

SIDM interpretations of Crater II and GD-1

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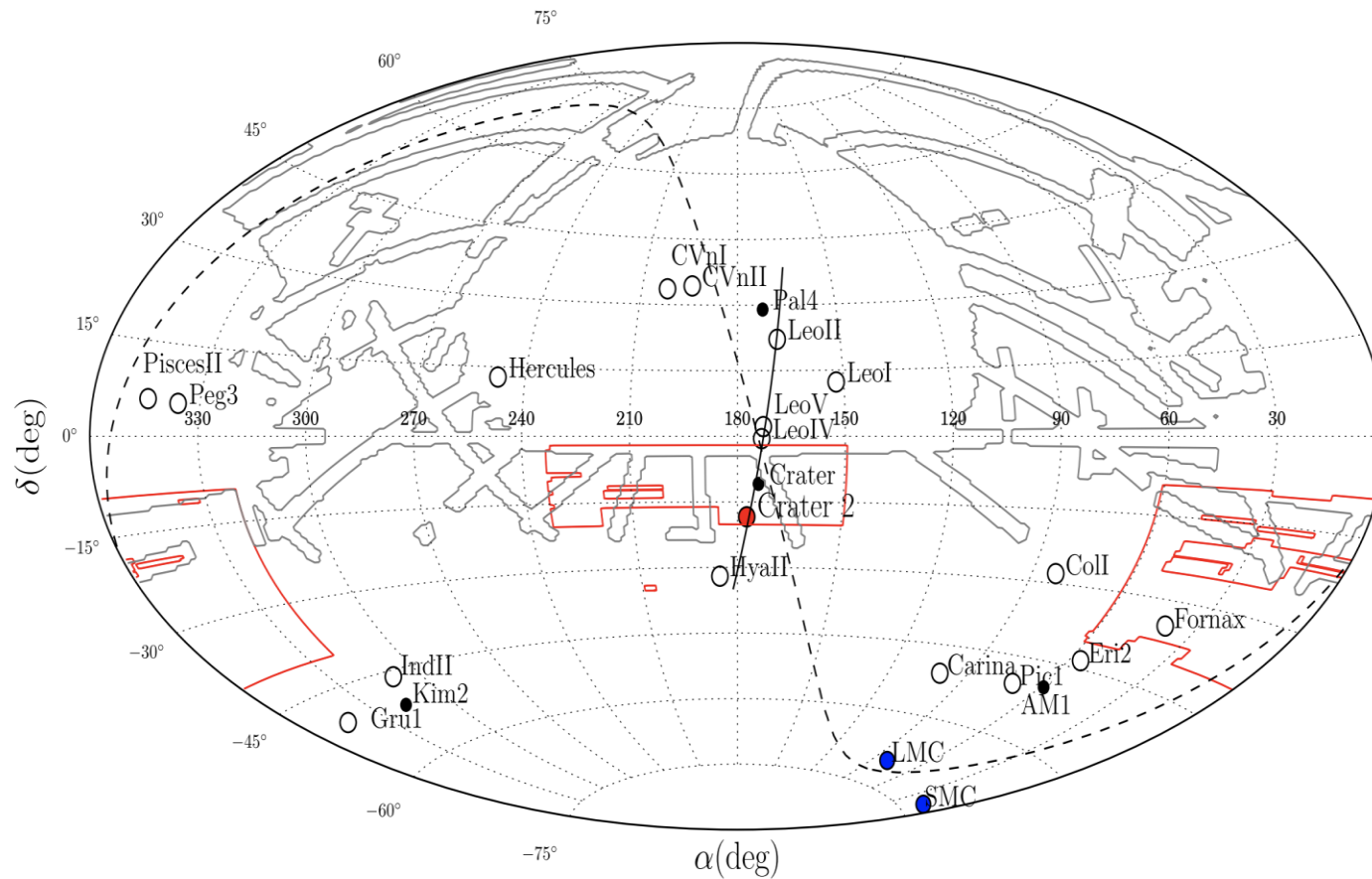
IFIC, Valencia, Spain



Xingyu Zhang, Hai-Bo Yu, Daneng Yang and Haipeng An, ApJL 968 L13 (2024) [2401.04985]

Xingyu Zhang, Hai-Bo Yu, Daneng Yang and Ethan Nadler, ApJL 978 L23 (2025) [2409.19493]

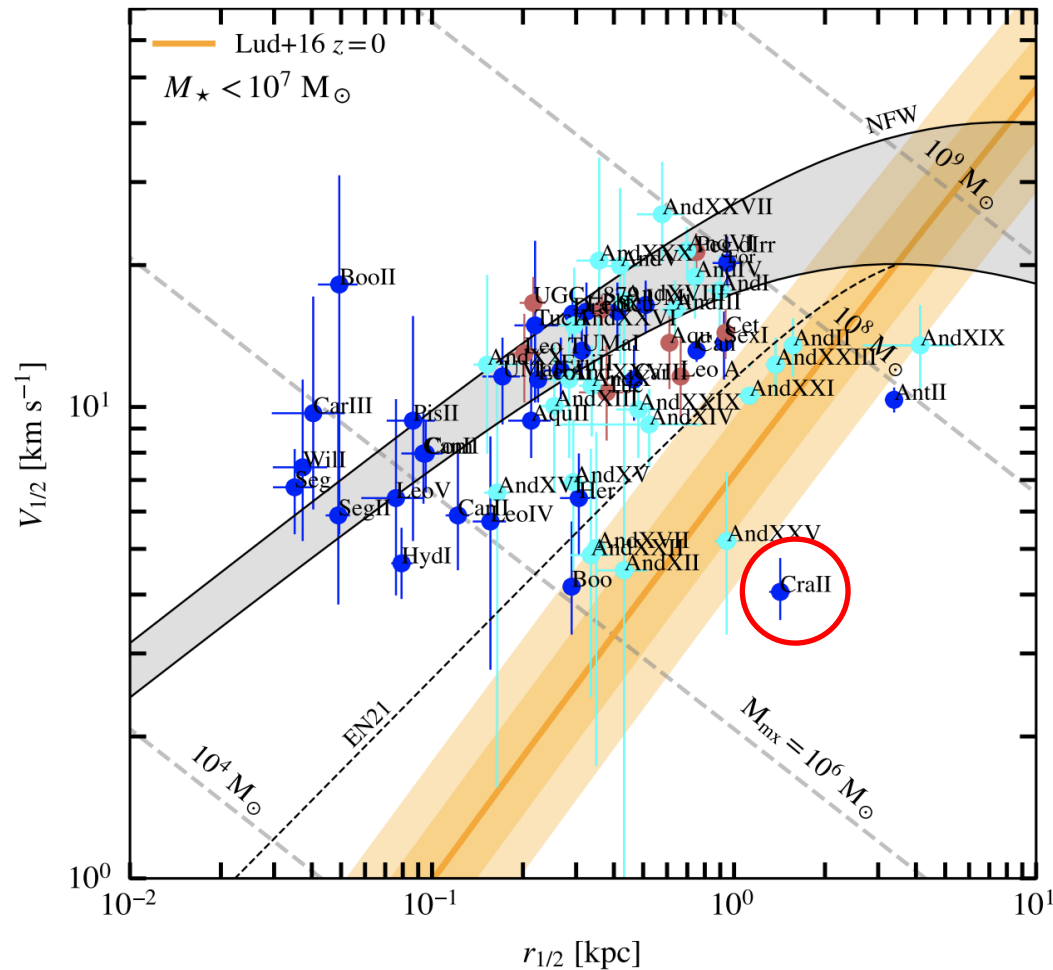
Ultra-diffuse satellite galaxy Crater II



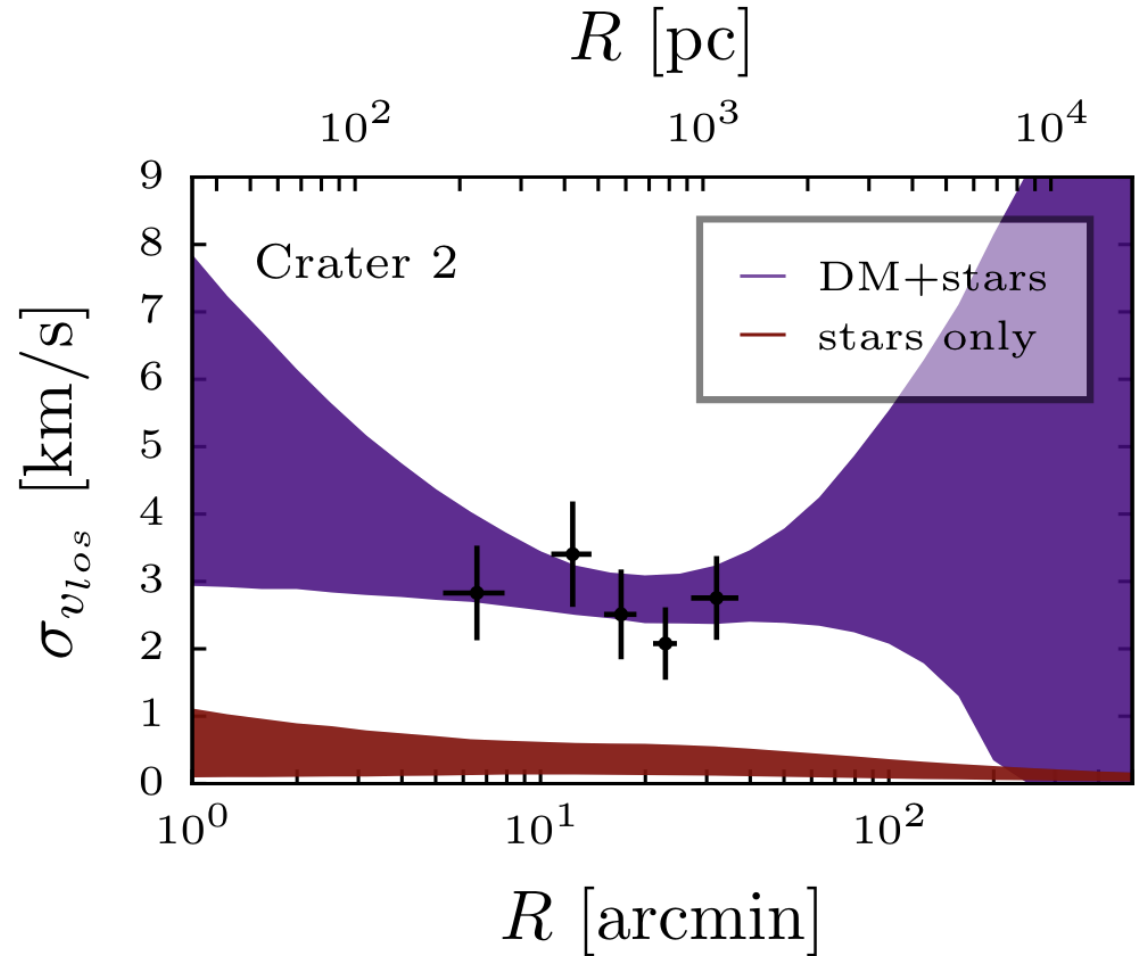
Crater II is one of Milky Way satellite galaxies discovered in 2016.

(Torrealba et al. 2016)

Ultra-diffuse satellite galaxy Crater II



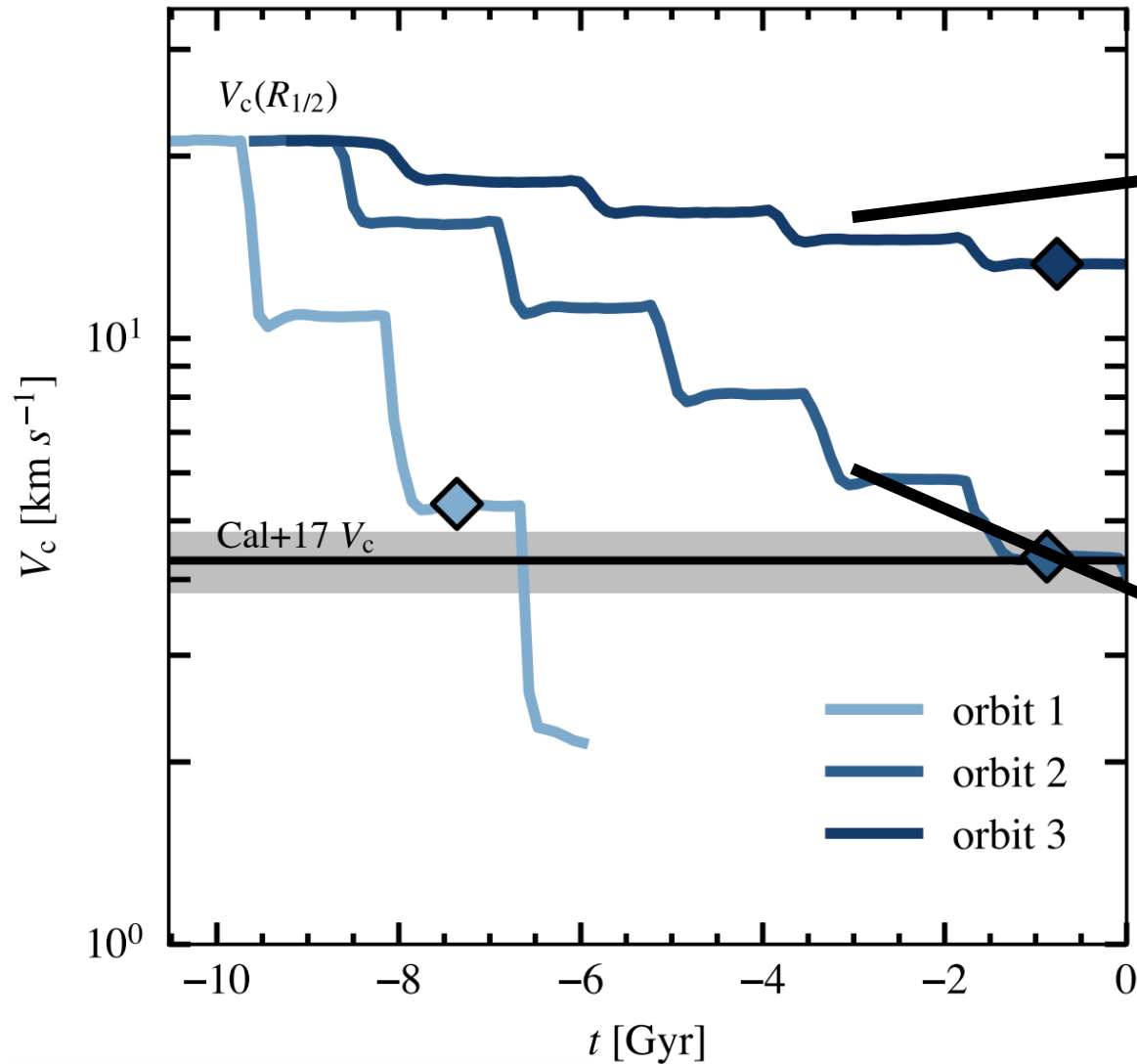
(Borukhovetskaya et al. 2022)



(Caldwell et al 2017)

Crater II is special because of its diffuse profile, $r_h = 1.06$ kpc, $\sigma_{\text{los}} \sim 2.3$ km/s, flat with respect to radius.

