

First LIV constraint from a cooperation of Imaging Atmospheric Cherenkov Telescopes



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For the γ LIV WG



6 November 2025

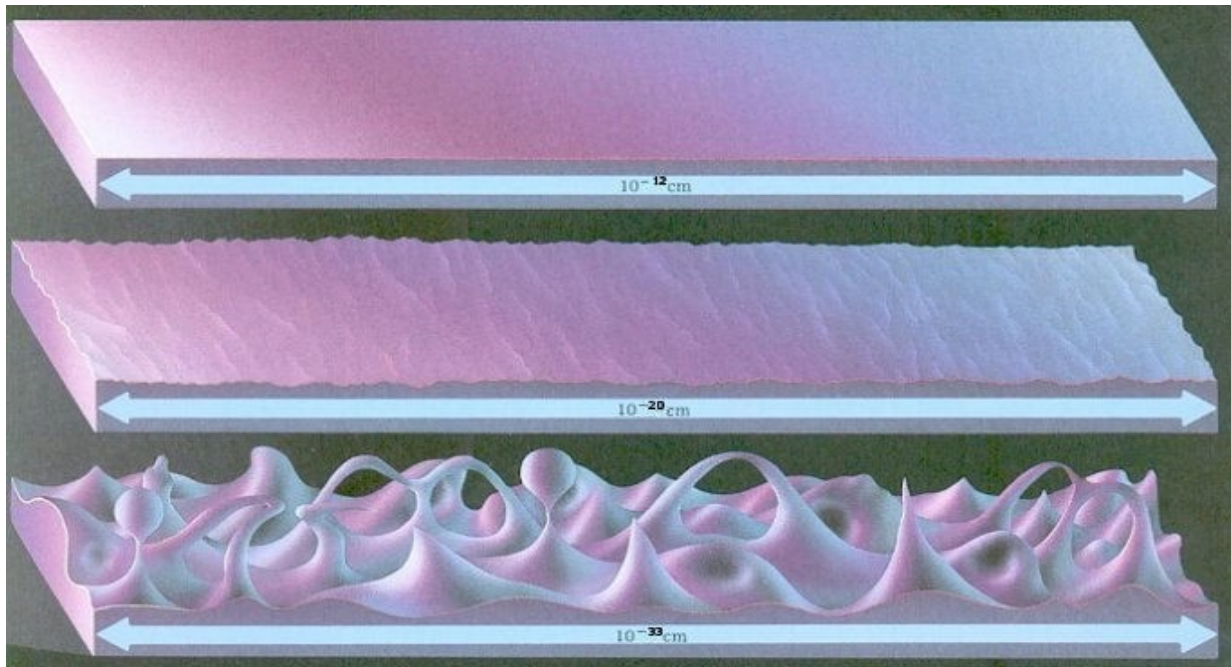


TeV Particle Astrophysics

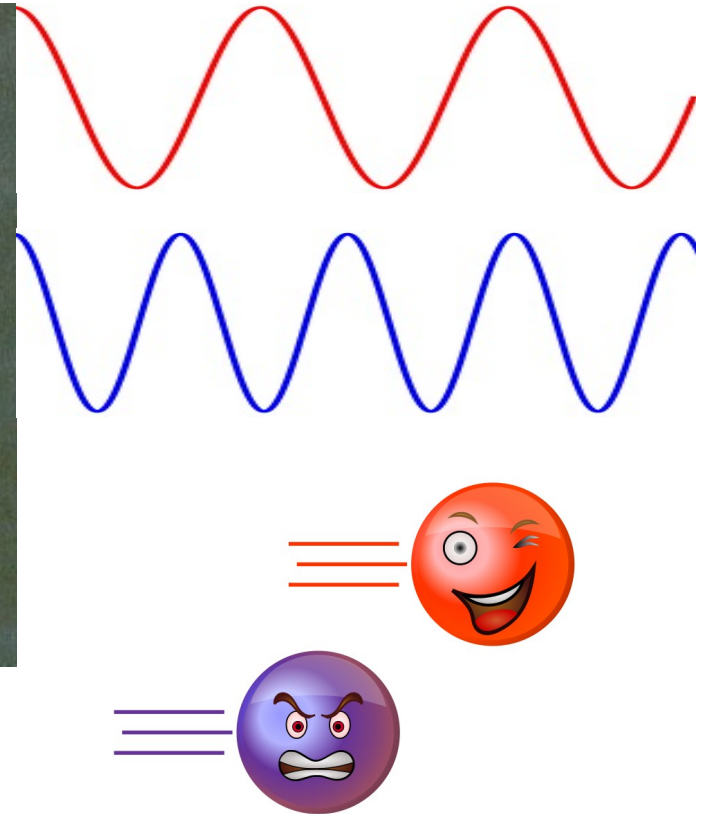
T^eVPA

Valencia 2025

Lorentz invariance violation (LIV)



