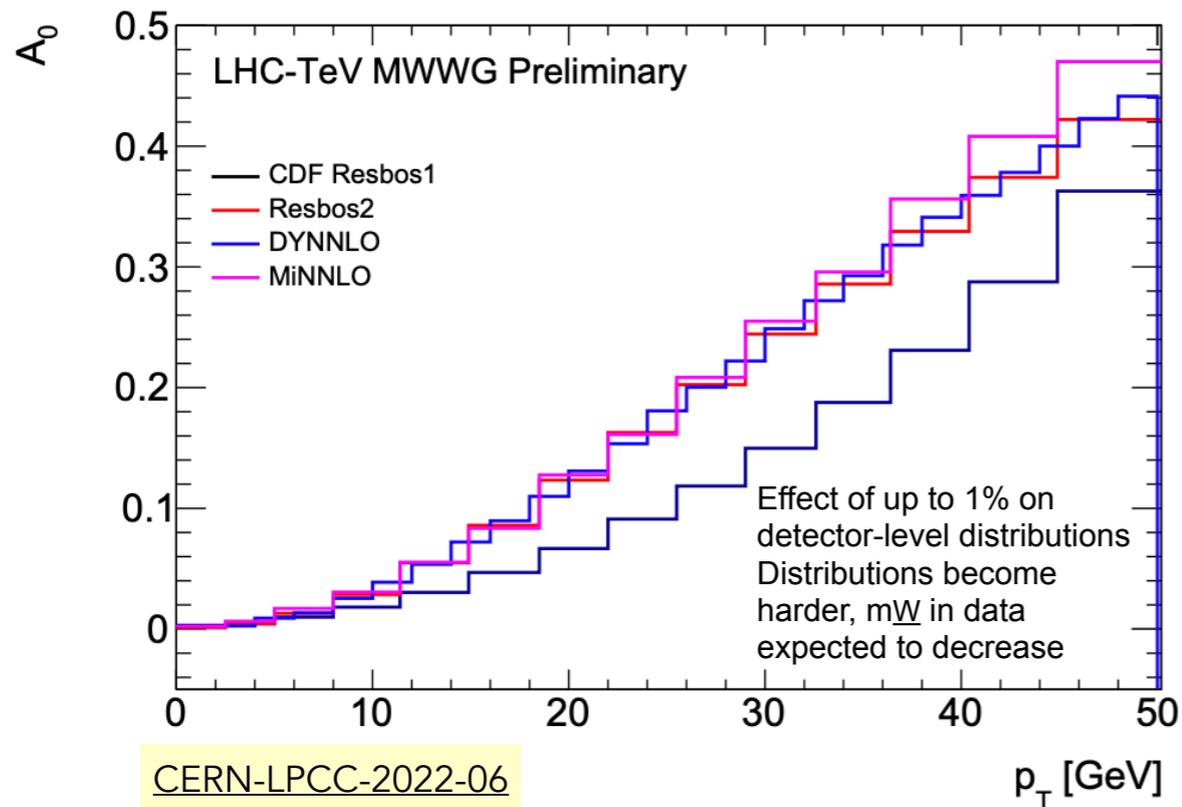
CDF has advantages from $p\bar{p}$, lower E, PU

- PDFs better understood (valence quarks)
- Less hadronic activity (simpler recoil calibration)
- Low tracking material aids lepton calibration

CDF

Several indications of potential bias in CDS measurement which require further studies

- Signal Modelling
- $Z \rightarrow \mu\mu$ Background Modelling (up to 8 MeV)



<https://arxiv.org/pdf/2507.07835>

