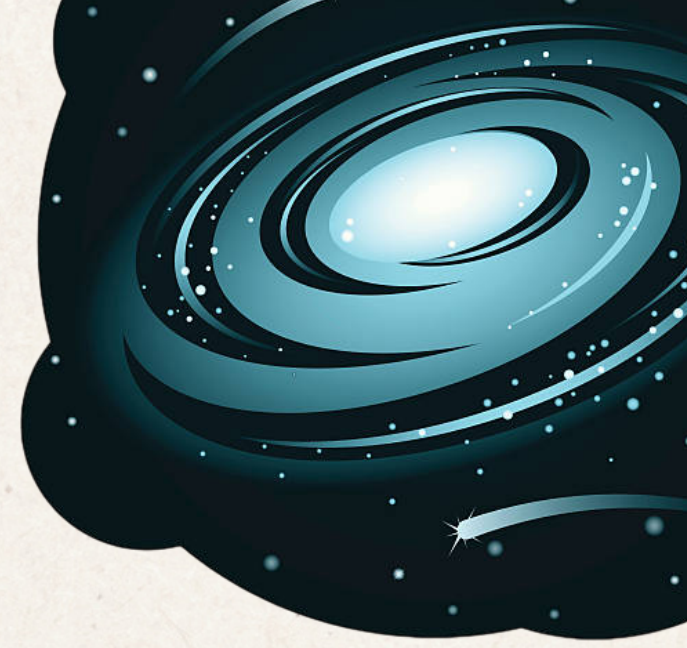


Minimal Dark Matter

in the sky



Updated Indirect Detection probes for WIMPs

Giulio Marino

(Università di Pisa, INFN)

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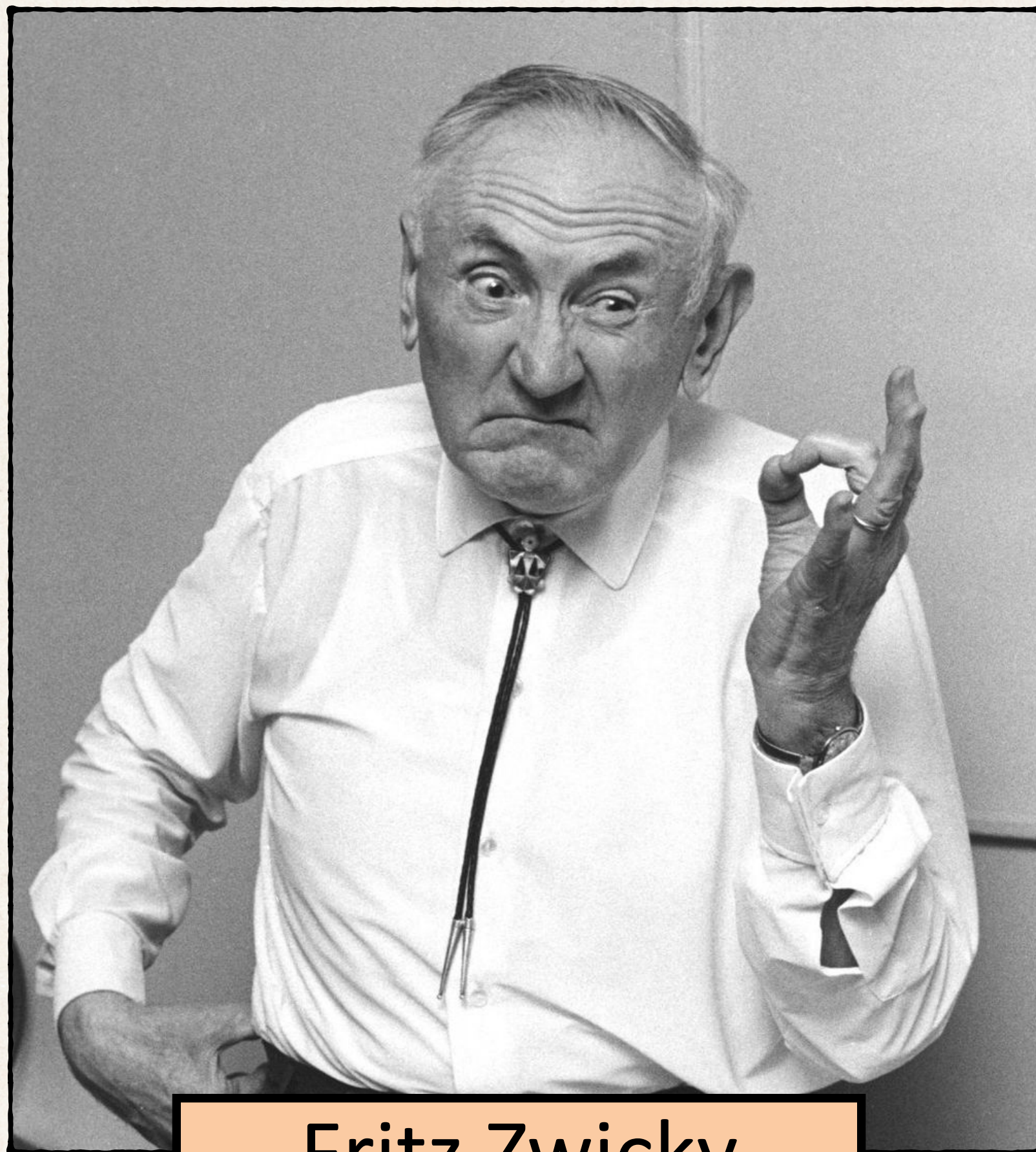
Istituto Nazionale di Fisica Nucleare
Sezione di Pisa



UNIVERSITÀ DI PISA

Dark Matter in a nutshell

1

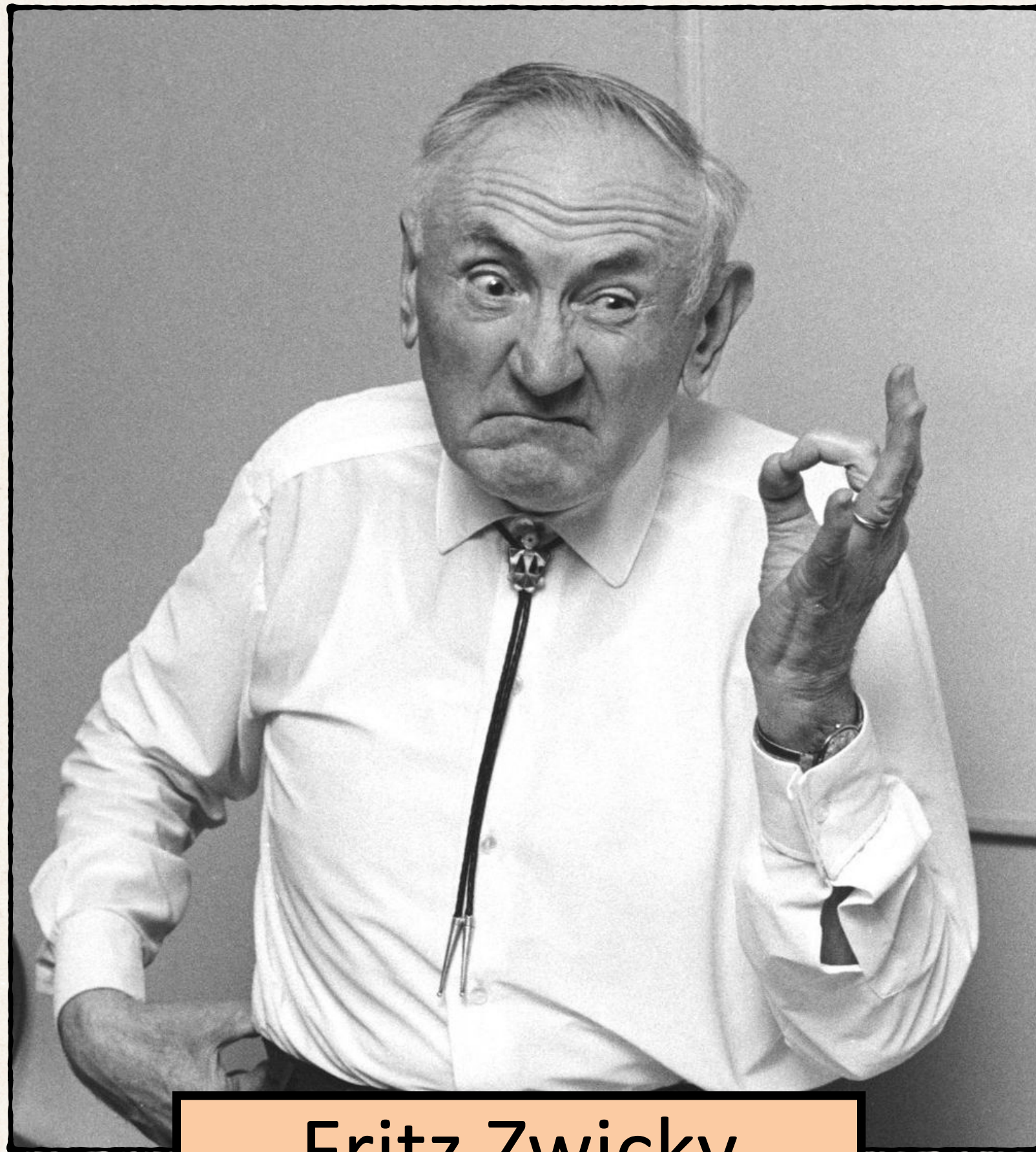


Fritz Zwicky

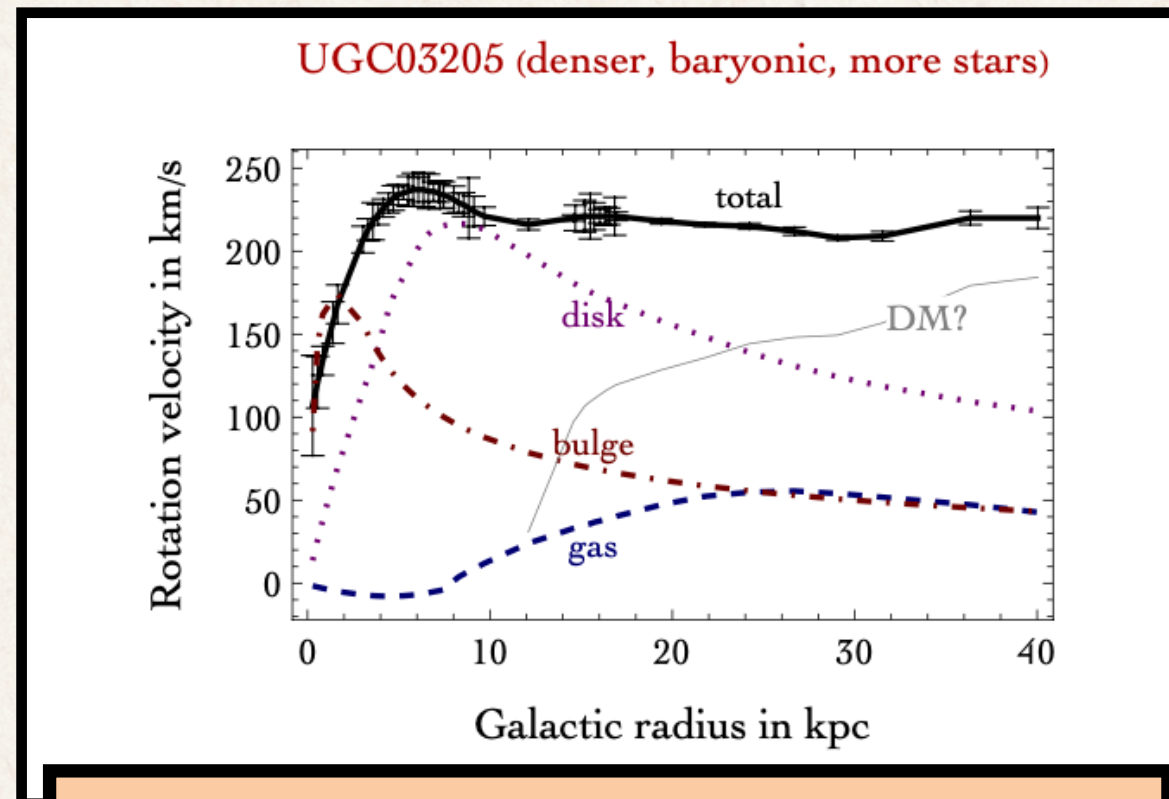
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[1] LSS Image: Galaxies in the local universe as seen by Sloan Digital Sky Survey

