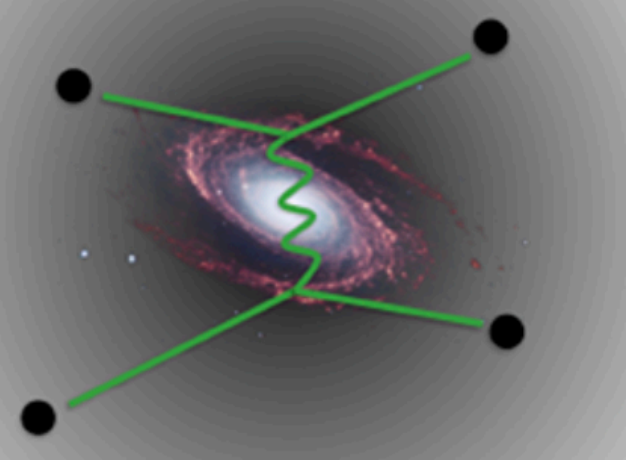


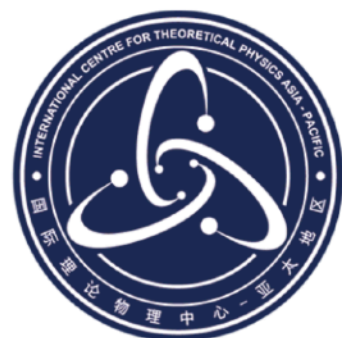


Valencia Workshop on the Small-Scale Structure of the Universe and Self-Interacting Dark Matter

Self-interacting dark matter from dark sectors

Xiaoyong Chu

(ICTP-Asia-Pacific, China)



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

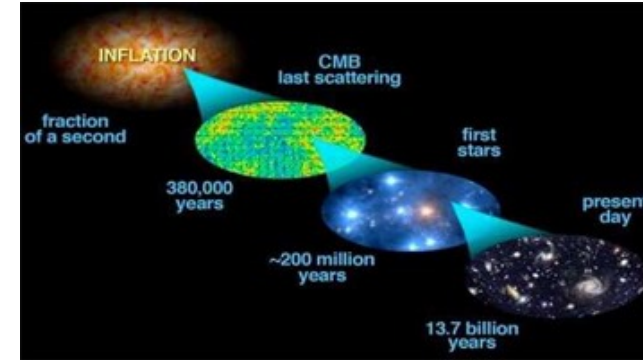


1. A paradigm shift

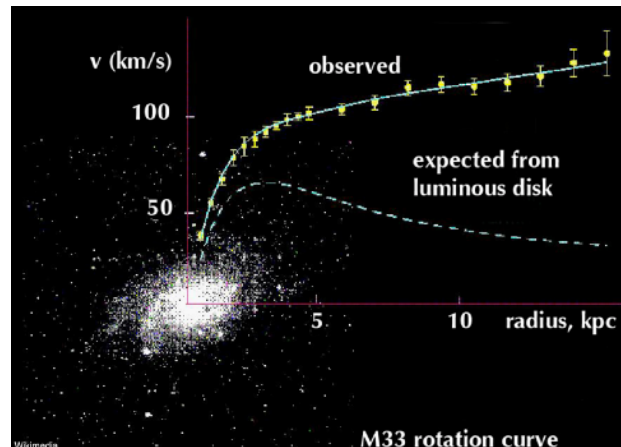
Understand **Dark Matter astrophysics** (DM): Gpc-Mpc✓, **kpc-pc**?

Structures grow:

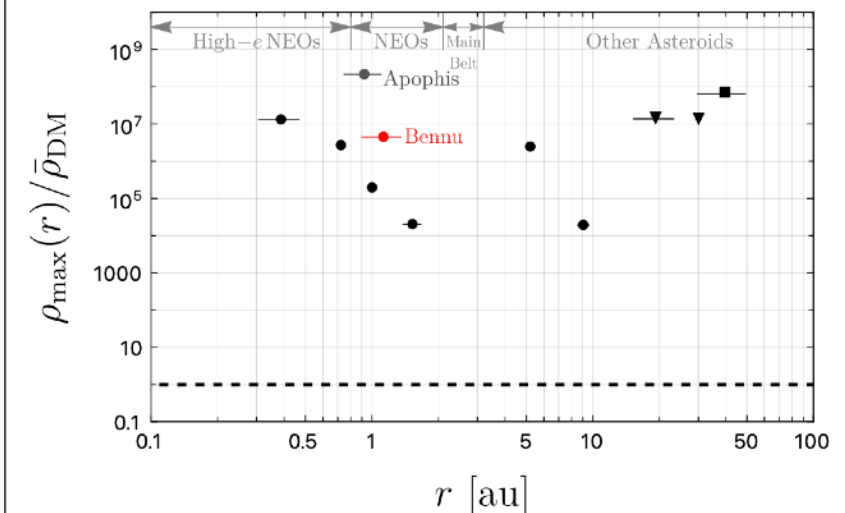
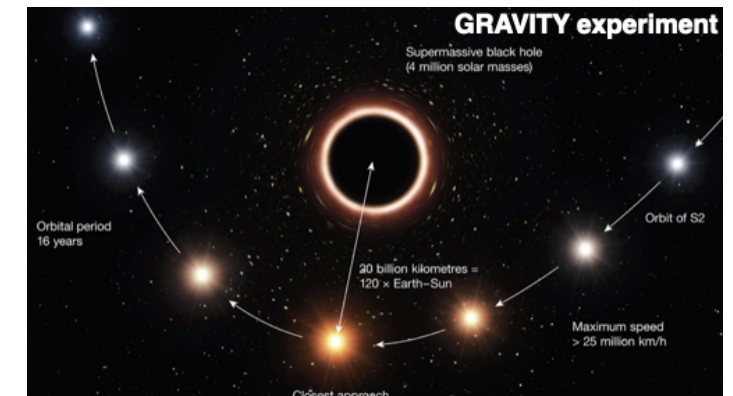
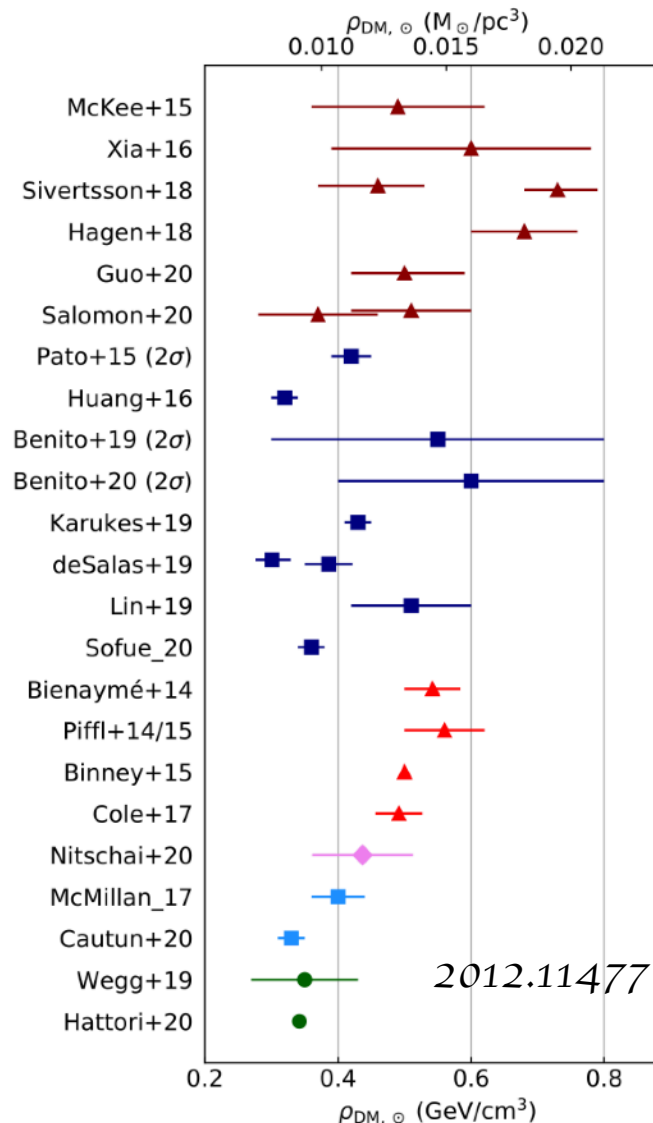
- from quantum to classic
- from dark to visible



In colliding clusters, **gas** interacts, while **DM** (+ **stars**) pass through each other.



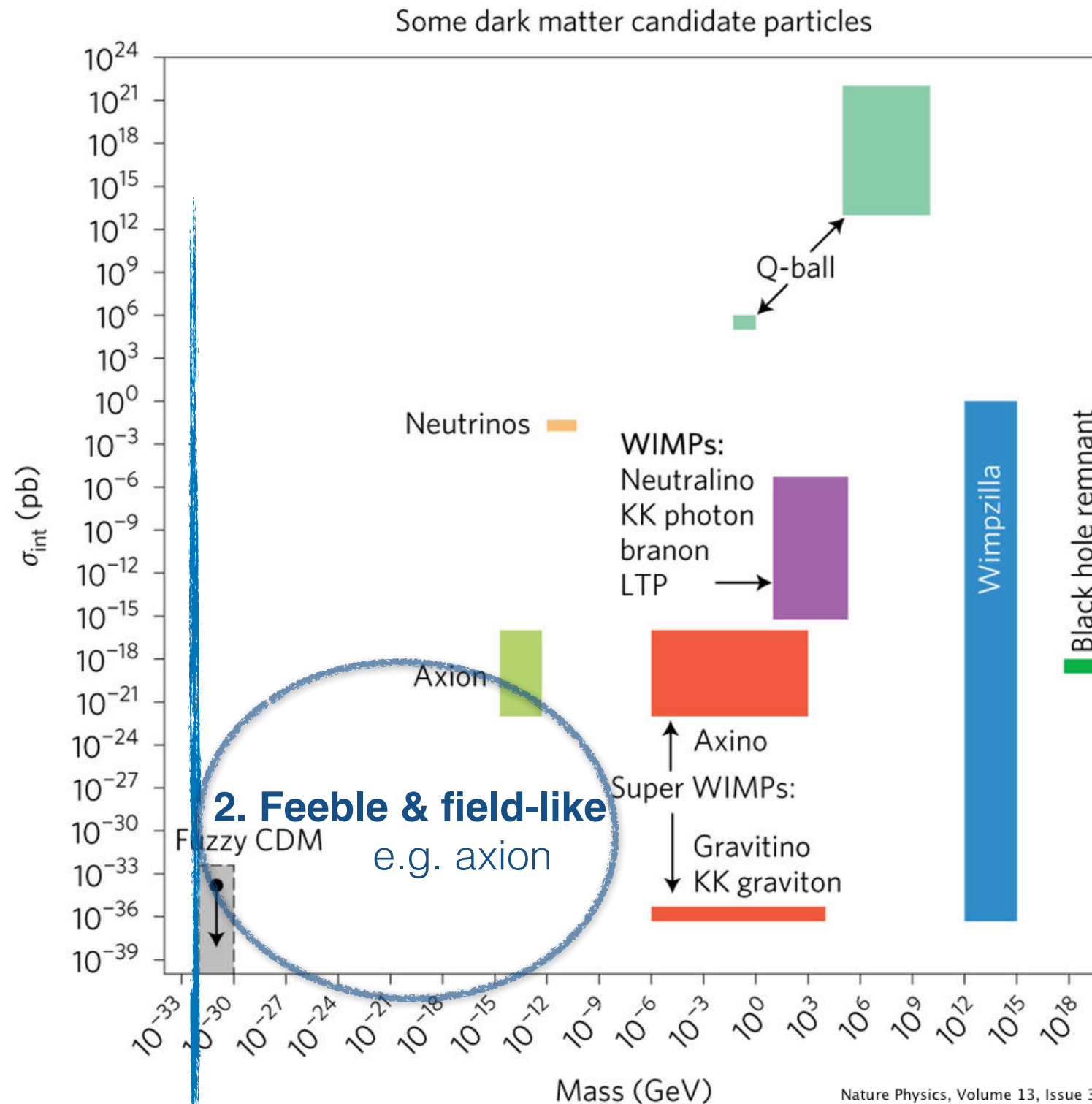
Gravity goes on well beyond the **gas-dense region** and **inner galaxy**.



Not confirmed in local group [2210.03749], or in Galactic centre, yet.

