

# A new approach to studying neutrino dynamics in the primordial era

Based on [2411.00931], [2411.00892], [2409.15129], [2409.07378]

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# Cosmological neutrinos, $N_{\text{eff}}$ and CMB

- ▶ CMB is among the most precise probes of cosmology and new physics
- ▶ Strongly depends on  $N_{\text{eff}}$

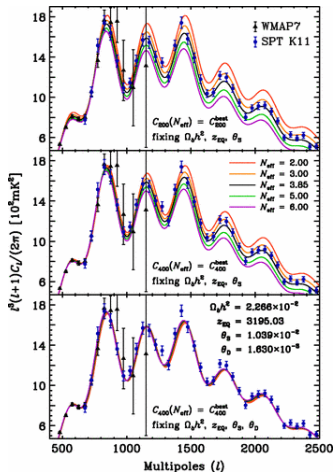
$$N_{\text{eff}} = \frac{8}{7} \left( \frac{\rho_{\text{rad}}}{\rho_{\gamma}} - 1 \right) \left( \frac{11}{4} \right)^{4/3}$$

- ▶ At 68% CL

$$N_{\text{eff}} = 2.99 \pm 0.17 - \text{Planck}$$

$$N_{\text{eff}} = 2.89 \pm 0.11 - \text{ACT}$$

- ▶ Simons Observatory aim to improve the precision to  $\sigma(N_{\text{eff}}) < 0.07$
- ▶ SM value  $N_{\text{eff}} = 3.043$



# New physics in the BBN Era

Addition of hypothetical particles can affect  $N_{\text{eff}}$  and the CMB:

- ▶ Contributing to the expansion rate
- ▶ Entropy injection (EM sector) at decays
- ▶ Injection of high-energy neutrinos  $\Rightarrow$  spectral distortions
- ▶ Mesons or unstable leptons decays  $\Rightarrow$  entropy release + secondary non-thermal neutrinos
- ▶ Additional lepton asymmetry

# Boltzmann Equation

- ▶ At  $T \sim \text{MeV}$ , EM sector - equilibrium. Dynamics of neutrinos - Boltzmann equation:

$$\frac{\partial f_{\nu\alpha}(E_\nu, t)}{\partial t} - E_\nu H \frac{\partial f_{\nu\alpha}(E_\nu, t)}{\partial E_\nu} = \sum_{\beta} \langle P_{\beta\alpha} \rangle \mathcal{I}_{\text{coll}, \nu\beta} [E_\nu, f_{\nu\alpha}, f_{\nu\beta}, T] \quad (1)$$

$$\mathcal{I}_{\text{coll}, \nu\alpha}(p_1) = \frac{1}{2E_{\nu\alpha}} \sum \int \prod_{i=2}^m \frac{d^3 \mathbf{p}_i}{(2\pi)^3 2E_i} \prod_{f=1}^{n-m} \frac{d^3 \mathbf{p}'_f}{(2\pi)^3 2E'_f} \\ \times |\mathcal{M}|^2 F[f] (2\pi)^4 \delta^{(4)} \left( \sum_{i=1}^m p_i - \sum_{f=1}^{n-m} p'_f \right). \quad (2)$$

## Solution

- ▶ **Integrated approach** — assume neutrino distributions  $f_\nu \equiv f_{\text{FD}}(T)$ , which reduces the problem to a system of ODEs for  $T_\gamma$  and  $T_{\nu_i}$ .
- ▶ **Discretized approach** — directly solve the Boltzmann equation numerically on a fixed energy grid for each  $f_{\nu_i}$ .

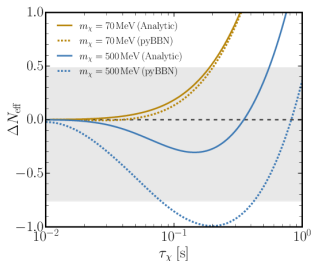
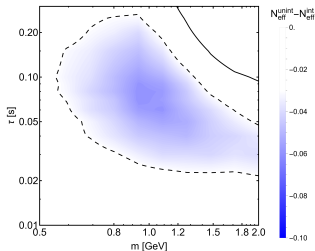
# Integrated Approach

## Pros

- ▶ Computation speed.
- ▶ Convenient for low-energy neutrino or EM injections.