<http://universe-review.ca/R01-07-quantumfoam.htm>



Lorentz invariance violation (LIV)

- Modified photon dispersion relation
- Usual starting point in searches for effects of QG with gamma rays

$$E^2 = p^2 c^2 \times \left[1 + \sum_{n=1}^{\infty} S_n \left(\frac{E}{E_{\text{QG},n}} \right)^n \right]$$

Diagram annotations:

- Red box labeled "photon energy" with an arrow pointing to the E in the numerator of the fraction.
- Red box labeled "QG energy scale" with an arrow pointing to the $E_{\text{QG},n}$ in the denominator of the fraction.
- Red box labeled " $S = \pm 1$ " with an arrow pointing to the S_n coefficient.

Expectation:

$$E_{\text{QG},n} = \mathcal{O}(E_{\text{Pl}}) \simeq 1.22 \times 10^{19} \text{ GeV}$$

- Not a direct consequence of any particular QG model
- Simple way of parametrizing “out of the ordinary” behaviour

Consequences of MDR

- Energy dependent photon group velocity
- Modified reaction thresholds
- Modified reaction cross sections
- Vacuum birefringence
- Modified Compton scattering
- Modified synchrotron radiation
- ...
-
- Tiny but **cumulative** effects

Consequences of MDR

Focus of today's talk

- Energy dependent photon group velocity

- Modified reaction thresholds
- Modified reaction cross sections
- Vacuum birefringence
- Modified Compton scattering
- Modified synchrotron radiation

...

-
- Tiny but **cumulative** effects

Check:

- Addazi et al. 2022 (arXiv:[2111.05659](#)) for a comprehensive review of QG models and tests with cosmic messengers
- Terzić et al. 2021 (arXiv:[2109.09072](#)) for a review focused on tests with gamma rays

Energy dependent photon group velocity

$$v_\gamma = \frac{\partial E}{\partial p} \simeq c \left[1 + \sum_{n=1}^{\infty} S_n \frac{n+1}{2} \left(\frac{E}{E_{QG,n}} \right)^n \right]$$

$S_n = \begin{cases} +1, & \text{superluminal} \\ -1, & \text{subluminal} \end{cases}$

$n = \begin{cases} 1, & \text{linear} \\ 2, & \text{quadratic} \end{cases}$

- Difference in the time of flight of two photons $E_h > E_l$

$$\Delta t_n \simeq \pm \frac{n+1}{2} \frac{E_h^n - E_l^n}{H_0 E_{QG}^n} \kappa_n(z)$$

Effect accumulates over astronomical distances

- Optimising for parameter

$$\lambda_n \equiv \frac{\Delta t_n}{\Delta E_n \kappa_n(z)} = \pm \frac{n+1}{2H_0 E_{QG}^n}$$

