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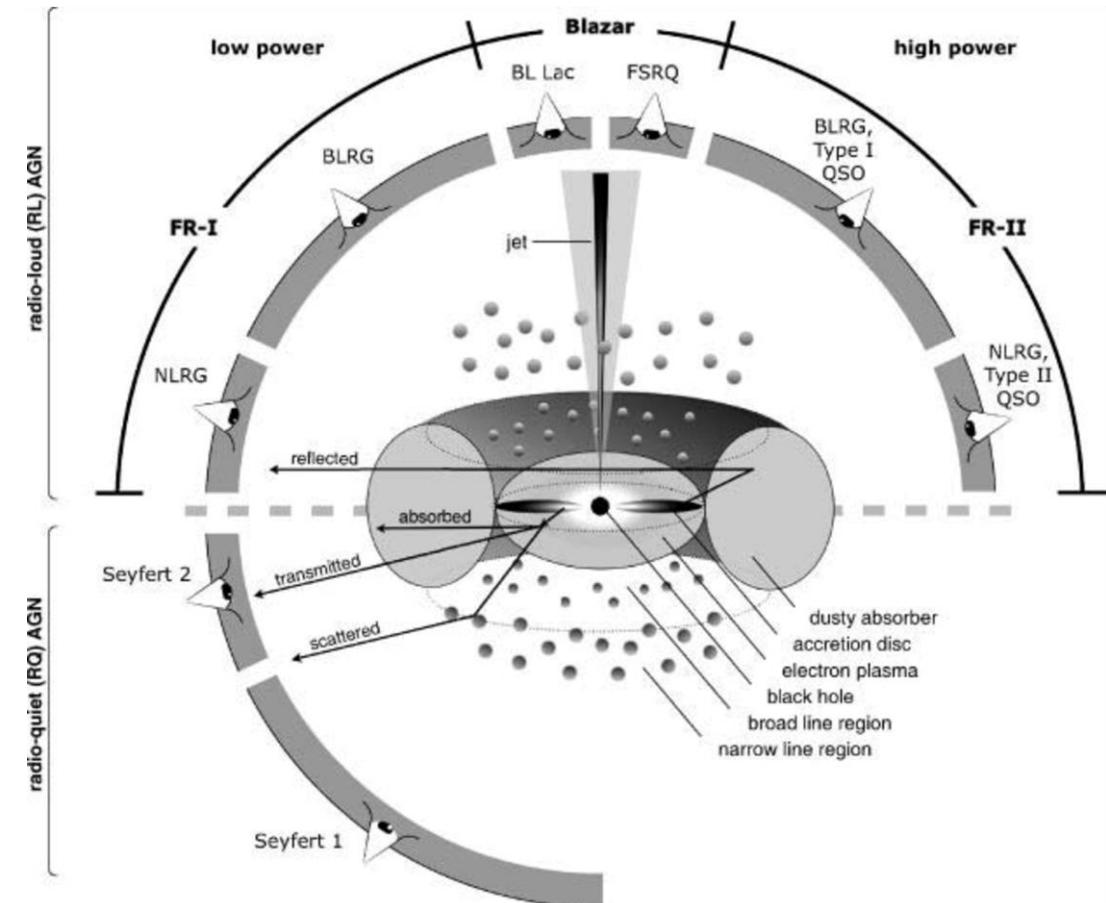
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# Active Galactic Nuclei

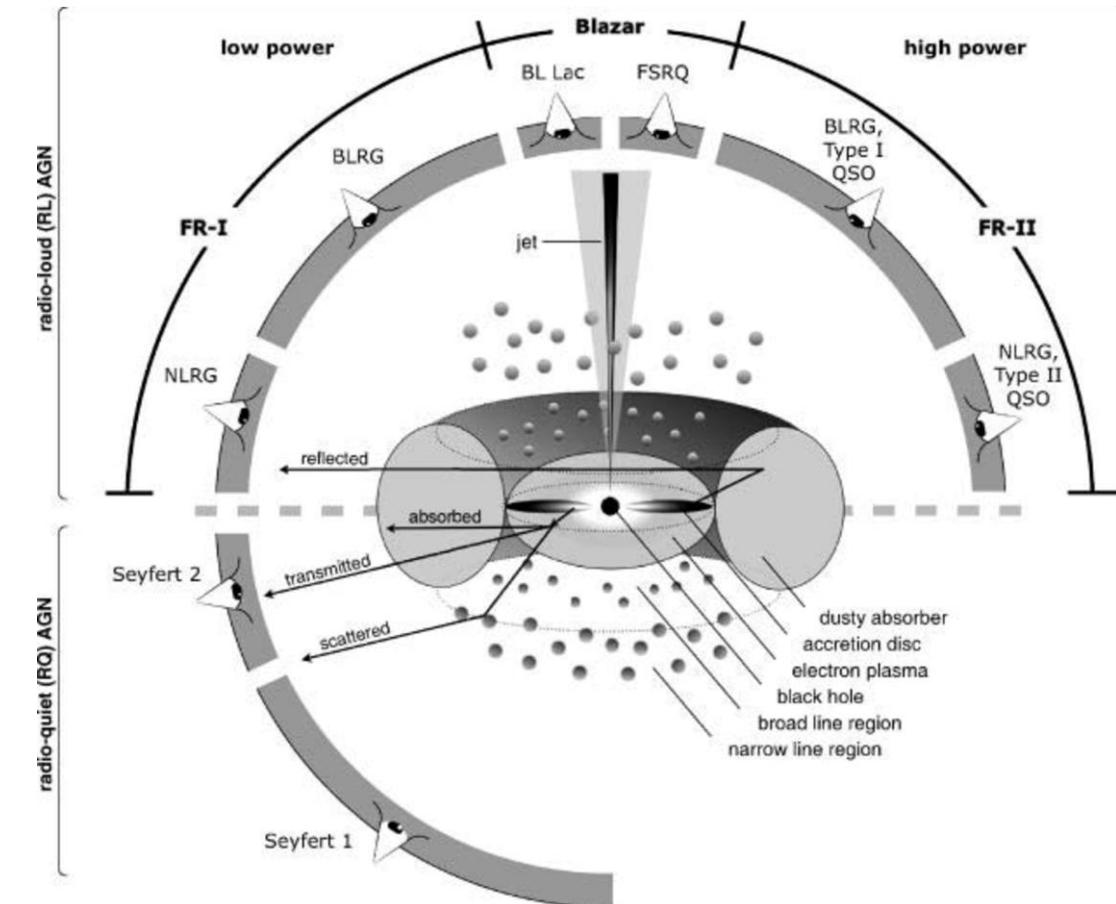
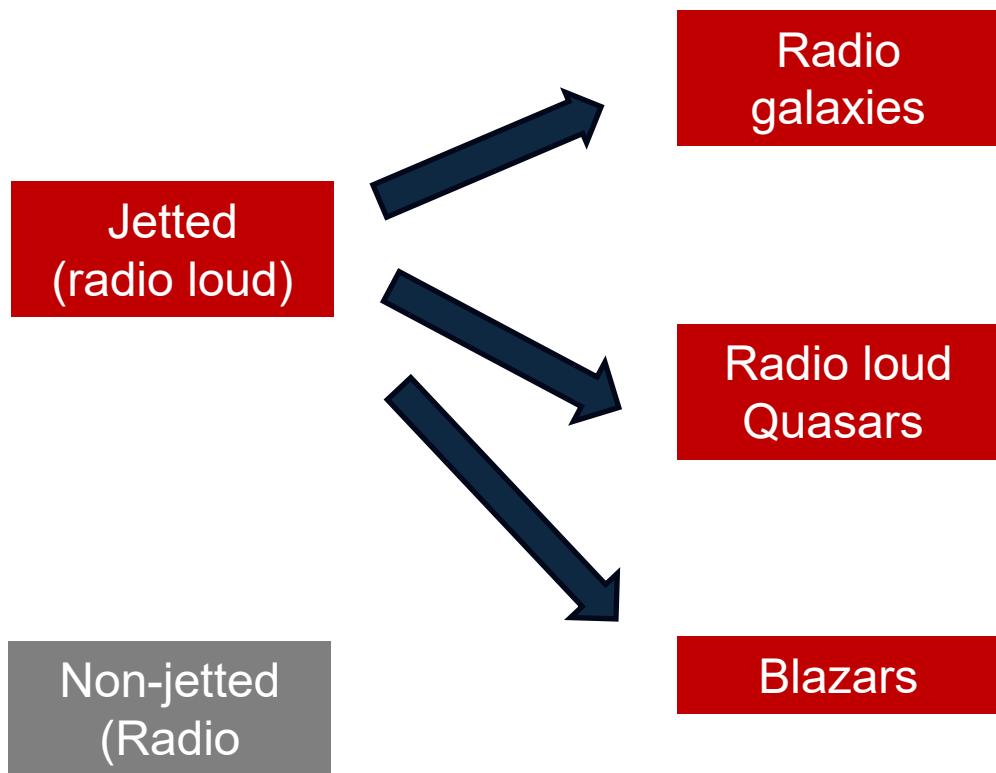
An active galactic nucleus (AGN) is the compact, highly luminous region at the center of a galaxy, powered by a supermassive black hole actively accreting gas and dust



Beckmann and Shrader, 2012, Figure 4.16

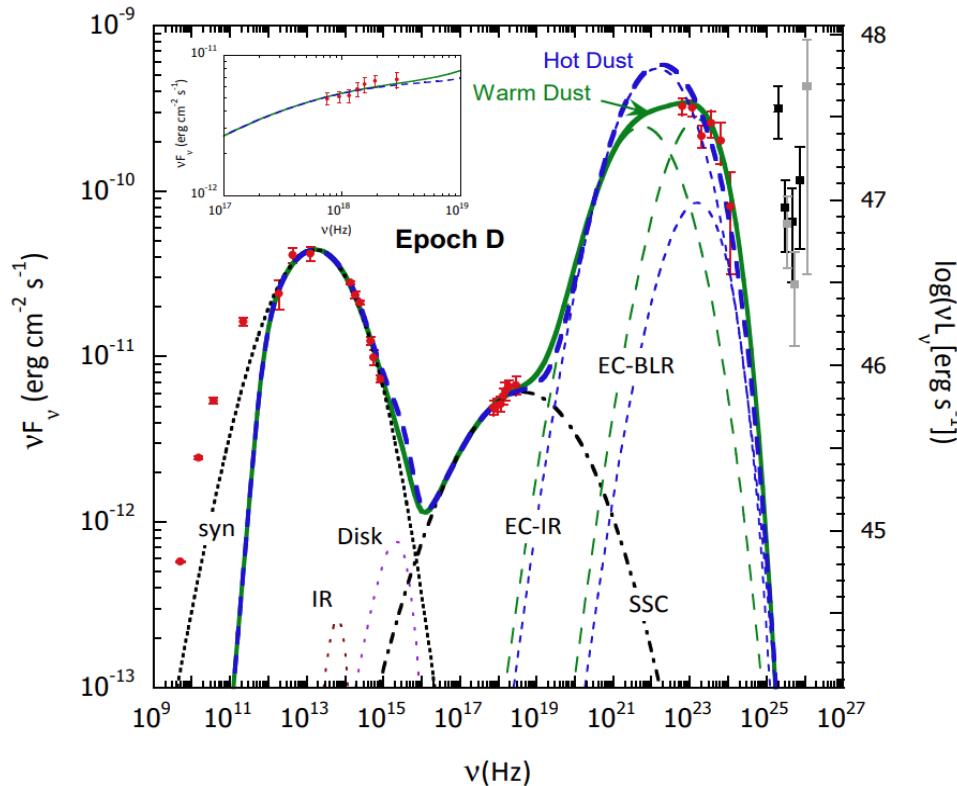


# Active Galactic Nuclei



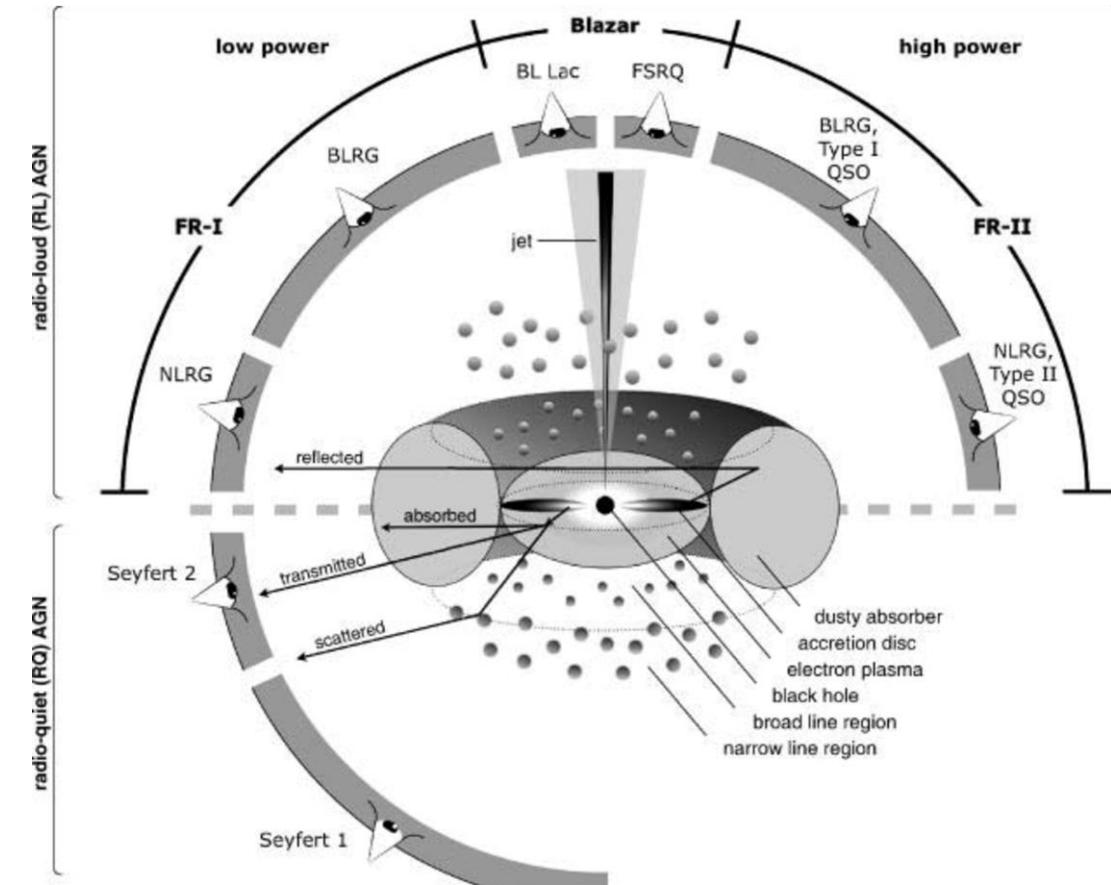
Beckmann and Shrader, 2012, Figure 4.16

# Active Galactic Nuclei



SED of 3C 279 with Leptonic emission models with contributions from different components in the AGN.

