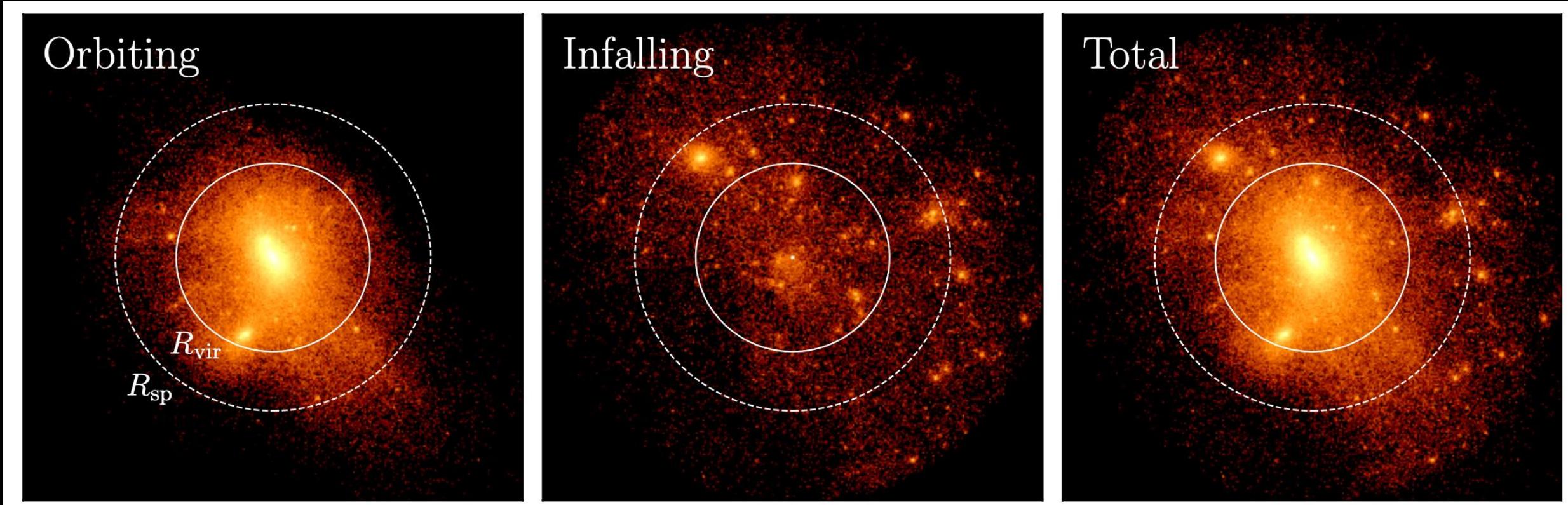


# Dynamical Halos are Better!



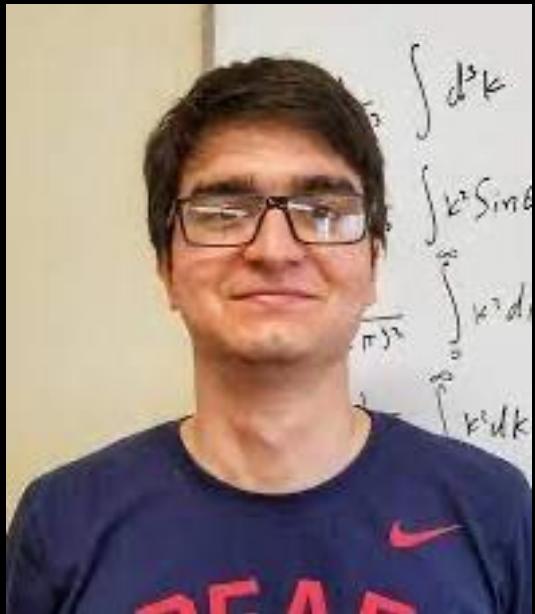
Eduardo Rozo



Valencia Workshop on the Small-Scale Structure of the  
Universe and Self-Interacting Dark Matter

Valencia, Spain, July 2025

Bulk of the work shown here was performed by:



Rafael Garcia



Edgar Salzar



Hengwei Chang



Tristen Shields

In collaboration with:

