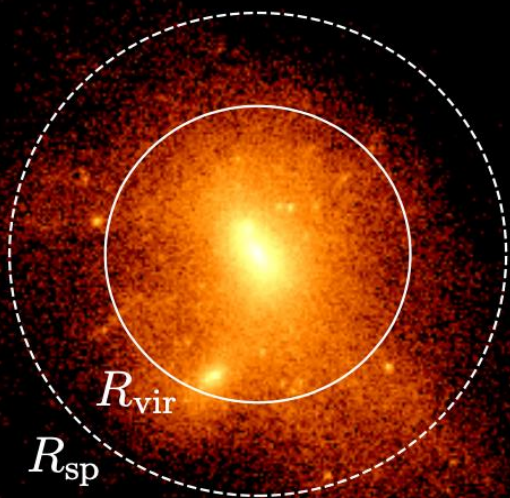
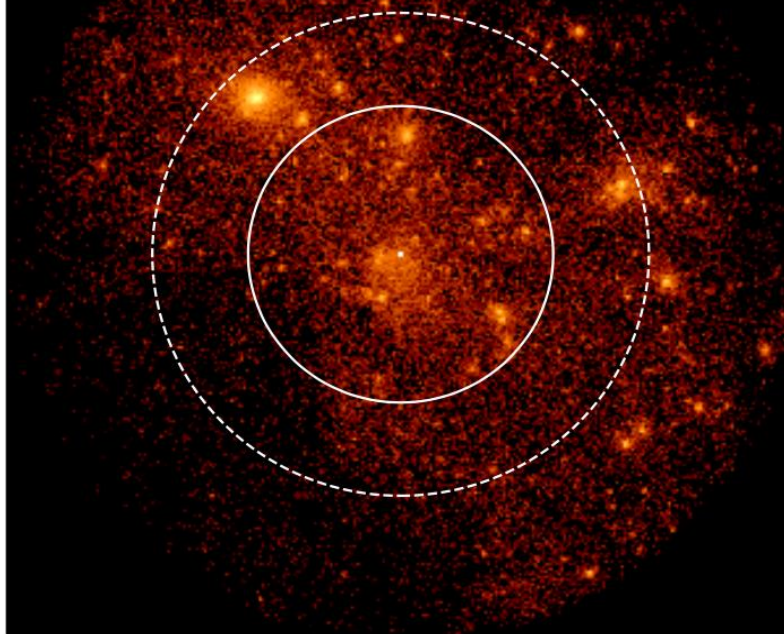


Dynamical Halos are Better!

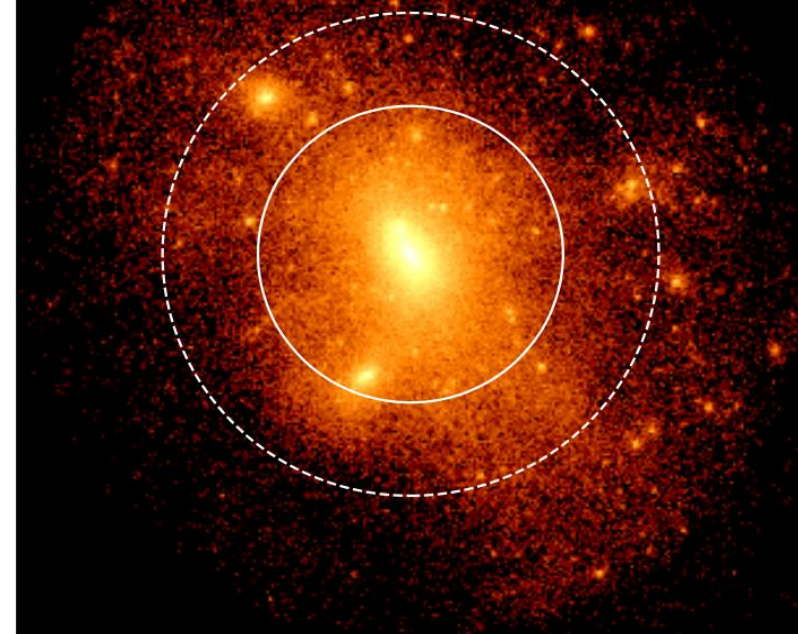
Orbiting



Infalling



Total



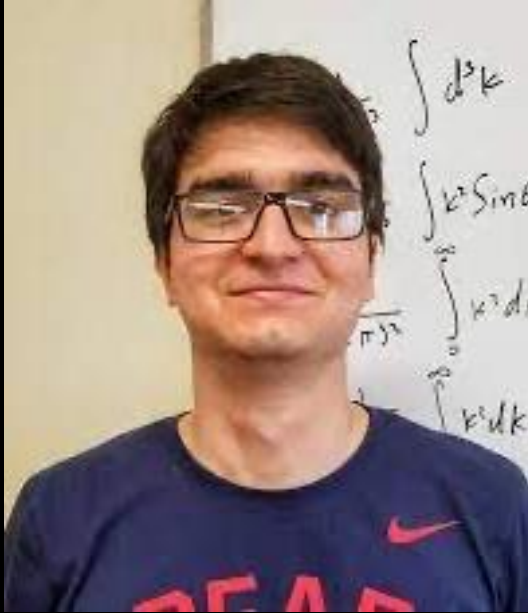
Eduardo Rozo



Valencia Workshop on the Small-Scale Structure of the
Universe and Self-Interacting Dark Matter

Valencia, Spain, July 2025

Bulk of the work shown here was performed by:



Rafael Garcia



Edgar Salzar



Hengwei Chang



Tristen Shields

In collaboration with:

Benedikt Diemer

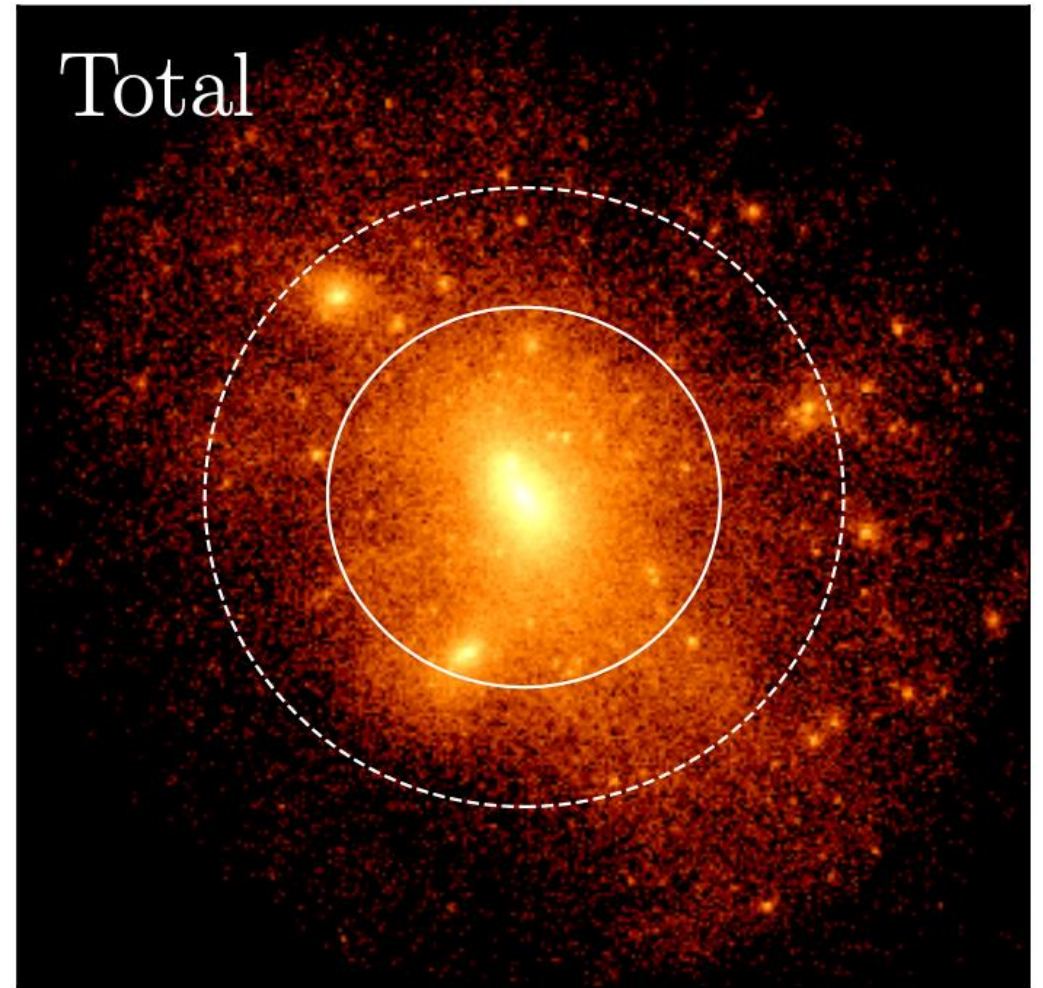
Vladimir Ze'ev

Calvin Onsaga

Susmita Adhikari

What is a halo?

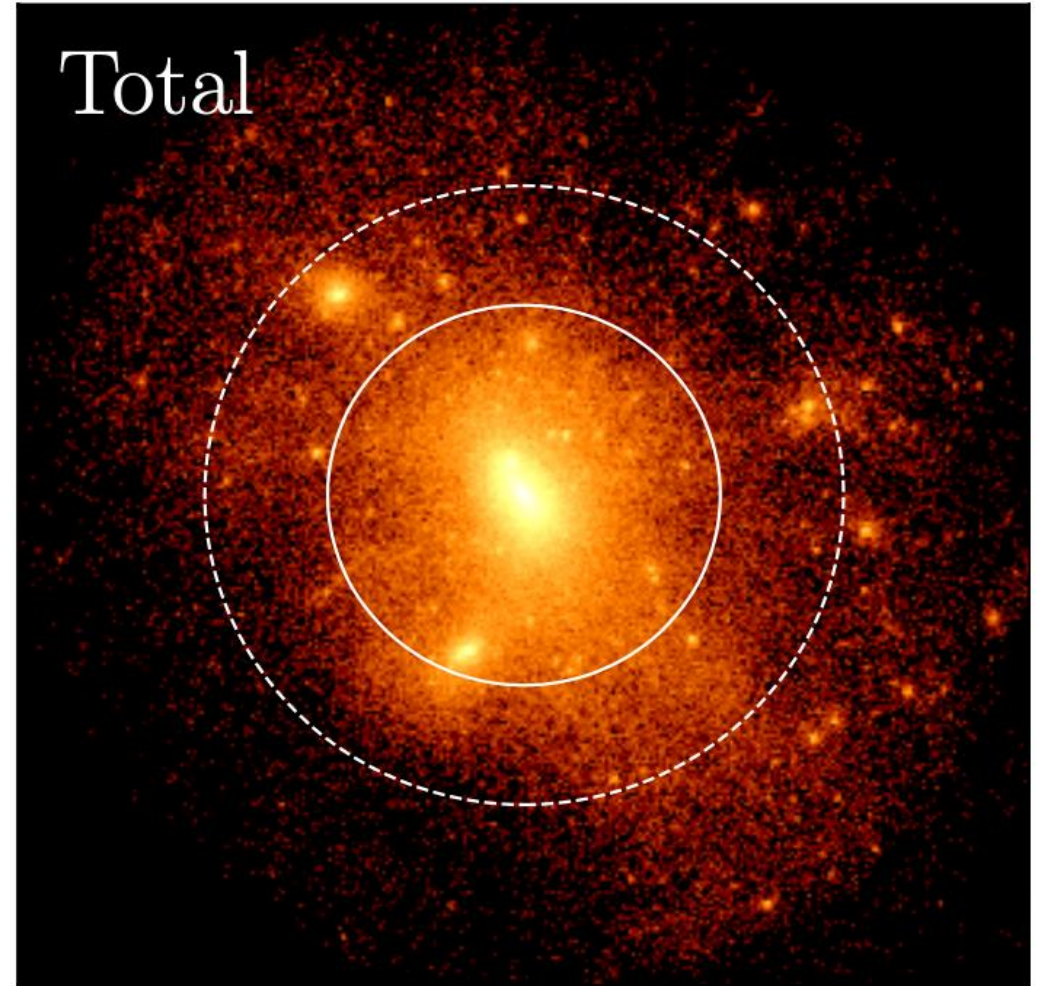
This is a halo.