Dermer, et al. 2014, ApJ, 782, 82

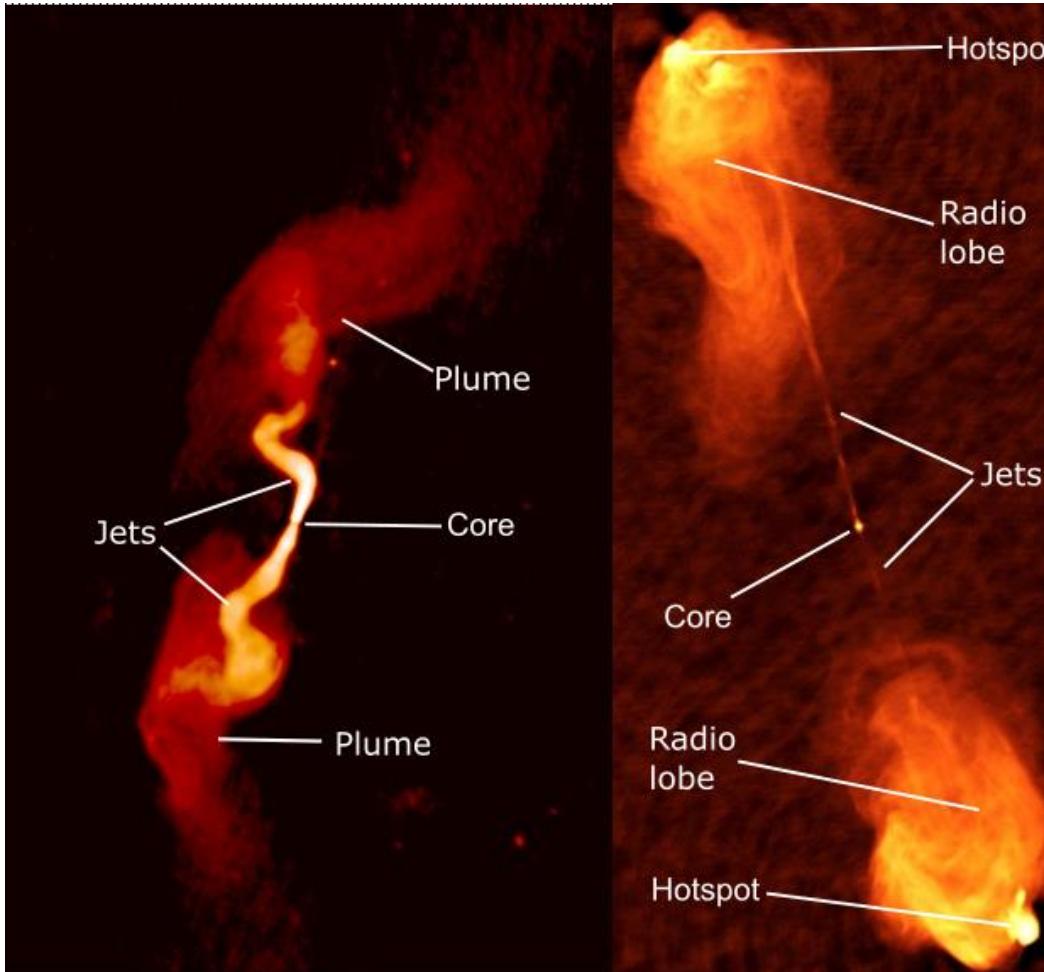


Beckmann and Shrader, 2012, Figure 4.16

# Large scale morphology

## FR I

- Typically two sided
- Brightness generally decreases with distance from the nucleus
- Lower luminosity



## FR II

- Jets can be single or double-sided
- Jet terminates in hotspots with bright lobe
- Higher luminosity

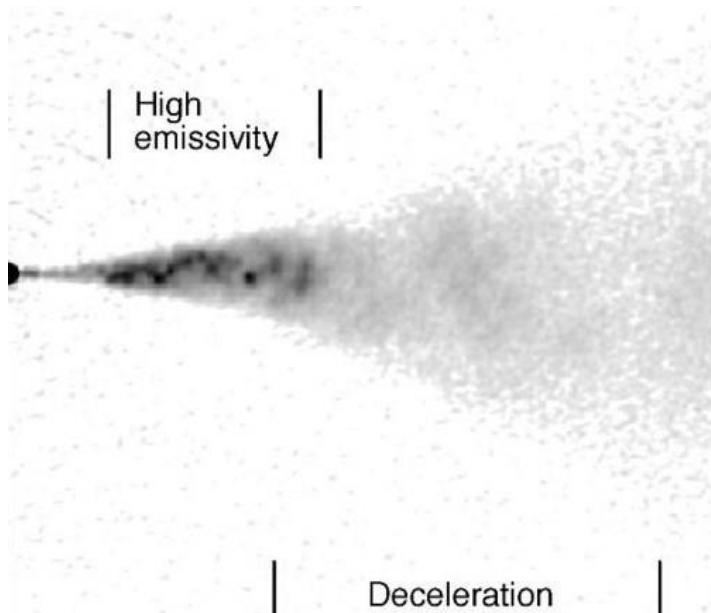
Left: 3C 31, NRAO, see Laing and Bridle(2002b).

Right: Cyg A, NRAO, see Carilli and Barthel (1996).

# Large scale morphology

## FR I

- Decelerate between parsec-kpc scales



Model for FR I deceleration, Laing and Bridle (2014)

## FR II

- Remains relativistic, terminates in a shock

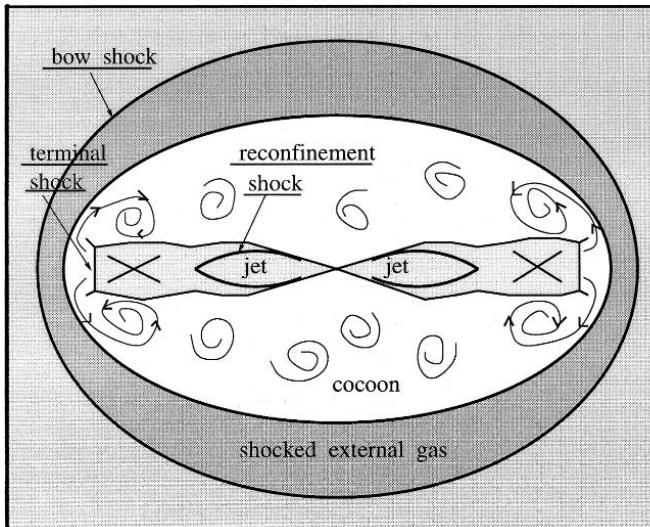


Diagram of the large scale structure of an FR II radio source, Komissarov and Falle (1998).

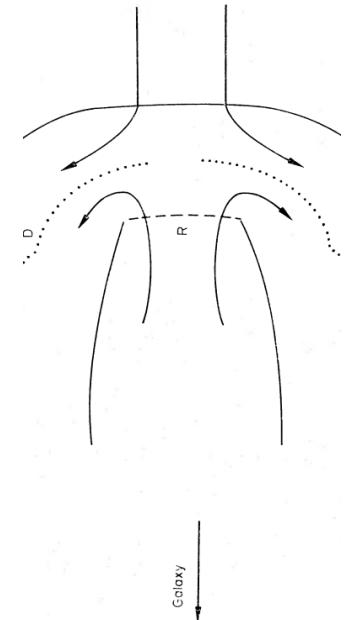
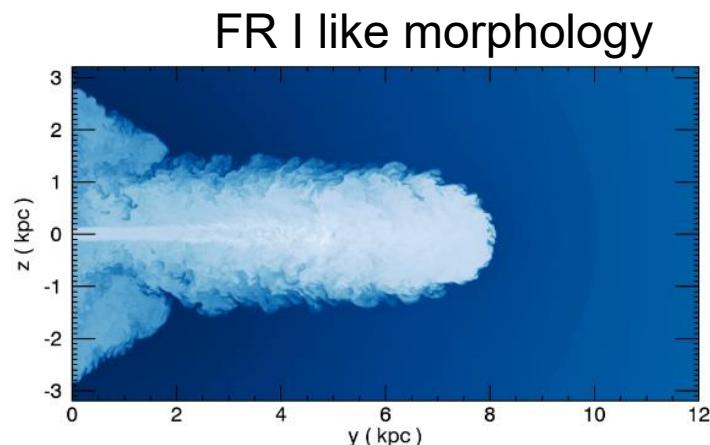
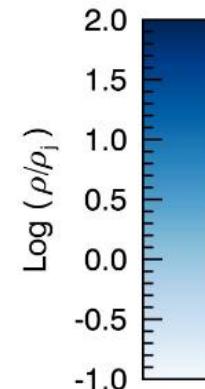
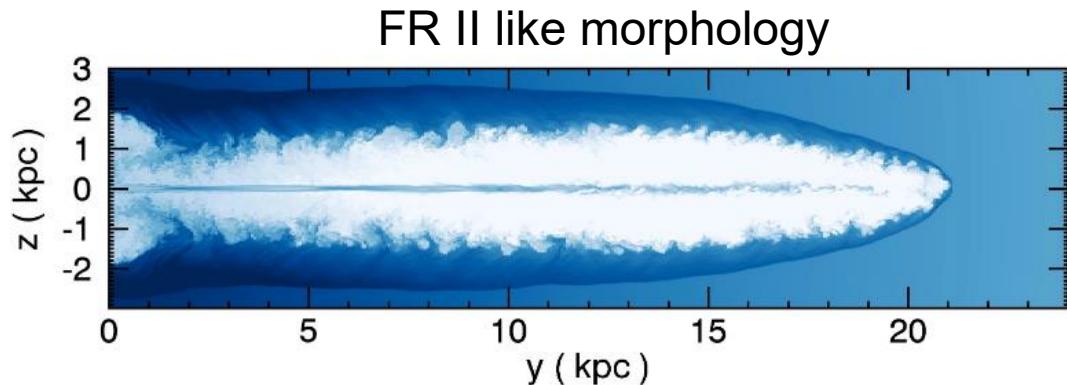


Diagram of flow at terminal shock, Blandford and Rees (1974)



# Simulating AGN jets



Massaglia, et.al. (2017)

The Morphology and kinematics of AGN jets can be simulated as a thermal fluid.

FR II like morphologies are “easy” to reproduce by injecting supersonic jet into a background region

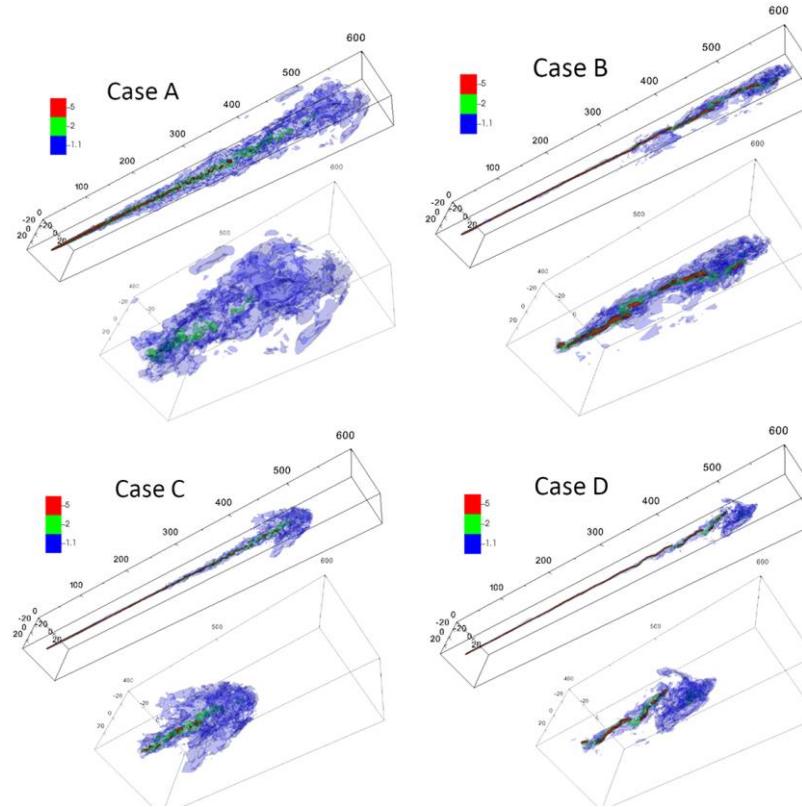
FR I like structures are more complicated to reproduce.

Massaglia, et.al. (2017) found kinetic luminosities of  $\approx 10^{42}$  erg.s<sup>-1</sup> produced FRI like structures on kiloparsec scales

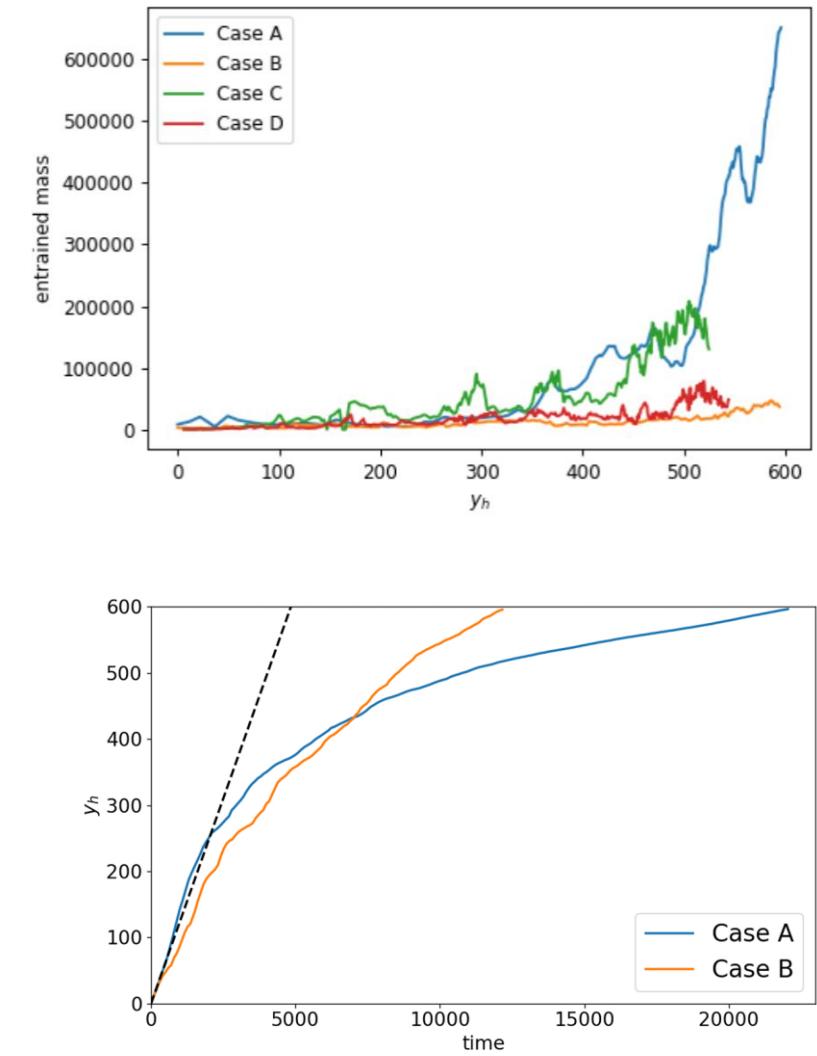
# Deceleration in Jets

Another way to produce FR I type morphologies is through deceleration

This can happen through entrainment of the ambient medium



Rossi et. al. (2024)