Benedikt Diemer

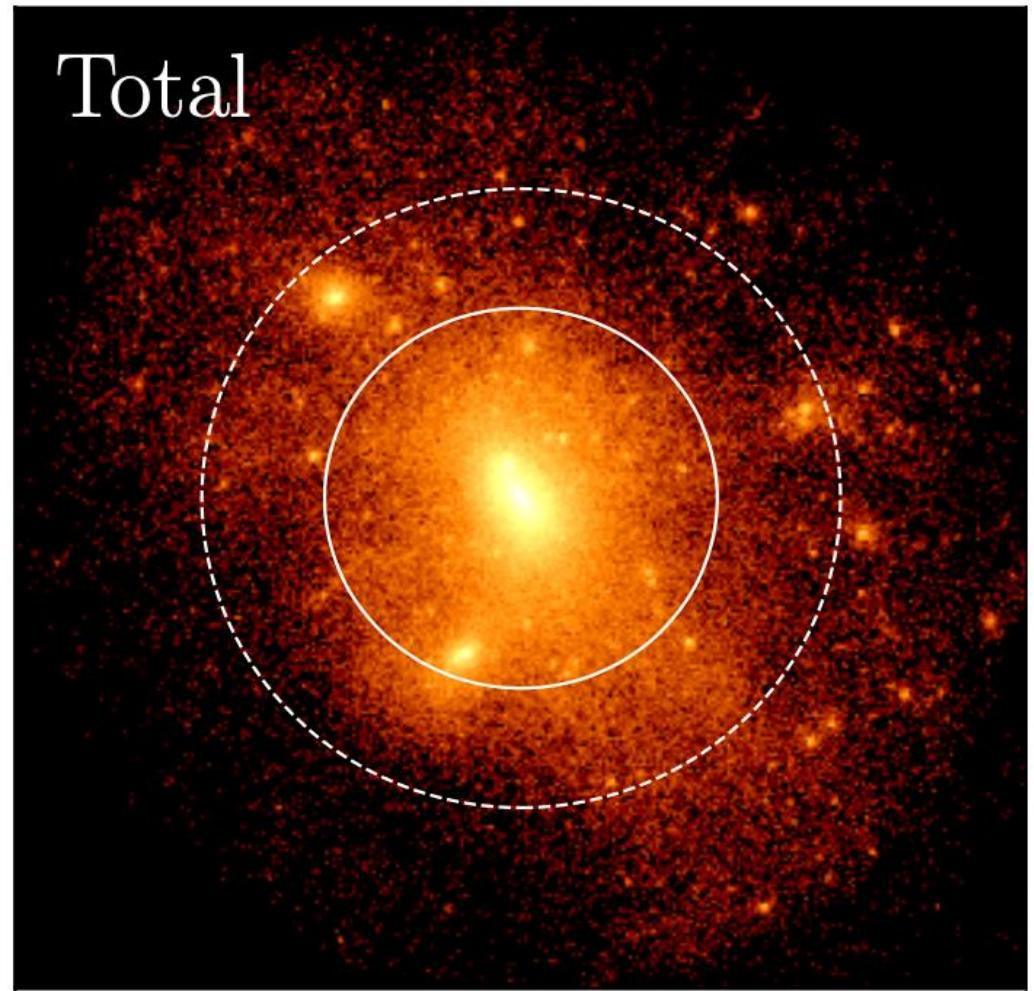
Vladimir Ze'ev

Calvin Onsaga

Susmita Adhikari

**what is a halo?**

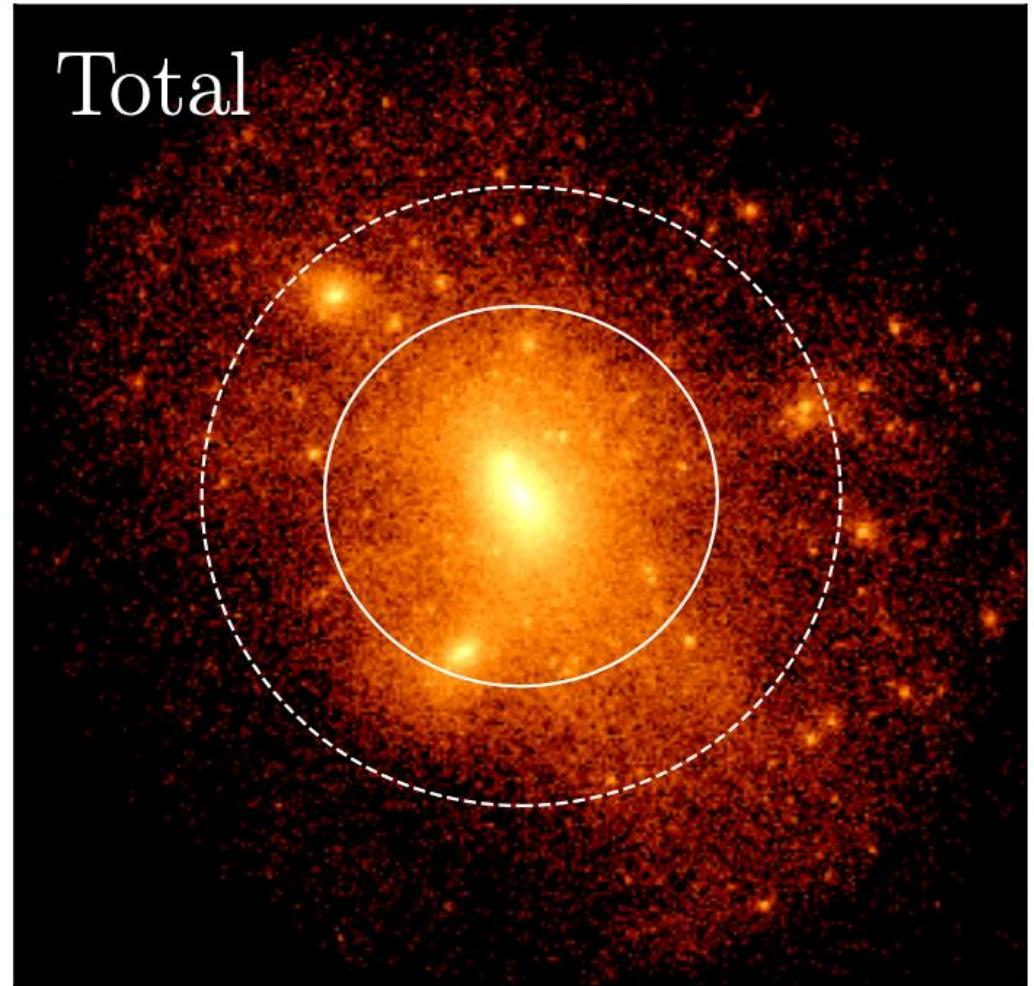
**This is a halo.**



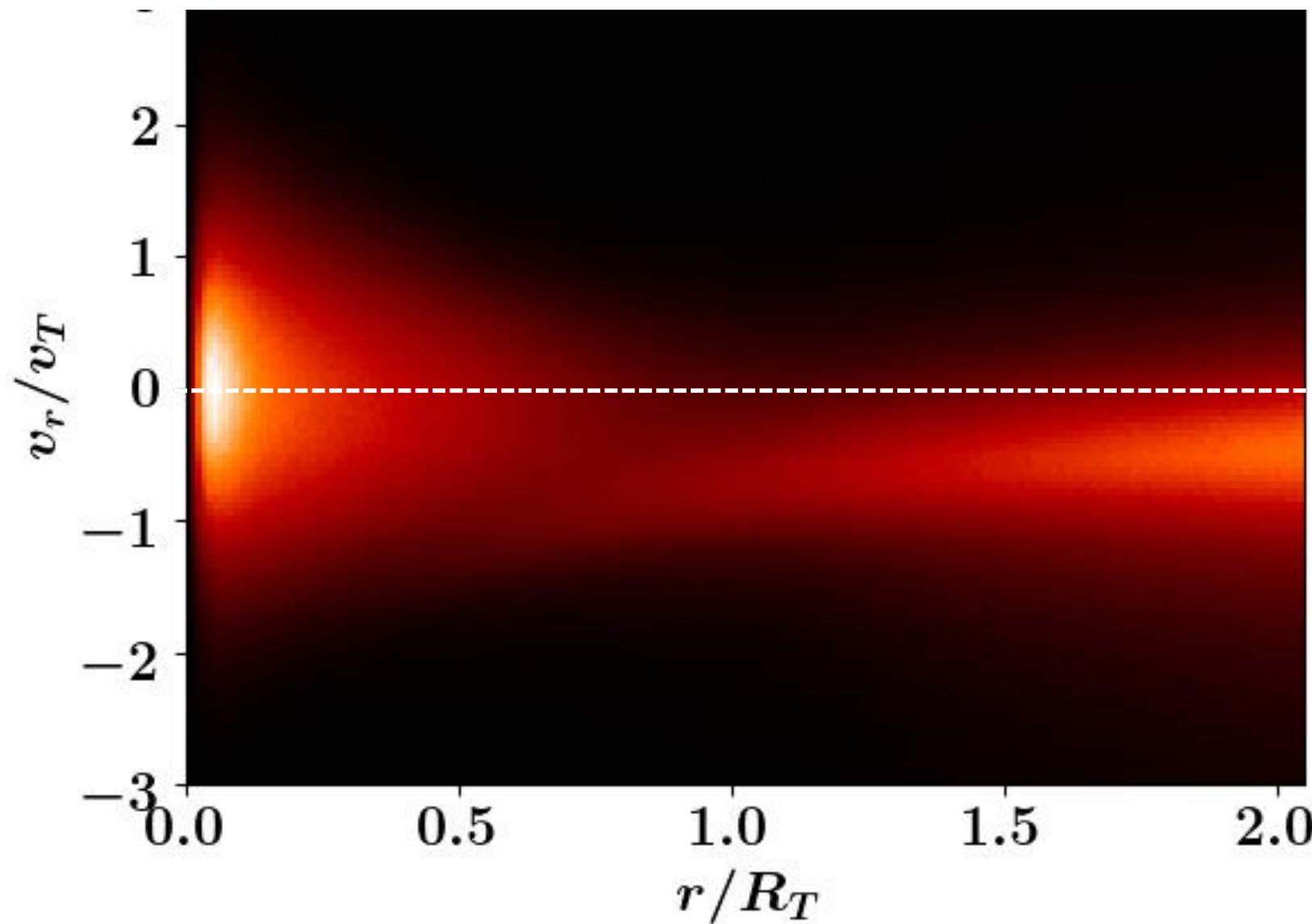
**This is a halo.**

**Question:**

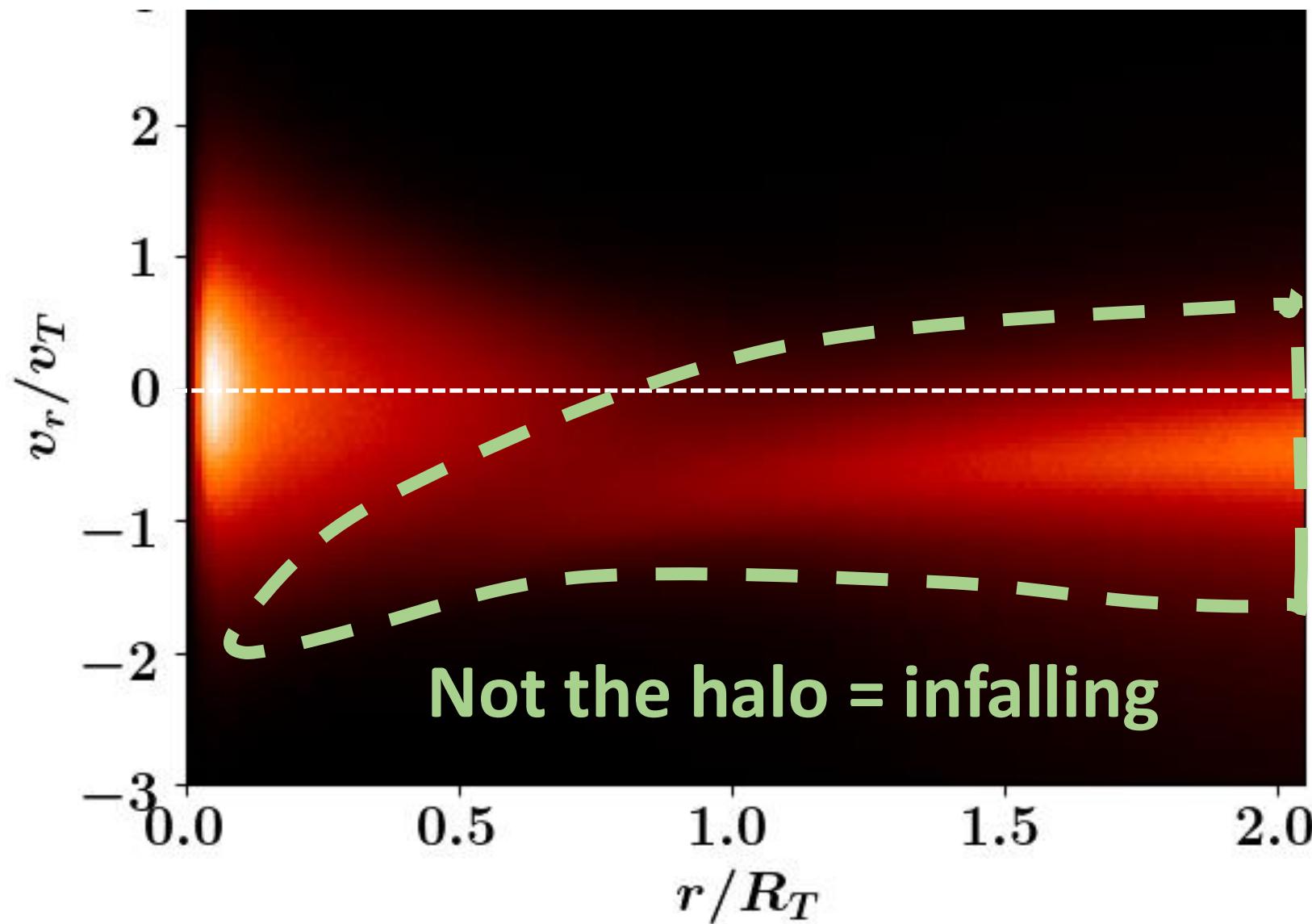
Which particles belong to the halo, and which don't?



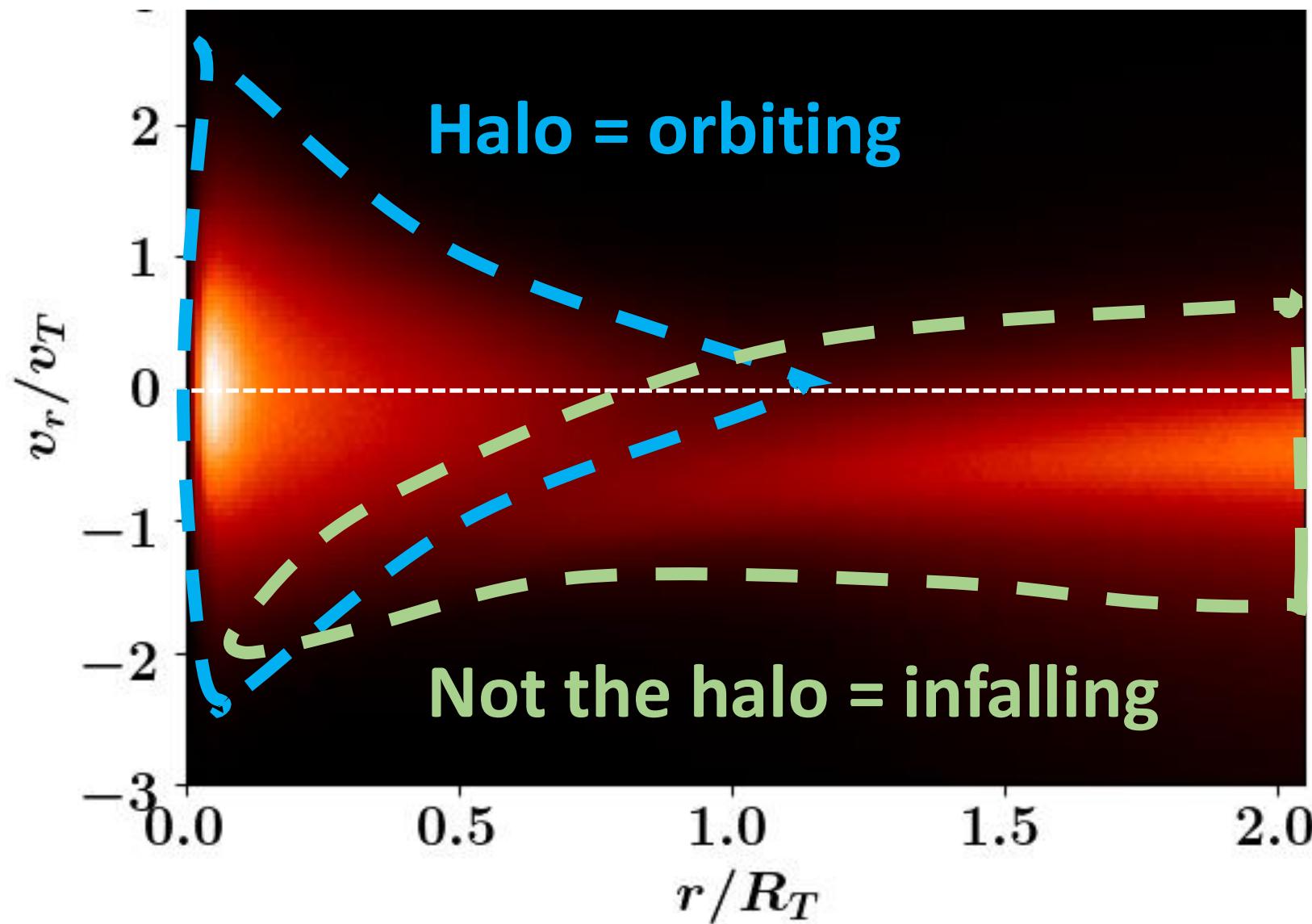
**The halo is easy to see in phase space!**



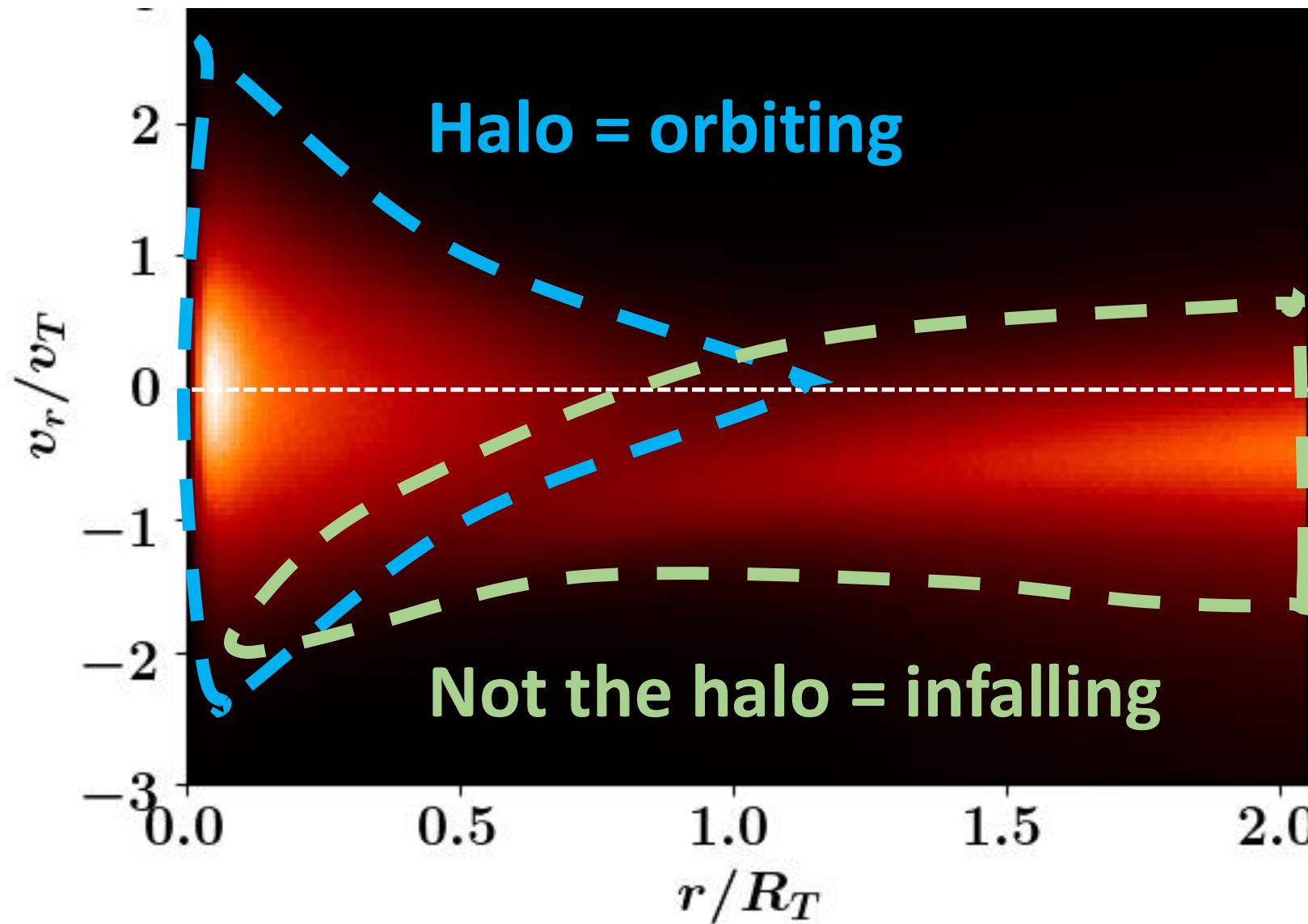
# The halo is easy to see in phase space!