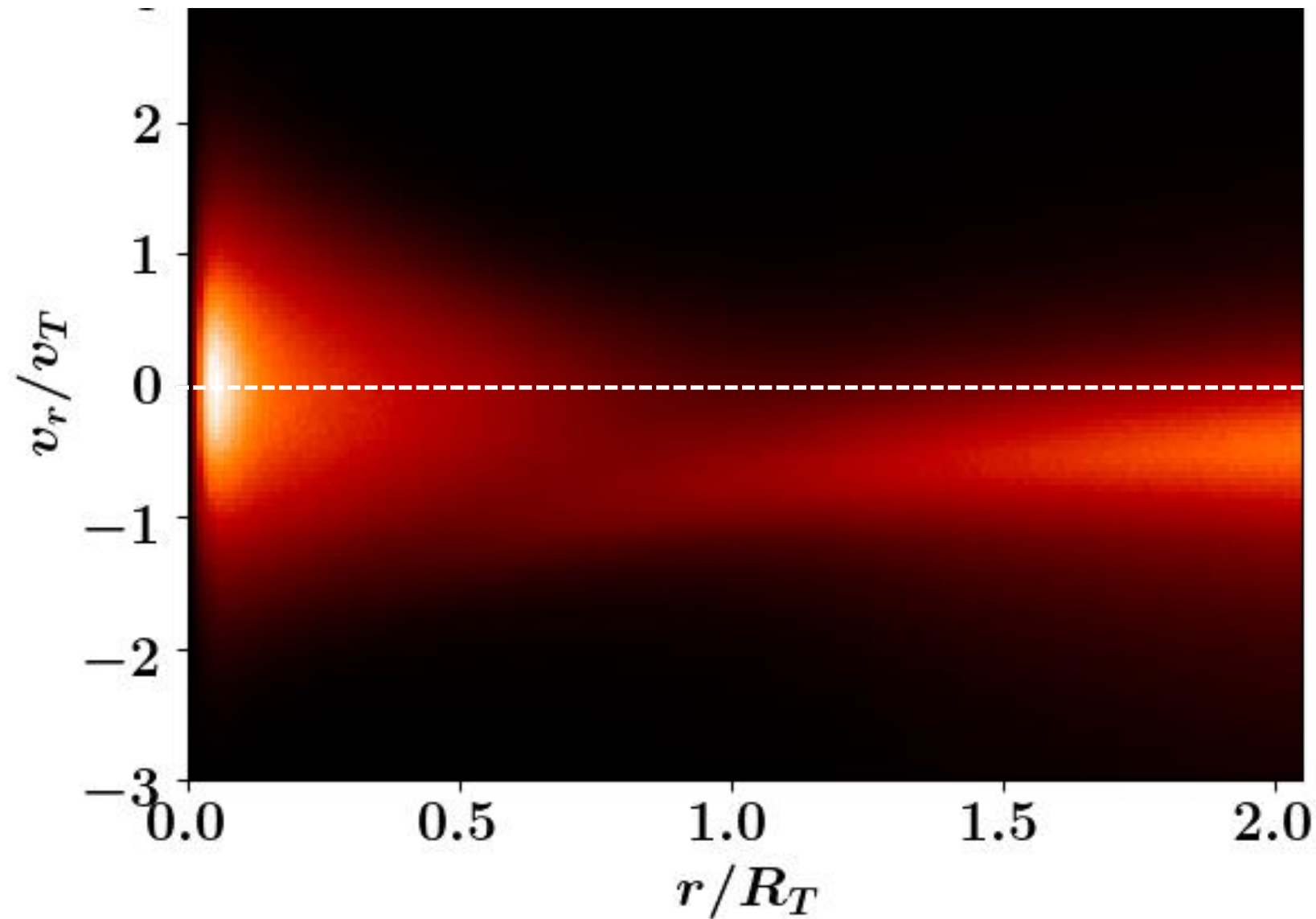
This is a halo.

Question:

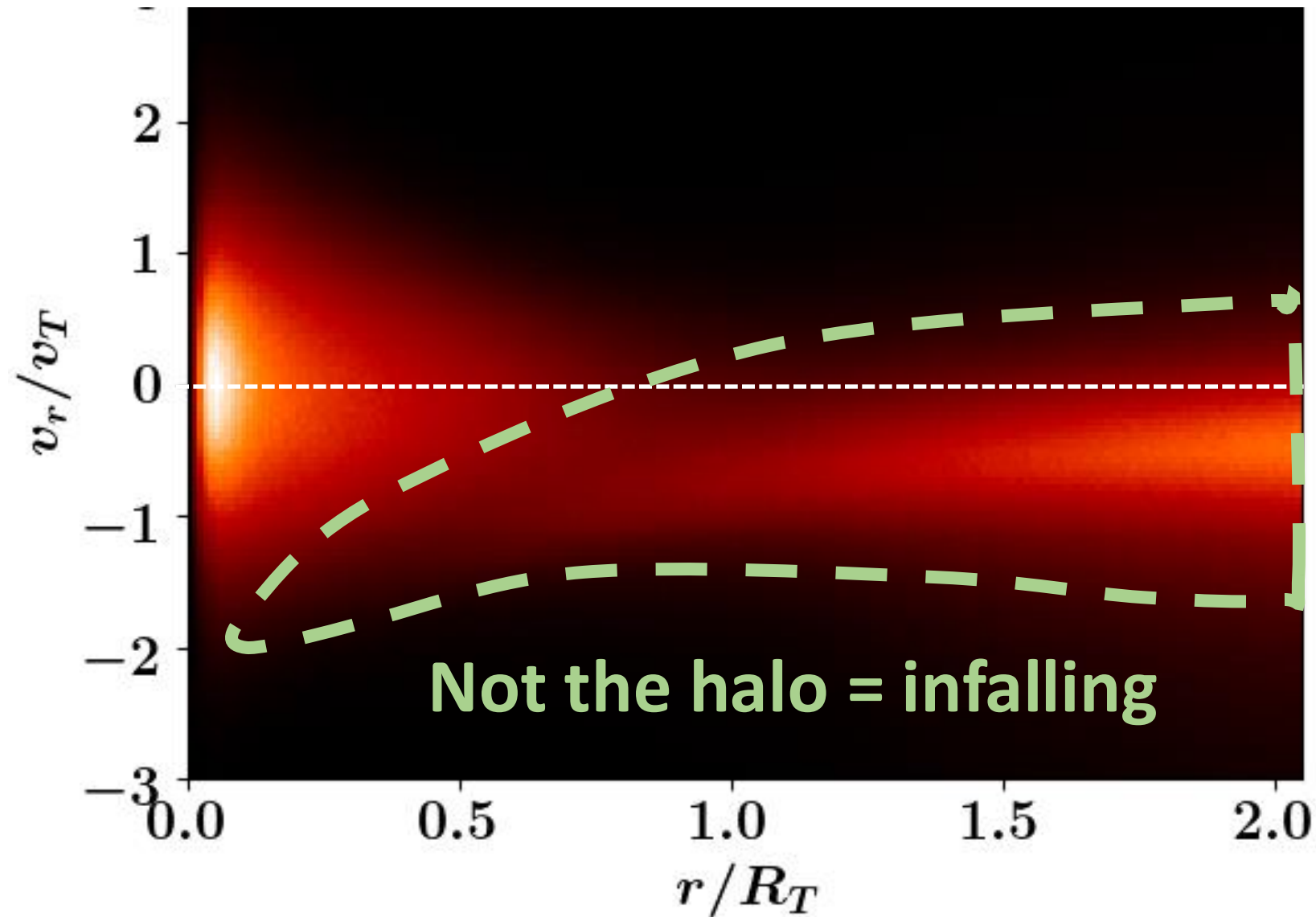
Which particles belong to the halo, and which don't?



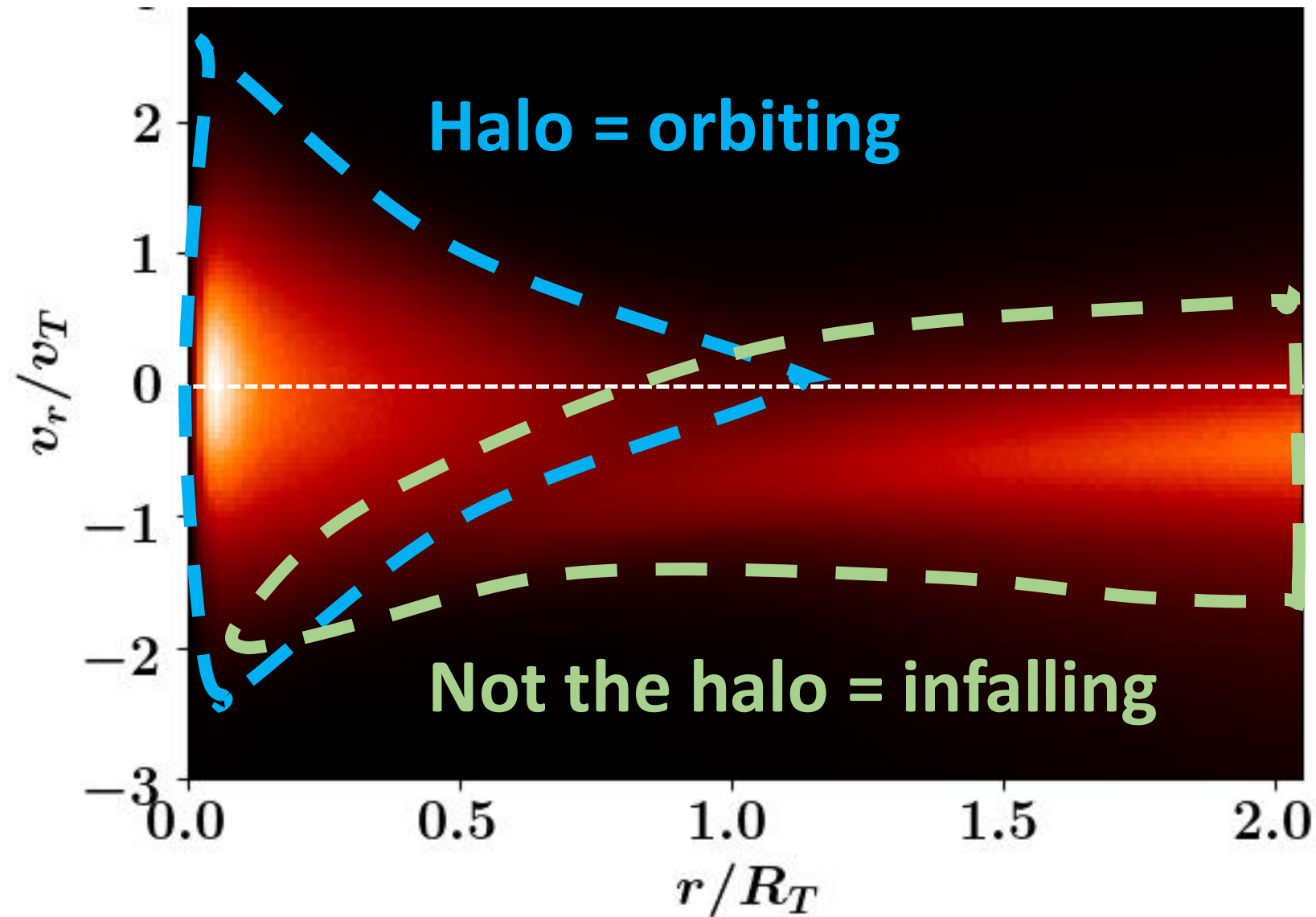
The halo is easy to see in phase space!