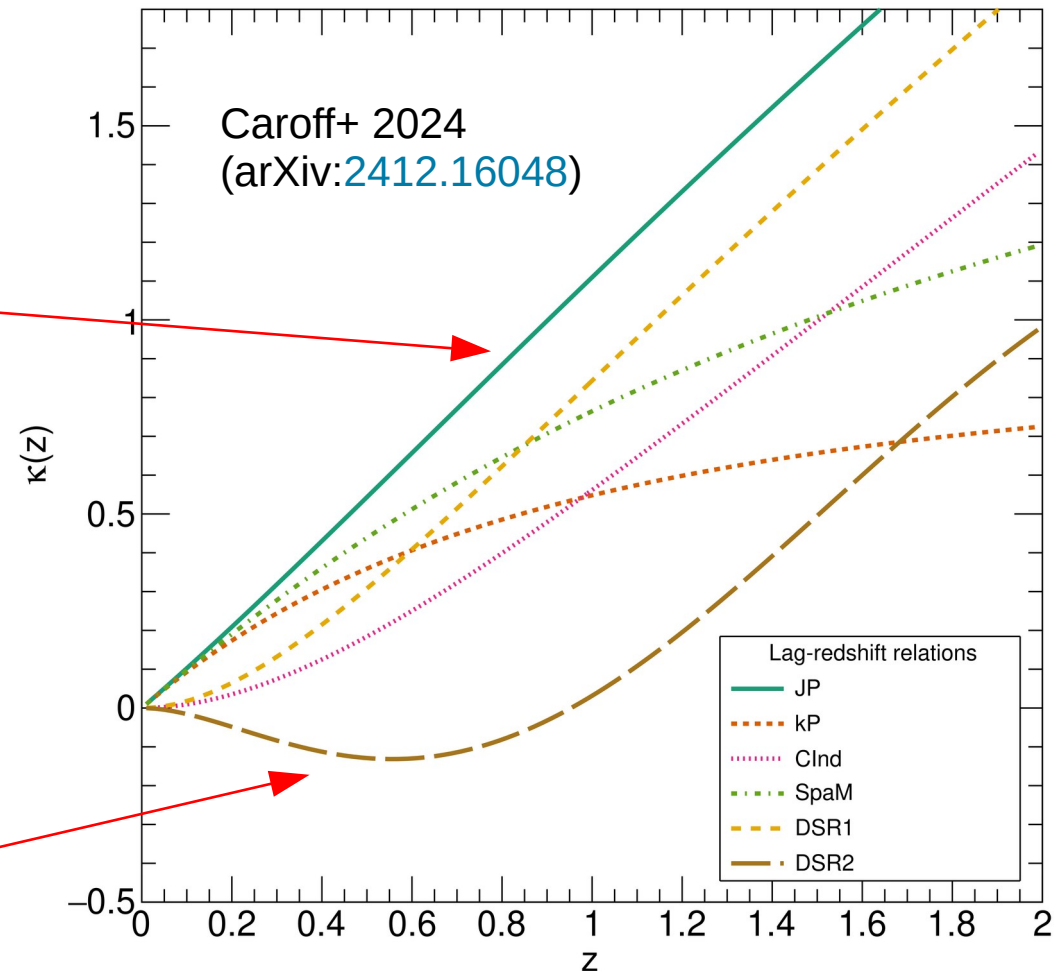
Distance contributions comparison

Standard:

Jacob & Piran (2008,
arXiv: 0712.2170)

$$\kappa_n^{\text{J\&P}}(z) \equiv \int_0^z \frac{(1+z')^n}{\sqrt{\Omega_m (1+z')^3 + \Omega_\Lambda}} dz'$$

Interesting to play with (DSR2)



- **First study** comparing two lag-redshift models
- Additional alternative expressions may be considered in future work

Time of Flight

- Sensitivity to QG energy scale

$E_{\text{QG},1}$	\propto	E_{max}	t_{var}^{-1}	$z_{\text{s}}^{\sim 1}$
$E_{\text{QG},2}$	\propto	E_{max}	$t_{\text{var}}^{-1/2}$	$z_{\text{s}}^{\sim 2/3}$

for JP

Terzić et al. 2021 (arXiv:[2109.09072](https://arxiv.org/abs/2109.09072))

- Challenges:
 - Constraining emission time → **Use fast variability sources**
 - Resolving intrinsic energy-dependent time delays from LIV-induced ones → **Use several different (types of) sources**

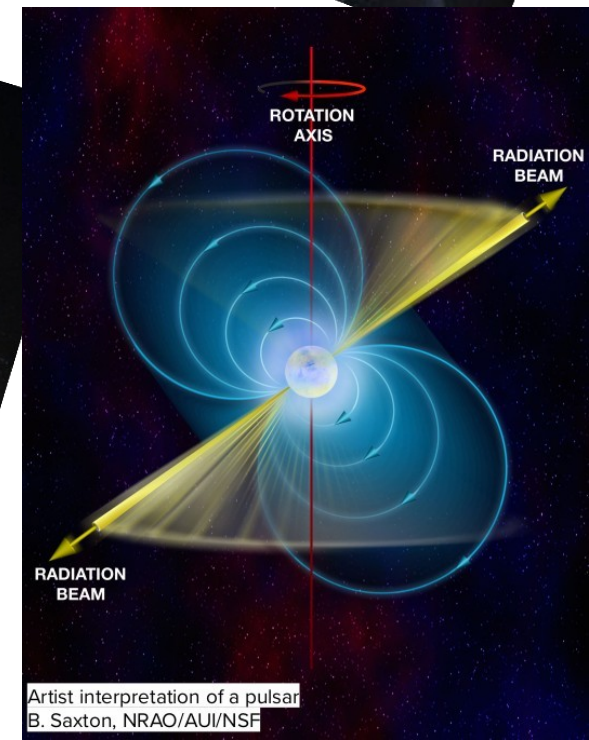
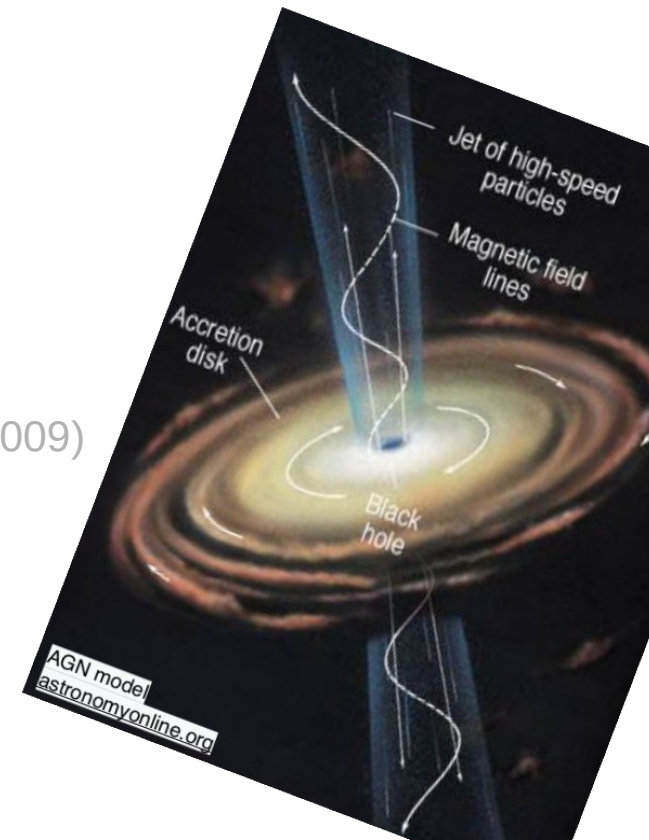
γ -ray LIV WG