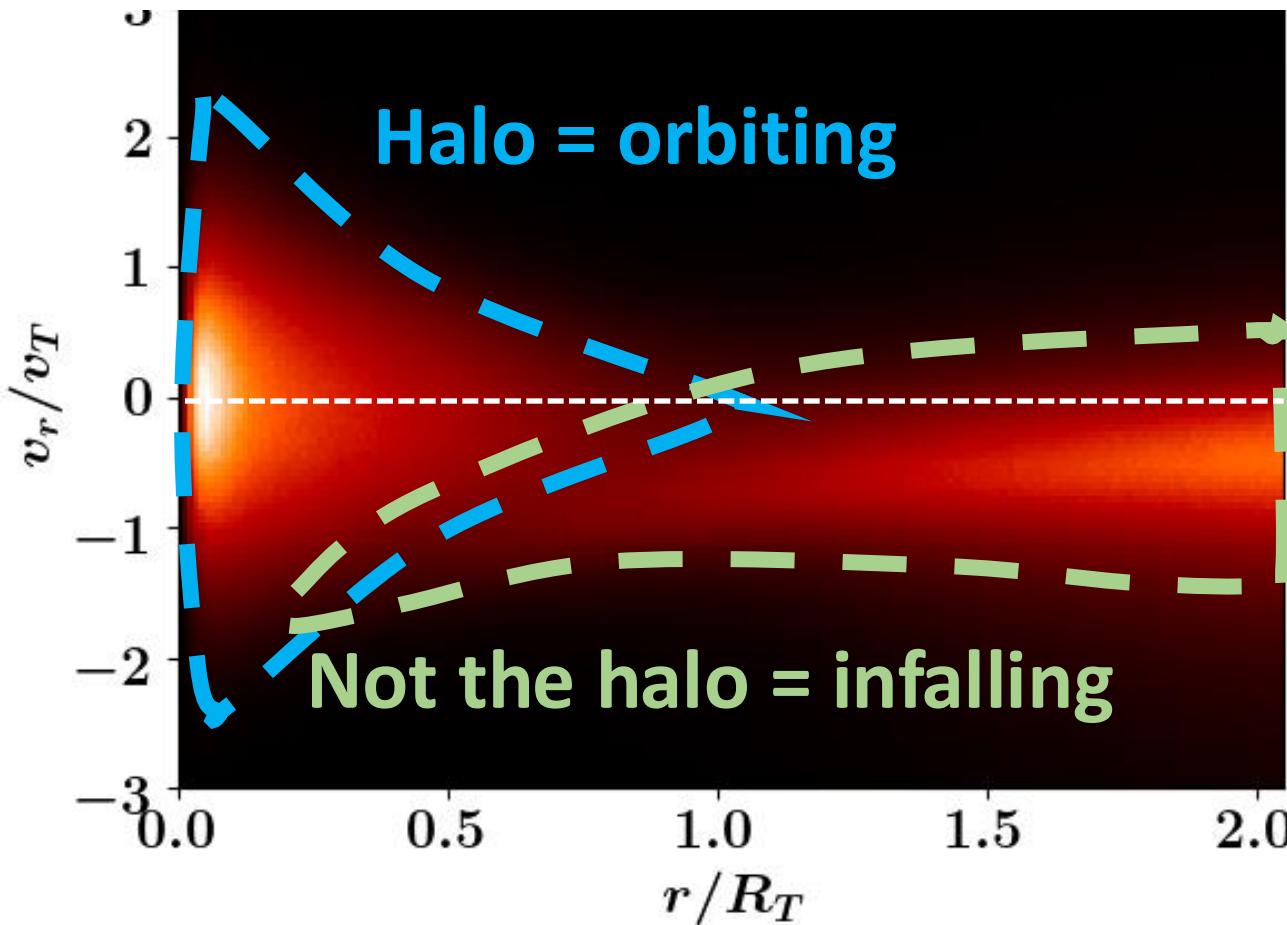
# The halo is easy to see in phase space!



There is no radial boundary that cleanly separates halo from non-halo particles.



There is no radial boundary that cleanly separates halo from non-halo particles.



Need a way to selected “orbiting” particles.

**Example:**

A particle is “orbiting” if it has had a pericentric passage.

➤ Requires particle tracking: this is resource intensive!

Proposed definition:

A dynamical halo is the collection of particles orbiting their self-generated potential.

This talk:

**Are there any advantages to foregoing the idea of a halo boundary?**

Proposed definition: A dynamical halo is the collection of particles orbiting their self-generated potential.

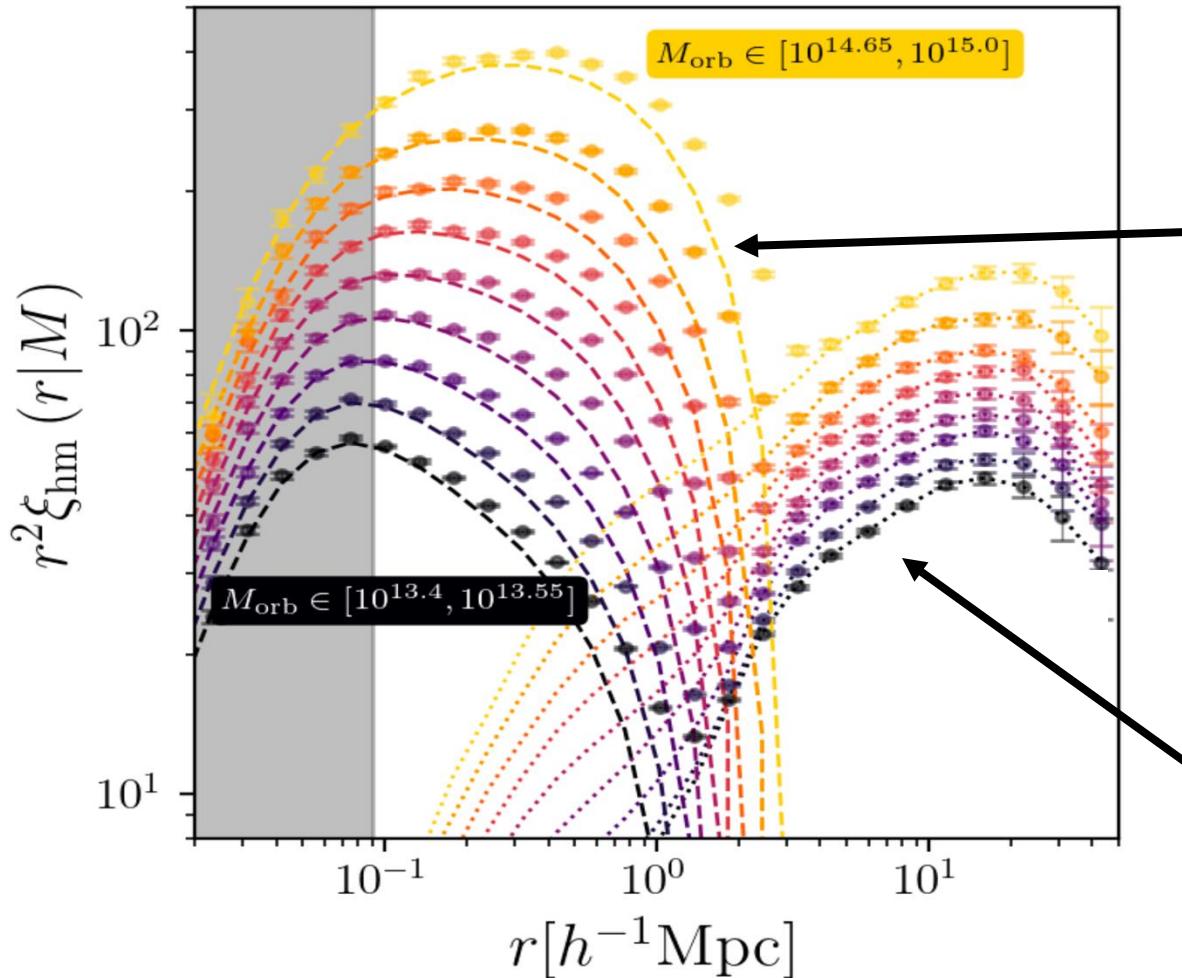
This talk:

Are there any advantages to foregoing the idea of a halo boundary?

Yes.

Advantage no. 1:

# Dynamical halos enable us to build a better halo model

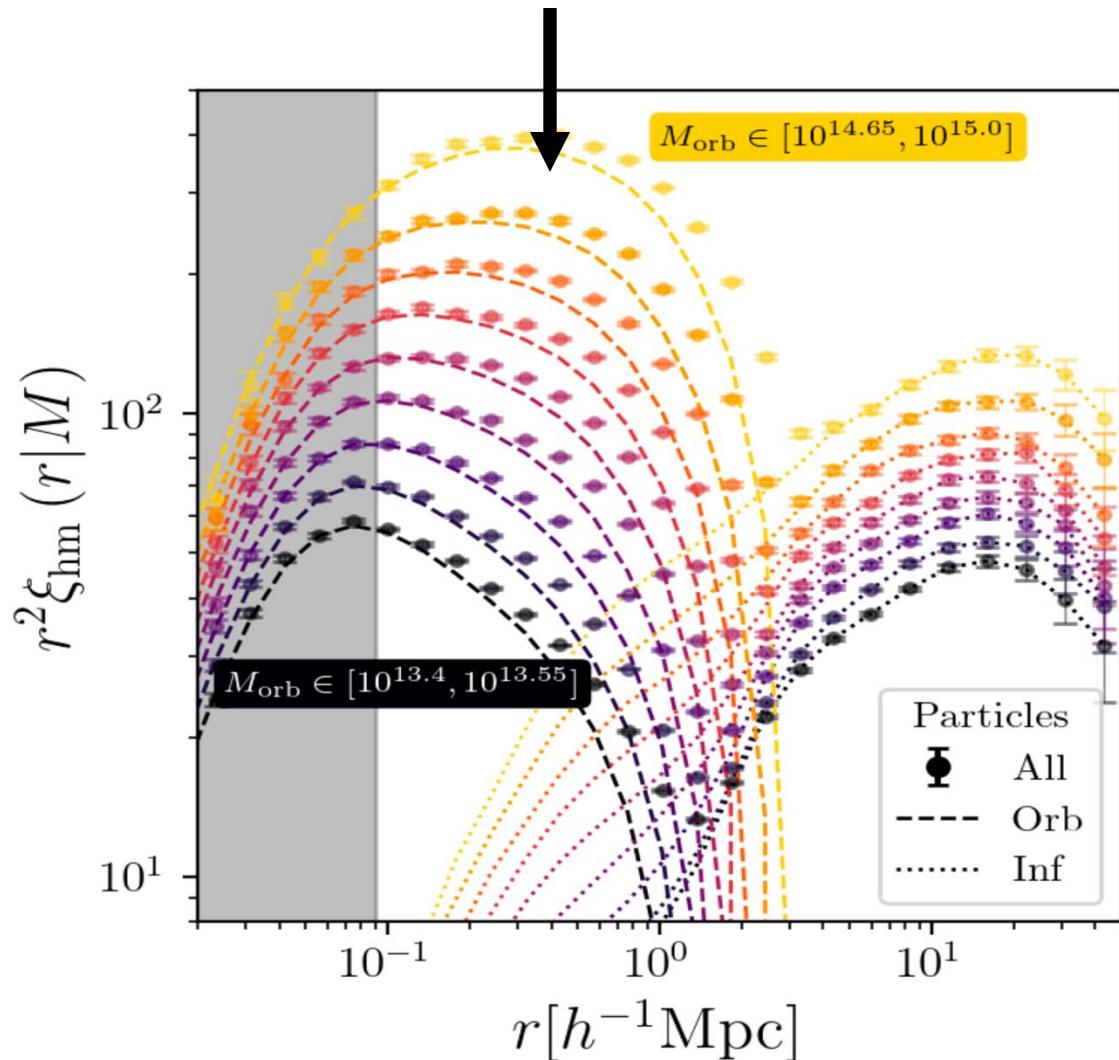


Points w/ error bars: simulation data.