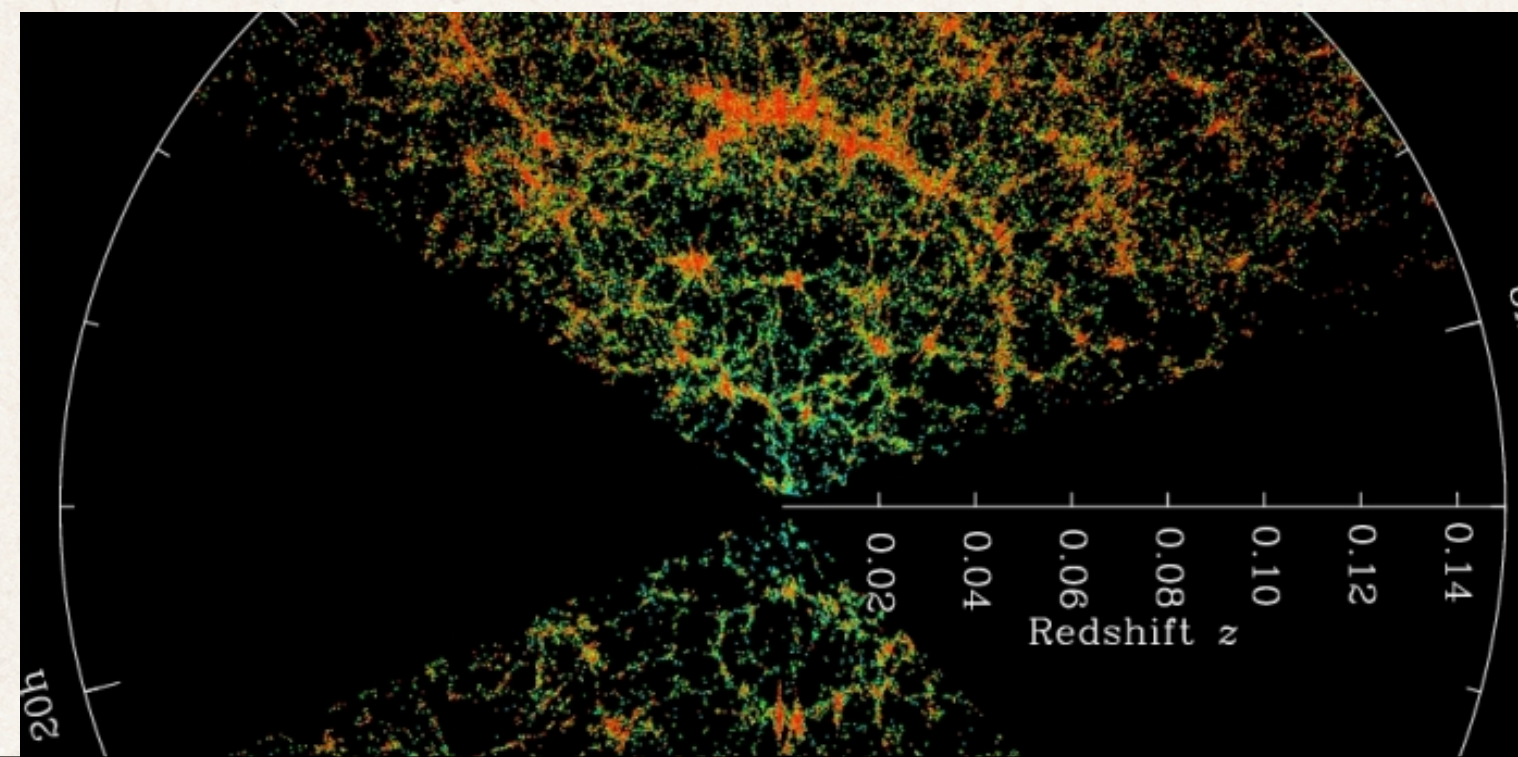
Dark Matter in a nutshell



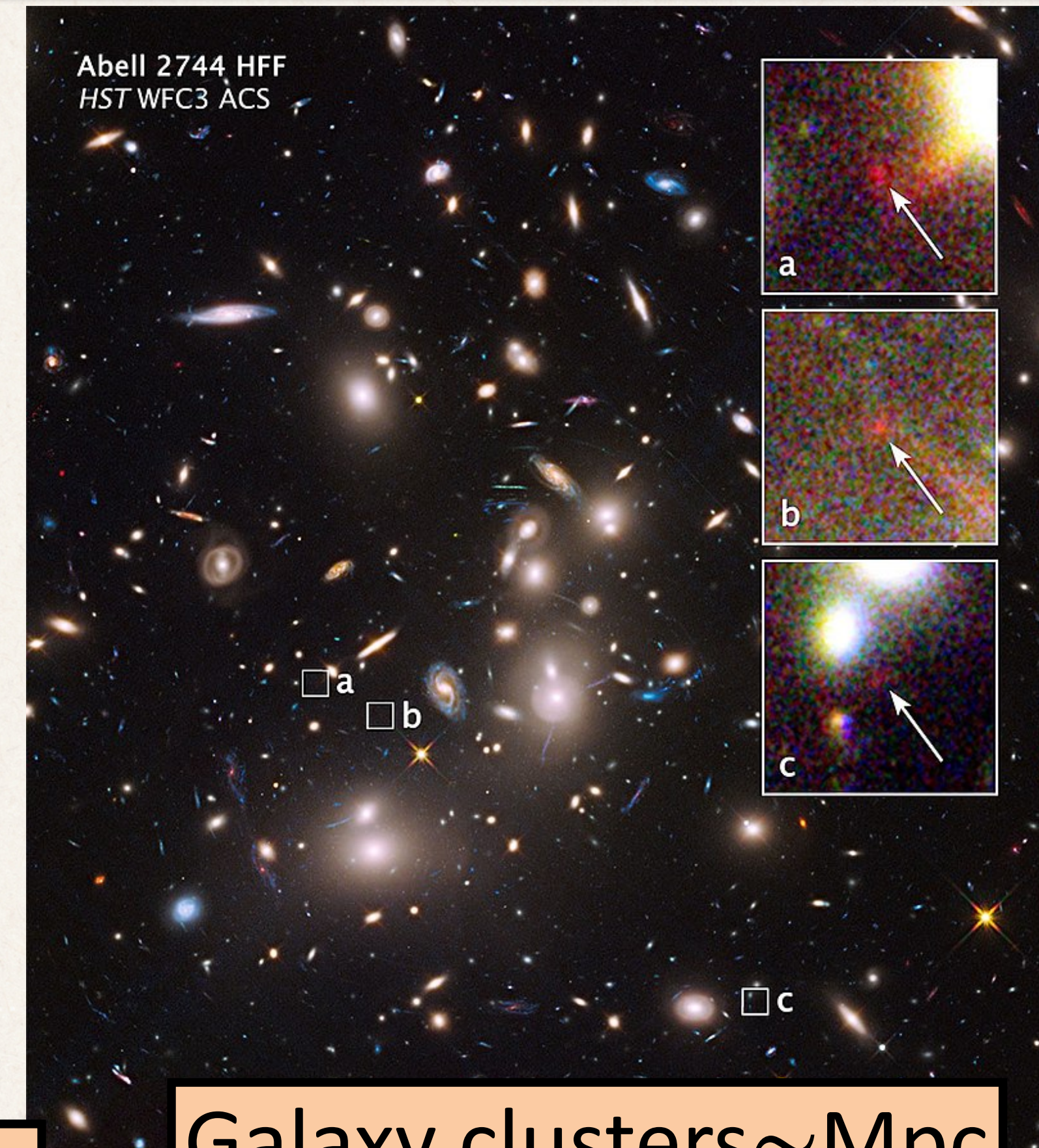
Fritz Zwicky



Rotational curves $\sim$ kpc



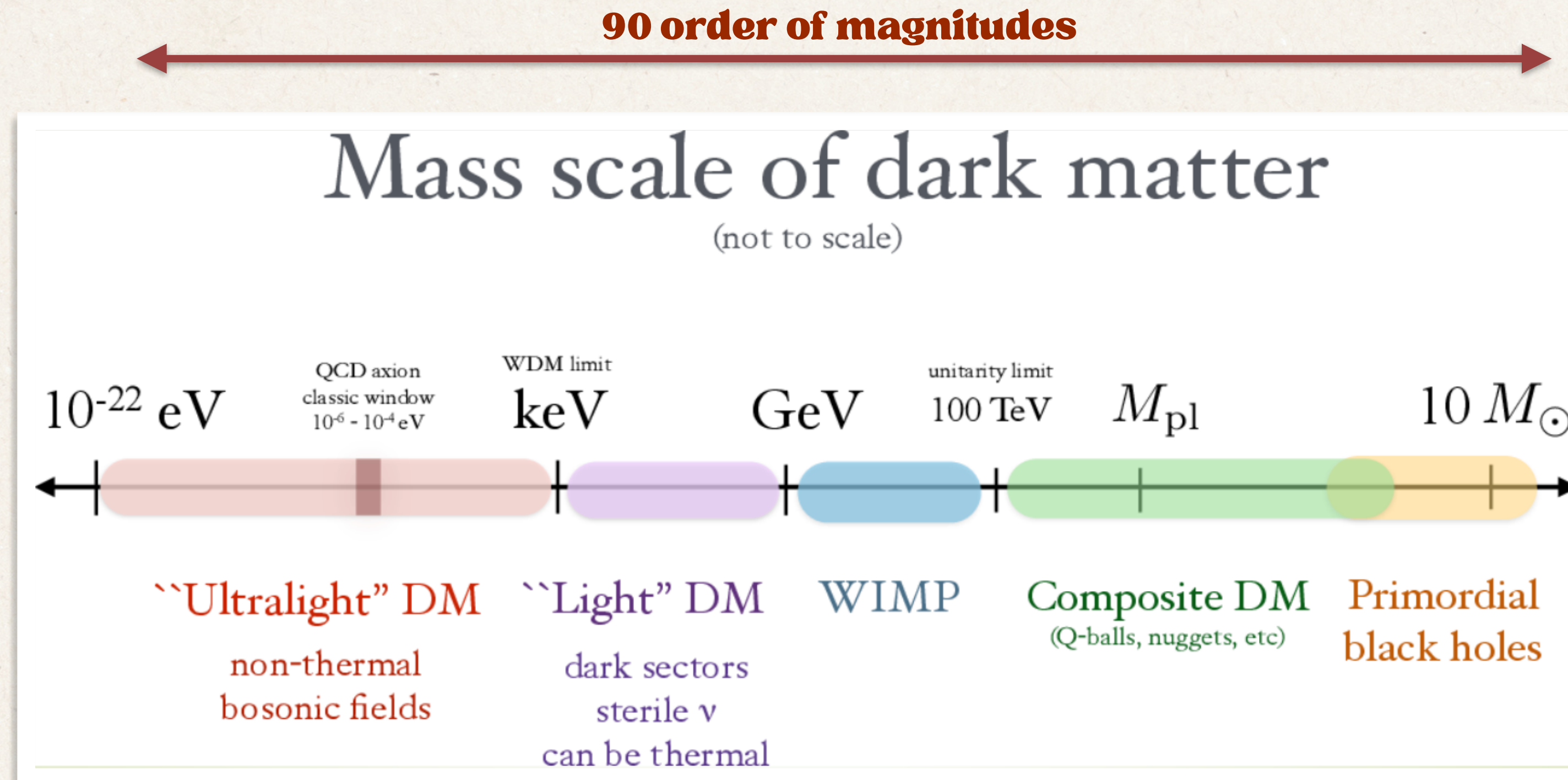
Large Scale Structure $\sim$ The Universe



Galaxy clusters $\sim$ Mpc

Dark Matter in a nutshell

1. **Unknown microphysics?**
2. **Which DM interactions/
Mass?**
3. **Production Mechanism?**

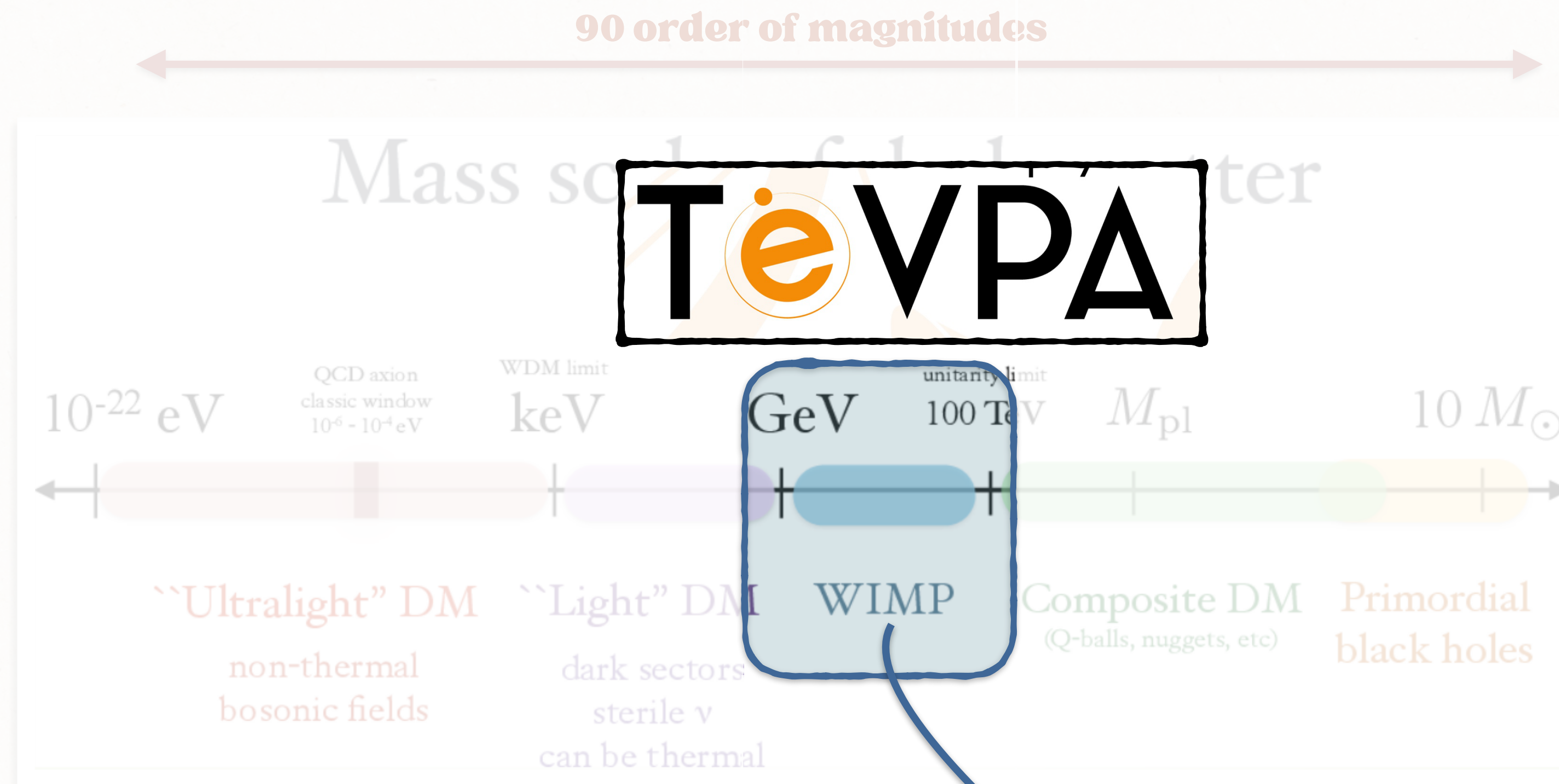


Stable
Non relativistic
Weakly Interacting

Dark Matter in a nutshell

2

1. Unknown microphysics?
2. Which DM interactions/
Mass?
3. Production Mechanism?



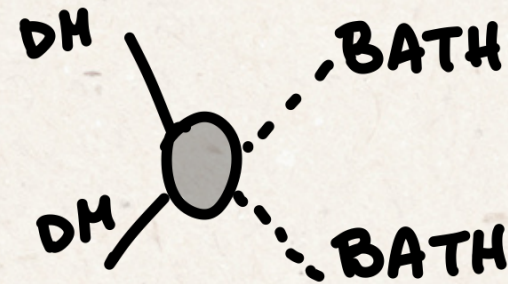
Stable
Non relativistic
Weakly Interacting

MDM in the sky: updated ID probes: 2507.17607
Aghaie, Dondarini, GM, Panci

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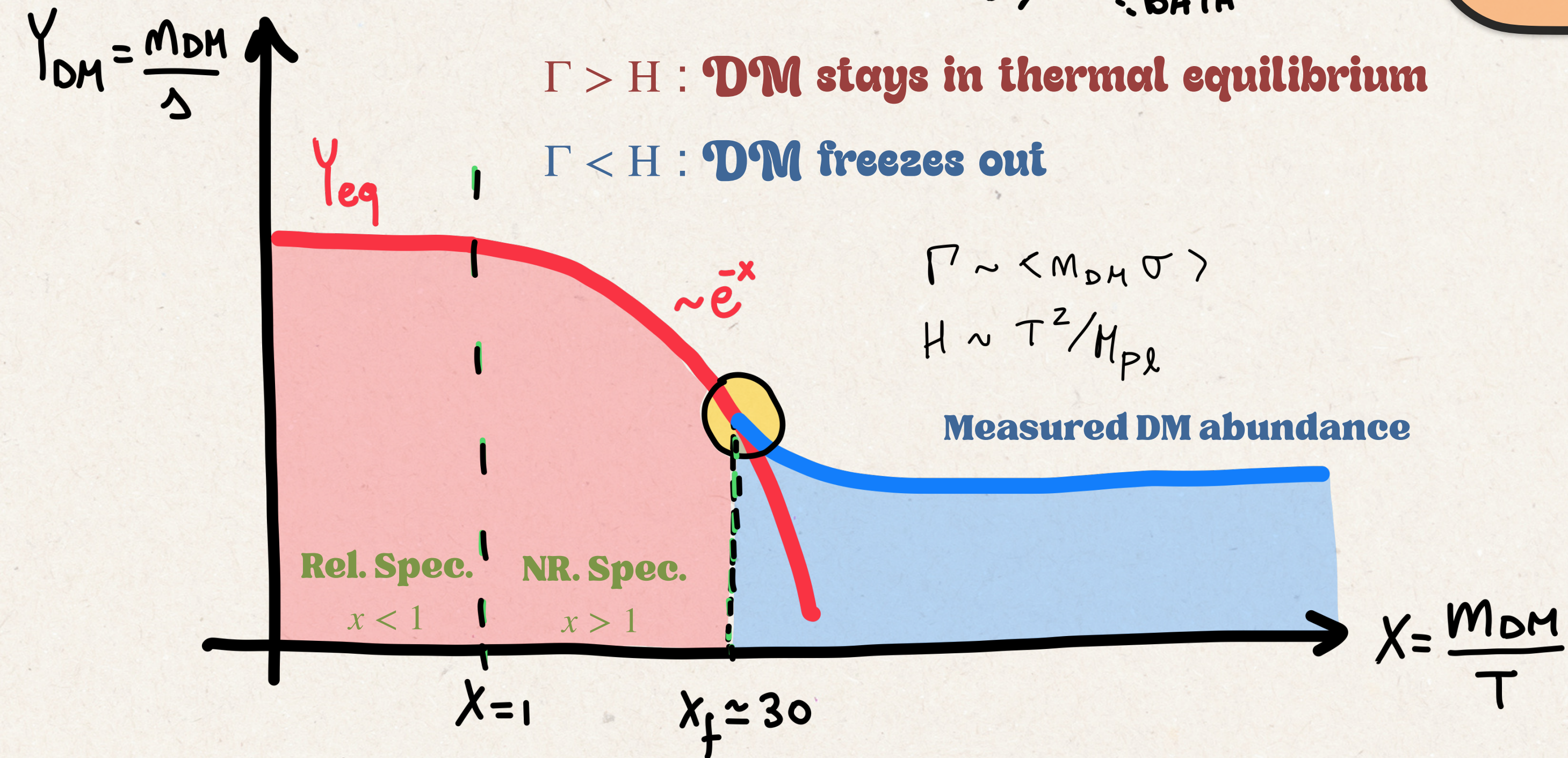
The WIMP Miracle

DM as a Thermal Relic



Thermal freeze-out relies only on one IR parameter

$$\langle \sigma v \rangle \sim 1 \text{ pb} \sim 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$



WIMP MIRACLE:

Weak-scale coupling + TeV scale DM

naturally matches the thermal xsec.

