

Understanding the nonlinear response of SiPMs

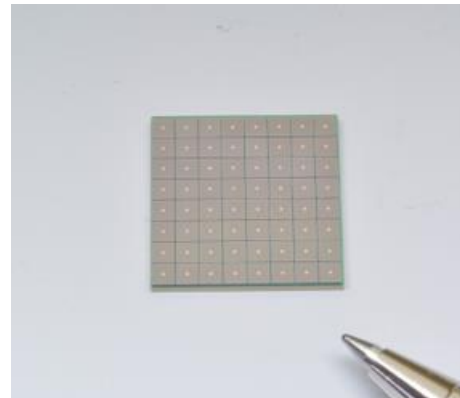
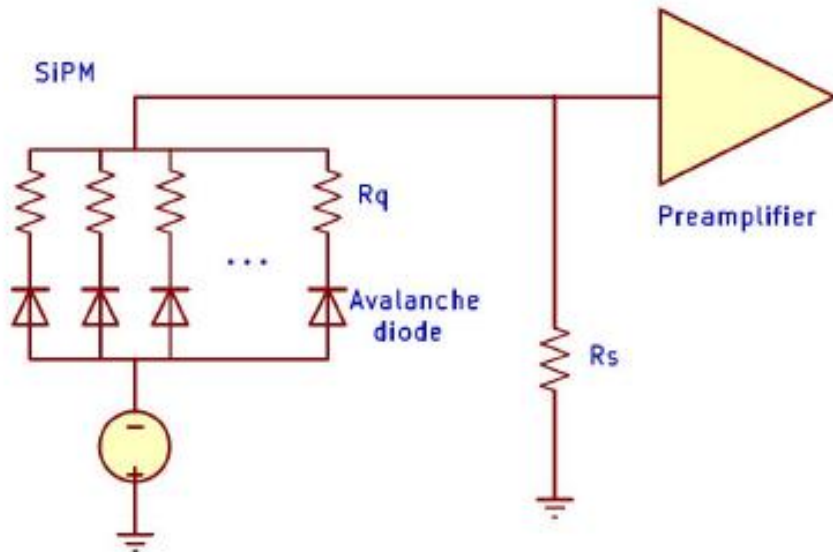
Alejandro Pérez, Víctor Moya-Zamanillo y Jaime Rosado

Grupo del Altas Energías GAE-UCM

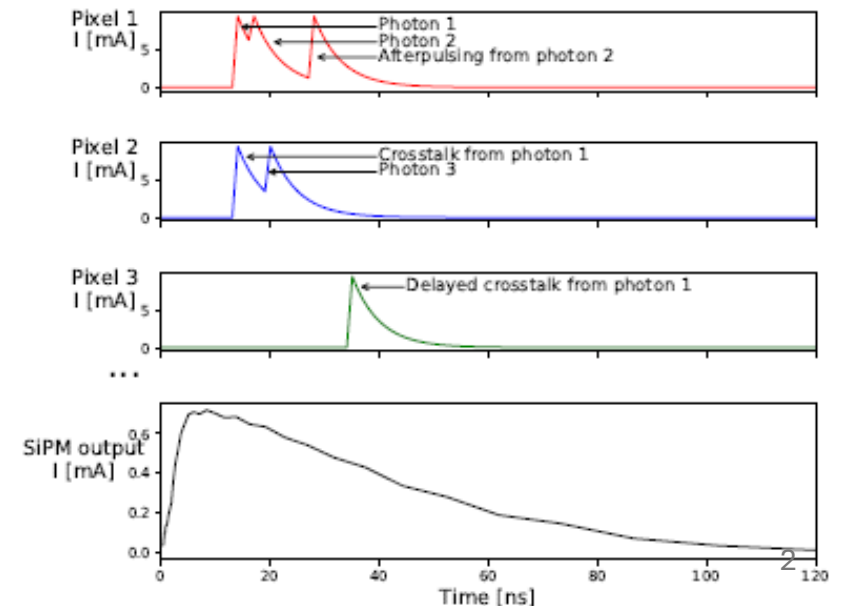
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Silicon Photomultipliers (SiPMs)

- Photonsensor increasingly used in many applications, especially in scintillator detectors
- Array of reverse biased avalanche photodiodes (pixels) operating in “Geiger mode”
- Ideally, when any pixel is triggered by a photon, an avalanche of fixed charge is produced
- A pixel takes some time τ_{rec} to recover after an avalanche \rightarrow If the number of photons of the light pulse is similar to the number of pixels, the SiPM response is nonlinear
- SiPMs also present:
 - Uncorrelated noise: “dark counts”
 - Correlated noise: crosstalk, afterpulsing, delayed crosstalk



Hamamatsu
S13361-2050



Nonlinear response

- Limitation to the dynamic range. Key factor in scintillator detectors
- Systematic analysis of the SiPM response through detailed MC simulations
- Response conveniently parameterized in terms of:

➤ Effective number of full avalanches per pixel: $y = \frac{\langle Q \rangle}{q_{av} \cdot N_{pix}}$

➤ Expected number of avalanches per pixel: $x = \frac{PDE \cdot N_{ph}}{N_{pix}}$

$\langle Q \rangle$: Mean output charge per pulse

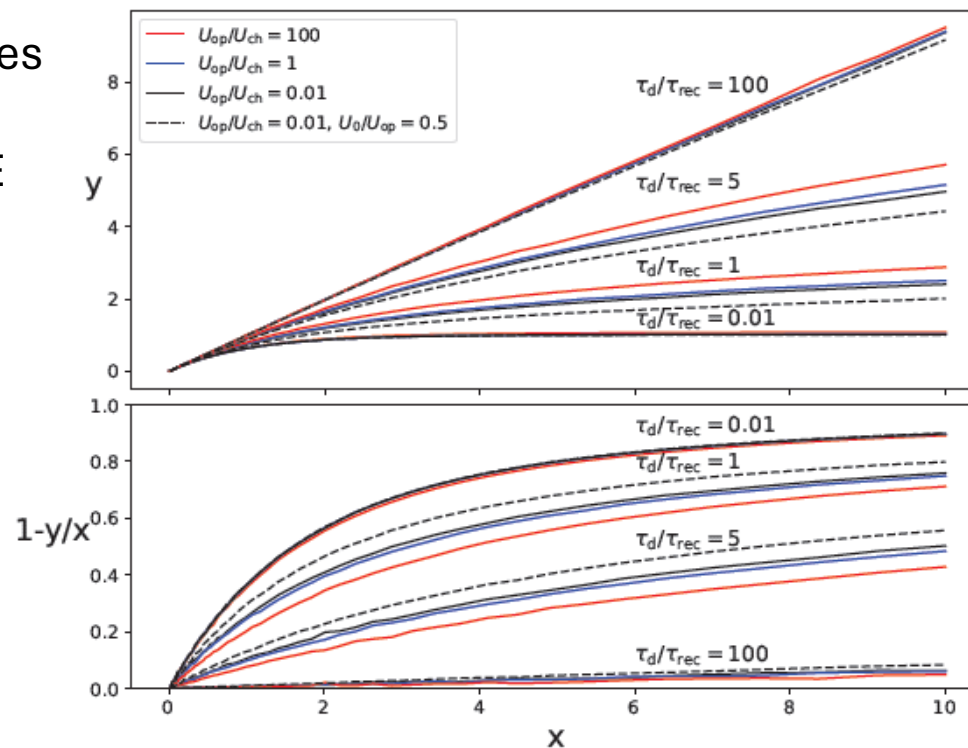
q_{av} : Charge of a single full avalanche

N_{pix} : Number of pixels

PDE : Photon Detection Efficiency

N_{ph} : Number of photons per pulse

Direct comparison of y vs x curves for SiPMs with different bias voltage, N_{pix} , q_{av} (gain) and PDE



Simulation code: Jha, A.K. et al. IEEE TNS 2013, 60, 336–351

This work: Moya-Zamanillo, V.; Rosado, J. Sensors 2024, 24(8), 2648

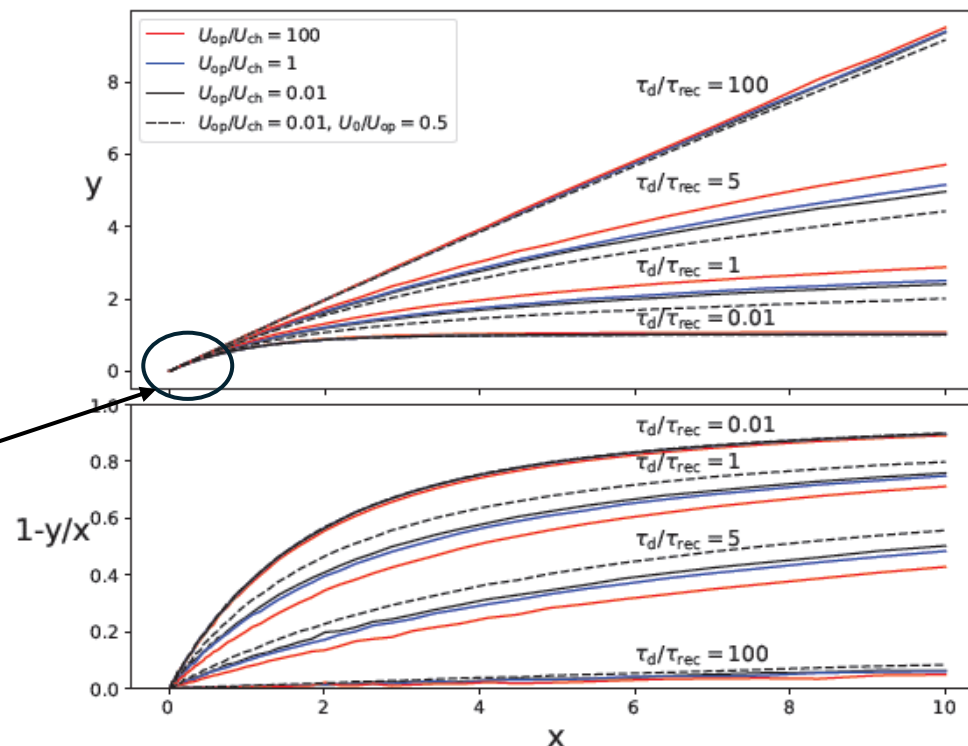
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Ideally, $y = x$ in the linear region ($x < 0.1$) and in the absence of correlated noise