- Present collaboration:
H.E.S.S. – LST – MAGIC – VERITAS
- Energy range: ~ 20 GeV – 100 TeV
- Combining available data
 - Increases statistics
 - Sources at different distances/redshifts
discriminates between different LIV models
 - Different (types of) sources
reduces the impact of intrinsic effects
- Analysis method: Bolmont+ 2022 (arXiv: [2201.02087](https://arxiv.org/abs/2201.02087))



Astrophysical sources

- Active Galactic Nuclei
 - Mrk 501 2005 flare: MAGIC (Albert+ 2008; Martinez & Errando, 2009)
 - PKS 2155-304 2006 flare: H.E.S.S. (Aharonian+ 2008; Abramowski+ 2011)
 - PG 1553+113 2012 flare: H.E.S.S. (Abramowski+ 2015)
 - Mrk 421 2014 flare: MAGIC (Abe+ 2024)
 - 1ES 1959+650 2012 flare: VERITAS
 - BL Lac 2020 – 2021 flares: CTAO-LST
- Pulsars
 - Crab: MAGIC (Ahnen+ 2017)
 - Vela: H.E.S.S. (Chrétien+ 2015)
- Gamma-ray Bursts
 - GRB 190114C: MAGIC (Acciari+ 2020)



Results

- Using **unbinned maximum likelihood** approach
- First results based on:
BL Lac (CTAO-LST), PKS 2155-304 (H.E.S.S.),
1ES 1959+650 (VERITAS), GRB 190114C (MAGIC)

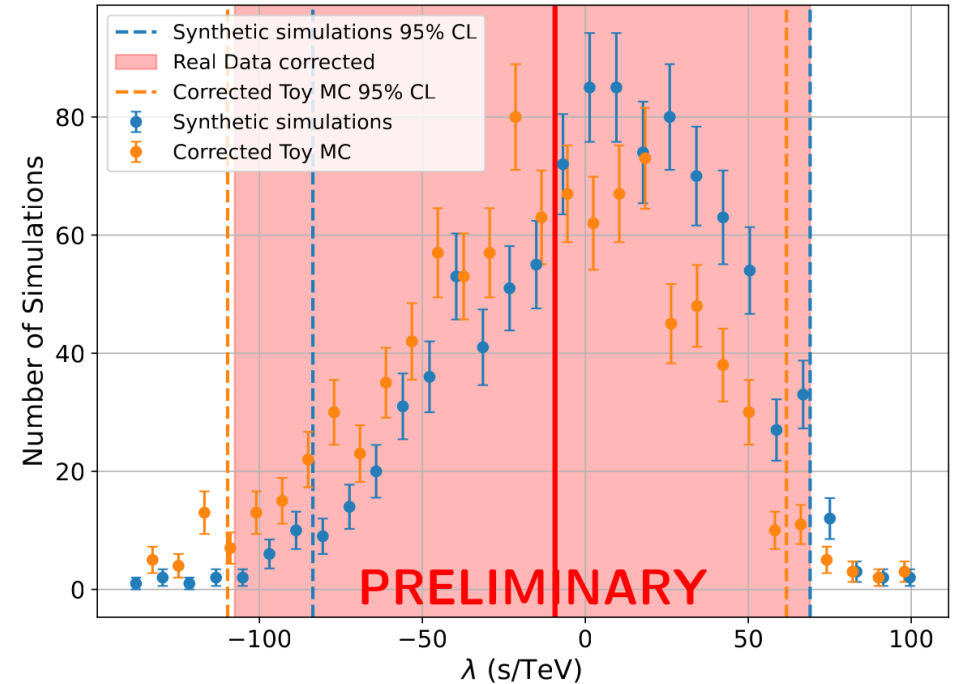
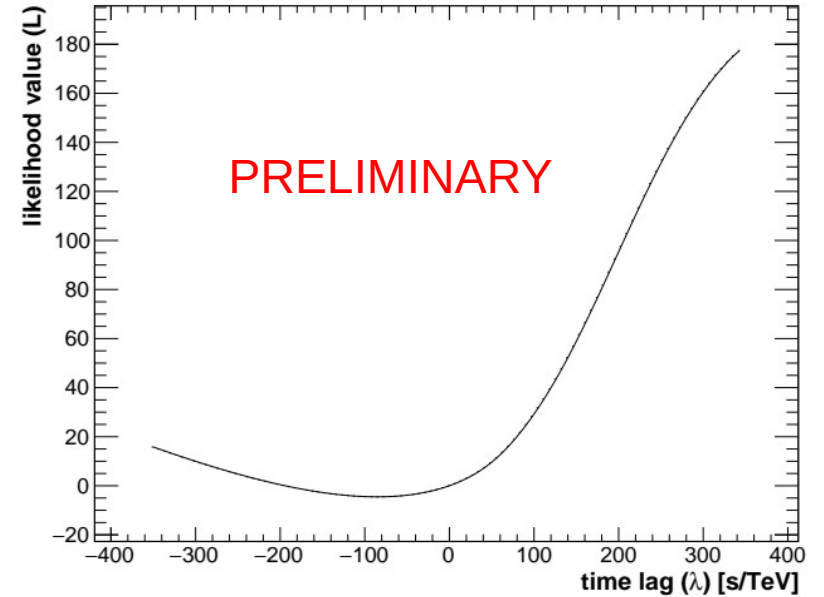
$$L_{comb}(\lambda_n) = \sum_{\text{all sources}} L_S(\lambda_n)$$