# PLUTO RMHD Simulations

PLUTO v4.4 <https://plutocode.ph.unito.it/>

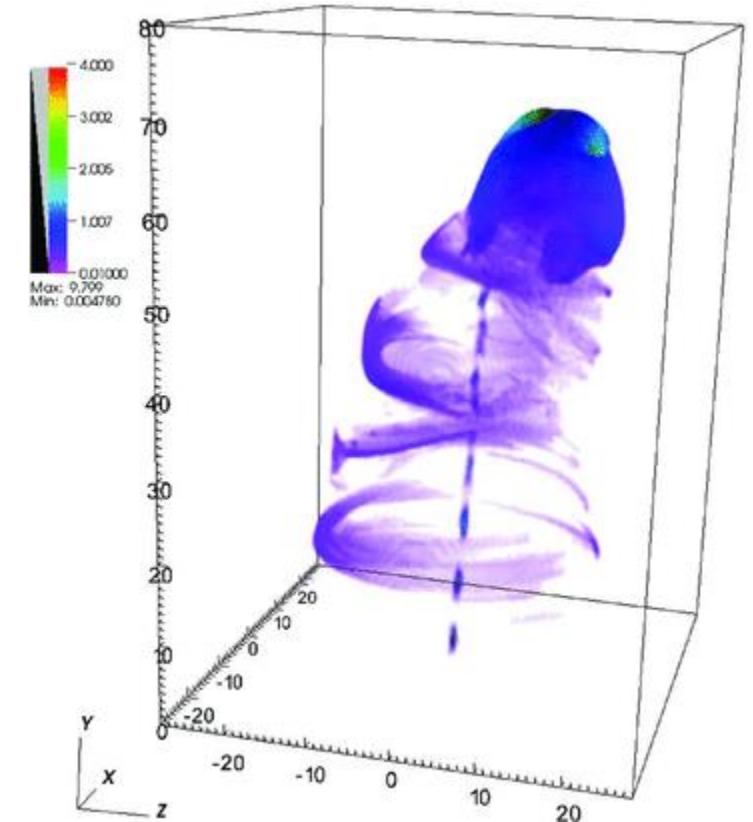
- Grid based hydrodynamics code
- Designed for high Mach number flows in astrophysical plasma dynamics
- Opensource

- Lagrangian particles module (Bhargav Vaidya, et. al. ApJ 865:144 (21pp), 2018)

- Separate particle entities suspended in fluid
- Represents an ensemble of particles with a finite energy distribution
- No back reaction on fluid
- Follow fluid streamlines
- Energy distribution is evolved with time

$$\frac{d\chi_p}{d\tau} + \frac{\partial}{\partial E} \left[ \left( -\frac{E}{3} \nabla_\mu u^\mu + \dot{E}_t \right) \chi_p \right] = 0,$$

- Adiabatic expansion
- Radiative losses
- Diffusive shock acceleration



Mignone et. Al., (2010)



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# Synchrotron Emission

Model the I, Q and U Stokes parameters of the Synchrotron emission

Emission coefficients:

$$j'_I(\nu', \hat{\mathbf{n}}'_{\text{los}}) = \frac{\sqrt{3}}{4\pi} \frac{q^3}{m_e c^2} |\mathbf{b} \times \hat{\mathbf{n}}'_{\text{los}}| \int n'_e(\gamma') F(x) d\gamma'.$$

$$j'_{\text{pol}}(\nu', \hat{\mathbf{n}}'_{\text{los}}) = \frac{\sqrt{3}}{2\pi} \frac{q^3}{m_e c^2} |\mathbf{b} \times \hat{\mathbf{n}}'_{\text{los}}| \int n'_e(\gamma') G(x) d\gamma'.$$

$$\boxed{j_Q = j_{\text{pol}} \cos 2\chi}$$
$$\boxed{j_U = j_{\text{pol}} \sin 2\chi,}$$

Absorption coefficients:

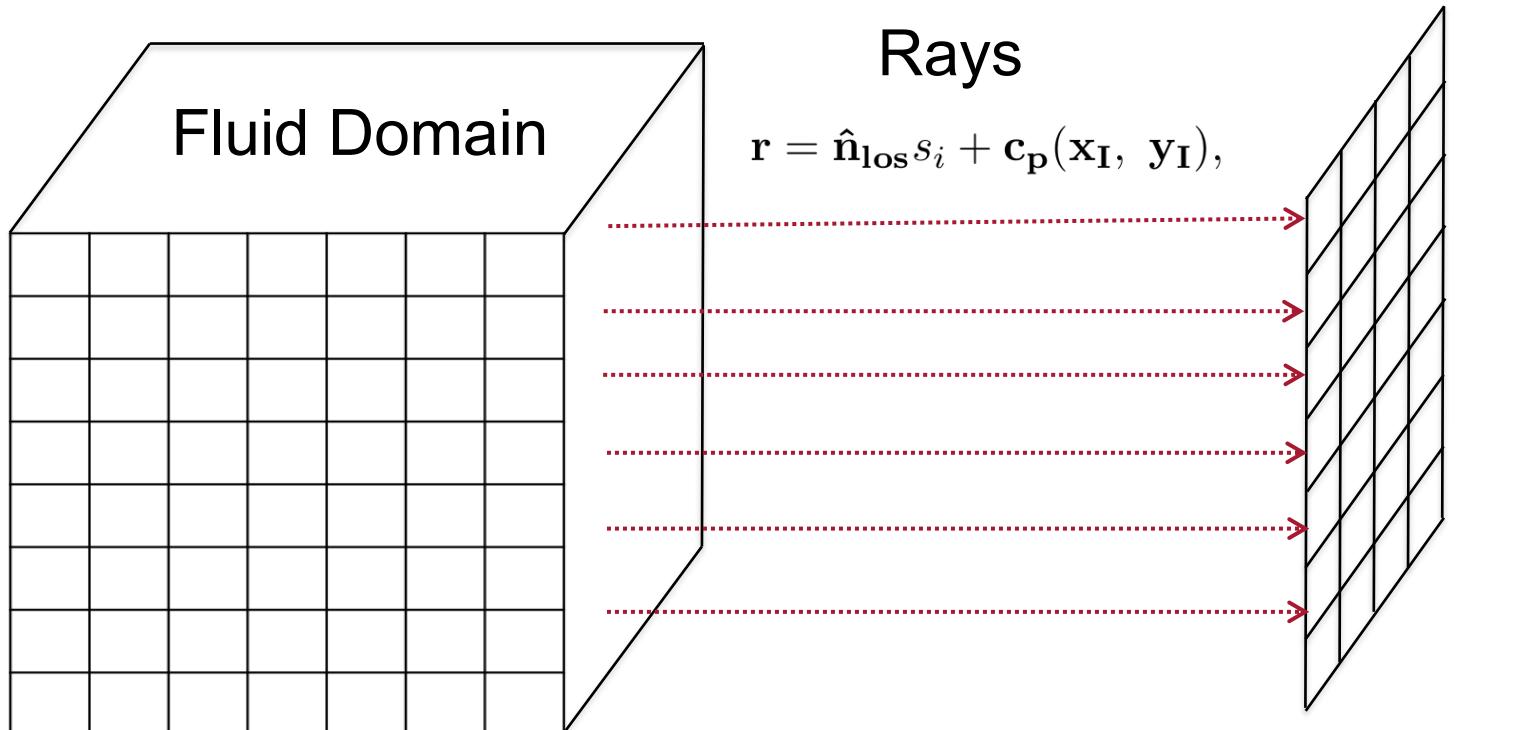
$$\alpha_I(\nu', \hat{\mathbf{n}}'_{\text{los}}) = -\frac{\sqrt{3}}{8\pi} \frac{q^3}{m_e^2 c^2 \nu^2} |\mathbf{b} \times \hat{\mathbf{n}}'_{\text{los}}| \int \gamma^2 \frac{\partial}{\partial \gamma} \left[ \frac{n'_e(\gamma')}{\gamma^2} \right] F(x) d\gamma' d\Omega'_\tau.$$

$$\alpha_{\text{pol}}(\nu', \hat{\mathbf{n}}'_{\text{los}}) = -\frac{\sqrt{3}}{8\pi} \frac{q^3}{m_e^2 c^2 \nu^2} |\mathbf{b} \times \hat{\mathbf{n}}'_{\text{los}}| \int G(x), \gamma^2 \frac{\partial}{\partial \gamma} \left[ \frac{n'_e(\gamma')}{\gamma^2} \right] d\gamma' d\Omega'_\tau.$$

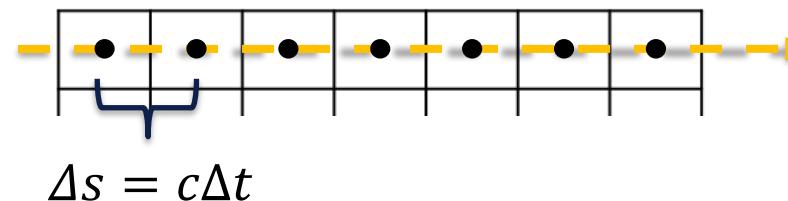
$$\boxed{\alpha_Q = \alpha_{\text{pol}} \cos 2\chi}$$
$$\boxed{\alpha_U = \alpha_{\text{pol}} \sin 2\chi,}$$

Lorentz transformations:  $j_I(\nu, \hat{\mathbf{n}}_{\text{los}}) = \delta_D^2 j'_I(\nu', \hat{\mathbf{n}}'_{\text{los}}),$   $\alpha_I(\nu, \hat{\mathbf{n}}_{\text{los}}) = \delta_D^{-1} \alpha'_I(\nu', \hat{\mathbf{n}}'_{\text{los}}).$

# Emission: Radiative transfer



Accounting for light travel time



$$\mathbf{r} = \hat{\mathbf{n}}_{\text{los}} c t_i + \mathbf{c}_p(\mathbf{x}_I, \mathbf{y}_I).$$

Image

$$\hat{\mathbf{n}}_{\text{los}} = (\sin \theta \cos \phi \hat{\mathbf{x}}, \sin \theta \sin \phi \hat{\mathbf{y}}, \cos \theta \hat{\mathbf{z}}).$$

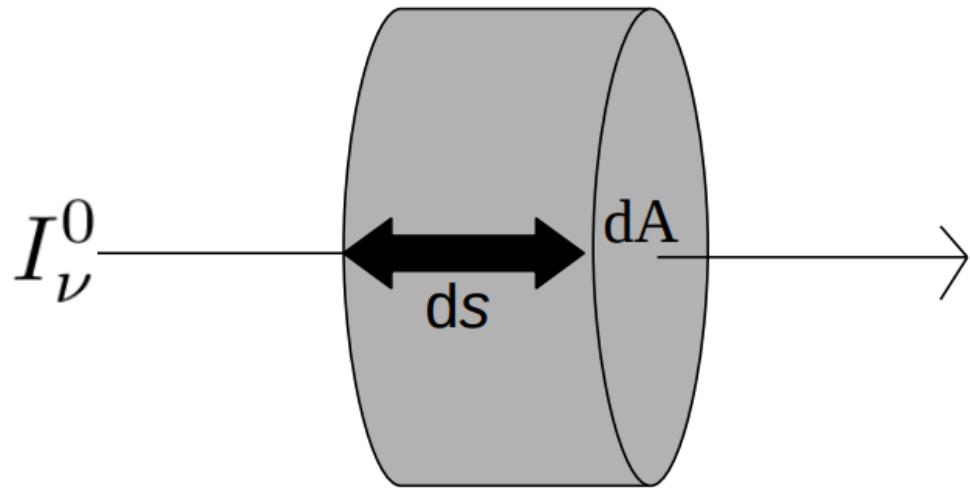
$$\hat{\mathbf{x}}_I = (-\sin \phi \hat{\mathbf{x}}, \cos \phi \hat{\mathbf{y}}, 0 \hat{\mathbf{z}})$$

$$\hat{\mathbf{y}}_I = (-\cos \phi \cos \theta \hat{\mathbf{x}}, -\sin \phi \cos \theta \hat{\mathbf{y}}, \sin \theta \hat{\mathbf{z}}).$$



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# Emission: Radiative transfer



Integration of radiative transfer equation along the path of the ray

$$\int \frac{dI(\mathbf{x}_I, \mathbf{y}_I)}{ds} ds \approx \sum_{i=0}^{i=N} \frac{dI(\mathbf{x}_I, \mathbf{y}_I)}{ds} \Delta s,$$

The integration is split for optically thick and thin regimes

$$I_{S[i]} = \begin{cases} I_{S[i-1]} + [J_{S[i]} - M_{ST[i]} I_{S[i-1]}] c \Delta t, & \Delta \tau_I < 1, \\ S_{S[i]} (1 - e^{-\Delta \tau_I}) + \Lambda_{\alpha[i]} I_{S[i-1]} e^{-\Delta \tau_I}, & \Delta \tau_I > 1. \end{cases}$$

$$\frac{d}{ds} \begin{bmatrix} I \\ Q \\ U \end{bmatrix} = \begin{bmatrix} j_I \\ j_Q \\ j_U \end{bmatrix} - \begin{bmatrix} \alpha_I & \alpha_Q & \alpha_U \\ \alpha_Q & \alpha_I & 0 \\ \alpha_U & 0 & \alpha_I \end{bmatrix} \begin{bmatrix} I \\ Q \\ U \end{bmatrix}.$$

Where,

$$S_i = \frac{J_i}{\alpha_i},$$

$$\tau = \alpha \Delta s$$

# RMHD Simulations

Three scenarios, with different velocities

- Relativistic jet:  $\Gamma = 10$
- Mildly relativistic jet:  $\Gamma = 1.2$
- Non-relativistic jet:  $\Gamma = 1.014$

Simulation	Relativistic	Mildly relativistic	Non-relativistic
Resolution [pc]	25	25	25
Lorentz factor ( $\Gamma$ )	10	1.2	1.014
Mach number (M)	30	17	5
Density ratio ( $\eta$ )	$10^{-4}$	$10^{-4}$	$10^{-3}$
Propagation velocity ( $V_{WS}$ )	0.904	0.301	0.0833
Kinetic luminosity ( $E_{kin}$ ) [erg.s <sup>-1</sup> ]	$10^{47}$	$10^{44}$	$10^{43}$
Magnetic field ( $B_0, B_1, B_c$ ) [ $\times 3.8 \times 10^{-5} G$ ]	1, 1, 0.001	1, 1, 0.001	1, 1, 0.001
Plasma parameter ( $\beta_m$ )	7.7	7.7	0.77
Magnetization parameter ( $\sigma$ )	$10^{-2}$	$10^{-2}$	$10^{-3}$
Number of Lagrangian particles	325 550	375 160	299 137