## Cons

- ▶ Breaks down if neutrinos are highly non-thermal ( $E_\nu \gg T$ ).
- ▶ May yield *qualitatively* incorrect results in such regimes.



**Figure:** *Left:* Integrated vs. unintegrated approach for a toy FIP decaying into the EM sector. *Right:* Impact on  $N_{\text{eff}}$  of a decaying HNL: unintegrated (analytic) vs. discretized (pyBBN) treatment.

# Discretized Approach

- ▶ Define a momentum grid with fixed step size in comoving momentum space:  $\tilde{p} = p_{\text{phys}} \cdot a(T)/a_0$ .
- ▶ Analytically reduce the collision integral.
- ▶ Solve the Boltzmann integro-differential equation on this grid.

## Pros

- ▶ Captures the full evolution of the neutrino plasma.
- ▶ Accuracy controlled by grid resolution.

## Cons

- ▶ Requires strong dimensional reduction of  $I_{\text{coll},\alpha}$ .
- ▶ Computational time scales as

$$t_{\text{comp}} \propto E_{\nu,\text{max}}^{k+2},$$

where  $k$  is the reduced dimensionality.

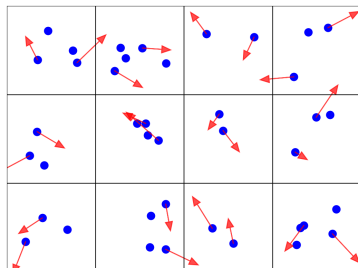
# Direct Simulation Monte Carlo (DSMC)

- ▶ Original DSMC was used for the simulation of rarefied gas flows
- ▶ States of individual particles  $\{\mathbf{r}_i, \mathbf{v}_i, t\}$
- ▶ Volume divided into cells -  $N_{\text{cell}}$  particles, interaction within cell
- ▶ At each iterative timestep  $\Delta t$

$$N_{\text{sampled}} = \frac{N_{\text{cell}}(N_{\text{cell}} - 1)}{2} \frac{(\sigma v)_{\text{max}} \Delta t}{V_{\text{cell}}}$$

pairs are sampled for interaction.

- ▶ Each interaction is accepted with probability  $P_{\text{acc}} = \frac{(\sigma v)}{(\sigma v)_{\text{max}}}$  and the outgoing kinematics is generated



# DSMC for Early Universe

DSMC can be adapted for the Early Universe dynamics:

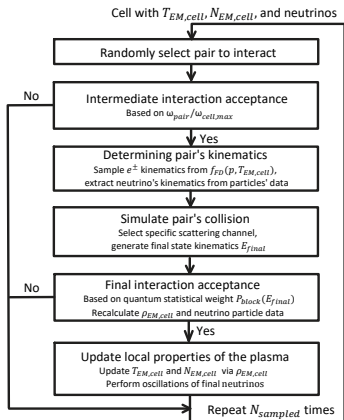
## General idea:

- ▶ System is presented as a set of individual particles ( $\nu_i/\bar{\nu}_i$  and  $\gamma, e^\pm$ , potentially  $X, Y...$  representing BSM species, mesons etc.).
- ▶ Isotropy and homogeneity - only momenta degrees of freedom  $\{\mathbf{p}_i, \mathbf{v}_i, t\}$ .
- ▶ System is split into subsets (cells) at each timestep, and only interactions within a cell are considered
- ▶ EM particles are in thermal equilibrium represented by  $T_{EM}/T_{EM,cell} \Rightarrow$   
No tracking, we *sample* them at every step.
- ▶ Additional Fermi/Bose factors
- ▶ Expansion of the Universe is included at each step  
 $V_{\text{system}} \rightarrow V_{\text{system}}(1 + 3H\Delta t), \quad E_i \rightarrow \frac{E_i}{1+H\Delta t}$