Ultra-diffuse satellite galaxy Crater II



Orbit 3: $r_p = 38$ kpc

Measured by Gaia DR3

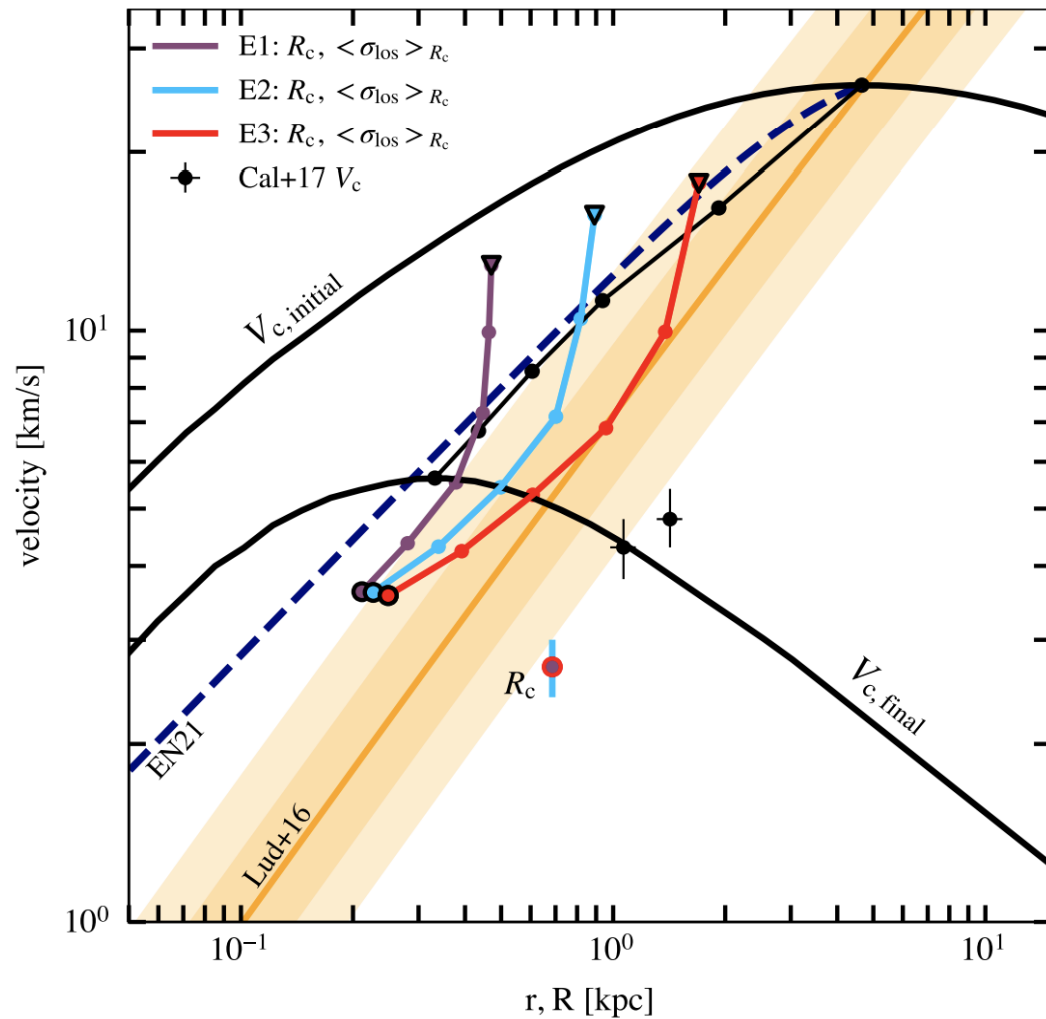
With the orbit, CDM fails

Orbit 2: $r_p = 14$ kpc

Required orbit to match V_c
in CDM is much lower

(Borukhovetskaya et al. 2022)

Ultra-diffuse satellite galaxy Crater II



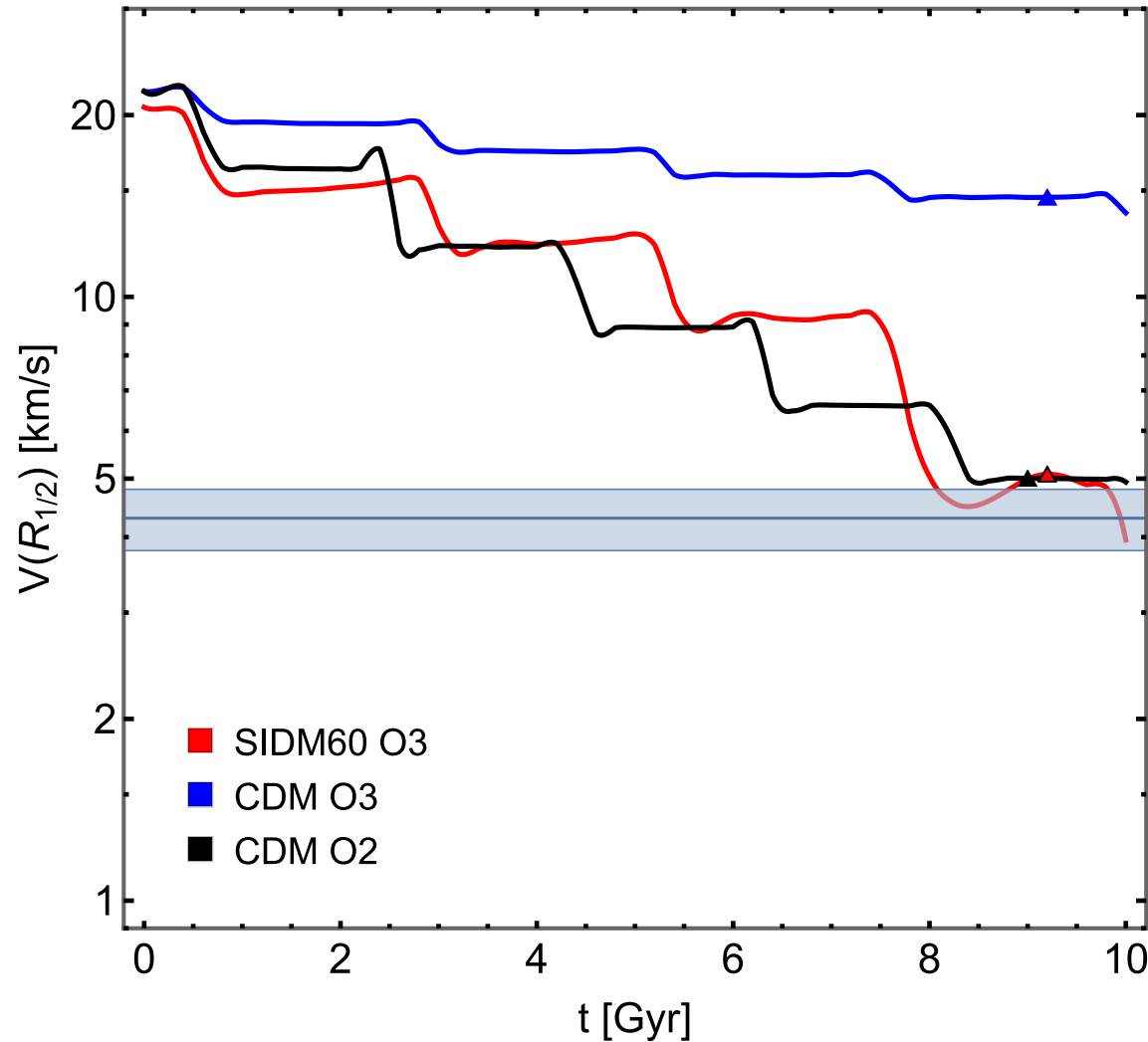
(Borukhovetskaya et al. 2022)

Orbit 2:

After tidal stripping, the halo mass could match the observation, but the half-light radius is too small.

Ultra-diffuse satellite galaxy Crater II

- SIDM solution: Mass



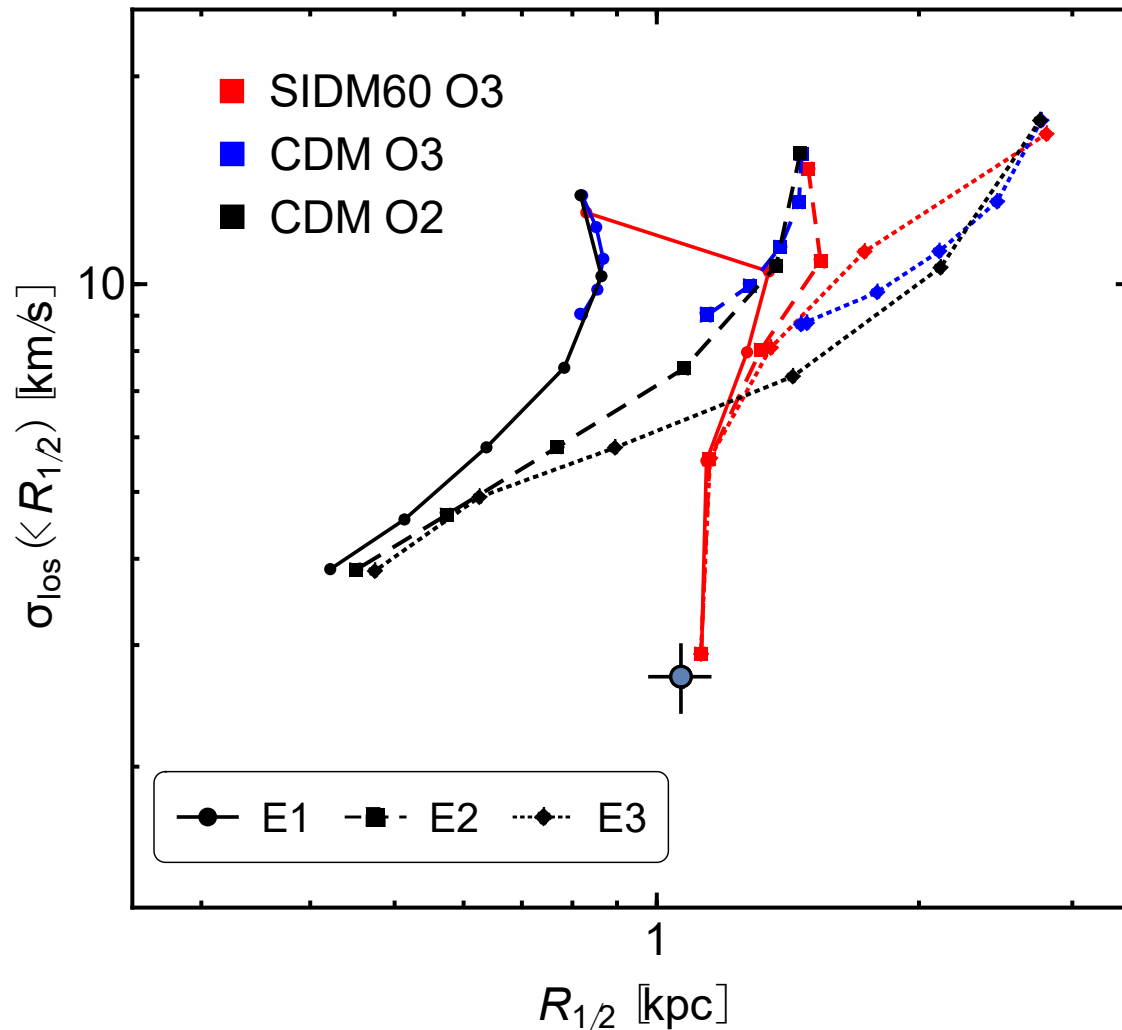
SIDM orbit 3, $r_p = 38$ kpc
 $\sigma/m = 60 \text{ cm}^2/\text{g}$

CDM orbit 3, $r_p = 38$ kpc

CDM orbit 2, $r_p = 14$ kpc

Ultra-diffuse satellite galaxy Crater II

- SIDM solution: Size (half-light radius)