# Simulations setup

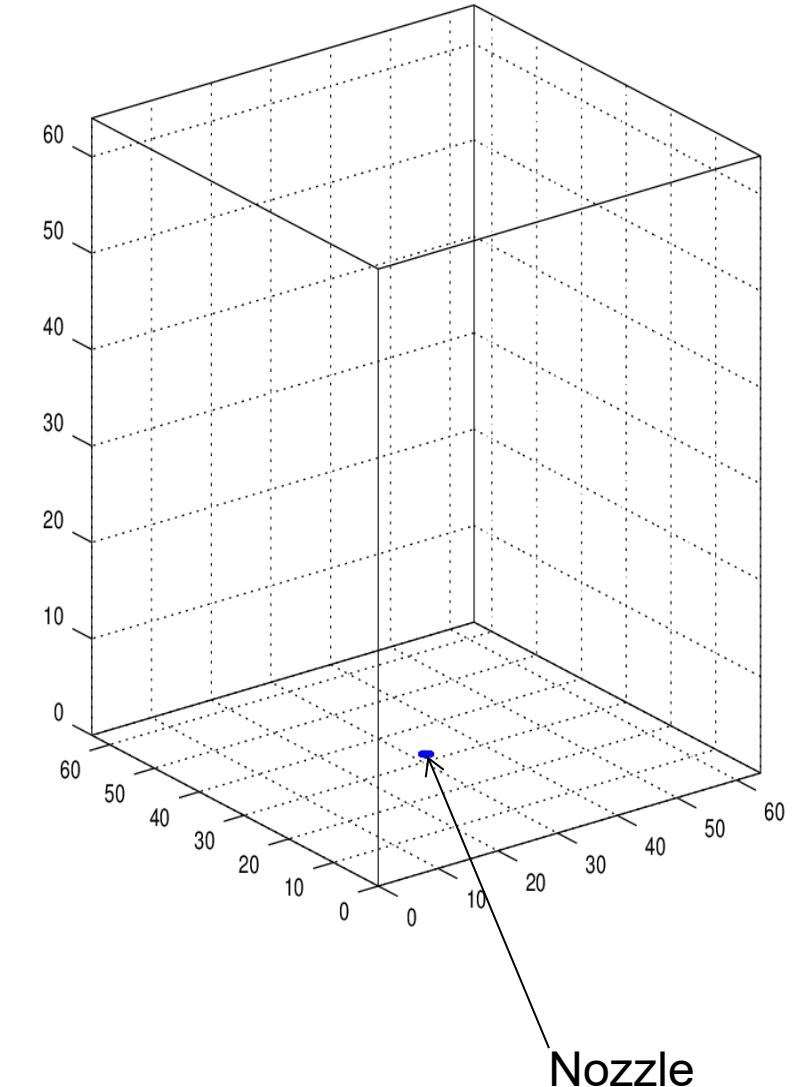
## Domain

- Cartesian computational grid
- Size: 64x64x128 jet radii
- Jet radius ( $r_j = 1$  unit  $\sim 100$  pc)

## Stationary ambient medium

- Stratified density  $\rho(r) = \frac{\rho_a}{1 + \left(\frac{r}{40}\right)^2}$

Jet material is injected through a profiled nozzle on the bottom z-boundary



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Jet material is injected through a profiled nozzle on the bottom z-boundary

$$\begin{aligned} B_r &= 2B_0 \frac{r_j \left(\frac{z}{z_j}\right)^3 \tanh\left(\frac{z}{z_j}\right)^4 \tanh\left(\frac{r}{r_j}\right)^2}{z_j \frac{r}{r_j} \cosh\left(\frac{z}{z_j}\right)^4} \\ B_z &= B_c + \frac{B_0}{\cosh^2\left(\frac{r}{r_j}\right)^2 \cosh\left(\frac{z}{z_j}\right)} \\ B_\phi &= \begin{cases} B_1 \tanh\left(\frac{r}{5}\right) & \text{for } r \leq r_j, \\ 0 & \text{for } r > r_j \end{cases} \end{aligned}$$

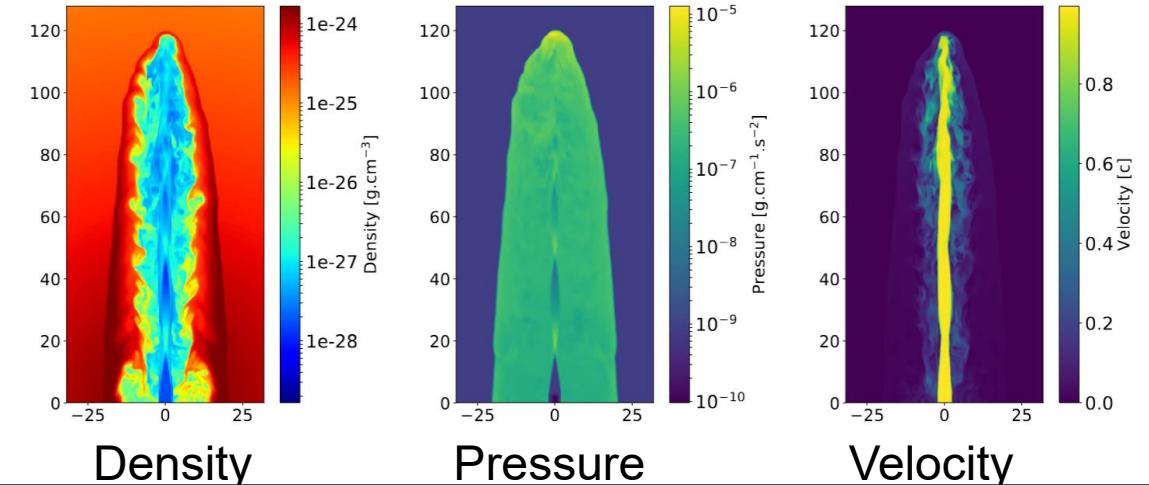
$$\begin{aligned} v_\phi &= \frac{B_\phi}{\sqrt{\rho_j}}, \quad \text{and,} \\ v_z &= \sqrt{1 - \frac{1}{\Gamma_z^2}}, \end{aligned}$$



# RMHD simulations

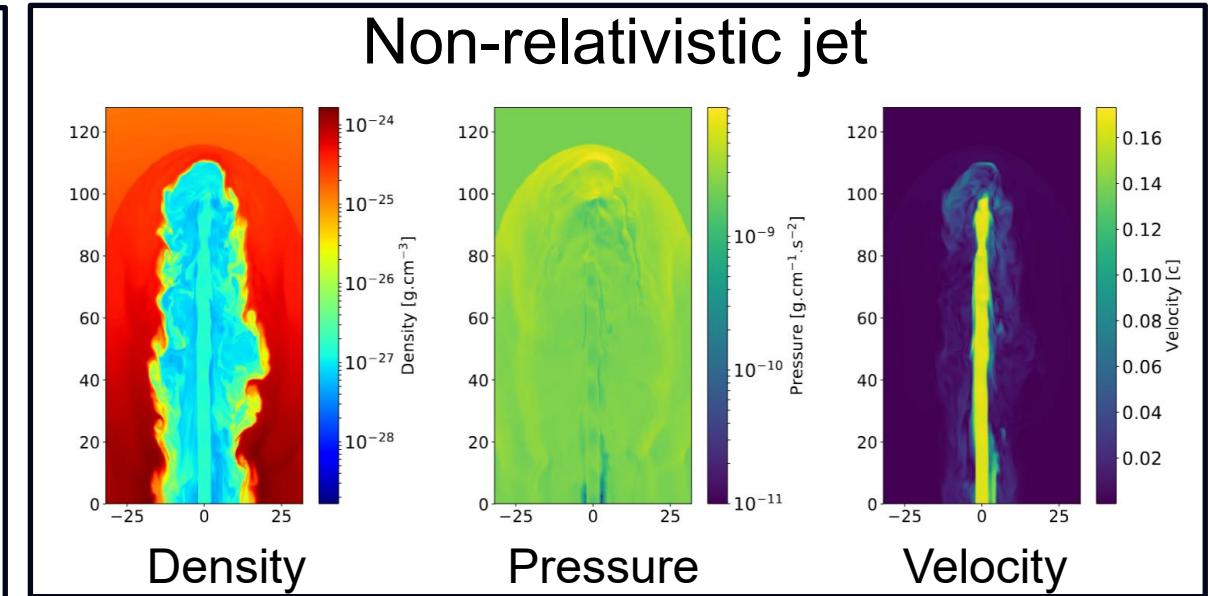
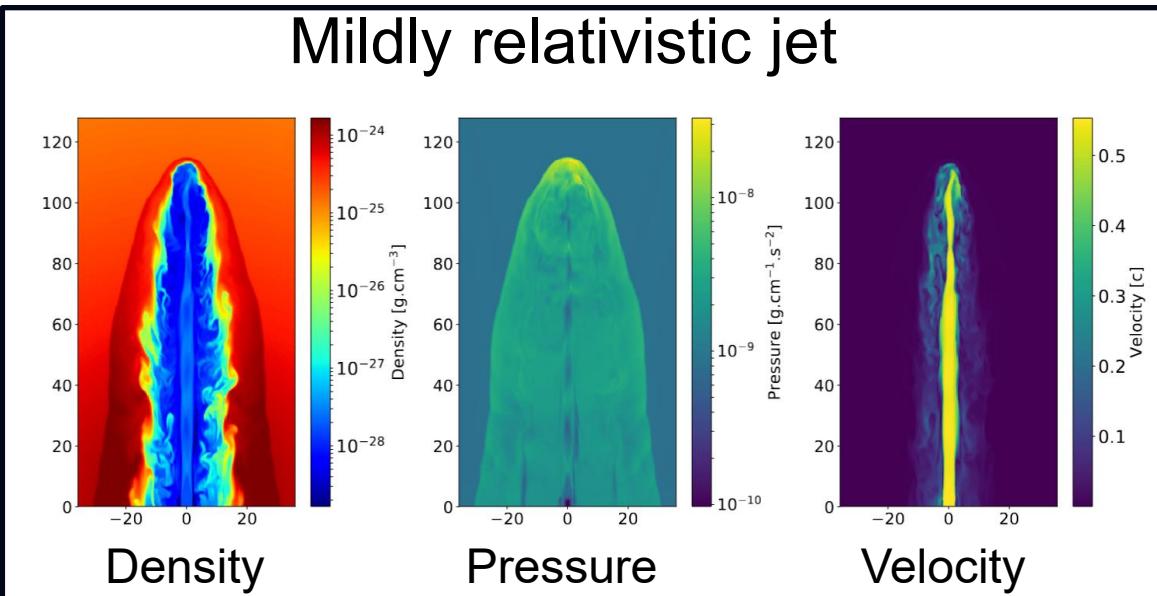
2D slices of the simulations through  
the xz-plane

Relativistic jet

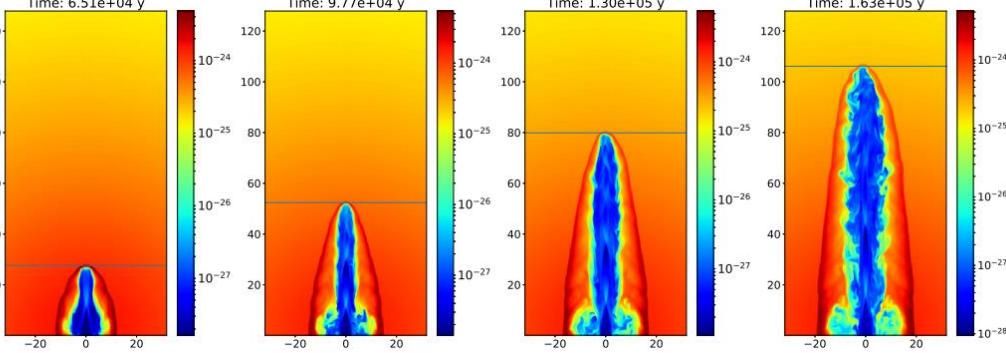


Mildly relativistic jet

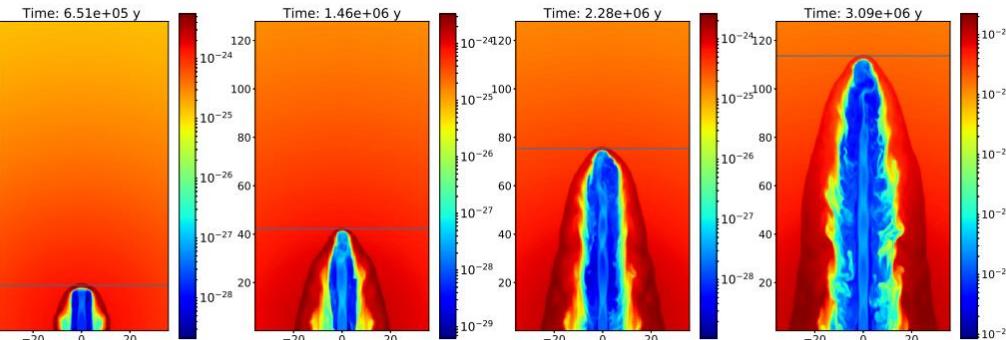
Non-relativistic jet



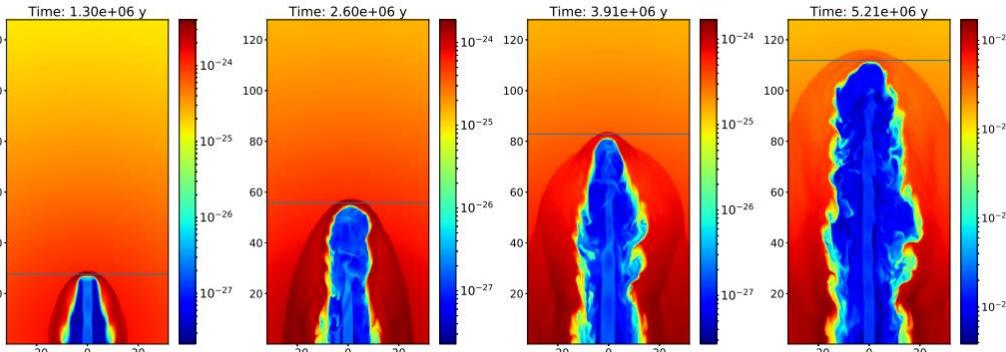
Relativistic jet



Mildly relativistic jet



Non-relativistic jet



# RMHD simulations evolution

Jet propagation

$$V_{ws} = \frac{\sqrt{\eta_R^*}}{1 + \sqrt{\eta_R^*}} v_j$$

$$\eta_R^* = \frac{\Gamma^2 \rho_j h_j}{\rho_{am} h_{am}}.$$

Case	Time [y]	Position [100 kpc]	Average velocity [c]	$\delta_R$
Relativistic	$6.51 \times 10^4$	27.1	0.136	1.43
	$9.77 \times 10^4$	451.9	0.247	2.02
	$1.30 \times 10^5$	79.4	0.275	1.71
	$1.63 \times 10^5$	105.6	0.262	1.31
Mildly relativistic	$6.51 \times 10^5$	18.1	0.00901	1.35
	$1.46 \times 10^6$	41.6	0.00940	1.15
	$2.28 \times 10^6$	74.9	0.0133	1.16
	$3.09 \times 10^6$	112.4	0.0150	0.915
Non-relativistic	$1.30 \times 10^6$	26.9	$6.72 \times 10^{-3}$	1.24
	$2.60 \times 10^6$	54.9	$7.00 \times 10^{-3}$	0.963
	$3.91 \times 10^6$	81.4	$6.63 \times 10^{-3}$	0.671
	$5.21 \times 10^6$	111.1	$7.44 \times 10^{-3}$	0.582

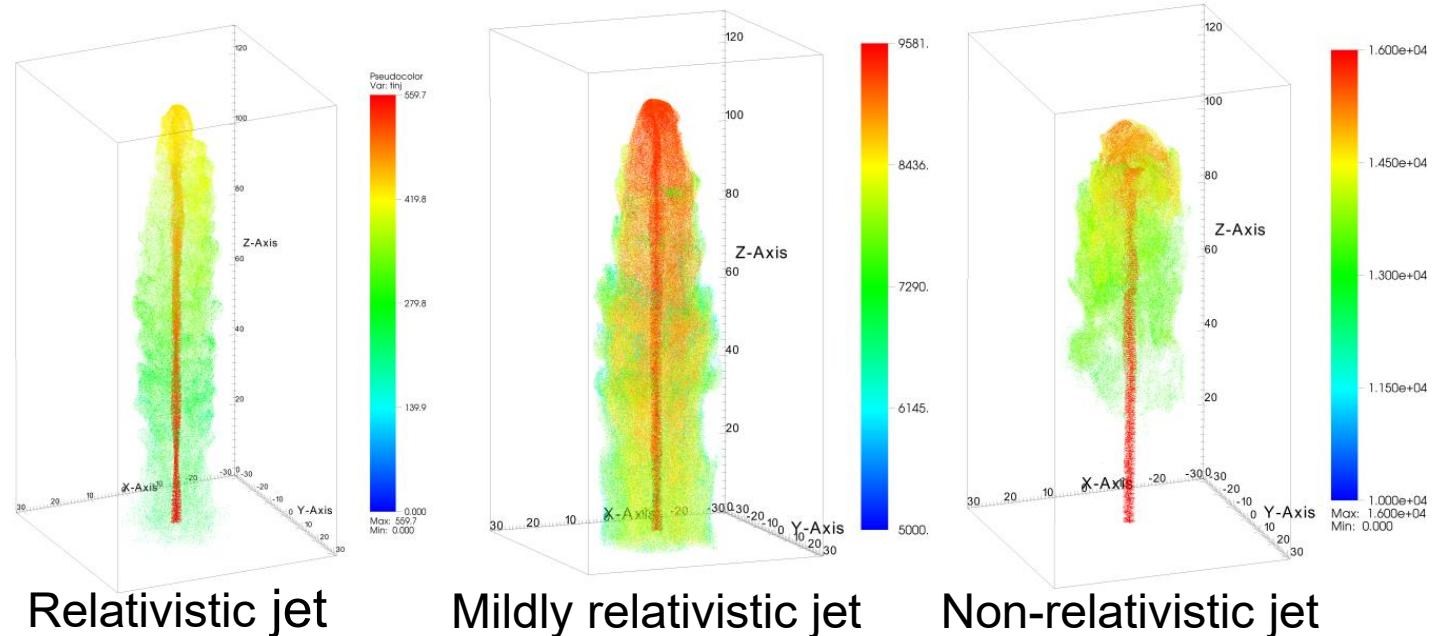


# Emission modelling

Lagrangian particles were injected at random positions inside the jet inlet.