## Interaction step

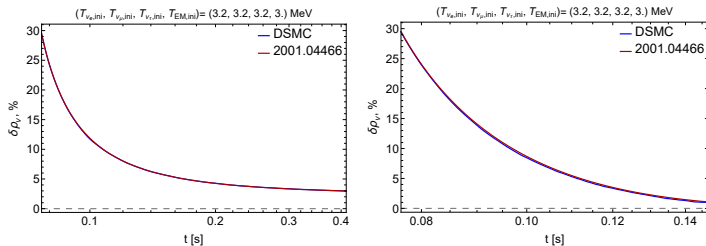
- ▶ Initialize the cell with  $T_{EM,cell} = T_{EM}$  and  $N_{EM}$
- ▶ Sample the interaction between  $N_{sampled}$  ( $\Delta t$  passed)
- ▶ In case of presence of extra species - determine their dynamics over  $\Delta t$  + inject neutrinos from decays
- ▶ Update the volume of the system and particles' energies due to expansion
- ▶ Repeat



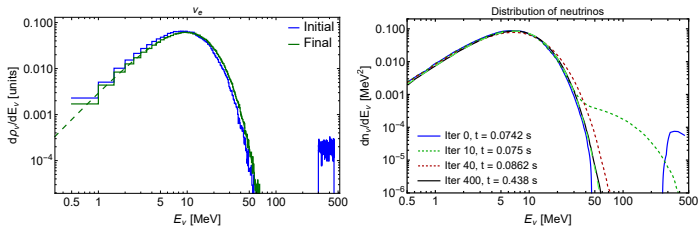
## What it gives?

- ▶ Weaker dependence of the complexity on the maximum neutrino energy in the system  $\Rightarrow$  significant speed-up compared to the traditional Boltzmann discretization approach.
- ▶ Possibility to study very high-energetic injections  $\gg$  GeV,
- ▶ Cross-checks for Boltzmann solver implementations.
- ▶ Easy tracking of the system at each step and more control over microscopics.

## Cross-checks and tests



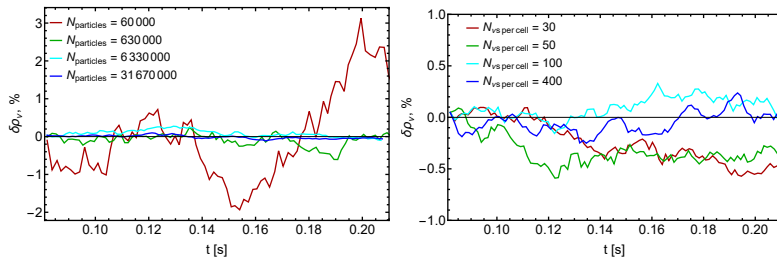
**Figure:** Energy density evolution if **all** species are assumed with equilibrium distribution (integrated approach) with (left) and without (right) expansion.



**Figure:** Approaching the thermal equilibrium in case of high-energy neutrino injection

## Cross-checks and tests

- ▶ Simulation with  $N = 3 \cdot 10^7$  has fluctuations at level  $\mathcal{O}(0.1\%)$
- ▶  $\text{few} \times 100$  is a sufficient number of neutrinos per cell



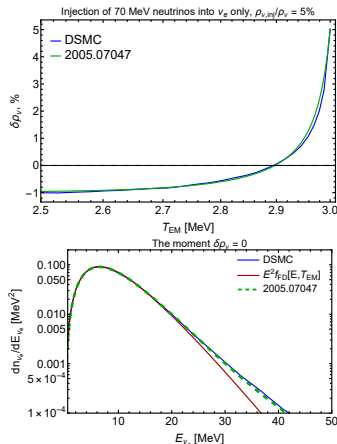
**Figure:** The temporal evolution of the quantity  $\delta\rho_\nu$  when varying numbers of neutrinos per cell  $N_{\text{cell},\nu}$  and particles in the system  $N$  with equilibrium starting conditions

- ▶ Comparison of the DSMC approach with the discretization code for the setup of injection of 70 MeV neutrinos into  $\nu_e$ .
- ▶ presented value  $\delta\rho_\nu$ :

$$\delta\rho_\nu = \left( \frac{\rho_{\text{EM}}}{\rho_\nu} \right)_{\text{SM}} \frac{\rho_\nu}{\rho_{\text{EM}}} - 1$$

- ▶ Injection of neutrinos with  $E_\nu \gg T$  eventually leads to **decrease** of  $N_{\text{eff}}$

- ▶ In recent update of the DSMC [2508.08379], complete SM setup including QED corrections were tested and result  $N_{\text{eff}} = 3.0439$  was obtained. It is in perfect agreement with previous calculations