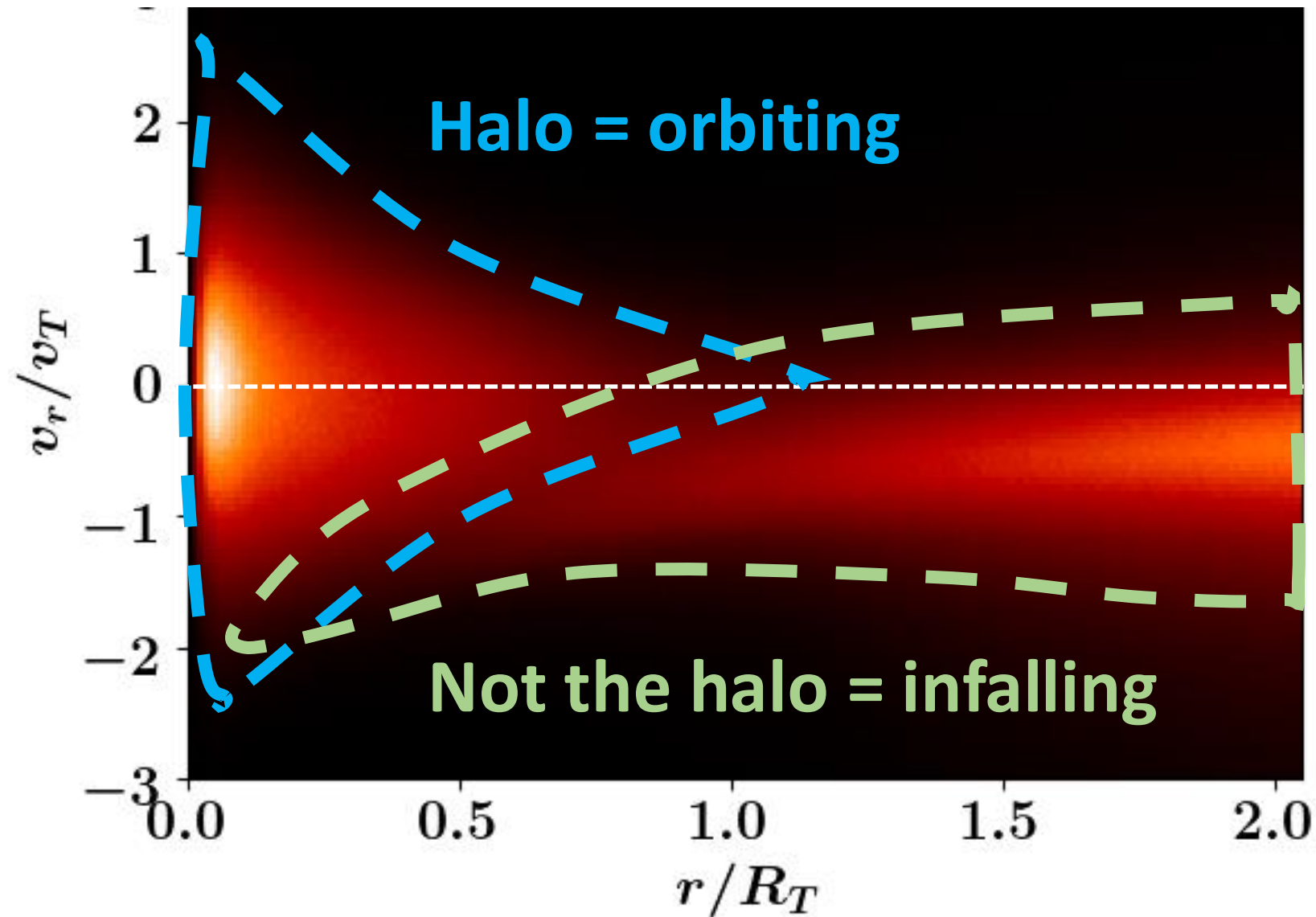
The halo is easy to see in phase space!



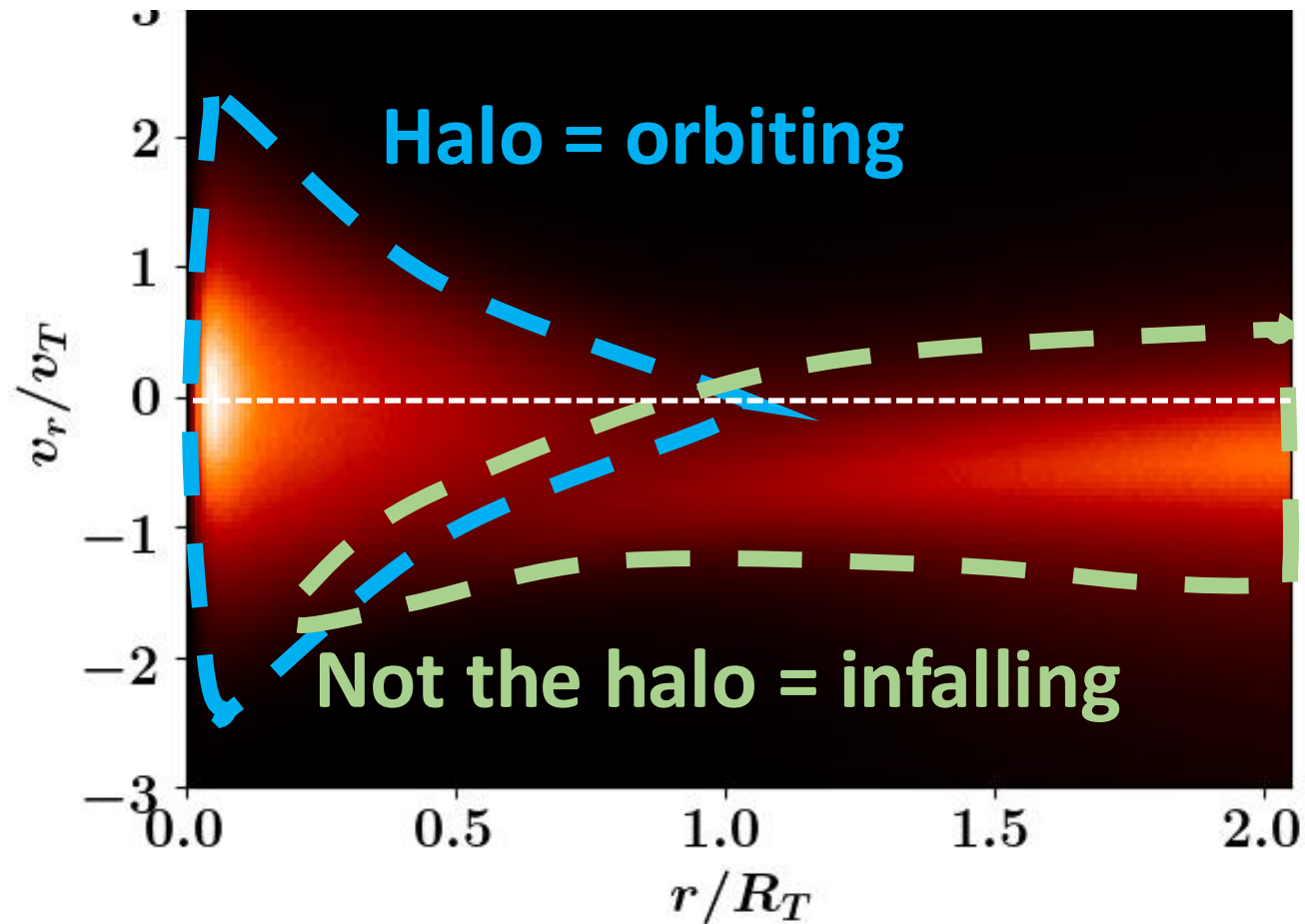
The halo is easy to see in phase space!



There is no radial boundary that cleanly separates halo from non-halo particles.



There is no radial boundary that cleanly separates halo from non-halo particles.



Need a way to selected “orbiting” particles.

Example:

A particle is “orbiting” if it has had a pericentric passage.

➤ Requires particle tracking: this is resource intensive!

Proposed definition: **A dynamical halo is the collection of particles orbiting their self-generated potential.**

This talk:

Are there any advantages to foregoing the idea of a halo boundary?

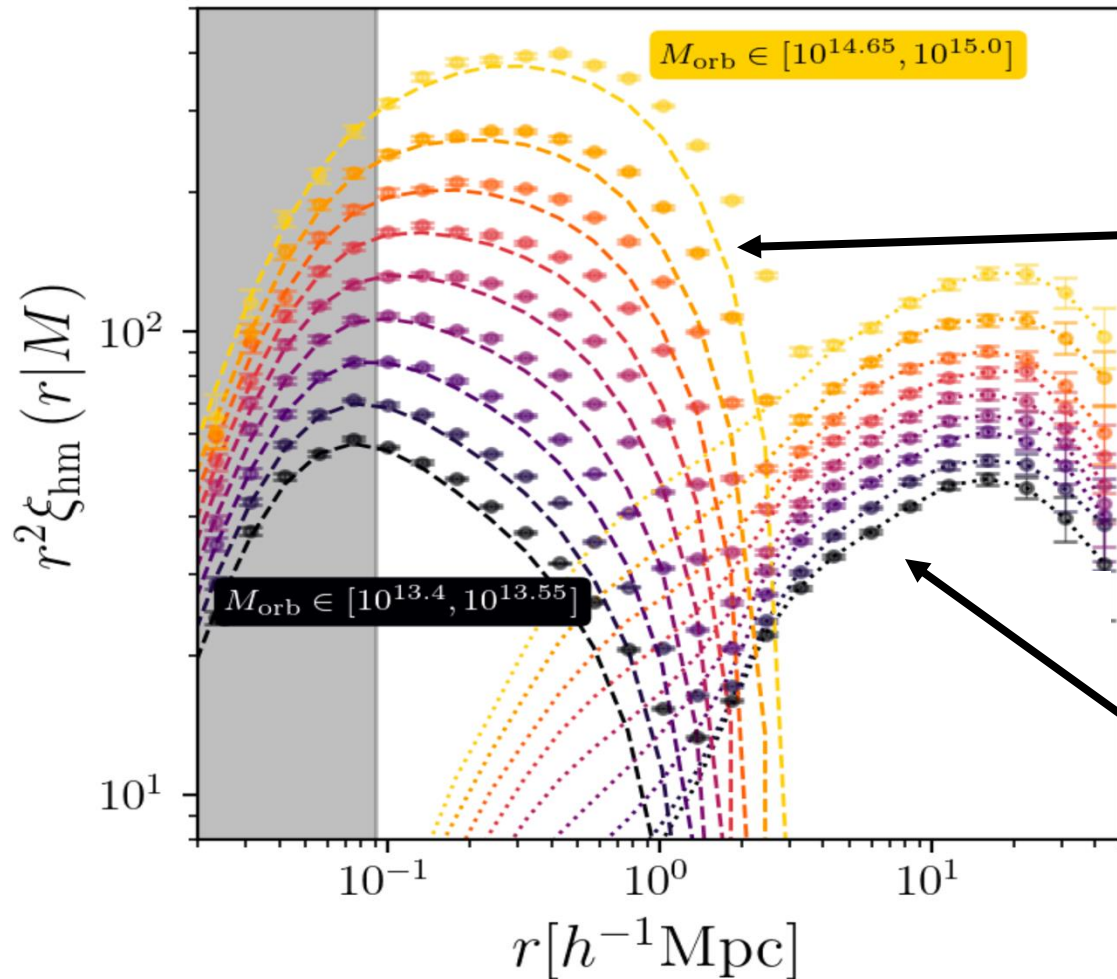
Proposed definition: **A dynamical halo is the collection of particles orbiting their self-generated potential.**

This talk:

Are there any advantages to foregoing the idea of a halo boundary?

Yes.