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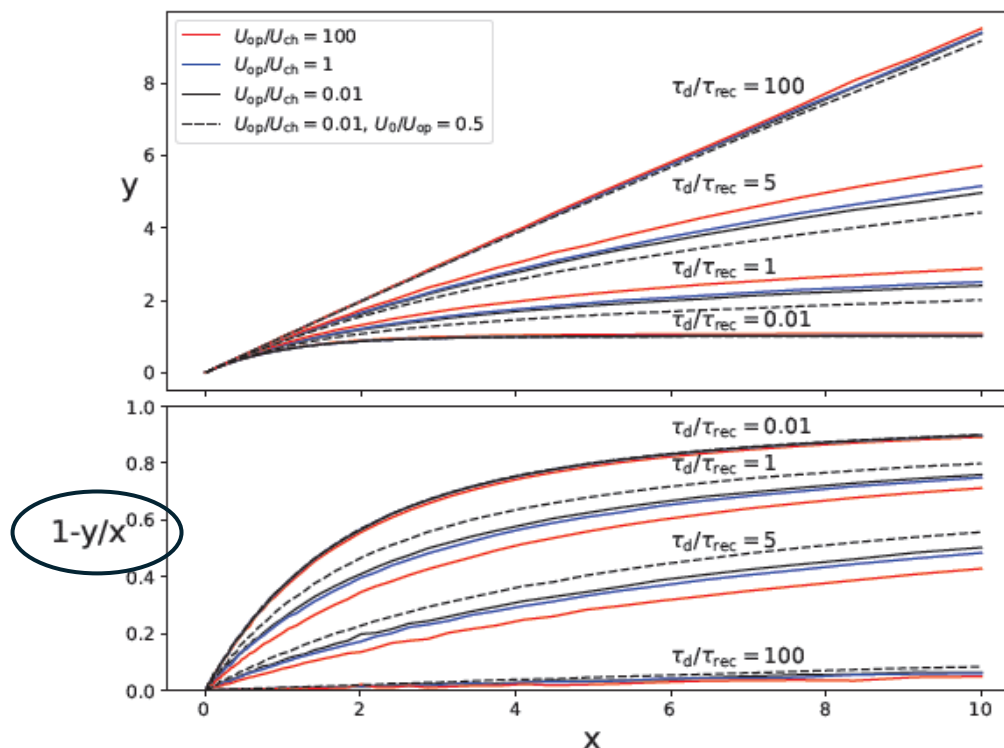
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Nonlinearity
parameter



Nonlinearity becomes stronger
when the pulse length decreases
relative to the recovery time

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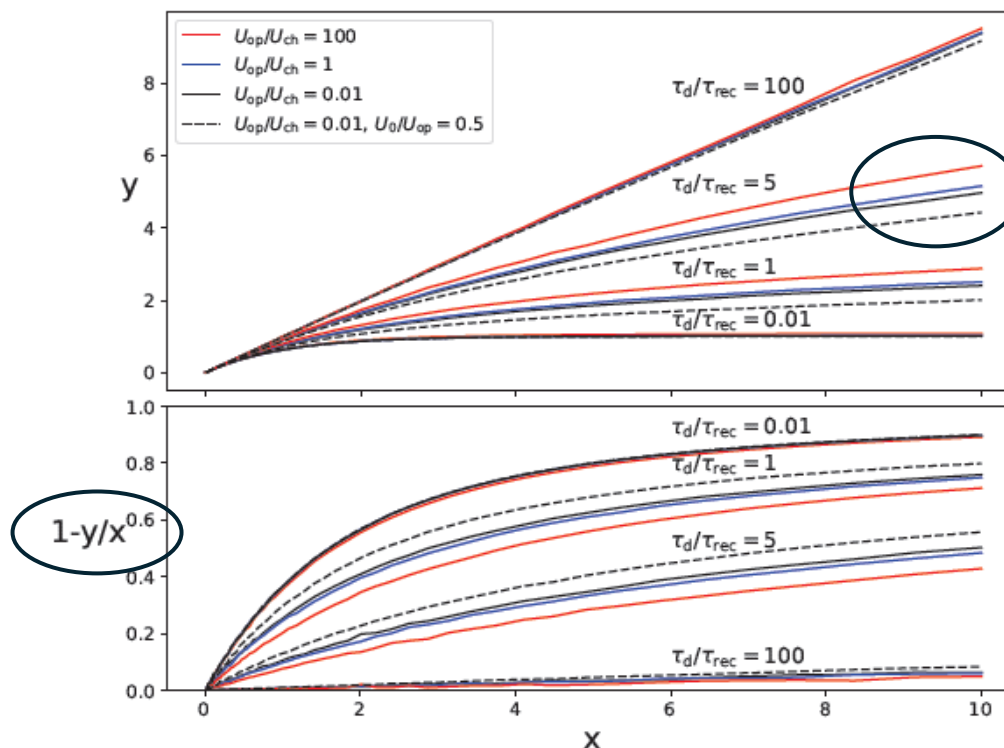
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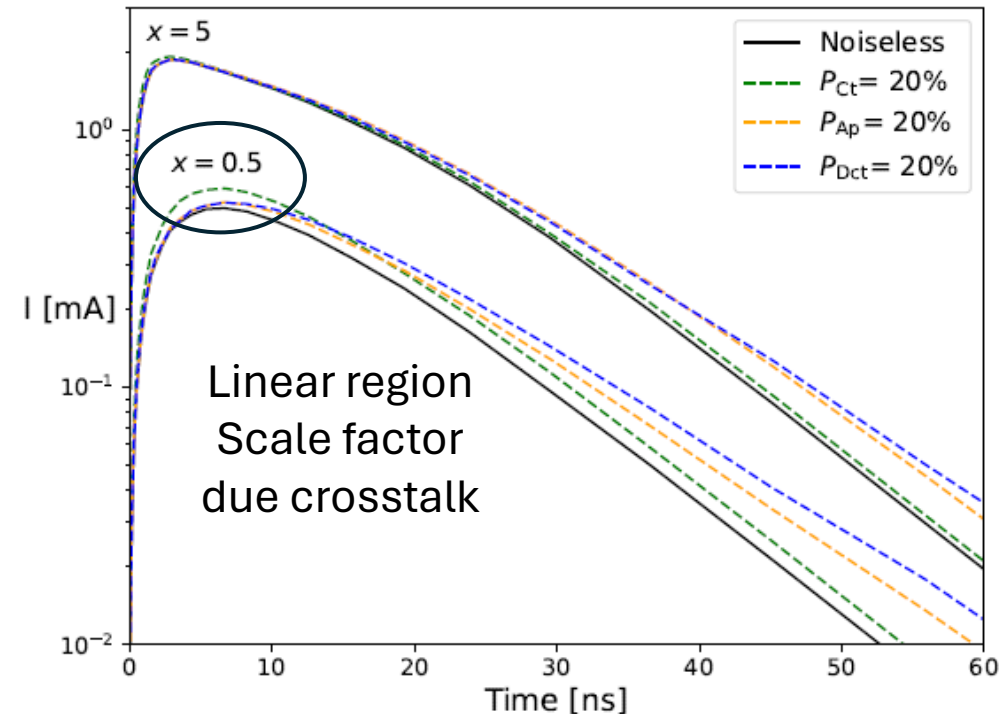
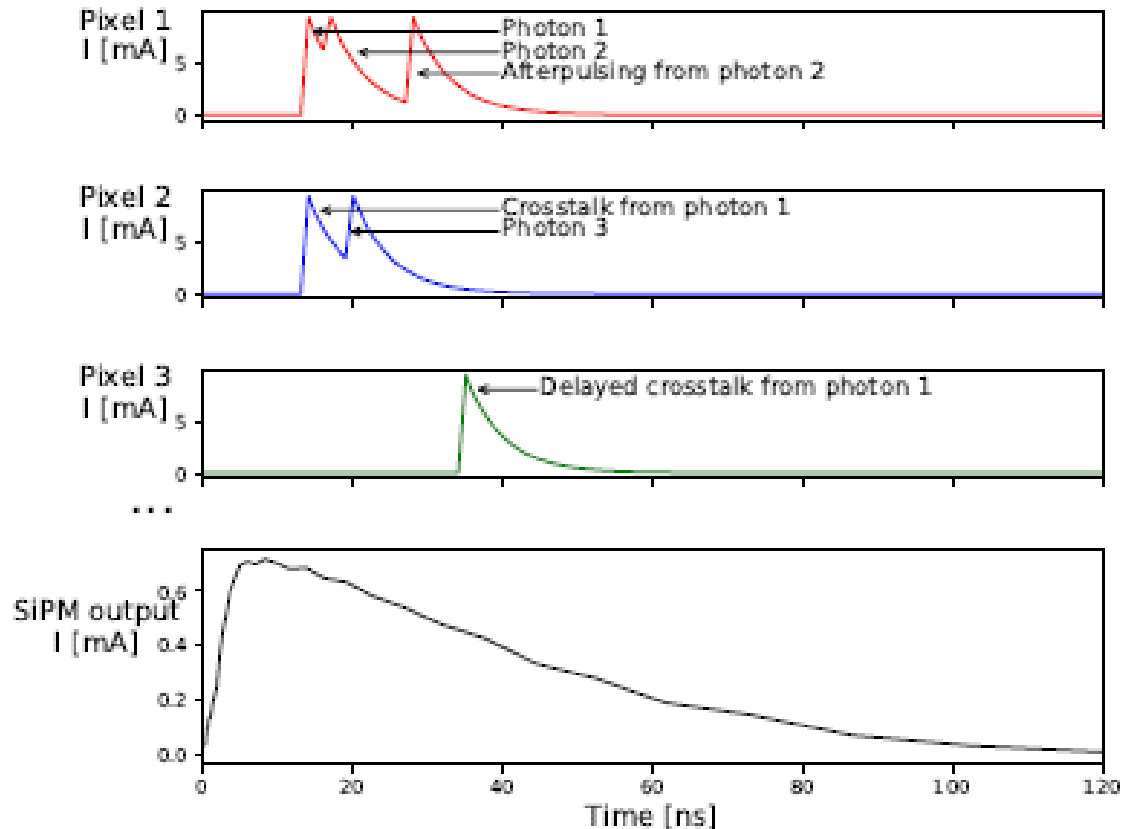
Nonlinearity also depends
on the characteristics of the
PDE vs voltage curve