For heavy DM this is a perfect MIRACLE

DM puzzle $\Leftrightarrow$ EW interactions

$$\frac{\Omega_{\text{DM}} h^2}{0.110} = \frac{x_{\text{fo}}}{25} \frac{2.18 \cdot 10^{-26} \text{ cm}^3 \text{ s}^{-1}}{\sigma_0 + 3\sigma_1/x_{\text{fo}}}$$

Minimal Dark Matter

*The Prototypical WIMP **

$$\chi \equiv \mathbf{1}_C, \left\{ \begin{pmatrix} \chi_1 \\ \chi_2 \\ \dots \\ \chi_n \end{pmatrix} \right\} SU(2)_{EW} \text{ and } Y$$

- 1 **Neutral under EM.** DM candidate is χ_0
- 2 **DM Stability.** χ_0 is stable on cosmo scales
- 3 **No coupling to Z-boson.** Avoid DD bounds

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* [1] Minimal Dark Matter: [arXiv:hep-ph/0512090](https://arxiv.org/abs/hep-ph/0512090)
 [2] Cosmology and Astrophysics of Minimal Dark Matter: [arXiv:hep-ph/0706.4071](https://arxiv.org/abs/hep-ph/0706.4071)
 [3] Minimal Dark Matter: Model and results: [arXiv:hep-ph/0903.3381](https://arxiv.org/abs/hep-ph/0903.3381)

Minimal Dark Matter

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- 1 **Neutral under EM.** DM candidate is χ_0
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Real EW representation

one viable possibility

Y=0 and odd n

for $n \gtrsim 5$ DM stability comes from
an accidental $\mathbb{Z}_2$ symmetry

Majorana SU(2)-5plet

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* [1] Minimal Dark Matter: [arXiv:hep-ph/0512090](https://arxiv.org/abs/hep-ph/0512090)
 [2] Cosmology and Astrophysics of Minimal Dark Matter: [arXiv:hep-ph/0706.4071](https://arxiv.org/abs/hep-ph/0706.4071)
 [3] Minimal Dark Matter: Model and results: [arXiv:hep-ph/0903.3381](https://arxiv.org/abs/hep-ph/0903.3381)

Minimal Dark Matter

**We focus on the
smallest accidentally stable MDM multiplet:**

the Majorana $\mathbf{5}$ -plet

Thermal freeze-out
fixes M_χ

DM physics is fully predicted !

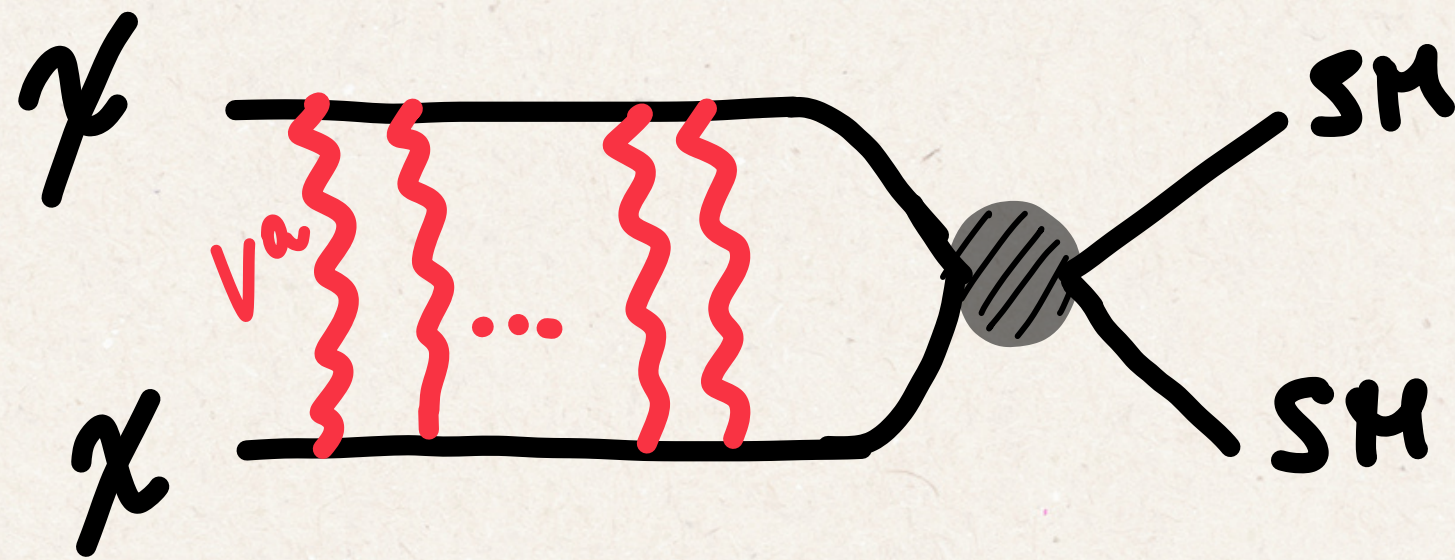
SE and BSF

$$\sigma v_{\text{rel}} = \frac{g_2^4(2n^4 + 17n^2 - 19)}{256\pi g_\chi M_\chi^2} \Rightarrow \text{However this is inaccurate} \rightarrow \text{Non perturbative and Non-relativistic}$$

Thermal mass window

$$M_\chi = 13.7^{+0.6}_{-0.3} \text{ TeV}^*$$

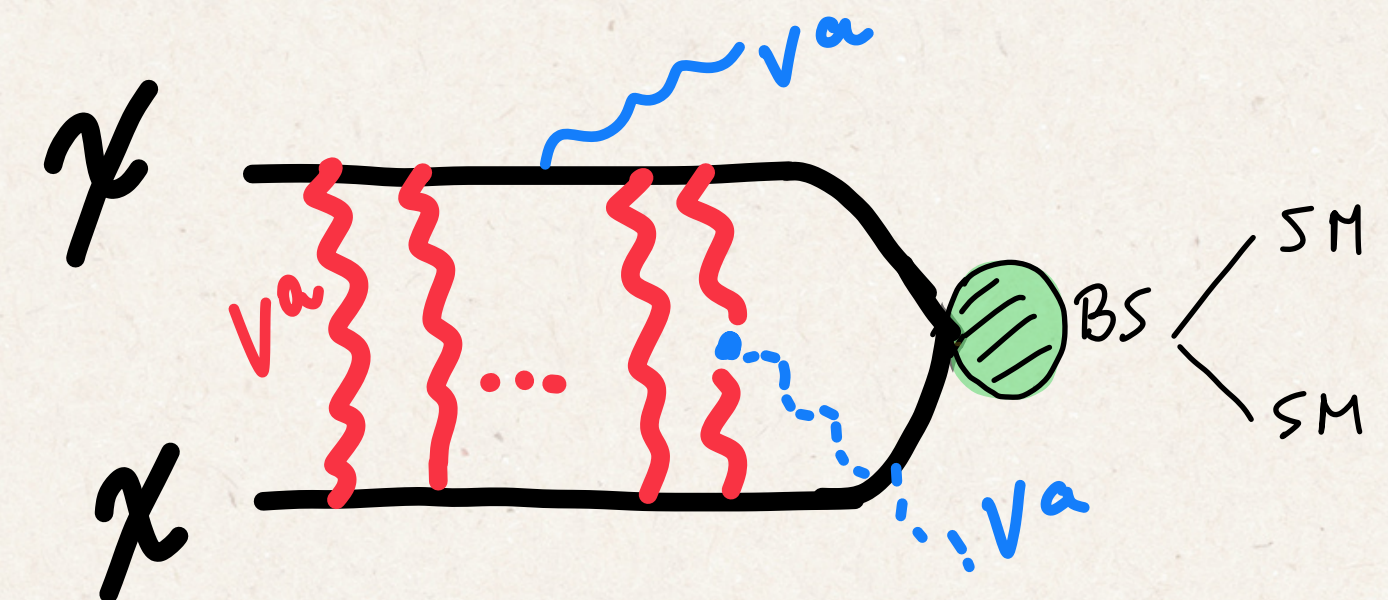
Sommerfeld Enhancement†



Long range effects modify the 2-body initial state W.F.

$$\sigma \rightarrow S \sigma_{\text{pert}}$$

Bound State Formation



$$^1s_3 : E_B \sim 80 \text{ GeV}$$

BS annihilation into SM particles ($f\bar{f}$ and HH^*)

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* [1] NLO electroweak potentials for minimal dark matter and beyond: [arXiv:hep-ph/2108.07285](#)

[2] The Sommerfeld enhancement at NLO and the dark matter unitarity bound: [arXiv:hep-ph/2305.01680](#)

† [3] Non-relativistic pair annihilation of nearly mass degenerate neutralinos and charginos III. Computation of the Sommerfeld enhancements: [arXiv:hep-ph/1411.6924](#)

[4] Capture and Decay of Electroweak WIMPonium: [arXiv:hep-ph/1610.07617](#)

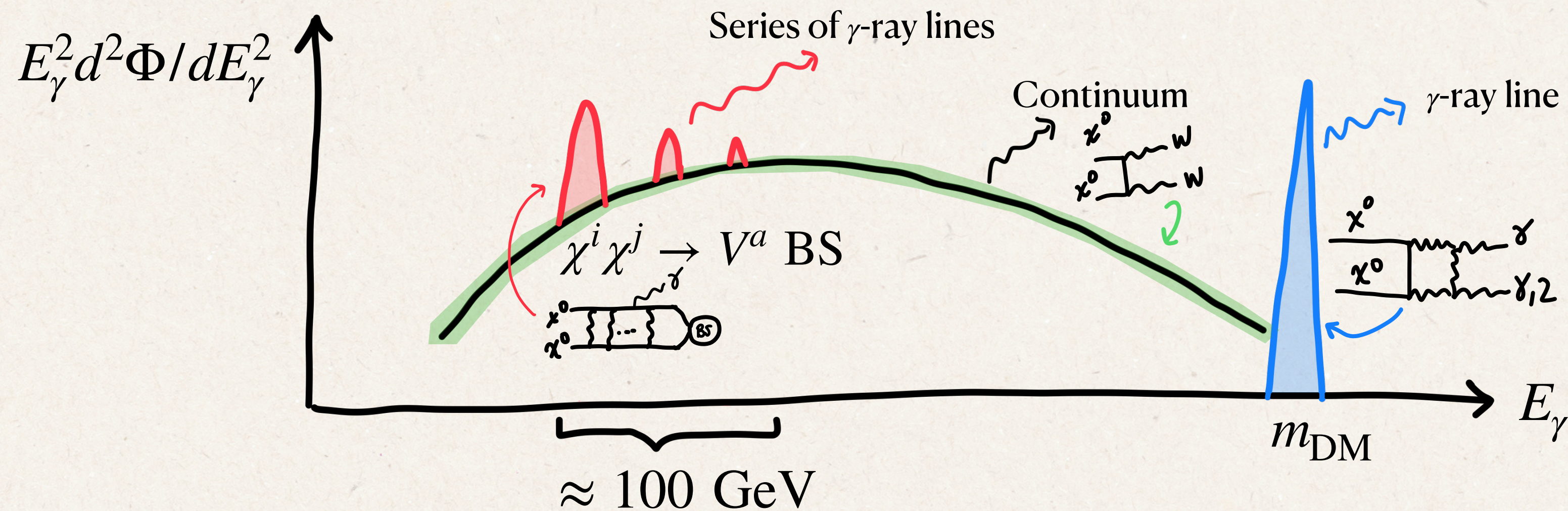
Indirect Detection

Can already offer valuable information!



Typical γ -ray flux

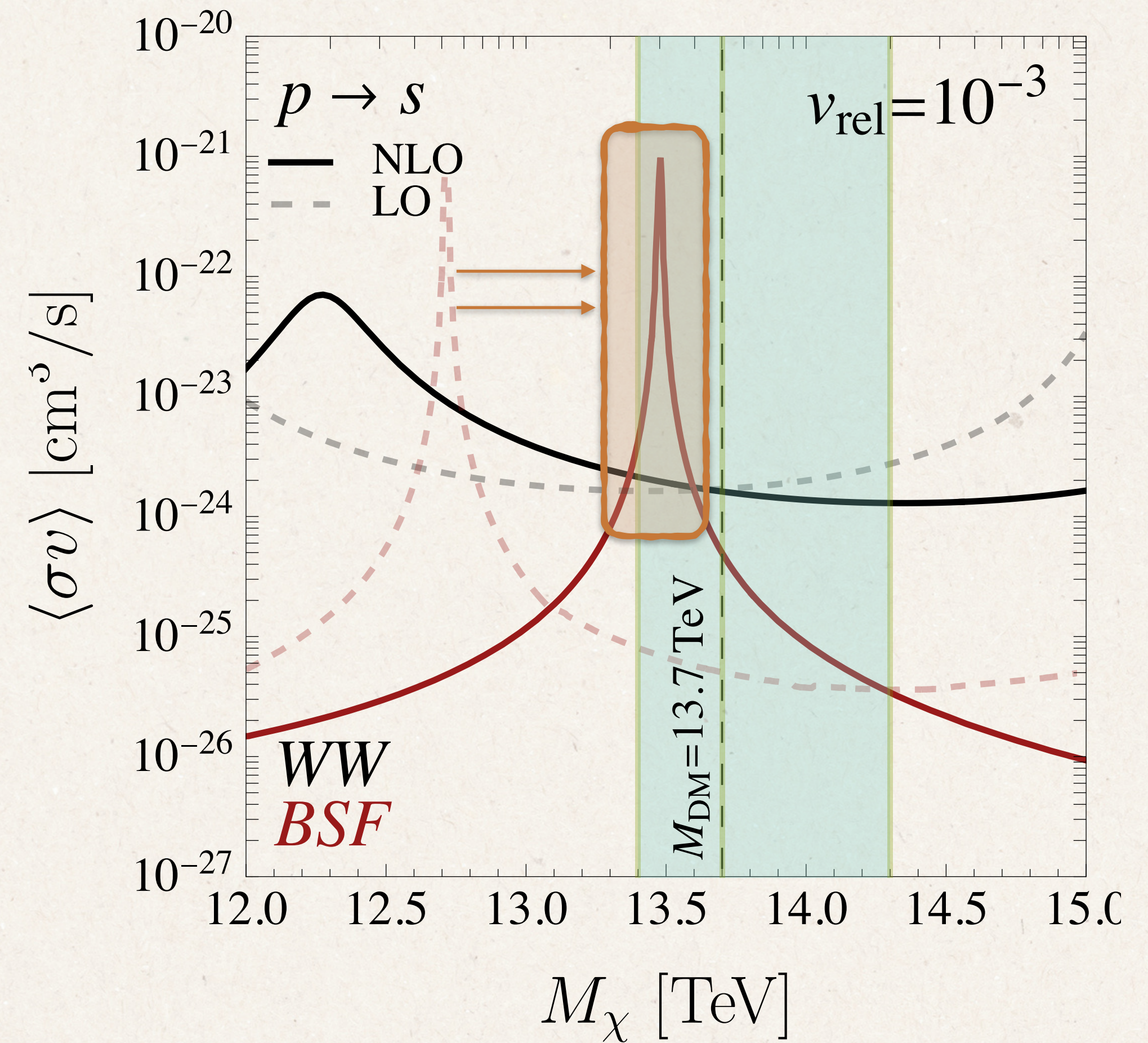
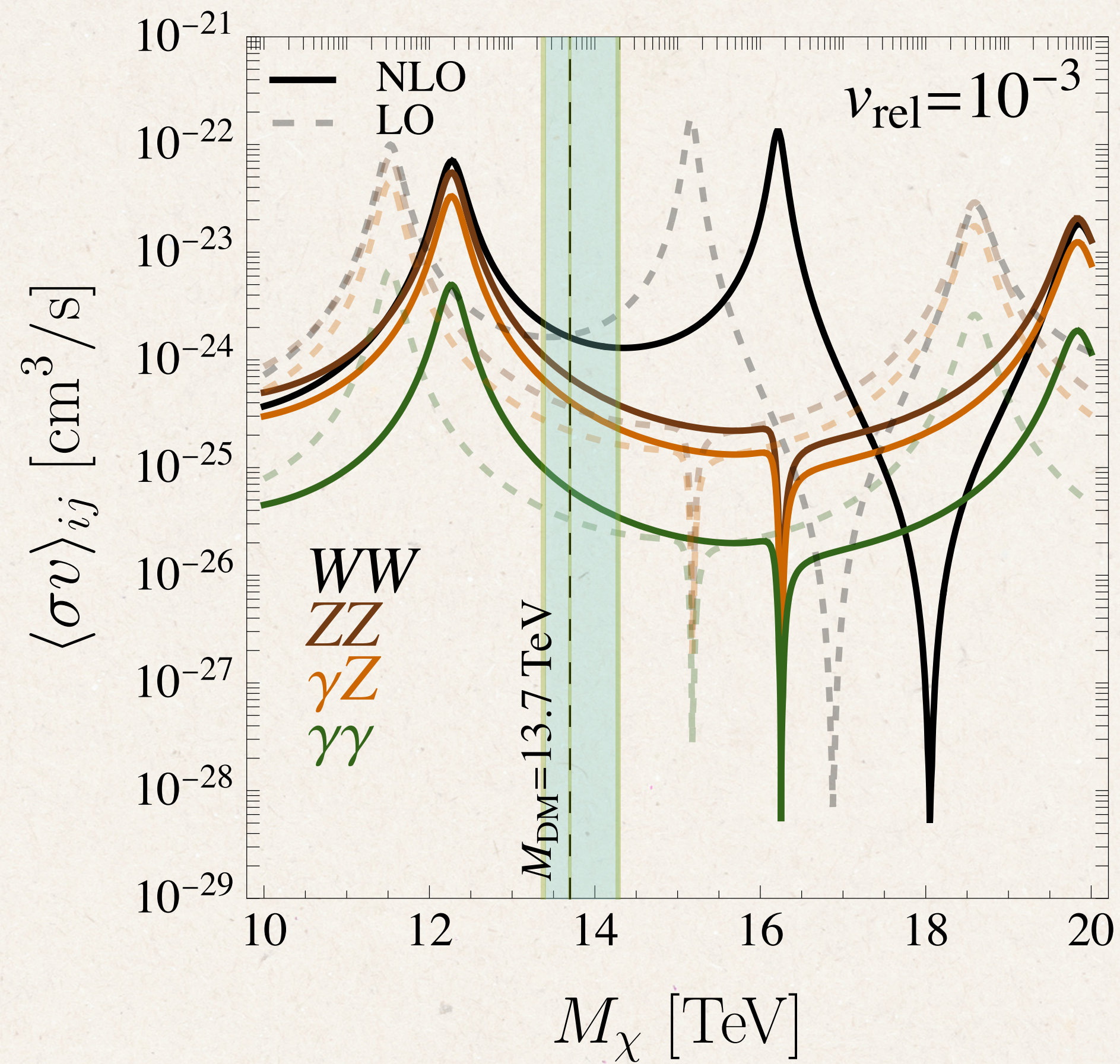
$$\frac{d\Phi}{dE_\gamma d\Omega} = \frac{J(\theta)}{8\pi} \frac{\langle \sigma v \rangle}{M_\chi^2} \frac{d\mathcal{N}}{dE_\gamma}, \quad \text{where } J(\theta) = \int_{\text{l.o.s.}} ds \rho(r(s, \theta))^2,$$