CDM orbit 2

$R_h = 0.45$ kpc, too compact

CDM orbit 3

Insufficient mass loss

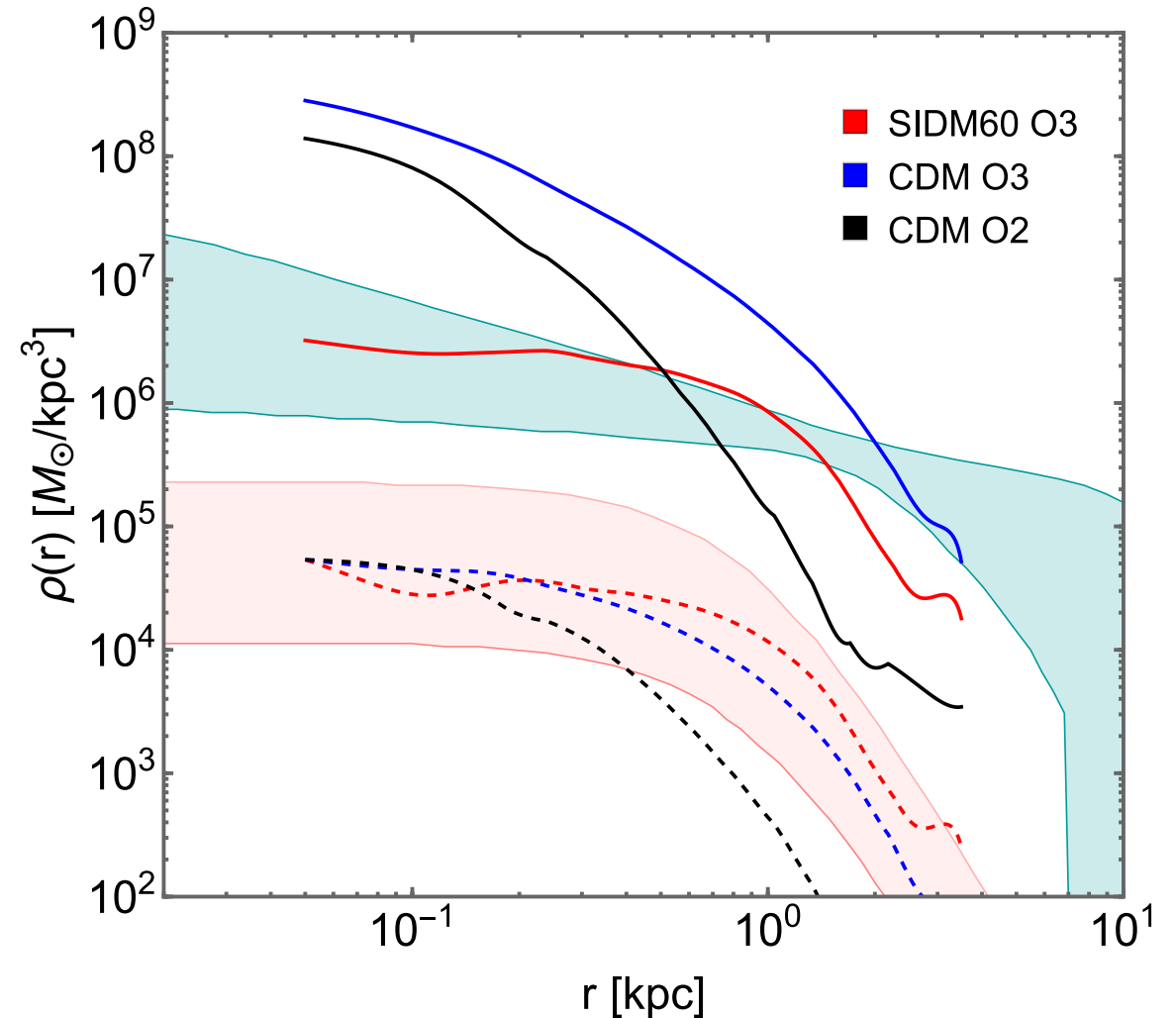
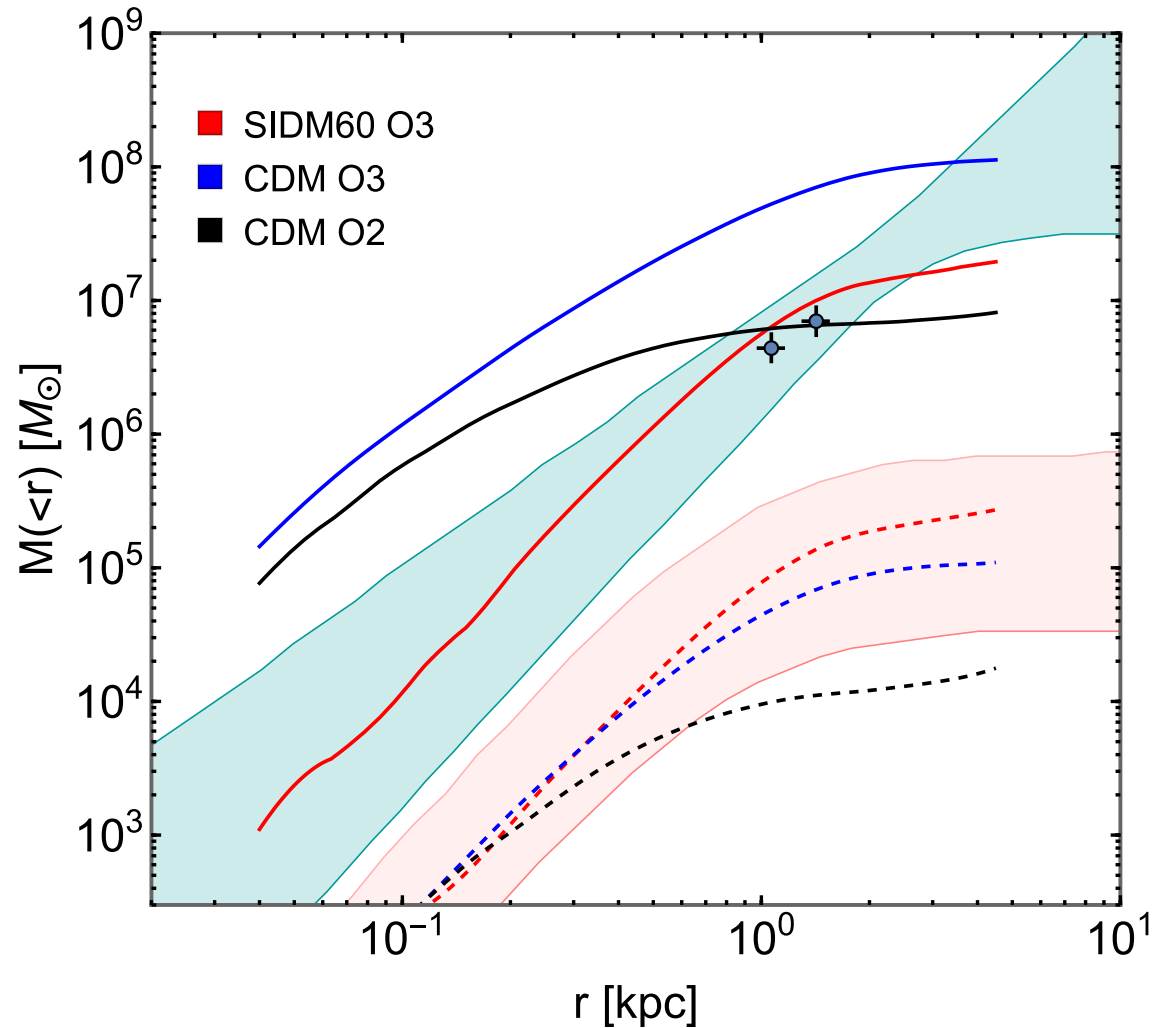
SIDM orbit 3

$R_h = 1.1$ kpc

Excellent agreement

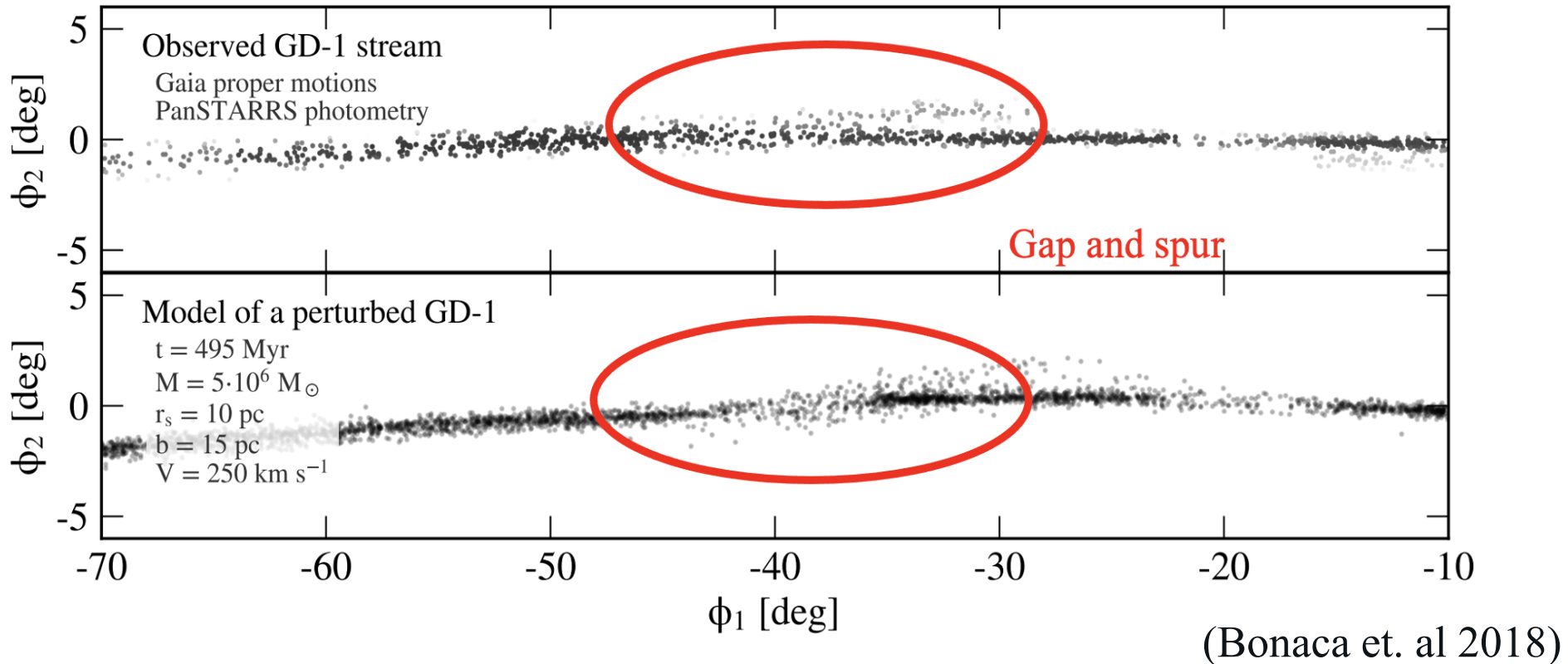
Ultra-diffuse satellite galaxy Crater II

- SIDM solution: Density and mass profile



Ultra-compact subhalo perturber for GD-1

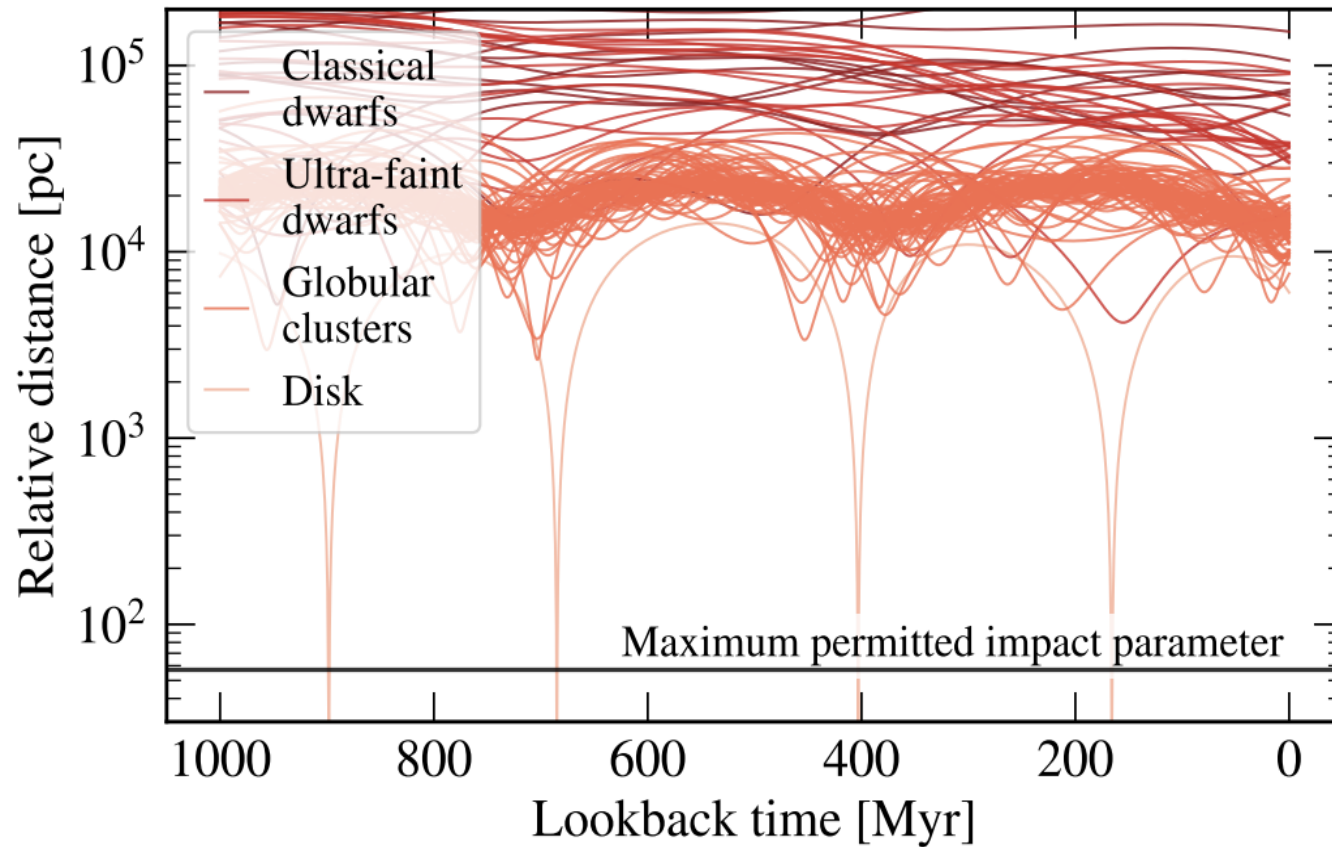
Spur and gaps of the GD-1 stellar stream



This gap-spur can be produced by a close encounter with an ultra-compact perturber