Understand **non-gravitational interactions** of DM

Conventional WIMP not found, suggesting **alternative ideas**:



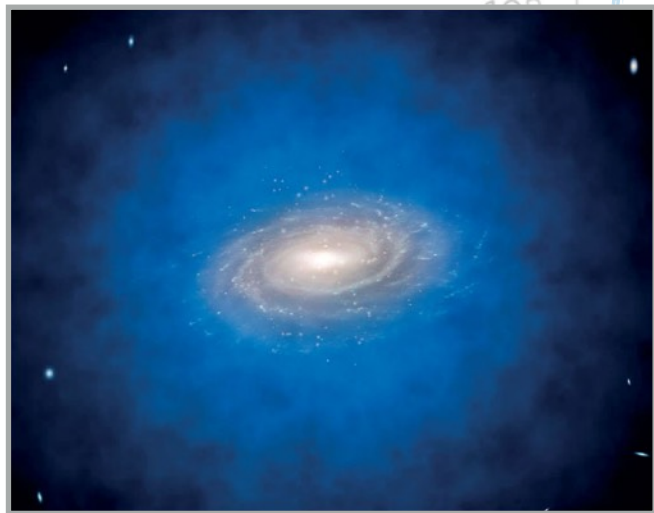
1. **big&rare**:
e.g. defects,
black holes

To make sure Universe
smooth for CMB photons.

Understand **non-gravitational interactions** of DM

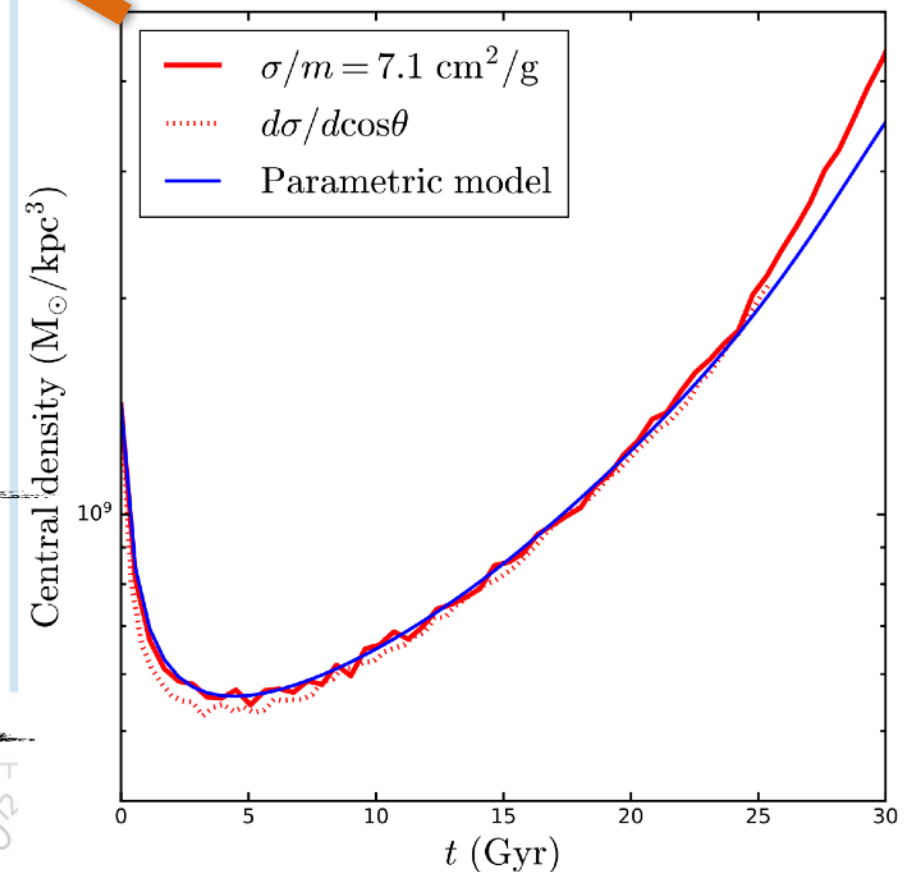
Conventional WIMP not found, suggesting **alternative ideas**:

3. Self-interaction not too far from cm^2/gram



It adds a new d.o.f. to make halos **cored**, or **core-collapsed** via propagating heat faster.

$$t_{\text{SIDM}} = \frac{1}{n_{\text{DM}} \sigma_{\text{eff}} v} = \frac{1}{\rho_{\text{DM}} \sigma_{\text{eff}} / m_{\text{DM}}} \sim \text{Gyr} \left(\frac{m_{\odot} / \text{pc}^3}{\rho_{\text{DM}}} \right) \left(\frac{\text{cm}^2 / \text{gram}}{\sigma_{\text{eff}} / m_{\text{DM}}} \right) \left(\frac{10^{-4}}{v} \right)$$

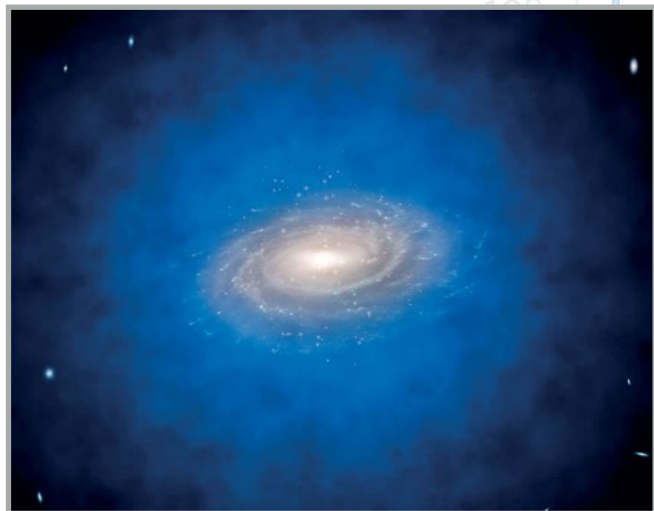


Taken from D.N. Yang, H.B. Yu et al. 2024

Understand **non-gravitational interactions** of DM

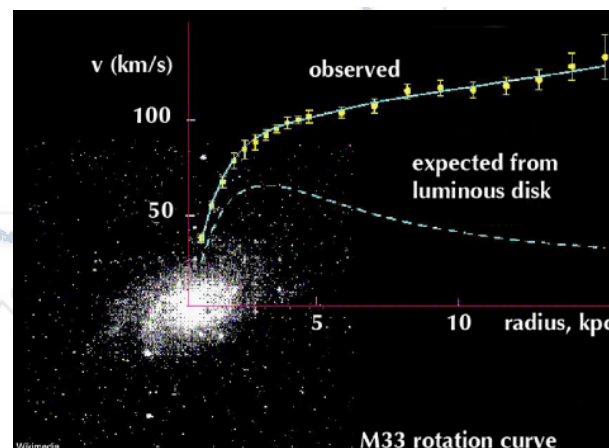
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It adds a new d.o.f. to make halos **cored**, or **core-collapsed** via propagating heat faster.

Upper bounds also exist (stronger from larger structures):



An increasing list:

- Core/cusp,
- Too-big-to-fail,
- Galaxy diversities,
- Early galaxy formation,
- SMBH last-pc problem,
- Assembly bias of dwarf galaxies, ...

Such DM candidates should satisfy:

At most **very weak** interaction
with visible matter.

Self-interaction not too far from cm^2/gram

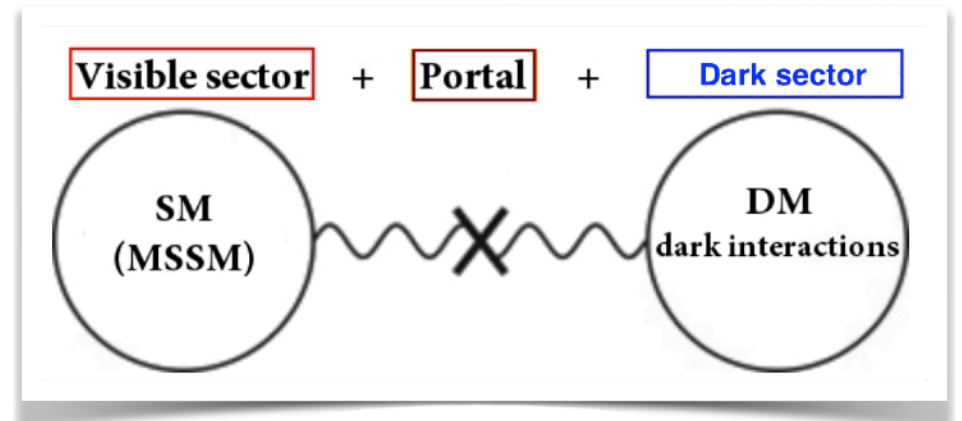
Strong self-interactions among dark matter.

Upper bounds also exist (stronger from larger structures):

Preferably, self-interaction decreases with halo size.

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A sector with its own structure.

Self-interaction not too far from cm^2/gram

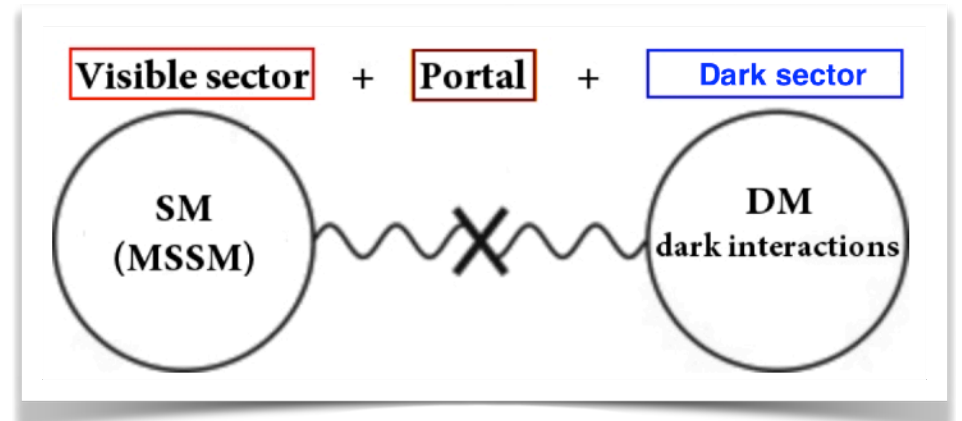
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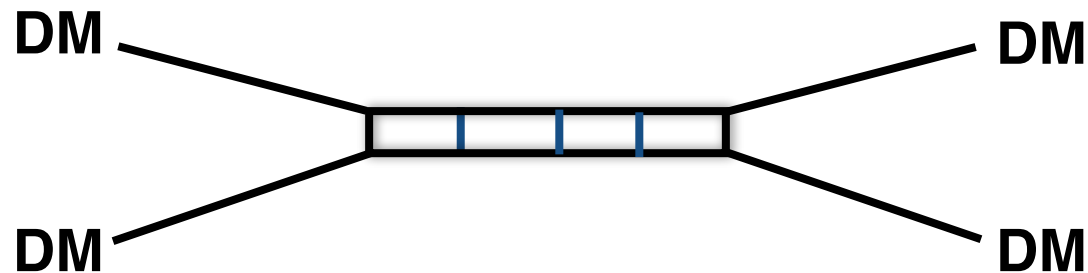


A sector with its own structure.

Self-interaction not too far from cm^2/gram

Strong self-interactions among dark matter.

A) Parametric enhancements



1. **A long-range force** (or equivalently, a light mediator)

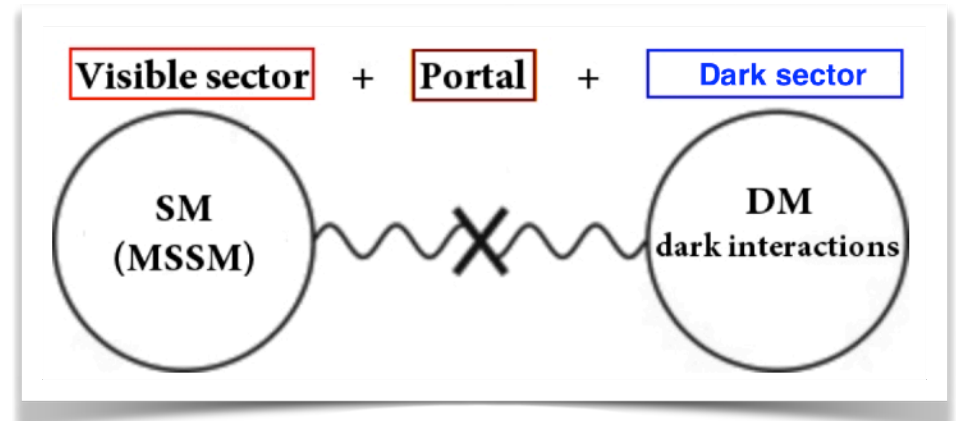
[D.N. Spergel & P. J. Steinhardt 1999, J. Feng, M. Kaplinghat & H.-B. Yu 2009, ...]

2. **A below-threshold bound state or above-threshold resonance**

[J. D. March-Russell & S. M. West 2008, E. Braaten & H. W. Hammer 2013, XC, C. García-Cely, H. Murayama 2018, ...]

