

$pp \rightarrow ttj$ @ NLO in QCD

Off-Shell Calculations & Mass Extraction

MALGORZATA WOREK

INSTEAD OF INTRODUCTION

■ NLO CORRECTIONS FOR STABLE TOP QUARKS

- General idea about size of NLO QCD corrections
- Can not provide reliable description of top quark decay products & radiation pattern

S. Dittmaier, P. Uwer, S. Weinzierl, Phys. Rev. Lett. 98 (2007) 262002

S. Dittmaier, P. Uwer, S. Weinzierl, Eur. Phys. J. C 59 (2009) 625

M. Czakon, H. B. Hartanto, M. Kraus, M. Worek, JHEP 06 (2015) 033

■ FOR MORE REALISTIC STUDIES DECAYS ARE NEEDED

- *NLO QCD for $pp \rightarrow ttj + PS$* $\Rightarrow$ Corrections to production & Top decays in parton shower approximation & omitting (even LO) *tt* spin correlations

A. Kardos, C. G. Papadopoulos, Z. Trocsanyi, Phys. Lett. B 705 (2011) 76

- *NLO QCD for $pp \rightarrow ttj + LO \text{ decays} + PS$* $\Rightarrow$ Top decays @ LO before matched to parton shower programs & LO *tt* spin correlations

S. Alioli, S. Moch, P. Uwer, JHEP 01 (2012) 137

- *NLO QCD for $pp \rightarrow ttj + LO \text{ decays}$* $\Rightarrow$ Top decays @ LO & LO *tt* spin correlations

K. Melnikov, M. Schulze, Nucl. Phys. B 840 (2010) 129

- *NLO QCD in NWA for $pp \rightarrow ttj$* $\Rightarrow$ NLO QCD corrections to top production & decays & NLO *tt* spin correlations

K. Melnikov, M. Schulze, Phys. Rev. D 85 (2012) 054002

- *NLO QCD with complete off-shell effects of top quarks for $pp \rightarrow ttj$* $\Rightarrow$ Additionally to previous effects $\Rightarrow$ Resonant & non-resonant diagrams & Interference effects & Off-shell *t* & *W* described by Breit-Wigner propagators

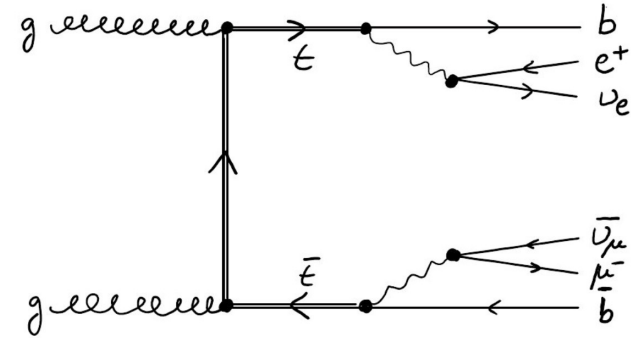
G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Worek, JHEP 11 (2016) 098

G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Worek, Phys. Rev. Lett. 116 (2016) 5, 052003

FULL OFF-SHELL PREDICTIONS

- Modelling of unstable particles based on $t\bar{t}$

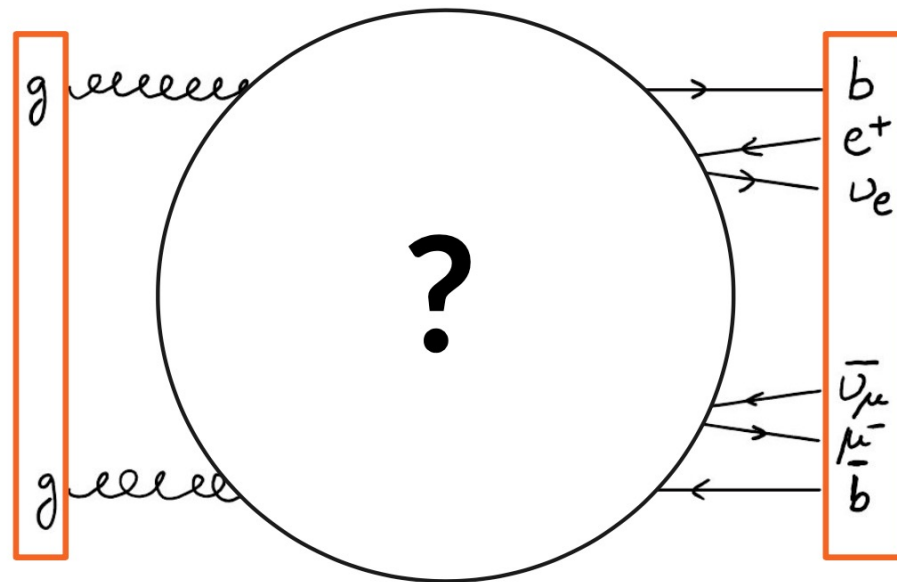
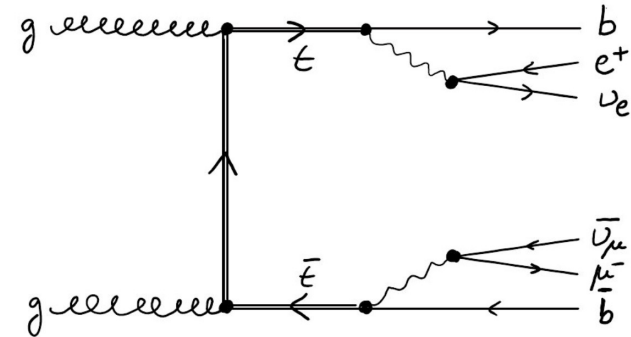
$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$



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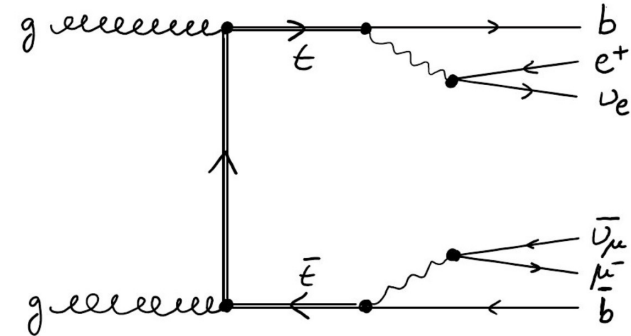
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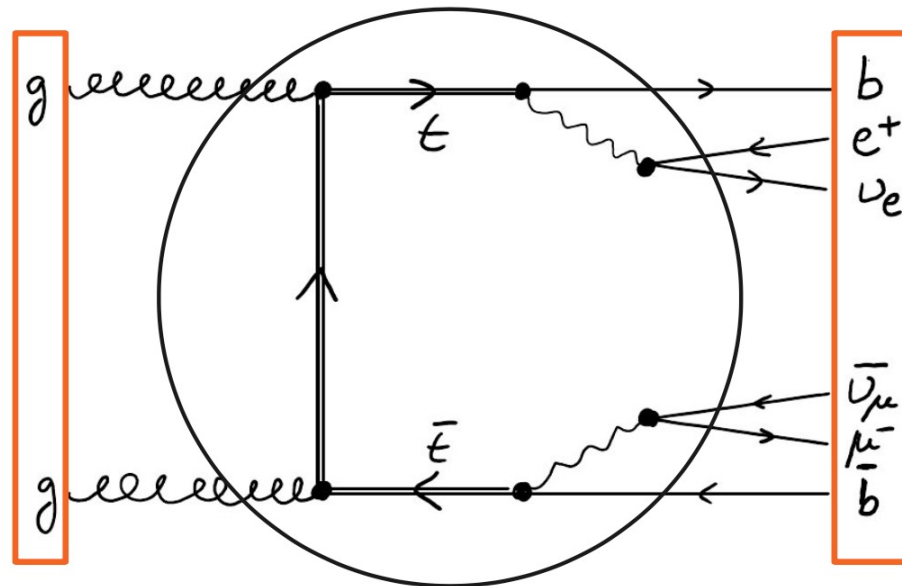
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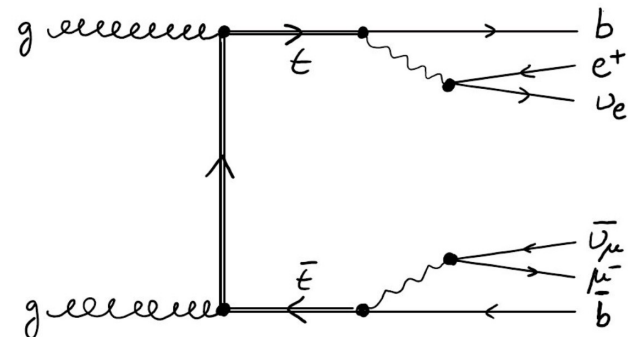
Double-
resonant
diagram



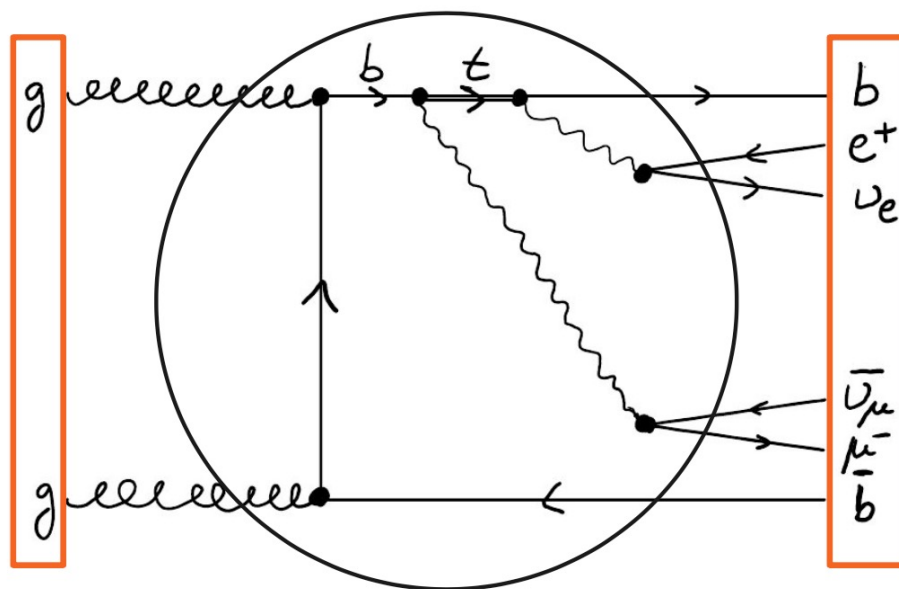
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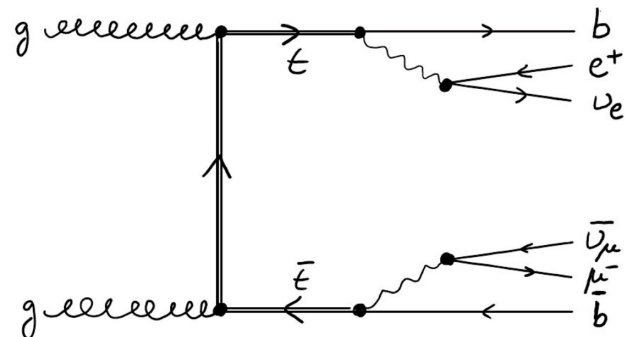
Single-
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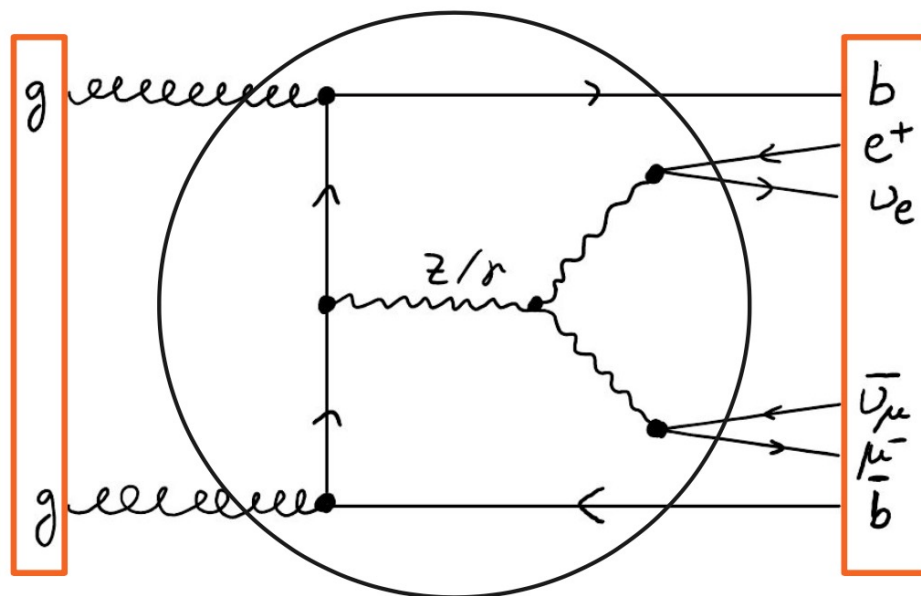
FULL OFF-SHELL PREDICTIONS