Dashed lines: *orbiting particles*.

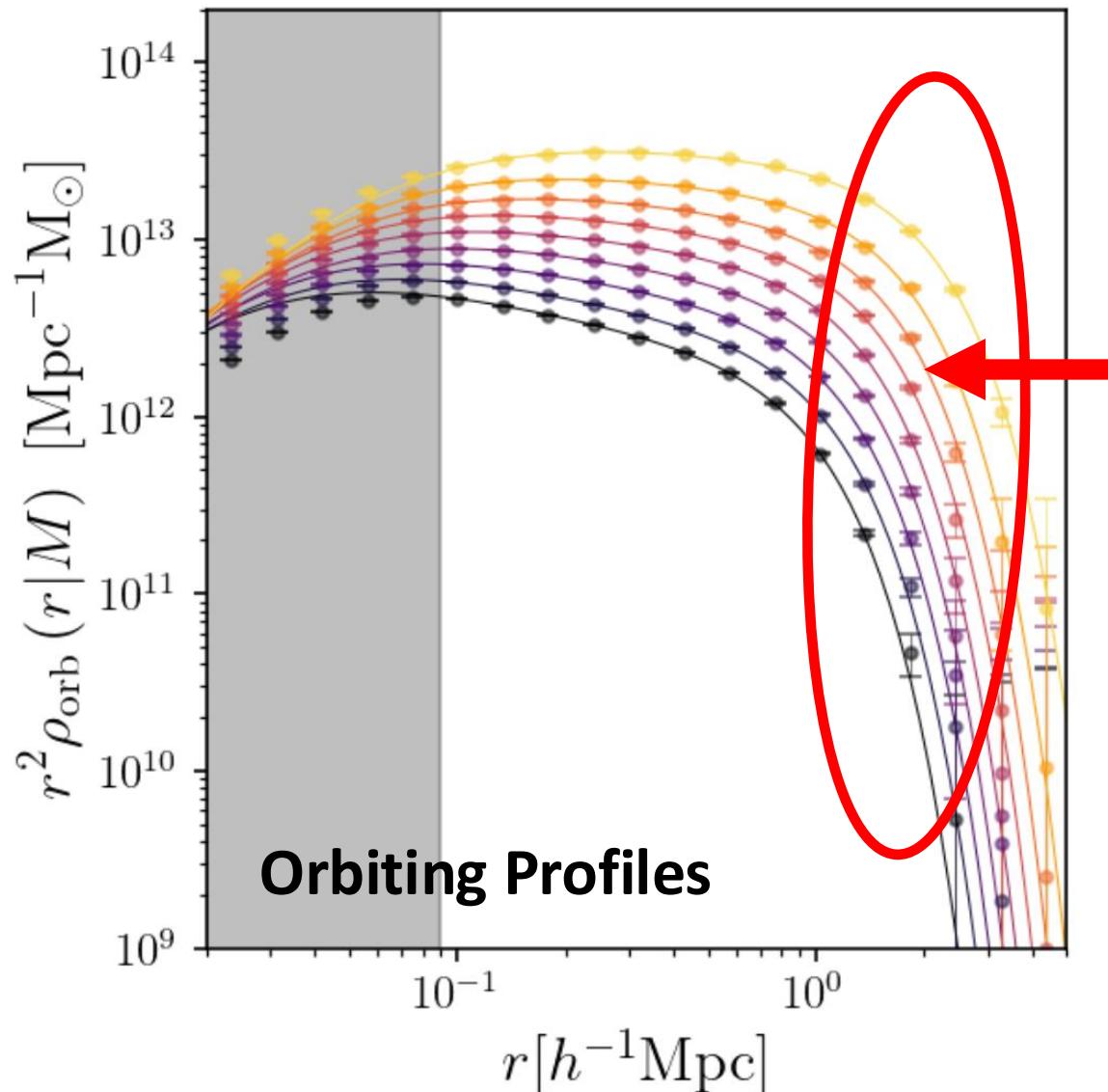
Dotted lines: *infalling particles*.

# Halos are not NFW!



- Halo concentration is in part due to to *infall* material.
- Infall material has never interacted with the core
- The c-M relation may not be the most useful way of talking about SIDM.

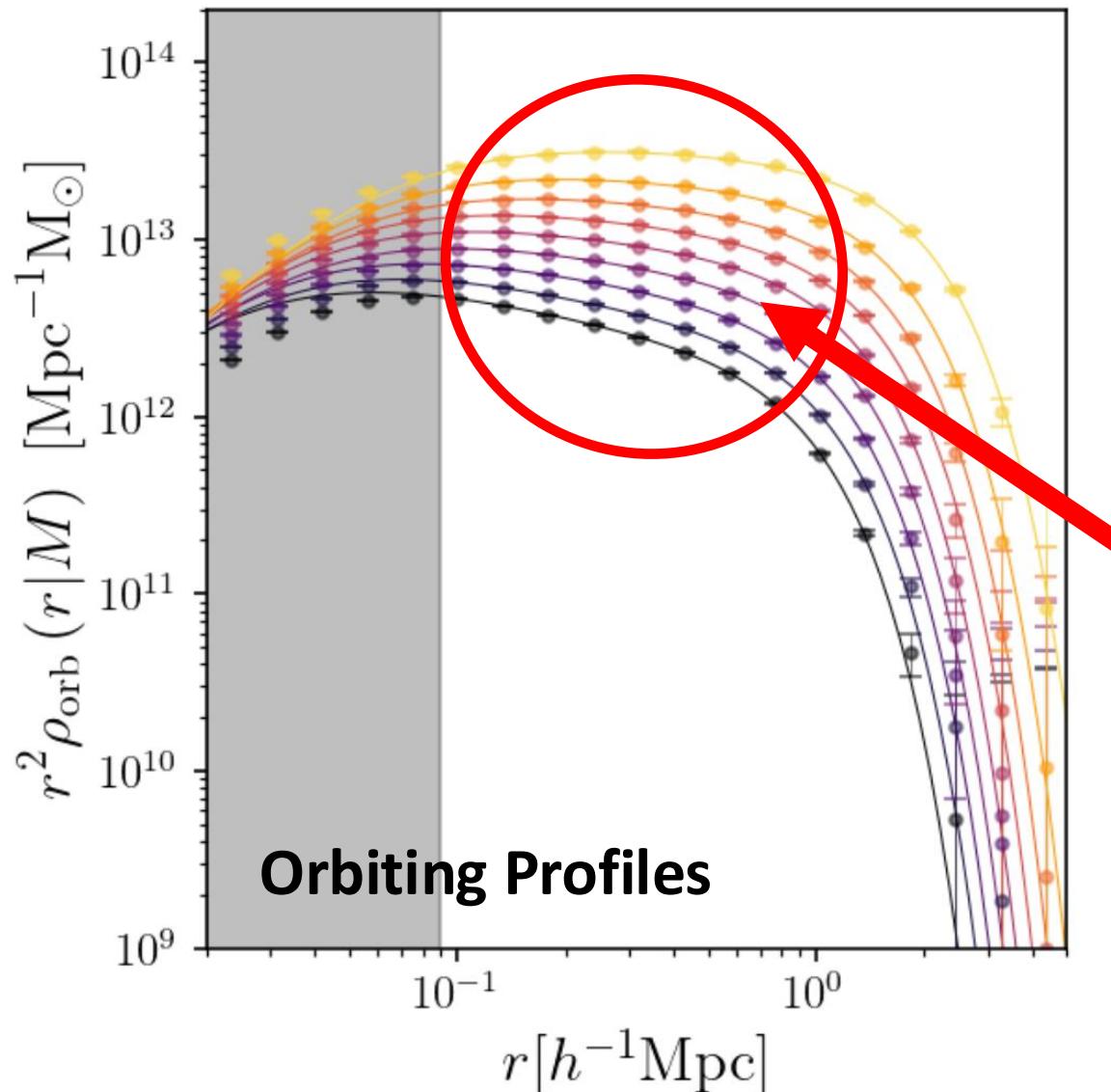
# Orbiting profile has a rich phenomenology that may be relevant for SIDM



Orbiting profiles have two parameters

1. Halo radius
  - Exponential truncation scale

# Orbiting profile has a rich phenomenology that may be relevant for SIDM



Orbiting profiles have two parameters

1. Halo radius
  - Exponential truncation scale
2. Slope of the inner profile
  - Plays the role of “concentration”
  - Tightly correlated with halo radius at fixed mass!

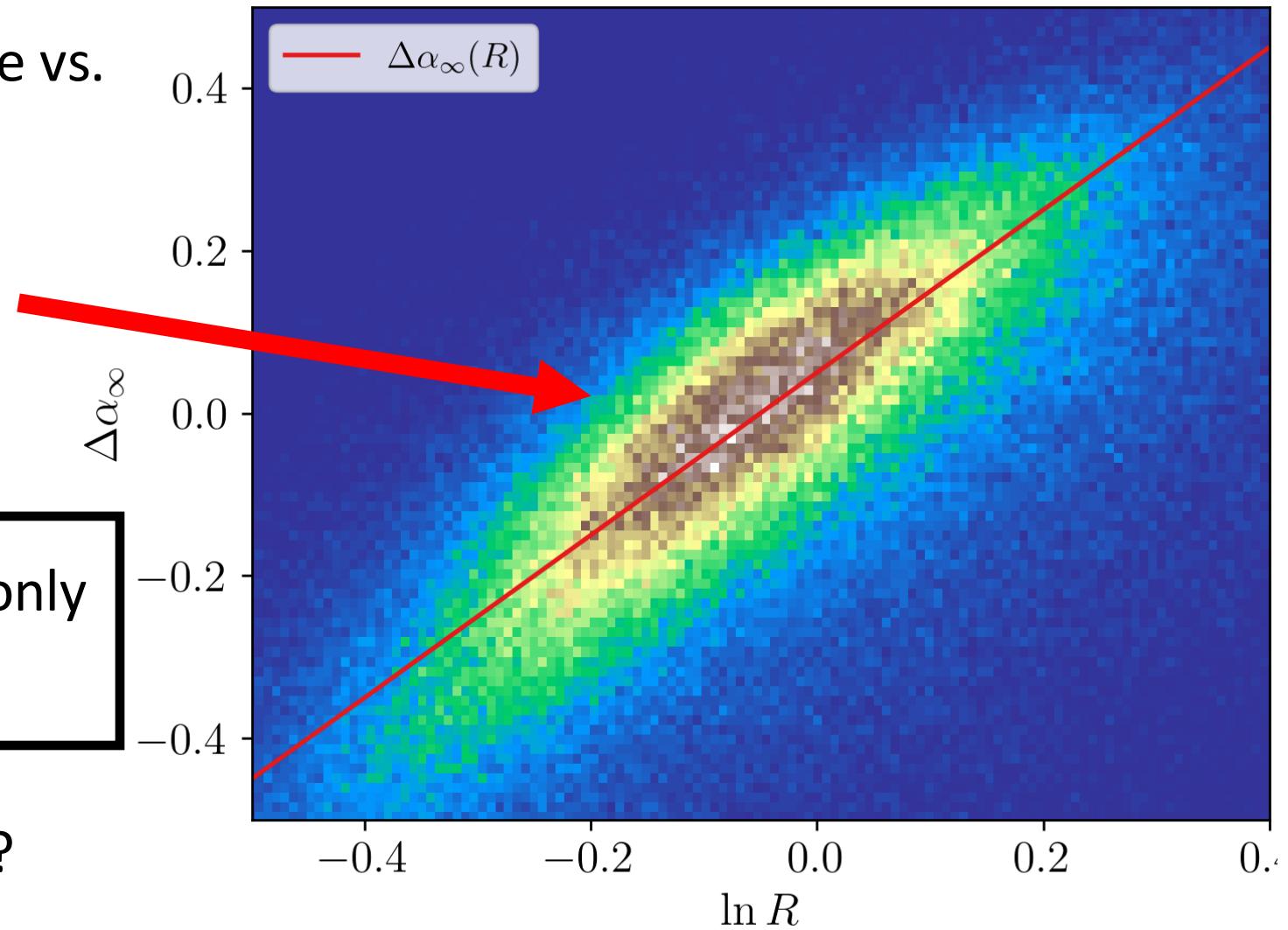
# At fixed mass, profiles have one degree of freedom: $r_h$ .

Fit individual halos, and plot slope vs. halo radius.