- Continuum:** Decay and hadronization of heavy EW gauge bosons
- γ -ray line:** SE boost the loop-induced annihilation into $\gamma\gamma$ and γZ
- Series of γ -ray lines:** Due to BSF

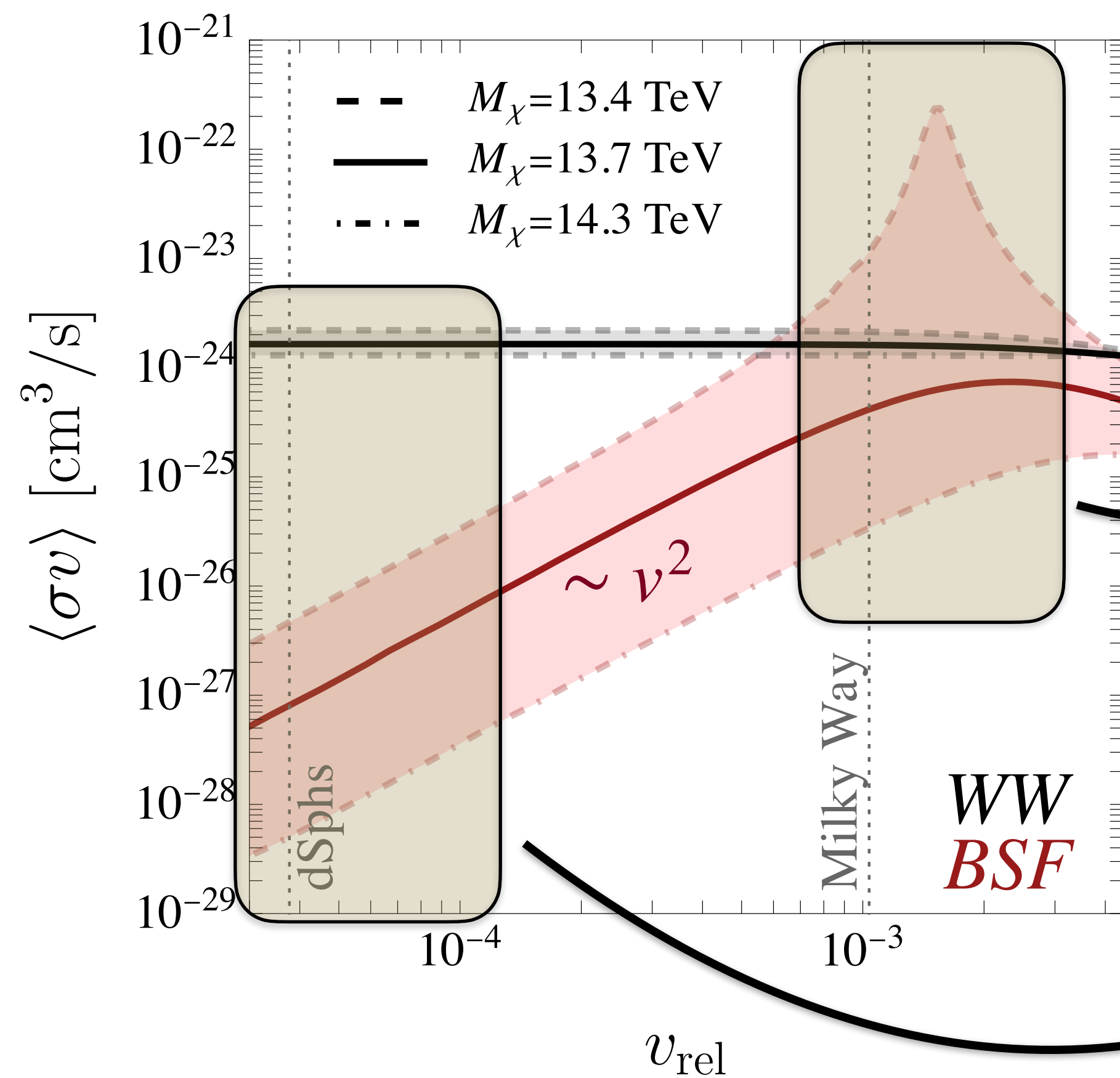
SMOKING GUN: Heavy EW multiplets are like atoms emitting in γ -rays

Annihilation cross sections



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Velocity dependence

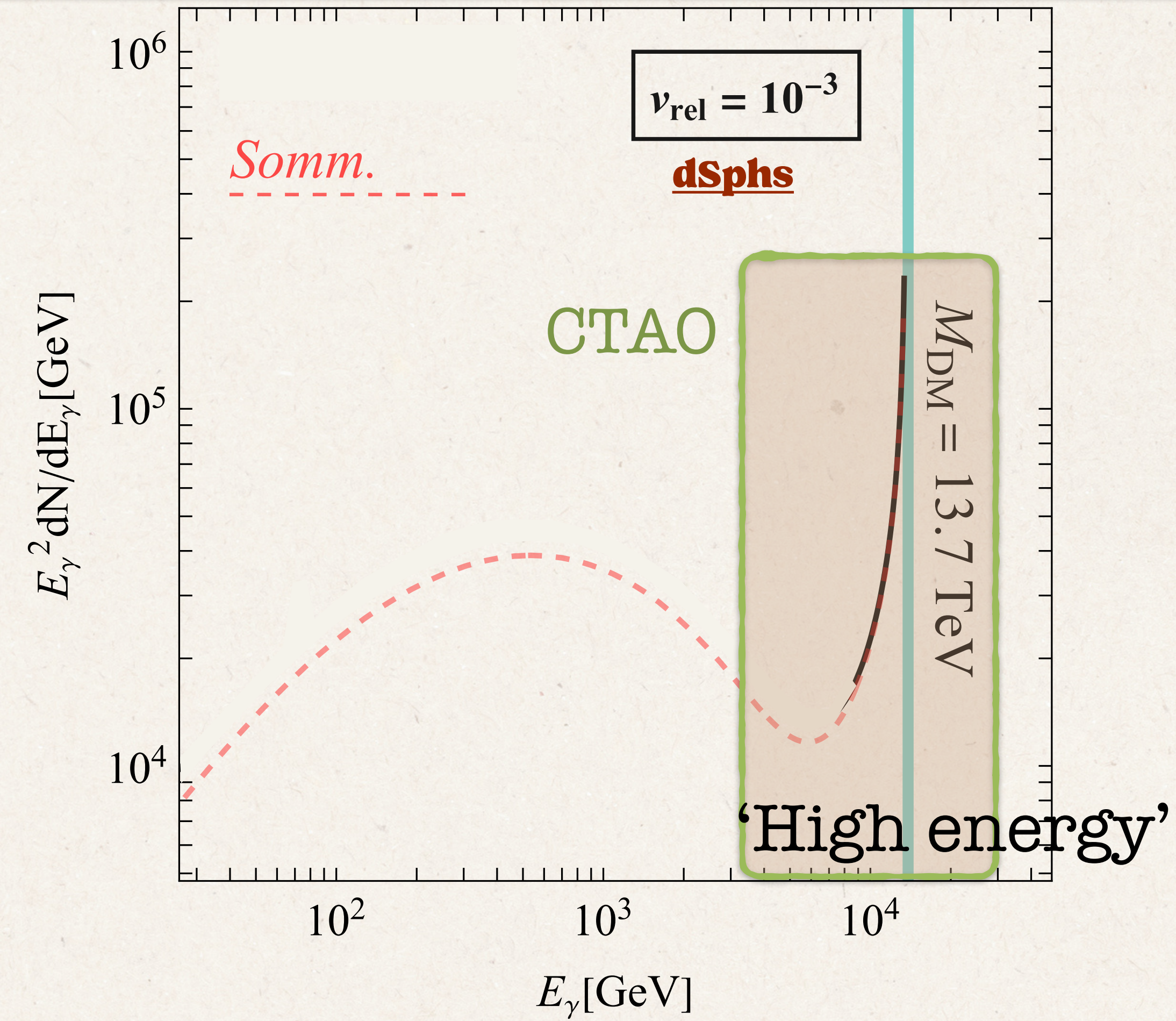
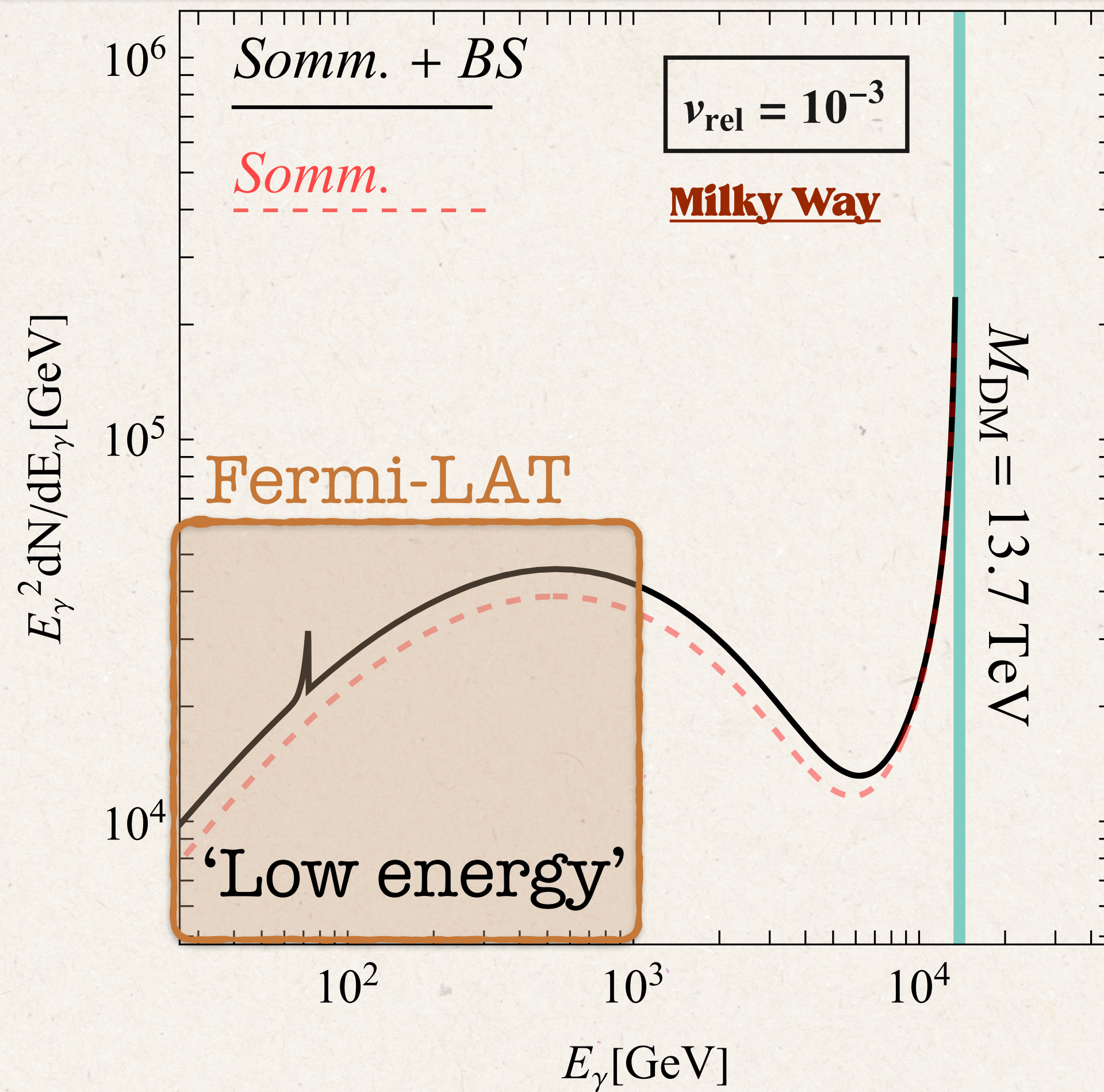


BSF xsec is velocity dependent (p-wave)

Here BSF is dominant

Here SE dominates

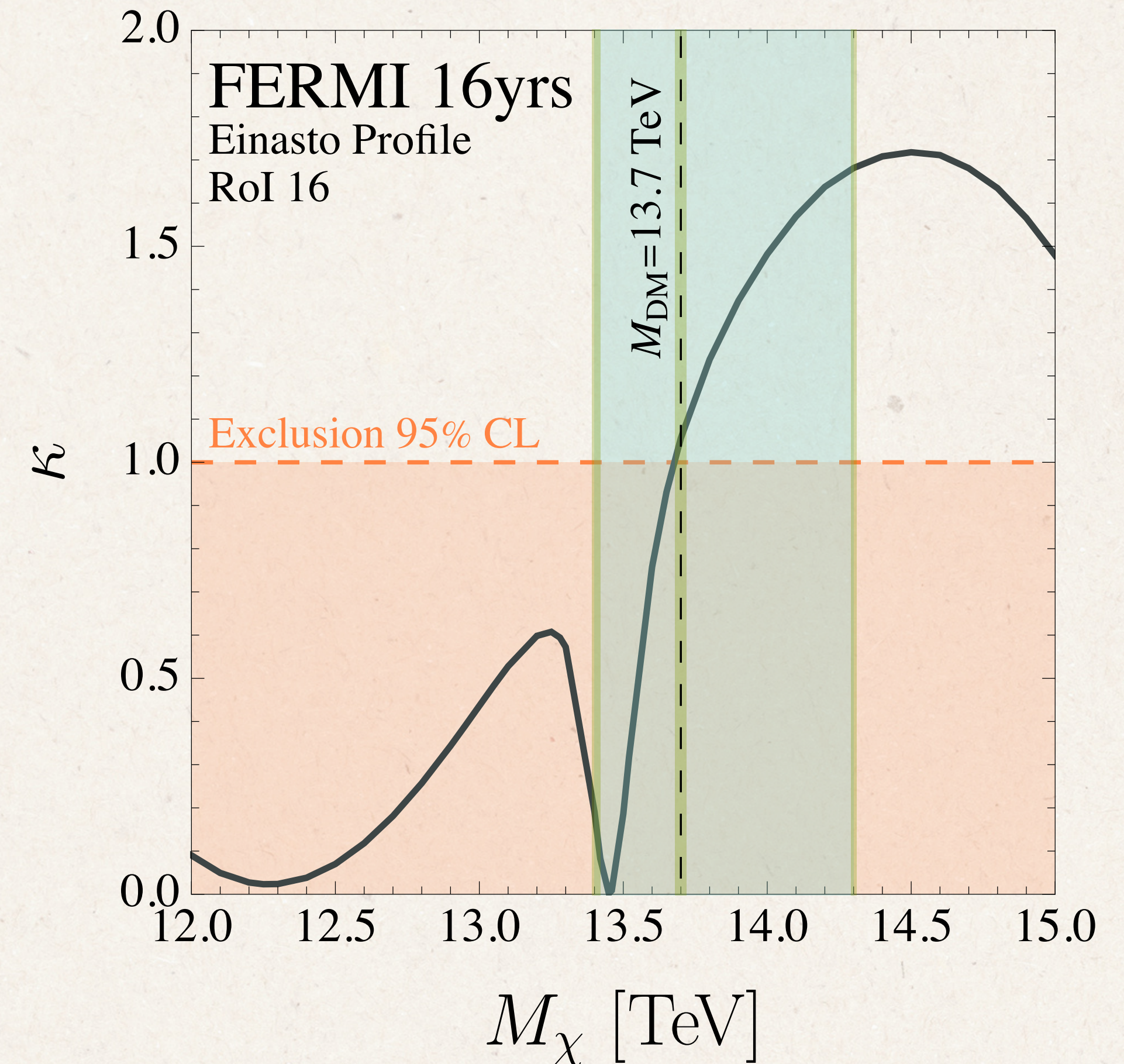
The γ ray spectrum



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- 16 yrs of data + Masking (Galactic plane + sources)
- Energy window $E_\gamma \in [25, 398]$ GeV
- We use the Fermi-LAT template for astro bkg modeling:
 - Galactic diffuse (A_{diff})
 - Isotropic emission (A_{iso})
- No free parameters in the theory: $\langle \sigma v \rangle \rightarrow \kappa \langle \sigma v \rangle$