- The injection was started after the jet established itself in the domain
- The injection rate was scaled according to mass flux of each simulation

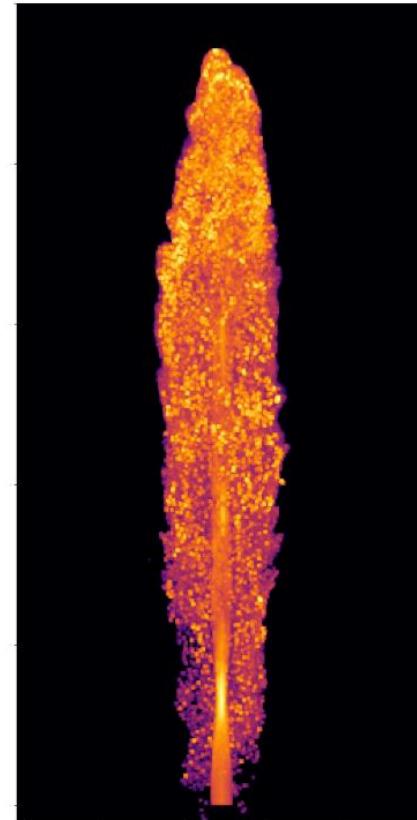
$n_e$	$10^{-3} n_{th}$
$\gamma_{min}$	$10^2$
$\gamma_{max}$	$10^5$
$p$	2.2



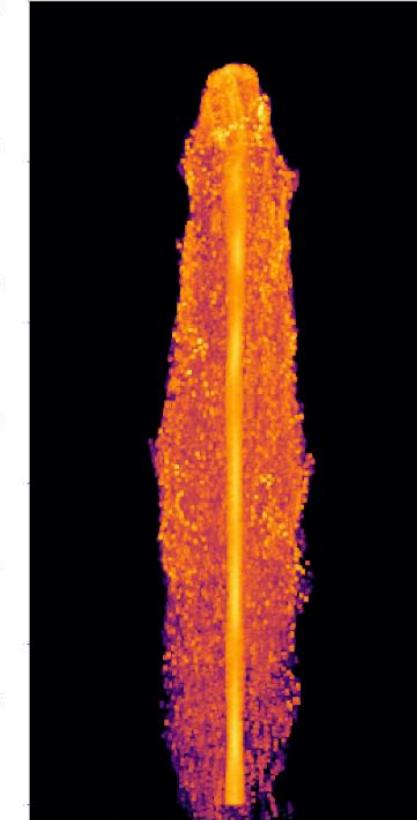
# Intensity maps: 10 GHz, $\theta = 90^\circ$

Intensity maps  
resemble FR II  
type radio  
galaxies for all  
cases

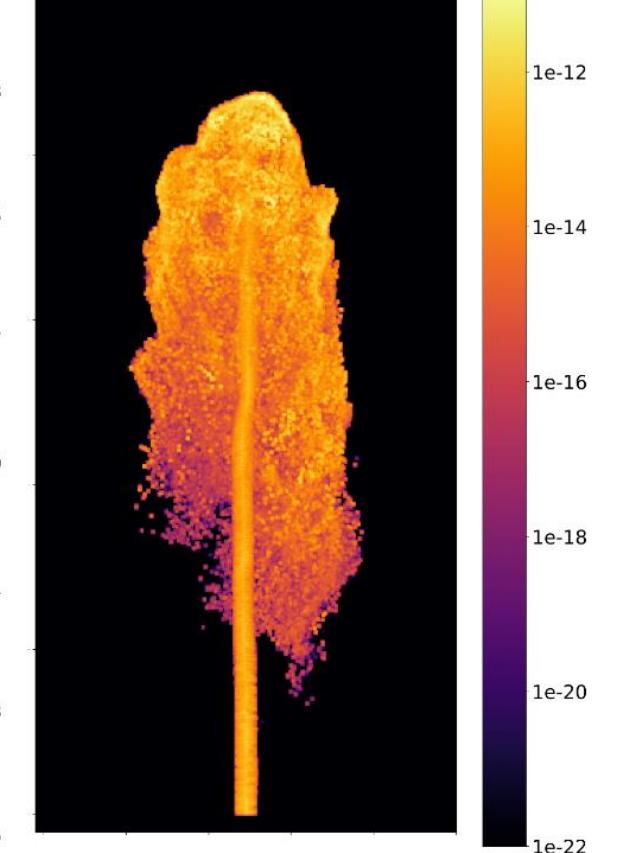
Relativistic jet



Mildly relativistic jet



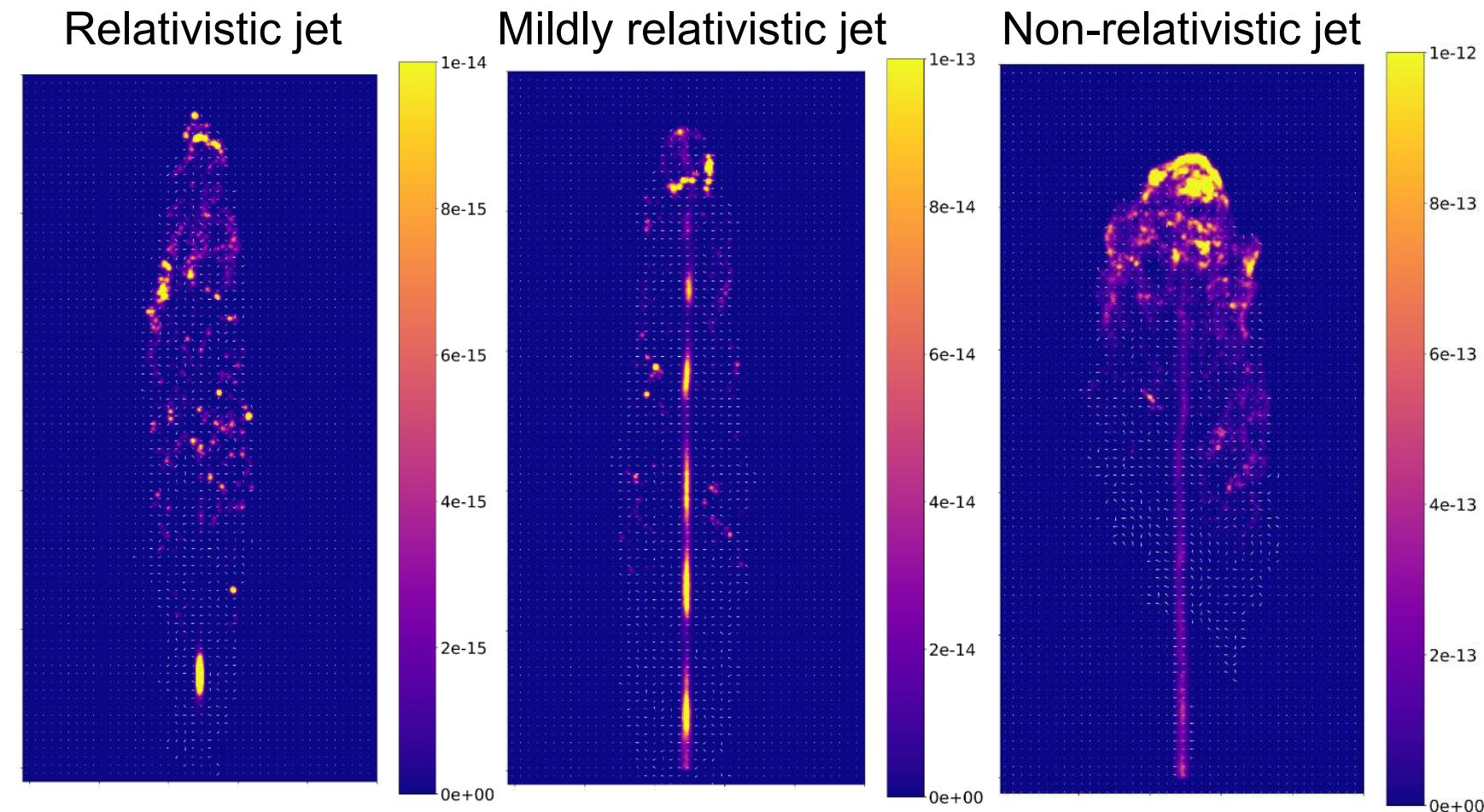
Non-relativistic jet



# Intensity maps: 10 GHz, $\theta = 90^\circ$

Intensity maps resemble FR II type radio galaxies for all cases

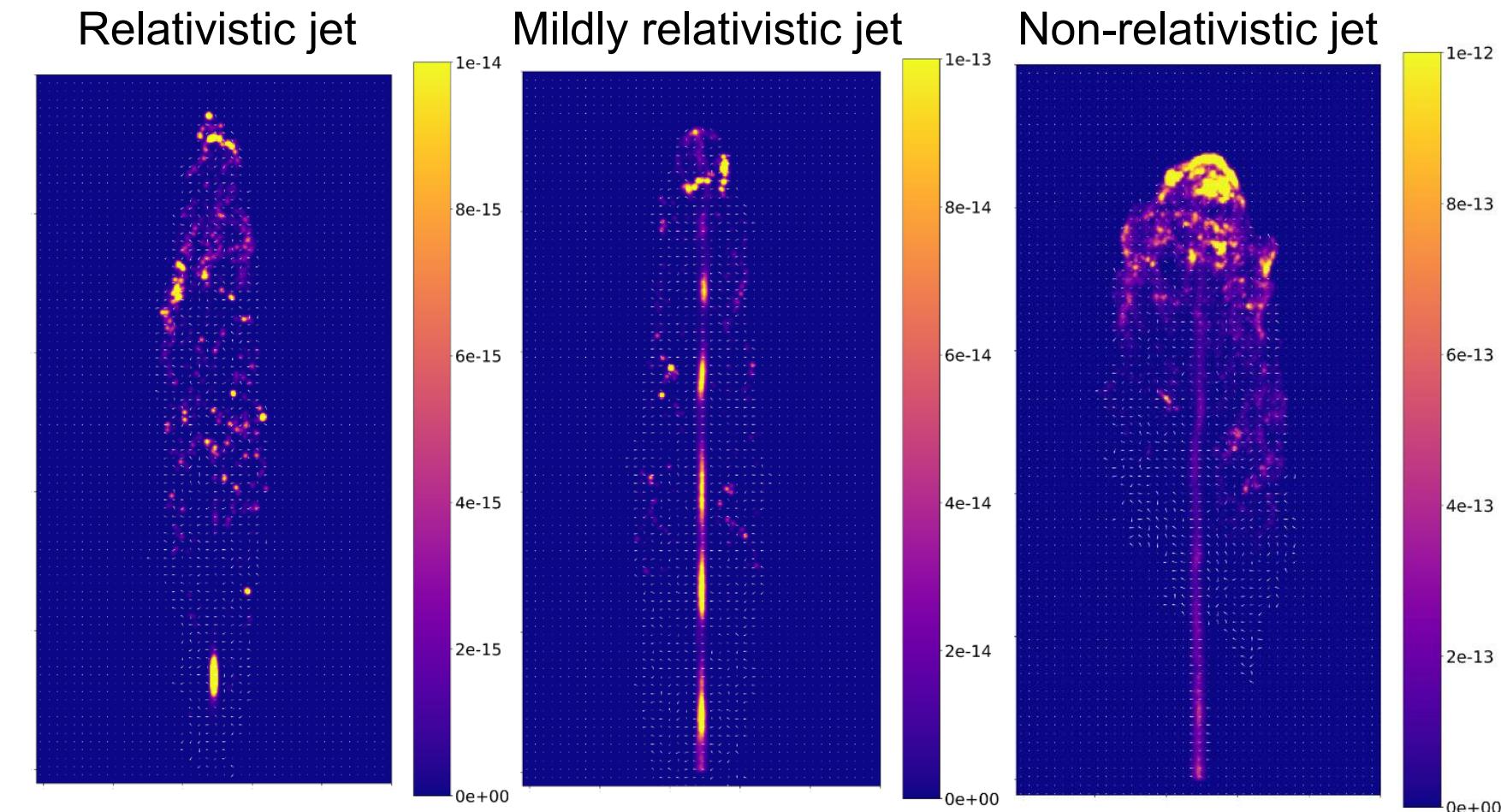
- Jets
  - Stationary emission components