Ultra-compact subhalo perturber for GD-1

The missing compact perturber



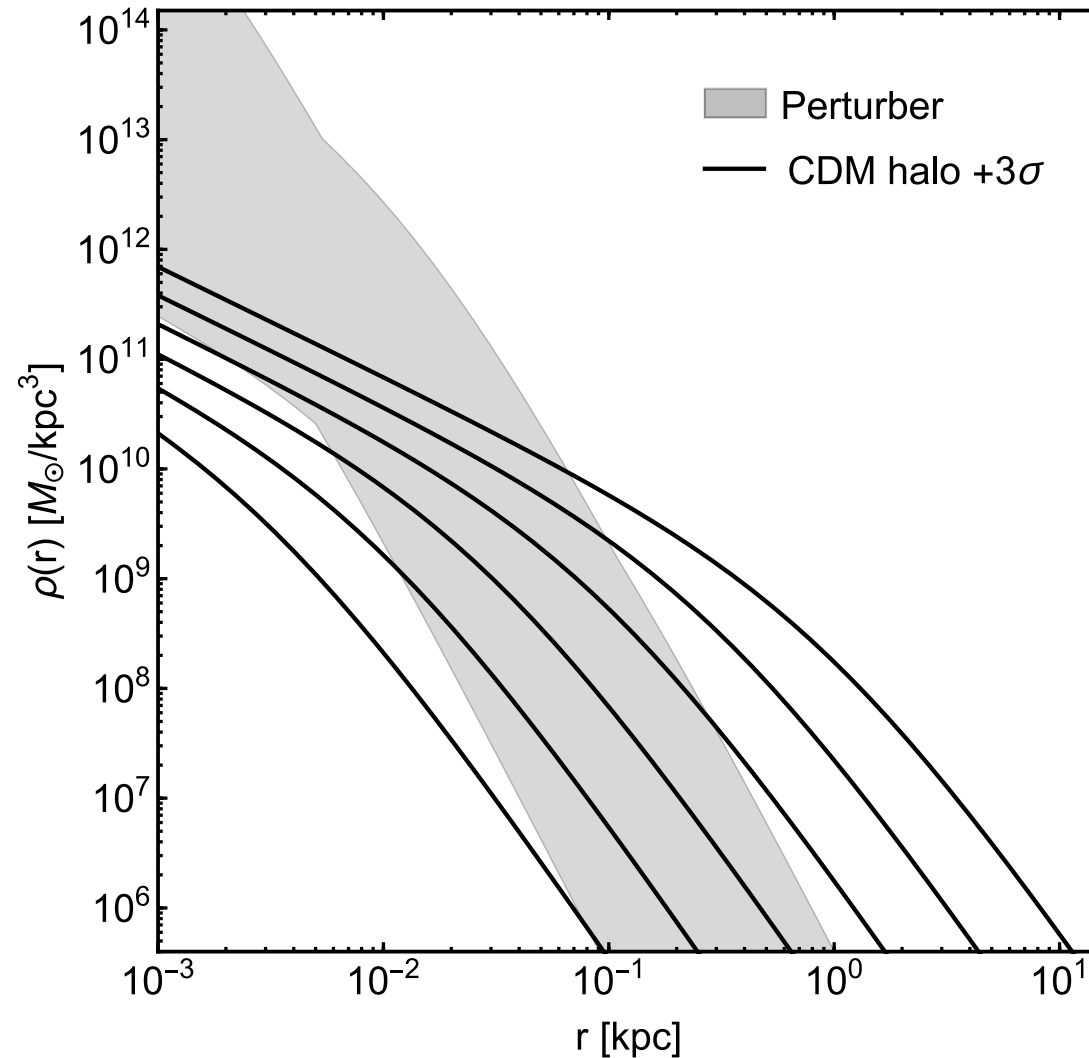
(Bonaca et. al 2018)

Through backward orbital integration, none of the observed objects matches the required orbit

The perturber is most likely a dark matter subhalo.

Ultra-compact subhalo perturber for GD-1

The missing compact perturber

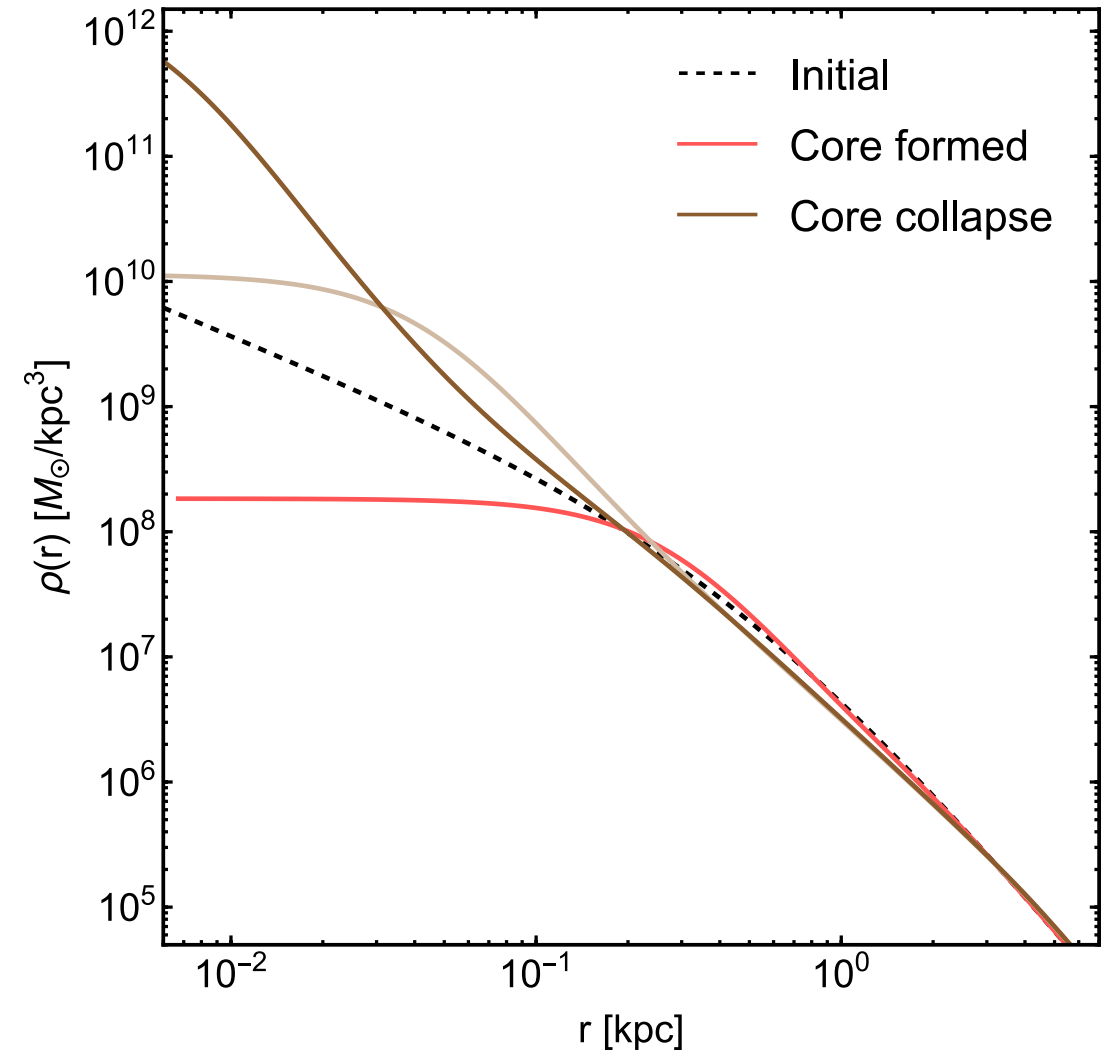
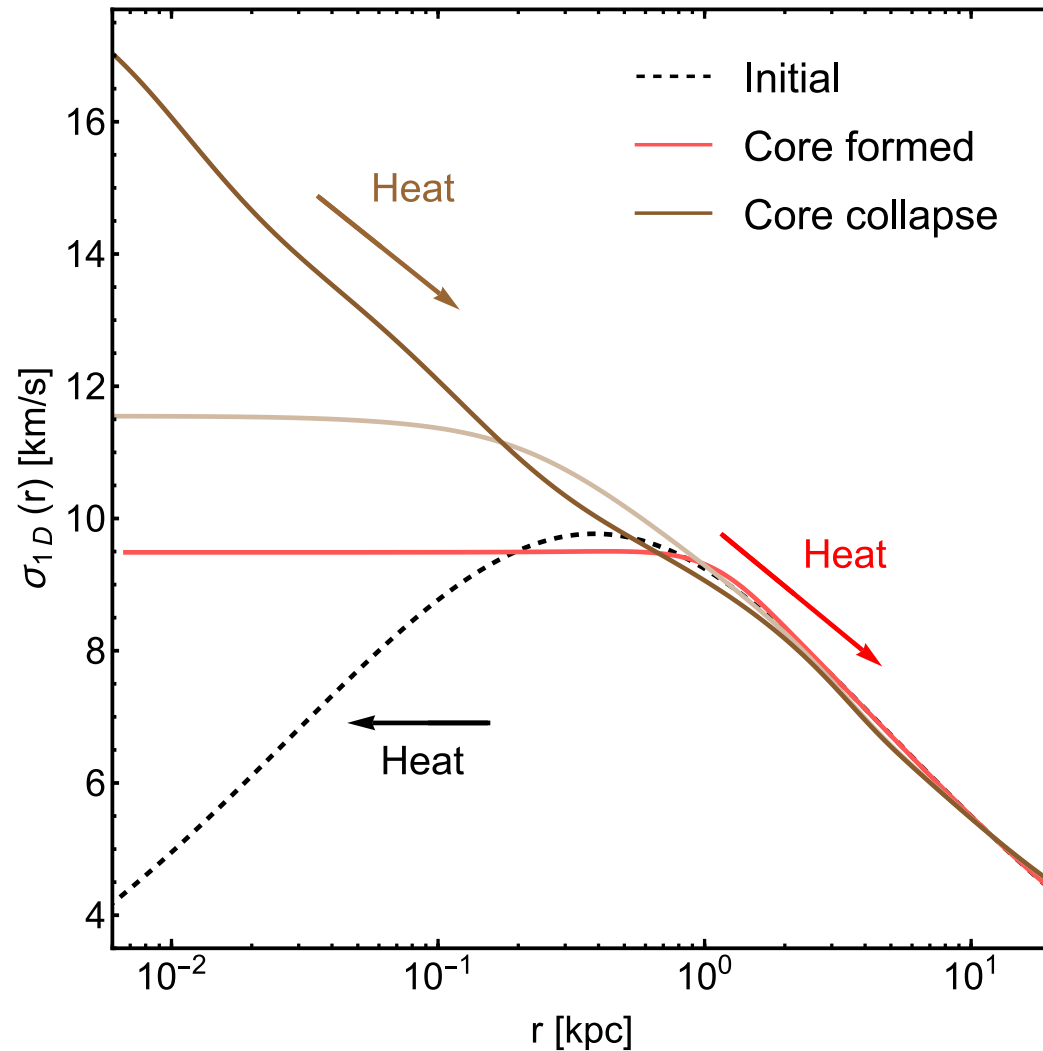


The reconstructed perturber density* is very compact, which is not likely to form in the CDM scenario

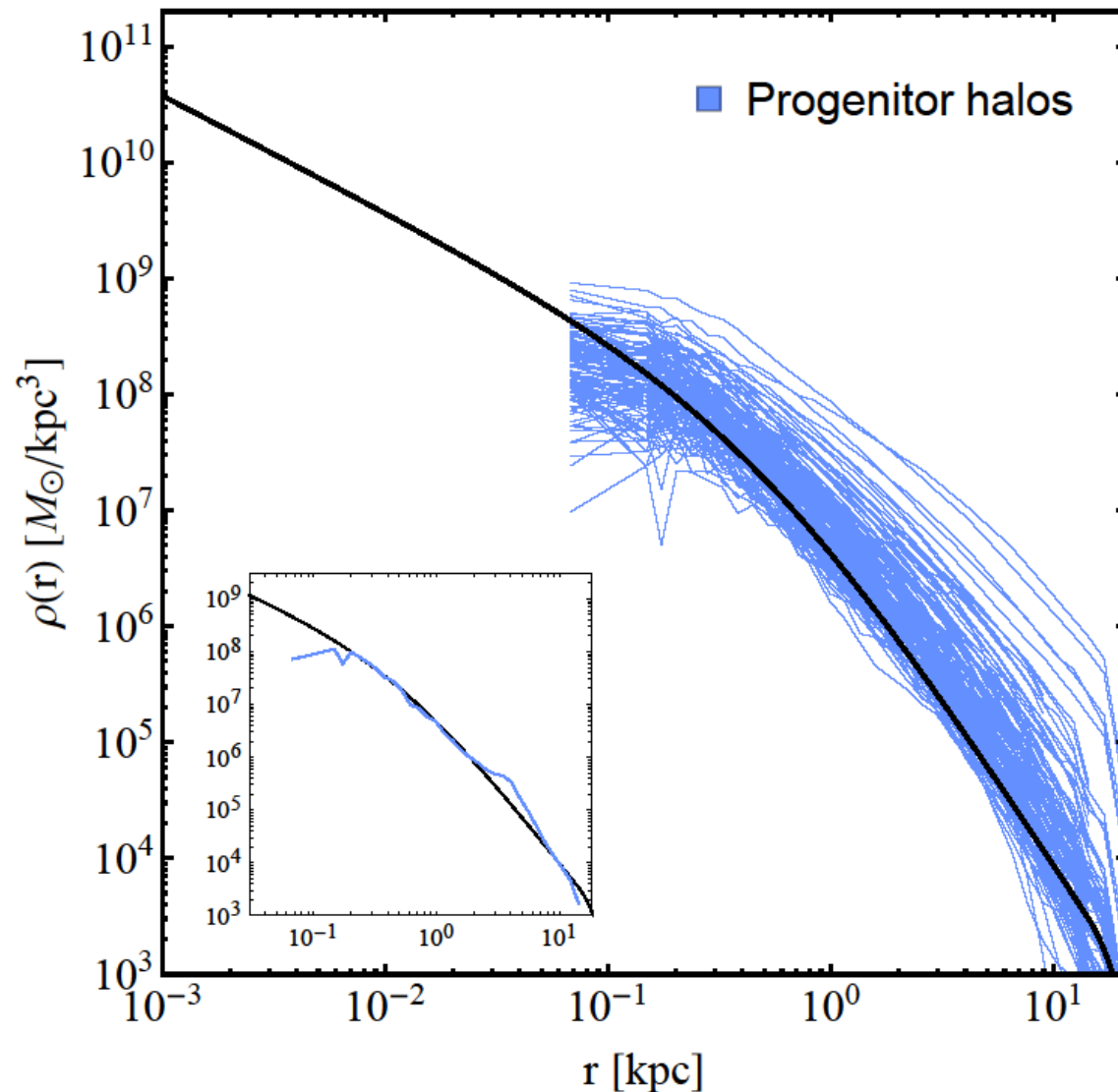
*(Bonaca et. al. 2018)