- Maximum likelihood for:

$$\lambda_{rec} = -80^{+78}_{-98} \text{ s/TeV}$$

- Bias estimated using bootstrap
Results corrected for bias:

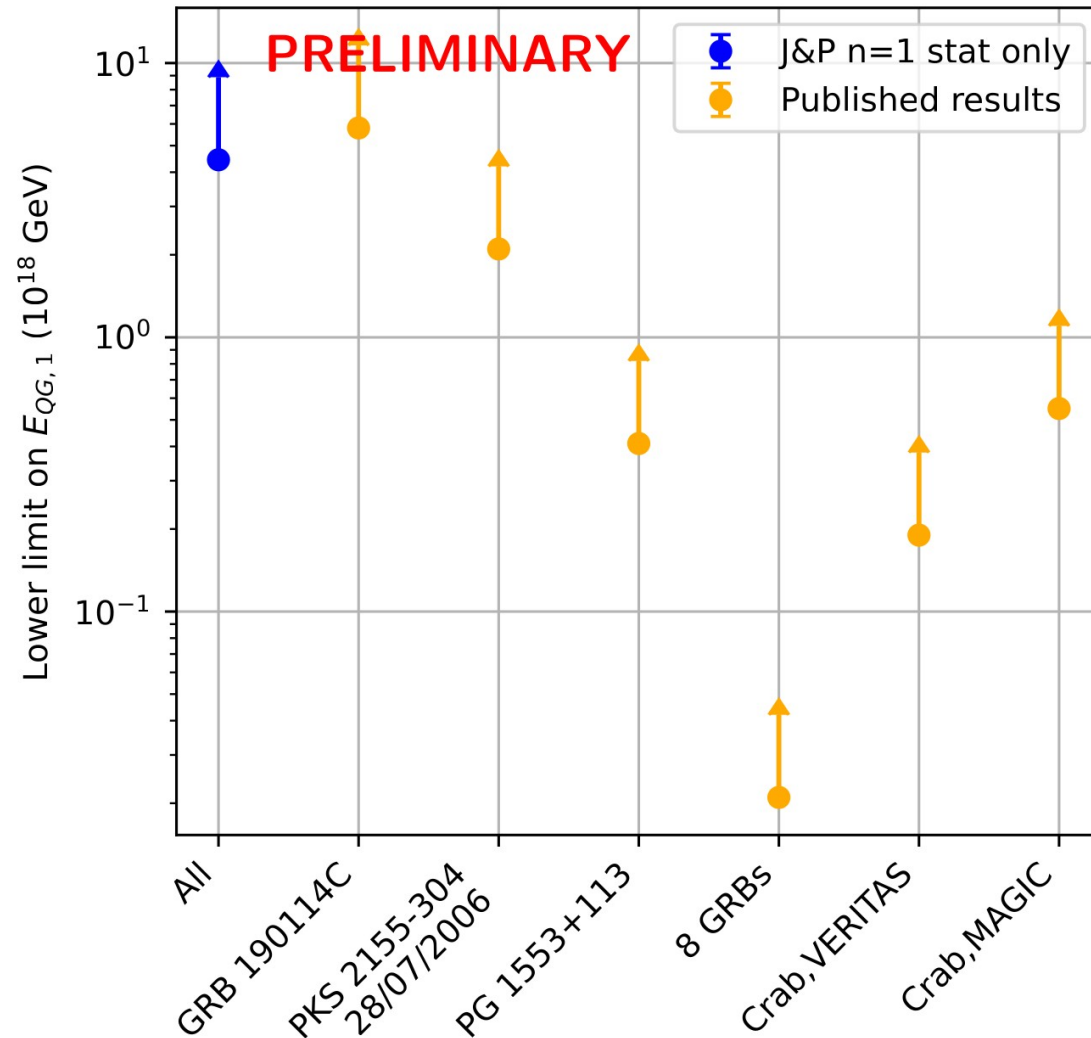
$$\lambda_{rec} = -9.3^{+78}_{-98} \text{ s/TeV}$$