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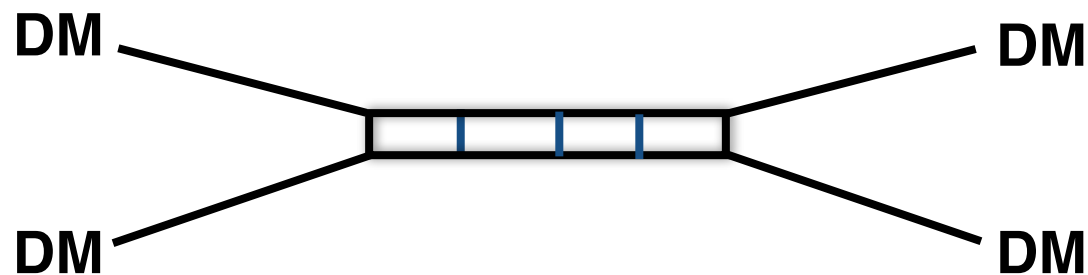


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B) Strong dynamics

Reviews: J. M. Cline, Z. Liu, et al., 2013, G. D. Kribs & E.T. Neil 2016

$$\frac{\sigma_{\text{SI}}}{m_{\text{DM}}} \sim \frac{\alpha_S^2}{m_{\text{DM}}^3} \sim \frac{1}{m_{\text{DM}}^3}$$

cm²/gram → **sub-GeV DM**

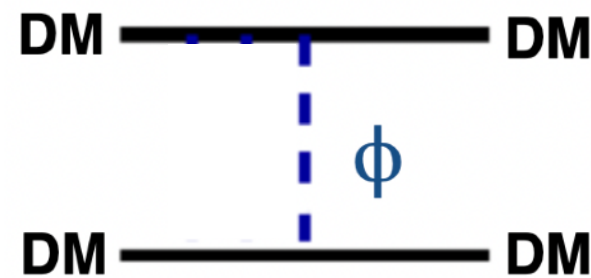
self-coupled keV-MeV DM (fluid) [F. Atrio-Barandela & S. Davidson 1997, S. Hannestad & R.J. Scherrer 2000]

More recently, R. Garani, M. Redí, A. Tesi 2022.

2. *S*IDM from parametric enhancements

Most popular **dark sector SIDM** scenario:

- introduce **a light mediator**



Even at tree level

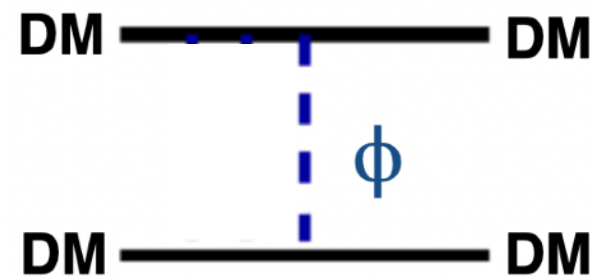
t-channel propagator $\sim \frac{1}{t - m_\phi^2}$

leading to velocity-dependent enhancement $\frac{m_{\text{DM}}^2}{m_{\text{DM}}^2 v_{\text{DM}}^2 + m_\phi^2}$

self-interaction decreases with halo size.

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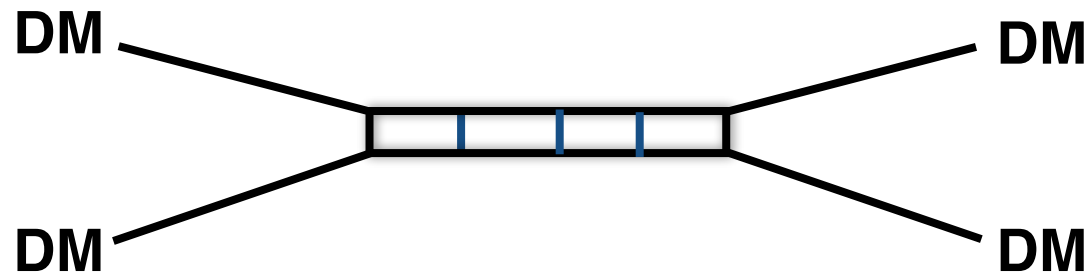
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(1st-order Born approximation does not always work)

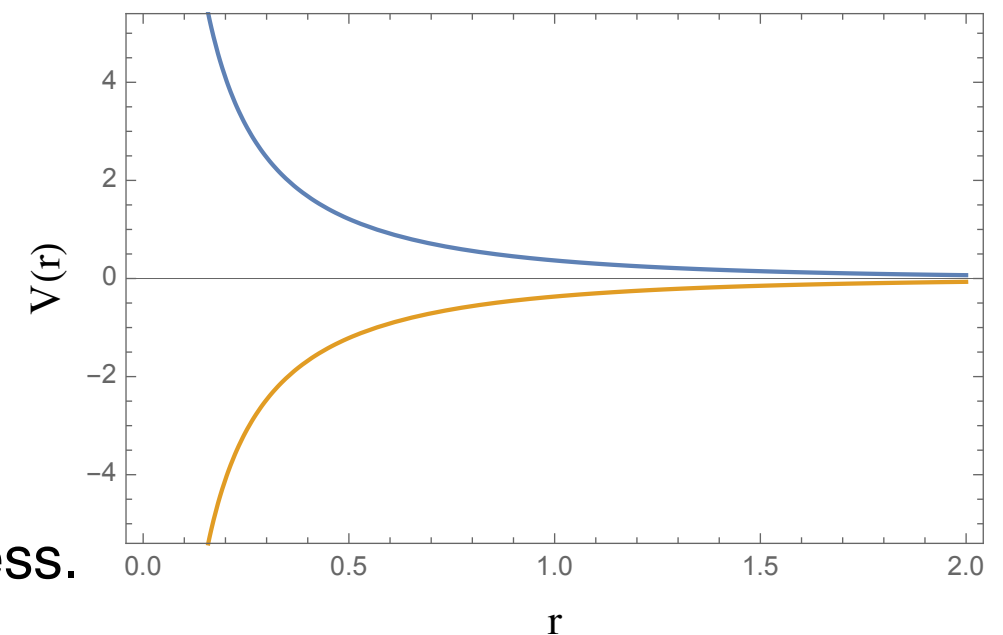


At non-relativistic limit, better described by a potential:

$$V(r) = \pm \frac{\alpha_X}{r} e^{-m_\phi r}$$

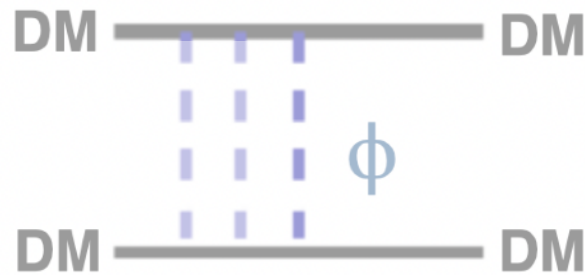
Scattered phase-shifts contain full information of the process.

(But difficult to solve for $\ell \gg 100$)

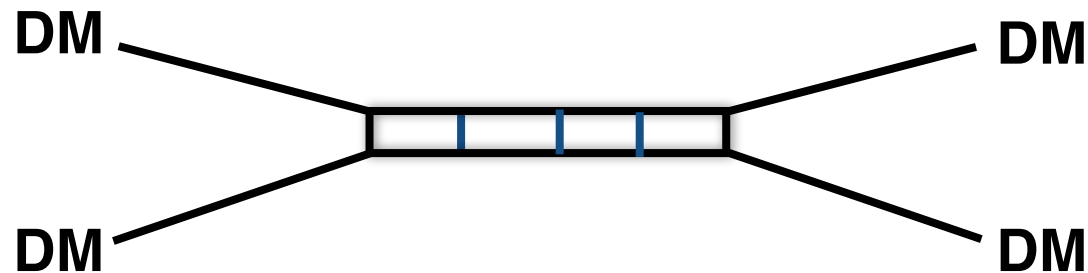


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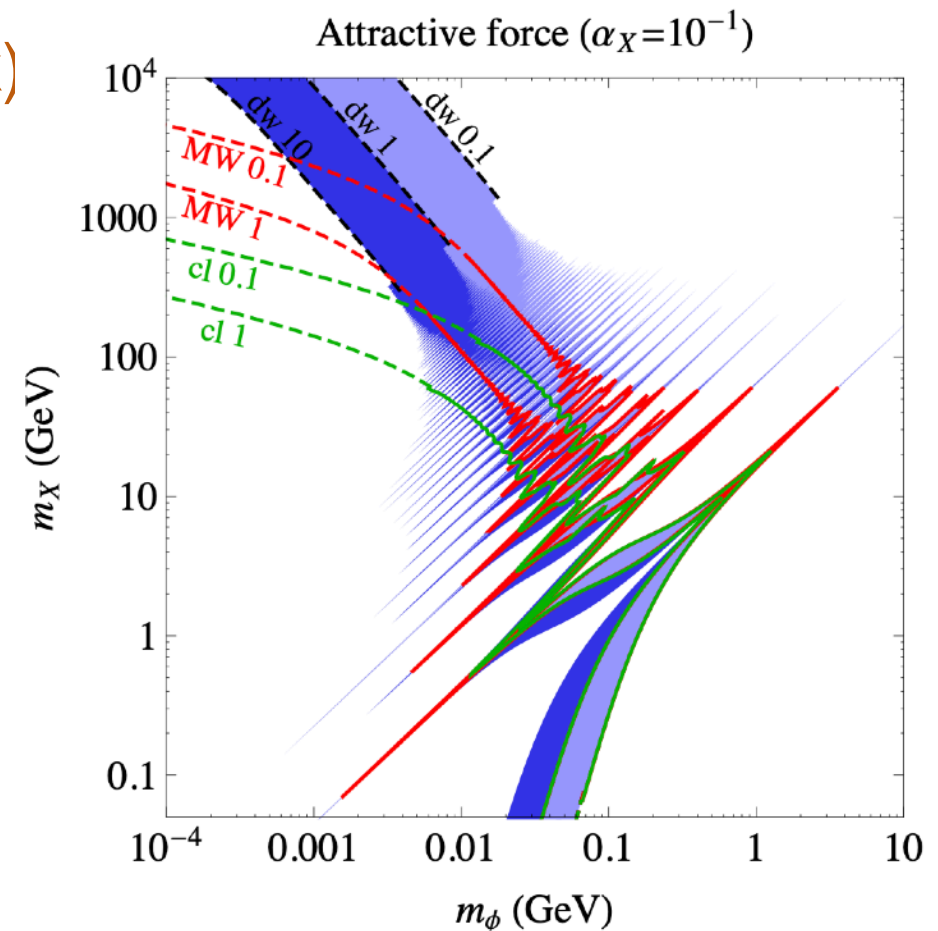


For instance, **bound state solutions** allowed for attractive

$$\alpha_X m_{\text{DM}}/m_\phi \gtrsim 1.7$$

(resonant enhancements at zero-energy bound states)

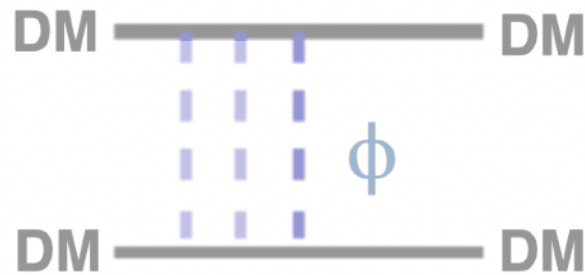
$$\sim \frac{1}{t - m_\phi^2} \frac{m_{\text{DM}}^2}{m_{\text{DM}}^2 v_{\text{DM}}^2 + m_\phi^2}$$



Taken from S. Tulín, H.-B. Yu, K. M. Zurek 2013

Most popular **dark sector SIDM** scenario:

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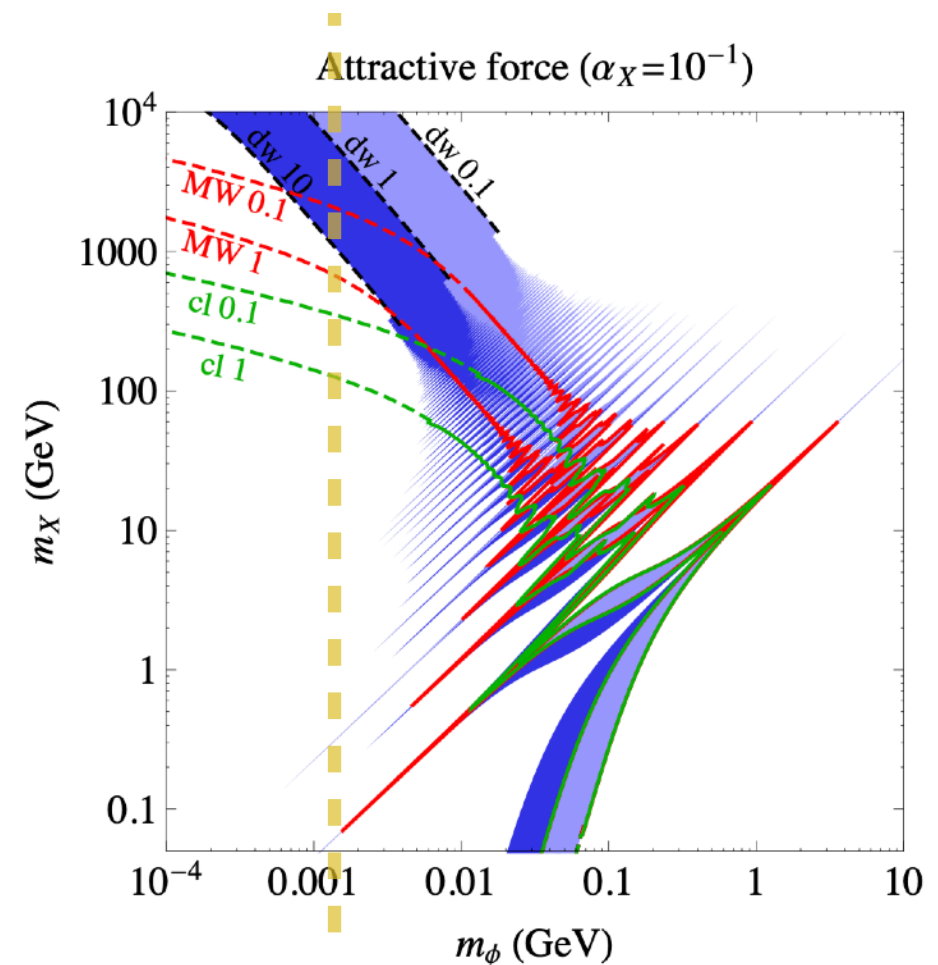


Potential signals of such dark sector models
depend on the **destiny of light mediator**:

- ↳ **displaced vertices at intensity frontier?**
- ↳ **enhanced cosmic ray excesses?**
- ↳ **anomalous stellar cooling?**
- ↳ **dark radiation?**

[J. L. Feng, M. Kaplinghat & H.-B. Yu 2009, S. Tulin, H.-B. Yu & K. M. Zurek 2012, 2013, M. Kaplinghat, S. Tulin, H.-B. Yu 2013, M. Abdullah, A. DiFranzo, A. Rajaraman, Tim M. P. Tait, et al. 2014, N. Bernal, XC, C. Garcia-Cely, T. Hambye, B. Zaldivar 2015, N. Bernal, XC, S. Kulkarni, J. Pradler 2019, R. Coy, T. Hambye, M. H.G. Tytgat & L. Vanderheyden 2021, ...]