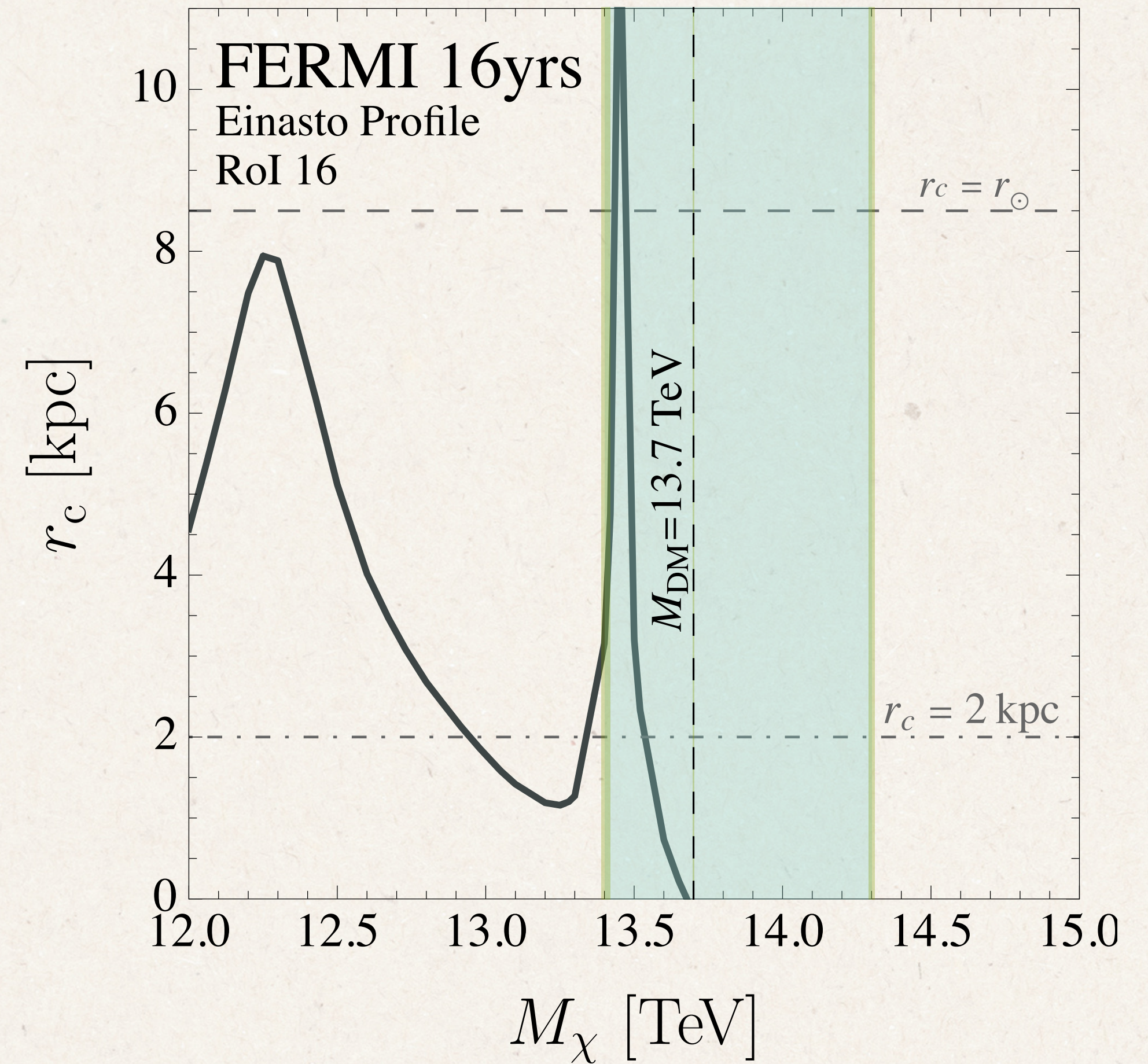
Changes of the DM profile can still mitigate the exclusion



*The exclusion depend on the uncertainty
in the DM density profile near the GC*

Results:

- 1) The big exclusion at 13.5 TeV is due to the BSF xsec peak
- 2) $13.4 \text{ TeV} \lesssim M_\chi \lesssim 13.6 \text{ TeV}$ are robustly excluded by Fermi-LAT observation of the Galactic diffuse emission
- 3) For 13.7 TeV we find a border-line exclusion since any r_c are needed to raise κ to unity



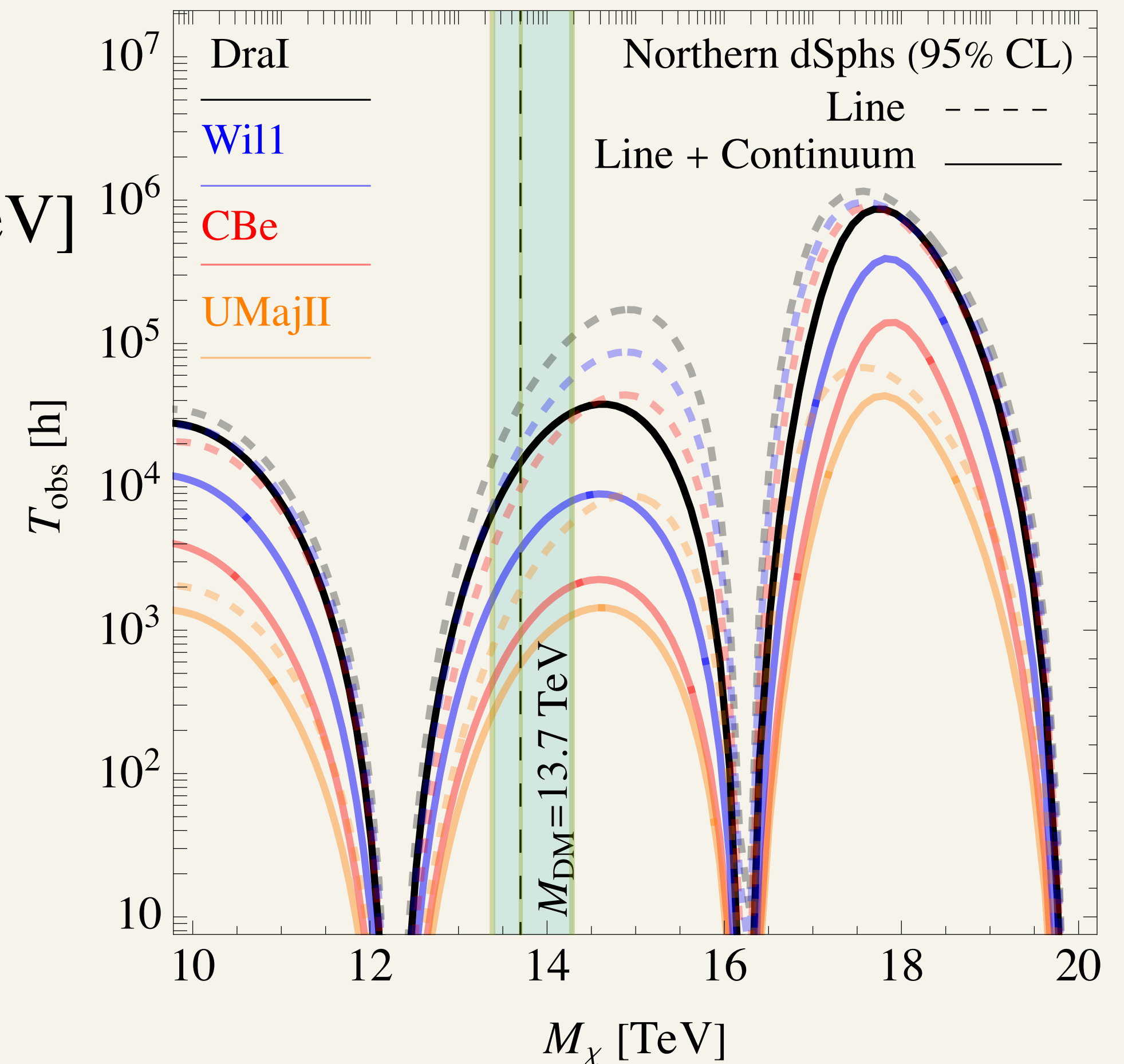
Cerenkov Telescope Array

14

- **No current data! near soon... stay tuned :)**
- We consider 20 energy bins spanning $E_\gamma \in [25 \text{ GeV}, 160 \text{ TeV}]$

Results:

- 1) Best sensitivity $\Rightarrow T_{\text{obs}}^{\text{UMajII}} \simeq 600 \text{ h}$ for $M_{\text{DM}} = 13.7 \text{ TeV}$
- 2) The other ultra-faint dSphs pose weaker bounds because the impact of the J-factor systematics
- 3) Including the continuum leads to a ~ 3 better sensitivity (UMajII)



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Take Home message

- Minimal Dark Matter is the prototype model of WIMP:
 - huge predictivity, few parameters
- Dark Matter as a WIMP remains one of the main motivation for NP at the multi-TeV scale

Take Home Message:

- 5-plet shows smoking-gun signatures for the ID
- Present data on the galactic diffuse can already place stringent constraints on the MDM 5-plet, particularly on the continuum from BSF
- CTA will be able to probe the model in the next decades by pointing the detectors towards dSphs (Few hour needed!)

thank
you
it was a pleasure!

Backup Slides



State of the Art

DM spin	EW n-plet	M_χ (TeV)	$(\sigma v)_{\text{tot}}^{J=0} / (\sigma v)_{\text{max}}^{J=0}$	$\Lambda_{\text{Landau}} / M_{\text{DM}}$	$\Lambda_{\text{UV}} / M_{\text{DM}}$
Real scalar	3	2.53 ± 0.01	—	2.4×10^{37}	$4 \times 10^{24*}$
	5	15.4 ± 0.7	0.002	7×10^{36}	3×10^{24}
	7	54.2 ± 3.1	0.022	7.8×10^{16}	2×10^{24}
	9	117.8 ± 15.4	0.088	3×10^4	2×10^{24}
	11	199 ± 42	0.25	62	1×10^{24}
	13	338 ± 102	0.6	7.2	2×10^{24}
Majorana fermion	3	2.86 ± 0.01	—	2.4×10^{37}	$2 \times 10^{12*}$
	5	13.6 ± 0.8	0.003	5.5×10^{17}	3×10^{12}
	7	48.8 ± 3.3	0.019	1.2×10^4	1×10^8
	9	113 ± 15	0.07	41	1×10^8
	11	202 ± 43	0.2	6	1×10^8
	13	324.6 ± 94	0.5	2.6	1×10^8

Real WIMPs

Odd n and $Y = 0$

$$\mathcal{L}_f = \frac{1}{2} \bar{\chi} (i \bar{\sigma}^\mu D_\mu - M_\chi) \chi$$

Majorana Fermion

$$\mathcal{L}_s = \frac{1}{2} (D_\mu \chi)^2 - \frac{1}{2} M_\chi^2 \chi^2 - \frac{\lambda_H}{2} \chi^2 |H|^2 - \frac{\lambda_\chi}{4} \chi^4$$

Real Scalar

- For $n = 3$ multiplets DM stability is achieved by enforcing a Z_2 symmetry;
- For $n \geq 5$ multiplets DM stability comes from an accidental Z_2 symmetry.

$$\begin{aligned} \mathcal{L}_s &\supset \frac{C_1^{(s)}}{\Lambda_{UV}^{n-4}} \chi (H^\dagger H)^{\frac{n-1}{2}} + \frac{C_2^{(s)}}{\Lambda_{UV}^{n-4}} \chi W_{\mu\nu} W^{\mu\nu} (H^\dagger H)^{\frac{n-5}{2}} + \dots + \frac{C_w^{(s)}}{\Lambda_{UV}^{n-4}} \chi (W_{\mu\nu} W^{\mu\nu})^{\frac{n-1}{4}} + \frac{C_{3\chi}^{(s)}}{\Lambda_{UV}} \chi^3 H^\dagger H, \\ \mathcal{L}_f &\supset \frac{C_1^{(f)}}{\Lambda_{UV}^{n-3}} (\chi H L) (H^\dagger H)^{\frac{n-3}{2}} + \frac{C_2^{(f)}}{\Lambda_{UV}^{n-3}} (\chi \sigma^{\mu\nu} H L) W_{\mu\nu} (H^\dagger H)^{\frac{n-5}{2}} + \dots + \frac{C_w^{(f)}}{\Lambda_{UV}^{n-3}} (\chi H L) (W_{\mu\nu} W^{\mu\nu})^{\frac{n-3}{4}} + \frac{C_{3\chi}^{(f)}}{\Lambda_{UV}^3} \chi^3 H L \end{aligned}$$

Thermal freeze-out

$$\frac{dn_{\text{DM}}}{dt} + 3Hn_{\text{DM}} = \langle \sigma v_{\text{rel}} \rangle (n_{\text{eq}}^2 - n_{\text{DM}}^2)$$

- DM abundance is fully controlled by the annihilation cross section
- The tree-level cross-section: $\sigma v_{\text{rel}} = \frac{g_2^4(2n^4 + 17n^2 - 19)}{256\pi g_\chi M_\chi^2}$
- However this is inaccurate → **Non perturbative** and **Non-relativistic** effects modify the cross section

Sommerfeld Enhancement
Bound State Formation

Thermal mass window

$$M_\chi = 13.7_{-0.3}^{+0.6} \text{ TeV}^*$$

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* [1] NLO electroweak potentials for minimal dark matter and beyond: [arXiv:hep-ph/2108.07285](#)
[2] The Sommerfeld enhancement at NLO and the dark matter unitarity bound: [arXiv:hep-ph/2305.01680](#)

SE and BSF

1

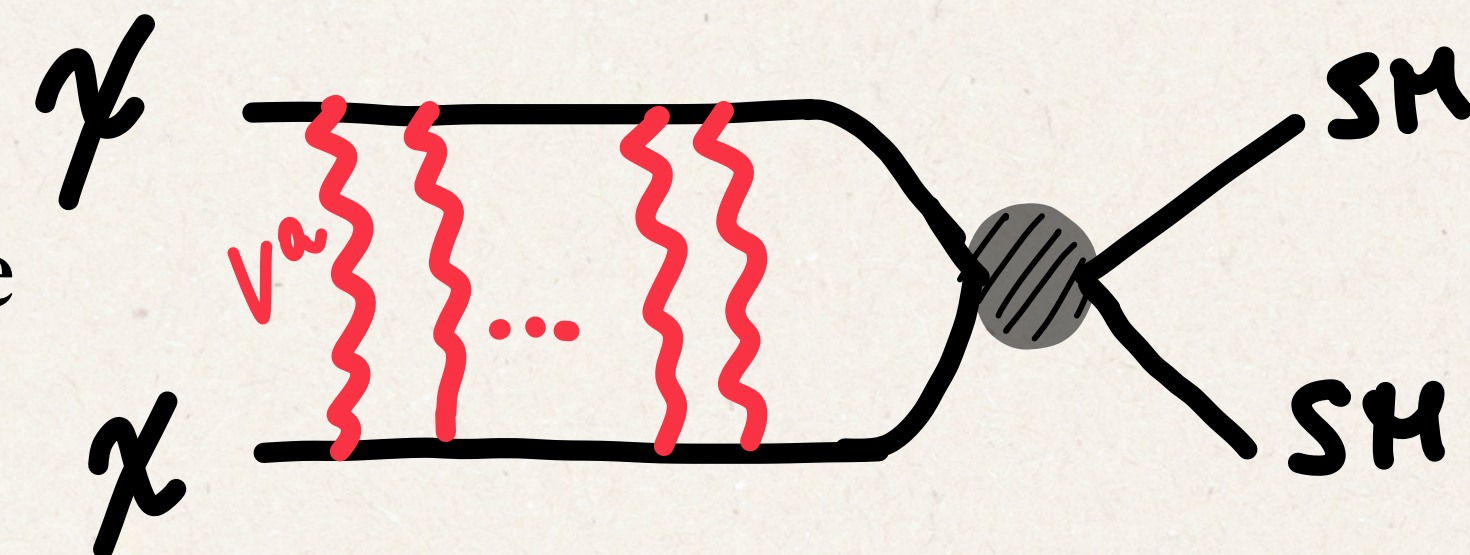
Sommerfeld $\chi^0 \chi^0 \rightarrow V^a V^a$

- Long range effects modify the wave function of the 2-body DM-DM initial state
- σ_{NR} can receive large non-perturbative corrections (low vel. Enhanced)

$$\sigma \rightarrow S \sigma_{\text{pert}}$$

Not so easy...