Results

- 2 time-delay models considered:
 - J&P (standard LIV, arXiv:[0712.2170](#))
 - DSR2 designed to cancel the contribution from GRB 190114C (arXiv:[2412.16048](#))

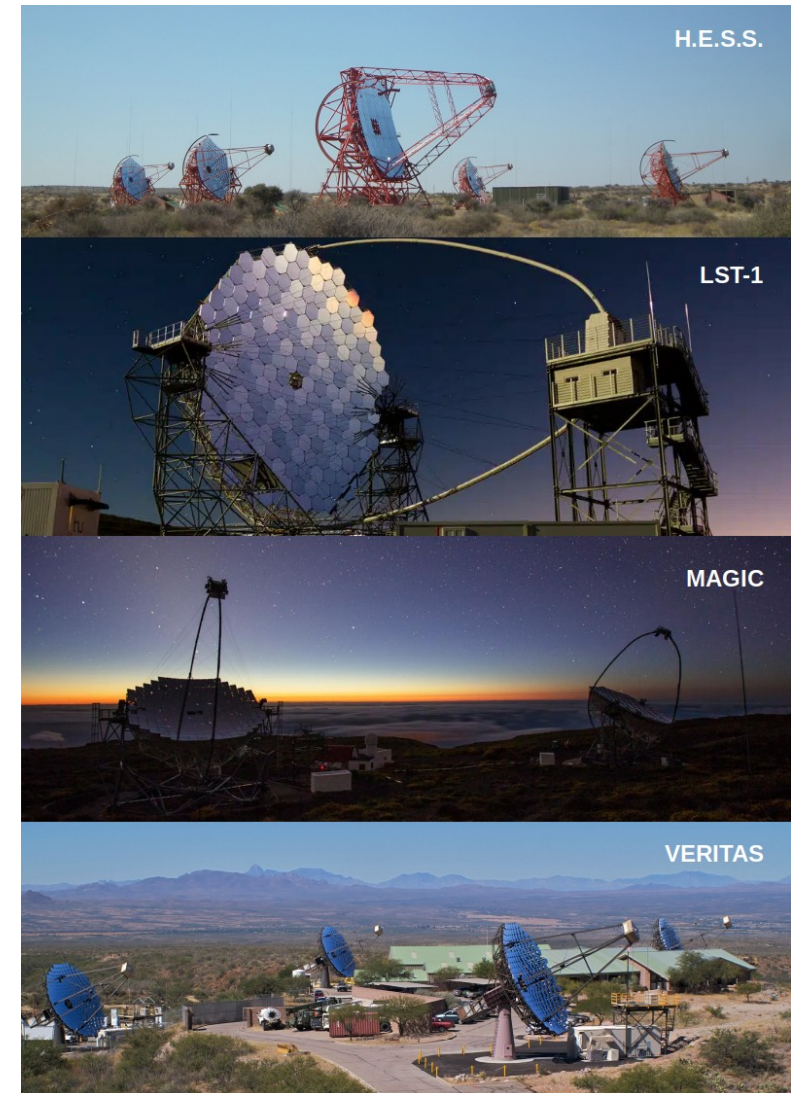
$E_{QG,1}$ [10^{18} GeV]	J&P	DSR2
superluminal	4.44	0.45
subluminal	5.58	0.62