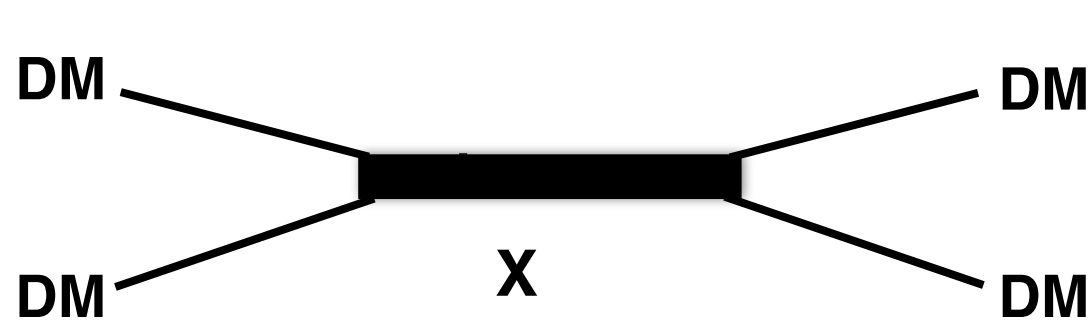
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Taken from S. Tulin, H.-B. Yu, K. M. Zurek 2013

New interesting **dark sector SIDM** scenarios:

- introduce **a heavy mediator X**



s-channel propagator $\sim \frac{1}{s - m_X^2 + i\Sigma_X(s)}$

Large enhancement at $m_X \sim 2m_{\text{DM}}$

&

velocity-dependence depending on location of m_X

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Large enhancement at $m_X \sim 2m_{\text{DM}}$

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velocity-dependence depending on location of m_X

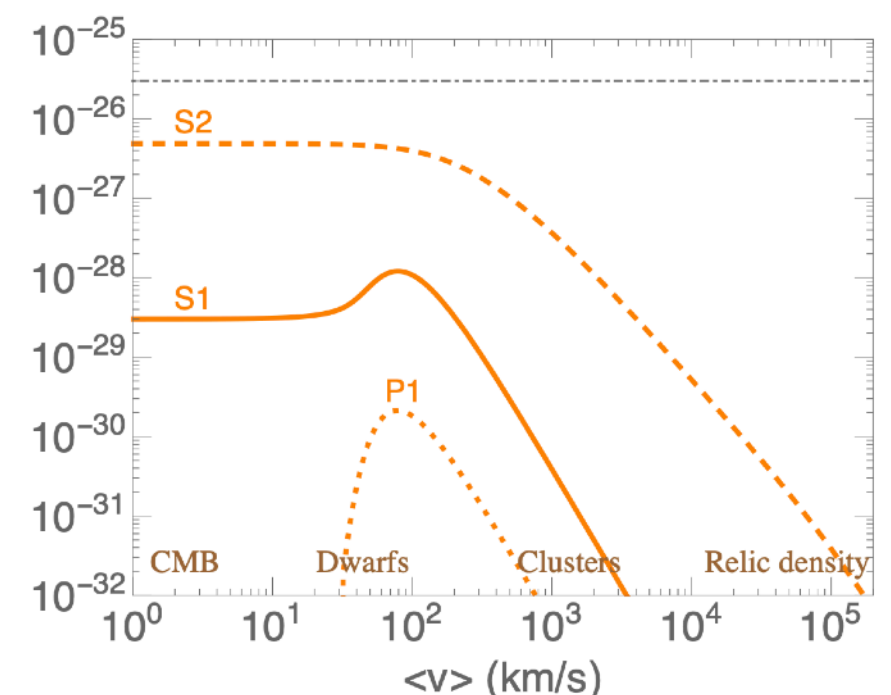
a) If $m_X > 2m_{\text{DM}}$, X is treated as a Breit-Wigner resonance [XC, C. García-Cely, H. Murayama 2018]

self-scattering cross section peaks at the resonant velocity:

$$v_R^2 \hat{=} \frac{m_X - 2m_{\text{DM}}}{2m_{\text{DM}}} \ll 1$$

and decreases quickly for $v \gg v_R$.

- novel feature in astrophysics [e.g. D. Gilman, Y.-M. Zhong & J. Bovy 2022, ...].
- fine-tuning to get tiny v_R ? [Y.-D. Tsai, R. McGehee, H. Murayama 2020, ...]



New interesting dark sector SIDM scenarios:

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s-channel propagator $\sim \frac{1}{s - m_X^2 + i\Sigma_X(s)}$

Large enhancement at $m_X \sim 2m_{\text{DM}}$

&

velocity-dependence depending on location of m_X

b) If $m_X < 2m_{\text{DM}}$, X may naturally appear as a weak bound state

appears already for an attractive light mediator.

No peak, as $v_R^2 \hat{=} \frac{m_X - 2m_{\text{DM}}}{2m_{\text{DM}}} < 0$

self-interaction decreases with halo size.

→ Such dark sector scenarios also have interesting applications in BAU/co-genesis [e.g. *M. Becker, K. Fridell, J. Harz & C. Hati 2024, ...*]

3. *S*IDM from Strong dynamics

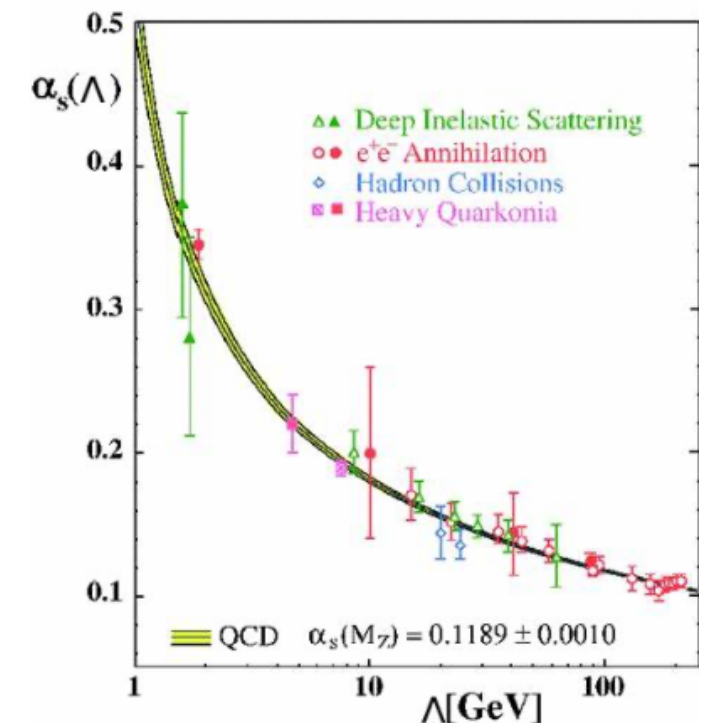
Lightest stable state from strong dynamics

The SIDM candidate can be

- dark baryon (if it is like the SM);
- dark pion (light-quark limit);
- dark glueball (heavy-quark limit);
- large-N nuclei, dark atom,....

J. M. Cline, Z. Liu, et al., 2013,

G. D. Kribs & E.T. Neil 2016



Need to be described by chiral EFT or lattice methods.

SIDM needs strong-interactions for sub-GeV masses.

(Interesting energy-scale for phase-transition-induced GW/PBH)

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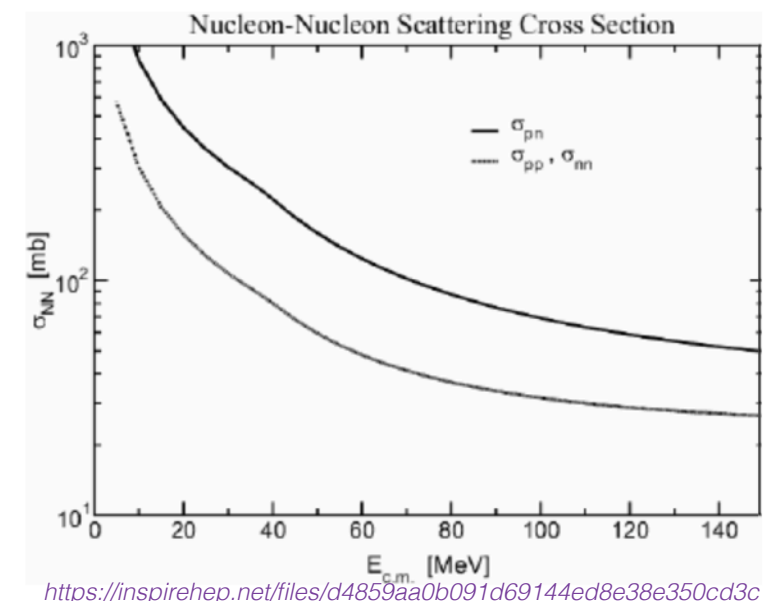
Production mechanism:

DM could be asymmetric, to prevent significant self-annihilation.

5 GeV to explain coincidence, or other co-genesis?

Velocity-dependent scattering:

Similar to SM nucleon scattering, naively dominated by **pion-exchange**.



<https://inspirehep.net/files/d4859aa0b091d69144ed8e38e350cd3c>

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*J. M. Cline, Z. Liu, et al., 2013,
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Production mechanism:

DM has to be symmetric, two-body annihilation seems too strong.

One thus needs **tuned freeze-in**, or $N \rightarrow 2$ freeze-out (FO):

↳ also applies to weaker coupled sub-MeV SIDM.

(e.g. production mechanisms of sterile neutrinos)

No obvious built-in mechanism to have velocity-dependence.

Lightest stable state from strong dynamics

The SIDM candidate can be

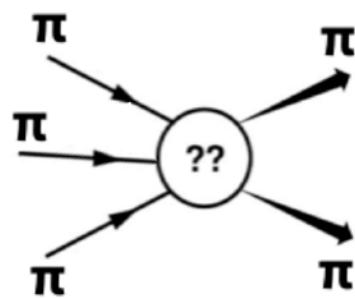
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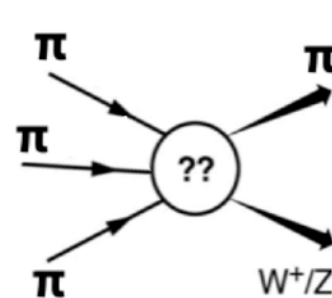
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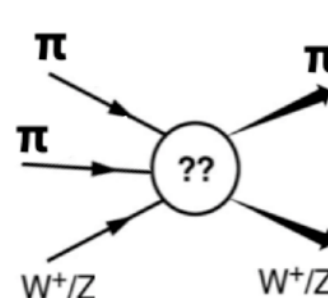
SIMP

[Y. Hochberg, E. Kuflik, T. Volansky, J. G. Wacker
1402.5143, ...]



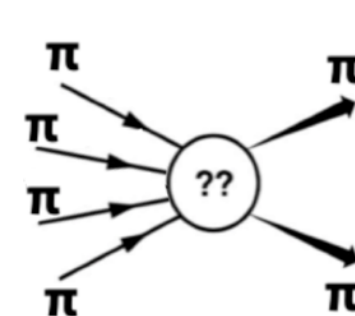
Enable forbidden

FO [J. M. Cline, H. Liu, T. R. Slatyer, W. Xue, 1702.07716, ...]