Ultra-compact subhalo perturber for GD-1

Two phase evolution of self-interacting dark matter halo



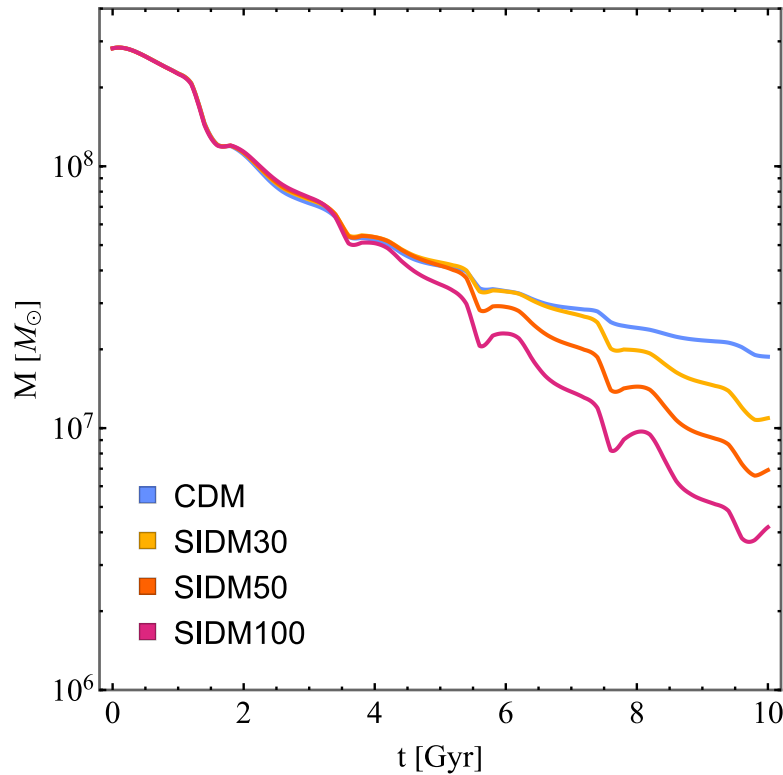
Ultra-compact subhalo perturber for GD-1



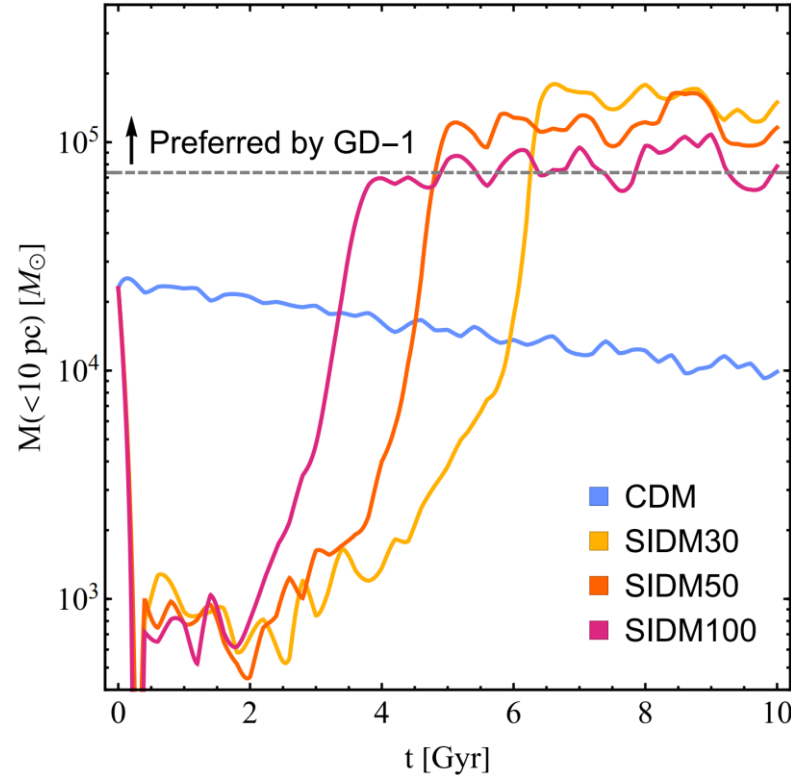
Milky Way subhalo progenitors from cosmological simulations

Select a small subhalo at infall as the initial condition

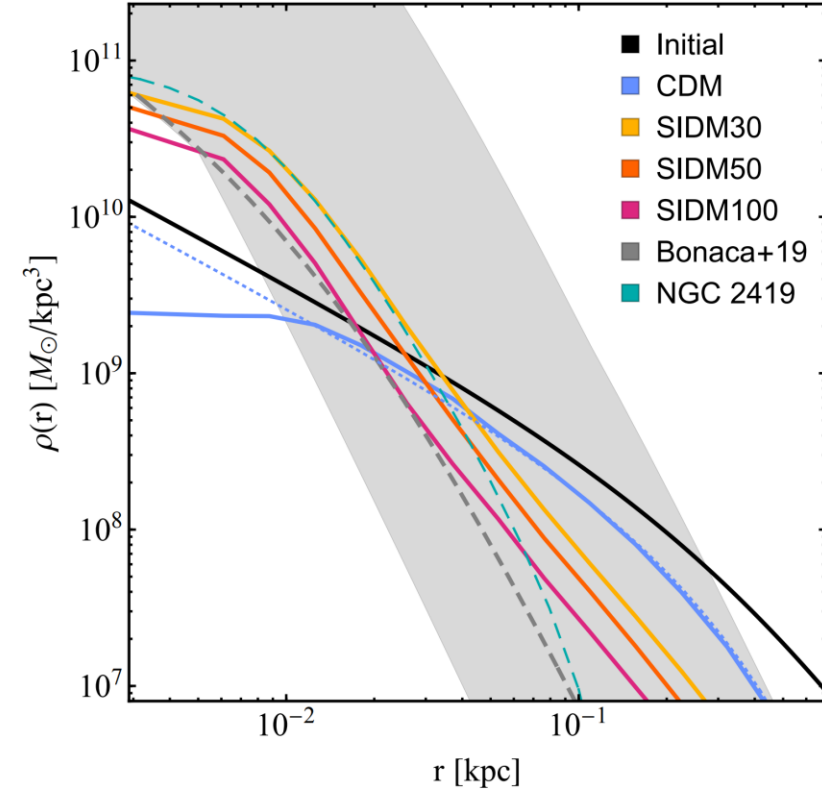
Ultra-compact subhalo perturber for GD-1



Total mass evolution



Enclosed mass within 10 pc



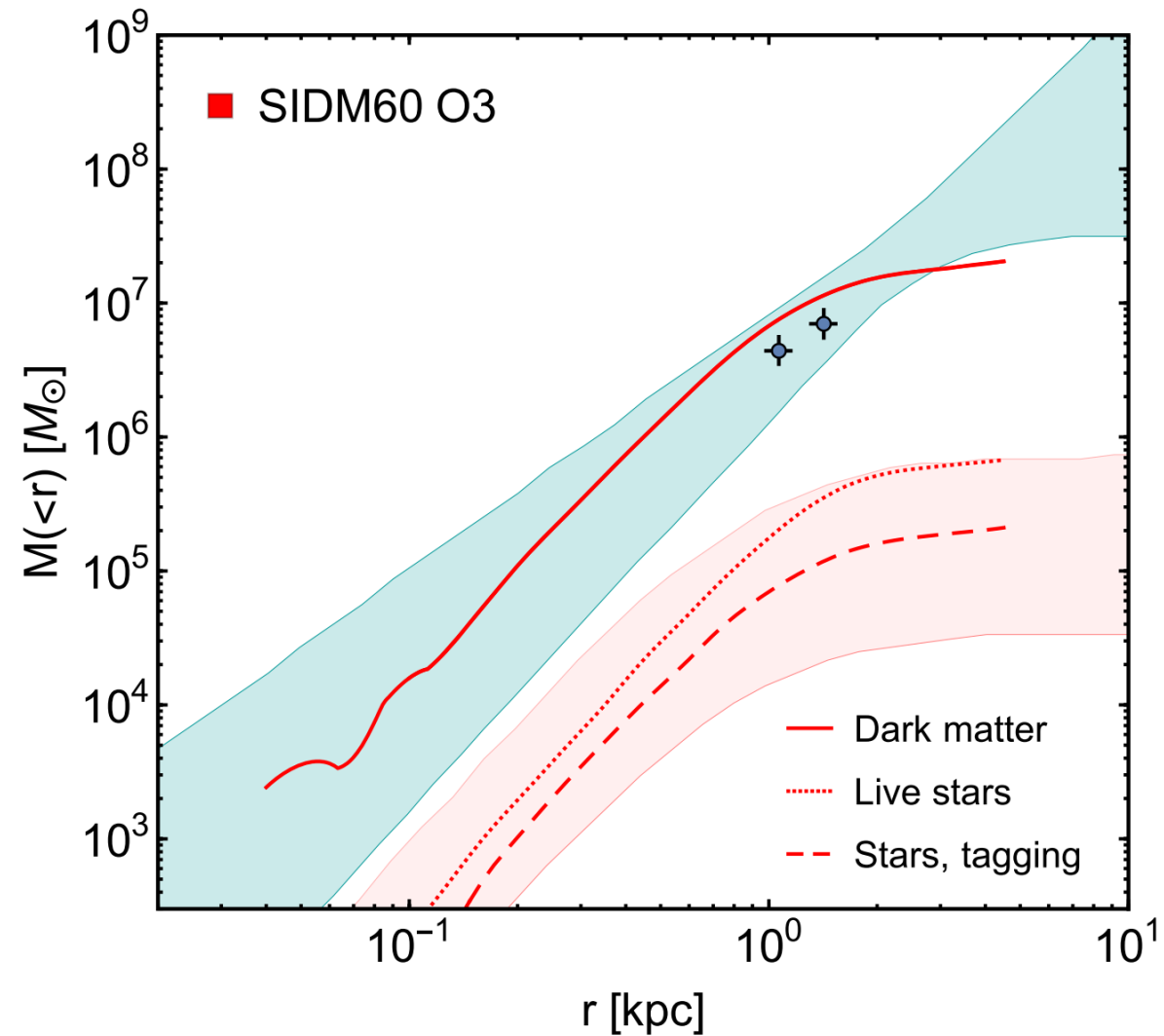
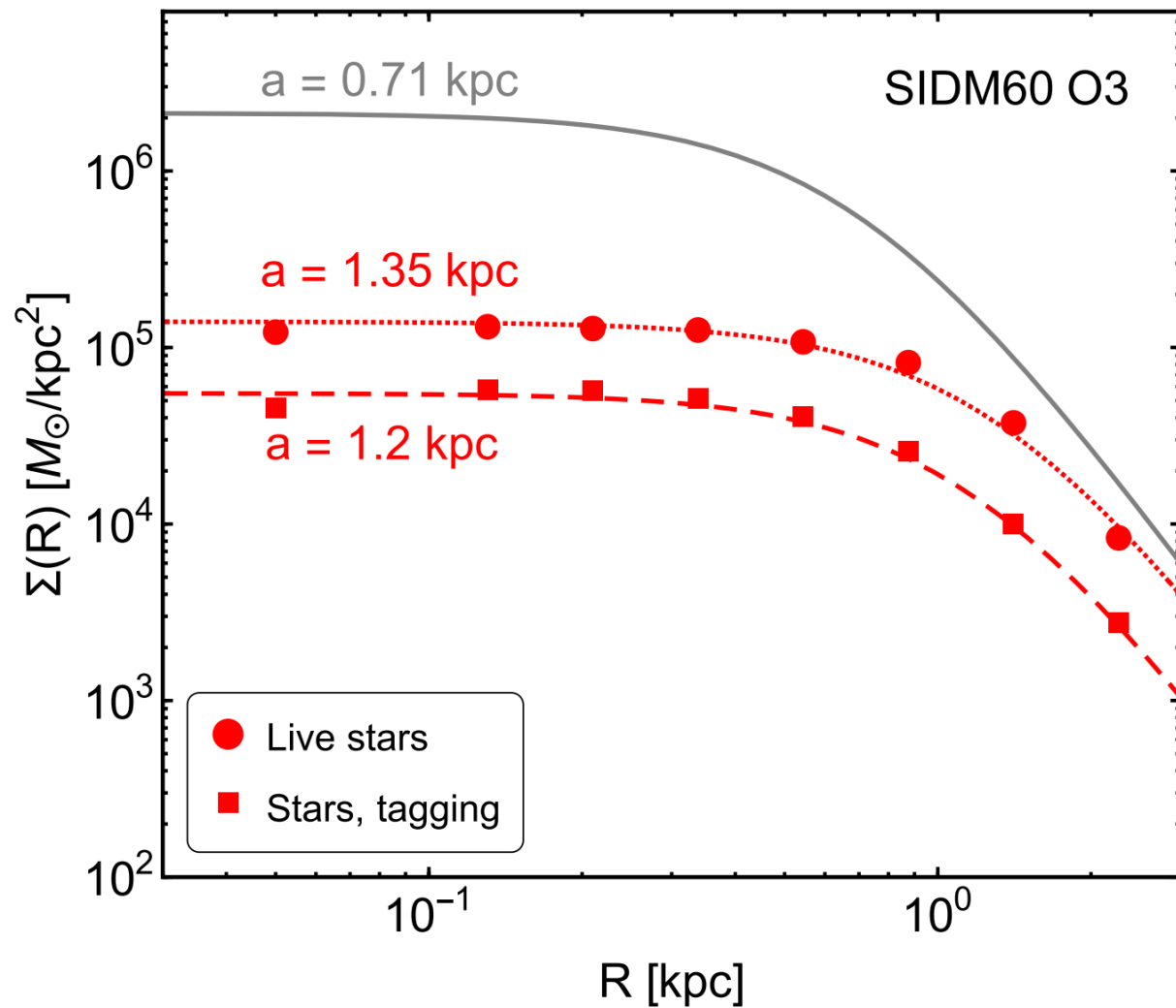
Final density profiles