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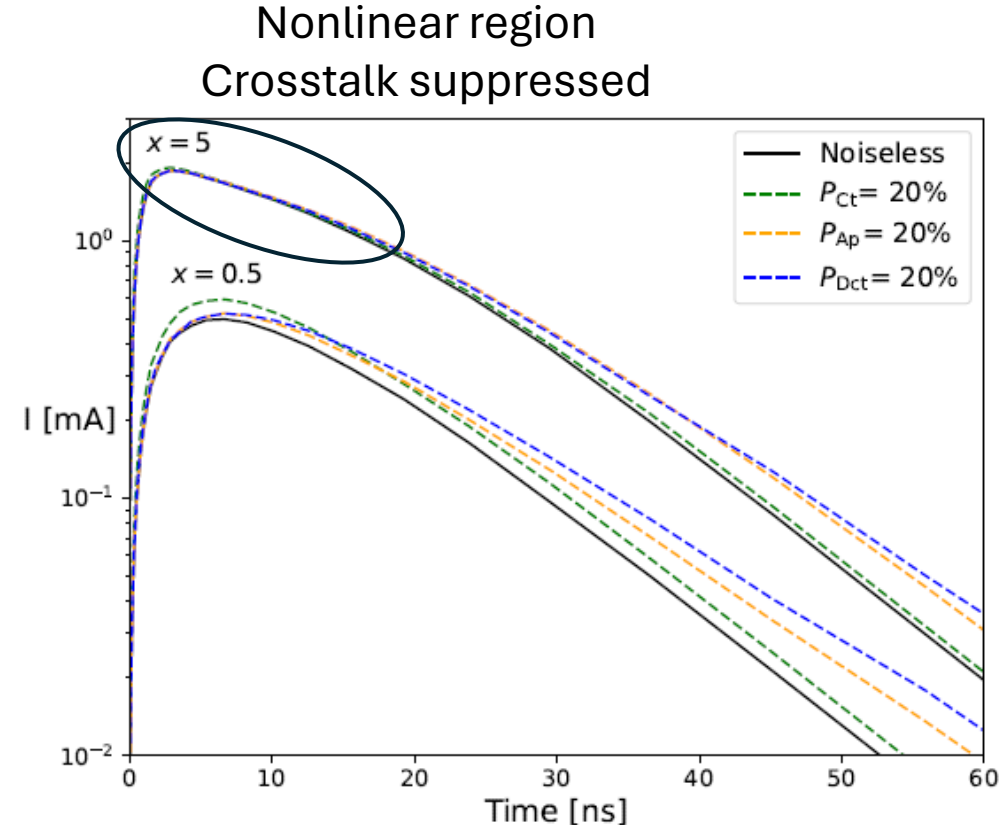
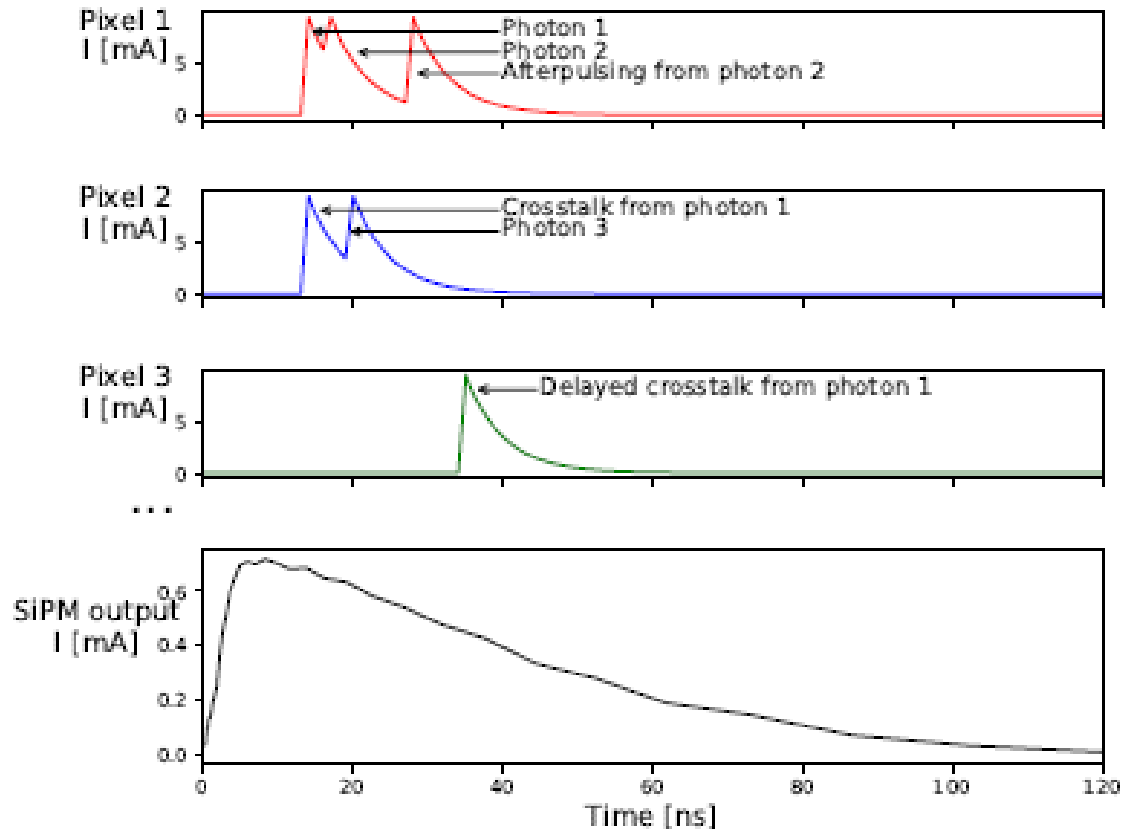
Correlated noise

- Correlated noise leads to an extra gain factor in the linear region
- Prompt crosstalk is strongly suppressed when nonlinearity becomes important
- Afterpulsing and delayed crosstalk less suppressed by nonlinearity and make the output signal longer