- Profile slope is tightly correlated with halo radius.

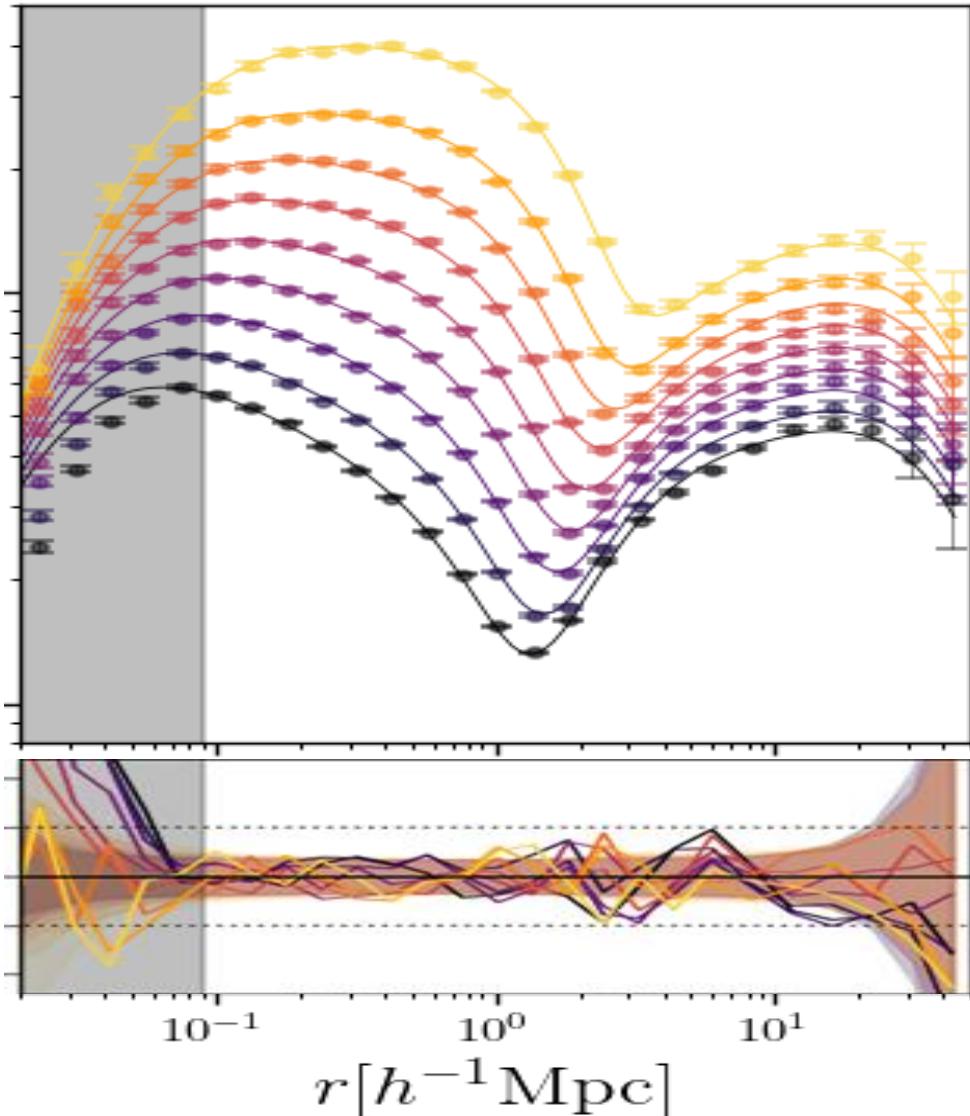
Profiles can be described using only one degree of freedom:  $r_h$ .

How does this change in SIDM?



Advantage no. 1:

## Dynamical halos enable us to build a better halo model



$$\xi_{\text{hm}} = \xi_{\text{hm}}^{1-\text{halo}} + \xi_{\text{hm}}^{2-\text{halo}}$$

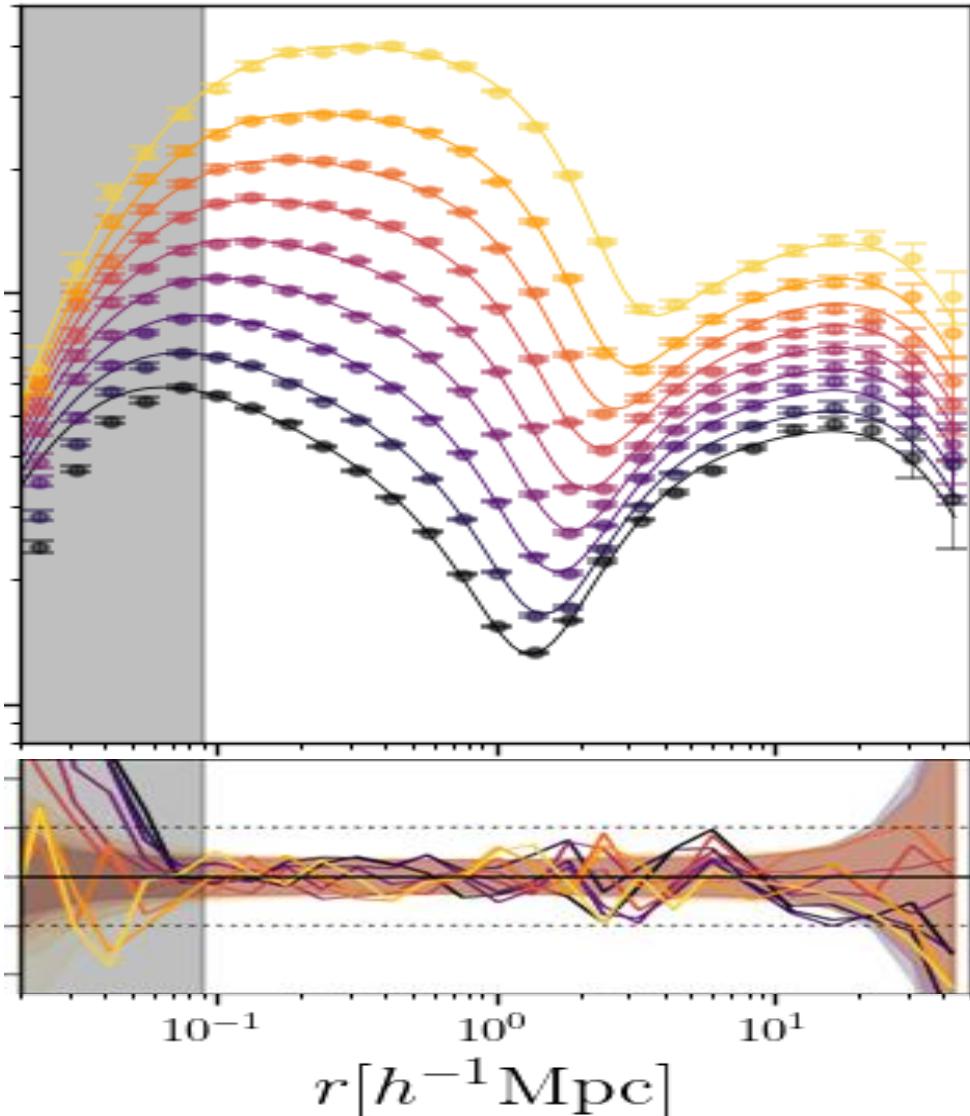
↓

$$\rho = \rho_{\text{orb}} + \rho_{\text{inf}}$$

- Revised halo model is accurate to  $\approx 2\%$  or better.

Advantage no. 1:

## Dynamical halos enable us to build a better halo model



**Problem:** Non-linear growth is treated in an ad-hoc way.

$$\xi_{\text{inf}} = b(1 + \Delta(r))\xi_{\text{LPT-lin}}$$



Power-law: captures non-liner growth

Advantage no. 2:

**The dynamical halo framework opens new theoretical avenues.**

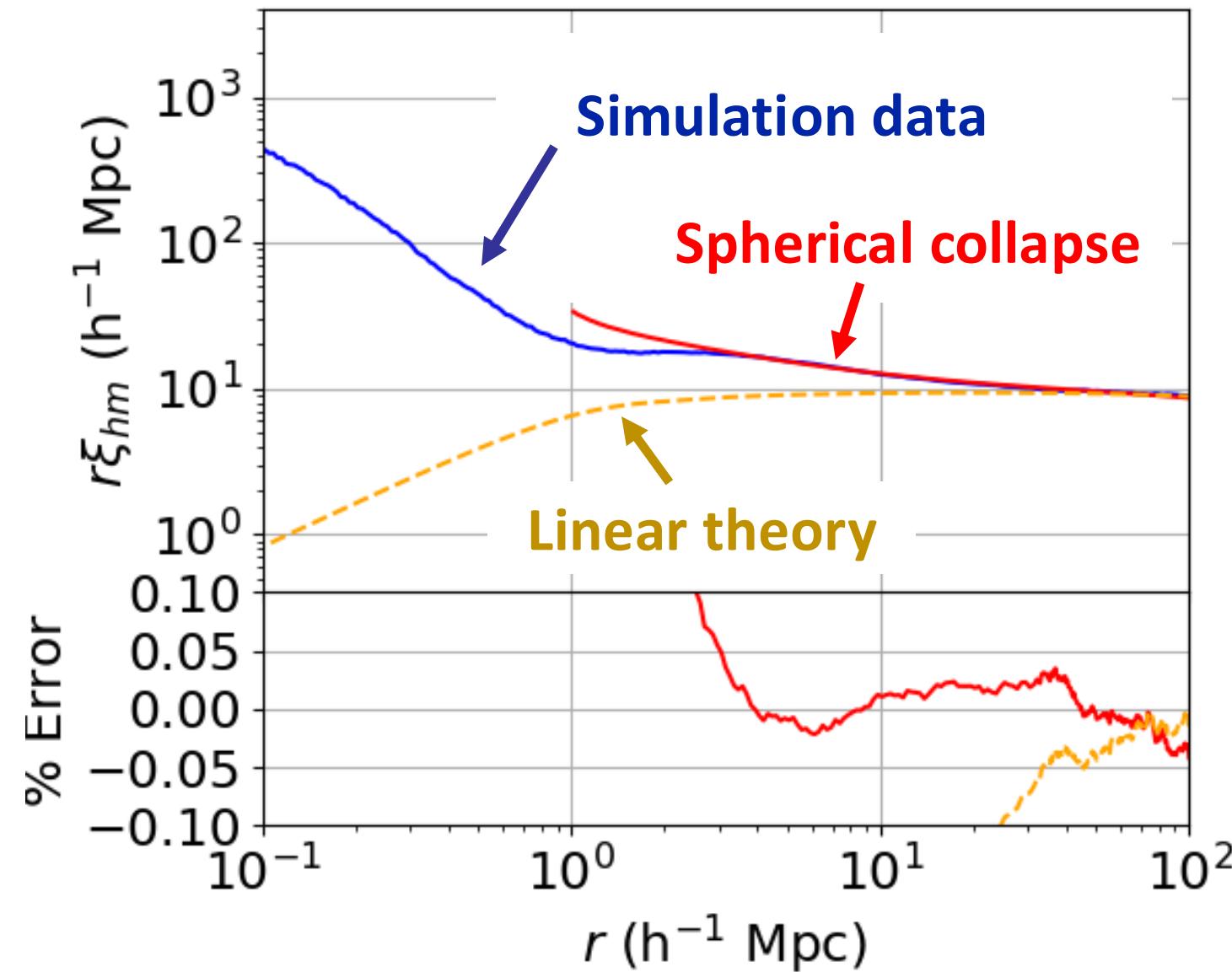
Key idea:

Non-linear evolution of the density field is due to mass falling in towards the halo.

- We can treat infall analytically using spherical collapse!
- Initial conditions set by linear theory.

Approach trades perturbative limit for spherical symmetry.

$$\Omega_m = 1$$



**Spherical collapse accurately models infall profiles.**

Recovers linear theory on large scales.

Generalization to  $\Lambda$ CDM in progress.