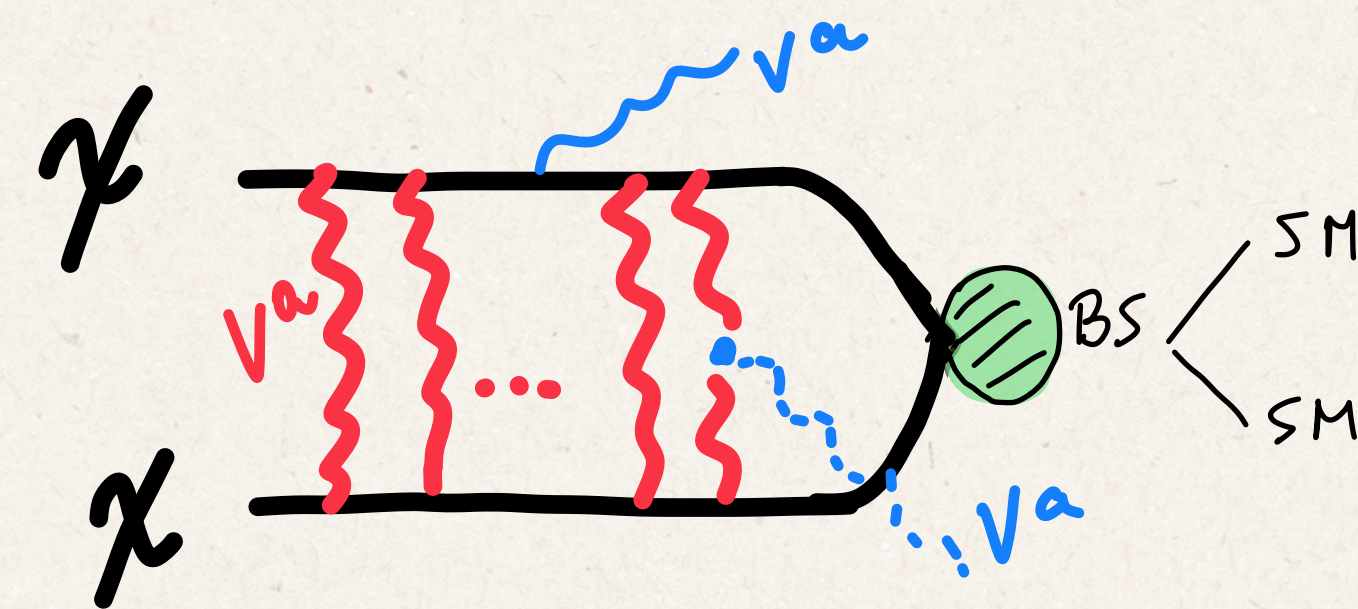
broken phase, NLO corrections, ecc...



2

BSF $\chi^0 \chi^0 \rightarrow V^a \text{ BS}$

- The same long-range potential is also responsible for BSF.
- $^1S_3 : E_B \sim 80 \text{ GeV}$
- BS annihilation with a rate $\Gamma_{\text{ann}} \sim \alpha_2^5 M_\chi$ into SM particles ($f\bar{f}$ and HH^*)



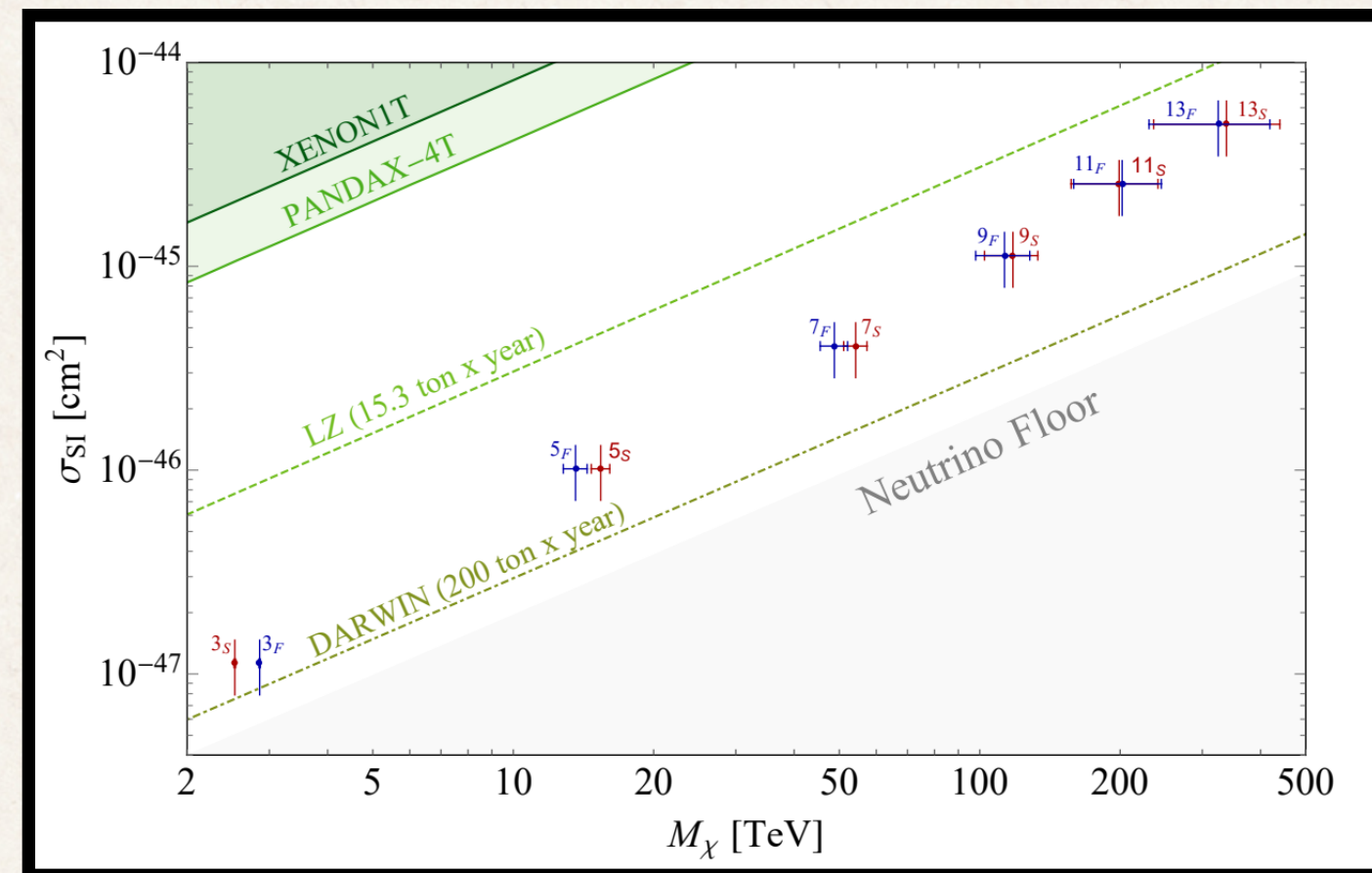
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* [1] Non-relativistic pair annihilation of nearly mass degenerate neutralinos and charginos III. Computation of the Sommerfeld enhancements: [arXiv:hep-ph/1411.6924](https://arxiv.org/abs/hep-ph/1411.6924)
 [2] Capture and Decay of Electroweak WIMPonium: [arXiv:hep-ph/1610.07617](https://arxiv.org/abs/hep-ph/1610.07617)

Detection Strategies

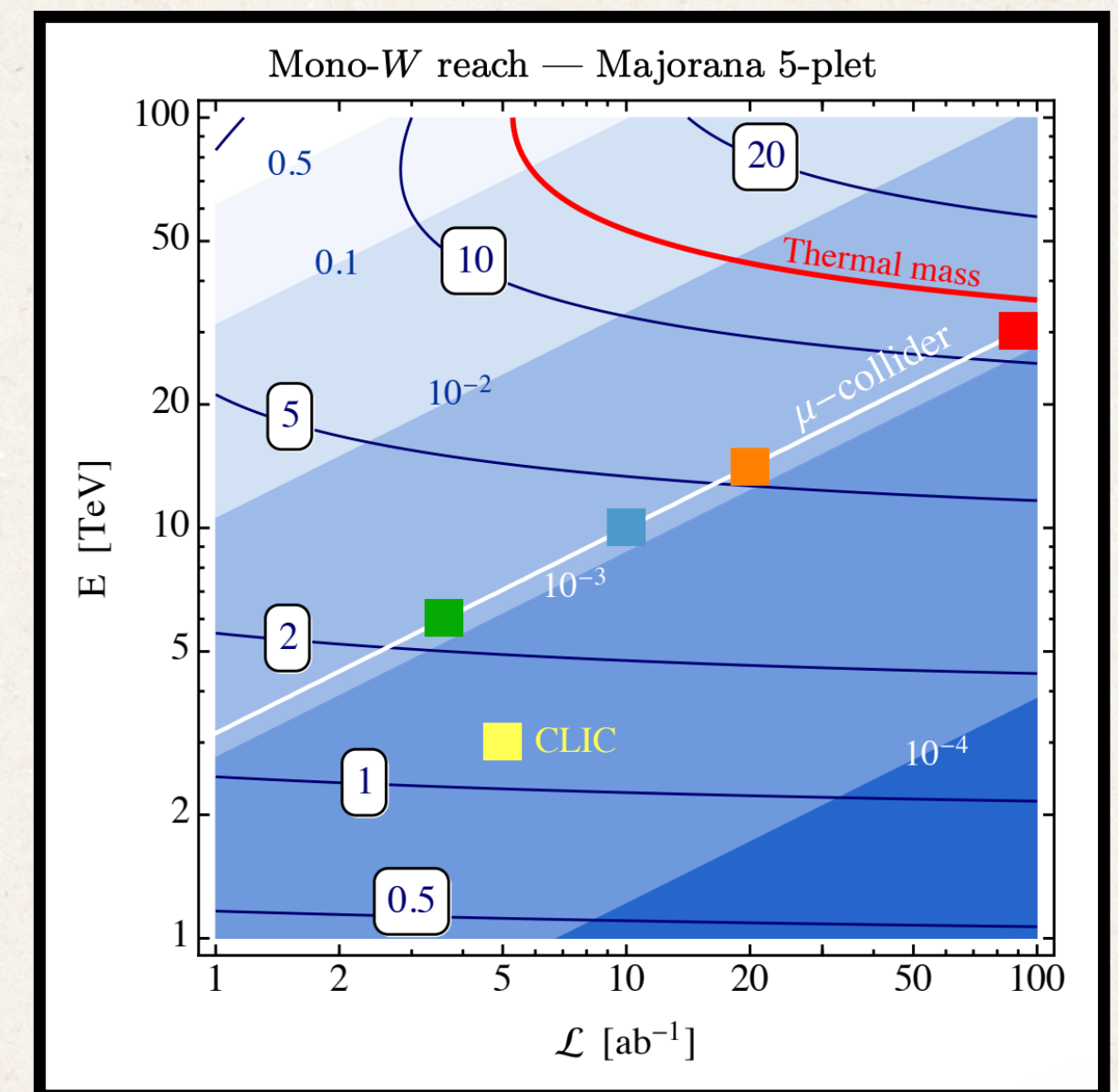
1 Direct Detection

- EW multiplets within the reach of next generation experiments (~30 yrs)



2 Collider searches

- Will probe small multiplets in the future ($\gtrsim 50$ yrs) !
Futuristic μ C???



SE and BSF

1

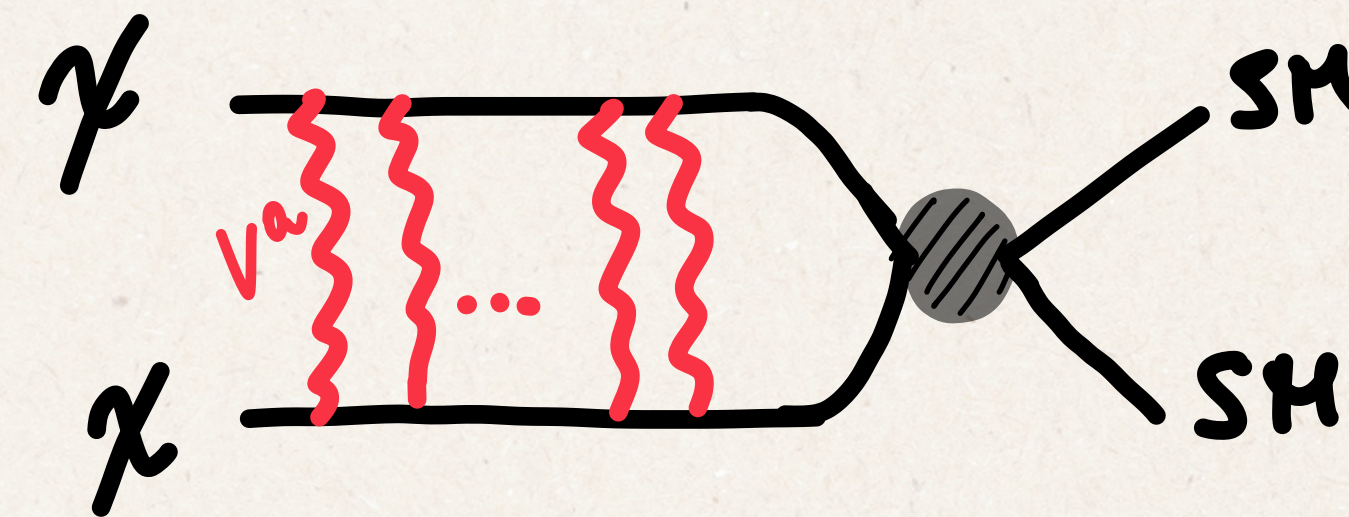
Sommerfeld

$$\chi^0 \chi^0 \rightarrow V^a V^a$$

- σ_{NR} can receive large non-perturbative corrections (low vel. Enhanced)

$$\sigma \rightarrow S \sigma_{\text{pert}}$$

- Relevant for cosmology and indirect detection where DM is non-relativistic
- DM couples to a mediator particle with $M_V \ll M_\chi \rightarrow$ The interaction is long range
- Long Range effects modify the DM wave function of the 2-body DM-DM initial state $\psi(\mathbf{r}) = u(r)/\sqrt{4\pi r}$



☐ In the unbroken regime and for a Coulomb like potential $V = -\alpha/r$

$$-u''/M_\chi - \alpha u/4\pi r = Eu$$

$$u'(\infty)/u(\infty) \simeq iMv_{\text{rel}}/2$$

$$S = \left| \frac{u(\infty)}{u(0)} \right|^2 = \frac{2\pi\alpha/v_{\text{rel}}}{1 - e^{-2\pi\alpha/v_{\text{rel}}}}$$

Not so easy...