Advantage no. 1: **Dynamical halos enable us to build a better halo model**

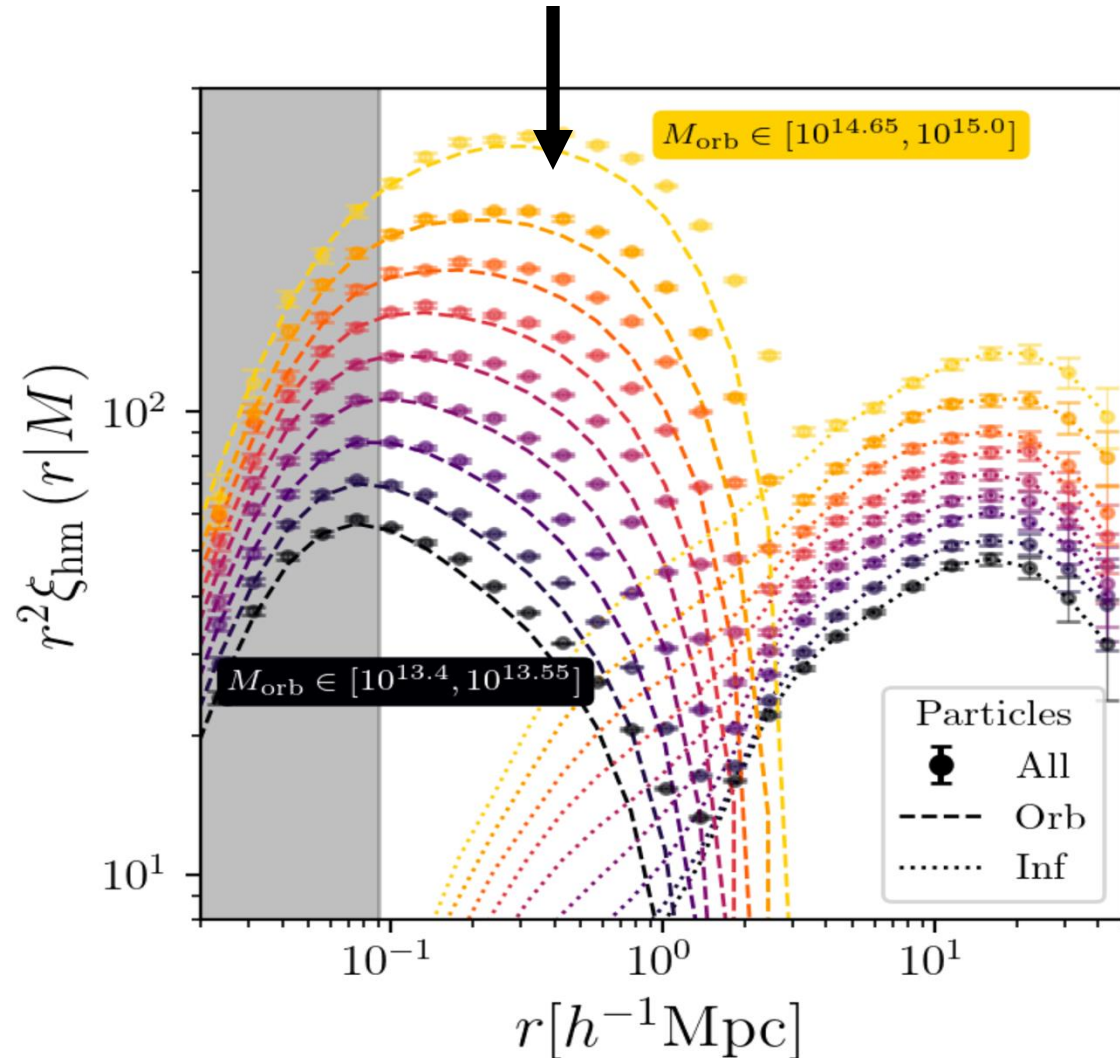


Points w/ error bars: simulation data.

Dashed lines: *orbiting particles*.

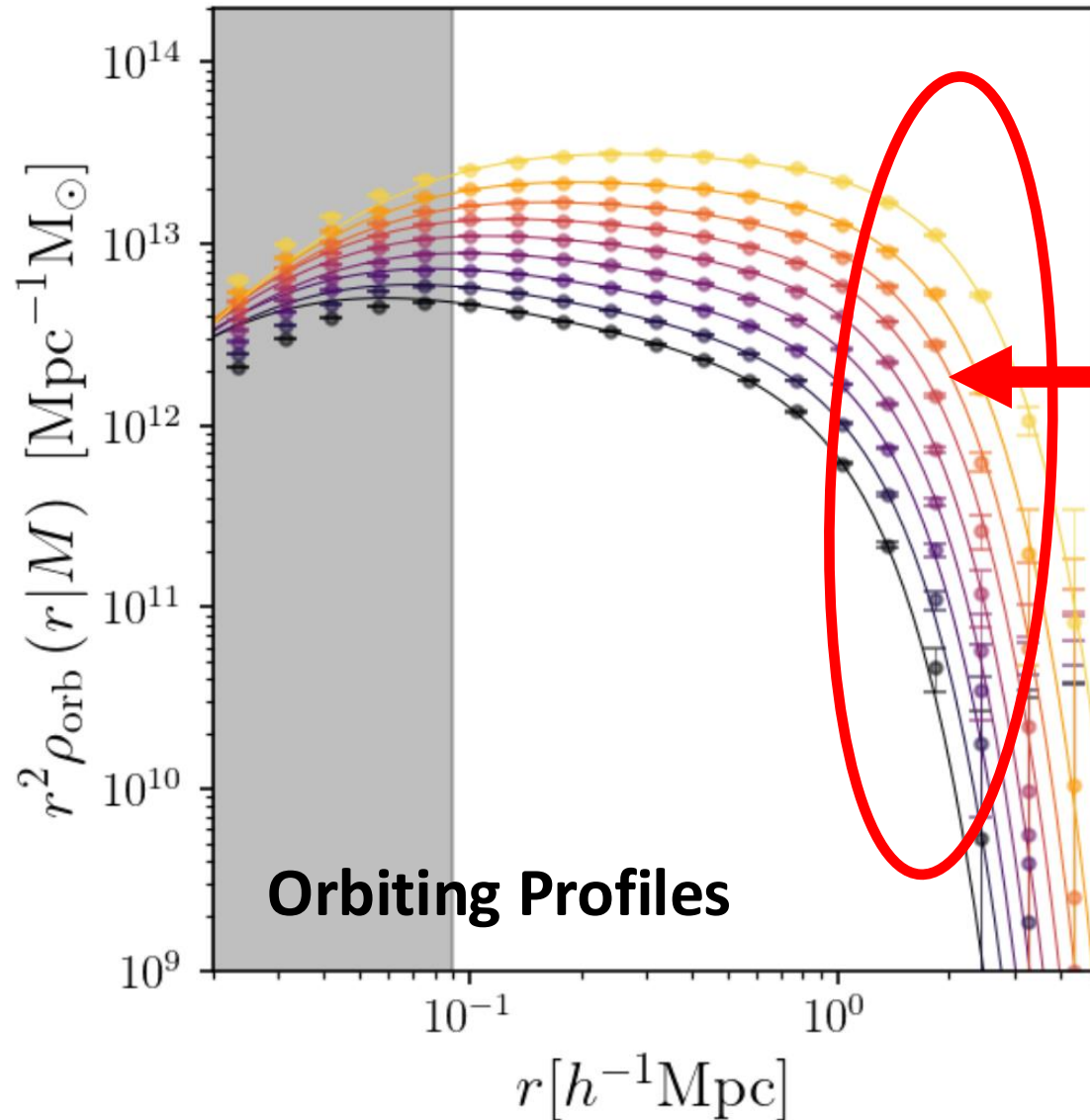
Dotted lines: *infalling particles*.

Halos are not NFW!



- Halo concentration is in part due to *infall* material.
- Infall material has never interacted with the core
- The c-M relation may not be the most useful way of talking about SIDM.

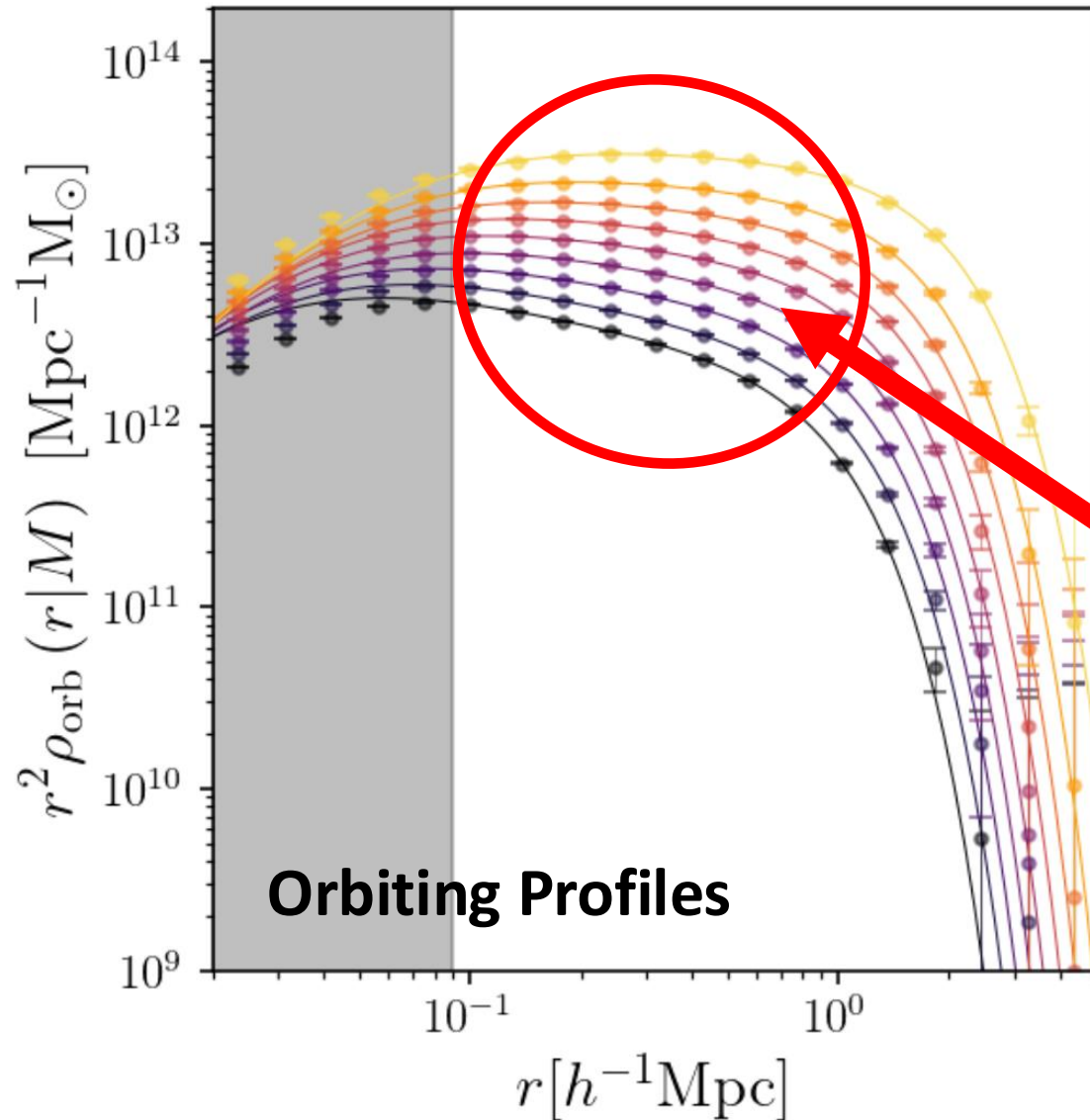
Orbiting profile has a rich phenomenology that may be relevant for SIDM



Orbiting profiles have two parameters

1. Halo radius
 - Exponential truncation scale

Orbiting profile has a rich phenomenology that may be relevant for SIDM



Orbiting profiles have two parameters

1. Halo radius
 - Exponential truncation scale
2. Slope of the inner profile
 - Plays the role of “concentration”
 - Tightly correlated with halo radius at fixed mass!