Co-SIMP

[J. Smirnov, J. F. Beacom,
2002.04038, ...]



Four-body FO

[N. Bernal, XC 2015, ...]

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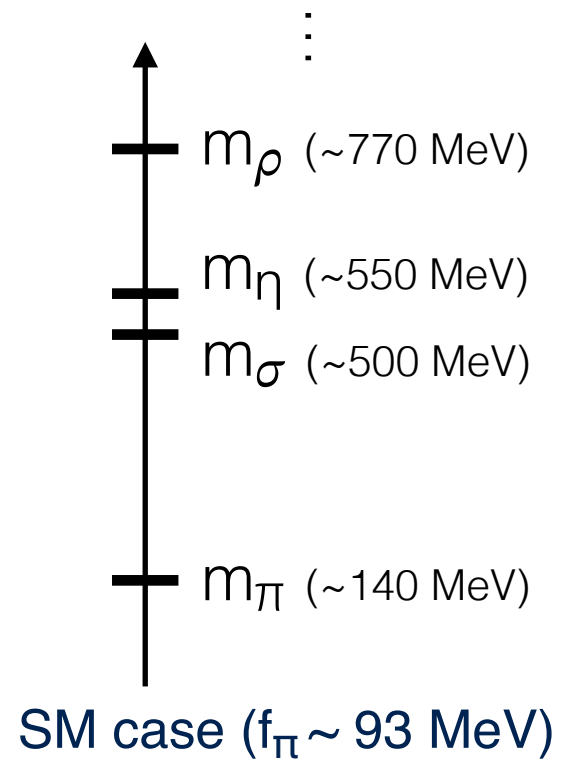
Velocity-dependent scattering?

Not explicitly.

Luckily (or unluckily), sectors of strong-dynamics are complicated.

Lightest stable state from strong dynamics

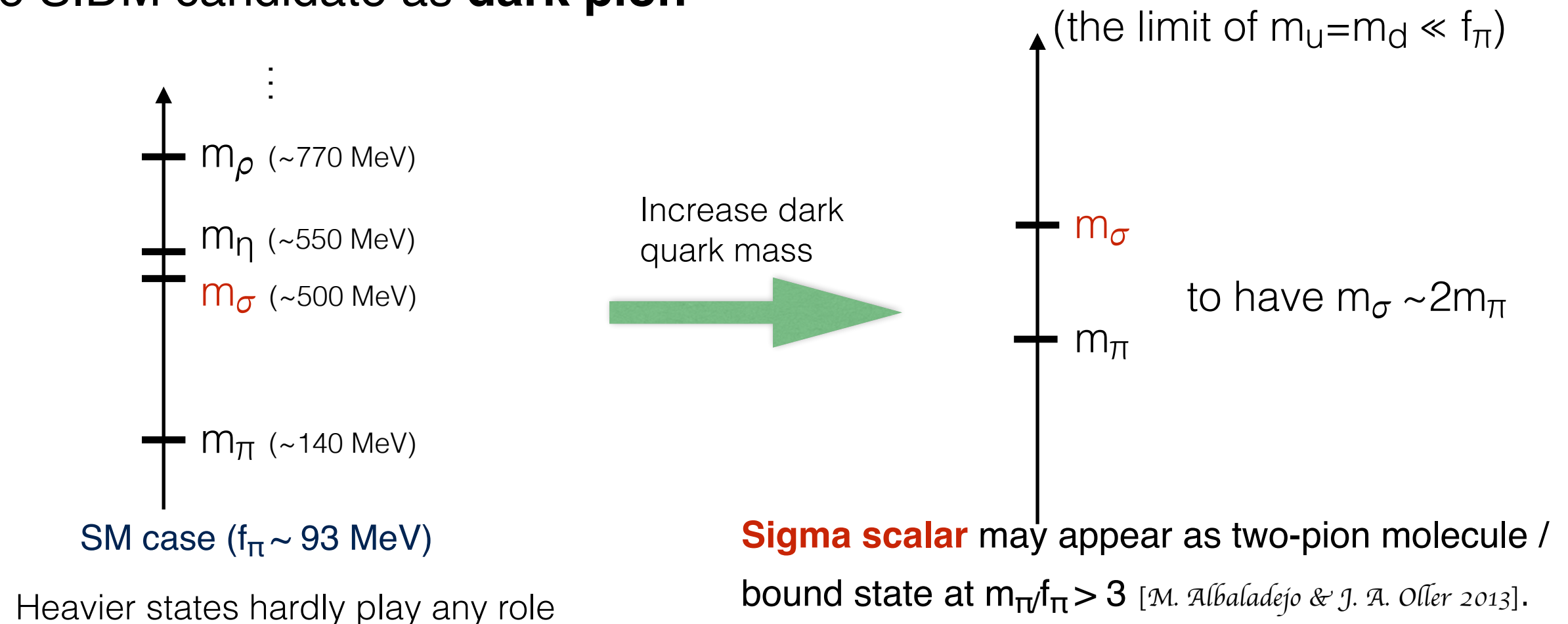
Take SIDM candidate as **dark pion**



Heavier states hardly play any role

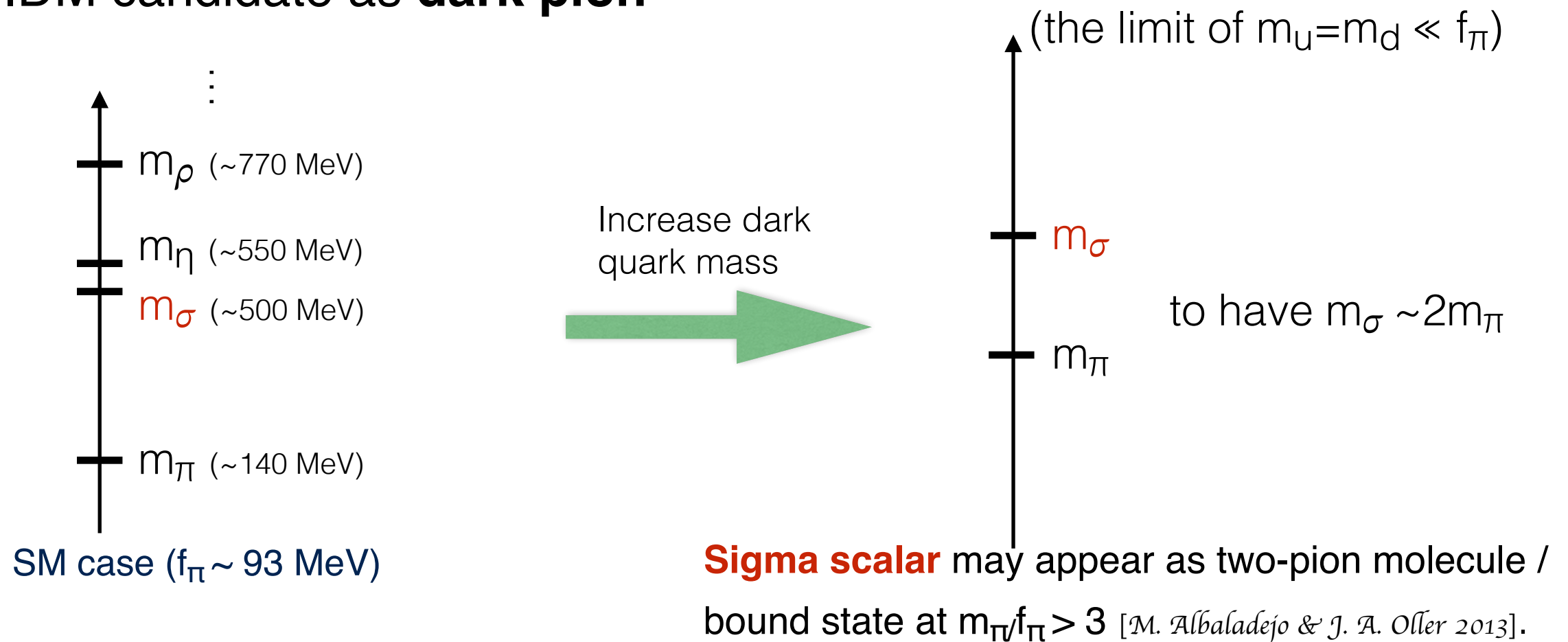
Lightest stable state from strong dynamics

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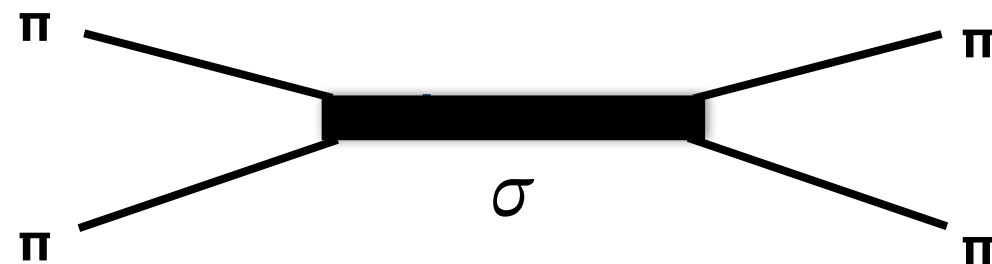
Lightest stable state from strong dynamics

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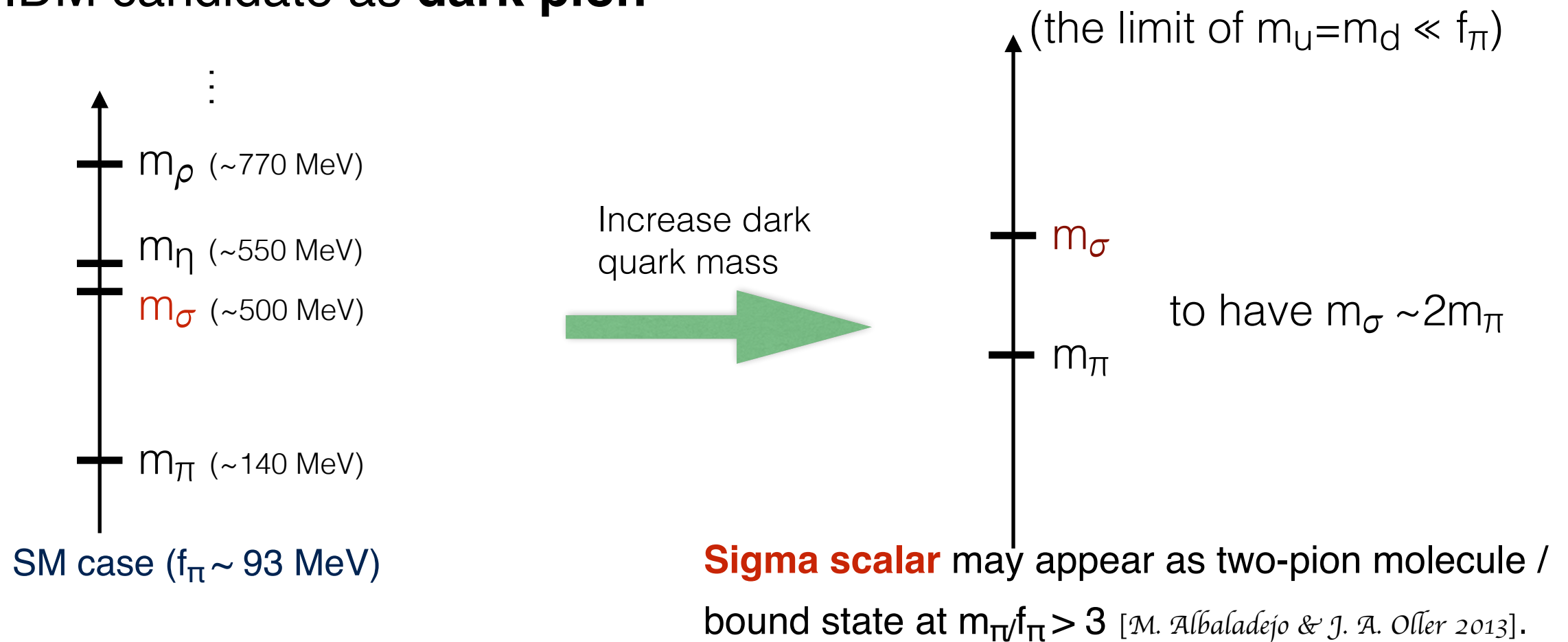
One interesting case is $m_\sigma \lesssim 2m_\pi$, appearing as a **(meta-)stable bound state**:

1. self-interaction decreases with halo size.