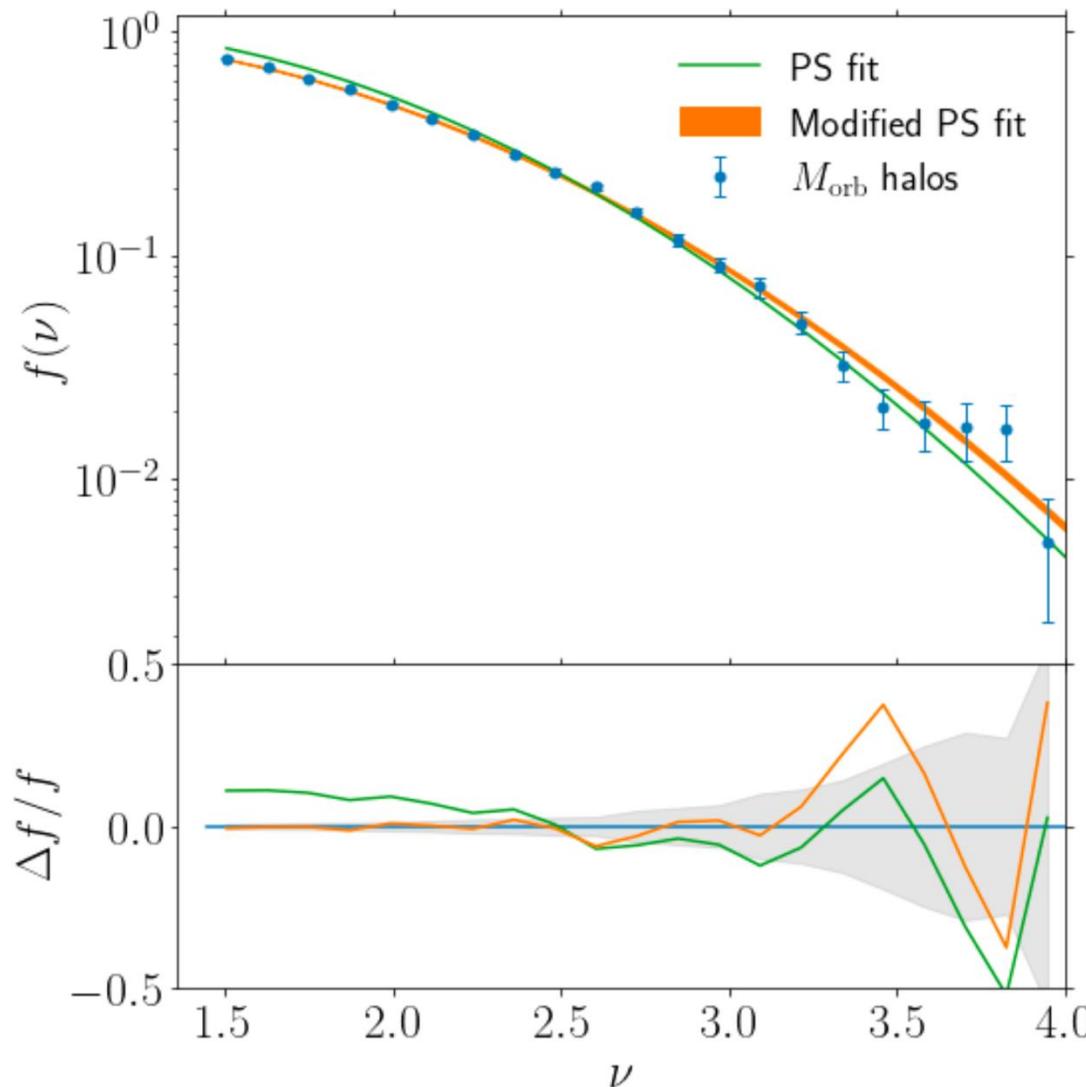
Advantage no. 3:

## The Mass Function + Bias of Dynamical Halos is Easier to Model!

- Spherical collapse predict a Press-Schechter mass function.
- Traditional approach: Identify collapsed mass with spherical overdensity (virial) mass.
- New approach: Identify collapsed mass with orbiting mass.
  - This is a very natural identification!
  - Formally correct for purely radial orbits!

Advantage no. 3:

## The Mass Function + Bias of Dynamical Halos is Easier to Model

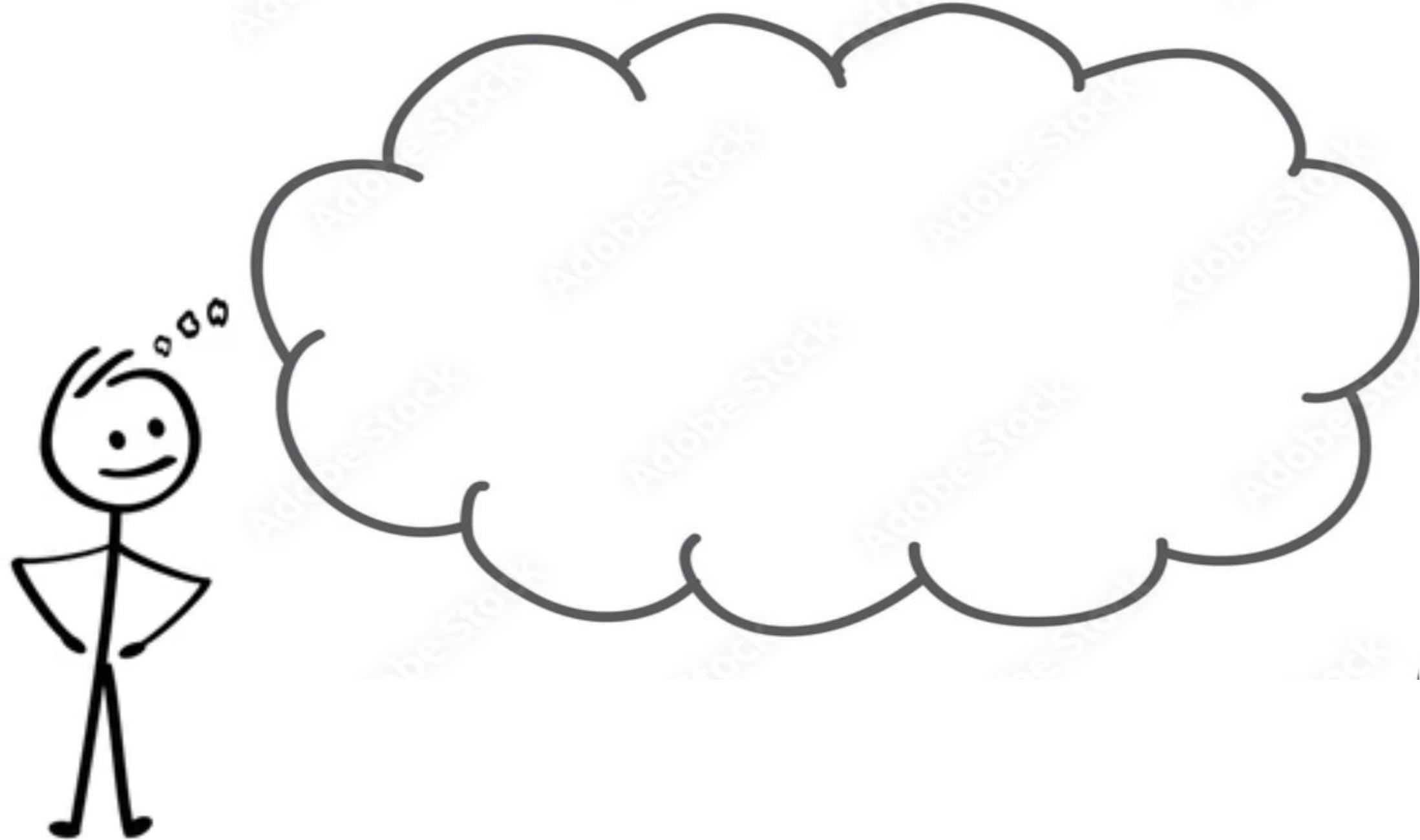


Excellent agreement with a mass-dependent threshold  $\delta_c$ .

Find:  $\delta_c \in [1.52, 1.68]$

Recovered values of  $\delta_c$  match expectations (Shapiro et al. 1999).

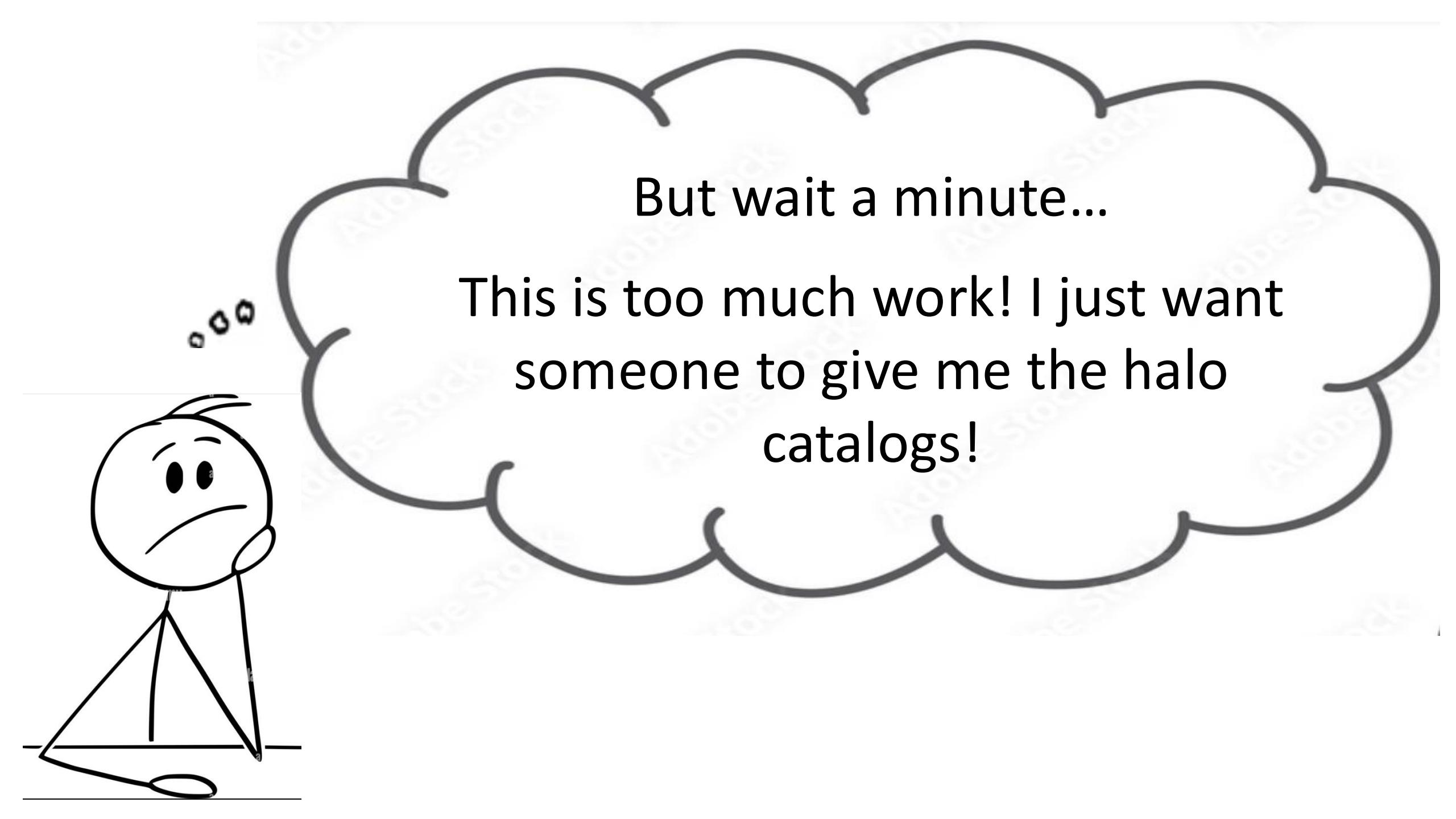
**Halo bias is consistent w/ peak/background split.**



A black and white line drawing of a stick figure with a circular head, two dots for eyes, and a curved line for a smile. The figure is standing with its arms slightly out. A large, irregularly shaped thought bubble originates from the figure's head and extends to the right. Inside the bubble, the text is written in a sans-serif font.

Wow! This is great!

I will only use dynamical halos  
from now on!

A simple line-drawn cartoon character with a large head, small body, and a single tuft of hair on top. The character has a neutral, slightly weary expression. A large, light-grey thought bubble surrounds the character's head, containing the text.

But wait a minute...