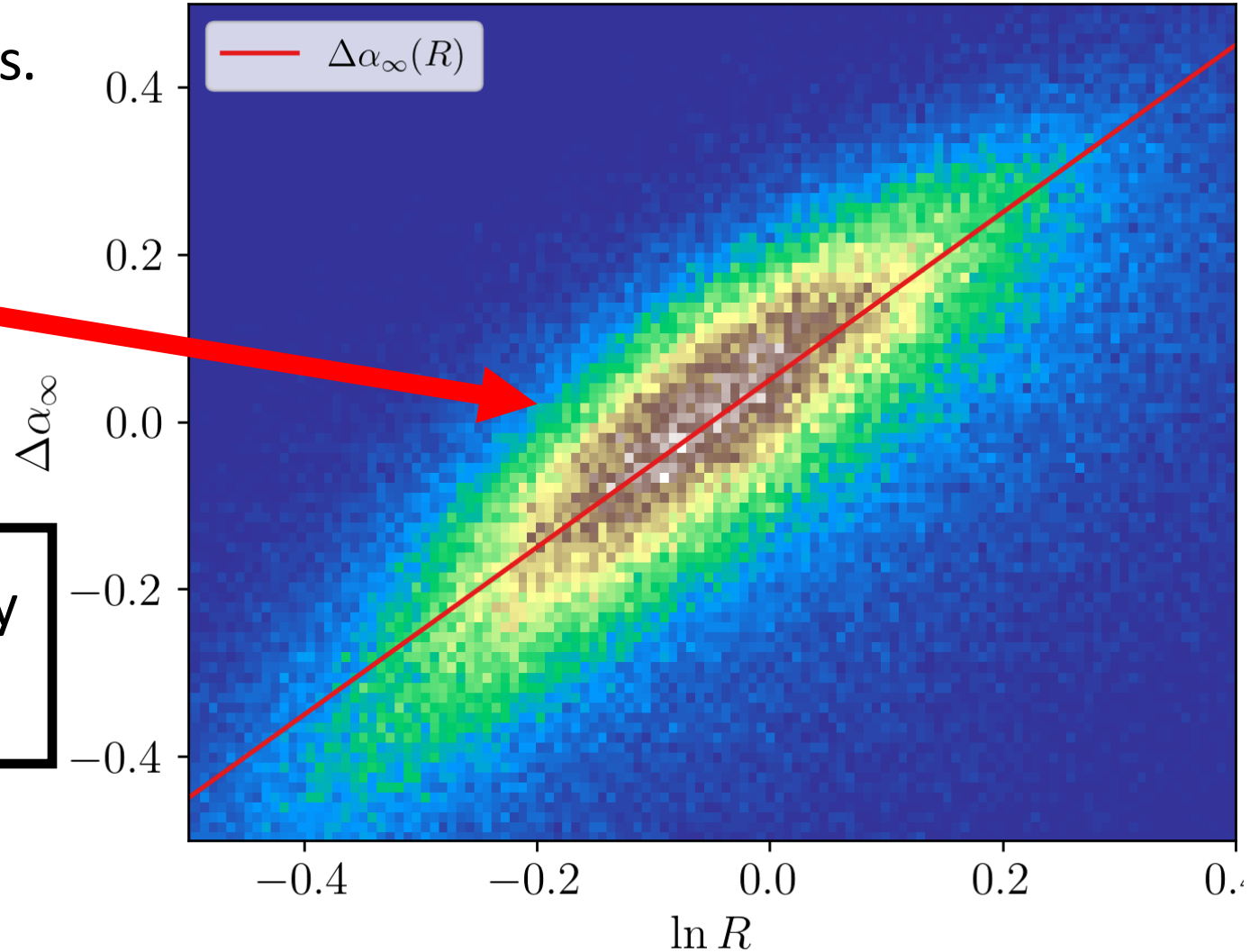
At fixed mass, profiles have one degree of freedom: r_h .

Fit individual halos, and plot slope vs. halo radius.

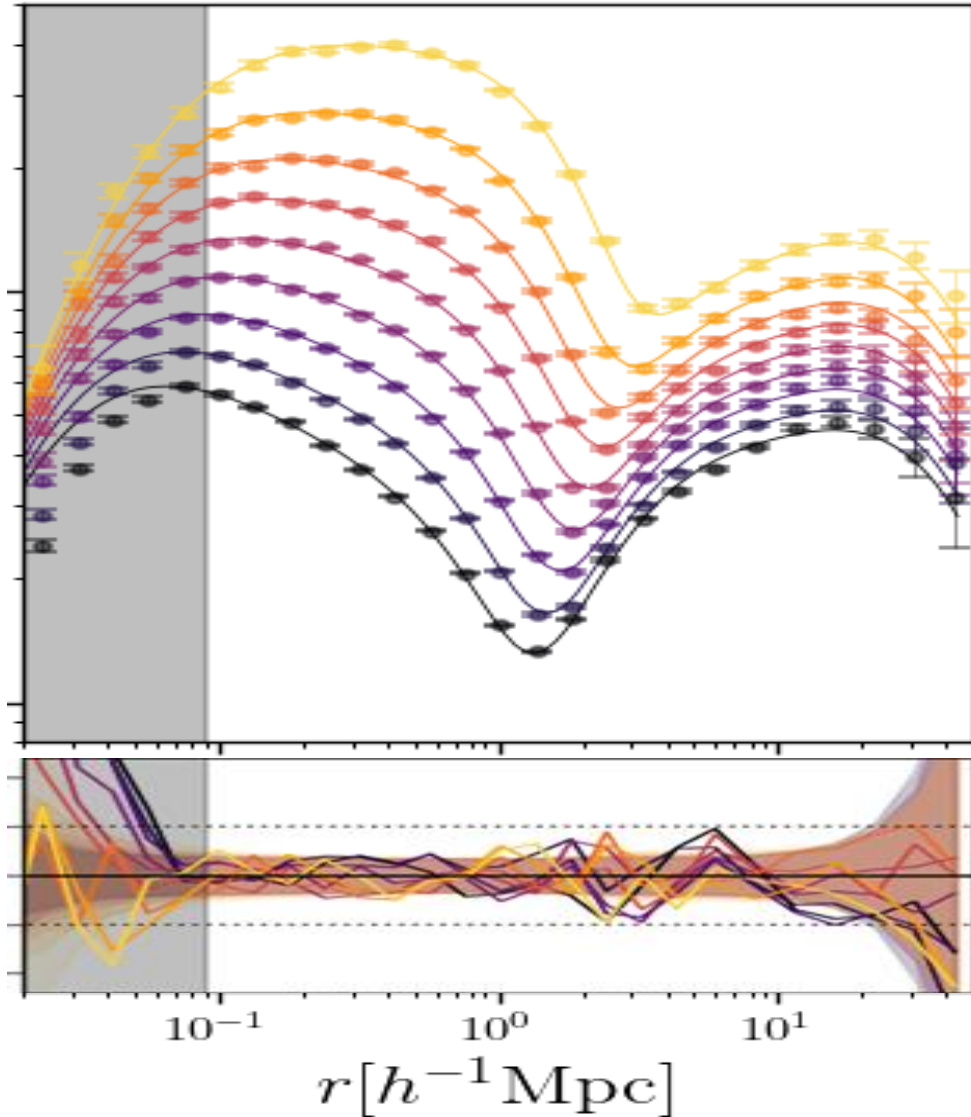
- Profile slope is tightly correlated with halo radius.

Profiles can be described using only one degree of freedom: r_h .

How does this change in SIDM?



Advantage no. 1: **Dynamical halos enable us to build a better halo model**



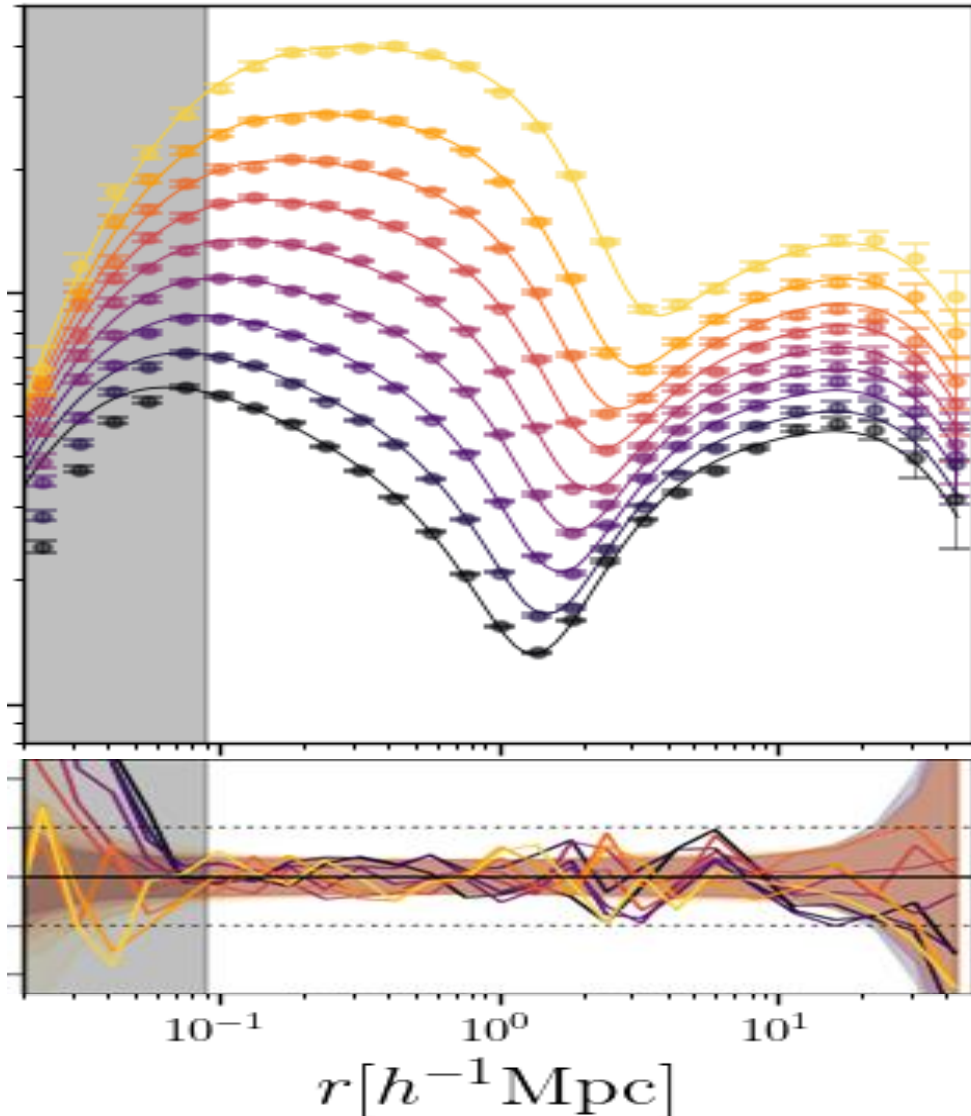
$$\xi_{\text{hm}} = \xi_{\text{hm}}^{1\text{-halo}} + \xi_{\text{hm}}^{2\text{-halo}}$$



$$\rho = \rho_{\text{orb}} + \rho_{\text{inf}}$$

- Revised halo model is accurate to $\approx 2\%$ or better.