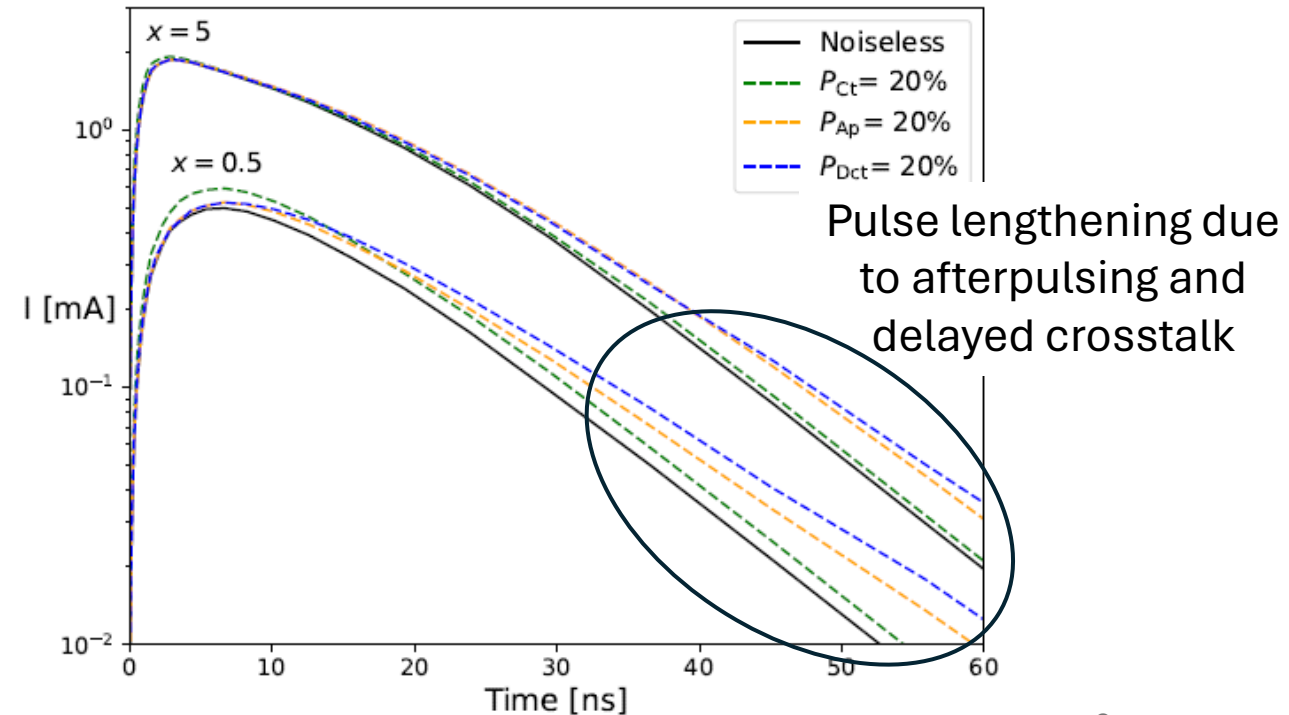
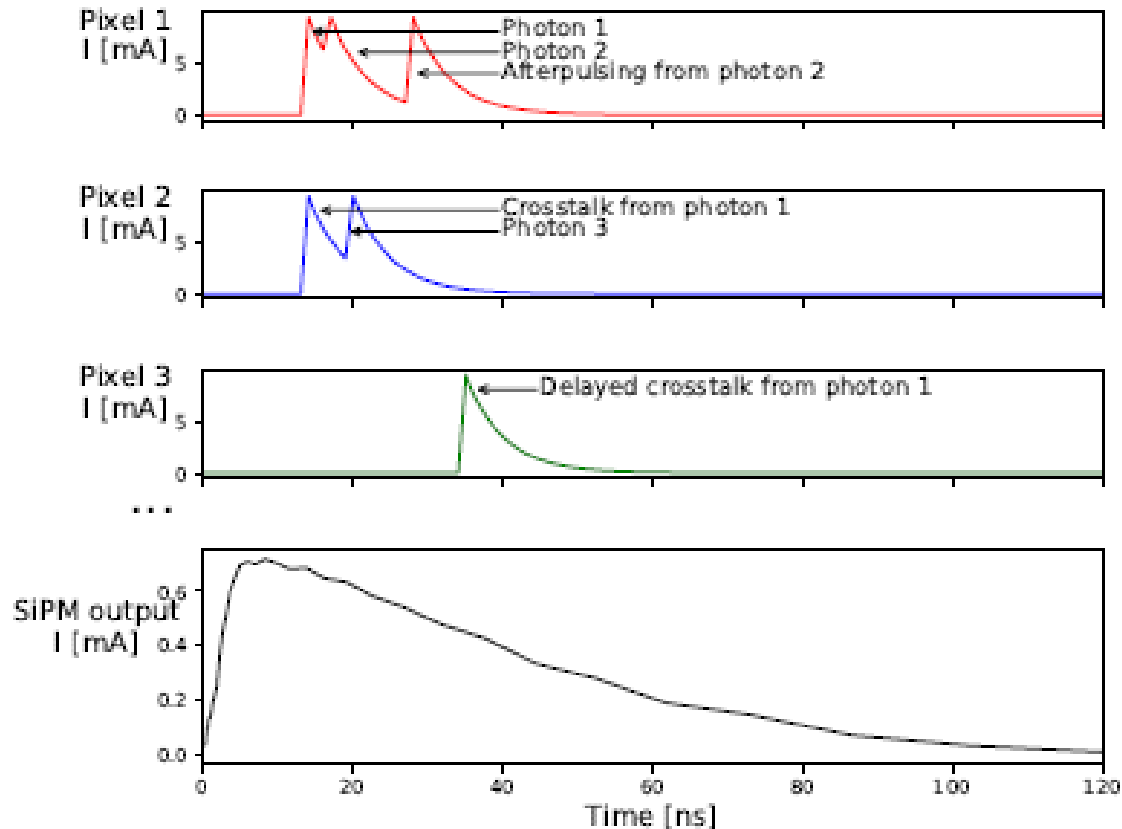
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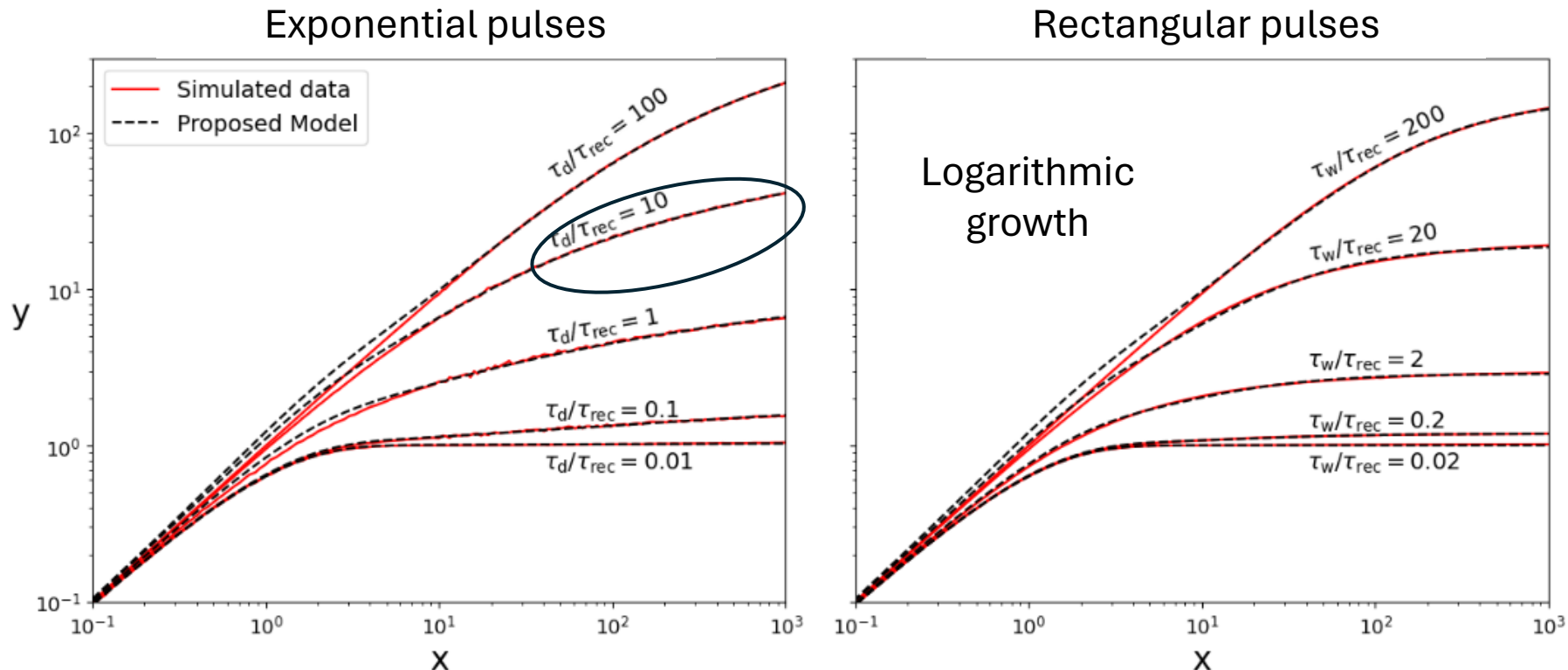
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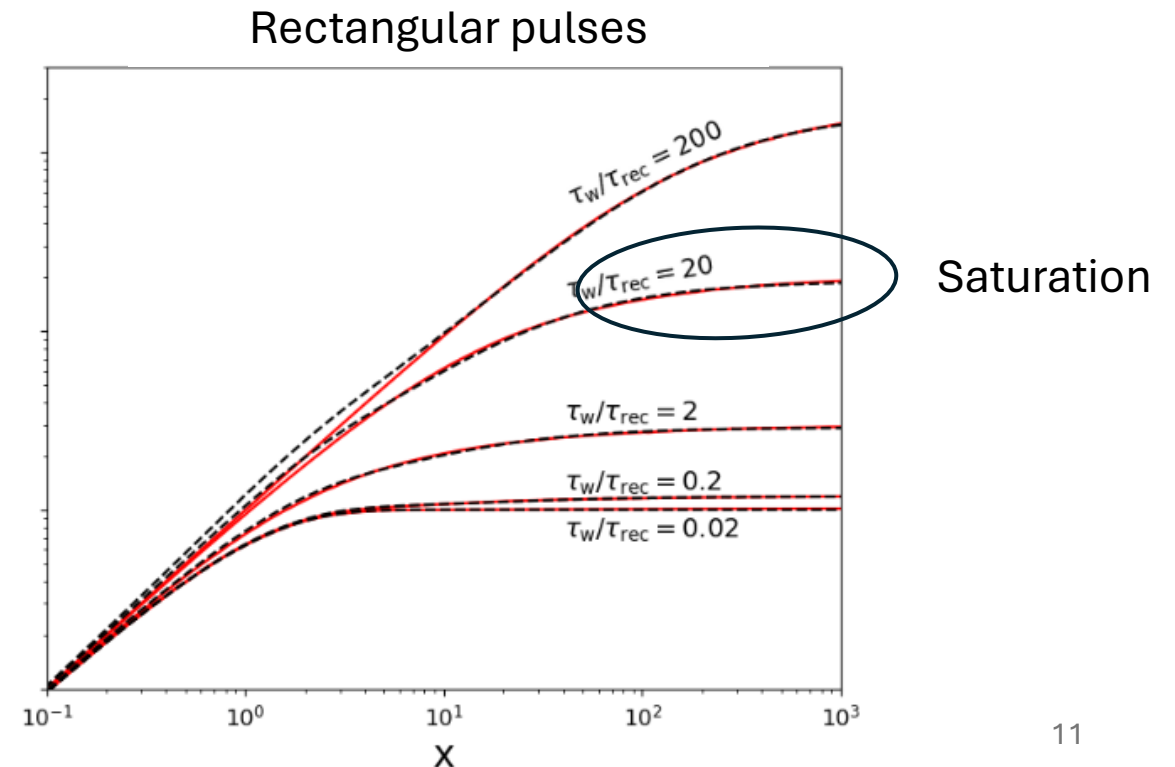
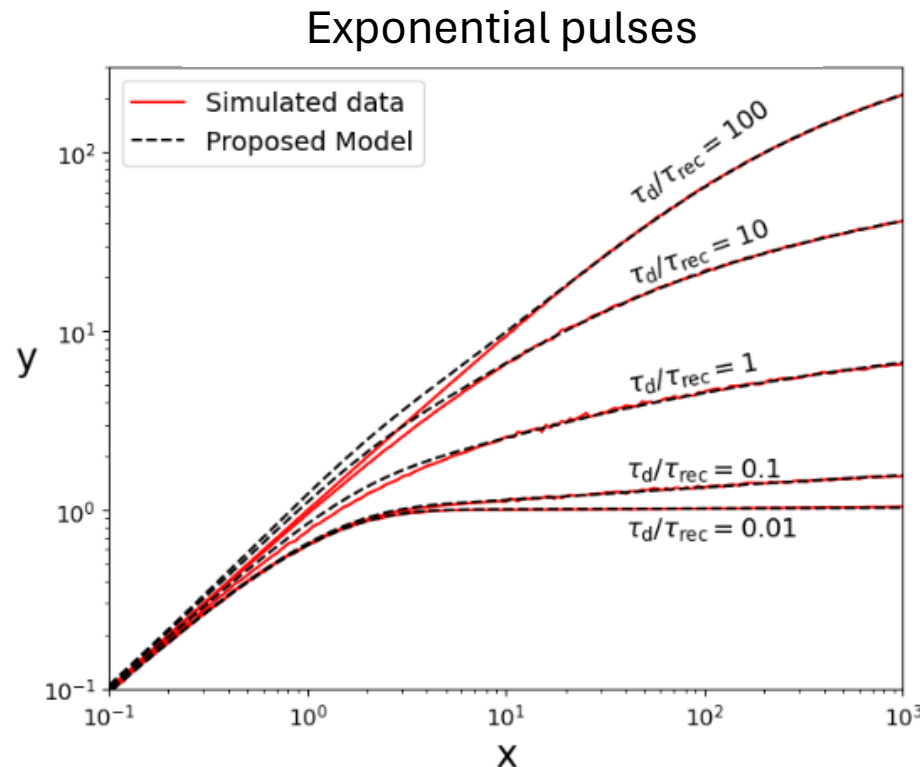
Response to different pulse shapes