- Modelling of unstable particles based on $t\bar{t}$

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$



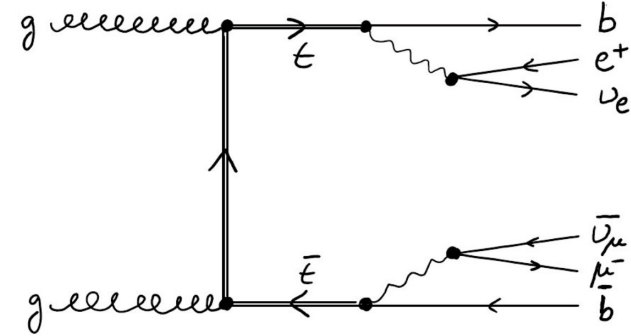
Non-
resonant
diagram



ON-SHELL PREDICTIONS

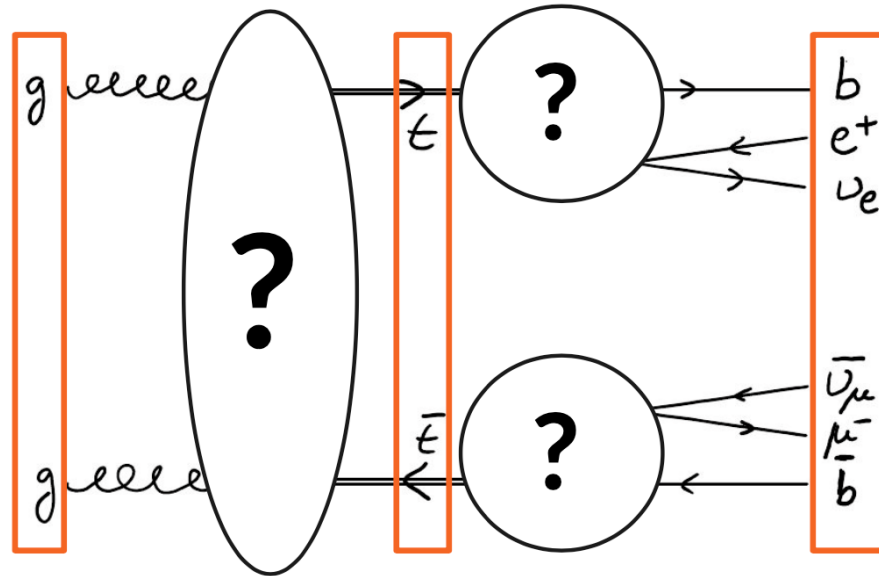
- Modelling of unstable particles based on $t\bar{t}$

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$



Narrow-width approximation (NWA)
 → Fix intermediate state to be on-shell

$$\frac{\Gamma}{m} \rightarrow 0$$



$$\frac{\Gamma_W}{m_W} > \frac{\Gamma_t}{m_t} \gg \frac{\Gamma_H}{m_H},$$

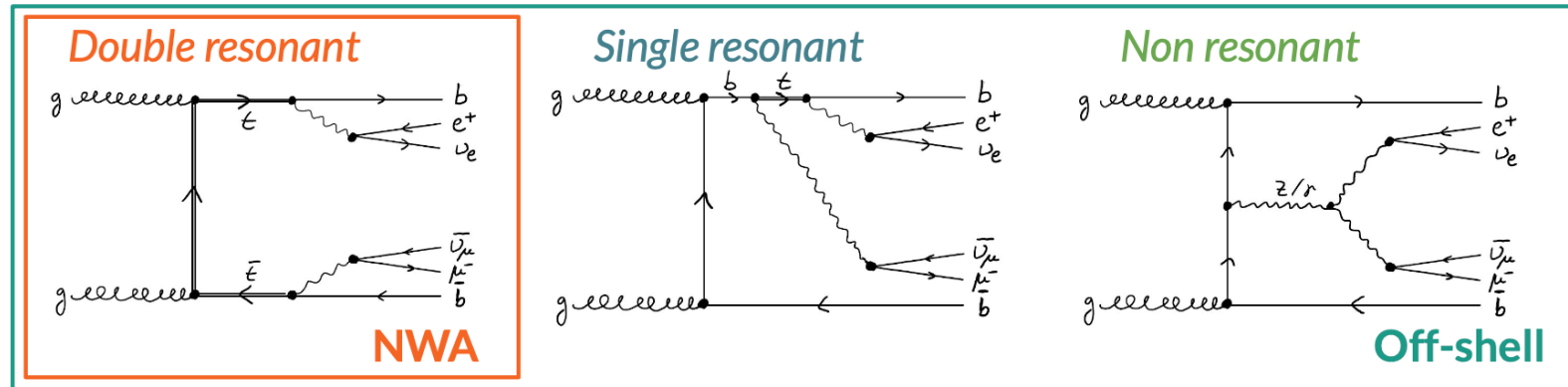
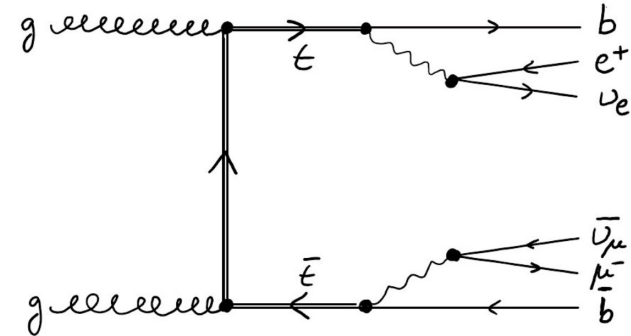
$$2.6\% > 0.8\% \gg 0.003\%$$

- Good approximation for very inclusive observables
 - Integrated cross sections
 - Angular distributions

OFF-SHELL VERSUS ON-SHELL PREDICTIONS

- Modelling of unstable particles based on $pp \rightarrow tt$

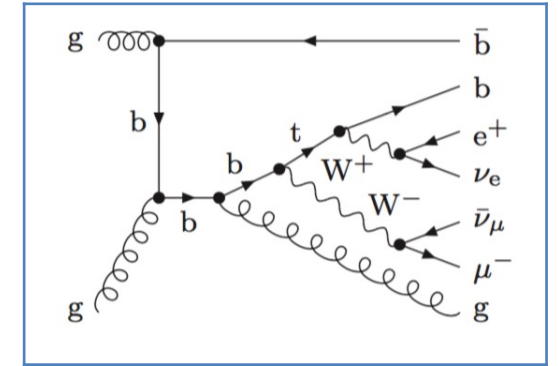
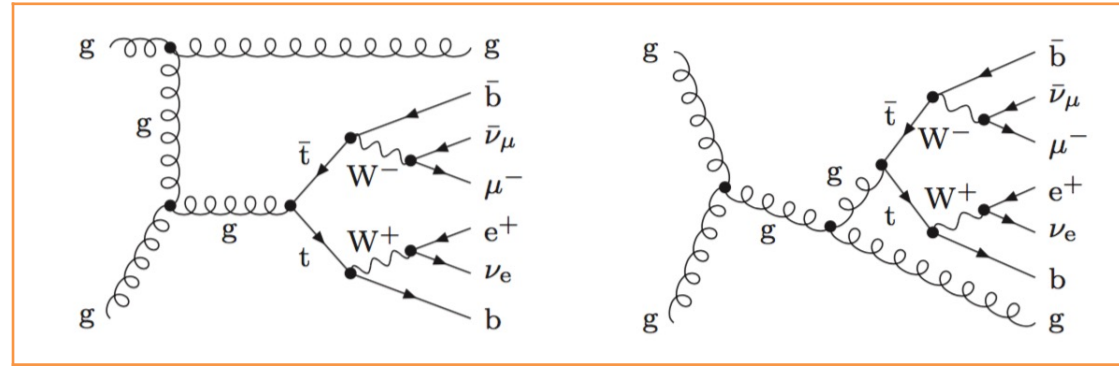
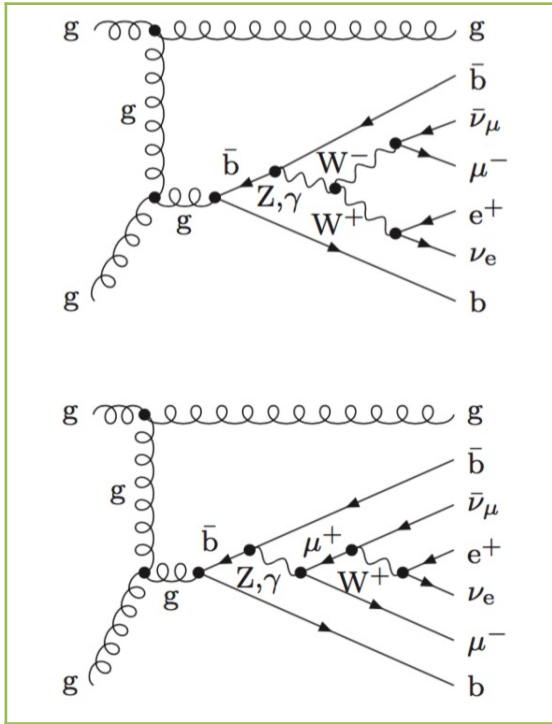
$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$



- ✓ Full off-shell = DR + SR + NR + interferences + Breit-Wigner propagators $\Rightarrow$ @ NLO QCD
- ✓ NWA = DR restricts unstable t & W to on-shell states $\Rightarrow$ @ NLO QCD
- ✓ NWA_{LO} = NLO QCD corrections to ttj production only

OFF-SHELL PREDICTIONS FOR TTJ

- Why do we not make such calculations for all processes?



$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

- $pp \rightarrow ttj$ with leptonic decays @ $\mathcal{O}(\alpha_s^4 \alpha^4)$
- $2 \rightarrow 5$ process from QCD point of view $\Rightarrow pp \rightarrow WWbbj$
- Diagrams with complete off-shell effects for t & W for gg initial state:
 - LO: 508*
 - Real emission: 4447*

OFF-SHELL PREDICTIONS FOR TTJ

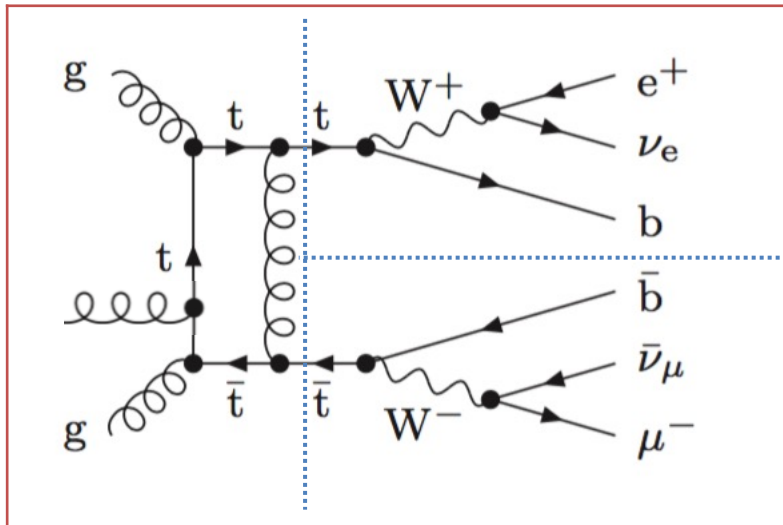
- gg channel comprises *39 180 one-loop diagrams* $\Rightarrow$ According to **QGRAF**

P. Nogueira, J. Comput. Phys. 105 (1993) 279

- Most complicated ones are *1155 hexagons & 120 heptagons*
- Tensor integrals up to rank six

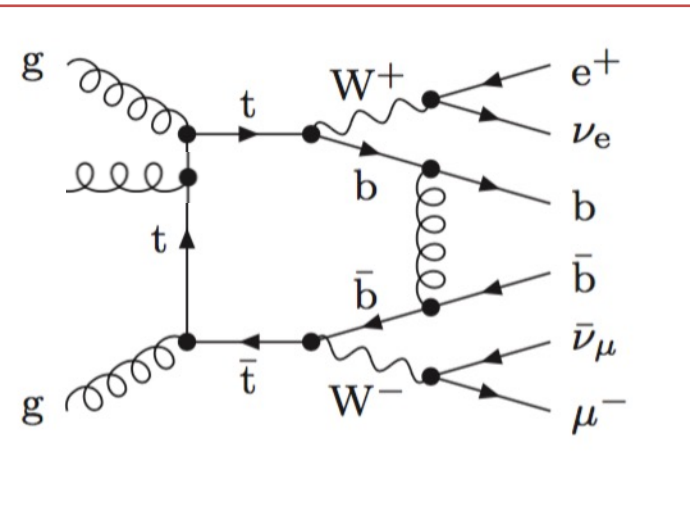
$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