Advantage no. 1: Dynamical halos enable us to build a better halo model



Problem: Non-linear growth is treated in an ad-hoc way.

$$\xi_{\text{inf}} = b(1 + \Delta(r))\xi_{\text{LPT-lin}}$$



Power-law: captures non-linear growth

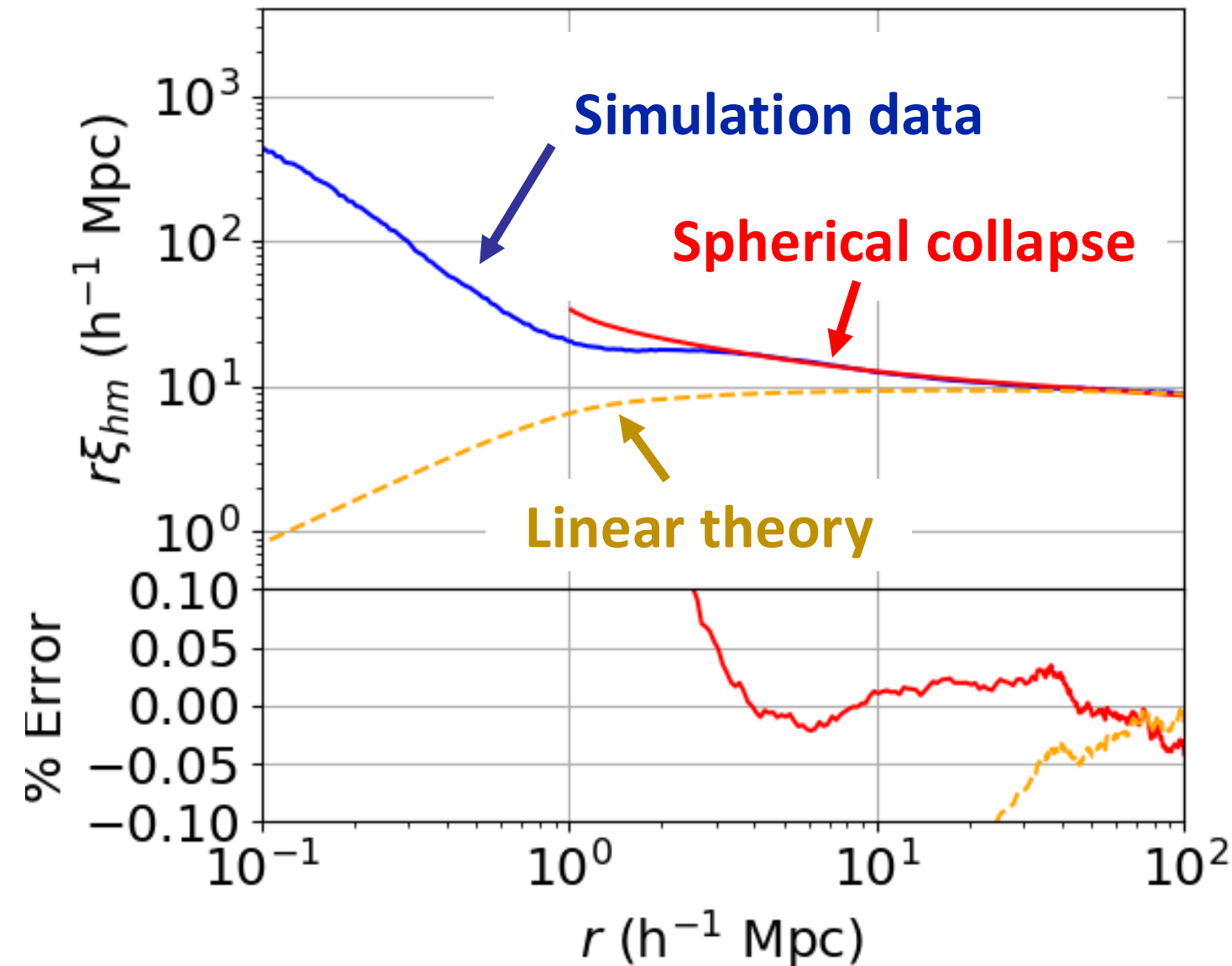
Advantage no. 2: **The dynamical halo framework opens new theoretical avenues.**

Key idea: Non-linear evolution of the density field is due to mass falling in towards the halo.

- We can treat infall analytically using spherical collapse!
- Initial conditions set by linear theory.

Approach trades perturbative limit for spherical symmetry.

$$\Omega_m = 1$$



Spherical collapse accurately models infall profiles.

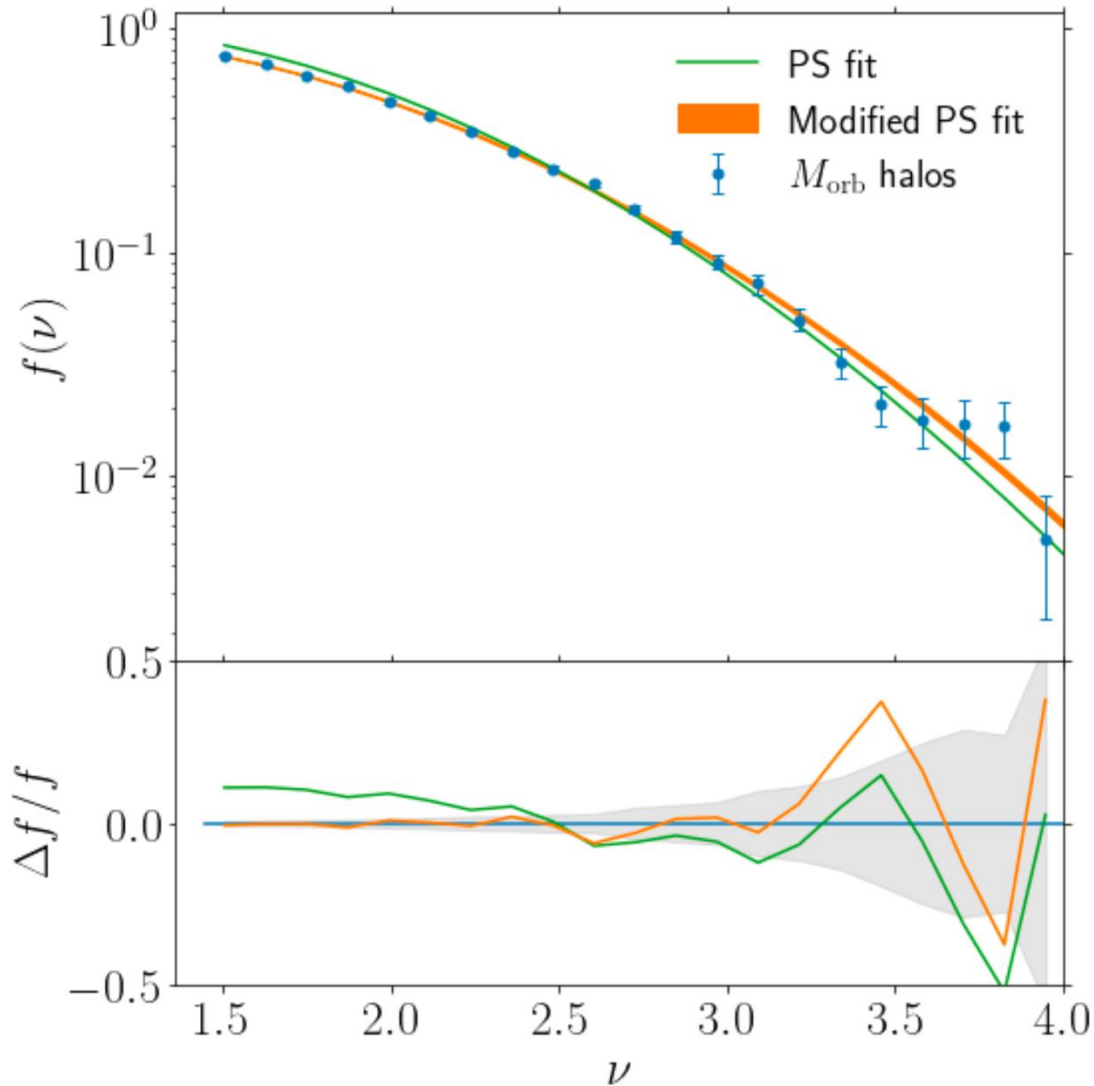
Recovers linear theory on large scales.

Generalization to Λ CDM in progress.

Advantage no. 3: **The Mass Function + Bias of Dynamical Halos is Easier to Model!**

- Spherical collapse predict a Press-Schechter mass function.
- Traditional approach: Identify collapsed mass with spherical overdensity (virial) mass.
- New approach: Identify collapsed mass with orbiting mass.
 - This is a very natural identification!
Formally correct for purely radial orbits!

Advantage no. 3: The Mass Function + Bias of Dynamical Halos is Easier to Model



Excellent agreement with a mass-dependent threshold δ_c .

Find: $\delta_c \in [1.52, 1.68]$

Recovered values of δ_c match expectations (Shapiro et al. 1999).

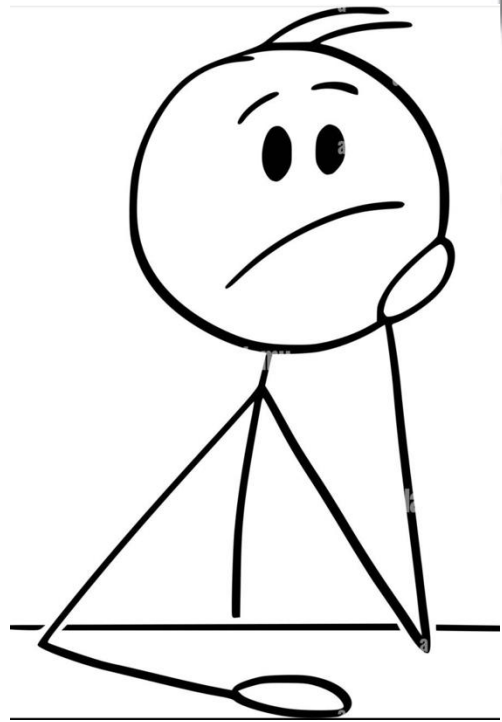
**Halo bias is consistent w/
peak/background split.**



A simple black stick figure stands on the left side of the image. Above its head is a large, cloud-like thought bubble. Inside the bubble, there is text. Three small circles lead from the figure's head to the bubble.

Wow! This is great!

I will only use dynamical halos
from now on!



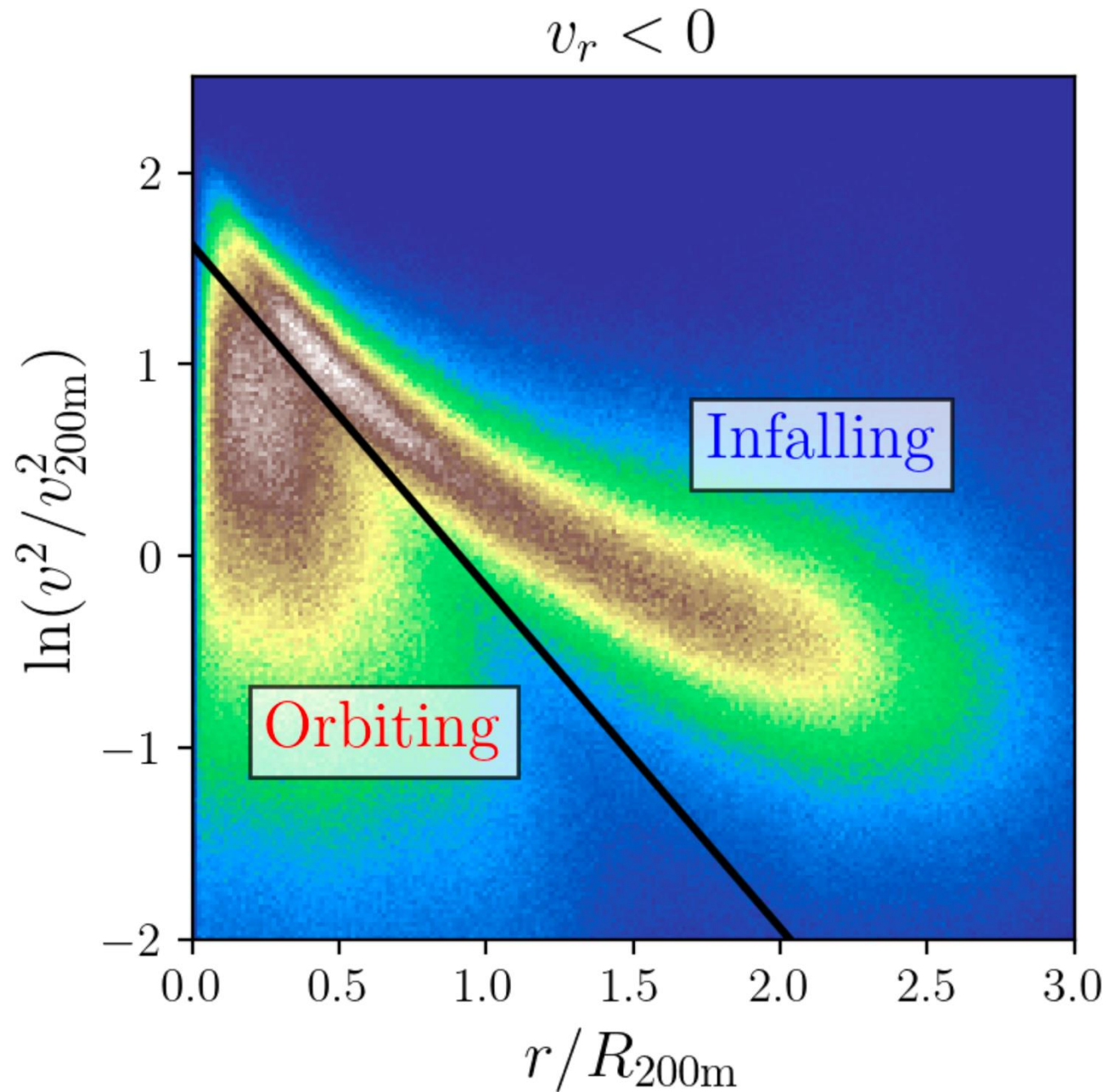
But wait a minute...