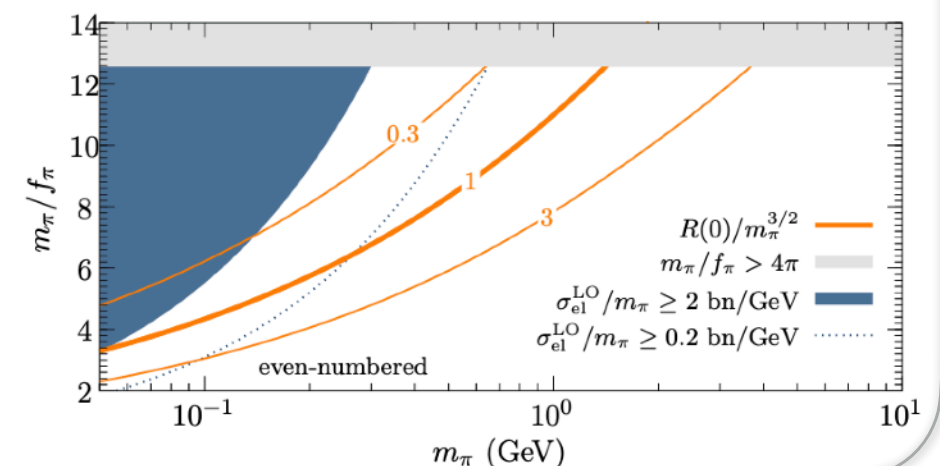
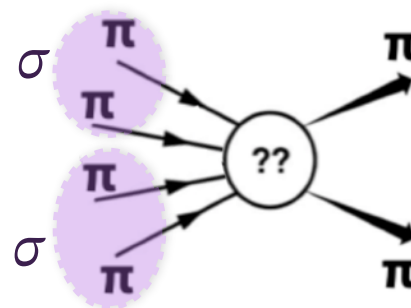
Lightest stable state from strong dynamics

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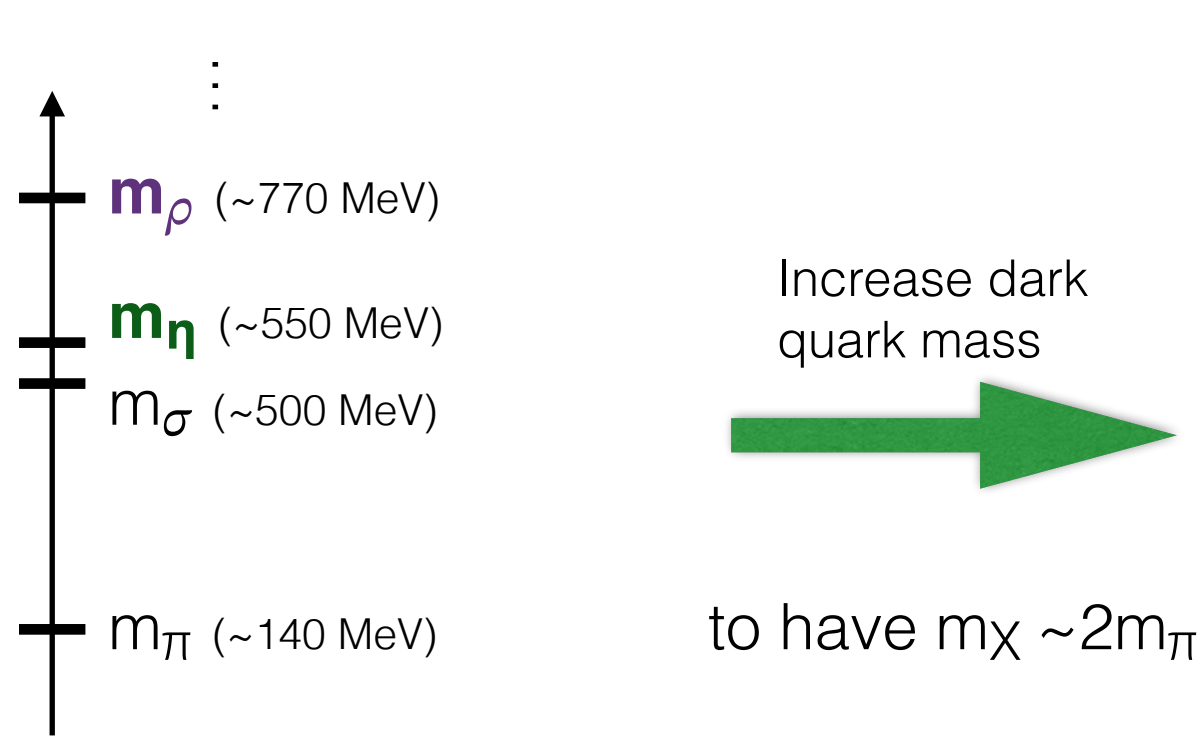
One interesting case is $m_\sigma \lesssim 2m_\pi$, appearing as a **(meta-)stable bound state**:

2. Freeze-out can be enhanced by bound state formation [XC, M. Nikolic, J. Pradler 2024].



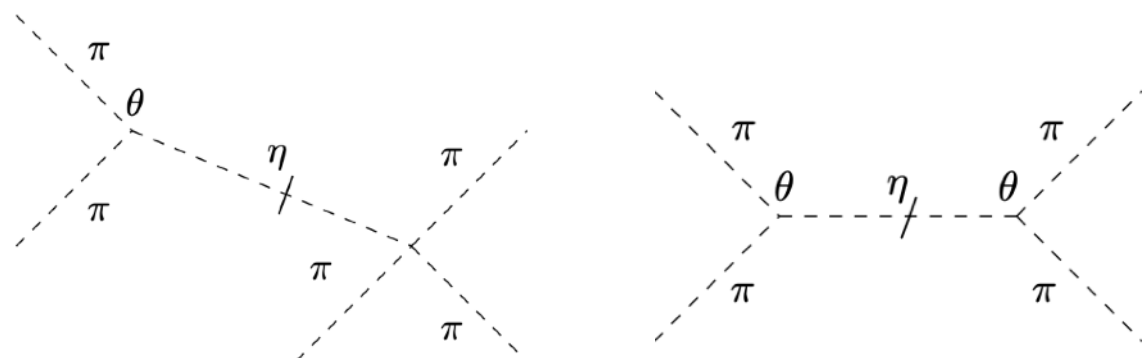
Lightest stable state from strong dynamics

Take SIDM candidate as **dark pion**



Eta meson, as a pseudo-scalar, couples to two pions via a **CP-violating phase**.

[C. García-Cely, G. Landini & O. Zapata 2024].

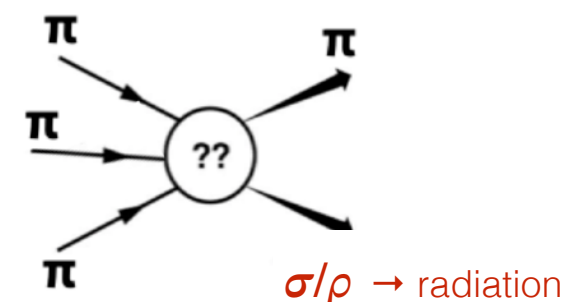


Rho meson may play a similar role if $m_\rho \sim 2m_\pi$

[E. Bernreuther, N. Hemme, F. Kahlhoefer & S. Kulkarni 2023]

(with additional p-wave suppression)

Mixing with Z/H may induce additional decay $\rightarrow$ enable forbidden FO.



Lightest stable state from strong dynamics

Take SIDM candidate as **dark pion** (and the limit of $m_u=m_d \ll f_\pi$)

Beyond mesons, other particles can help too.

such as **gauged Wess-Zumino-Witten terms** and/or **dark axion**.

- If dark quarks are charged under a **local U(1)** [e.g. *P. Braata & M. Postma 2023*]

$$\begin{aligned}\mathcal{L}_{\text{WZW}} = & \frac{2N_c}{15\pi^2 f_\pi^5} \epsilon^{\mu\nu\rho\sigma} \text{Tr} [\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi] - i \frac{N_c g_d}{3\pi^2 f_\pi^3} \epsilon^{\mu\nu\rho\sigma} V_\mu \text{Tr} (Q \partial_\mu \pi \partial_\rho \pi \partial_\sigma \pi) \\ & + \frac{N_c g_d^2}{4\pi^2 f_\pi} \epsilon^{\mu\nu\rho\sigma} (\partial_\mu V_\nu) V_\rho \text{Tr} (Q^2 \partial_\sigma \pi) . \text{ (Not the same as a dark rho meson)}\end{aligned}$$

- If a **global U(1)** breaking leads to dark axion [most recently, *Yang Bai, Ting-Kuo Chen et al. 2023*].

$$\mathcal{L} \ni -\frac{3c_{gg}}{16\pi^2 f_a} a F_{\mu\nu}(\rho) F^{\mu\nu}(\rho) \quad \text{(anomalous terms and/or WZW terms)}$$

SIDM candidate can also be **dark glueball**:

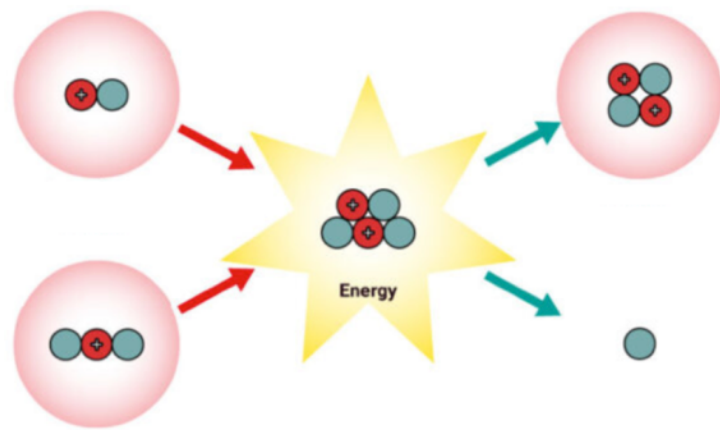
- **Glueball-onium is also possible** [e.g. *F. Giacosa, A. Pilloni, E. Trottí 2021*]

Or, **many stable states** from strong dynamics

The SIDM candidate can be

- dark baryon (if it is like the SM);
- dark pion (light-quark limit);
- dark glueball (heavy-quark limit);
- **large-N nuclei, dark atom,**

[e.g. *M. B. Wise and Y. Zhang 2014, E. Hardy, R. Lasenby, J. March-Russell & S. M. West, 2014, 2015, M. I. Gresham, H. K. Lou, and K. M. Zurek, 2017, 2018 ...*]



↳ Dark fusion?

[e.g. *S. D. McDermott 2017, ...*]

↳ Energy equipartition?

[See Daneng Yang's talk]

↳ Finite-sized (puffy) DM?

[*XC, C. García-Cely & H. Murayama 2018*]

Binding/kinetic energy
heats up halo core?

Form-factor induces
velocity-dependence?

4. Beyond dark sector models

What we are now?

Strong self-interactions without underlying UV theory

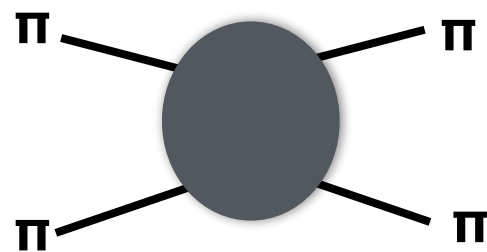
→ Similar to **hadron physics before quarks**.

S-matrix (bootstrap) methods developed in 1960s.



Assuming analyticity, crossing, unitarity etc, **elastic scattering** amplitude has certain form:

$$T_{ab,cd} = A(s, t, u)\delta_{ab}\delta_{cd} + A(t, s, u)\delta_{ac}\delta_{bd} + A(u, t, s)\delta_{ad}\delta_{bc}$$



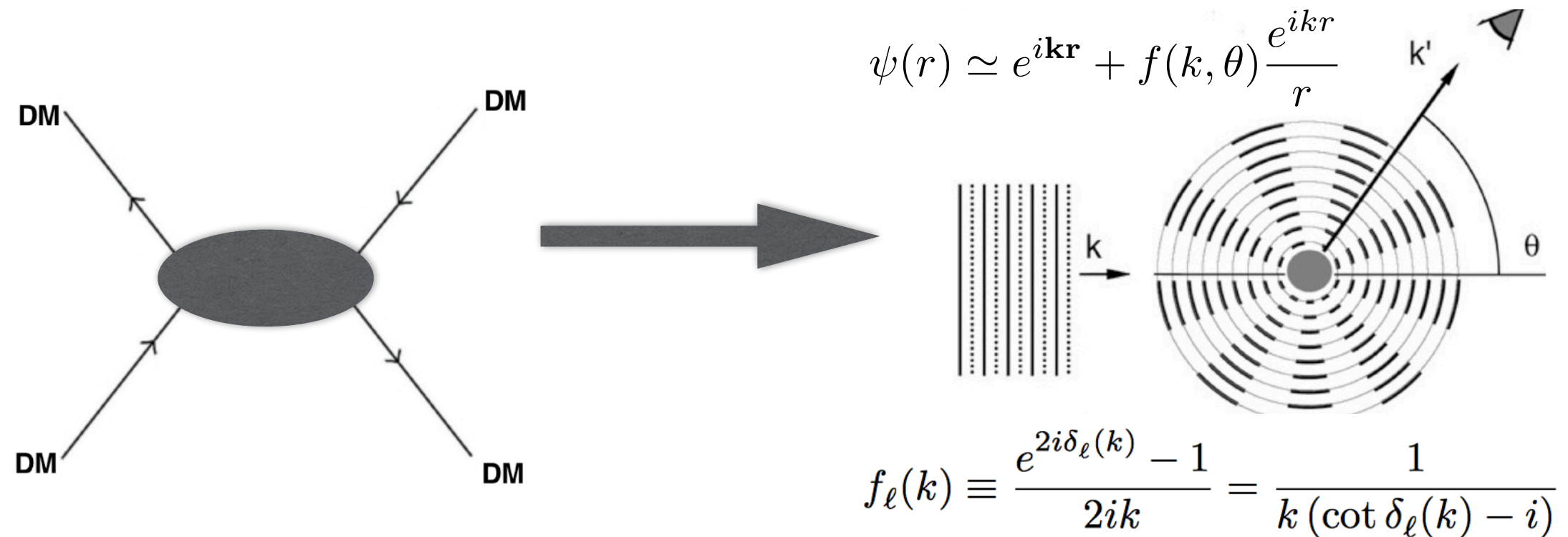
$$\begin{aligned} A(s, t, u) = & T_0 + \frac{1}{\pi} \int_4^\infty dx \frac{\sigma_1(x)}{x-s} + \frac{1}{\pi} \int_4^\infty dx \sigma_2(x) \left[\frac{1}{x-t} + \frac{1}{x-u} \right] \\ & + \frac{1}{\pi^2} \int_4^\infty dx \int_4^\infty dy \frac{\rho_1(x, y)}{x-s} \left[\frac{1}{y-t} + \frac{1}{y-u} \right] \\ & + \frac{1}{\pi^2} \int_4^\infty dx \int_4^\infty dy \frac{\rho_2(x, y)}{(x-t)(y-u)} \end{aligned}$$

[Relevant recent work: Y.f. He & M Kruczenski 2023, 2024, A. Guerrieria, K. Haringa & N. Su 2024, J. A. Oller 2024, ...]