# Intensity maps: 10 GHz, $\theta = 90^\circ$

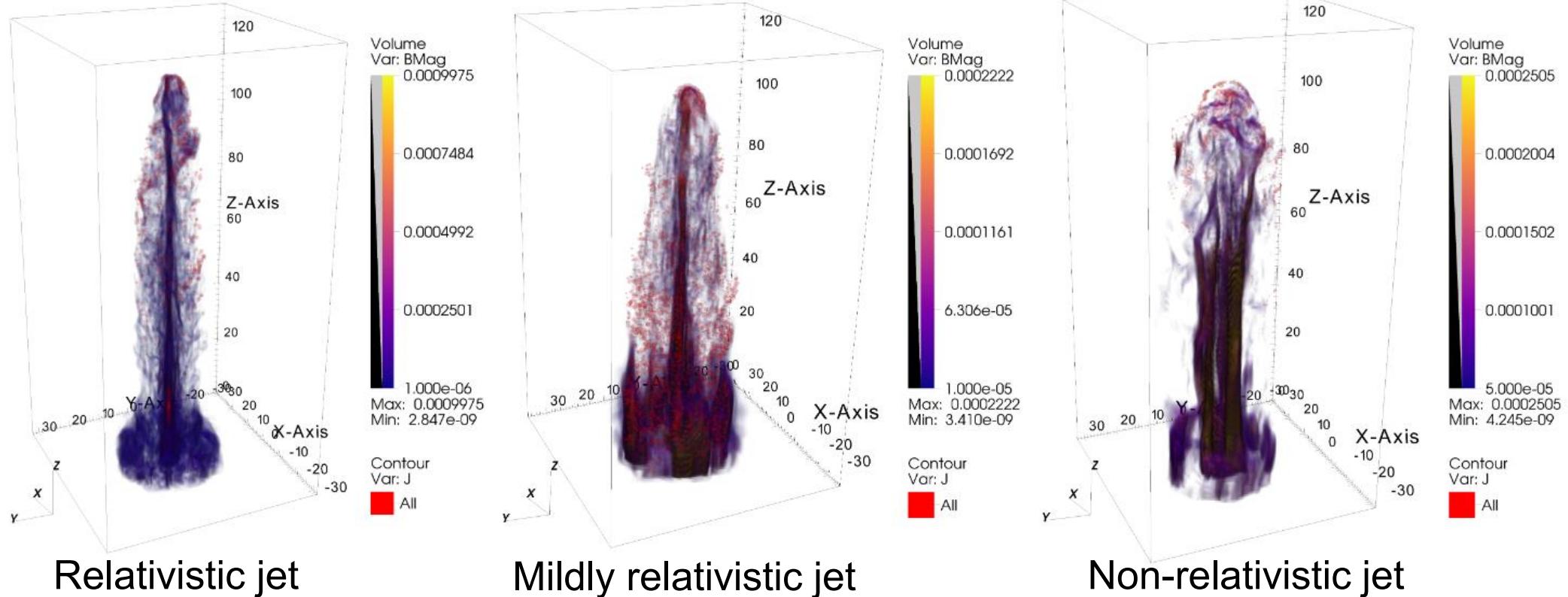
Intensity maps resemble FR II type radio galaxies for all cases

- Jets
  - Stationary emission components
- Lobes
  - Hotspots
  - Filaments



# Intensity maps: 10 GHz, $\theta = 90^\circ$

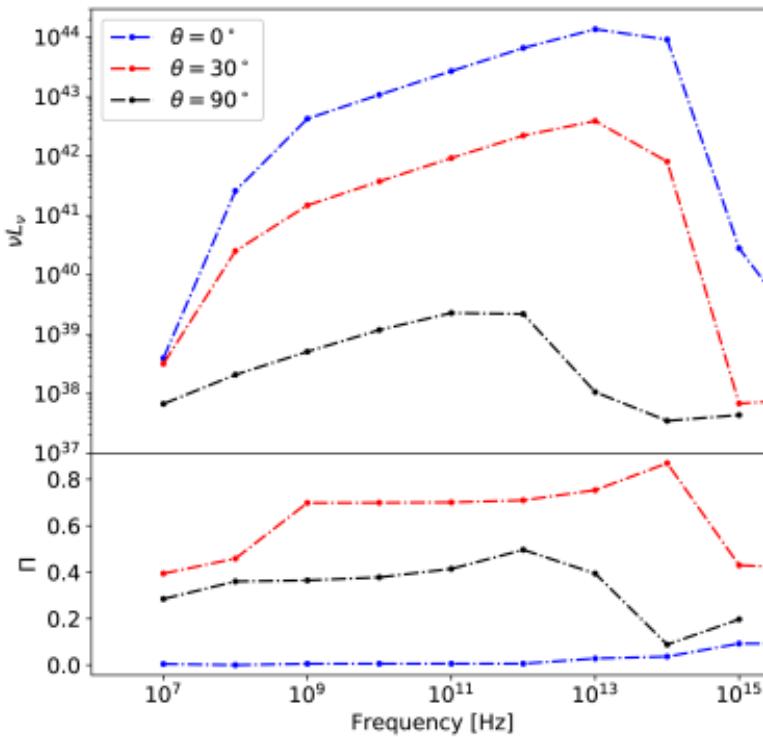
Filaments and hot spots follow magnetic filaments in the lobes



# SED modelling

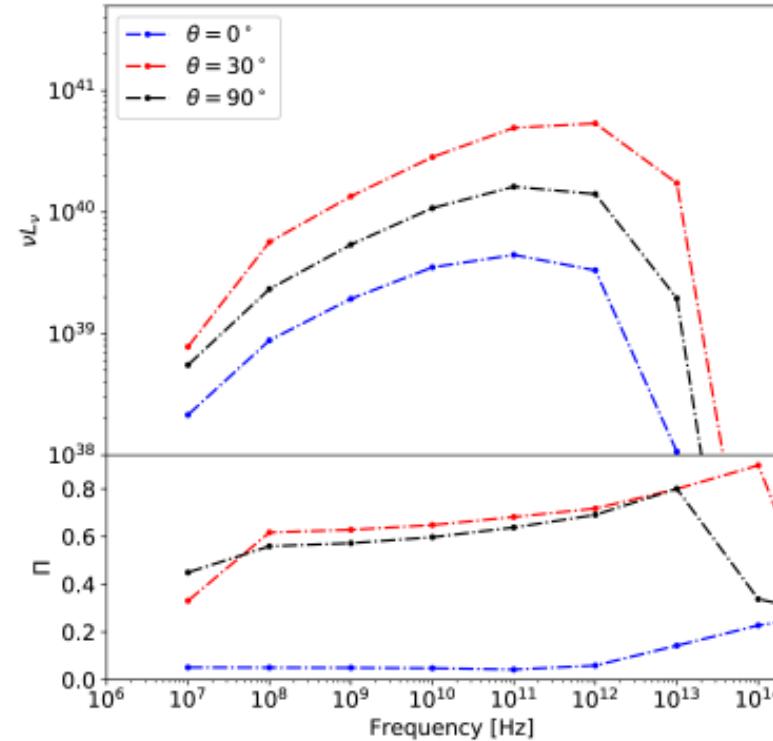
## Relativistic model

Features are dominated by Doppler boosting



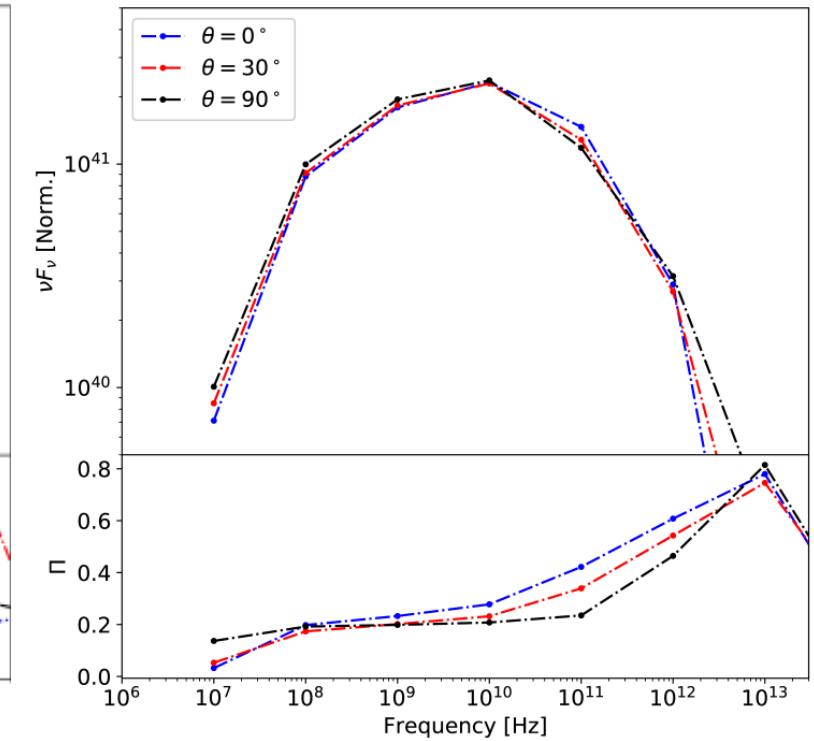
## Mildly relativistic model

Magnetic field geometry is important



## Non-relativistic model

Emission dominated by lobe region



# What about FRI's?

For FRI type structure we require deceleration

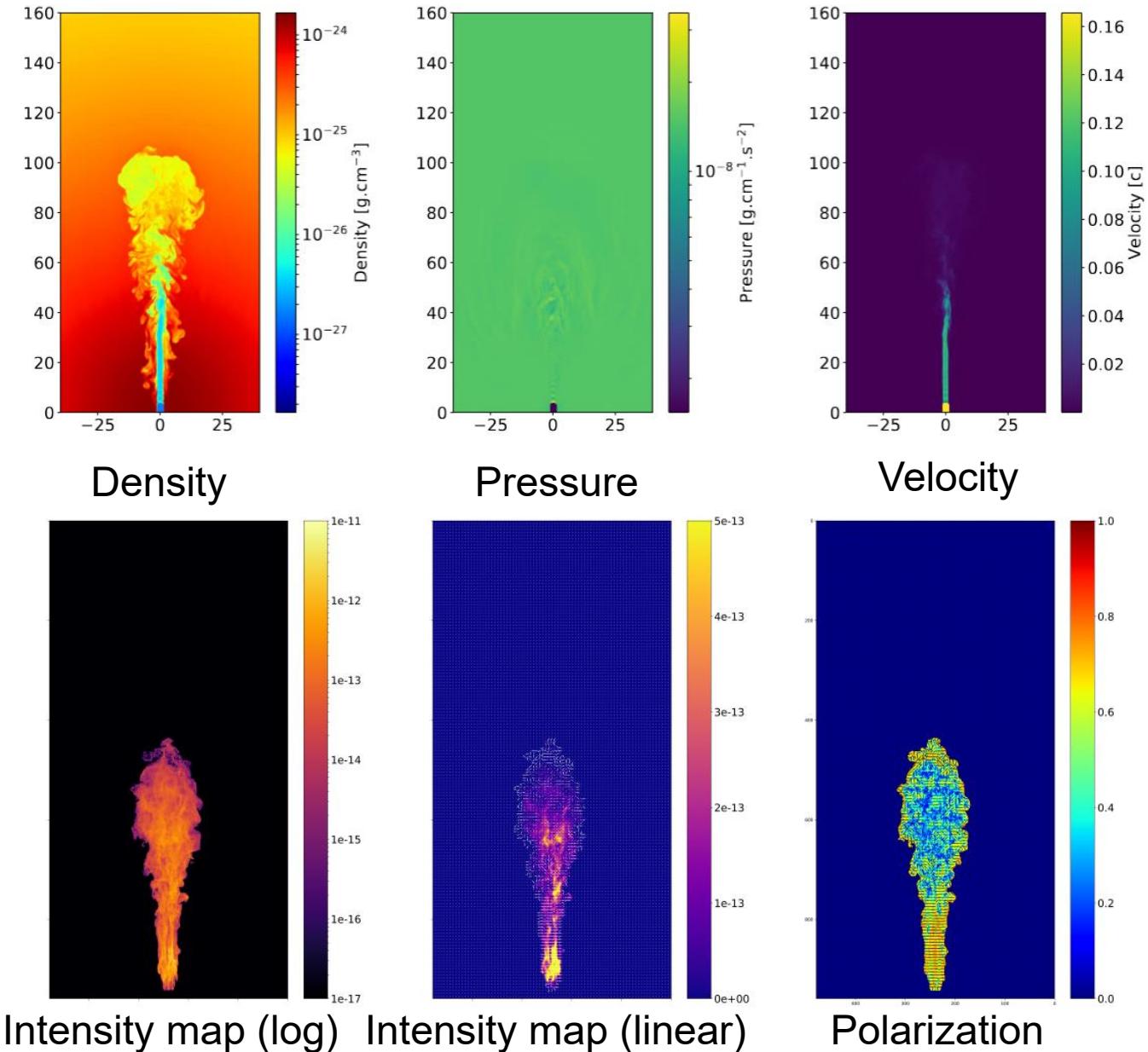
This can be achieved by a pressure mismatch

Simulation	Under-pressured jet
Resolution [pc]	16.6
Lorentz factor ( $\Gamma$ )	1.014
Mach number ( $M$ )	5
Density ratio ( $\eta$ )	$10^{-3}$
Propagation velocity ( $V_{WS}$ )	0.0051
Kinetic luminosity [erg.s $^{-1}$ ]	$10^{43}$
Magnetic field ( $B_0$ , $B_1$ , $B_c$ ) [ $\times 3.8 \times 10^{-5}$ G]	0.01, 0.04, 0.001
Plasma parameter ( $\beta_m$ )	$10^{-4}$
Magnetization parameter ( $\sigma$ )	$10^{-7}$
Number of Lagrangian particles	1 140 765

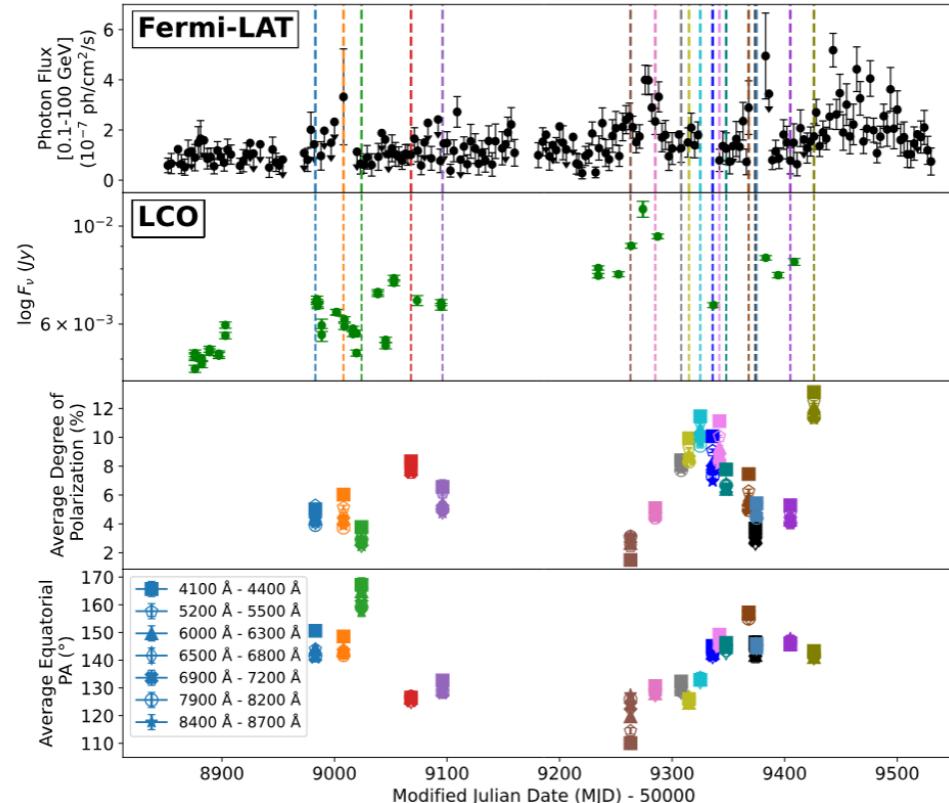
# Decelerated jet

For FRI type structure we require deceleration

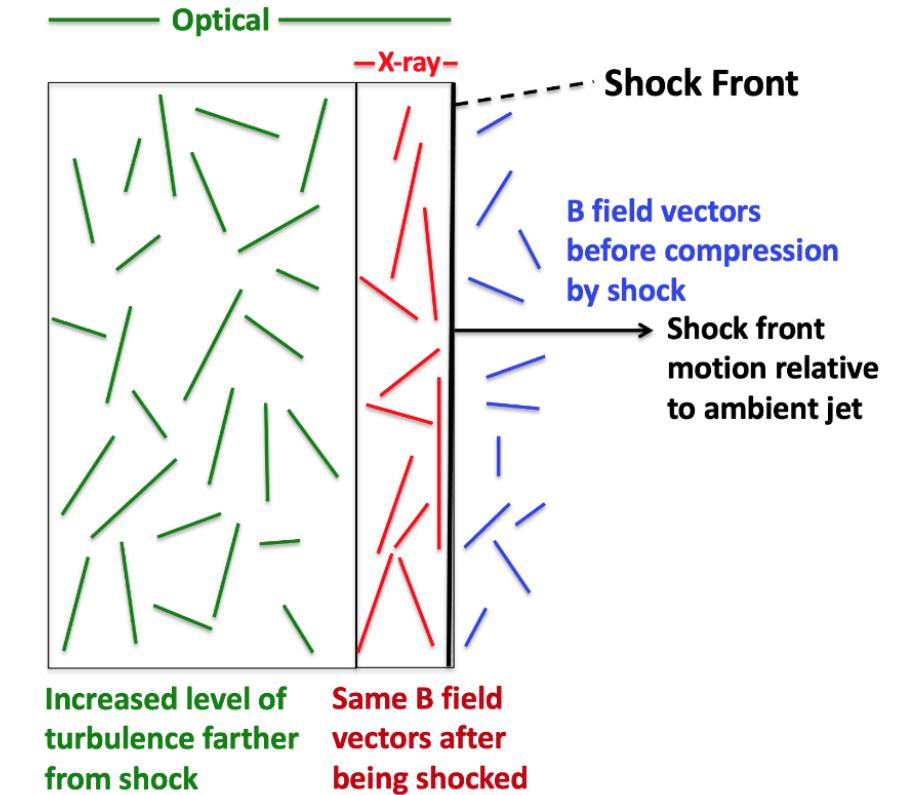
This can be achieved by a pressure mismatch