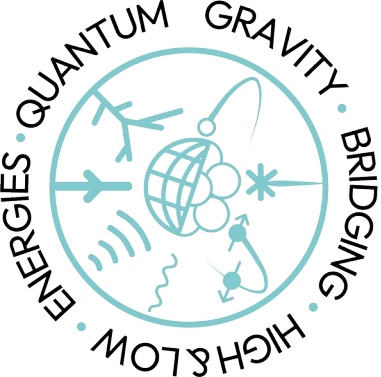


- Systematics not fully taken into account → Final result will be less constraining
- Some sources still to be included in the analysis

Takeaways

- **First joint analysis** from a cooperation of IACTs data for LIV
 - H.E.S.S., CTAO-LST, MAGIC and VERITAS
 - Higher statistics of sources and photons
- **First combination of different types of sources**
 - Different intrinsic characteristics reduce influence of source intrinsic effects
 - Redshift dependency on the LIV effect
- **First comparison of different distance models**
- Instrument Response Functions
 - Vary for each source and for each instrument
 - Fully taken into account





BridgeQG



- COST Action CA23130: <https://www.cost.eu/actions/CA23130/>
Bridging high and low energies in search of quantum gravity (BridgeQG)

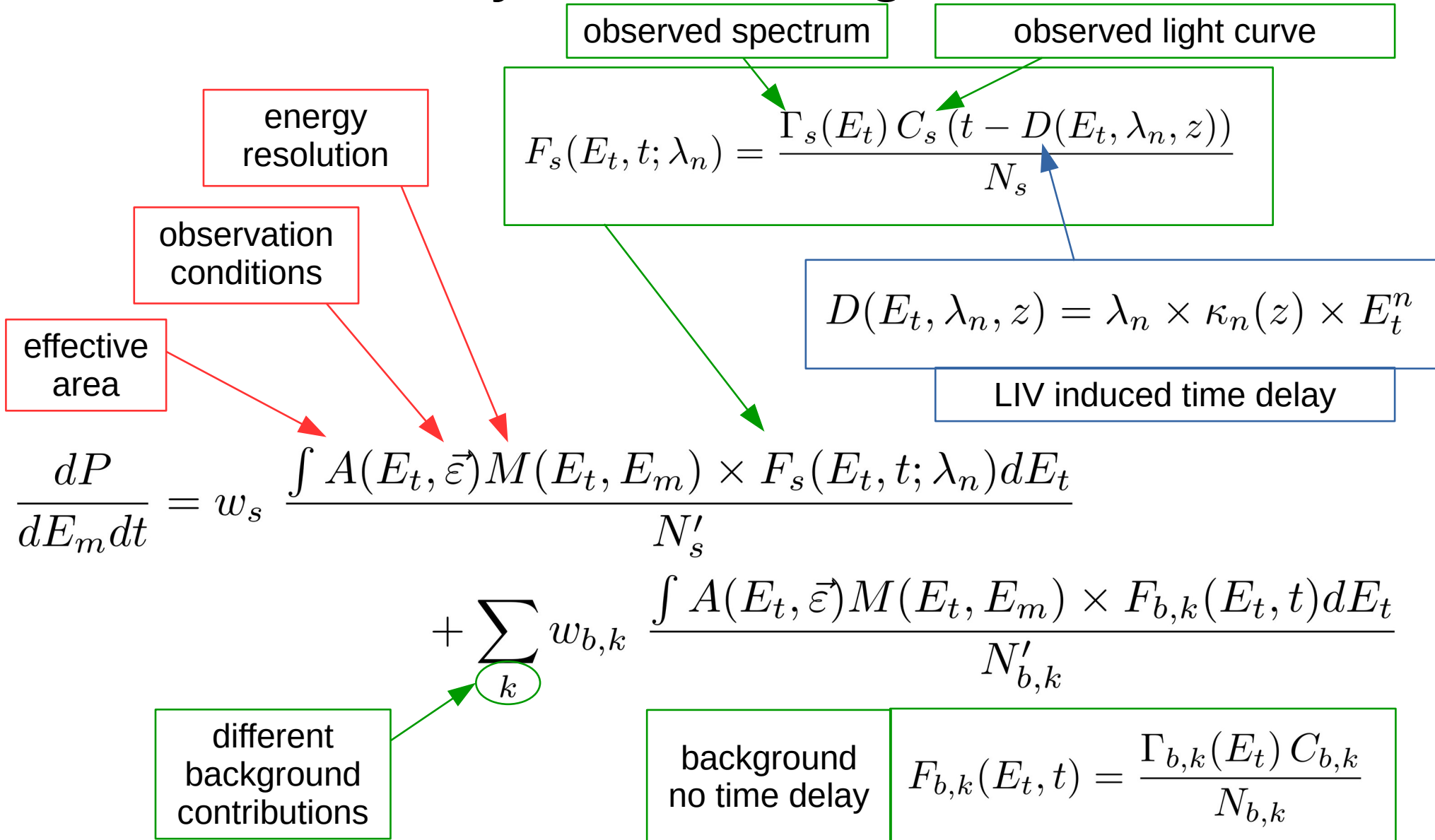
Working Groups' Structure

WG	Working Group	Leader	Vice Leader
1	High-energy quantum gravity theory	Dr Christian Pfeifer	Prof Alessia Platania
2	High-energy quantum gravity experiment	Dr Tomislav Terzić	Dr Alba Domi
3	Low-energy gravitational effects in quantum systems	Dr Lin-Qing Chen	Dr Thomas Galley
4	Low-energy high-precision experiment	Dr Matteo Fadel	Dr Catalina Oana Curceanu
5	Connection between low-energy and high-energy QG	Dr Flavio Mercati	Dr Giacomo Rosati
6	Dissemination and Diversity	Dr Jelena Strišković	Dr Denitsa Staicova

Discover More

Back-up

Likelihood analysis – for single observation



Likelihood analysis – combining observations

- Single observation

$$L_S(\lambda_n) = - \sum_i \log \left(\frac{dP}{dE_m dt}(E_{m,i}, t_i); \lambda_n \right)$$

- Combining observations

$$L_{comb}(\lambda_n) = \sum_{\text{all sources}} L_S(\lambda_n)$$

- Optimising for parameter