## Conclusion

- ▶ DSMC presents a new approach of studying the dynamics of neutrinos during their decoupling
- ▶ Their non-trivial evolution can lead to unexpected outcomes in terms of  $N_{\text{eff}}$
- ▶ DSMC proposes a cross-check **alternative** for SM BBN/CMB scenario, significantly **more efficient** option for heavy ( $m_{\text{FIP}} \lesssim \text{GeV}$ ) FIPs+BBN/CMB and the **only** option to study ultra-high energy neutrino injections  $E_\nu \gg \text{GeV}$

Thank you for your attention

# Metastable Particles

# Metastable particles

- ▶ EM and neutrino injections can appear through metastable particles produced in FIPs' decays
- ▶ It was common to treat them as instantly decaying
- ▶ They can participate in (i) annihilations, (ii) interactions with nuclei, (iii) EM scatterings (iv) decays
- ▶ Except for EM scatterings  $\Gamma_{EM} \gg \Gamma_{\text{ann, nucl, dec}}$  no clear hierarchy

We focus on the dynamics of  $\mu^\pm, \pi^\pm, K^\pm, K_L^0$

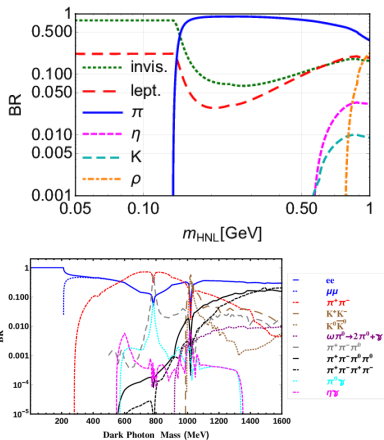


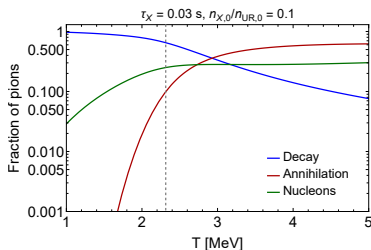
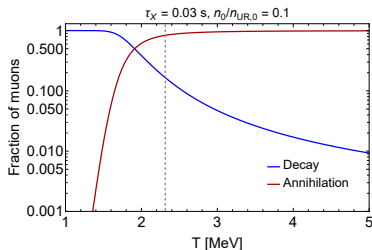
Figure: BR of different FIPs



# Evolution of metastable particles

- We solve a system of coupled equations for each  $Y = \mu^\pm, \pi^\pm, K^\pm, K_L$ .

$$\frac{dn_Y}{dt} + 3Hn_Y = \frac{n_X}{\tau_X} N_Y^X - \frac{n_Y}{\tau_Y} - n_Y n_{\bar{Y}} \langle \sigma_{\text{ann}}^Y v \rangle + \left( \frac{dn_Y}{dt} \right)_{\mathcal{N}} + \sum_{Y' \neq Y} n_{Y'} \Gamma_{Y' \rightarrow Y}$$



**Figure:** The yields of muons and pions that would decay, annihilate, or interact with the nucleons if injected by decaying toy-model FIP with BR solely into a  $\pi^+\pi^-/\mu^+\mu^-$ .

## $N_{\text{eff}}$ change for toy models and scalar

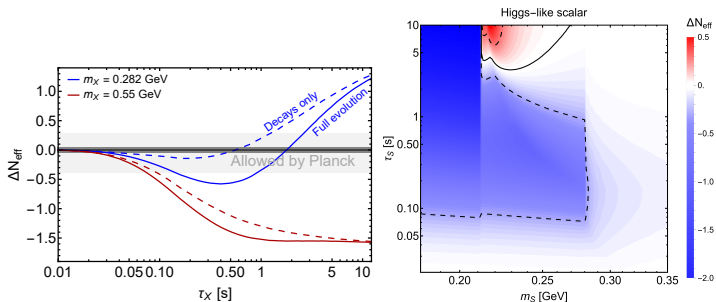


Figure: Left: toy model decaying only into pions, Right: Higgs-like scalar effect on  $N_{\text{eff}}$

- ▶ Accurate account of  $Y$ 's evolution change the outcome of  $N_{\text{eff}}$  value.
- ▶ Especially important near the decay mass threshold.