*NWA for ttj (on-shell top-quark production)
– up to pentagons !*



*No cross-talk between
 ttj production & top-
quark decays*

*Full calculations for ttj
– up to heptagons !*

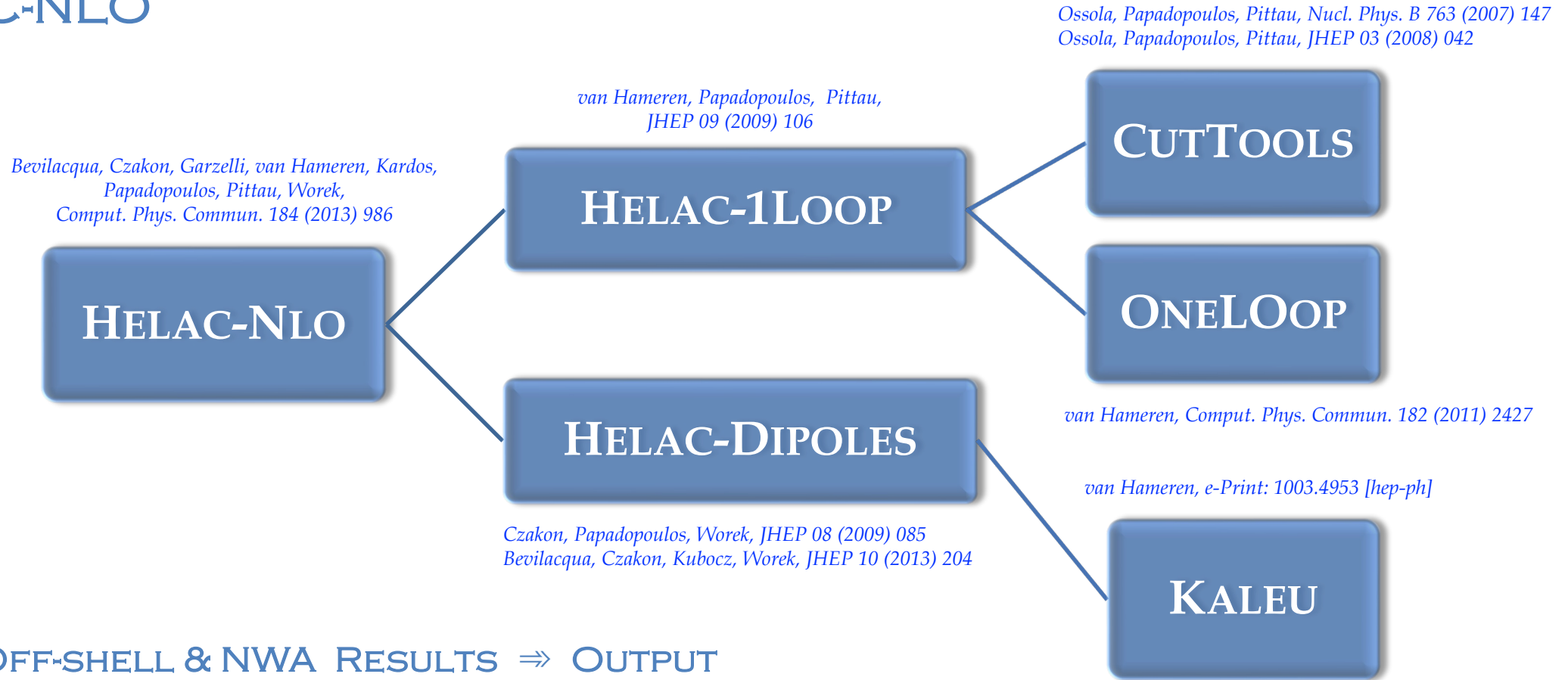


*factorizable & non-
factorizable
QCD corrections
included*

OFF-SHELL VERSUS ON-SHELL PREDICTIONS

- Modelling of unstable particles in di-lepton channel for $t\bar{t}j$ @ LHC
 - Full off-shell = DR + SR + NR + interferences + Breit-Wigner propagators
 - NWA = DR restricts unstable t & W to on-shell states
- Understand two approaches & compare them
- Generally full off-shell predictions impact:
 - IR-safe (integrated) cross sections $\Rightarrow$ Normalisation in BSM $\Rightarrow pp \rightarrow t\bar{t} + A$ pseudoscalar Higgs boson
 - IR-safe (differential) observables $\Rightarrow$ Shape of dimensionful distributions $\Rightarrow$ high p_T & kinematical edges
 - SM parameter extraction $\Rightarrow m_t$
 - BSM exclusion limits $\Rightarrow pp \rightarrow t\bar{t} + DM$ @ LHC with SM background processes $pp \rightarrow t\bar{t}$ & $pp \rightarrow t\bar{t}Z$
 - New Physics signal modelling $\Rightarrow pp \rightarrow t\bar{t}H$ with anomalous couplings $\Rightarrow pp \rightarrow t\bar{t}H$ in SMEFT
 - Definition of $pp \rightarrow t\bar{t}W$ & $pp \rightarrow t\bar{t}$ $\Rightarrow$ Diagram removal versus Diagram subtraction
 - Final systematic uncertainties
 - Matching to parton shower programs $\Rightarrow$ Resonant aware matching is required

HELAC-NLO



■ FULL OFF-SHELL & NWA RESULTS $\Rightarrow$ OUTPUT

- Predictions stored as partially unweighted “events” $\Rightarrow$ *ROOT-Ntuples Files & Les Houches Files*
- Each “event” provided with supplementary matrix element & PDF information
- Results for different scale settings & PDF choices by can be obtained by reweighting
- Different observables and/or binning can be provided + more exclusive cuts $\Rightarrow$ With caveat

SCALE DEPENDENCE

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

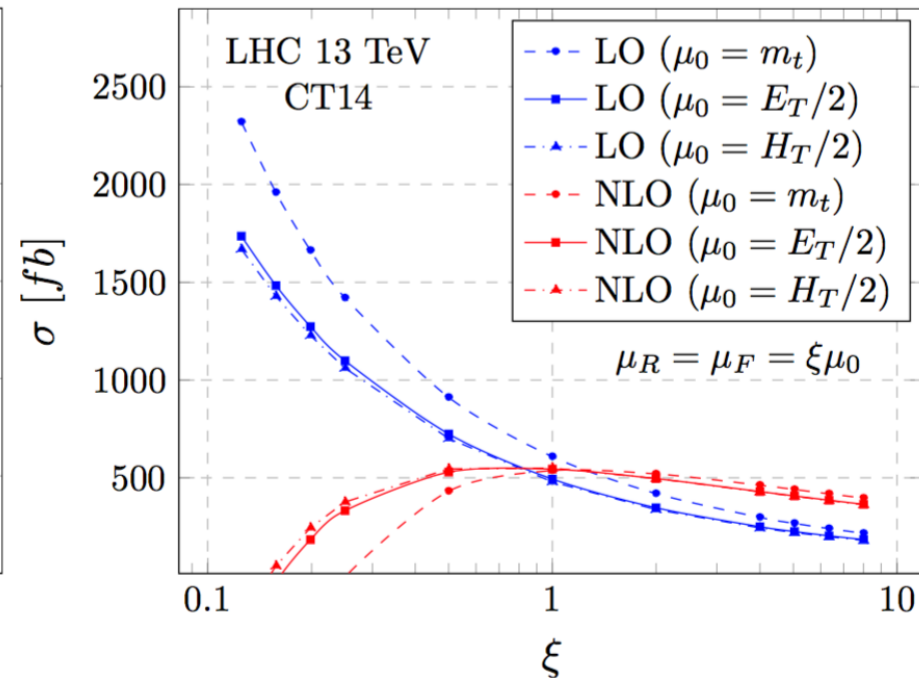
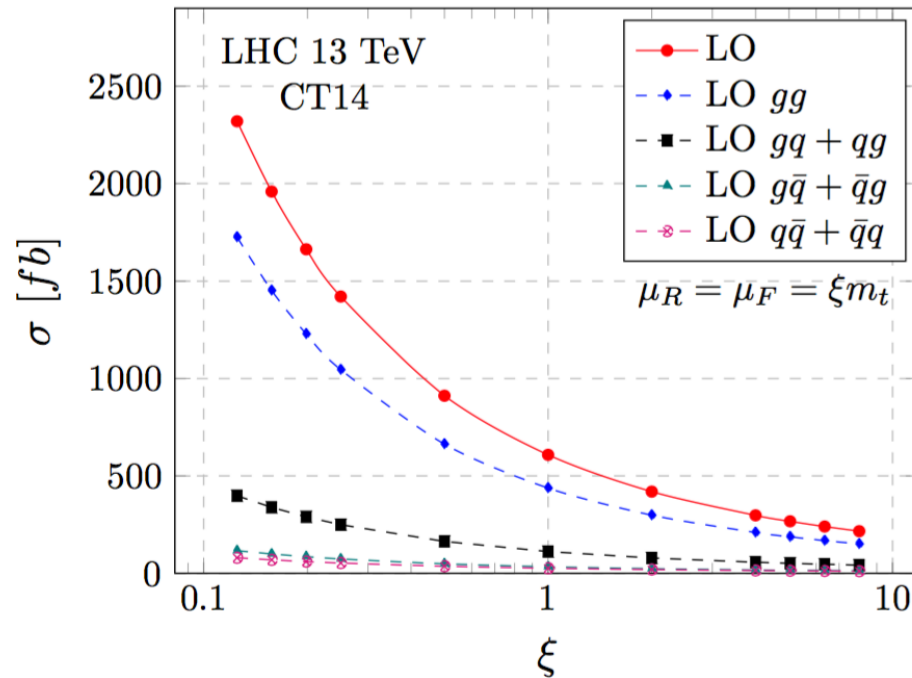
G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Worek, JHEP 11 (2016) 098

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- Integrated cross section @ LHC 13 TeV
- Scales: $\mu_R = \mu_F = \mu_0 = m_t, E_T/2, H_T/2$

$$H_T = \sum_i p_{T,i} + p_T^{\text{miss}}$$

$$E_T = m_{T,t} + m_{T,\bar{t}}$$



- LO contributions: gg : 72%, gq : 18%, $g\bar{q}$: 6%, $q\bar{q}$: 4%

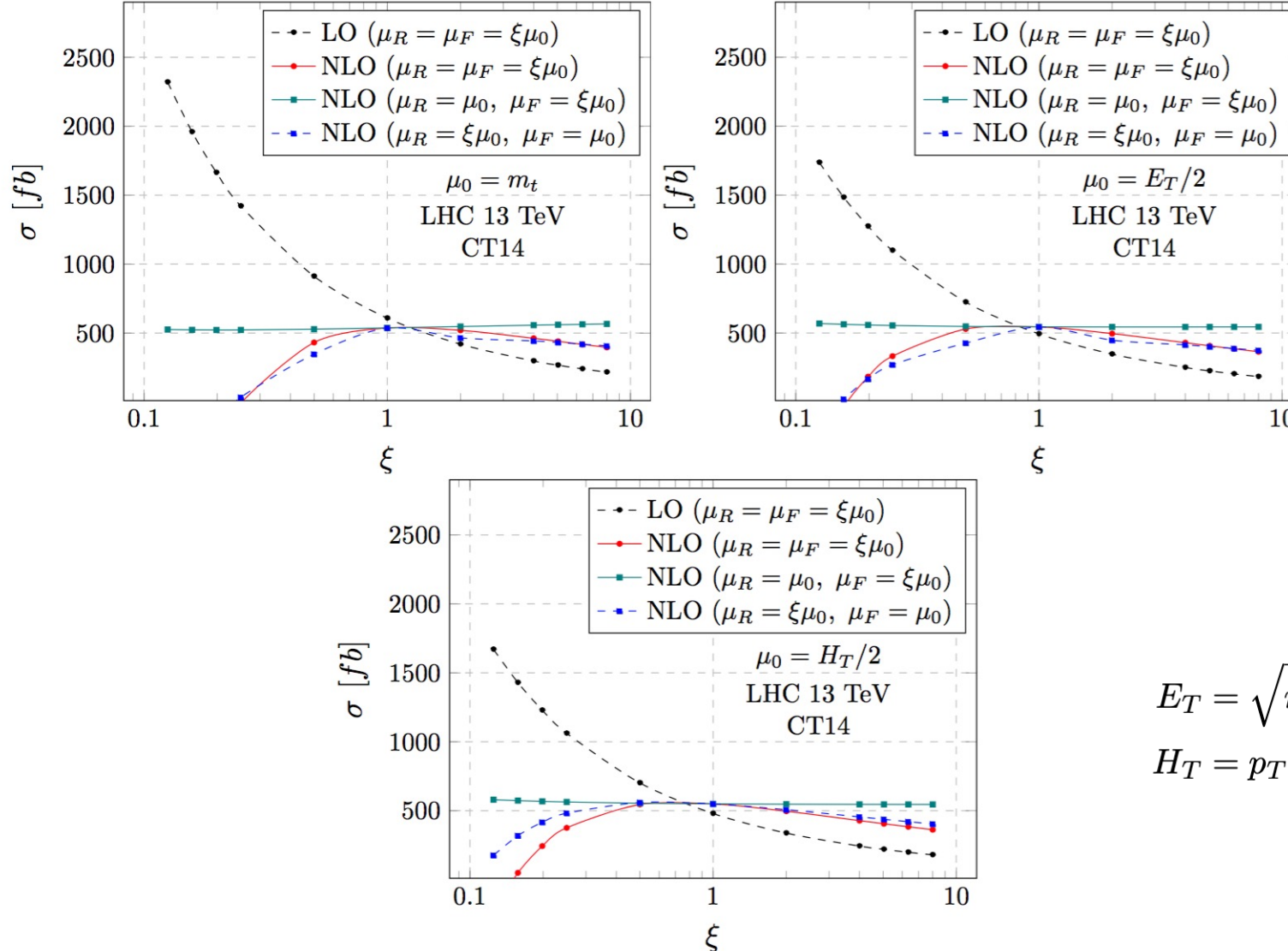
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■ Integrated cross section @ LHC 13 TeV



$$\mu_R = \mu_F = \mu_0 = m_t, E_T/2, H_T/2$$

- scale variation fully driven by changes in μ_R independently of scale choice
- 7-point scale variation and 3-point scale variation would give similar results

$$E_T = \sqrt{m_t^2 + p_T^2(t)} + \sqrt{m_t^2 + p_T^2(\bar{t})},$$

$$H_T = p_T(e^+) + p_T(\mu^-) + p_T(j_{b_1}) + p_T(j_{b_2}) + p_T(j_1) + p_T^{\text{miss}}$$