This is too much work! I just want
someone to give me the halo
catalogs!



- Parallelized post-processing of Rockstar catalogs to produce a catalog of dynamical halos.

<https://github.com/edgarmsalazar/oasis>

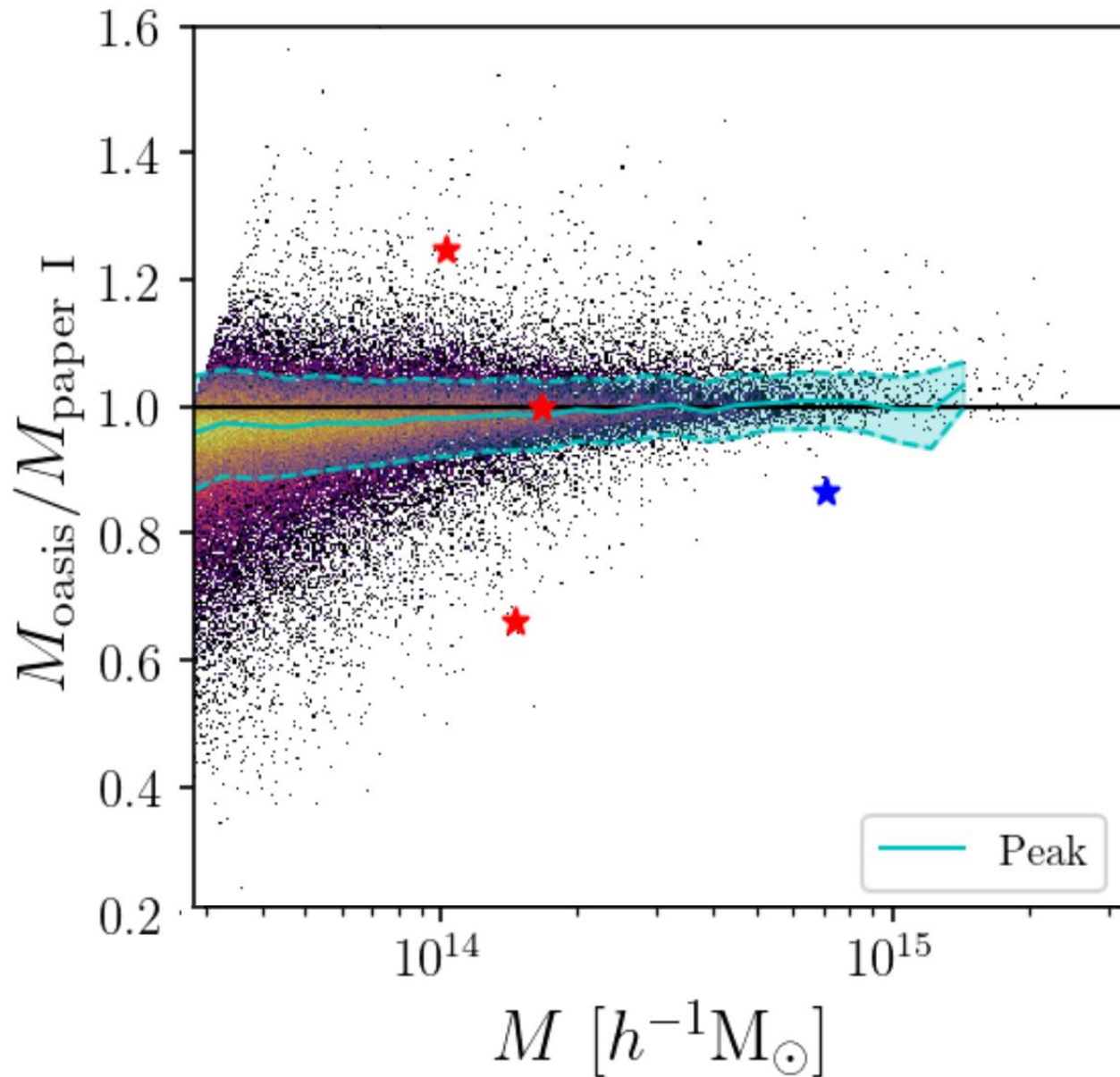


Key idea:

Orbiting particles are (or will be) bound.

- Orbiting particles have less KE than infalling particles!
- Select orbiting particles with a KE energy cut.

KE can be self-calibrated from the simulation.



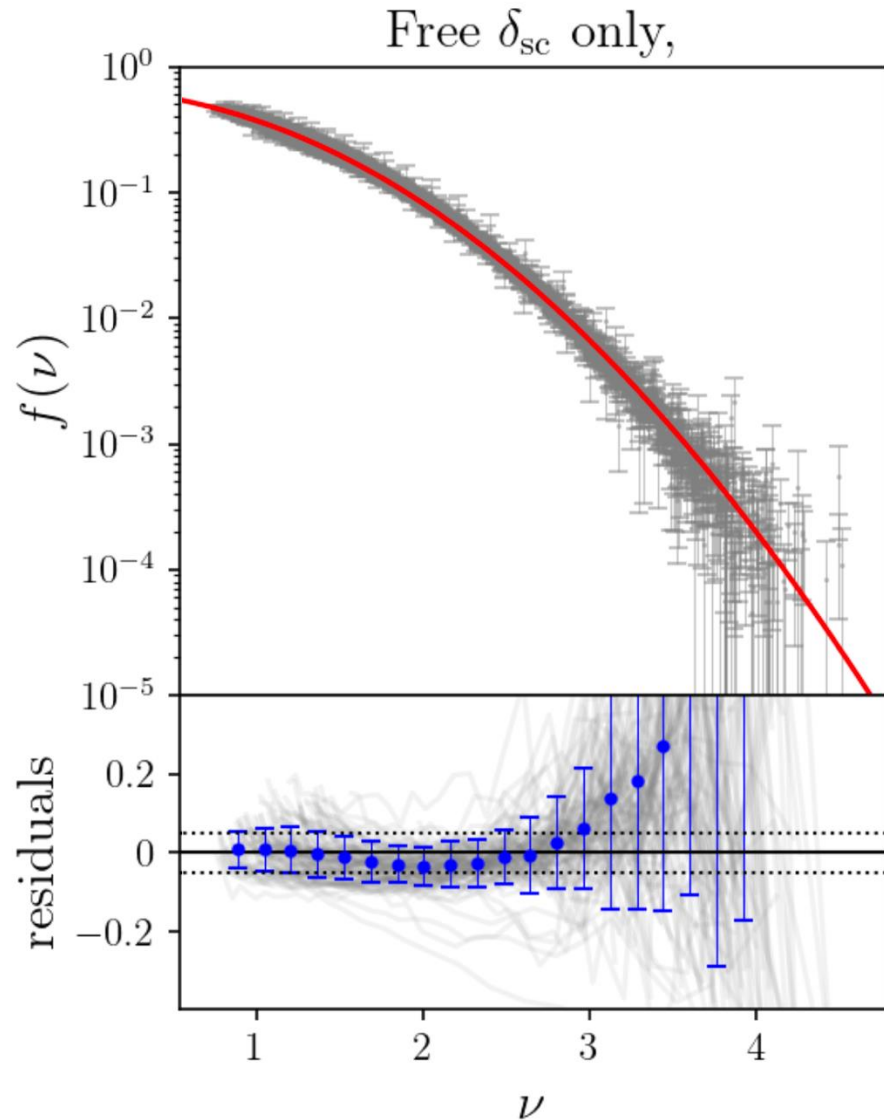
Oasis Results:

- KE and orbit-based masses are tightly correlated.

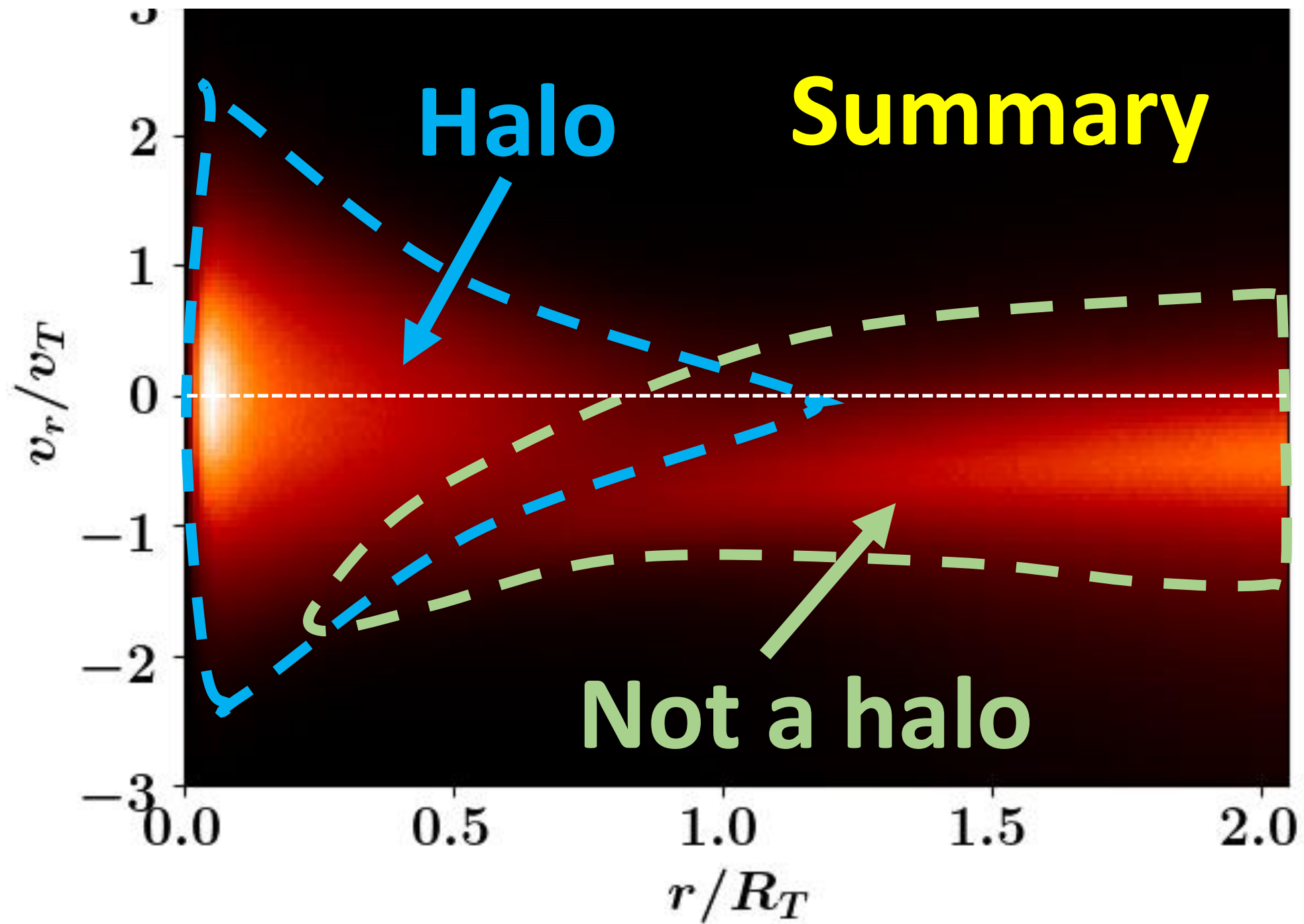
Nearly no offset, and $\approx 4\%$ scatter.