The King model well fits the inner region of the core-collapsed subhalo

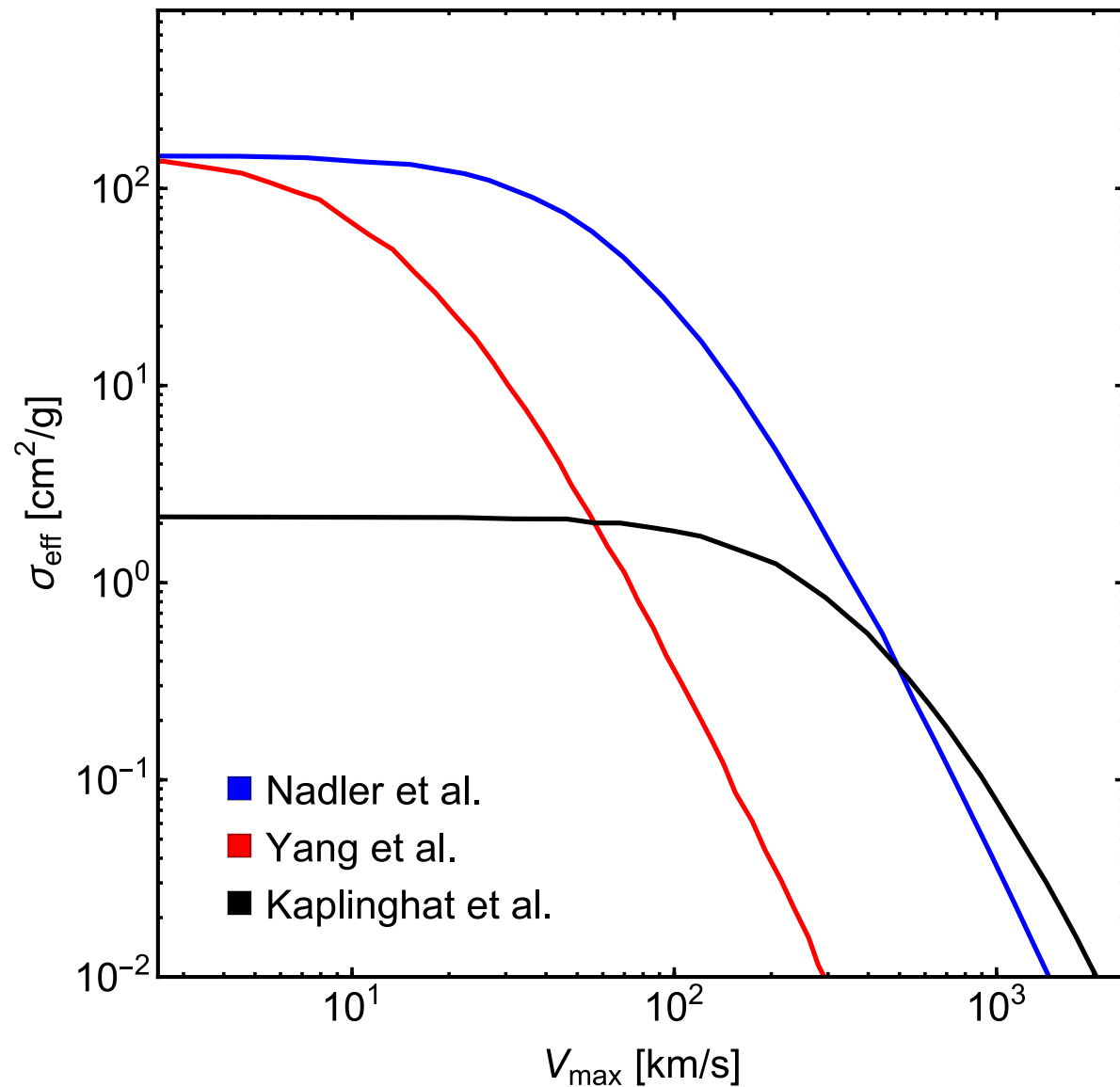


Appendix

Ultra-diffuse satellite galaxy Crater II

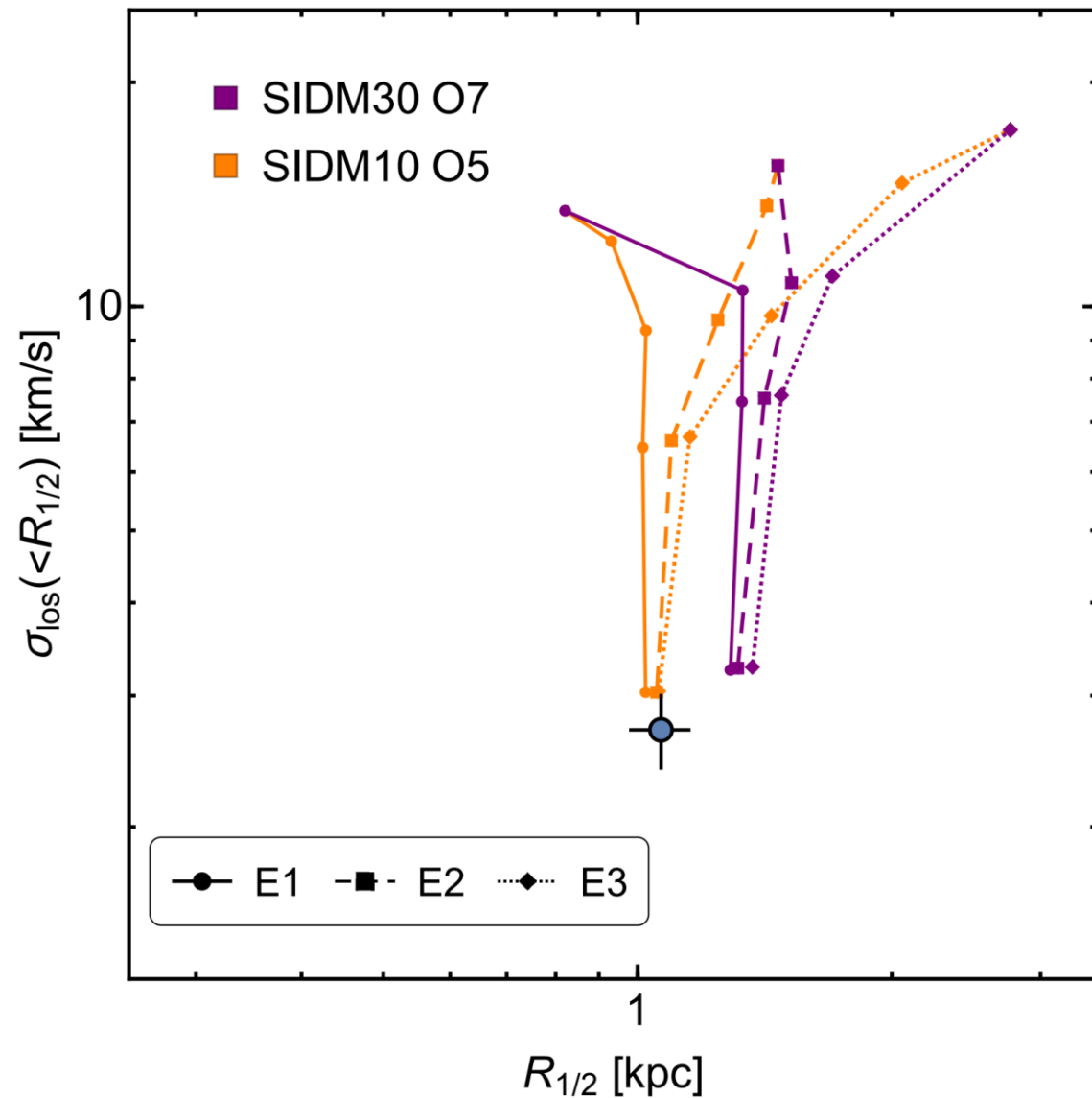


Appendix: velocity dependence



Self-interacting dark matter
Velocity-dependent cross section

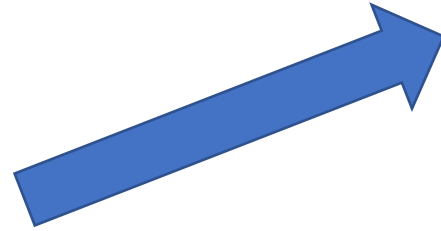
Appendix: Crater II with different cross section



Other cross sections with
different orbits

Appendix: equations of gravitational system

$$\begin{aligned}\frac{\partial M}{\partial r} &= 4\pi r^2 \rho , \\ \frac{\partial(\rho v^2)}{\partial r} &= -G \frac{M \rho}{r^2} , \\ \frac{L}{4\pi r^2} &= -\kappa \frac{\partial T}{\partial r} ,\end{aligned}$$



$$\begin{aligned}\frac{\partial \tilde{M}}{\partial \tilde{r}} &= \tilde{r}^2 \tilde{\rho} , \\ \frac{\partial(\tilde{\rho} \tilde{v}^2)}{\partial \tilde{r}} &= -\frac{\tilde{M} \tilde{\rho}}{\tilde{r}^2} , \\ \frac{\partial(\tilde{v}^3/\tilde{\rho})}{\partial \tilde{t}} &= \frac{3}{2} \frac{1}{\tilde{\rho}} \frac{\partial}{\partial \tilde{r}} \left(a \hat{\sigma}^2 + \frac{1}{\tilde{\rho} \tilde{v}^2} \right)^{-1} \frac{\partial \tilde{v}^2}{\partial \tilde{r}} .\end{aligned}$$

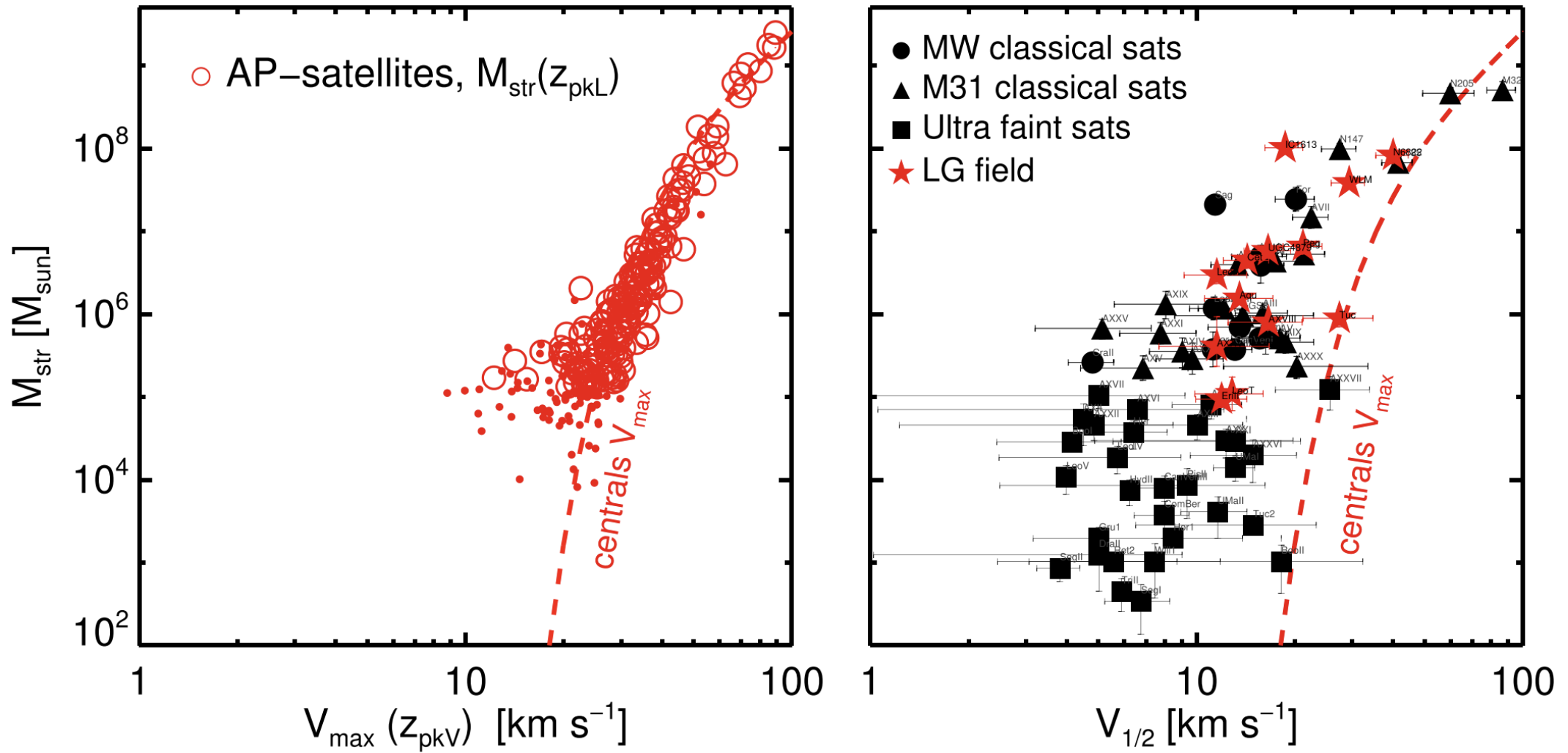
$$\begin{aligned}\frac{\partial L}{\partial r} &= -4\pi r^2 \rho \left[\left(\frac{\partial}{\partial t} \right)_M \frac{3v^2}{2} + p \left(\frac{\partial}{\partial t} \right)_M \frac{1}{\rho} \right] \\ &= -4\pi r^2 \rho v^2 \left(\frac{\partial}{\partial t} \right)_M \log \left(\frac{v^3}{\rho} \right) .\end{aligned}$$

$$\rho_0 = \frac{M_0}{4\pi R_0^3} , \quad v_0 = \left(\frac{GM_0}{R_0} \right)^{1/2} , \quad L_0 = \frac{GM_0^2}{R_0 t_0} .$$

$$\frac{L}{4\pi r^2} = -\frac{3}{2} b \rho v \left[\left(\frac{1}{\lambda} \right) + \left(\frac{v t_r}{H^2} \right) \right]^{-1} \frac{\partial v^2}{\partial r} .$$