Unlikely to have many data points at different kinetic energies for SIDM

But, still possible to get some information under simply assumptions.

Go beyond concrete dark sector models



Assume **s-channel-dominated self-scattering**

- quite likely as high- ℓ partial waves receive velocity suppression.
- not for very-long-range force, where many partial waves contribute.

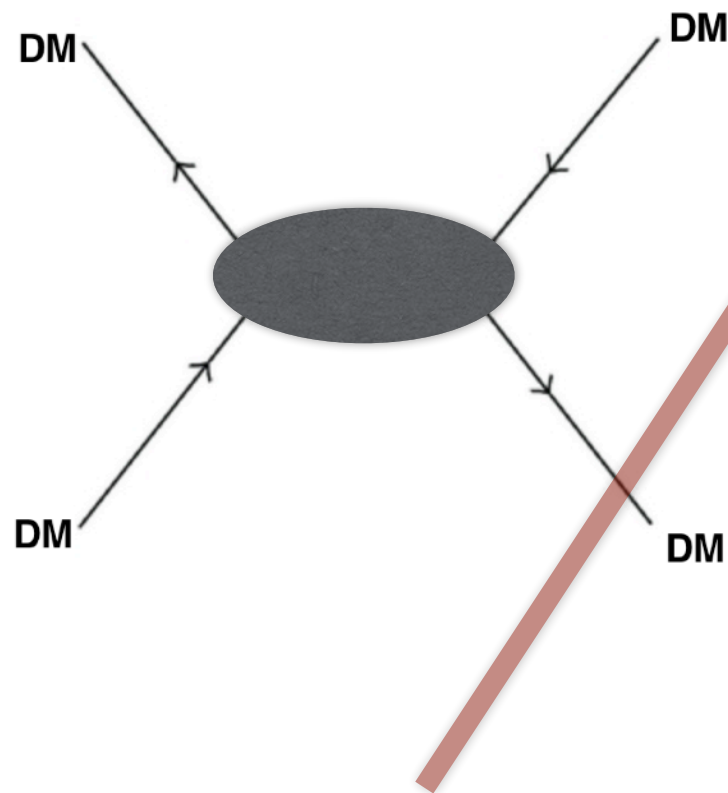
boundary conditions of finite-range potential allows an expansion of the phase shift at very low velocities [Schwinger, Blatt&Jackson, Bethe, 1940s] :

$$k \cot \delta_0 = -\frac{1}{a_0} + \frac{k^2}{2r_{e,0}} + \mathcal{O}(k^4)$$

(strong non-relativistic scattering, suggesting $\text{Im}[\delta_0] \ll \text{Re}[\delta_0]$, and neglected)

Effective-range parametrization of SIDM [XC, C. García-Cely, H. Murayama 2019]

S-wave self-interaction: $\sigma_0 = \frac{4\pi}{k^2} \sin^2 \delta_0 \approx \frac{4\pi a^2}{1 + k^2 (a^2 - ar_e) + \frac{1}{4}a^2 r_e^2 k^4}$
(angle-independent)



- **For hard scattering** ($1/k \gg |a| \gg |r_e|$) .

$$\sigma_0 \rightarrow 4\pi a^2 \quad (\text{contact interaction})$$

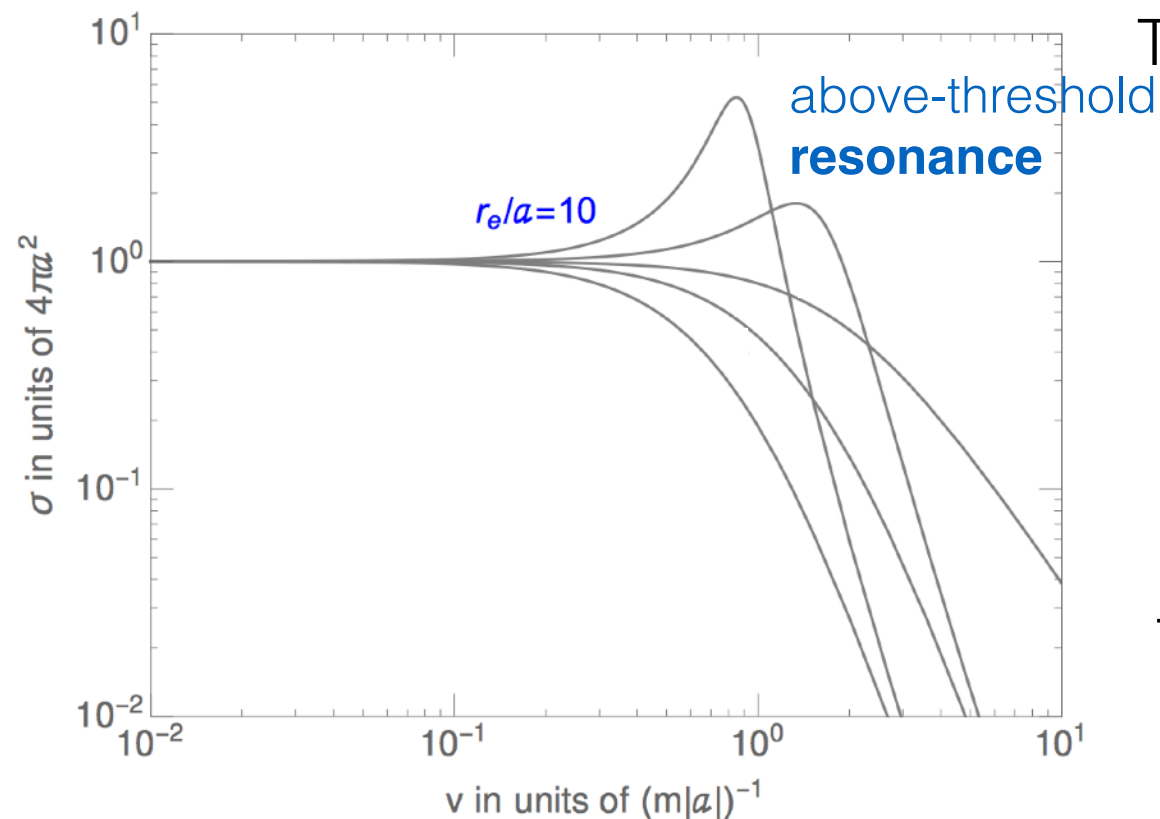
- **For very large scattering length** ($a \rightarrow \infty$) :

$$\sigma_0 \rightarrow \frac{4\pi}{k^2} \quad \text{Unitary fermi gas?}$$

$$k \cot \delta_0 = -\frac{1}{a_0} + \frac{k^2}{2r_{e,0}} + \mathcal{O}(k^4)$$

Effective-range parametrization of SIDM [XC, C. García-Cely, H. Murayama 2019]

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 (angle-independent)



Take **Breit-Wigner resonance** from PDG

$$\sigma(E) = \frac{2J+1}{(2S_1+1)(2S_2+1)} \frac{4\pi}{k^2} \left[\frac{\Gamma^2/4}{(E-E_0)^2 + \Gamma^2/4} \right] B_{in} B_{out}$$

J=0, and classical limit does treat $S_{1,2}$.

Br=1, as $Im[\delta_0]$ neglected.

That is,

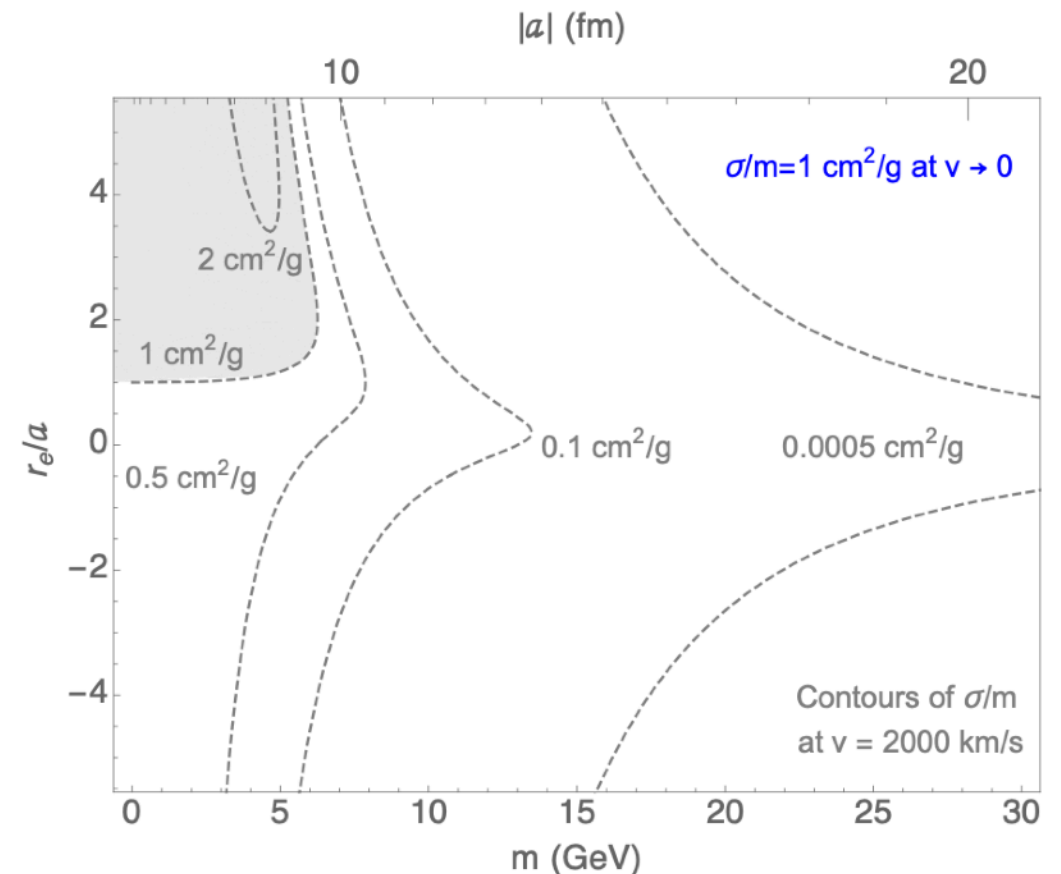
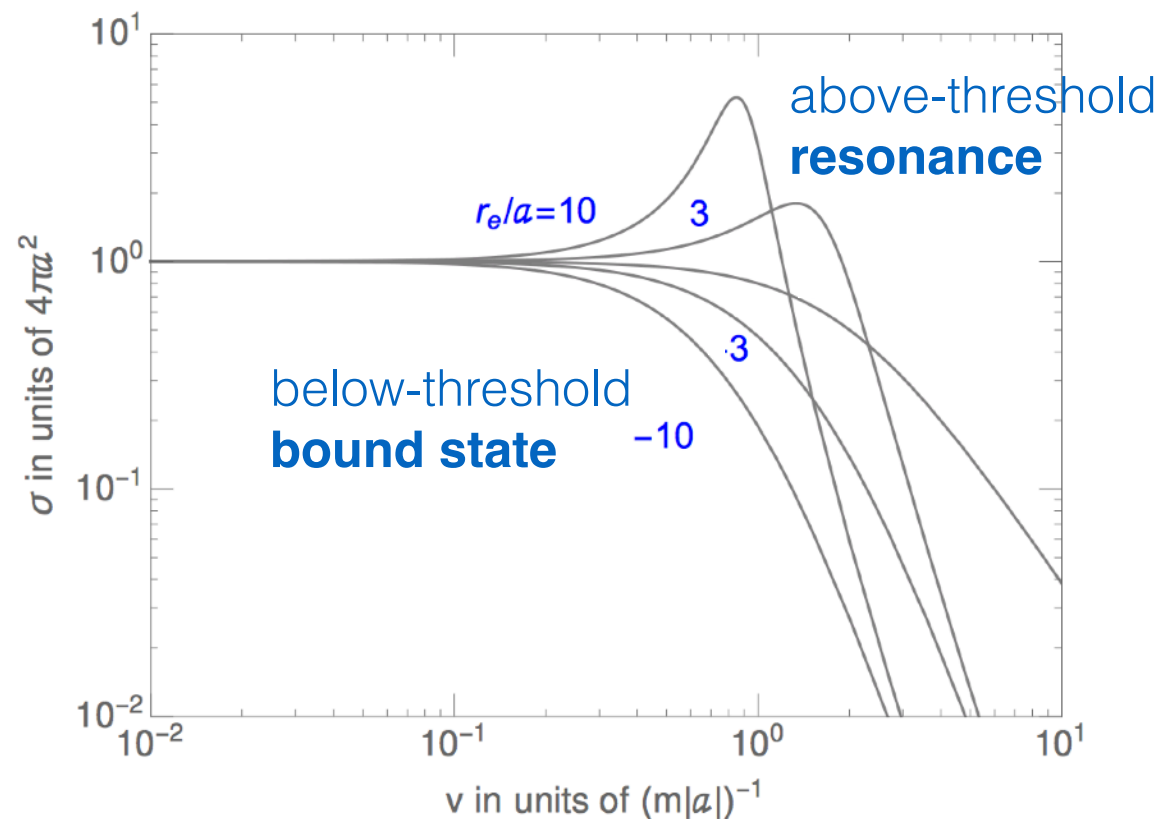
a and r_e are both functions of E_0 and $\Gamma(E_0)$.