$$\lambda_n \equiv \frac{\Delta t_n}{\Delta E_n \kappa_n(z)} = \pm \frac{n+1}{2H_0 E_{QG}^n}$$

Systematics

Table A1. Summary of systematic uncertainties for all sources and combinations simulated for the J&P case.

Source	Correction order	Template statistics (s.TeV ⁻ⁿ)	Energy scale (s.TeV ⁻ⁿ)	Background normalization (s.TeV ⁻ⁿ)	Uncertainty on power law index (s.TeV ⁻ⁿ)	Distance/redshift uncertainty (s.TeV ⁻ⁿ)	Reconstruction uncertainty (s.TeV ⁻ⁿ)	All syst. combined (s.TeV ⁻ⁿ)
GRB 190114C	$n = 1$	17.8	6.9	8.0	9.4	< 7.7	3.0	25.6
	$n = 2$	9.4	12.4	1.7	15.4	< 9	4.2	24.1
PKS 2155-304	$n = 1$	101	11.7	< 20	< 22	17.8	< 3.3	107
	$n = 2$	21.8	19.3	0.7	8.1	12.0	< 2.2	37.4
Mrk 501	$n = 1$	155	56	< 51	49	1.	< 8.5	197
	$n = 2$	11.2	18.3	< 10.3	9.3	0.19	< 1.6	28.8
PG1553+113	$n = 1$	631	150	324	< 361	112	< 64	727
	$n = 2$	916	638	537	< 552	338	< 112	1282
Crab V	$n = 1$	897	137	< 73	142	145	< 25	1135
	$n = 2$	1141	410	< 264	694	265	< 174	1820
Crab M	$n = 1$	371	66	7	23	74	< 11	416
	$n = 2$	167	64.5	61	24	48	< 72	190
Vela	$n = 1$	1.36×10^4	1.03×10^4	0.46×10^4	$< 1.3 \times 10^4$	1.30×10^3	$< 5.87 \times 10^3$	2.28×10^4
	$n = 2$	1.0×10^5	2.05×10^5	0.48×10^5	$< 1.5 \times 10^5$	1.57×10^5	$< 0.95 \times 10^5$	3.05×10^5
Crab (M+V)	$n = 1$	357	49	< 56	32	61	< 32	398
	$n = 2$	161	59	45	59	38	< 83	197
PSR	$n = 1$	355	52	< 58	38	58	< 11	394
	$n = 2$	90	71	49	24	62	< 55	138
AGN	$n = 1$	89.5	12	< 15	3.7	15.8	< 2.9	94.9
	$n = 2$	10.1	11.1	< 6	6.2	3.4	< 1.3	19.7
AGN+PSR	$n = 1$	85	11	< 18	5	15	< 2.9	91
	$n = 2$	9.6	10.9	< 8	5.9	4.5	< 1.1	17.8
GRB+AGN	$n = 1$	17.8	5.8	6.8	8.3	1.4	3.3	24.5
	$n = 2$	6.8	7.8	< 6.6	9.0	1.7	1.4	16.2
GRB+PSR	$n = 1$	17.5	6.7	7.9	9.1	1.0	3.2	24.9
	$n = 2$	8.1	11.3	1.6	12.7	2.8	< 1.1	19.4
All	$n = 1$	18.0	5.8	6.7	8.2	1.5	4.1	24.8
	$n = 2$	7.5	7.7	< 6.2	8.2	2.4	4.8	16.4