SCALE & PDF UNCERTAINTIES

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- Size of NLO corrections for CT14 NLO

$\mu_0 = m_t$	$\mathcal{K} = 0.88$	-12%
$\mu_0 = E_T/2$	$\mathcal{K} = 1.10$	$+10\%$
$\mu_0 = H_T/2$	$\mathcal{K} = 1.12$	$+12\%$

7-point scale variation

$$1/2\mu_0 \leq \mu_R, \mu_F \leq 2\mu_0$$

$$1/2 \leq \mu_R/\mu_F \leq 2$$

- PDFs: CT14, MMHT14, NNPDF3.0
- Integrated fiducial cross sections for $\mu_0 = H_T/2$

$$\begin{aligned} \sigma_{e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j}^{\text{NLO}}(\text{CT14}, \mu_0 = H_T/2) &= 549.65^{+10.25}_{-53.42} \begin{pmatrix} +2\% \\ -10\% \end{pmatrix} [\text{scales}] +18.00^{(+3\%)}_{-19.15^{(-3\%)}} [\text{PDF}] \text{ fb} \\ \sigma_{e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j}^{\text{NLO}}(\text{MMHT14}, \mu_0 = H_T/2) &= 554.61^{+10.85}_{-54.51} \begin{pmatrix} +2\% \\ -10\% \end{pmatrix} [\text{scales}] +12.06^{(+2\%)}_{-12.22^{(-2\%)}} [\text{PDF}] \text{ fb} \\ \sigma_{e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j}^{\text{NLO}}(\text{NNPDF3.0}, \mu_0 = H_T/2) &= 572.18^{+11.14}_{-56.23} \begin{pmatrix} +2\% \\ -10\% \end{pmatrix} [\text{scales}] +11.31^{(+2\%)}_{-11.31^{(-2\%)}} [\text{PDF}] \text{ fb} \end{aligned}$$

68% C.L.

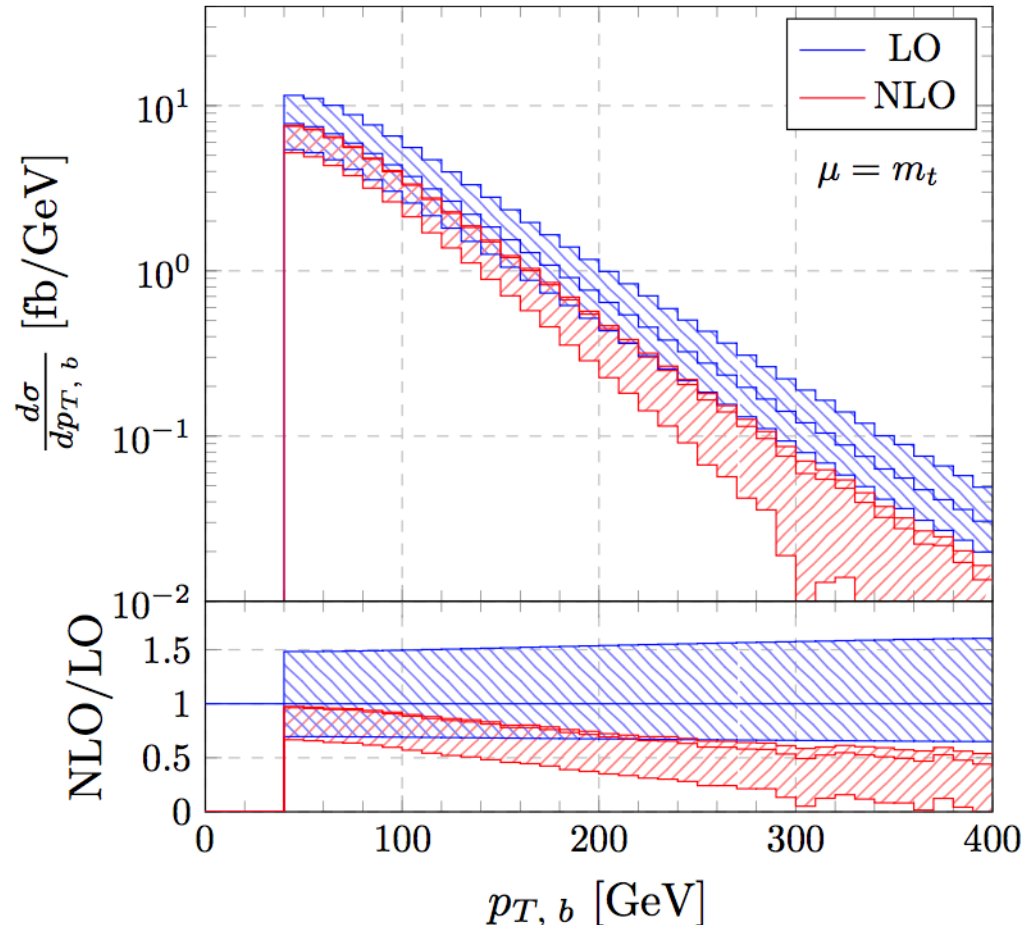
DIFFERENTIAL DISTRIBUTIONS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

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- 16 differential cross section distributions have been examined, here are just few examples...
- Dimensionful observable: $p_T(b)$ with $\mu_0 = m_t$*



- NLO do not simply rescale shape of LO $p_T(b)$
- NLO corrections up to -55%
- $p_T(b)$ properly described only via NLO
- Negative NLO results in high p_T tails
- LO higher than NLO in p_T tails
- Dynamic scale should depend on p_T of hardest jet & top-quark decay products $\uparrow$
- Asymptotic freedom $\Rightarrow \alpha_s \downarrow$ in tails
- Dependence on $\alpha_s @ \text{LO} \gg @ \text{NLO}$
- Would drive positive NLO/LO ratio in this region

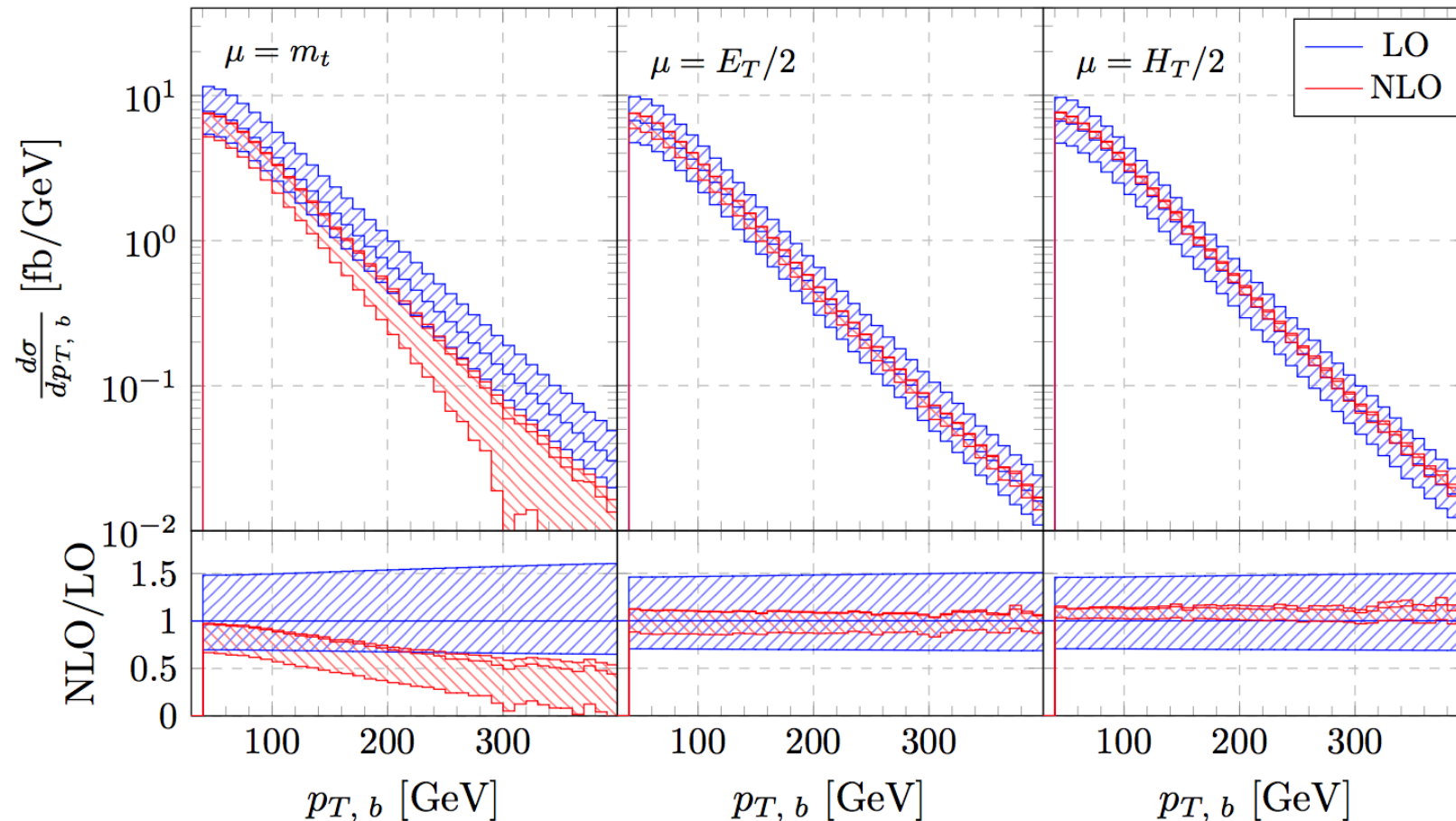
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- Dimensionful observable: $p_T(b)$ with all 3 scale settings
- Positive corrections below 20% when $\mu_F = \mu_R = \mu_0 = \frac{1}{2} E_T$ or $\mu_F = \mu_R = \mu_0 = \frac{1}{2} H_T$ used instead



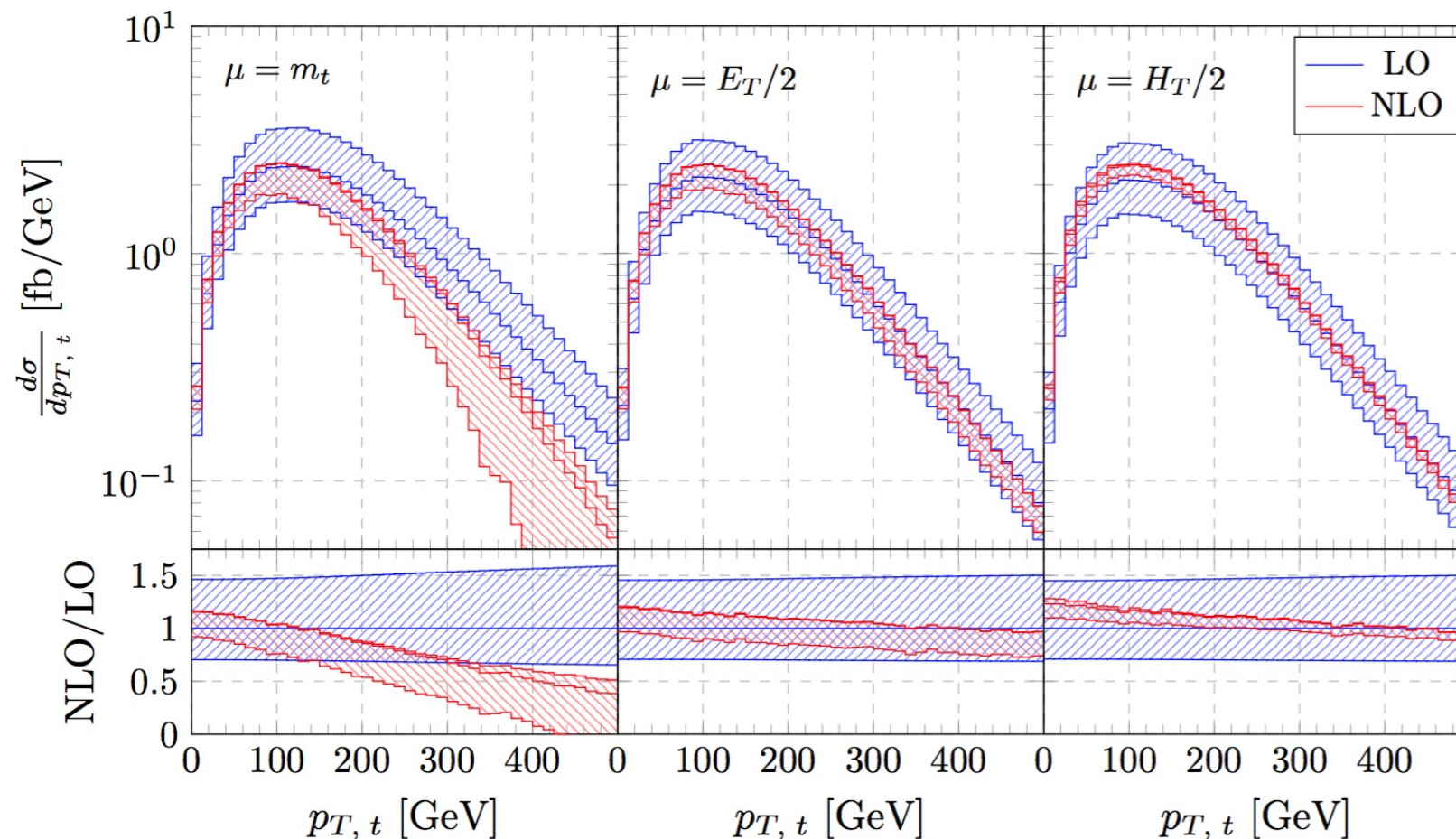
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- Dimensionful observable: $p_{T,t}$ with all 3 scale settings