# Blazar emission



Barnard, et al. (2024). MNRAS, 532,  
<https://doi.org/10.1093/mnras/stae1576>

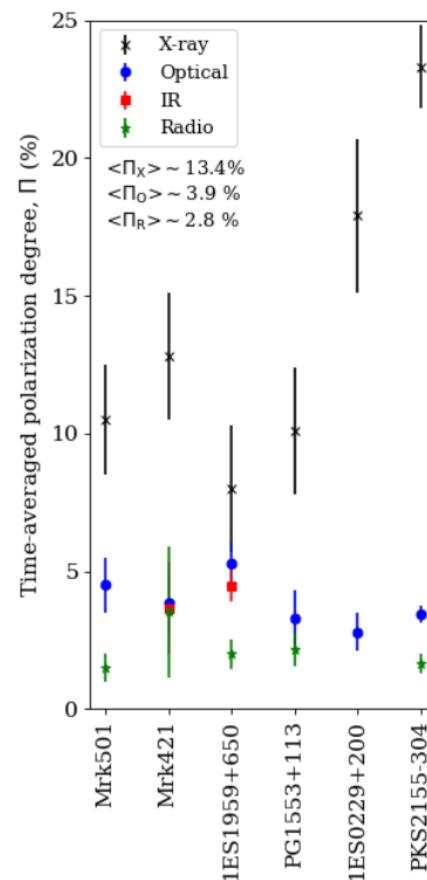


Marscher, A. P., et al. (2024). Galaxies, 12(4), 50.  
<https://doi.org/10.3390/galaxies12040050>

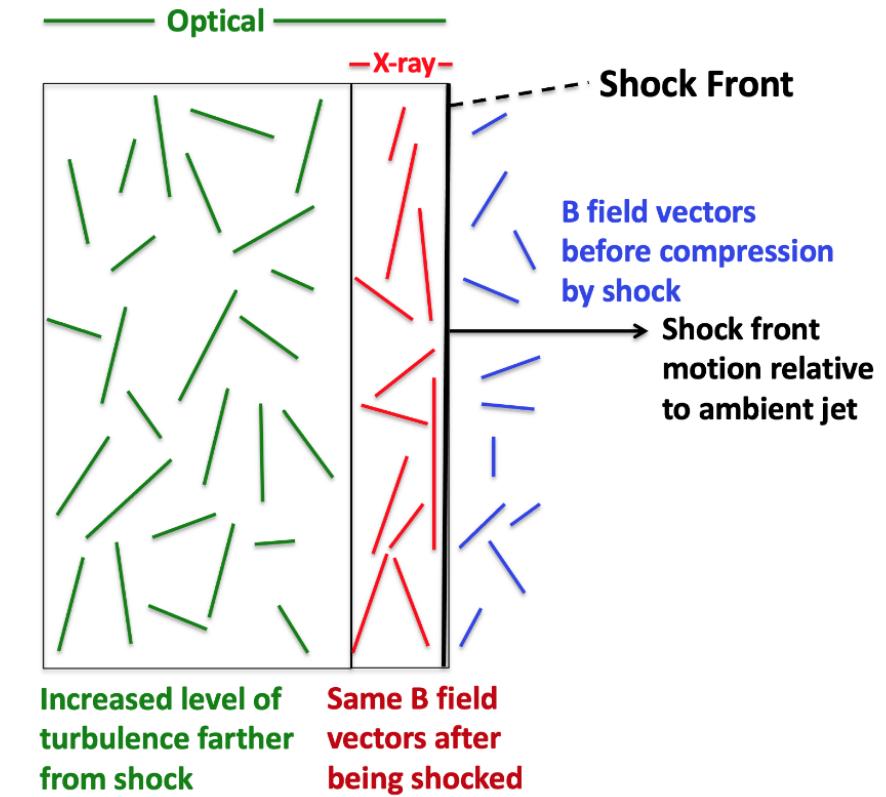
# Blazar emission

Recent IXPE observations show X-ray polarization is typically higher than Optical (see e.g. Kouch, et. al., 2024)

This is consistent with the shock in jet model (see e.g. Marscher, A. P., et al. 2024).



Kouch, et. al., 2024



Marscher, A. P., et al. (2024). *Galaxies*, 12(4), 50.

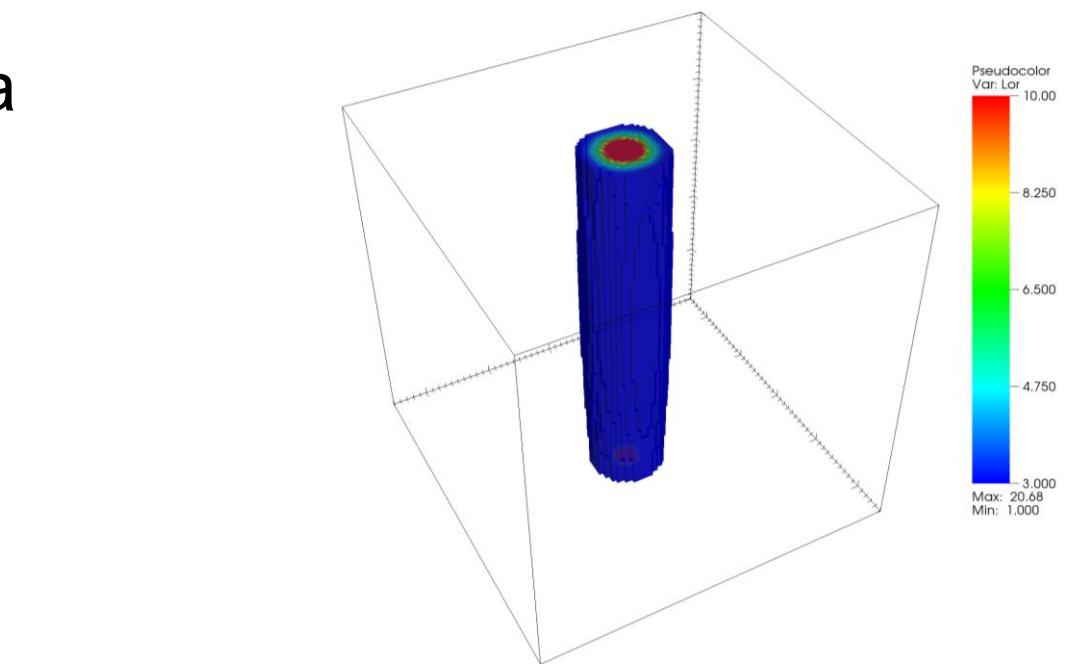
<https://doi.org/10.3390/galaxies12040050>

# Parsec scale Jet model

Initial setup consists of cylindrical jet in a uniform background

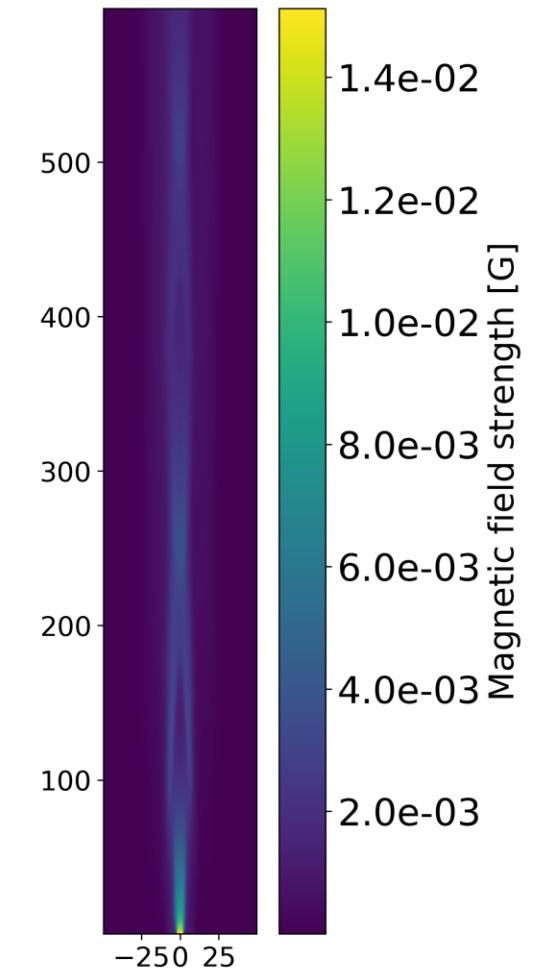
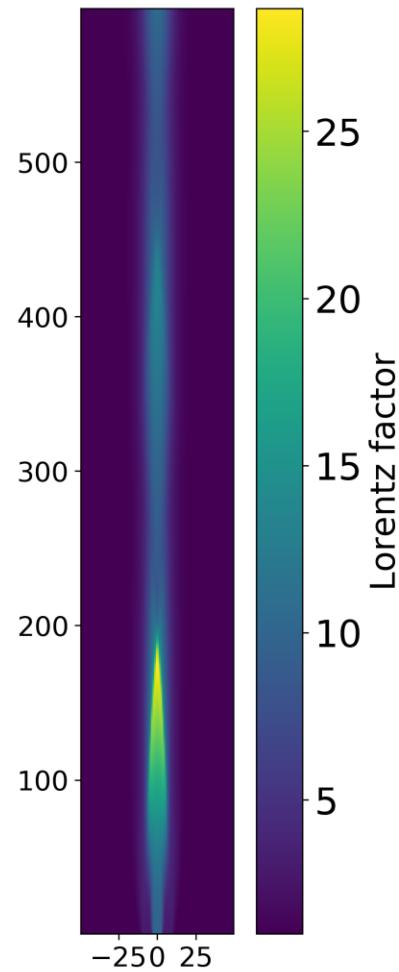
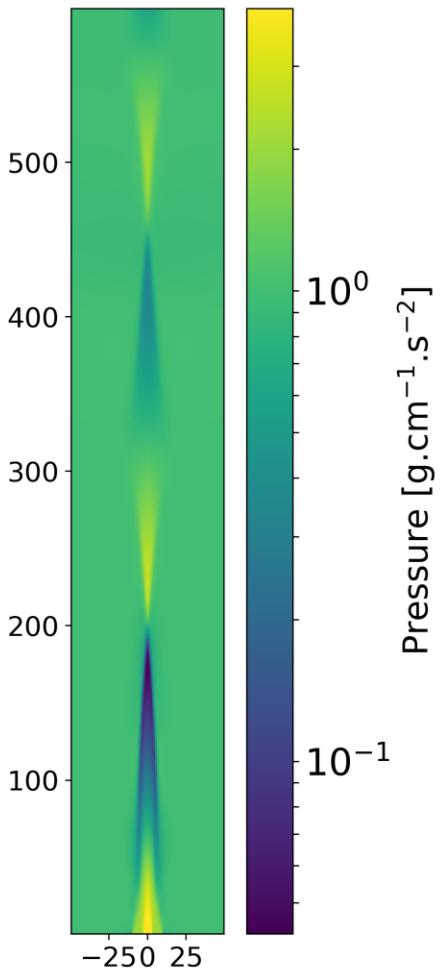
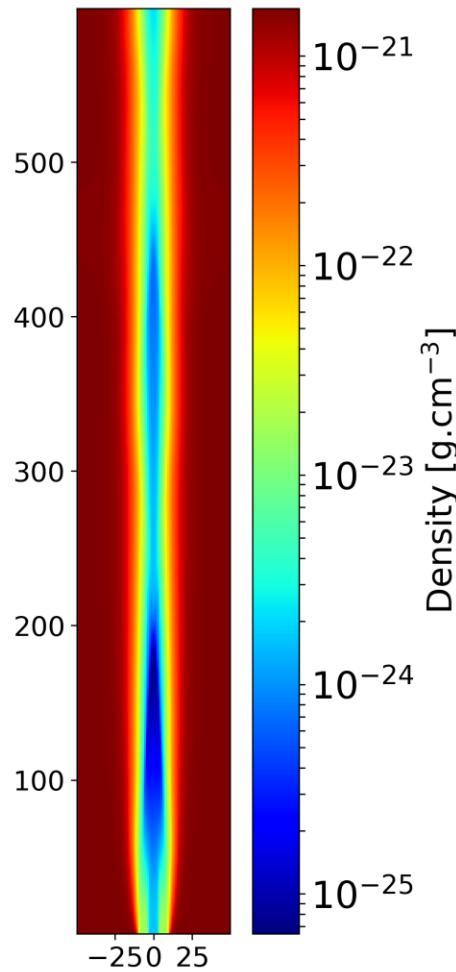
Parameter:	Spine:	Sheath:
Lorentz factor ( $\Gamma$ )	10	3
Jet Radius ( $R$ )	0.33 pc	1.0 pc
Density ratio ( $\eta_\rho$ )	$10^{-3}$	$10^{-2}$
Pressure ratio ( $\eta_p$ )	4.0	2.0
Magnetic field ( $B$ )	50 mG	5 mG
Pitch profile parameter ( $\alpha$ )	0.5	-2.0

Helical magnetic field :  
(Melianni and Keppens, APJ, 705:1594–1606, 2009)



$$B_\phi = \begin{cases} B_{\phi,\text{spine}} \left( \frac{R}{R_{\text{spine}}} \right)^{\alpha_{\text{spine}}/2}; & \text{if } 0 \leq R < R_{\text{spine}} \\ B_{\phi,\text{sheath}} \left( \frac{R}{R_{\text{spine}}} \right)^{\alpha_{\text{sheath}}/2}; & \text{if } R_{\text{spine}} \leq R \leq R_{\text{sheath}} \\ 0; & \text{if } R > R_{\text{sheath}} \end{cases}$$

# Jet cross-section



# Lagrangian particles

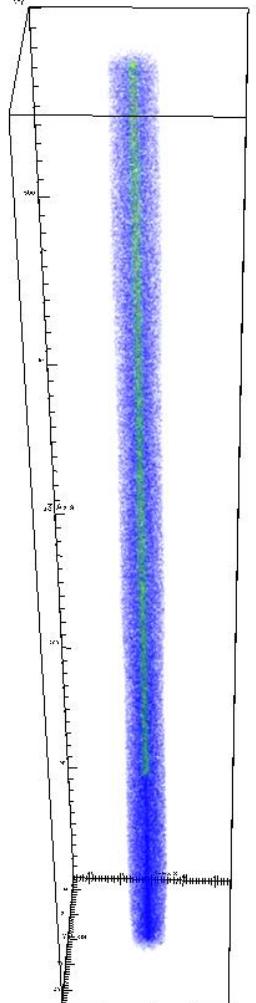
Lagrangian particles were injected at random positions inside the jet inlet.