- Apart from the photon rate, the SiPM response depends on the light pulse shape
- Long tailed pulses (e.g., scintillation pulses): logarithmic growth at large x values
- Finite pulses (e.g., rectangular pulses): saturation at large x values
- The flatter the pulse (the smaller variance of the photon rate), the stronger the nonlinearity



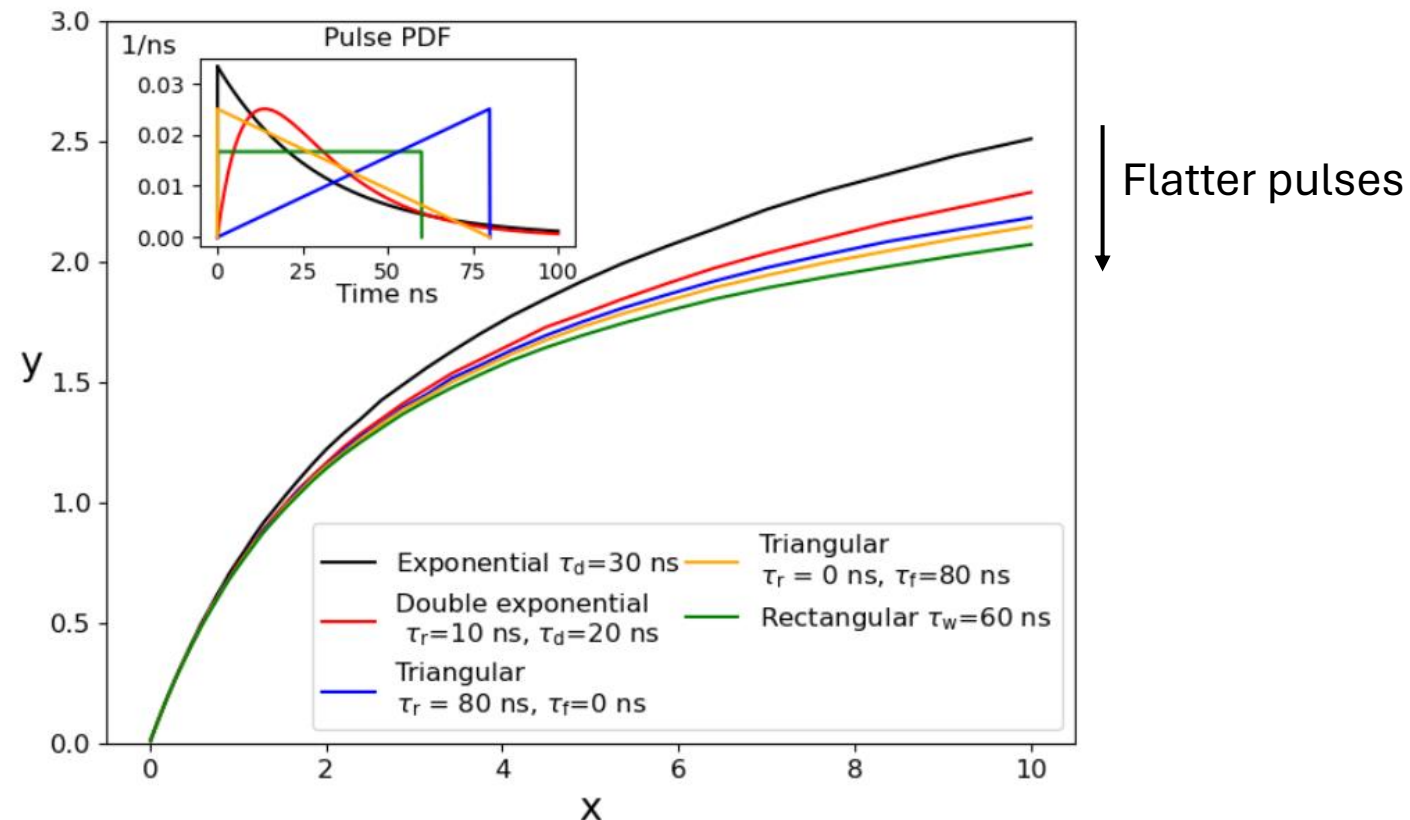
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Fitting model

- Based on our simulation results, we modeled the SiPM nonlinear response as

$$y = (1 + N(x) + R(x)) \cdot (1 - e^{-x})$$

y : Number of full avalanches per pixel

x : Expected number of avalanches per pixel

$1 - e^{-x}$: fraction of triggered pixels (from Poisson distribution of photons)