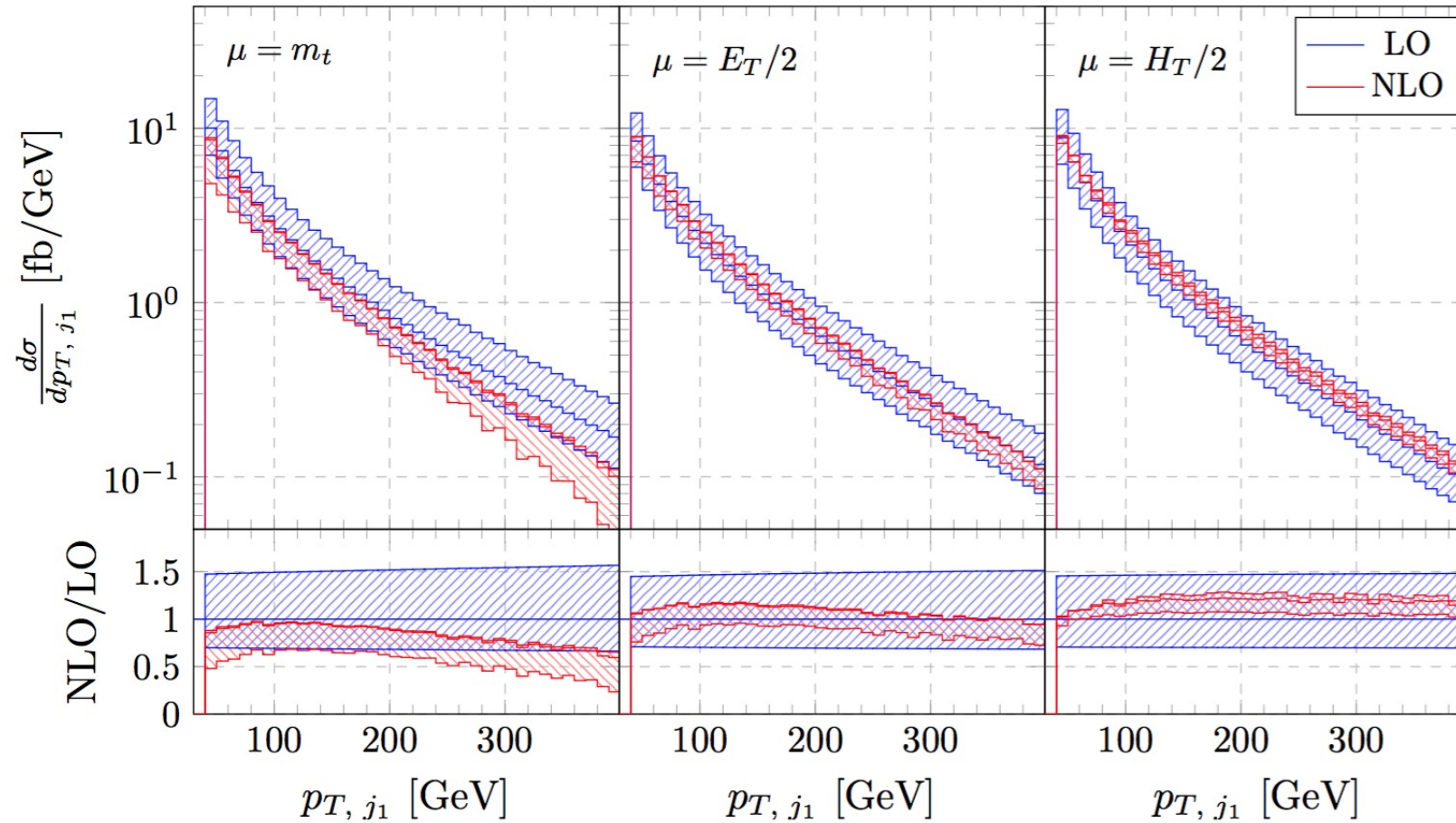
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- Dimensionful observable: $p_T(j_1)$ with all 3 scale settings



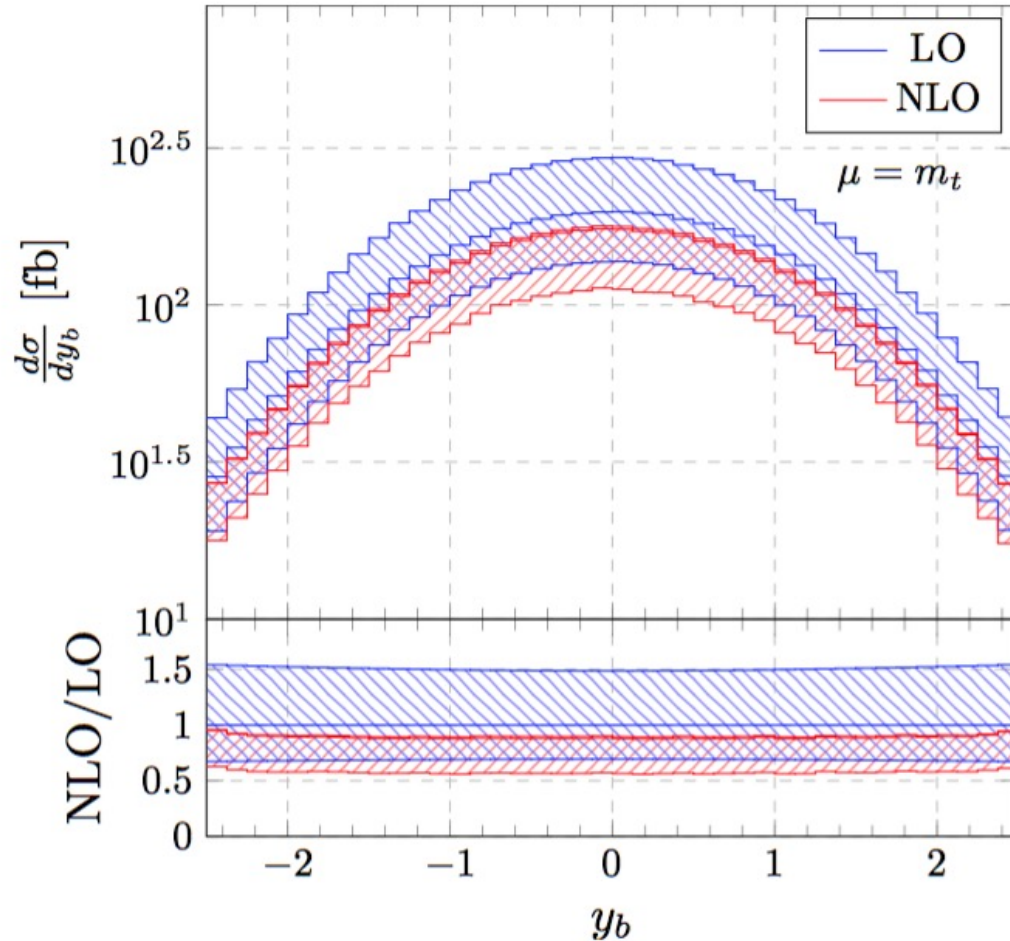
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- Dimensionless observable: $y(b)$ with $\mu_0 = m_t$



- Negative, moderate 10% $\Rightarrow$ But quite stable NLO corrections
- Receives contributions from various scale settings $\Rightarrow$ Also from these sensitive to threshold for $t\bar{t}$ production
- For $\mu_F = \mu_R = \mu_0 = m_t$ effects of phase-space regions close to $t\bar{t}j$ threshold dominate

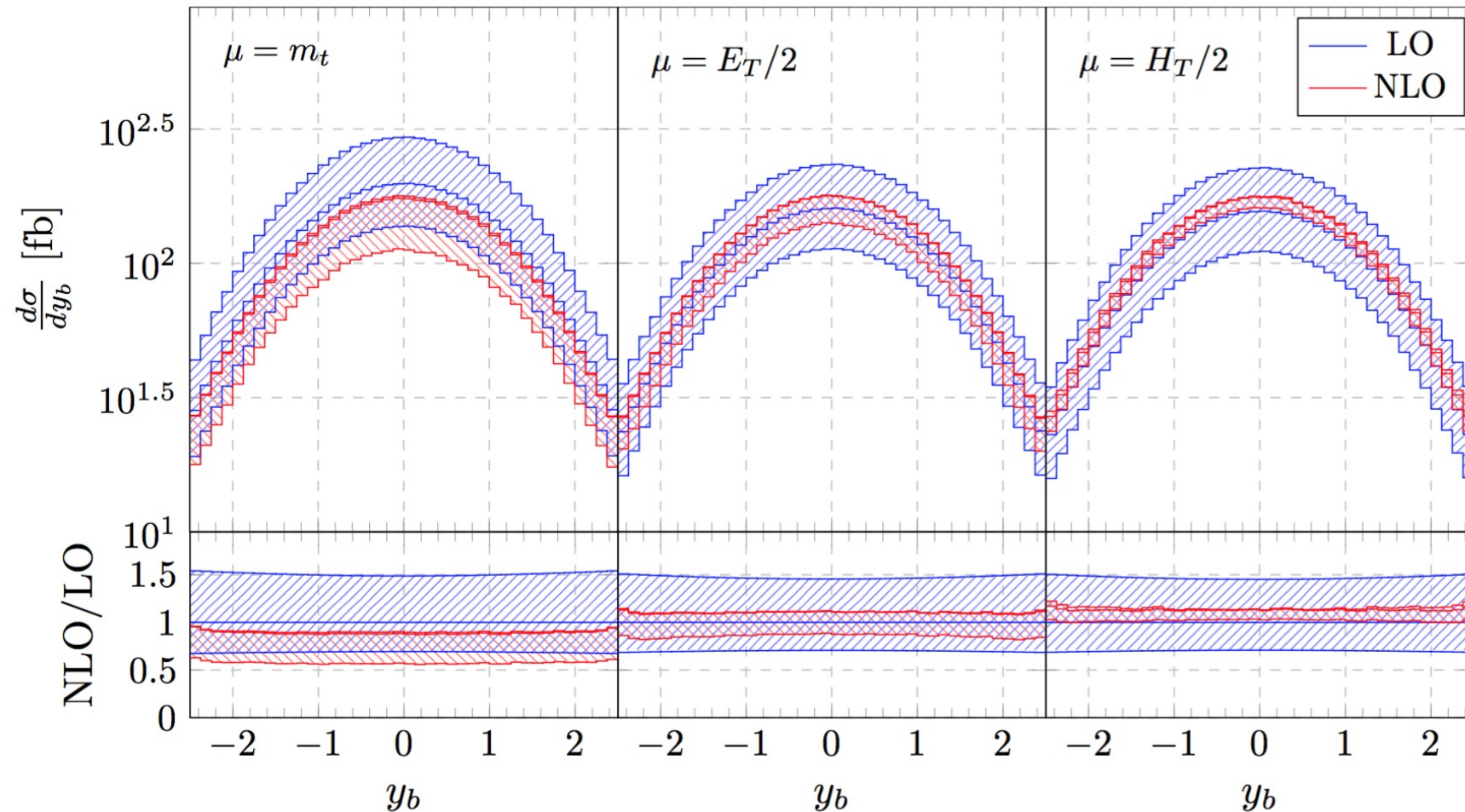
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- Dimensionless observable: $y(b)$ with all 3 scale settings
- Replaced by positive moderate NLO corrections for dynamical scale settings