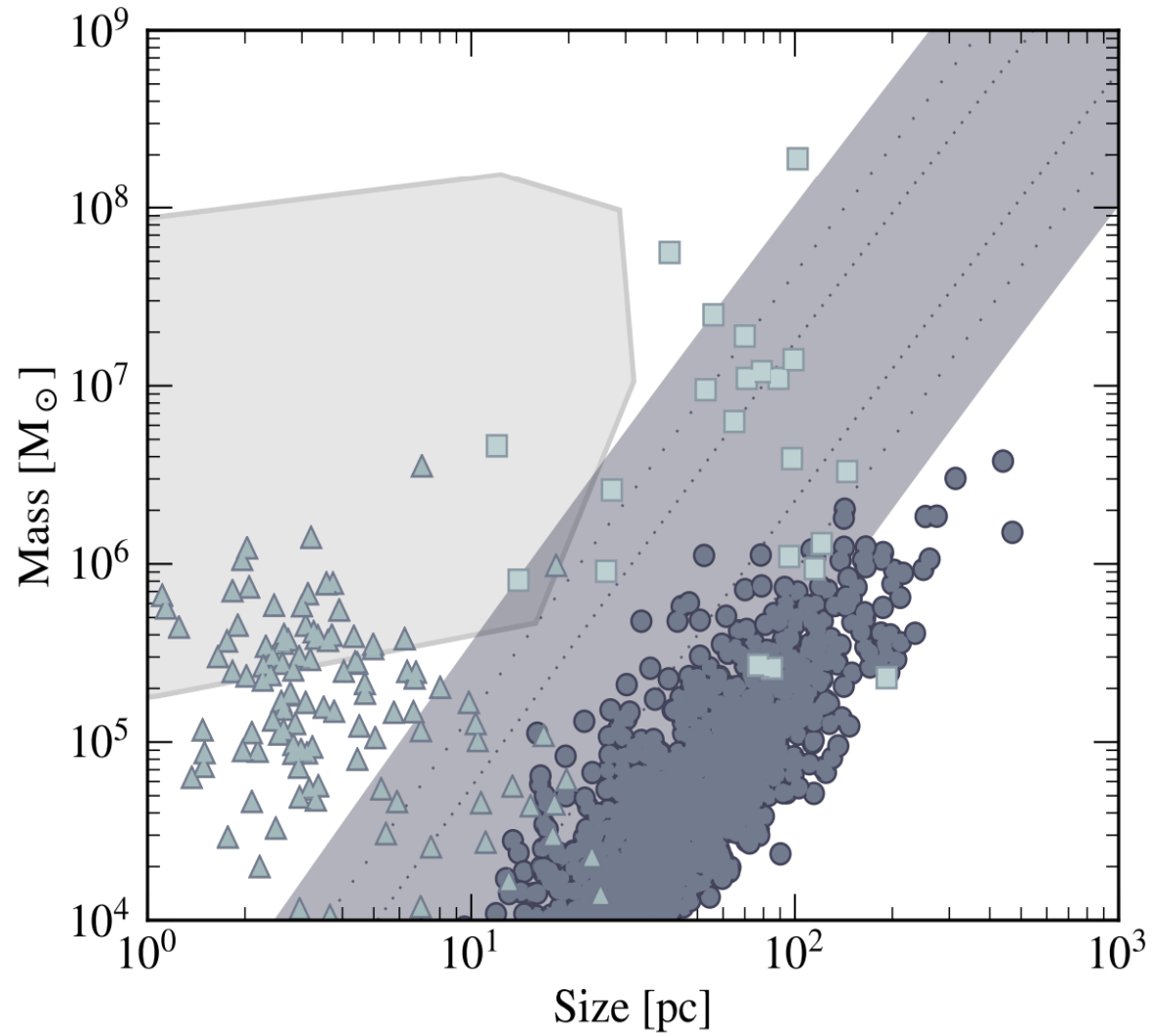
(Balberg et al 2002)

Appendix: observed satellites

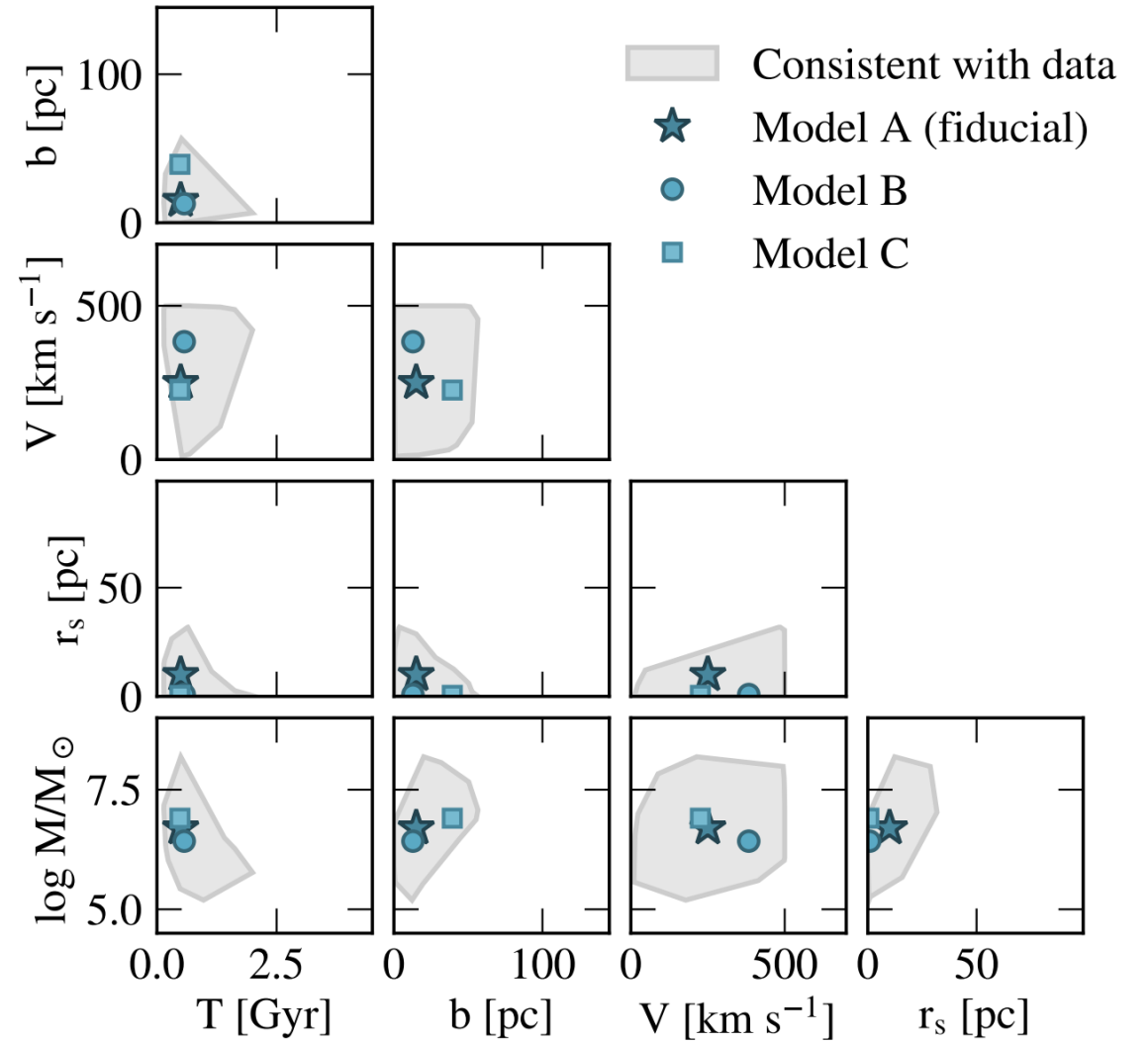


(Fattahi et. al 2018)

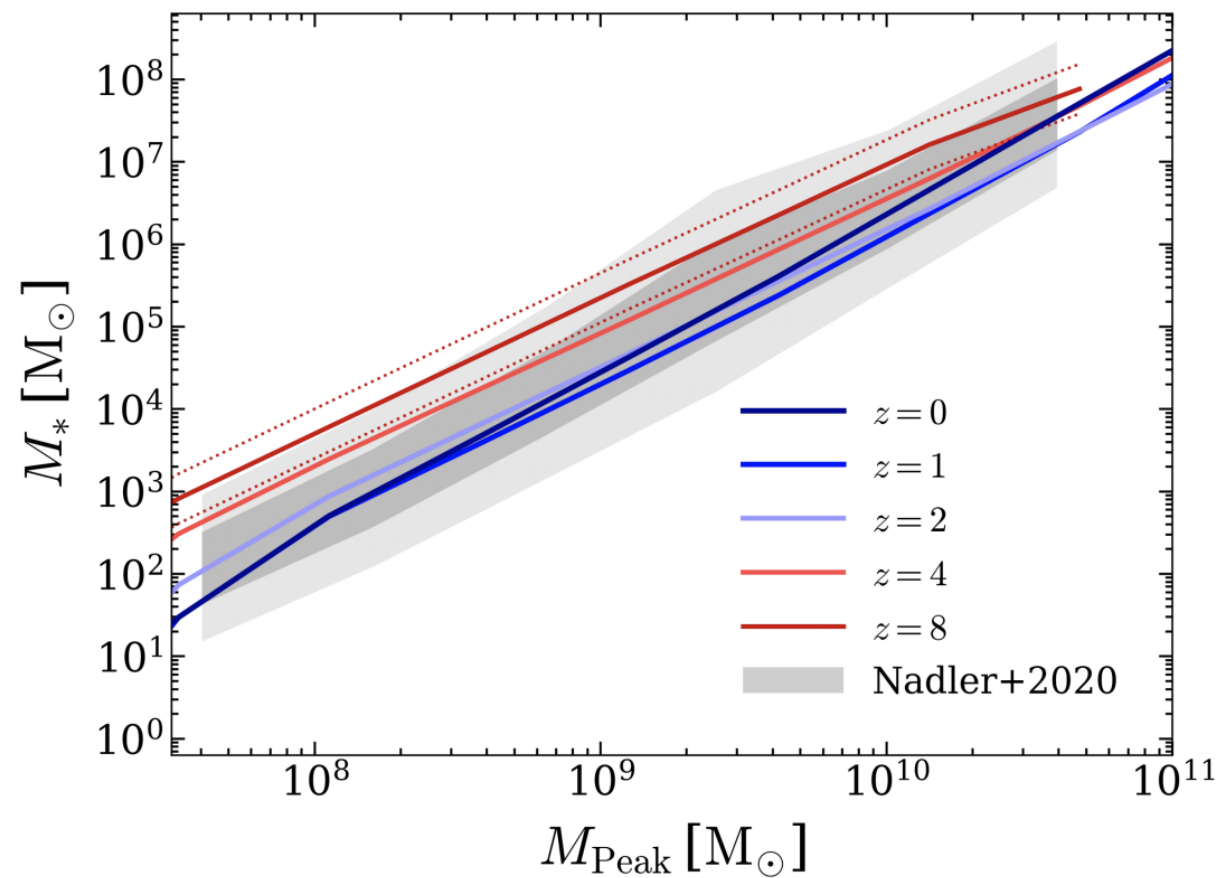
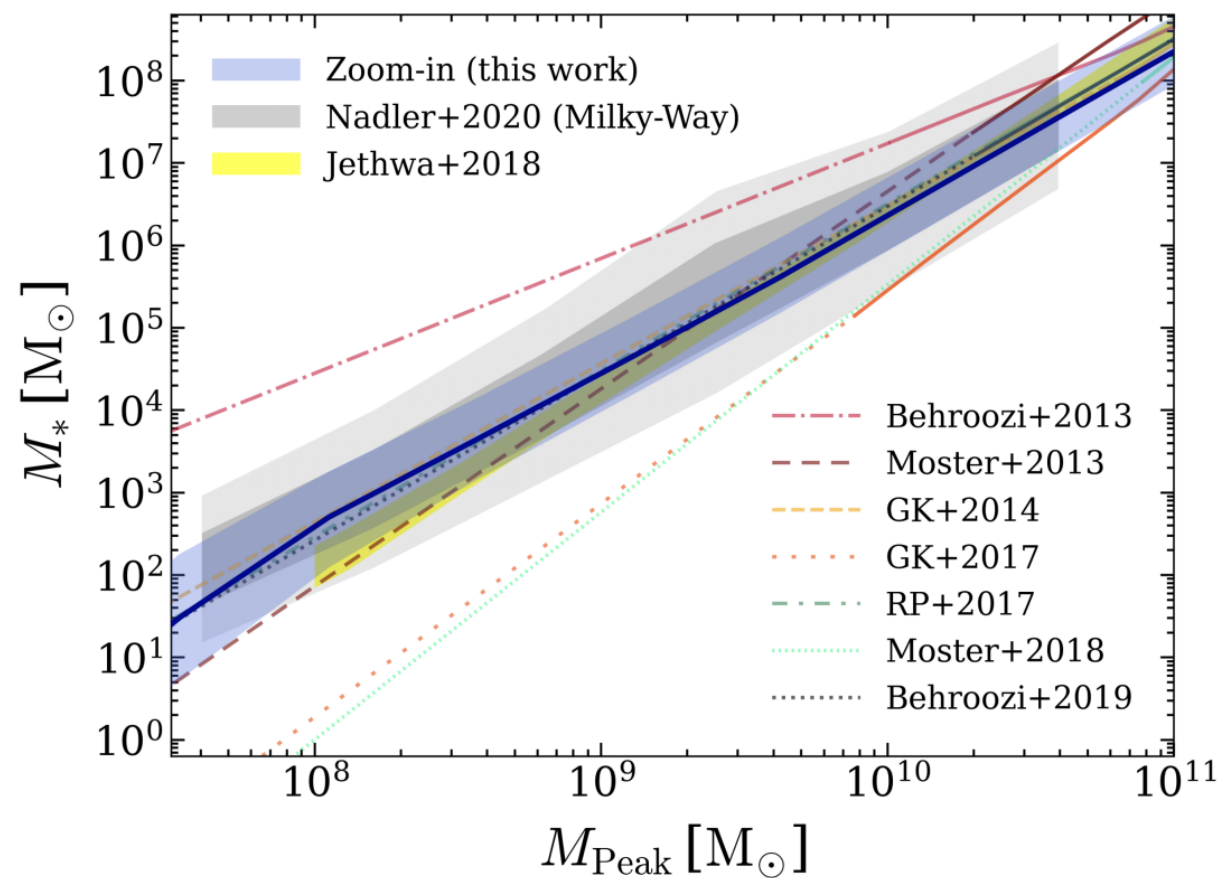
Appendix: parameter space



(Bonaca et al. 2018)