- 1) broken phase
- 2) NLO corrections

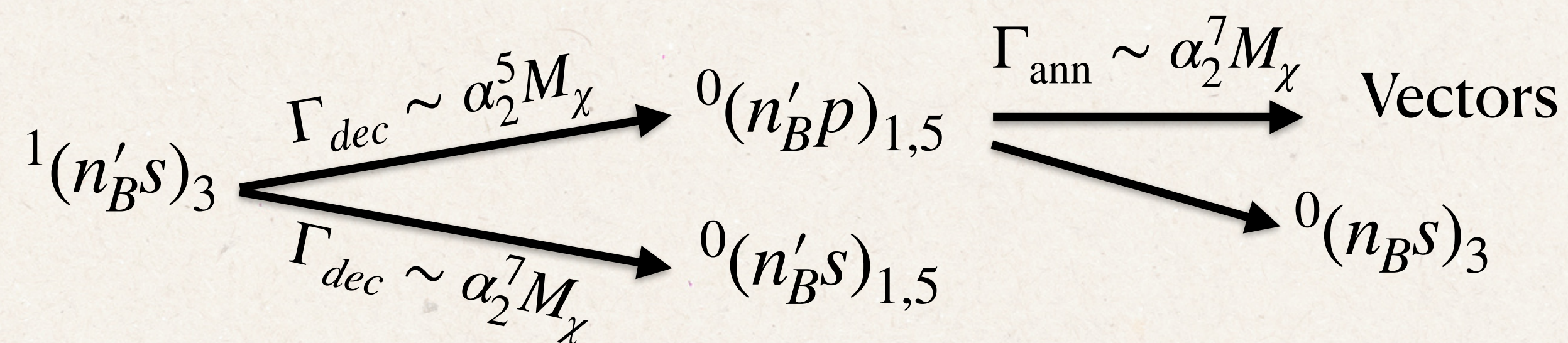
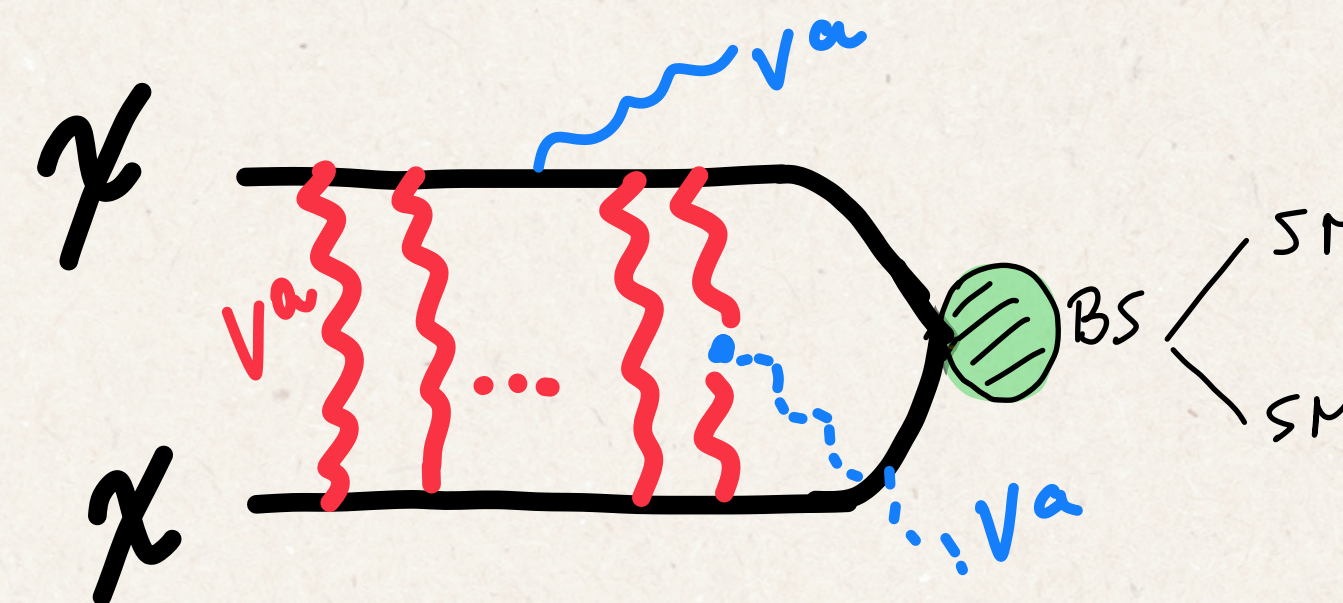
SE and BSF

2

BSF

$$\chi^0 \chi^0 \rightarrow V^a \text{ BS}$$

- The same long-range potential is also responsible for BSF.
- At leading order the capture occurs via $\chi_i \chi_j \rightarrow V^a + \text{BSF}$
- In the electric dipole approx $\Delta L = 1$ and $\Delta S = 0$, $E_B \sim \alpha_2^2 M_\chi$
- The dominant SBF channel consists in $p \rightarrow s$ transitions with $S = 1$ and principal quantum number $^1(n_{BS})_3$
- Once formed they annihilate with a rate $\Gamma_{\text{ann}} \sim \alpha_2^5 M_\chi$ into SM particles ($f\bar{f}$ and HH^*)



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Spectrum

$$\frac{d\mathcal{N}}{dE_\gamma} = \frac{1}{\langle\sigma v\rangle_{\text{line}}^{\text{NLL}}} \left(\frac{d\langle\sigma v\rangle}{dE_\gamma} \Big|_{\text{Cont}} + \frac{d\langle\sigma v\rangle}{dE_\gamma} \Big|_{\text{BS-line}} + \frac{d\langle\sigma v\rangle}{dE_\gamma} \Big|_{\text{line}}^{\text{NLL}} \right)$$

1

Continuum

$$\frac{d\langle\sigma v\rangle}{dE_\gamma} \Big|_{\text{Cont}} = \langle\sigma v\rangle_{1s3} \sum_{i=\{q,\ell,h\}} \text{BR}_i \frac{dN_\gamma^i}{dE_\gamma}(M_\chi) + \langle\sigma v\rangle_{WW} \frac{dN_\gamma^W}{dE_\gamma}(M_\chi) + \frac{\langle\sigma v\rangle_{\text{line}}^{\text{NLL}}}{\tan^2 \theta_w} \frac{dN_\gamma^Z}{dE_\gamma}(M_\chi) ,$$

2

BSF line

$$\frac{d\langle\sigma v\rangle}{dE_\gamma} \Big|_{\text{BS-line}} = \frac{1}{2} \langle\sigma v\rangle_{1s3} \frac{dN_\gamma^\gamma}{dE_\gamma}(E_b)$$

3

Endpoint

$$\frac{d\langle\sigma v\rangle}{dE_\gamma} \Big|_{\text{line}}^{\text{NLL}} = \langle\sigma v\rangle_{\text{line}}^{\text{NLL}} \left(2\delta(E_\gamma - M_\chi) + \mathcal{E}^{\text{NLL}}(E_\gamma) \right) ,$$

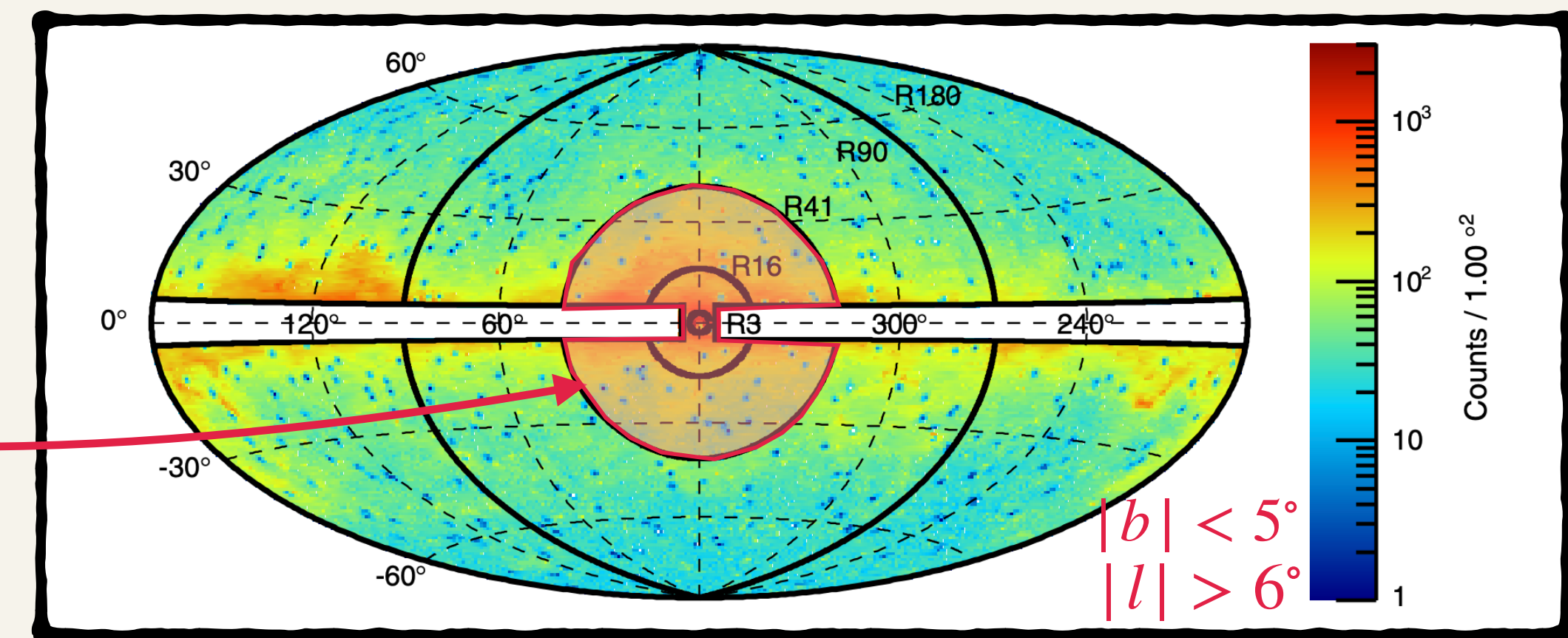
Choice of the Targets

1 Galactic Halo (Fermi-LAT)

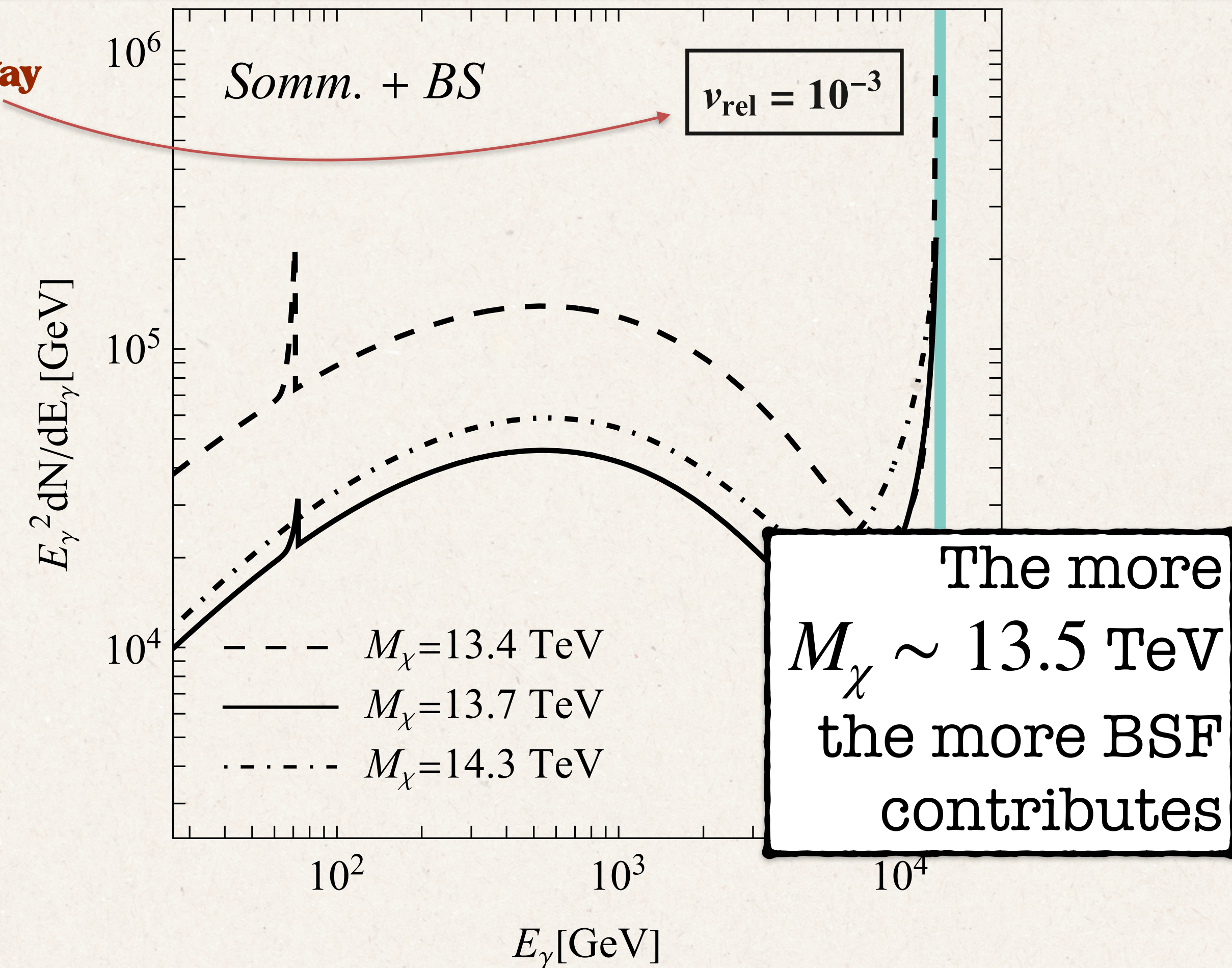
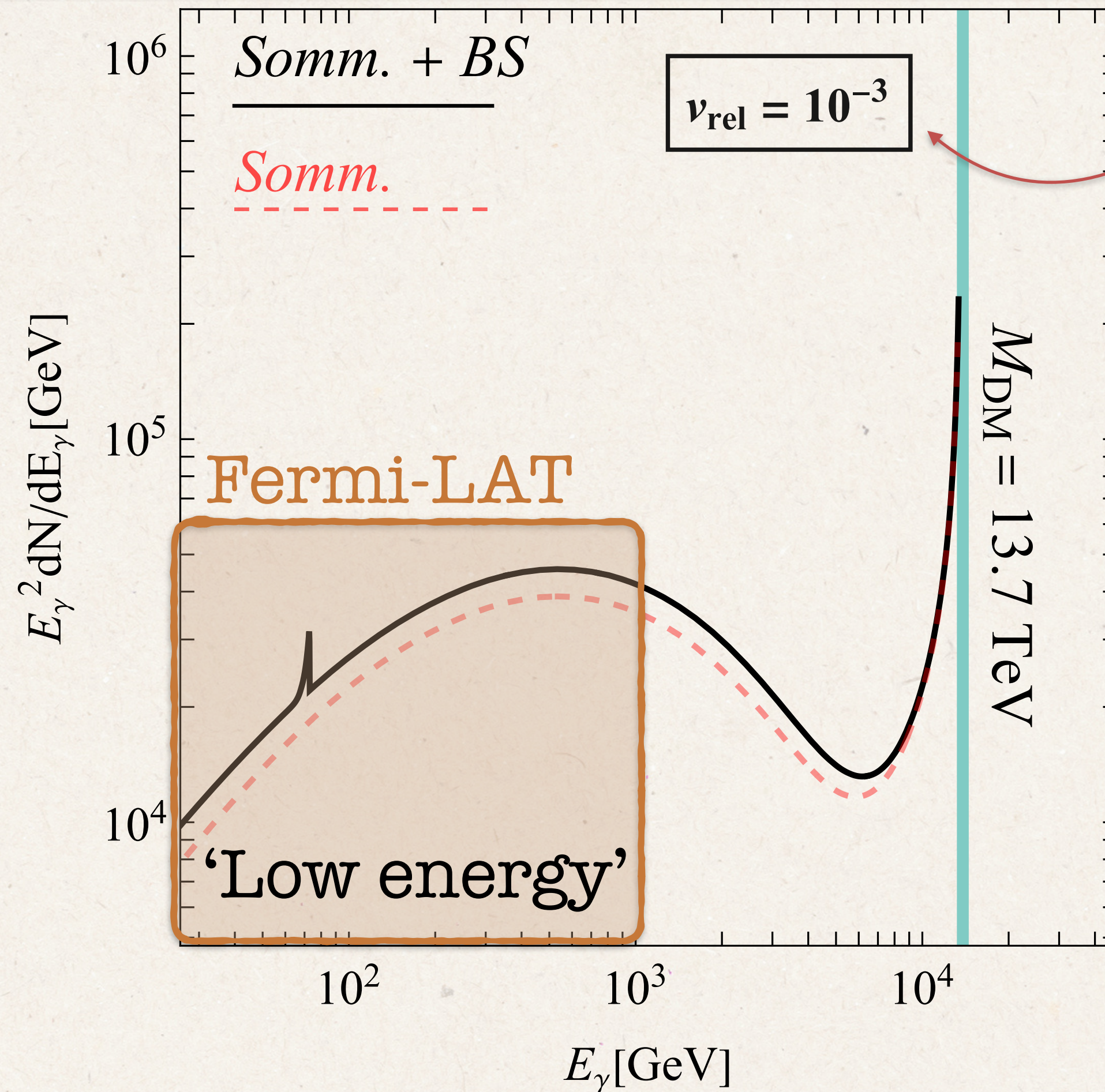
- We focus on a specific RoI:
 - The presence of a γ -ray line at E_b well within Fermi-LAT
 - Large angular size to mitigate DM density profile uncertainties
 - But not so large as to introduce template fit mismodelling for the galactic diffuse emission
 - J factor uncertainties well under control
- We identify the RoI 16 as the optimal fiducial region.
- It optimizes the SNR for an Einasto profile