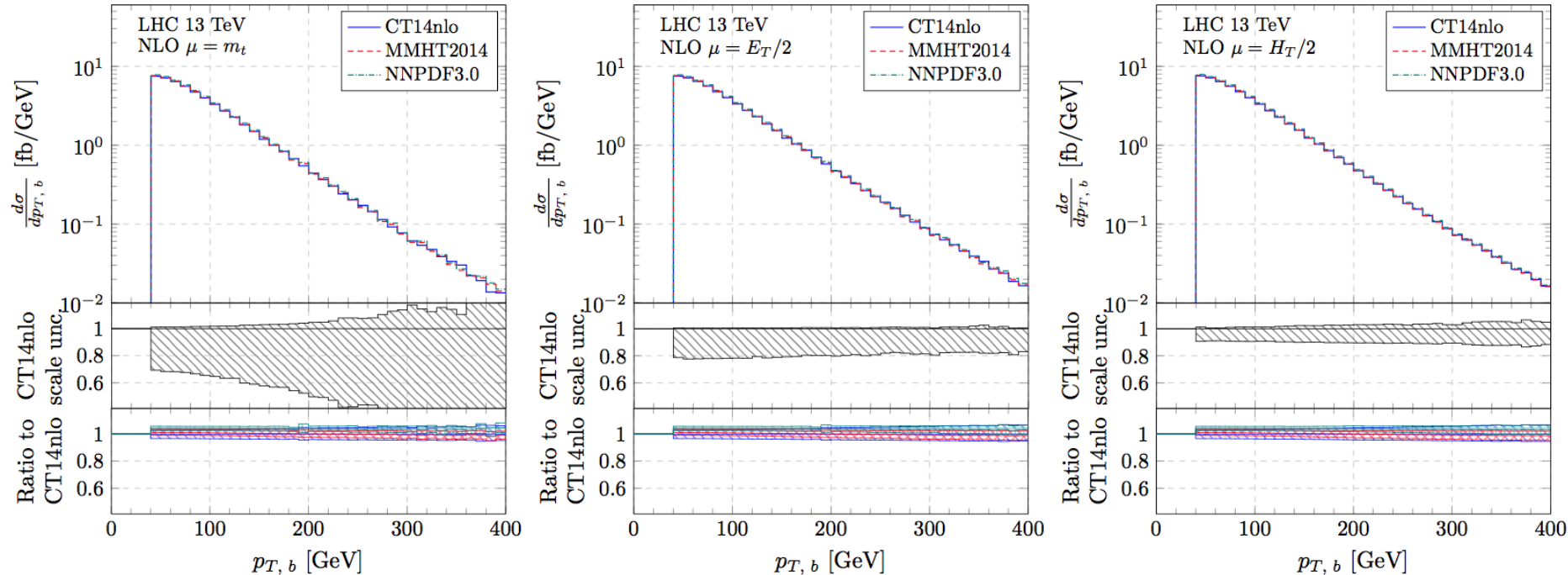
SCALE & PDF UNCERTAINTIES

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- *Upper panel*
 - NLO prediction for three different PDF sets at $\mu_F = \mu_R = \mu_0$
- *Middle panel*
 - NLO scale-dependence band normalized to central CT14 NLO prediction
- *Lower panel*
 - PDF uncertainties obtained for each PDF set separately $\Rightarrow$ Normalized to central NLO prediction with CT14 PDF set



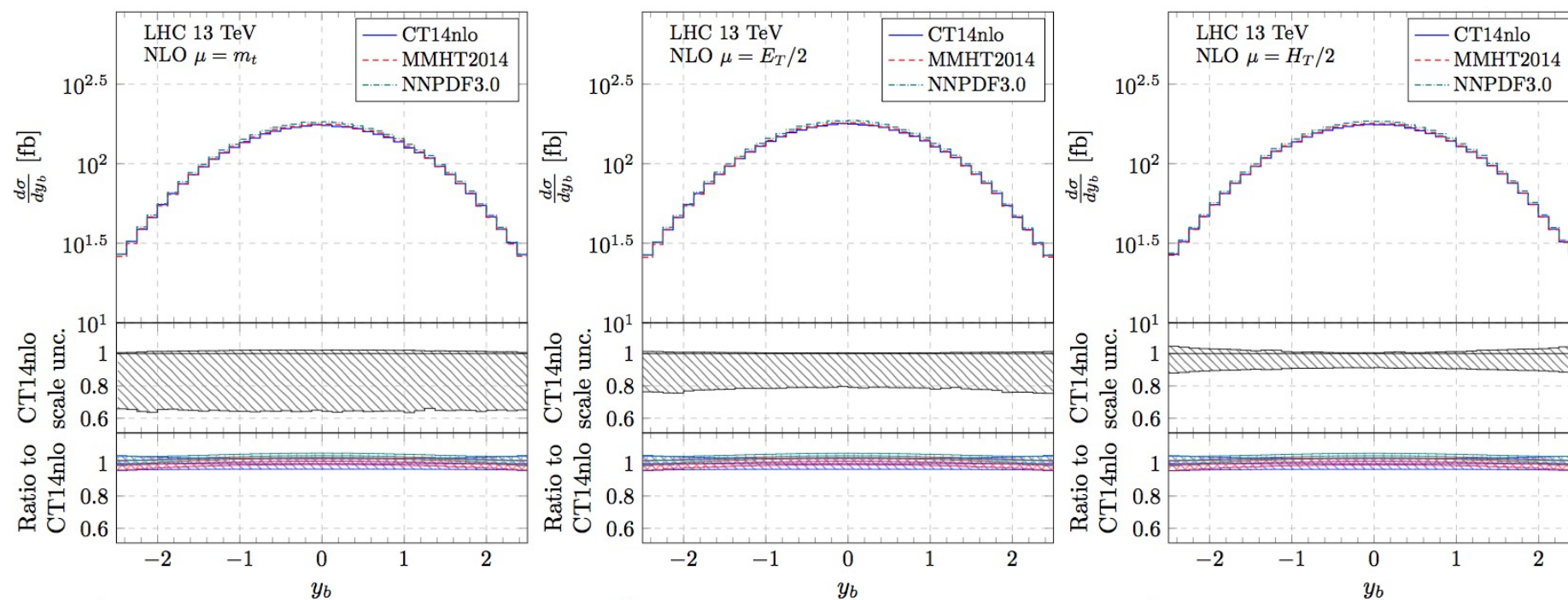
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- $p_T(b) \Rightarrow$ For $\mu_0 = \frac{1}{2} H_T$ scale uncertainties have reached almost 10% $\Rightarrow$ PDF uncertainties stayed below 6%
- $y(b) \Rightarrow$ For $\mu_0 = \frac{1}{2} H_T$ scale uncertainties are below 8% $\Rightarrow$ PDF uncertainties are below 5%
- Scale uncertainties dominant source of theoretical uncertainties

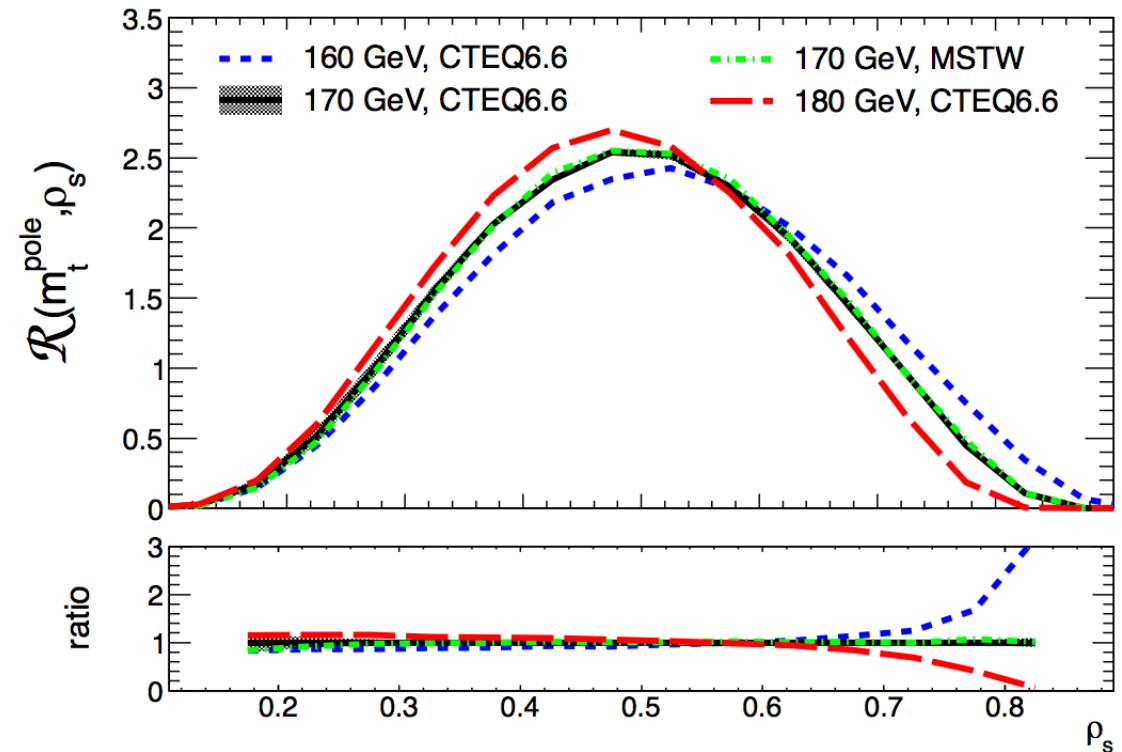


APPLICATIONS

- Alternative method for m_t
- m_t from normalized differential cross section for $pp \rightarrow ttj$
- $\mathcal{R}$ has been calculated using $pp \rightarrow ttj$ @ NLO in QCD + **POWHEG** matched with **PYTHIA**
- Theoretical uncertainties & PDF uncertainties affect m_t extraction $< 1 \text{ GeV}$
- Worth looking at ...

$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}(m_t^{\text{pole}}, \rho_s)$$

$$\rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}j}}}.$$

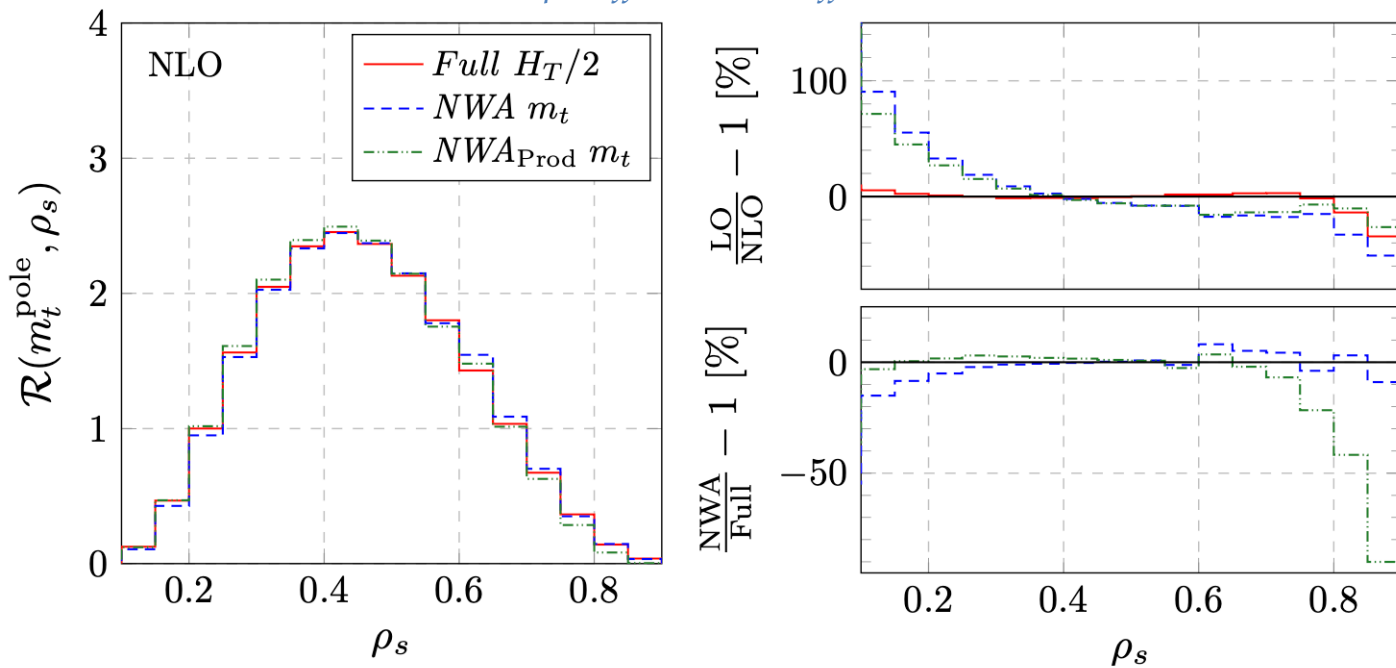


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Eur. Phys. J. C 73 (2013) 2438

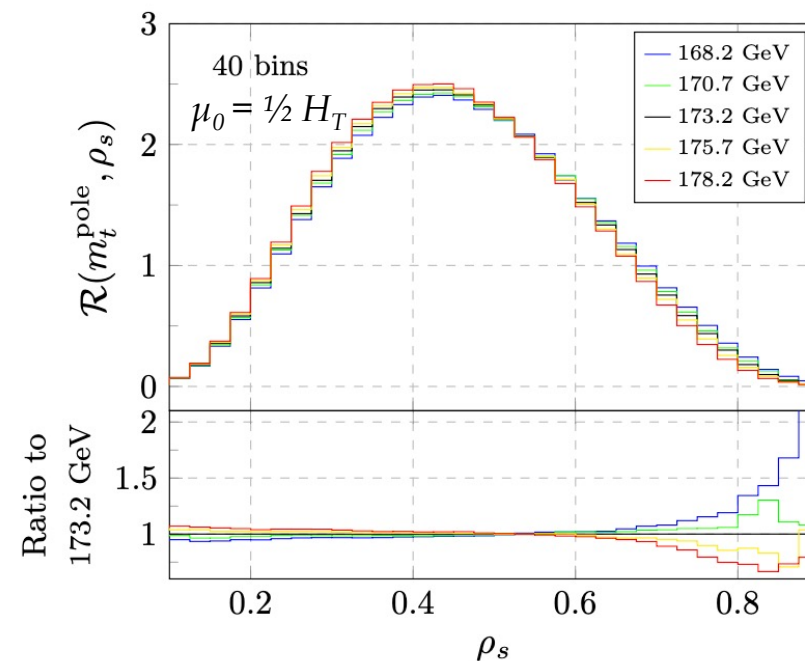
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Shape differences @ differential level