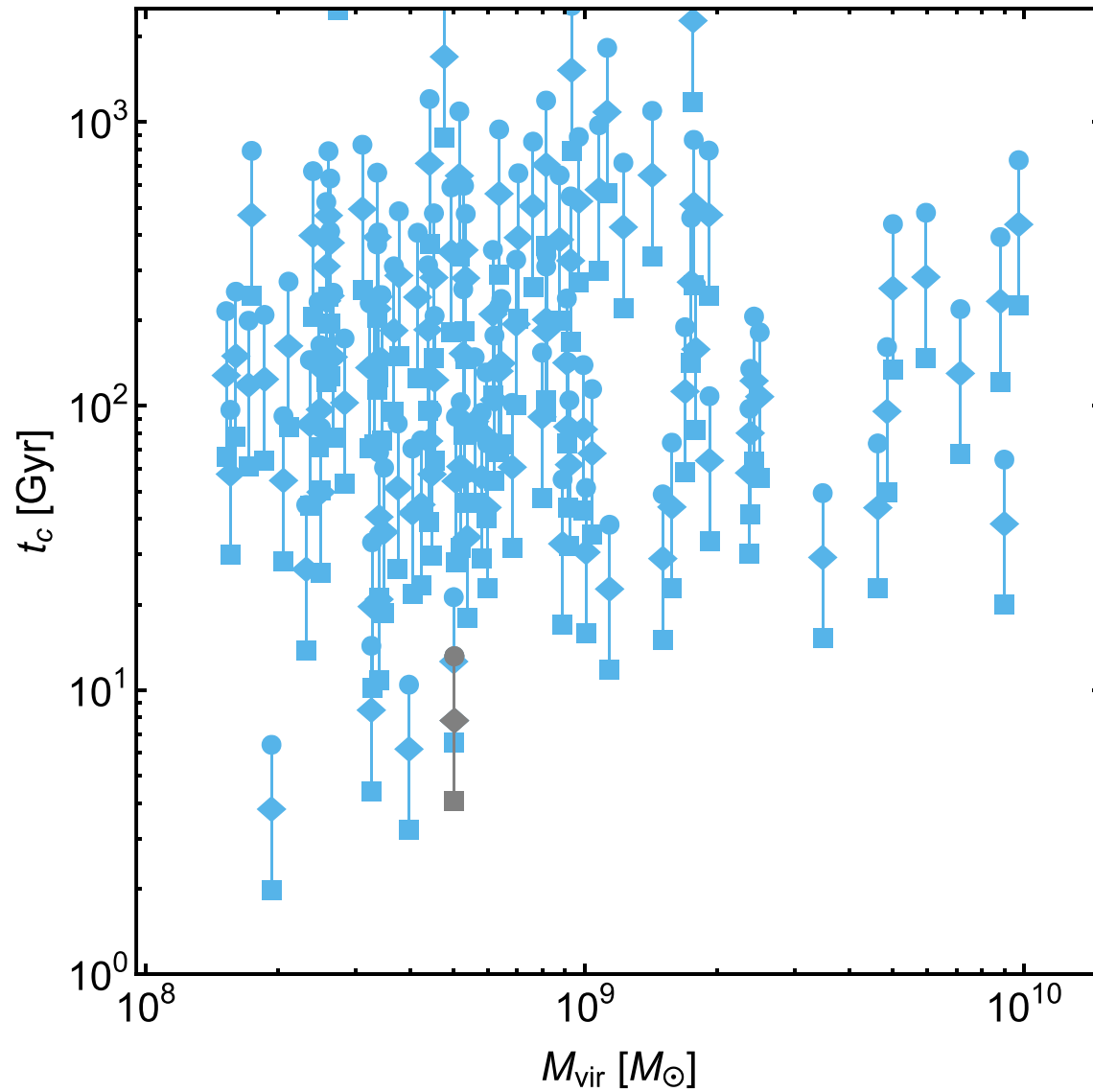


Appendix: stellar mass-halo mass relation



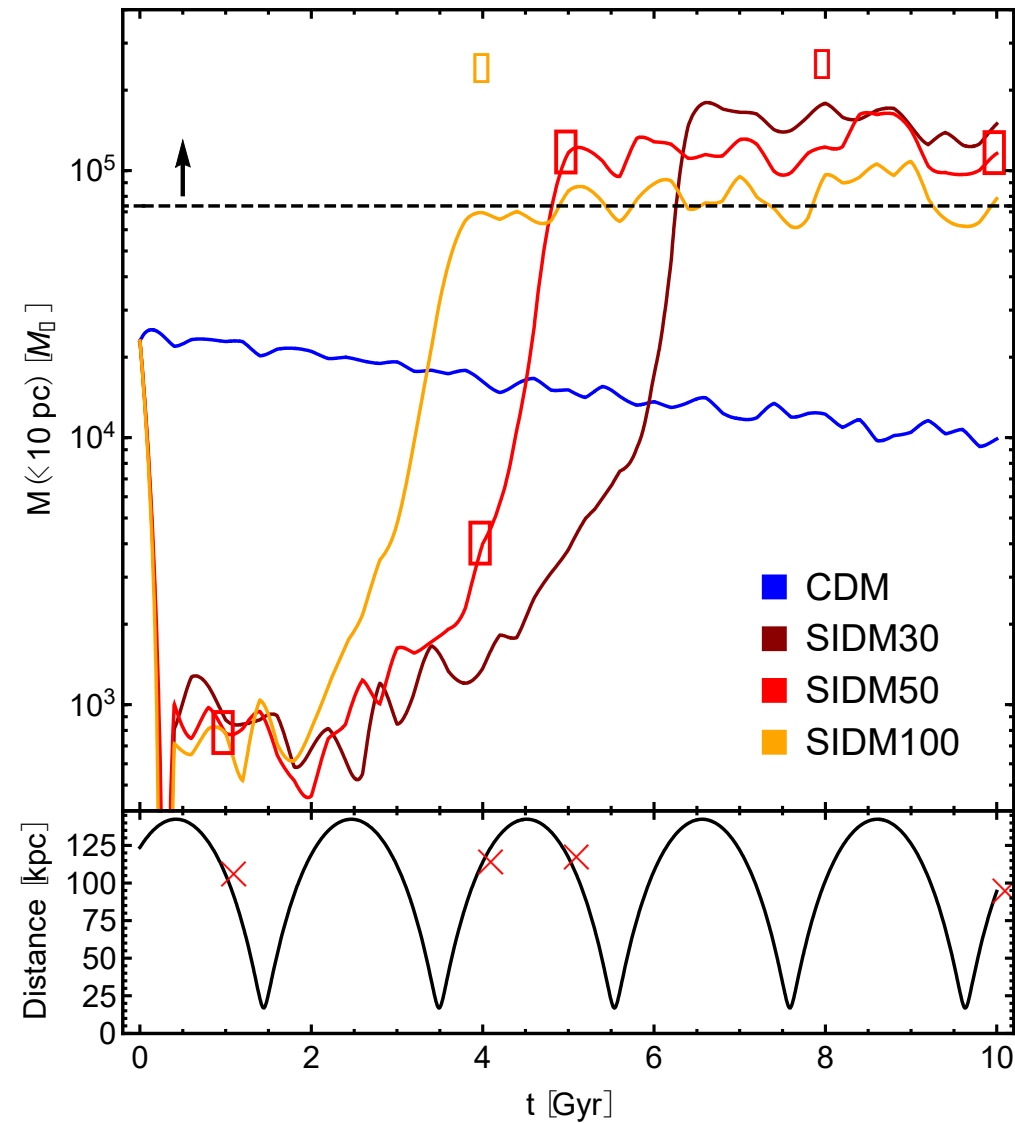
(Wang et. al 2021)

Appendix: initial condition selection

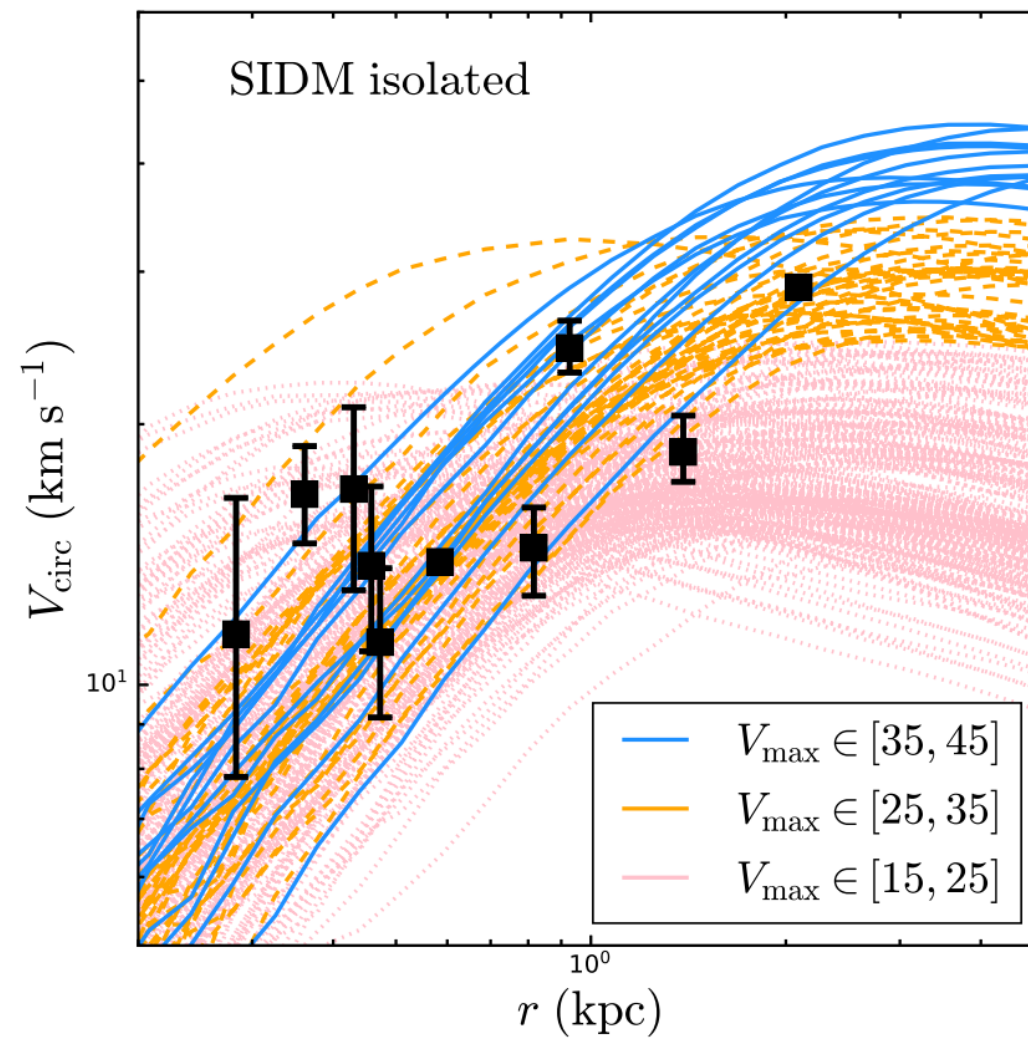
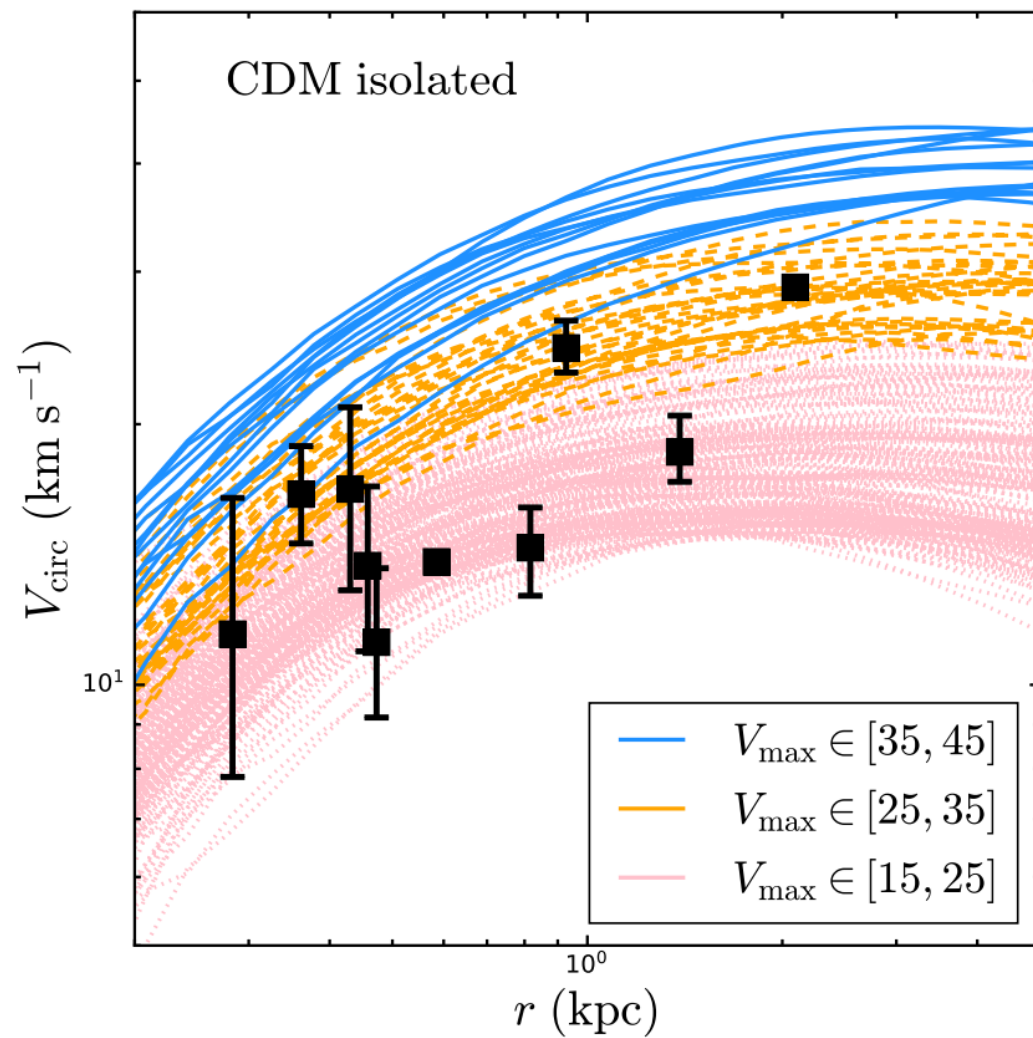


$$t_{\text{c,iso}} \simeq \frac{200}{r_s \rho_s (\sigma_{\text{eff}}/m)} \frac{1}{\sqrt{4\pi G \rho_s}}$$

Appendix: inner 10 pc mass of various cross sections



Appendix: diversity of SIDM halos



(Yang et al. 2023)

Appendix: energy inconservation of N-body simulation