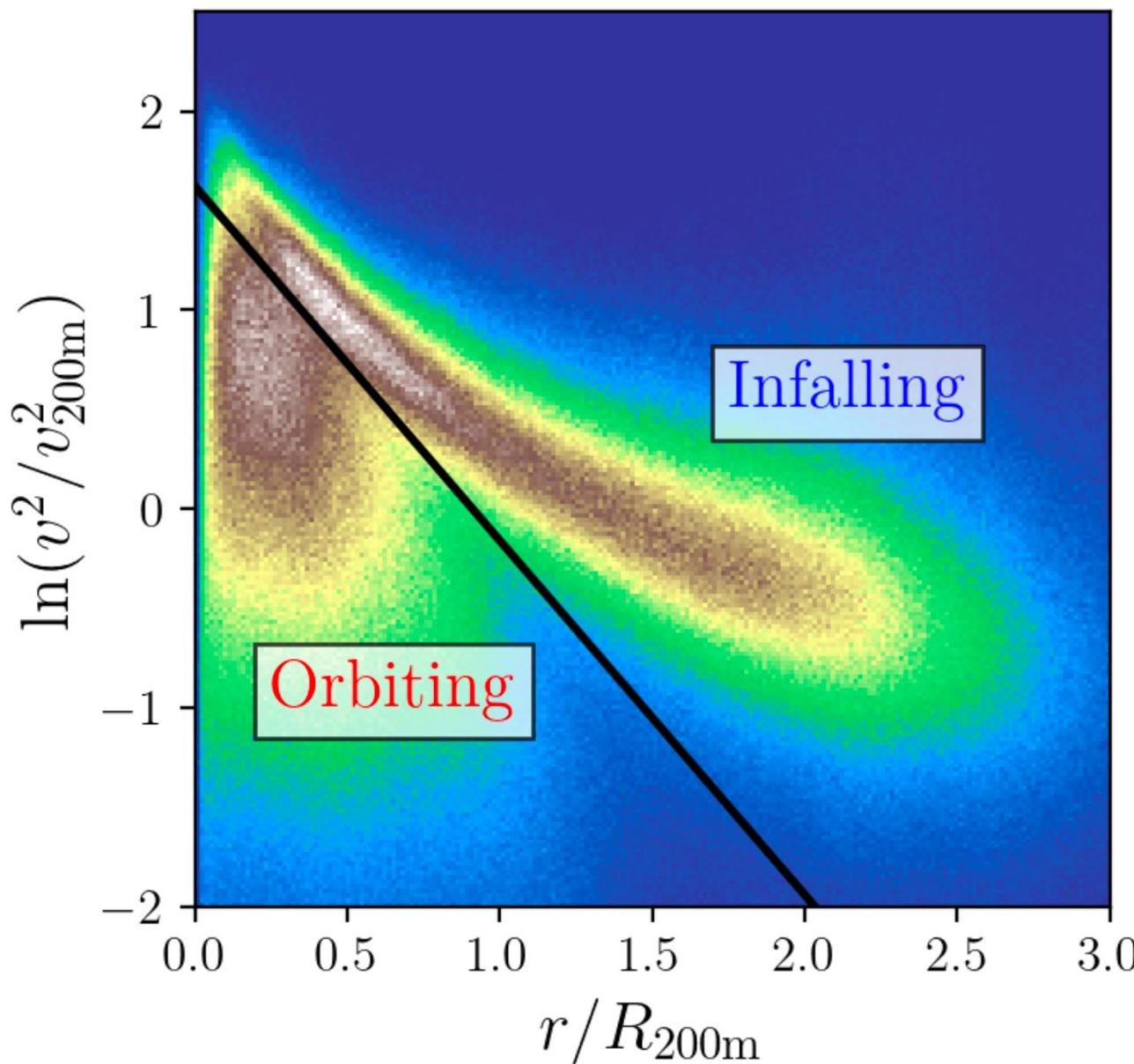
This is too much work! I just want someone to give me the halo catalogs!

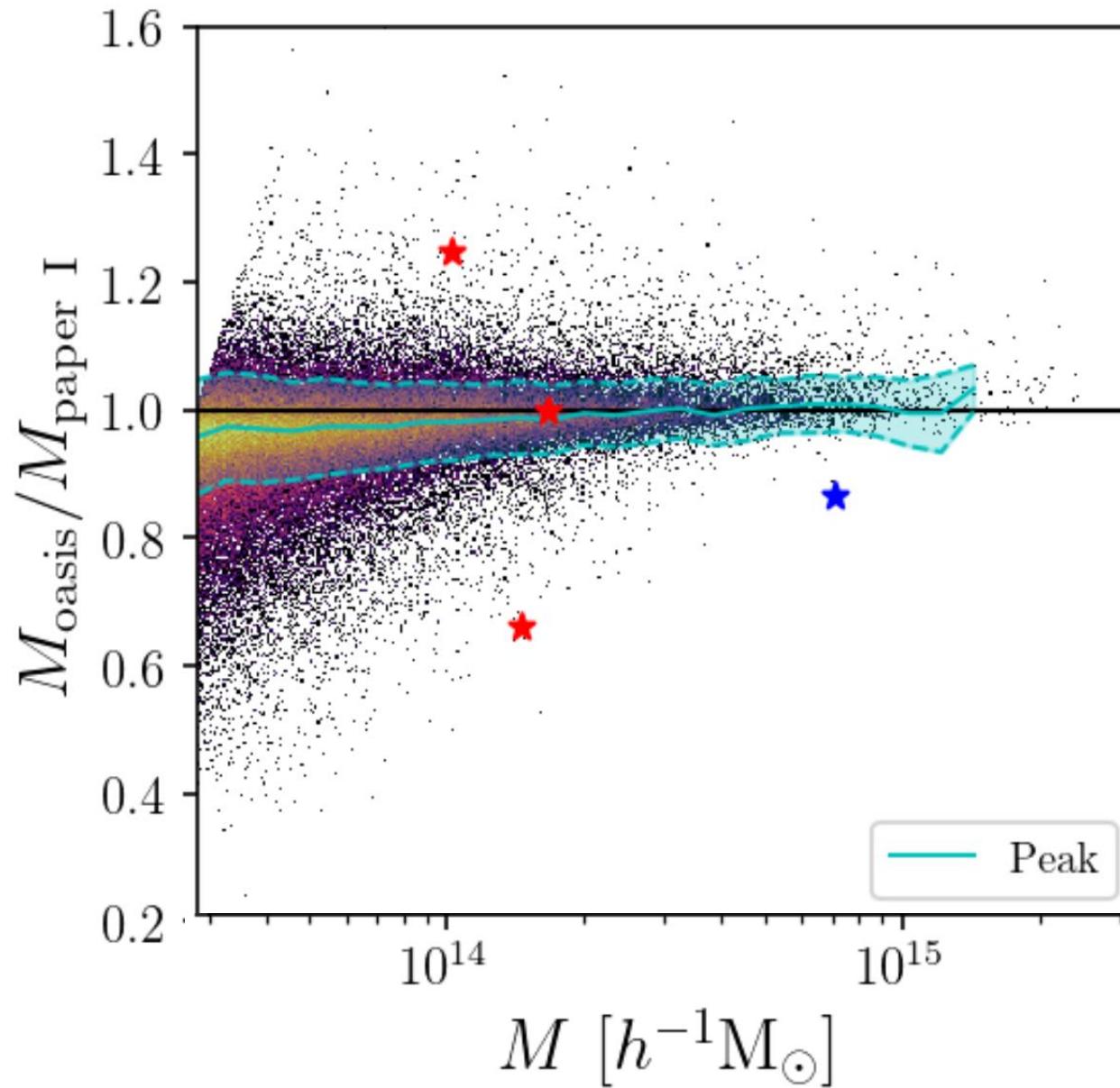


- Parallelized post-processing of Rockstar catalogs to produce a catalog of dynamical halos.

<https://github.com/edgarsalazar/oasis>

$$v_r < 0$$





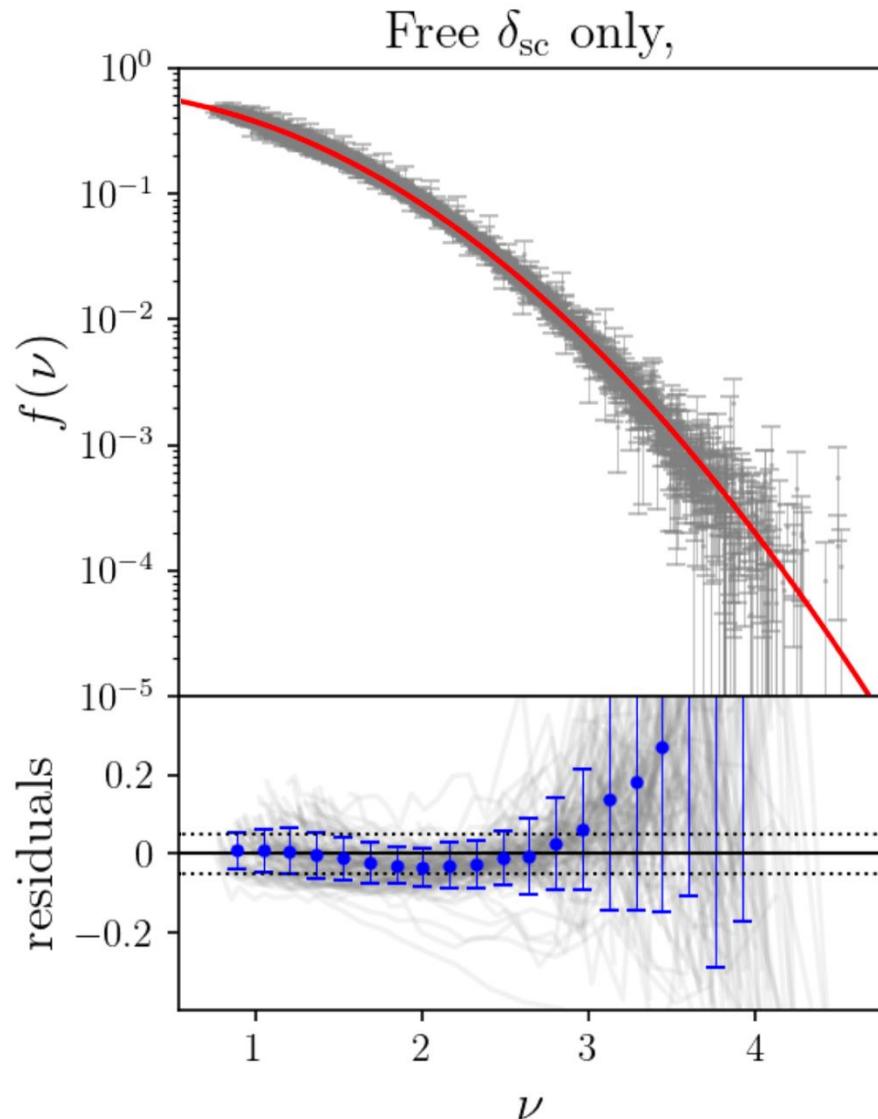
## Oasis Results:

➤ KE and orbit-based masses are tightly correlated.

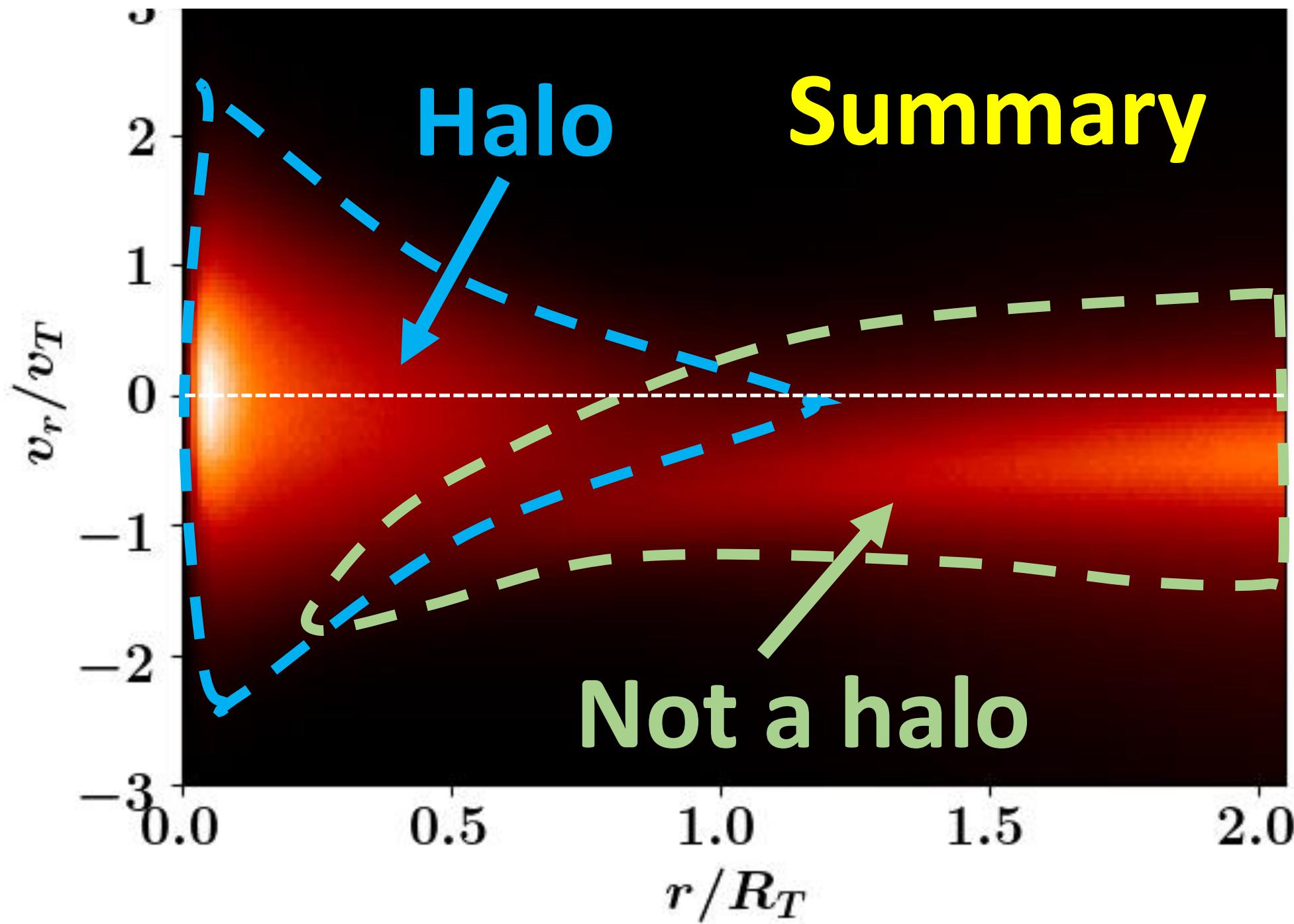
Nearly no offset, and  $\approx 4\%$  scatter.