Full case for five different top quark masses



- Normalised ρ_s differential distribution
- Three different theoretical descriptions
 - Relative size of NLO QCD corrections
 - Relative size of full off-shell t & W effects
 - Relative size of corrections to top-quark decays

Normalisation differences @ integrated level

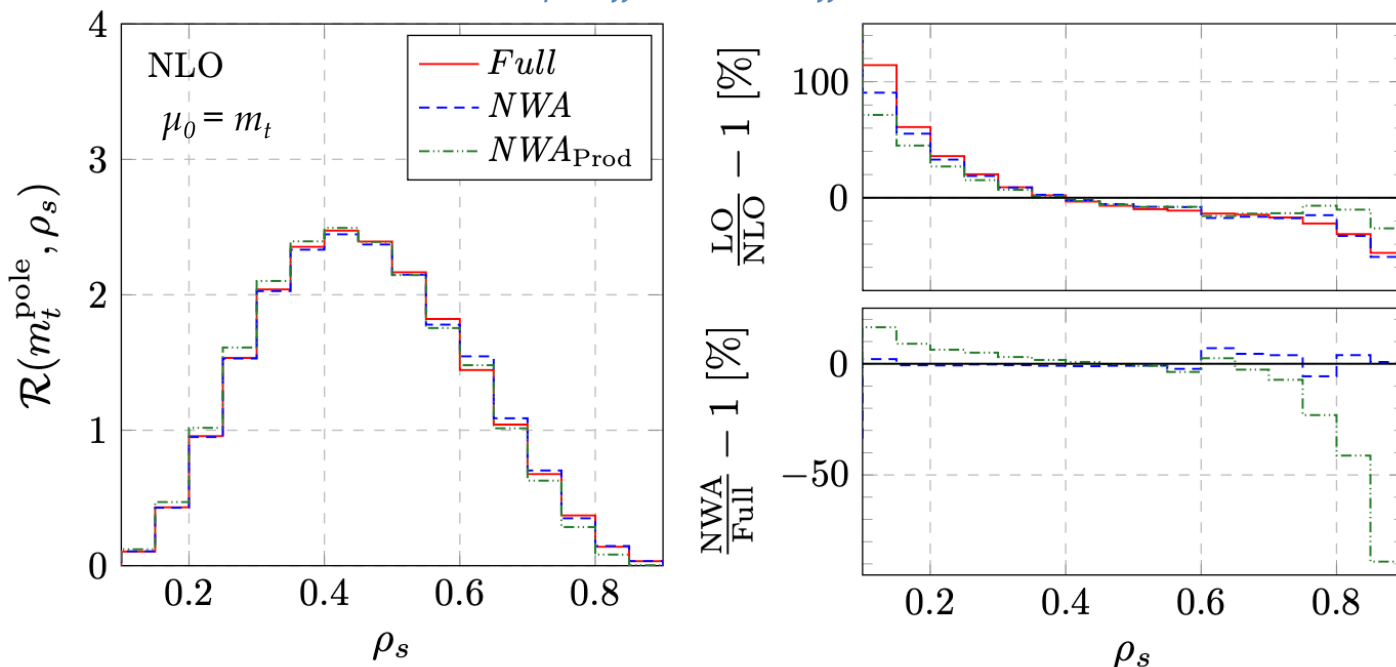
	$Full$ $[m_t]$	$Full$ $[\frac{1}{2}H_T]$	NWA $[m_t]$	$NWA_{\text{Prod.}}$ $[m_t]$	$\frac{NWA}{Full} - 1$ $[m_t/m_t]$	$\frac{NWA}{Full} - 1$ $[m_t/\frac{1}{2}H_T]$
$\sigma_{t\bar{t}j}^{\text{NLO}}$ [fb]	537.2	538.6	527.1	656.1	-1.9%	-2.1%

- Full off-shell effects change NLO cross section by 2%
- Consistent with uncertainty of NWA $\Rightarrow \mathcal{O}(\Gamma_t/m_t)$

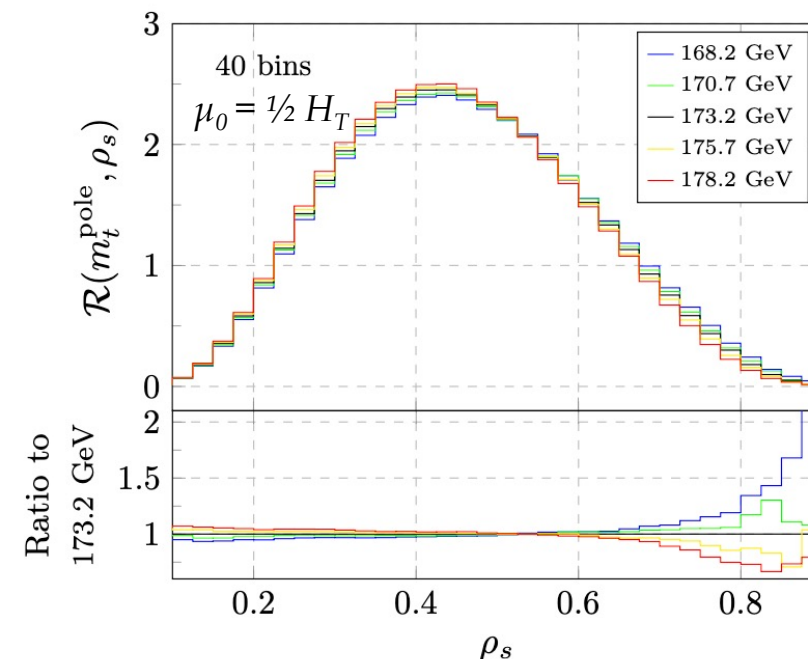
OFF-SHELL VERSUS ON-SHELL PREDICTIONS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

Shape differences @ differential level



Full case for five different top quark masses



- Normalised ρ_s differential distribution
- Three different theoretical descriptions
 - Relative size of NLO QCD corrections
 - Relative size of full off-shell t & W effects
 - Relative size of corrections to top-quark decays

Normalisation differences @ integrated level

	Full [m_t]	Full [$\frac{1}{2} H_T$]	NWA [m_t]	$NWA_{\text{Prod.}}$ [m_t]	$\frac{\text{NWA}}{\text{Full}} - 1$ [m_t/m_t]	$\frac{\text{NWA}}{\text{Full}} - 1$ [$m_t/\frac{1}{2} H_T$]
$\sigma_{t\bar{t}j}^{\text{NLO}}$ [fb]	537.2	538.6	527.1	656.1	-1.9%	-2.1%

- Full off-shell effects change NLO cross section by 2%
- Consistent with uncertainty of NWA $\Rightarrow \mathcal{O}(\Gamma_t/m_t)$

OFF-SHELL VERSUS ON-SHELL PREDICTIONS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

Luminosity of 2.5 fb^{-1} & $m_t^{\text{in}} = 173.2 \text{ GeV}$

	Theory, NLO QCD	$m_t^{\text{out}} \pm \delta m_t^{\text{out}}$	Averaged	Probability	$m_t^{\text{in}} - m_t^{\text{out}}$
	CT14 PDF	[GeV]	$\chi^2/\text{d.o.f.}$	$p\text{-value}$	[GeV]
Same bin size	31 bins				
	Full, $\mu_0 = H_T/2$	173.38 ± 1.34	1.04	0.40 (0.8 σ)	-0.18
	Full, $\mu_0 = E_T/2$	172.84 ± 1.33	1.05	0.39 (0.9 σ)	+0.36
	Full, $\mu_0 = m_t$	174.11 ± 1.39	1.07	0.37 (0.9 σ)	-0.91
	NWA, $\mu_0 = m_t$	175.70 ± 0.96	1.17	0.24 (1.2 σ)	-2.50
	NWA _{Prod.} , $\mu_0 = m_t$	169.93 ± 0.98	1.20	0.20 (1.3 σ)	+3.27
	5 bins				
	Full, $\mu_0 = H_T/2$	173.15 ± 1.32	0.93	0.44 (0.8 σ)	+0.05
	Full, $\mu_0 = E_T/2$	172.55 ± 1.18	1.07	0.37 (0.9 σ)	+0.65
	Full, $\mu_0 = m_t$	173.92 ± 1.38	1.48	0.20 (1.3 σ)	-0.72
Different bin size	NWA, $\mu_0 = m_t$	175.54 ± 0.97	1.38	0.24 (1.2 σ)	-2.34
	NWA _{Prod.} , $\mu_0 = m_t$	169.37 ± 1.43	1.16	0.33 (1.0 σ)	+3.83
	ATLAS binning				
	Full, $\mu_0 = H_T/2$	173.05 ± 1.31	0.99	0.42 (0.8 σ)	+0.15
	Full, $\mu_0 = E_T/2$	172.19 ± 1.34	1.05	0.39 (0.9 σ)	+1.01
	Full, $\mu_0 = m_t$	173.86 ± 1.39	1.42	0.21 (1.2 σ)	-0.66
	NWA, $\mu_0 = m_t$	175.22 ± 1.15	1.38	0.23 (1.2 σ)	-2.02
	NWA _{Prod.} , $\mu_0 = m_t$	169.39 ± 1.46	1.12	0.35 (0.9 σ)	+3.81
	CMS binning				
	Full, $\mu_0 = H_T/2$	173.09 ± 1.53	0.94	0.44 (0.8 σ)	+0.11
	Full, $\mu_0 = E_T/2$	172.20 ± 1.54	0.96	0.43 (0.8 σ)	+1.00
	Full, $\mu_0 = m_t$	173.94 ± 1.49	1.42	0.22 (1.2 σ)	-0.74
	NWA, $\mu_0 = m_t$	175.66 ± 1.10	1.42	0.22 (1.2 σ)	-2.46
	NWA _{Prod.} , $\mu_0 = m_t$	169.96 ± 1.80	1.00	0.41 (0.8 σ)	+3.24

- Agreement within $0.8\sigma - 1.3\sigma$ between various theoretical descriptions & pseudo-data
- 68 % C.L. (1σ) statistical error $\Rightarrow$ Still large $\Rightarrow 0.96 - 1.80$
- Averaged minimal $\chi^2/\text{d.o.f.}$ is of order of 1
- Number of standard deviations for each $p\text{-value}$
- Top quark mass shift $\Rightarrow$ Depending on theory used various mass shifts are observed
 - $2.0 - 2.5 \text{ GeV}$ mass shift is visible for NWA with $\mu_0 = m_t$ if pseudo data obtained from full off-shell case with $\mu_0 = \frac{1}{2} H_T$
 - $1.2 - 2.0 \text{ GeV}$ mass shift is visible for NWA with $\mu_0 = m_t$ if pseudo data obtained from full off-shell case with $\mu_0 = m_t$
 - For NWA_{Prod.} substantial deviation $\Rightarrow 3.2 - 3.8 \text{ GeV}$

OFF-SHELL VERSUS ON-SHELL PREDICTIONS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

- For higher luminosity despite diminished quality of $\chi^2/\text{d.o.f}$ fit mass shifts persist
 - Up to 2.5 GeV for NWA with $\mu_0 = m_t$ when pseudo-data are generated from full off-shell case with $\mu_0 = \frac{1}{2} H_T$
 - Up to 2.0 GeV for NWA with $\mu_0 = m_t$ when pseudo-data are generated from full off-shell case with $\mu_0 = m_t$
- Statistical error $\Rightarrow 0.3 - 0.4 \text{ GeV}$ only
- NWA case is disfavoured at $4\sigma - 5\sigma$ level
- NWA_{Prod.} at $2\sigma - 5\sigma$ level
- Full off-shell case with $\mu_0 = m_t$ at $3\sigma - 4\sigma$ level
- *Off-shell effects and non-resonant contributions of t & W are not negligible for top-quark mass extraction*
- *Scale setting plays important role*