$$(m_{\text{DM}}, a, r_e)$$

An easy way to parametrize **resonant SIDM**.

Effective-range parametrization of SIDM [XC, C. García-Cely, H. Murayama 2019]

S-wave self-interaction: $\sigma_0 = \frac{4\pi}{k^2} \sin^2 \delta_0 \approx \frac{4\pi a^2}{1 + k^2 \left(a^2 - ar_e \right) + \frac{1}{4} a^2 r_e^2 k^4}$
 (angle-independent)



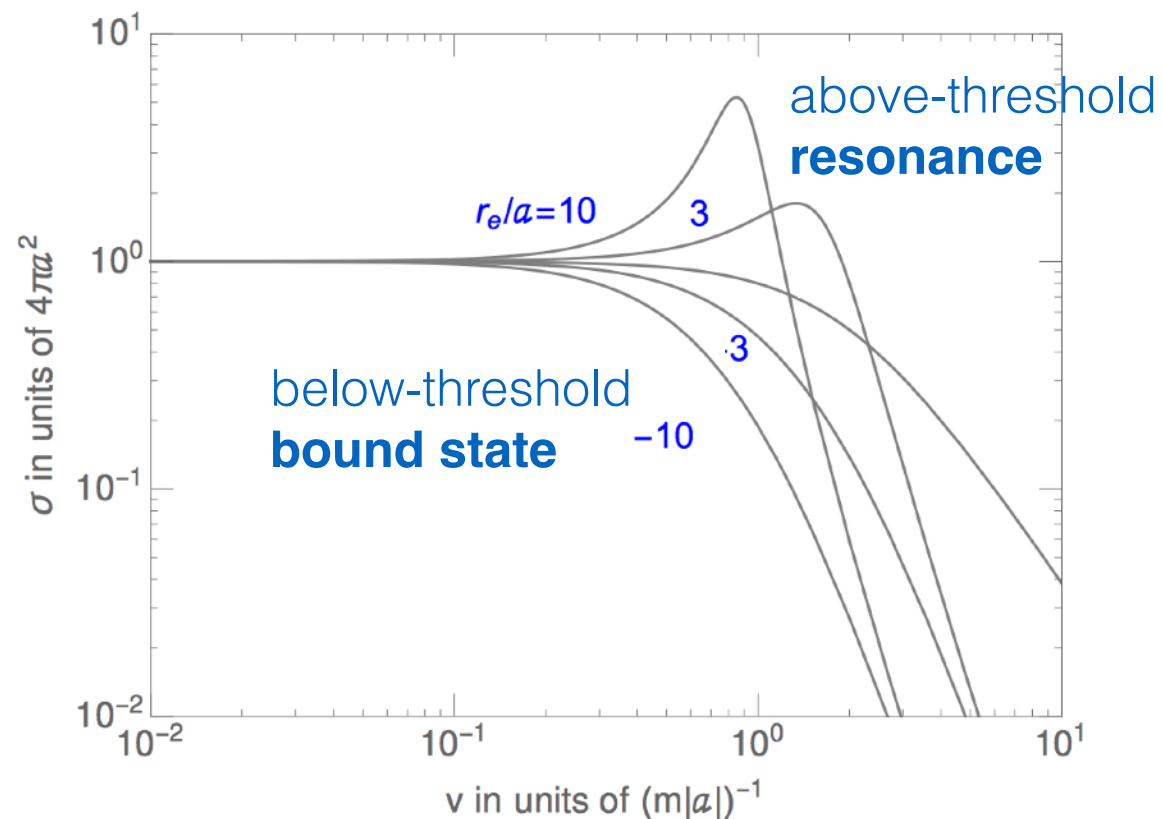
$$(m_{\text{DM}}, a, r_e)$$

An easy way to parametrize general **S-wave-dominated SIDM**.

e.g. resonant/bound-state SIDM, Yukawa SIDM with mediator mass larger than k , ...

Effective-range parametrization of SIDM [XC, C. García-Cely, H. Murayama 2019]

S-wave self-interaction: $\sigma_0 = \frac{4\pi}{k^2} \sin^2 \delta_0 \approx \frac{4\pi a^2}{1 + k^2 \left(a^2 - ar_e \right) + \frac{1}{4} a^2 r_e^2 k^4}$



Explains why so often to have **DM self-scattering decreasing with higher velocities.**

A few data points may suggest the existence of **bound state** or **resonance**, modifying freeze-out.

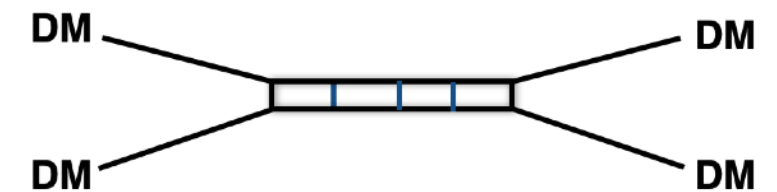
5. Conclusions

DM self-scattering from dark sector physics

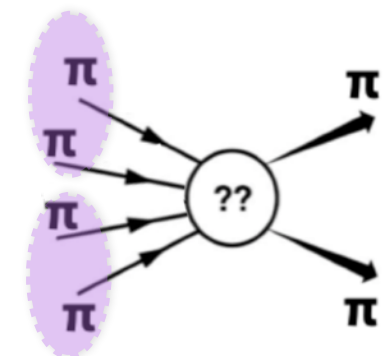
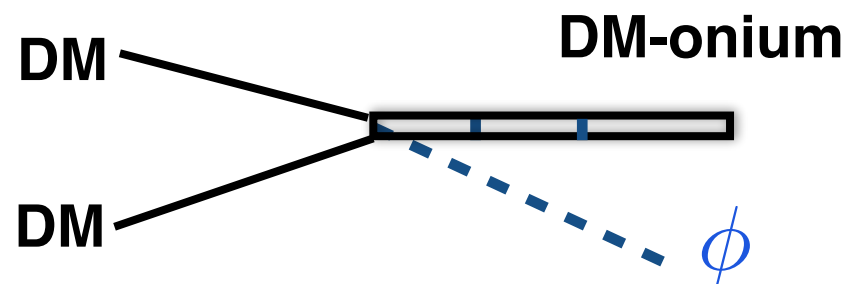
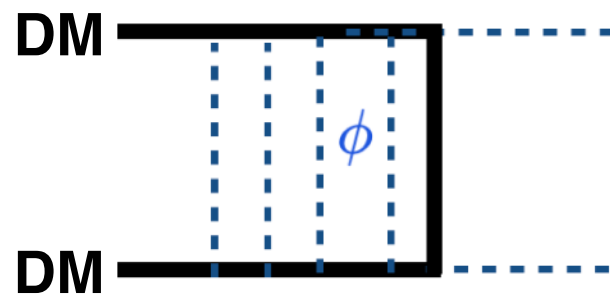
- It needs to induce **velocity-dependent** self-scattering:

elastic scattering

Strong and alleviating galaxy/cluster bounds.



- It may modify **mechanisms/predictions** of DM production:



DM self-scattering from dark sector physics

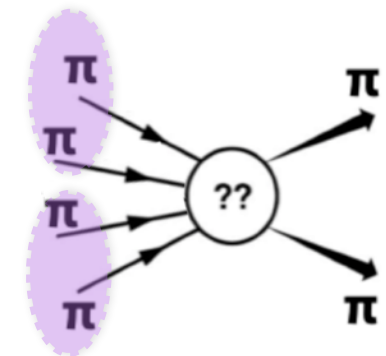
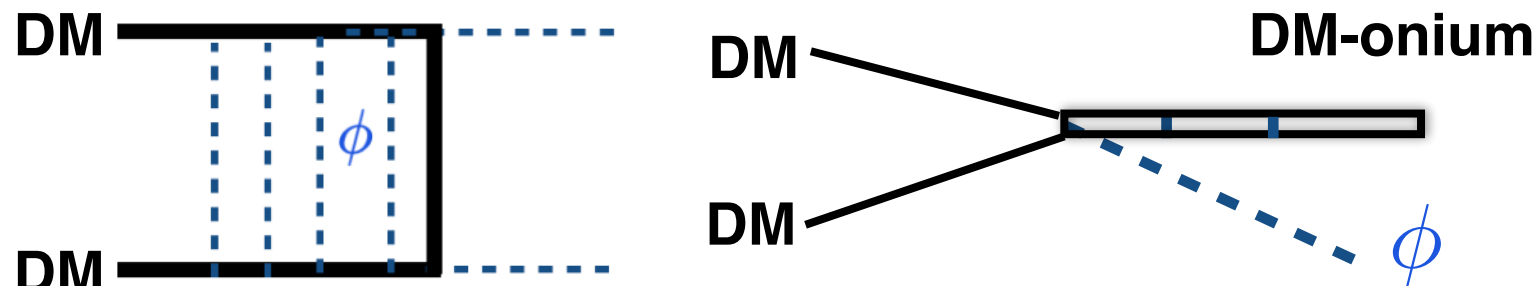
- It needs to induce **velocity-dependent** self-scattering:

Strong and alleviating galaxy/cluster bounds.

elastic scattering



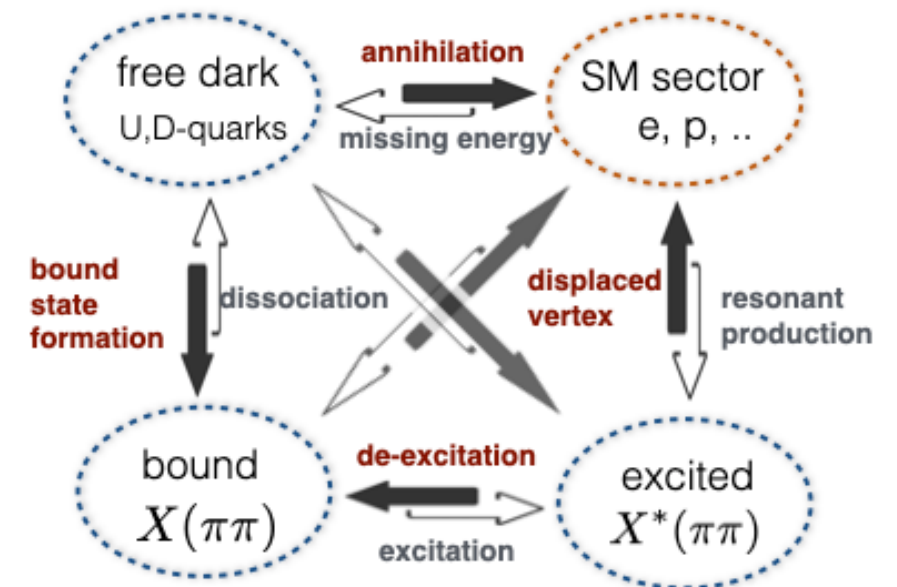
- It may modify **mechanisms/predictions** of DM production:



- It also leads to novel signatures in astrophysics & territorial experiments:

Inelastic scatterings of astrophysical DM?

- It may be relevant for baryonic asymmetry too.



Thanks!