Clearly a step up from spherical overdensity halos!

# The Dynamical Halo Mass Function from Oasis



- Measured the mass function for 100 Quijote simulations.
- High mass end is universal and Press-Schechter to within  $\approx 5\%$ .
- Effective threshold for collapse is  $\delta_{\text{sc}} = 1.52$ .



# Summary

- Halos do not have radial boundaries: rather, *halos should be defined as the collection of all orbiting particles.*

## Dynamical halos have many advantages:

- Naturally gives rise the 1-halo/2-halo structure of the halo model.
- Orbiting profile has a single degree of freedom: *the halo radius.*
- Infall profile can be modelled using spherical collapse (in progress).
- Improves agreement between simulations and Press-Schechter

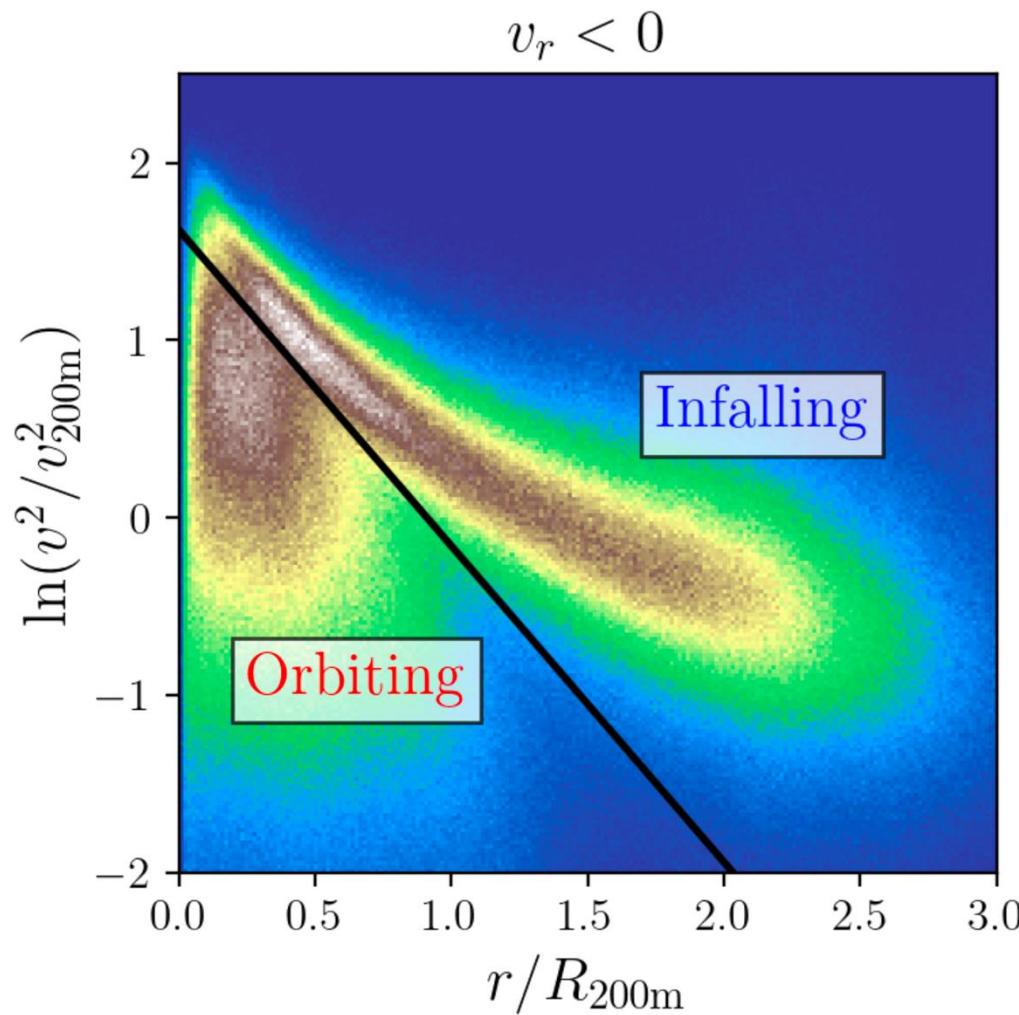


**Developed a fast algorithm to generate dynamical halo catalogs from simulations.**

<https://github.com/edgarsalazar/oasis>

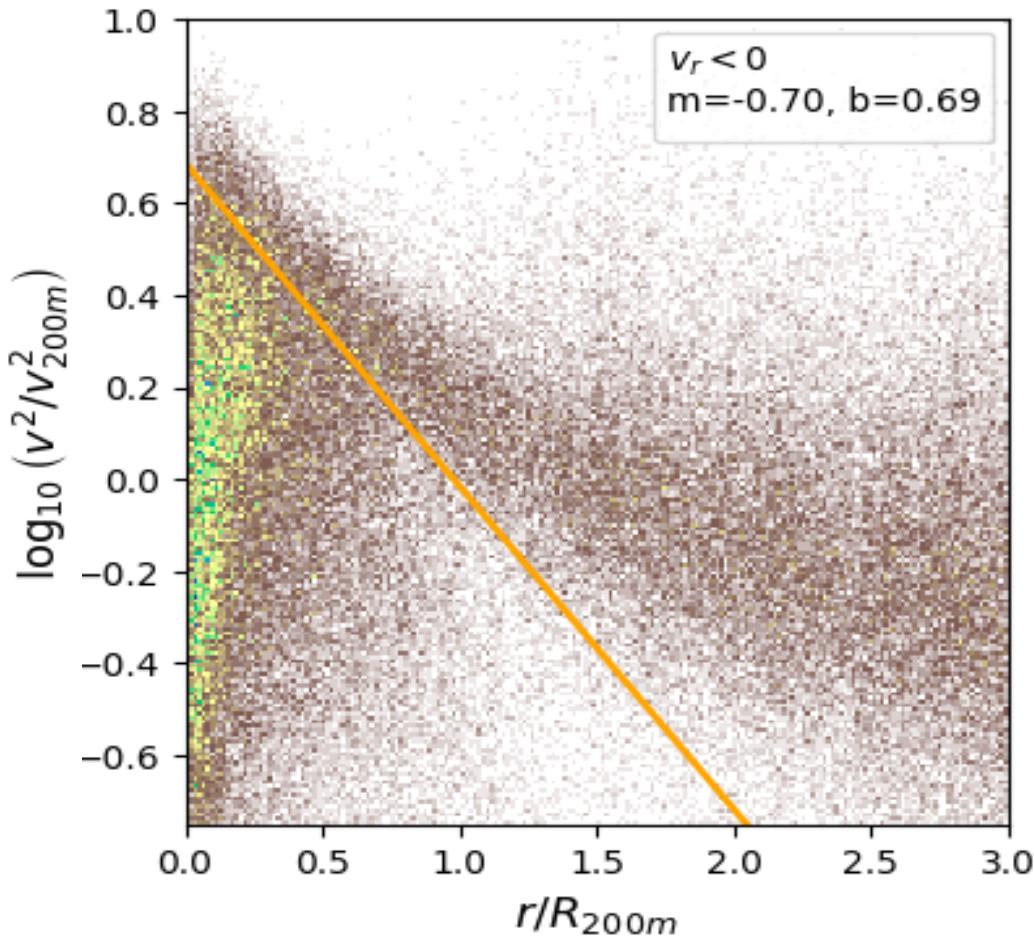
# Extra Slides

# Will Baryons Mess Everything Up?



- Orbiting/infall split is well motivated for DM particles.
- Does this kind of thinking even make sense for baryons?

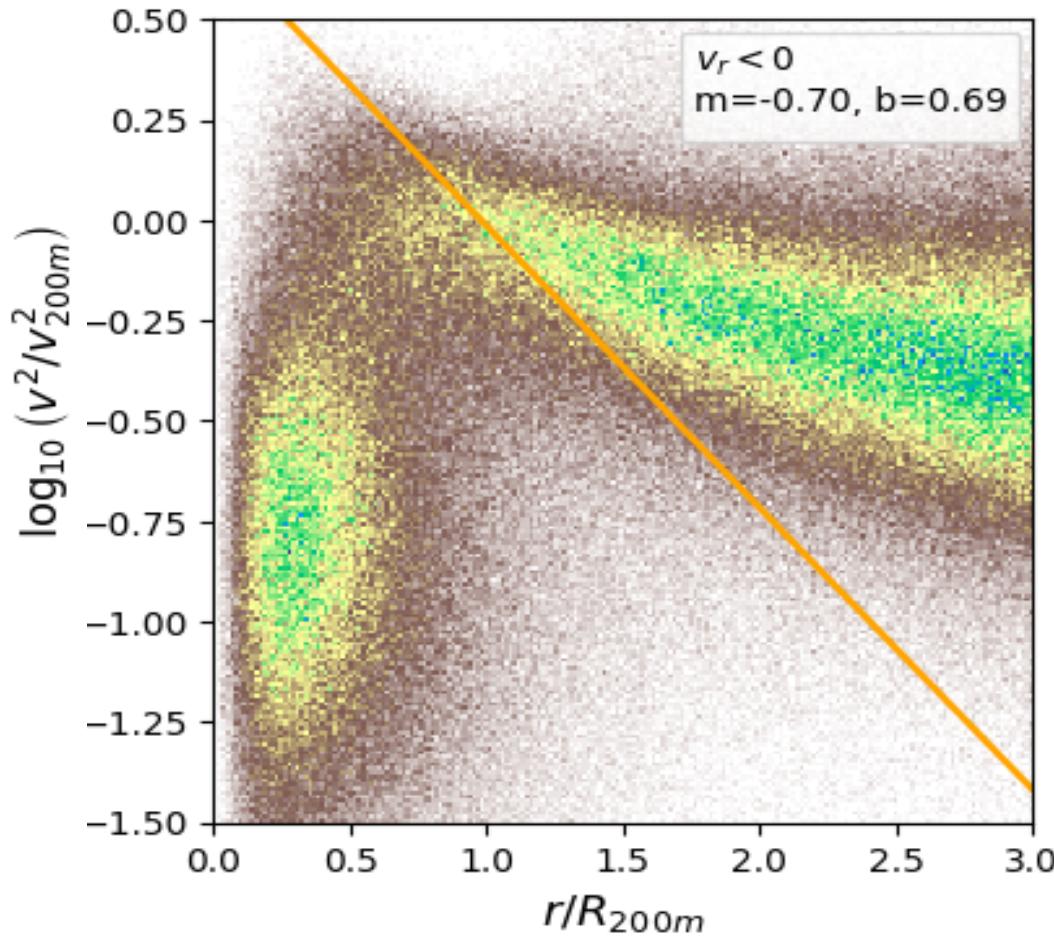
# Baryons Can Be Accommodated!



- Stars are collisionless, so they behave similarly to dark matter.

# Baryons Can Be Accommodated!

Y-axis scale changed



- Stars are collisionless, so they behave similarly to dark matter.
- Infall gas hits the halo atmosphere and comes to “rest”
  - KE cuts are even *cleaner* with gas particles!

Expect the orbiting/infall framework will generalize to  $\Lambda$ CDMB.