Luminosity of 25 fb^{-1} & $m_t^{\text{in}} = 173.2 \text{ GeV}$

Theory, NLO QCD CT14 PDF	$m_t^{\text{out}} \pm \delta m_t^{\text{out}}$ [GeV]	Averaged $\chi^2/\text{d.o.f.}$	Probability $p\text{-value}$	$m_t^{\text{in}} - m_t^{\text{out}}$ [GeV]
<i>31 bins</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.09 ± 0.42	1.04	0.41 (0.8σ)	+0.11
<i>Full, $\mu_0 = E_T/2$</i>	172.45 ± 0.39	1.12	0.30 (1.0σ)	+0.75
<i>Full, $\mu_0 = m_t$</i>	173.76 ± 0.40	1.87	0.003 (3.0σ)	-0.56
<i>NWA, $\mu_0 = m_t$</i>	175.65 ± 0.31	2.99	$7 \cdot 10^{-8}$ (5.4σ)	-2.45
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.59 ± 0.30	3.10	$2 \cdot 10^{-8}$ (5.6σ)	+3.61
<i>5 bins</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.08 ± 0.40	0.94	0.44 (0.8σ)	+0.12
<i>Full, $\mu_0 = E_T/2$</i>	172.48 ± 0.38	1.58	0.18 (1.3σ)	+0.72
<i>Full, $\mu_0 = m_t$</i>	173.75 ± 0.40	6.76	$2 \cdot 10^{-5}$ (4.3σ)	-0.55
<i>NWA, $\mu_0 = m_t$</i>	175.49 ± 0.30	5.31	$2 \cdot 10^{-4}$ (3.7σ)	-2.29
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.39 ± 0.47	3.42	$8 \cdot 10^{-3}$ (2.6σ)	+3.81
<i>ATLAS binning</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.06 ± 0.44	0.97	0.44 (0.8σ)	+0.14
<i>Full, $\mu_0 = E_T/2$</i>	172.36 ± 0.44	1.38	0.23 (1.2σ)	+0.84
<i>Full, $\mu_0 = m_t$</i>	173.84 ± 0.42	5.12	$1 \cdot 10^{-4}$ (3.9σ)	-0.64
<i>NWA, $\mu_0 = m_t$</i>	175.23 ± 0.37	5.28	$7 \cdot 10^{-5}$ (4.0σ)	-2.03
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	169.43 ± 0.50	2.61	0.02 (2.3σ)	+3.77
<i>CMS binning</i>				
<i>Full, $\mu_0 = H_T/2$</i>	173.09 ± 0.50	0.96	0.43 (0.8σ)	+0.11
<i>Full, $\mu_0 = E_T/2$</i>	172.22 ± 0.48	1.32	0.26 (1.1σ)	+0.98
<i>Full, $\mu_0 = m_t$</i>	174.02 ± 0.46	6.57	$3 \cdot 10^{-5}$ (4.2σ)	-0.82
<i>NWA, $\mu_0 = m_t$</i>	175.74 ± 0.34	6.00	$8 \cdot 10^{-5}$ (3.9σ)	-2.54
<i>NWA_{Prod.}, $\mu_0 = m_t$</i>	170.22 ± 0.53	2.19	0.07 (1.8σ)	+2.98

$$(\Delta m_t^{\text{out}})_\mu = \pm \max \left\{ \left| m_t^{\text{out}} \left(\frac{\mu_0}{2}, \text{CT14} \right) - m_t^{\text{out}}(\mu_0, \text{CT14}) \right| \right. \\ \left. \left| m_t^{\text{out}}(2\mu_0, \text{CT14}) - m_t^{\text{out}}(\mu_0, \text{CT14}) \right| \right\}$$

$$(\Delta m_t^{\text{out}})_{\text{PDF}} = \pm \max \left\{ \left| m_t^{\text{out}}(\mu_0, \text{MMHT14}) - m_t^{\text{out}}(\mu_0, \text{CT14}) \right| \right. \\ \left. \left| m_t^{\text{out}}(\mu_0, \text{NNPDF3}) - m_t^{\text{out}}(\mu_0, \text{CT14}) \right| \right\}$$

*Default setup
with $\mu_0 = \frac{1}{2} H_T$*

- Simultaneous variation of renormalisation & factorisation scales up & down by factor of 2 around central value μ_0
- For $\mu_0 = \frac{1}{2} H_T$ & $\mu_0 = \frac{1}{2} E_T$ theoretical uncertainties stemming from scale variation $\Rightarrow 0.6 \text{ GeV} - 1.2 \text{ GeV}$
- For $\mu_0 = m_t$ they are larger $\Rightarrow 2.1 \text{ GeV} - 2.8 \text{ GeV}$
- PDF uncertainties $\Rightarrow 0.4 \text{ GeV} - 0.7 \text{ GeV}$
- **COMPARISON WITH ATLAS** $\Rightarrow$ *New setup* $\Rightarrow$ Full 7-point scale variation & internal PDF uncertainties for NNPDF3.0 with α_s variations, CT18, PDF4LHC21 for 7 different top-quark masses

- Complete description for $pp \rightarrow ttj$ process with **HELAC-NLO** for di-lepton channel
 - “resonant” and “non-resonant” contributions at NLO QCD
- Various scale settings: $\mu_0 = \frac{1}{2} H_T$ & $\mu_0 = \frac{1}{2} E_T$ & $\mu_0 = m_t$
- $\mu_0 = \frac{1}{2} H_T$ “better” than $\mu_0 = \frac{1}{2} E_T \Rightarrow$ Booth stabilizes *high p_T tails* but $\mu_0 = \frac{1}{2} H_T$ gives smaller error
- Scale & PDF uncertainties for σ & various $d\sigma/dX$
- Further studies are needed:
 - Bottom-mass effects $\Rightarrow$ Comparisons between Five- & Four-Flavor schemes
- Phenomenological applications $\Rightarrow$ Alternative method for m_t extraction
 - Shape-based m_t measurement (e.g. end point of M_{e+b} and/or ρ_s)
 - Relies on precise modeling of top-quark decays
 - *Off-shell effects and non-resonant contributions of t & W are not negligible for top-quark mass extraction*
 - *Scale setting plays important role*
 - Predictions for $pp \rightarrow ttj$ should go beyond simple approximation of factorizing top quark production & decays

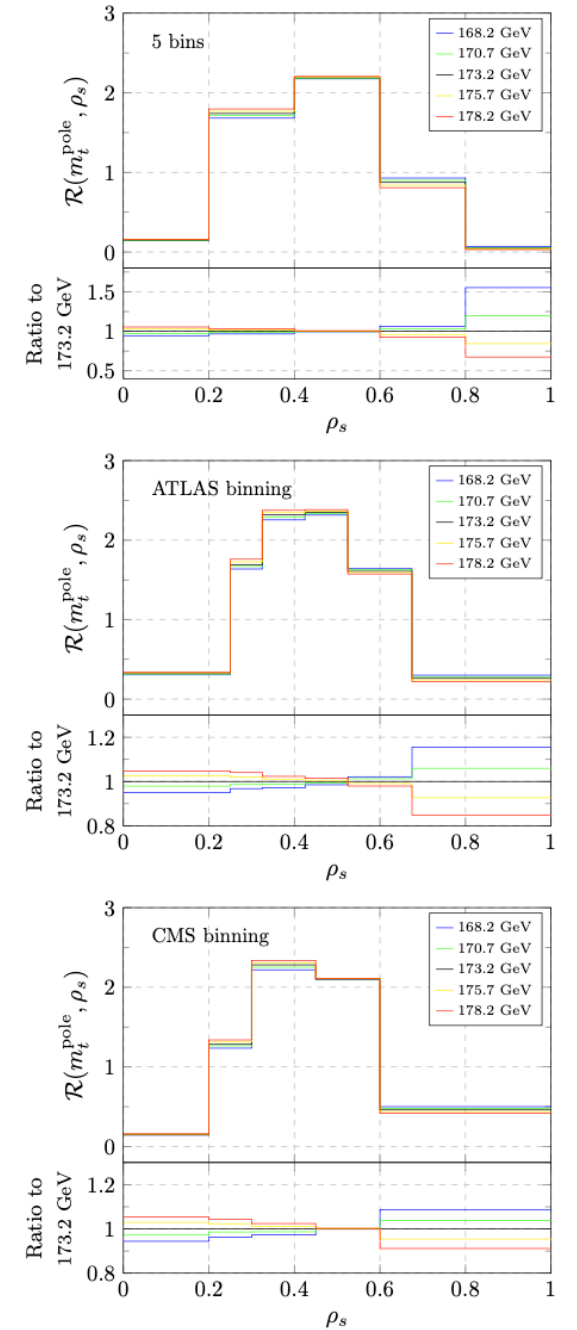
BACKUP

NORMALISED ρ_s DISTRIBUTION

5 equal size bins	ATLAS binning	CMS binning
0.00–0.20	0.000–0.250	0.00–0.20
0.20–0.40	0.250–0.325	0.20–0.30
0.40–0.60	0.325–0.425	0.30–0.45
0.60–0.80	0.425–0.525	0.45–0.60
0.80–1.00	0.525–0.675	0.60–1.00
—	0.675–1.000	—

- Various binnings used in m_t extraction from normalised ρ_s distribution
- Three cases are shown:
 - 5 equal size intervals
 - ATLAS intervals
 - CMS intervals
- The latter two optimised for $l+jets$ & $di-lepton$ channels @ 7 TeV & 8 TeV

$$R_i(m_t^{\text{pole}}) = \int_{\rho_{i-1}}^{\rho_i} d\rho_s \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s}(m_t^{\text{pole}}, \rho_s), \quad i = 1, \dots,$$



Off-shell $t\bar{t}j$

Results are provided for 7 input mass parameters m_t :

- ▶ 169 GeV, 170 GeV, 171 GeV, 172 GeV, 172.5 GeV, 173 GeV, 174 GeV

Scale choice:

- ▶ $\mu = H_T/2$, where $H_T = p_T^{l_1} + p_T^{l_2} + p_T^{b_1} + p_T^{b_2} + p_T^{miss} + p_T^{j_1}$

Uncertainties:

- ▶ 7-point scale variations
- ▶ Internal PDF uncertainties for $m_t = 172.5$ GeV for all PDF sets
- ▶ Results are provided for multiple PDF sets
- ▶ Variations + bands provided for both PDF and scale uncertainties
- ▶ All uncertainties are calculated after summing all channels and normalizing

PDF sets:

- ▶ NNPDF30_nlo_as_0118_hessian (303000)
 - In addition: α_S variations (265000, 266000)
- ▶ CT18NLO (14400)
- ▶ PDF4LHC21_40_pdfas (93300)

Off-shell $t\bar{t}j$

- ▶ exactly two b -jets, at least one light jet, two charged leptons and missing transverse momentum, denoted as p_T^{miss}

- ▶ Cuts:

$$\begin{array}{lll}
 p_{T\ell_1}(p_{T\ell_2}) > 28(20) \text{ GeV}, & p_{Tb} > 30 \text{ GeV}, & p_{Tj} > 60 \text{ GeV}, \\
 |y_\ell| < 2.5, & |y_b| < 2.5, & |y_j| < 2.5, \\
 \Delta R_{\ell\ell} > 0.4, & \Delta R_{bb} > 0.4, & \Delta R_{jj} > 0.4, \\
 \Delta R_{\ell b} > 0.4, & \Delta R_{\ell j} > 0.4, & \Delta R_{bj} > 0.4
 \end{array}$$

- ▶ In the same flavor channels e^+e^- and $\mu^+\mu^-$, we apply $p_T^{miss} > 30 \text{ GeV}$.
- ▶ anti- k_T jet clustering algorithm with $R = 0.4$

NORMALISED ρ_s DISTRIBUTION & TTJ @ NLO QCD

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

$p_{T,\ell} > 30 \text{ GeV} ,$	$p_{T,j} > 40 \text{ GeV} ,$
$\cancel{p}_T > 40 \text{ GeV} ,$	$\Delta R_{jj} > 0.5 ,$
$\Delta R_{\ell\ell} > 0.4 ,$	$\Delta R_{\ell j} > 0.4 ,$
$ y_\ell < 2.5 ,$	$ y_j < 2.5 ,$

JETS:

Final-state quarks and gluons with pseudo-rapidity $|y| < 5$ recombined into jets using *anti- k_T jet algorithm* with $R = 0.5$

REQUIREMENT:

Exactly *2 b-jets*, at least one light-jet, *2 charged leptons & missing p_T* $\Rightarrow$ Fairly inclusive cuts

$$p_{T,i} = \sqrt{p_{x,i}^2 + p_{y,i}^2} ,$$

$$y_i = \frac{1}{2} \ln \left(\frac{E_i + p_{z,i}}{E_i - p_{z,i}} \right) ,$$

$$\Delta R_{ik} = \sqrt{\Delta \phi_{ik}^2 + \Delta y_{ik}^2} .$$

NORMALISED ρ_S DISTRIBUTION & TTJ @ NLO QCD

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

$G_\mu = 1.16637 \cdot 10^{-5} \text{ GeV}^{-2},$ $m_W = 80.399 \text{ GeV},$ $m_Z = 91.1876 \text{ GeV},$	$m_t = 173.2 \text{ GeV}$ $\Gamma_W = 2.09875 \text{ GeV},$ $\Gamma_Z = 2.50848 \text{ GeV}.$
$\alpha = \frac{\sqrt{2}}{\pi} G_\mu m_W^2 \sin^2 \theta_W$	$\sin^2 \theta_W = 1 - \frac{m_W^2}{m_Z^2}$
$\Gamma_t^{\text{LO}} = 1.47834 \text{ GeV},$	$\Gamma_t^{\text{NLO}} = 1.35146 \text{ GeV}.$

- Different lepton generations
- Same lepton interference effects neglected $\Rightarrow$ per-mille level @ LO
- Top width for unstable W bosons, neglecting bottom quark mass
- All light quarks including b -quarks & leptons are massless
- Contribution from b quarks in initial state neglected $\Rightarrow$ Effect $< 1\%$ @ LO