2 Dwarf Spheroidal Galaxies (CTAO)

- DM-dominated with low astro bkg. $\Rightarrow$ Robust constraints
- Less luminosity
- We focus on a sample of dSphs located in the northern hemisphere: (Draco I, Willman I, Coma Berenices and Ursa Major II)



The γ ray spectrum



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CTAC Analysis

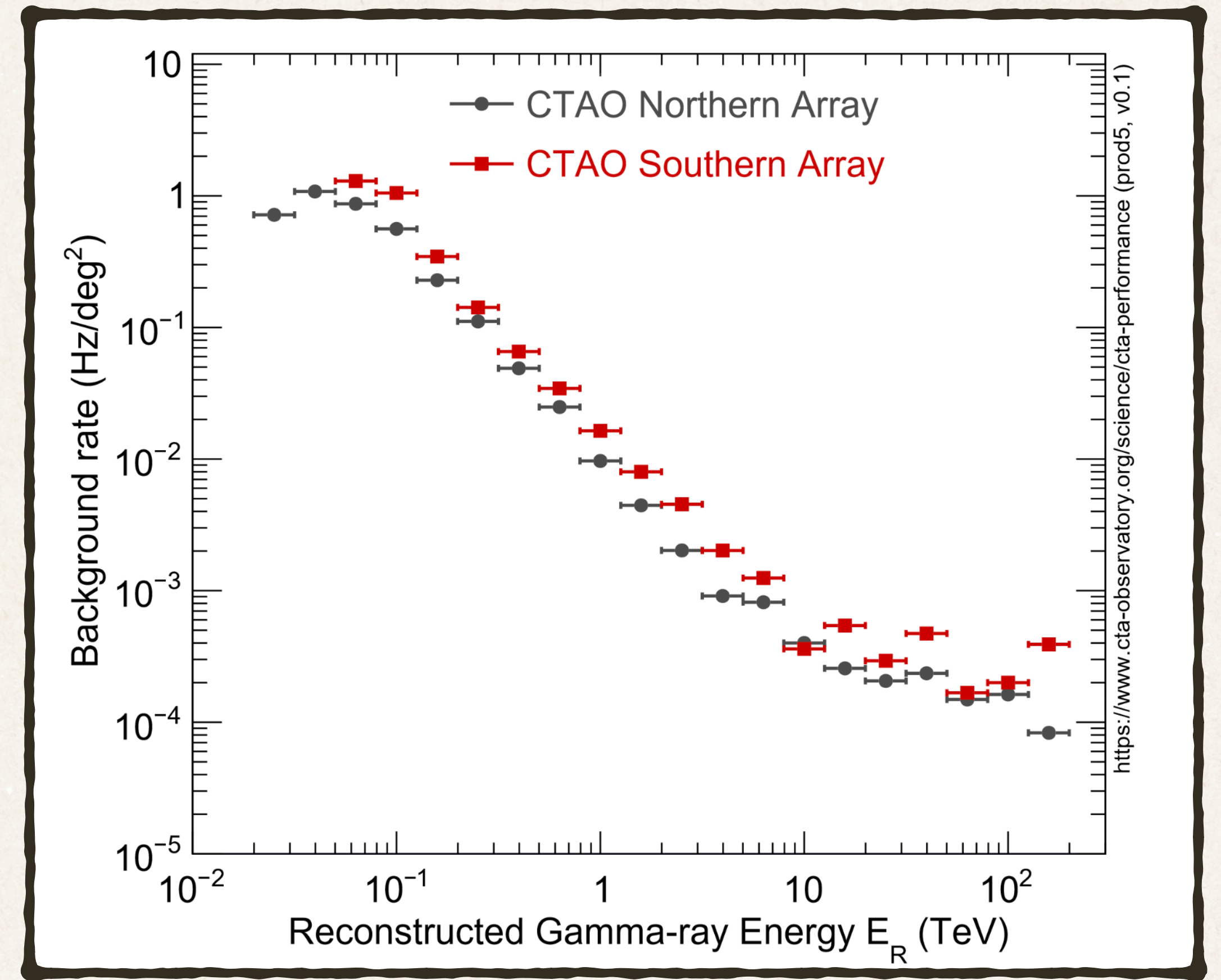
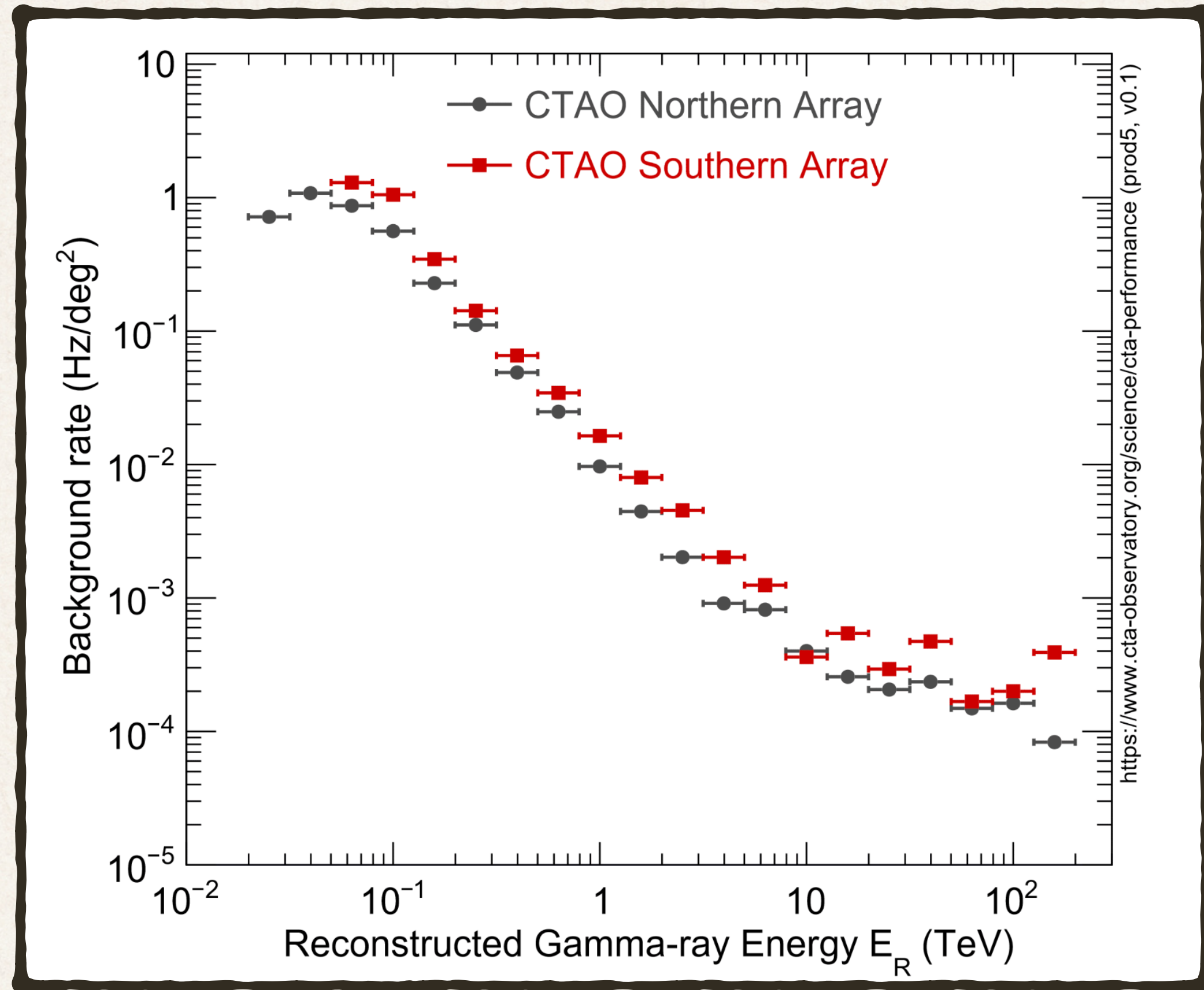
- **No current data! near soon... stay tuned :)**
- We consider 20 energy bins spanning $E_\gamma \in [25 \text{ GeV}, 160 \text{ TeV}]$
- Northern hemisphere and Rol with $\Delta\theta_{\text{dPhs}} = 0.5^\circ$

$$N_{bkg}^i = T_{\text{obs}} \frac{\Delta\Gamma_{\text{bkg}}^i}{\Delta\Omega} \Delta\Omega_{\text{dSphs}} \text{ where } \Delta\Omega_{\text{dSphs}} \approx 2.4 \times 10^{-4} \text{sr}$$

$$N_{\text{DM}}^i = T_{\text{obs}} \int_{E_i}^{E_{i+1}} dE' \frac{d\Gamma_{\text{DM}}(E')}{dE'}$$

$$\frac{d\Gamma_{\text{DM}}(E')}{dE'} = \int_0^{M_\chi} dE_\gamma \frac{d\Phi_{\text{DM}}(E_\gamma)}{dE_\gamma} \mathcal{A}(E_\gamma) R(E_\gamma, E')$$

CTAO Analysis



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<https://www.ctao.org/>

CTAC Analysis

We fix $\kappa = 1$ in order to determine T_{obs} and we define a poissonian likelihood:

$$\mathcal{L}(T_{\text{obs}}) = \prod_{i=1}^{\mathcal{N}} \frac{N_{\text{th}}^i(T_{\text{obs}})^{N_{\text{obs}}^i(T_{\text{obs}})}}{N_{\text{obs}}^i(T_{\text{obs}})!} e^{-N_{\text{th}}^i(T_{\text{obs}})} \equiv \prod_{i=1}^{\mathcal{N}} \mathcal{L}_i(T_{\text{obs}}),$$

We add also the systematic uncertainty of the J-factor as

$$\mathcal{L}_{\text{sys}}(T_{\text{obs}}) = \prod_{i=1}^{\mathcal{N}} \max_J [\mathcal{L}_i(T_{\text{obs}}) \times \mathcal{L}^J]$$

$$\text{with } \mathcal{L}^J = \frac{1}{\ln(10)J_{\text{obs}}} \mathcal{G}(\log_{10} J | \log_{10} J_{\text{obs}})$$

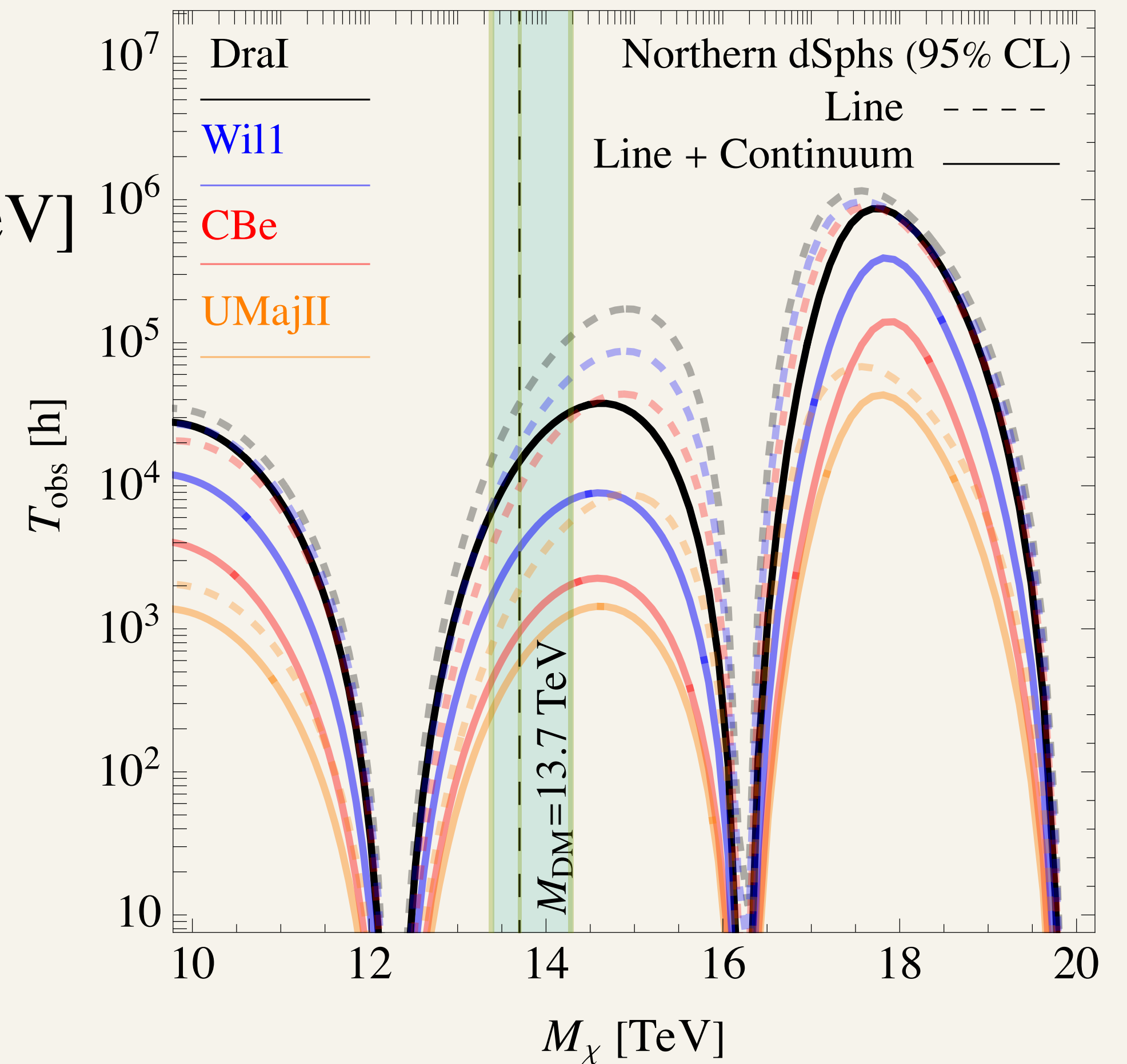
$$\text{TS}(T_{\text{obs}}) = -2 \ln \left(\mathcal{L}_{\text{sys}}(T_{\text{obs}}) / \mathcal{L}_{\text{sys}}^0(T_{\text{obs}}) \right),$$

Cerenkov Telescope Array

- **No current data! near soon... stay tuned :)**
- We consider 20 energy bins spanning $E_\gamma \in [25 \text{ GeV}, 160 \text{ TeV}]$

Results:

- 1) Best sensitivity $\Rightarrow T_{\text{obs}}^{\text{UMajII}} \simeq 600 \text{ h}$ for $M_{\text{DM}} = 13.7 \text{ TeV}$
- 2) The sharp variation are due to the ann. xsec peak
- 3) The other ultra-faint dSphs pose weaker bounds because the impact of the J-factor systematics
- 4) Including the continuum leads to a ~ 3 better sensitivity (UMajII)



Cerenkov Telescope Array

Systematic uncertainties have a greater impact on line only analysis $\Rightarrow$ a sharp feature affect less bins in the spectrum.

As a result, the systematic uncertainty from the J-factor leads to a stronger penalization of the sensitivity compared to continuum searches, where the deviation with respect to the background only hypothesis is distributed over a larger number of bins. As a consequence, we find that in the line-only case, the CTAO sensitivity across the various dSphs tends to be comparable, despite the differences in the central values of the J-factors