Clearly a step up from spherical overdensity halos!

The Dynamical Halo Mass Function from Oasis



- Measured the mass function for 100 Quijote simulations.
- High mass end is universal and Press-Schechter to within $\approx 5\%$.
- Effective threshold for collapse is $\delta_{\text{sc}} = 1.52$.



Summary

- Halos do not have radial boundaries: rather, *halos should be defined as the collection of all orbiting particles.*

Dynamical halos have many advantages:

- Naturally gives rise the 1-halo/2-halo structure of the halo model.
- Orbiting profile has a single degree of freedom: *the halo radius.*
- Infall profile can be modelled using spherical collapse (in progress).
- Improves agreement between simulations and Press-Schechter

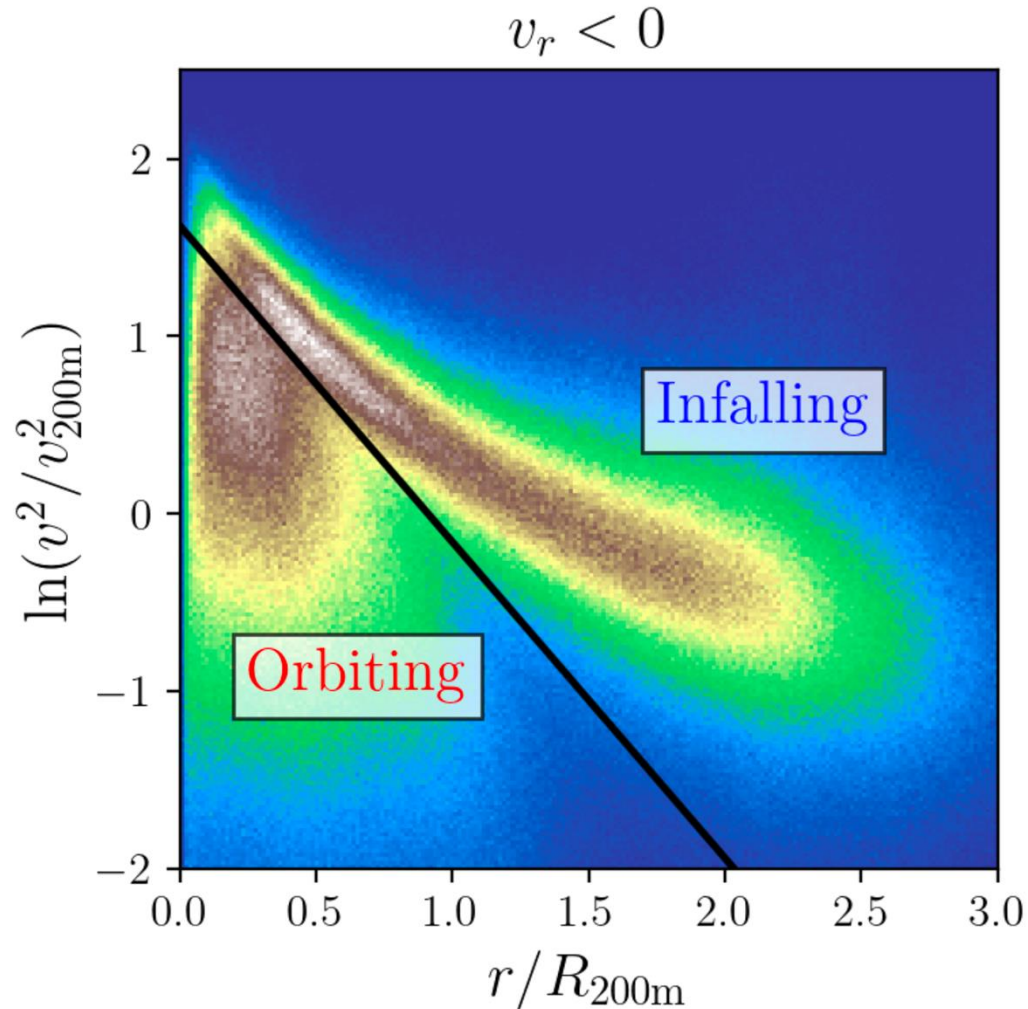


Developed a fast algorithm to generate dynamical halo catalogs from simulations.

<https://github.com/edgarmsalazar/oasis>

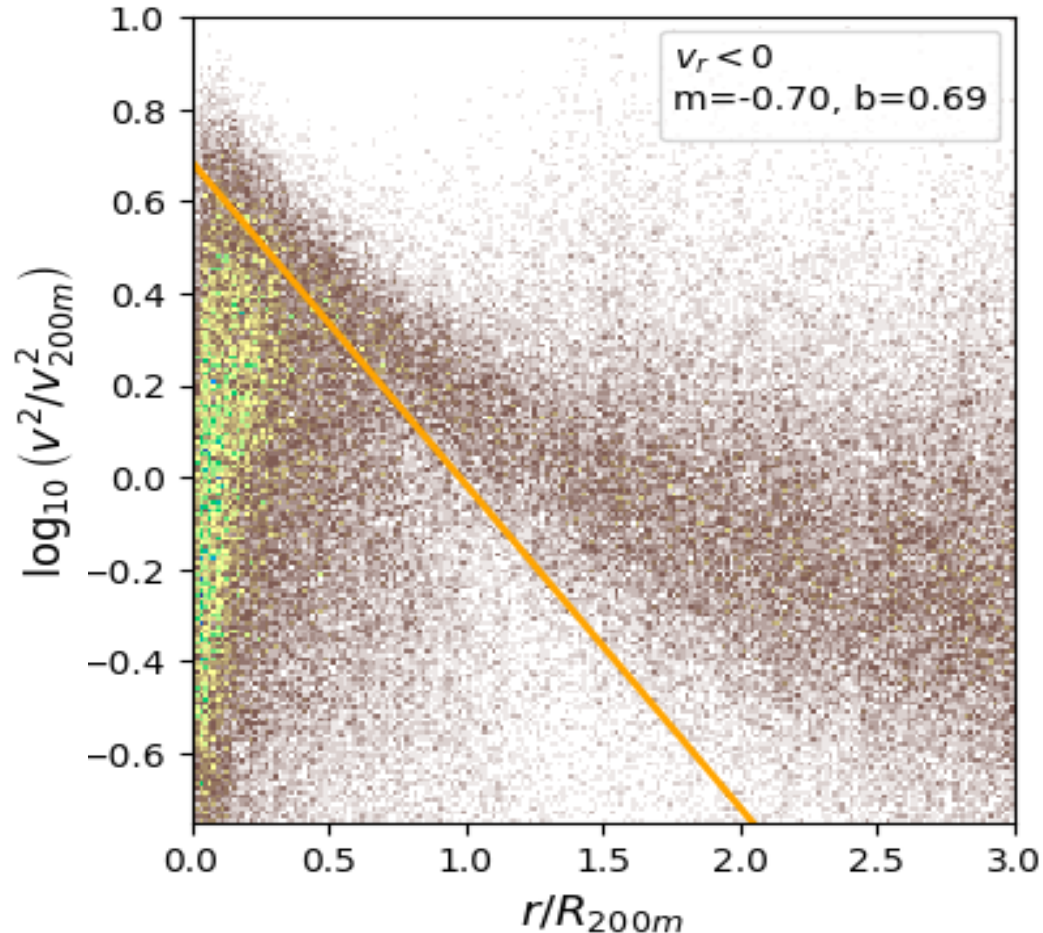
Extra Slides

Will Baryons Mess Everything Up?



- Orbiting/infall split is well motivated for DM particles.
- Does this kind of thinking even make sense for baryons?

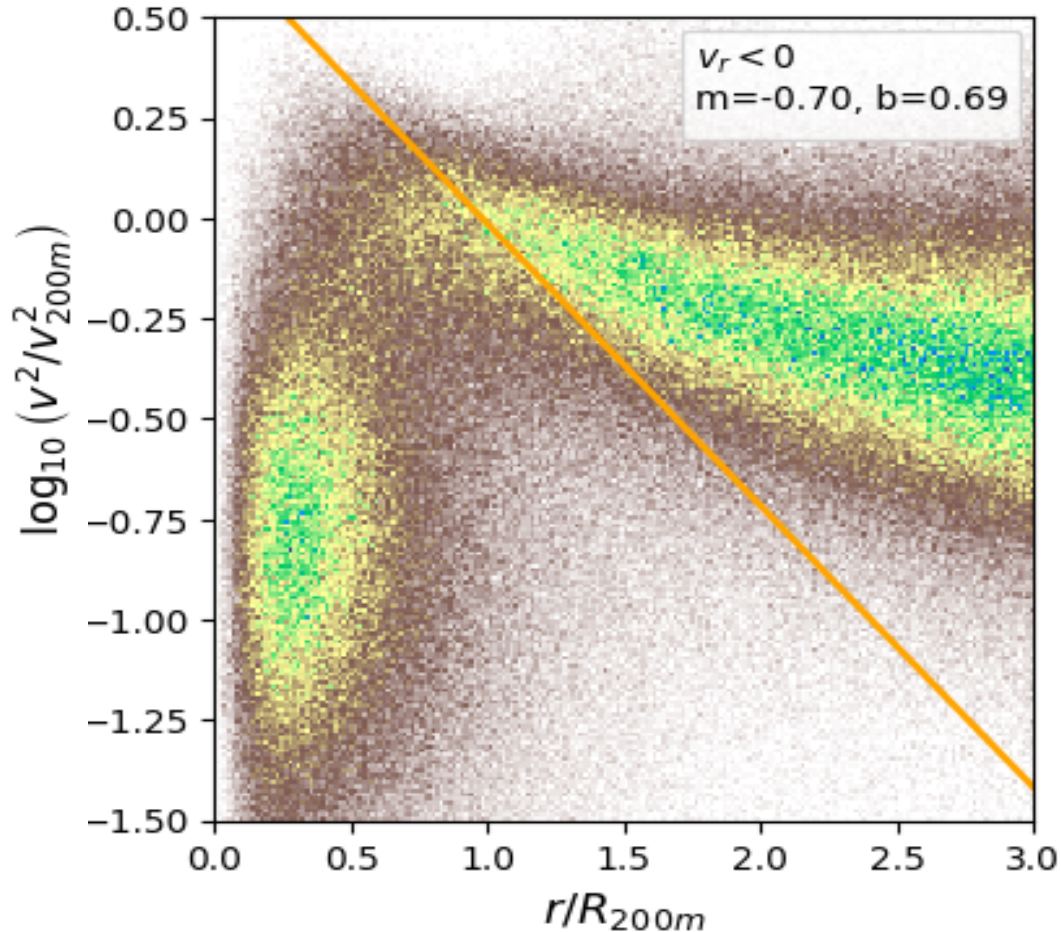
Baryons Can Be Accommodated!



- Stars are collisionless, so they behave similarly to dark matter.

Baryons Can Be Accommodated!

Y-axis scale changed



- Stars are collisionless, so they behave similarly to dark matter.
- Infall gas hits the halo atmosphere and comes to “rest”
 - KE cuts are even *cleaner* with gas particles!

Expect the orbiting/infall framework will generalize to Λ CDMB.