- The injection was started after the jet established itself in the domain
  - 50 Particles per time step
  - 100 000 Particles total
- Injected with a single power-law distribution

$$n'_e(\gamma') = n'_0 \gamma'^{-p}.$$

- The injection was normalized to  $10^{-3}$  the density of the thermal fluid

$\gamma_{min}$	$\gamma_{max}$	$p$
$10^2$	$10^7$	5



Spatial distribution  
of particles in  
simulation



# Intensity maps

Different frequencies  
( $\theta = 30^\circ$ )

Radio ( $\nu = 10^9$  Hz):

- Entire jet is bright

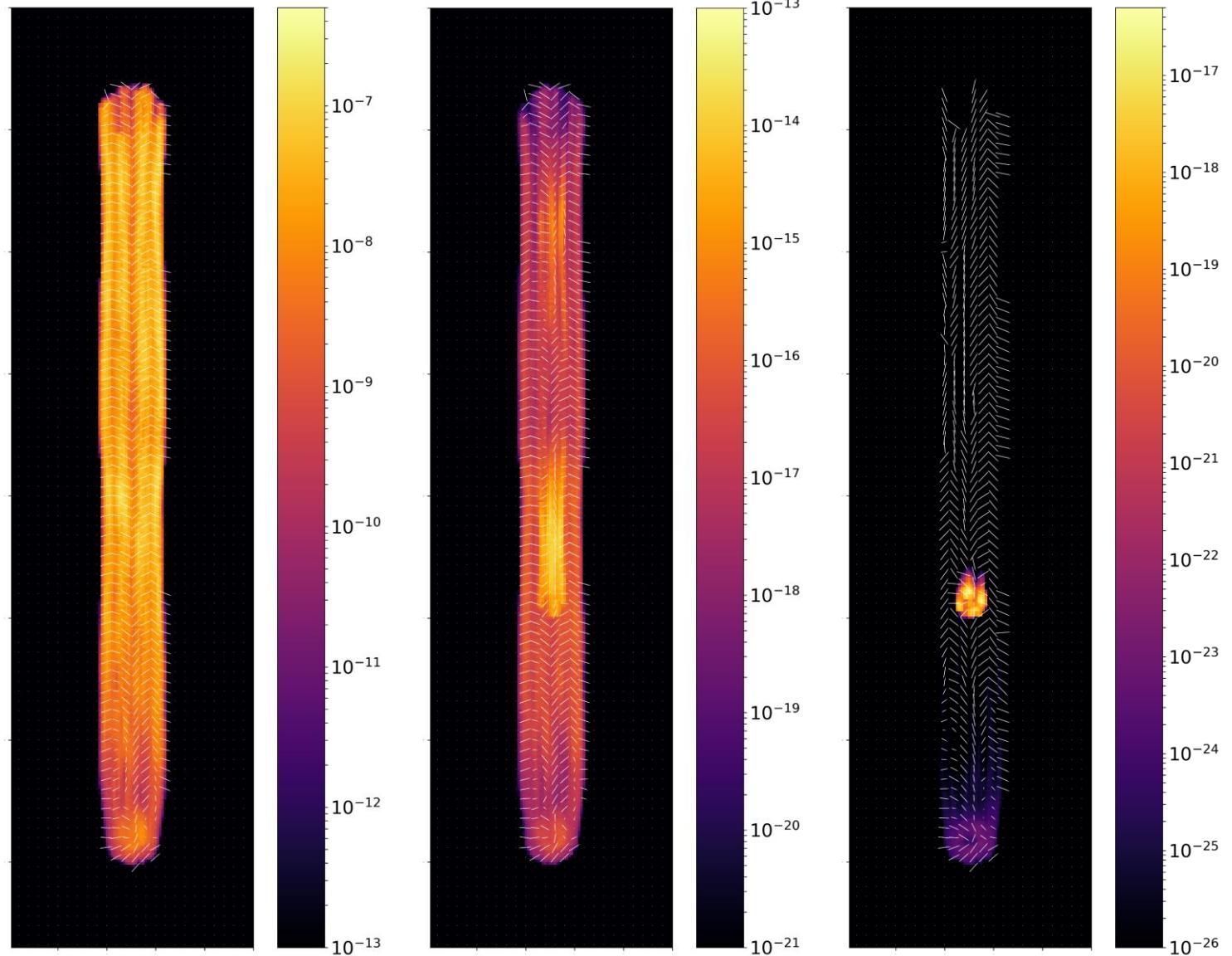
Optical ( $\nu = 10^{14}$  Hz):

- Recollimation shock brighter than jet

X-rays ( $\nu = 10^{17}$  Hz):

- Only at recollimation shock

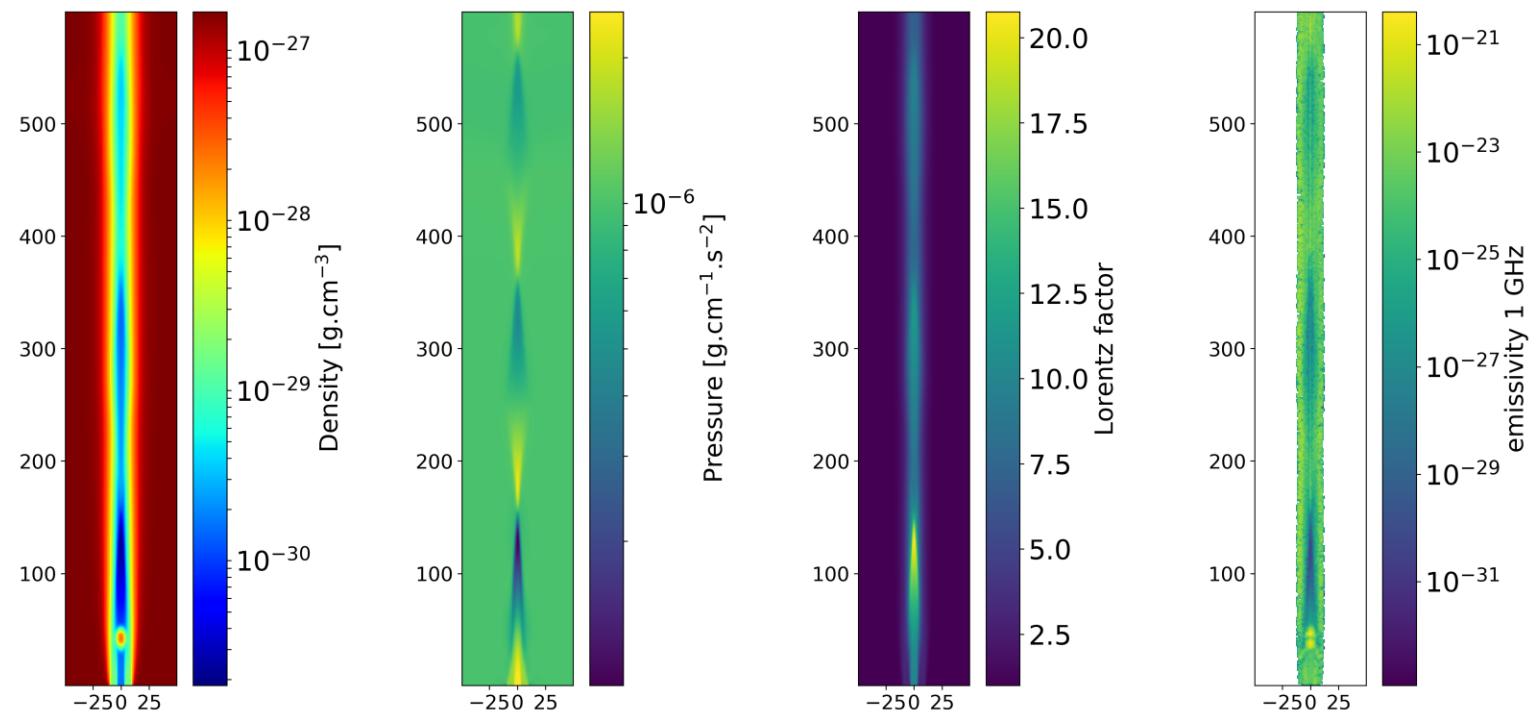
$\nu = 10^9$  Hz       $\nu = 10^{14}$  Hz       $\nu = 10^{17}$  Hz



# Variability

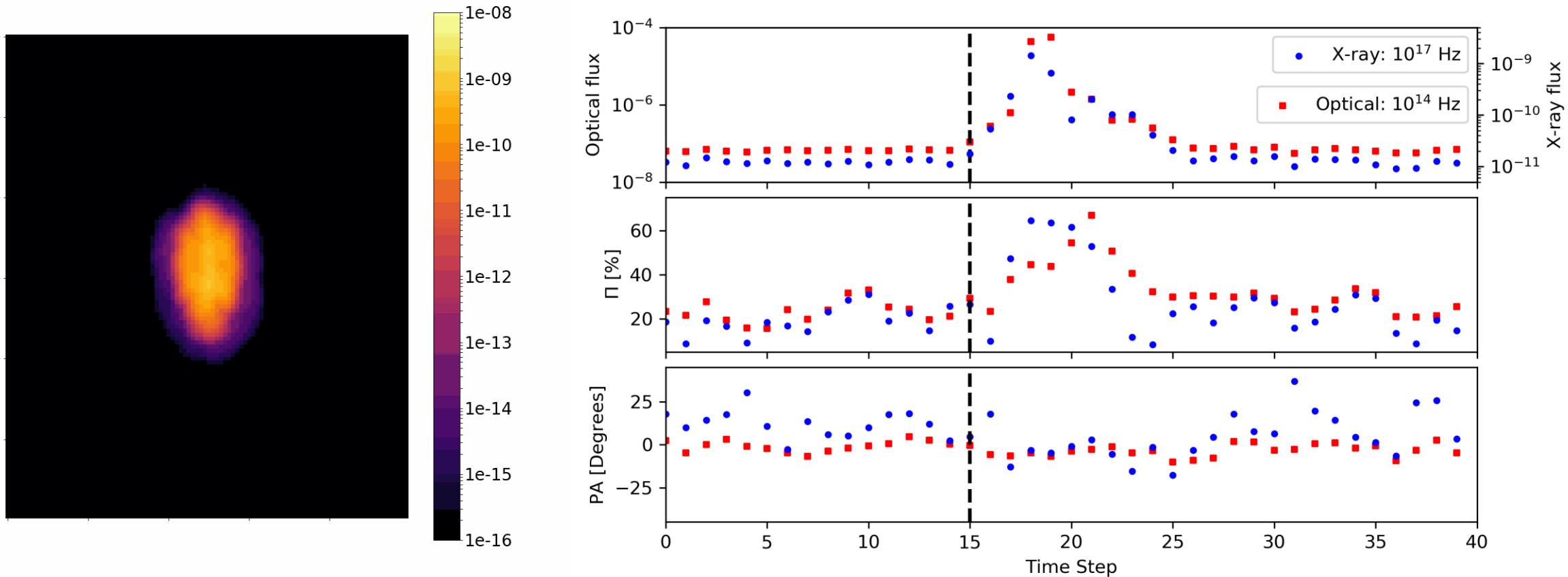
Variability is simulated through the injection of a region of increased density and magnetic field

$\rho$	$10^3 \rho_0$
$B$	$10 B_0$
$R$	$0.5 R_{spine}$



# Intensity maps and light curve

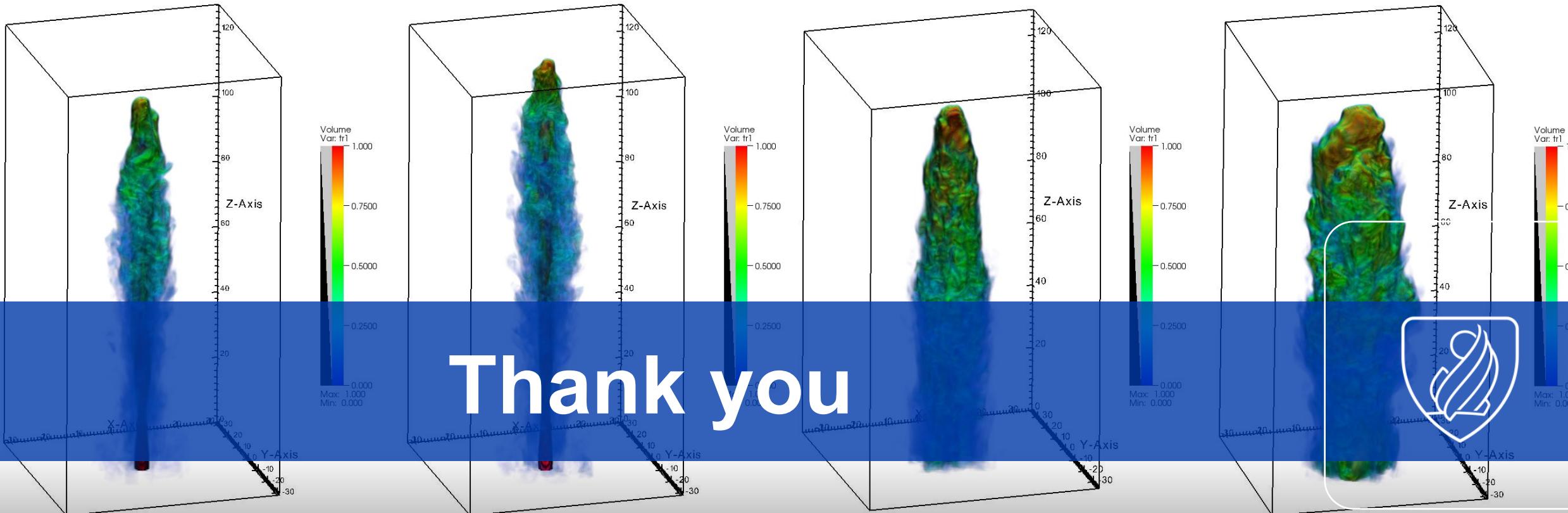
$$\theta = 2^\circ$$



# Conclusions

In this study the synchrotron emission of 3D RMHD simulations of the PLUTO code.

- Lagrangian particles were used to represent non-thermal electrons in the jet and used to calculate the synchrotron emission
  - Included synchrotron self absorption
  - Included relativistic effects and light travel time for any viewing angles
  - I,Q, U Polarization calculations
  - Reproduce SED's
- Reproduced some morphologies and characteristics seen in observations
  - Most simulations showed FR II morphology
    - Radio lobes with hotspots and filaments
  - Reproduced FRI type morphology by inducing deceleration in the jet after injection
  - Bright stationary emission components that correspond to recollimation shocks
  - Filaments and hotspots in lobes correspond to magnetic field structure in cocoon correspond to magnetic
- Variability was investigated in the form of a dense region injected into the jet.
  - Increased in flux coincided with component propagating through recollimation shock
  - X-ray increase lag behind optical
  - Increased flux coincided with an increase in polarization, peak polarization lags behind flux in optical



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