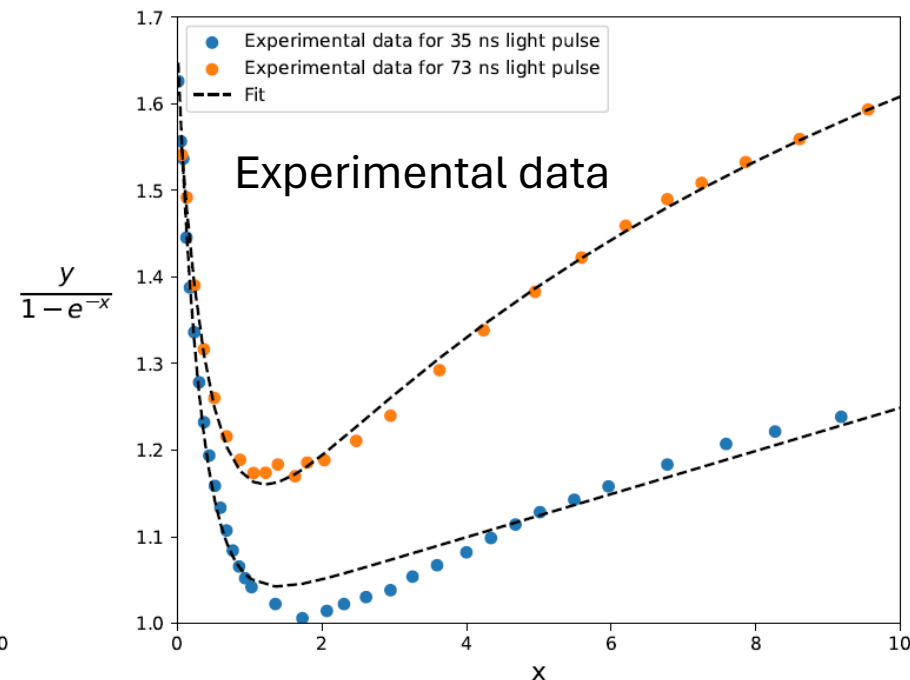
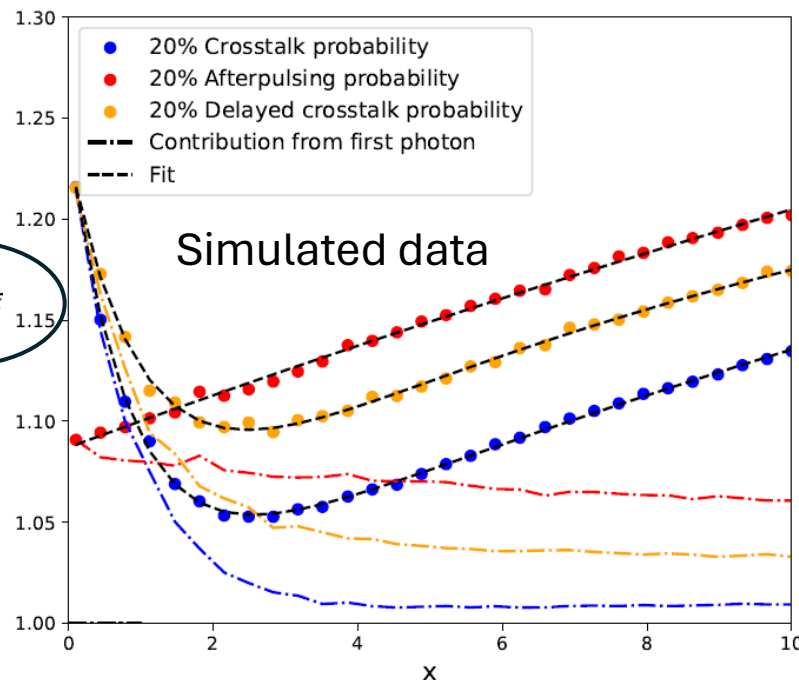
$1 + N(x) + R(x)$: average contribution per triggered pixel

$1 + N(x)$: First avalanche and correlated noise that it induces

$R(x)$: Avalanches produced during pixel recovery after first avalanche

Contribution per triggered pixel

$$\frac{y}{1 - e^{-x}}$$



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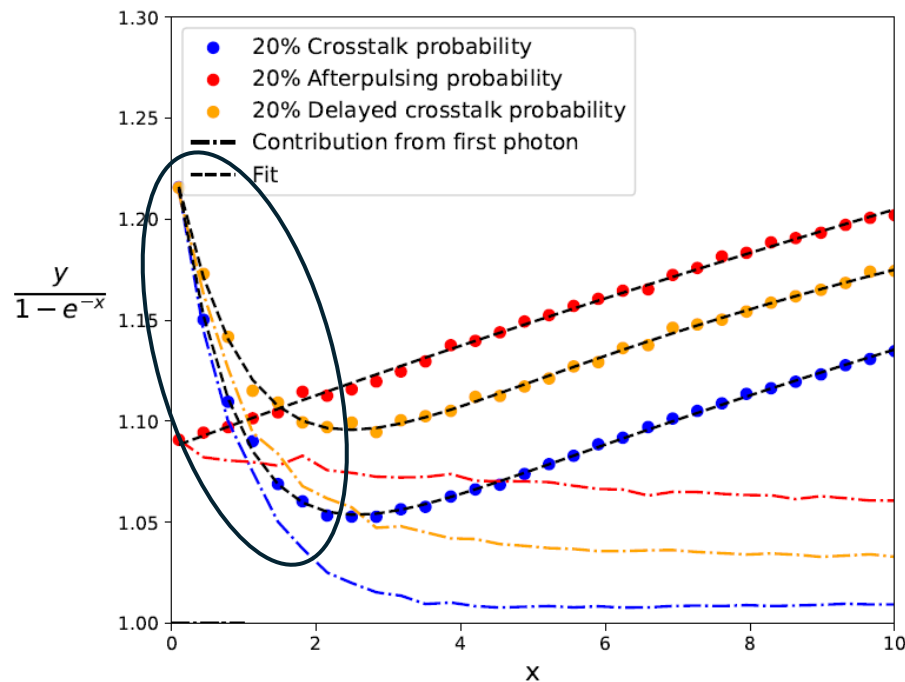
x : Expected number of avalanches per pixel

- Exponential suppression of correlated noise

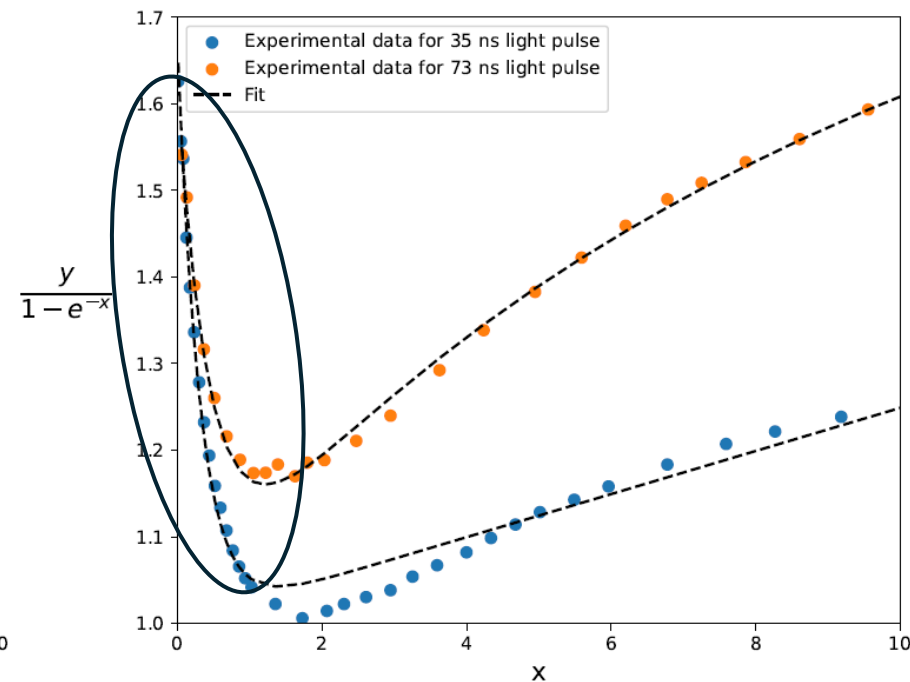
$$N(x) = c \cdot e^{-d \cdot x}$$

c and d are fitting parameters

Simulated data



Experimental data



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y : Number of full avalanches per pixel

x : Expected number of avalanches per pixel

- Different response to different pulse shapes:

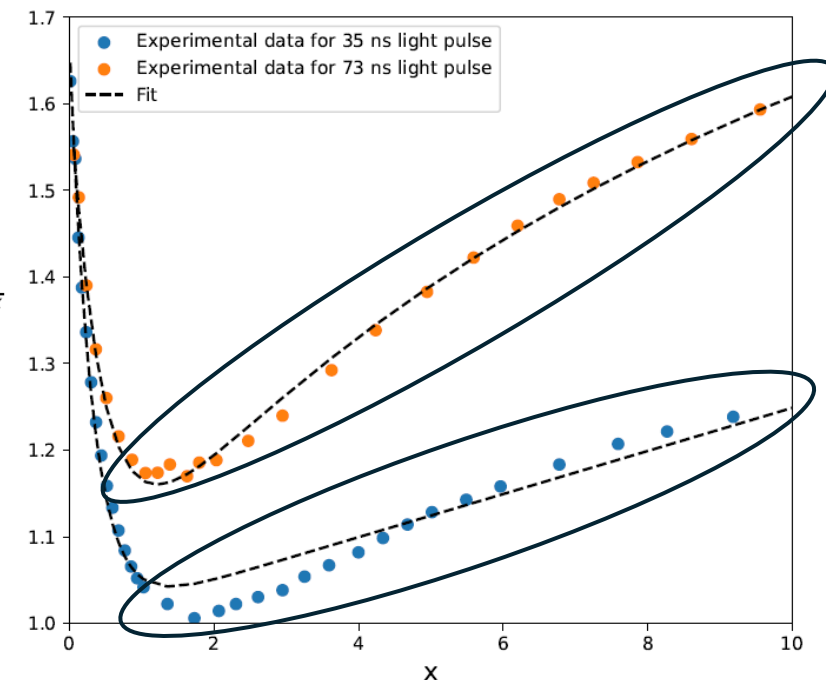
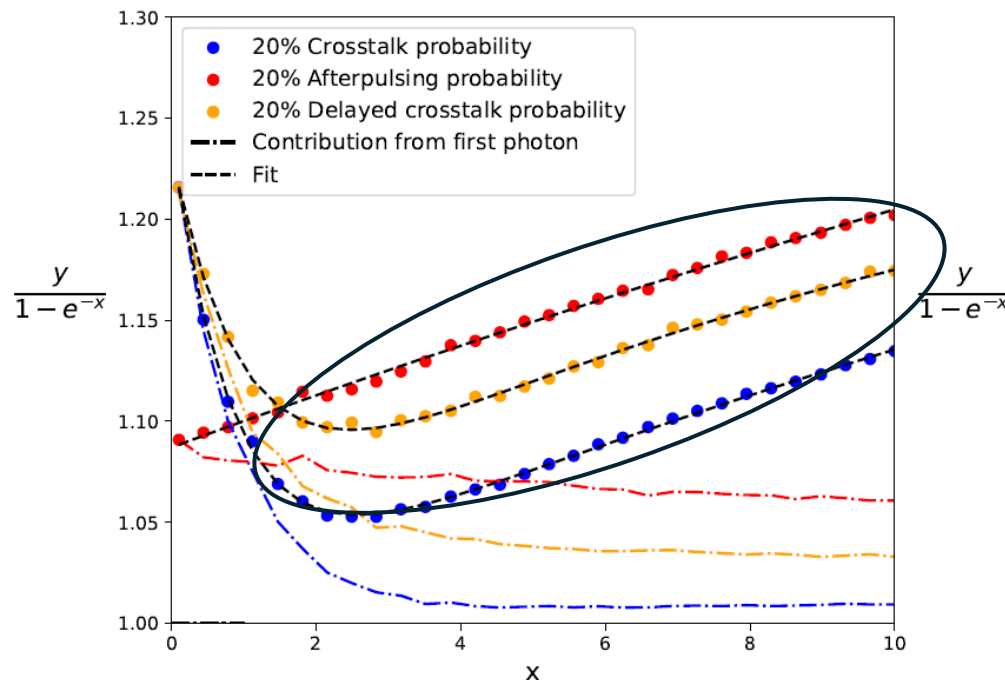
➤ Long tailed pulses: $R(x) = a \cdot \ln(1 + b \cdot x)$

Both models are equivalent for $x \lesssim 10$

➤ Finite pulses: $R(x) = \frac{a \cdot x}{1 + b \cdot x}$

$$R(x) \propto x$$

Results for rectangular LED pulses



Fitting model

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$$y = (1 + N(x) + R(x)) \cdot (1 - e^{-x})$$

y : Number of full avalanches per pixel

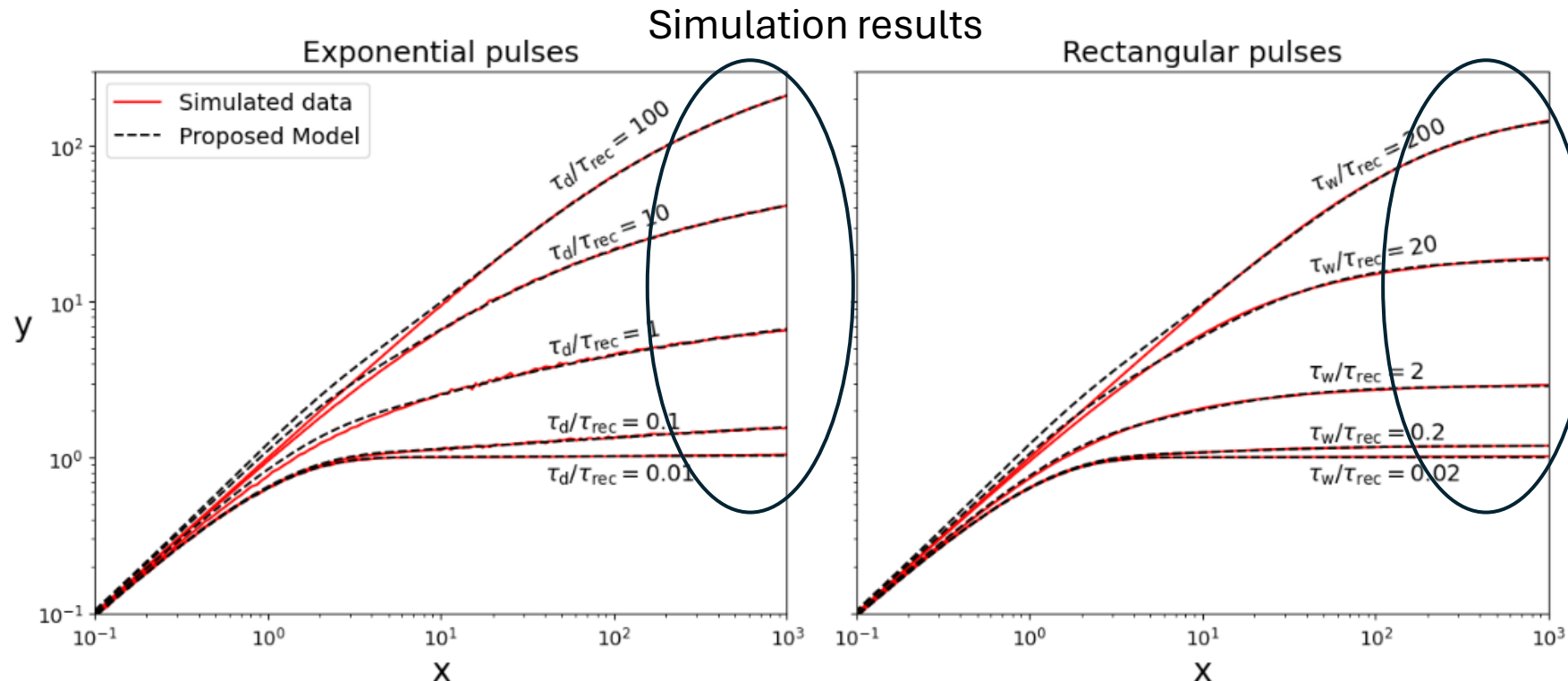
x : Expected number of avalanches per pixel

- Different response to different pulse shapes:

➤ Long tailed pulses: $R(x) = a \cdot \ln(1 + b \cdot x)$

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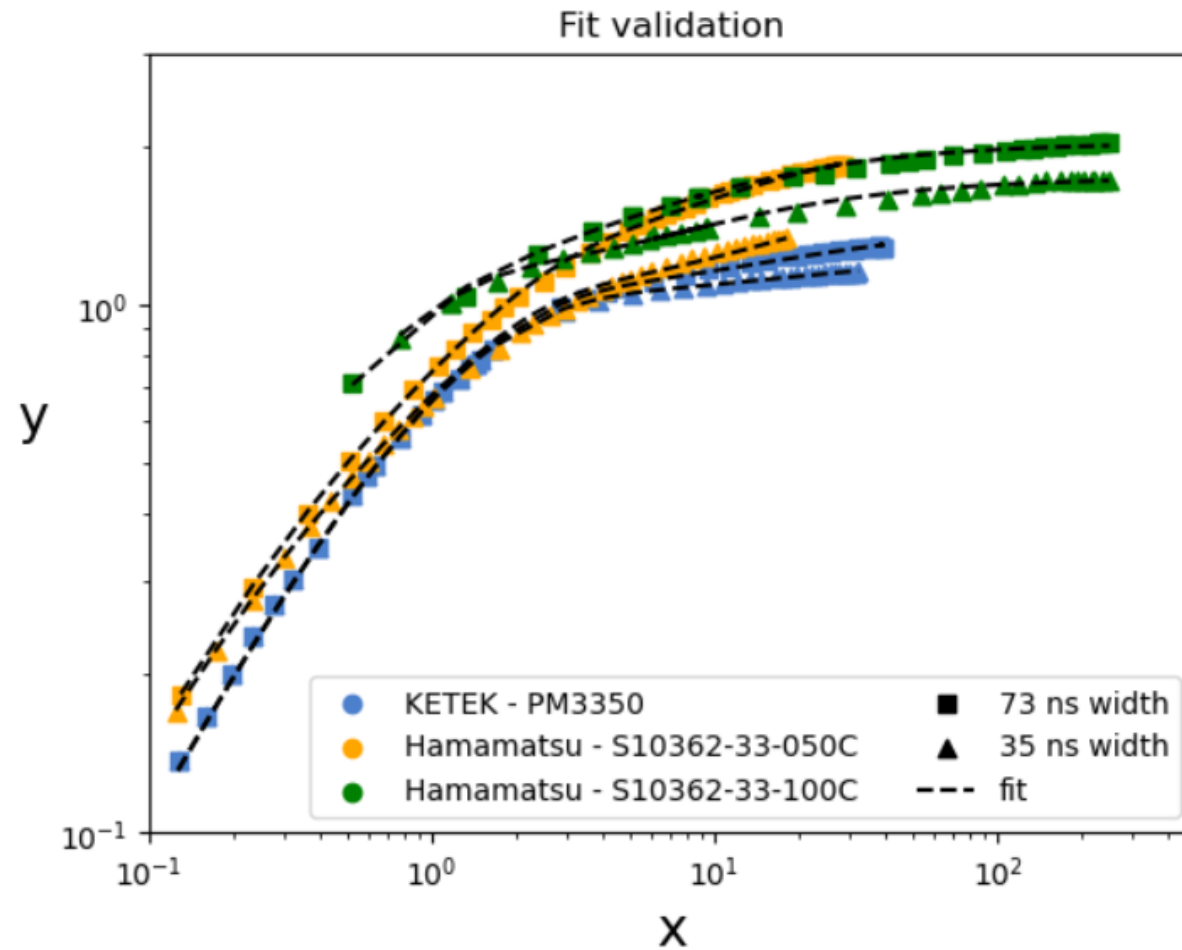
The models reproduce the asymptotic behavior at very large x
 a and b are fitting parameters



Previous models fail at large x

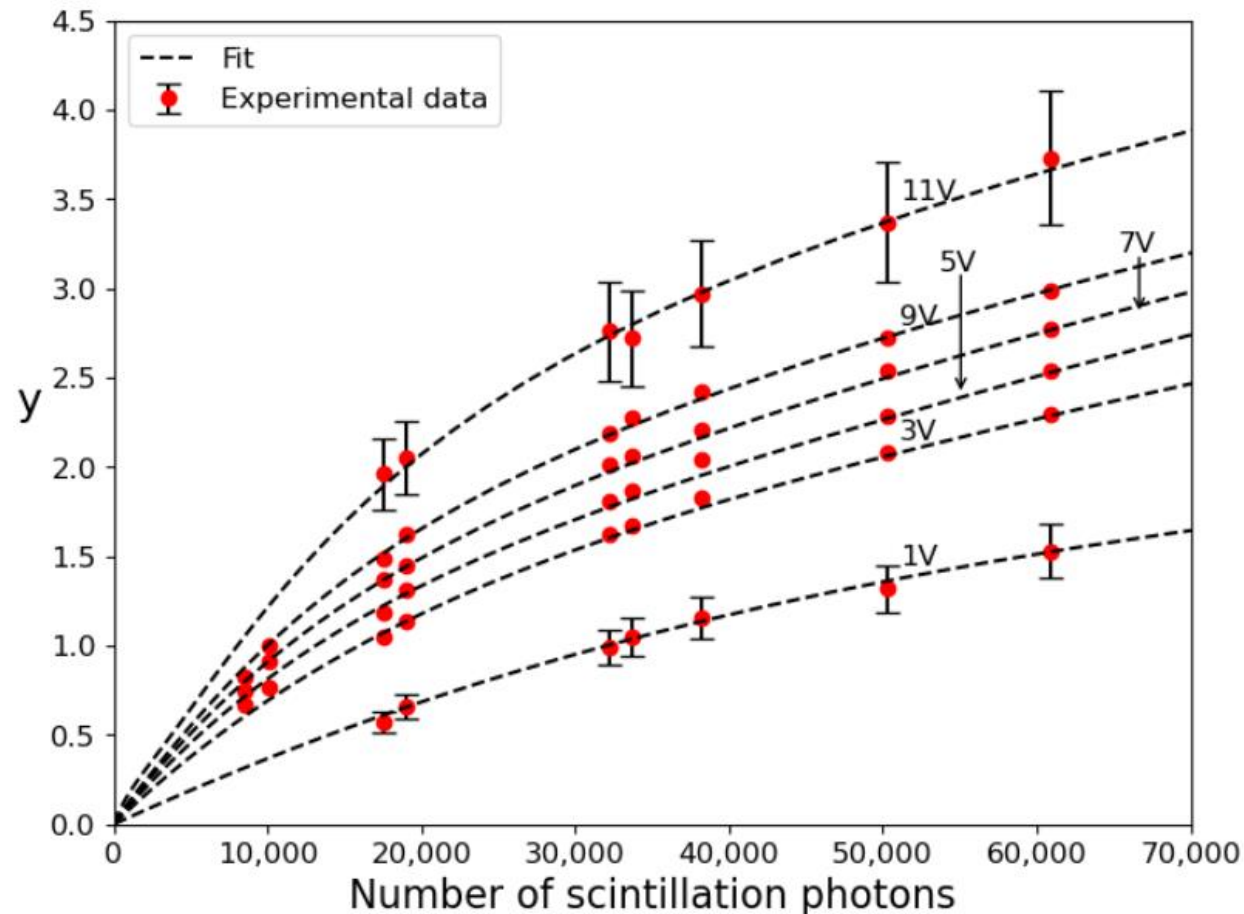
Model validation

- Model validated against experimental data for different SiPMs and pulse widths for from *Bretz, T et al. JINST 2016, 11, P03009*
- Residuals smaller than 5% in a very large range of light pulse intensities



Example of a scintillator detector

- LYSO(Ce)+Hamamatsu S13360-1350CS exposed to gamma rays from 300 to 2100 keV (^{22}Na , ^{60}Co , ^{137}Cs and ^{226}Ra)
- Residuals smaller than experimental errors (10%) in all the energy range



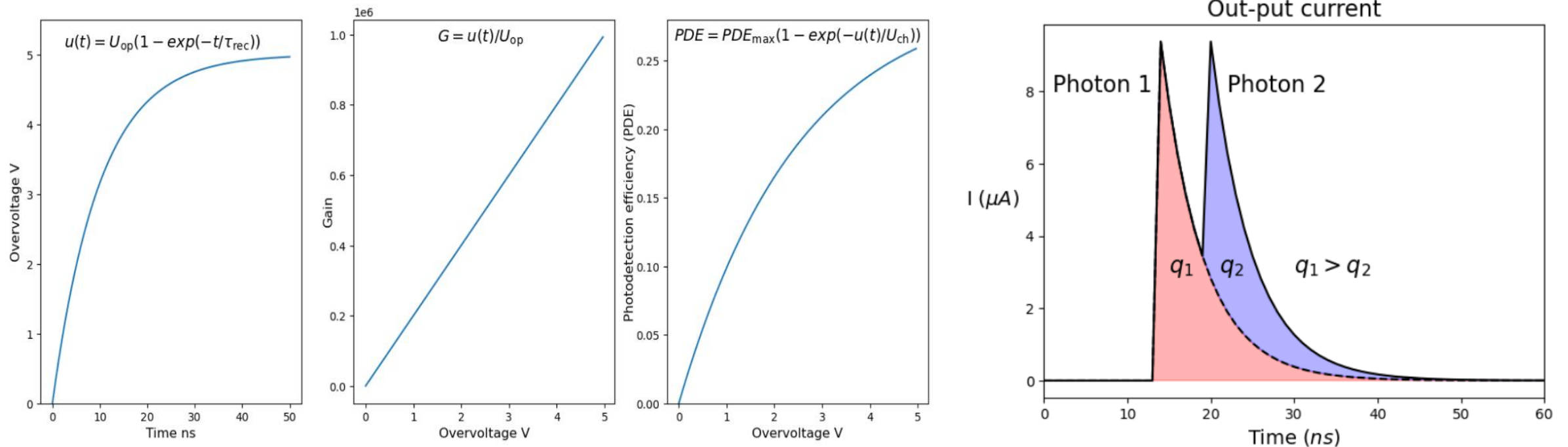
Conclusions and future plans

- SiPMs are photonsensors with excellent properties, but their use in scintillation detectors is limited by their nonlinear response
- A systematic study of the SiPM nonlinear response and its causes was performed by means of Monte Carlo simulations
- We propose a simple fitting model depending on 4 fitting parameters that reproduce both simulated and experimental data for light pulses of arbitrary shape and intensity
- Using our model may allow extending the dynamic range of scintillation detectors
- We plan to study in detail nonlinear effects on the output pulse signal as well as on the energy resolution

Back-up slides

SiPM recovery

- After a charge avalanche in a microcell its overvoltage drops to 0 and starts recovering
- PDE and Gain also drop to 0.
- The charge created by a charge avalanche in a recovering pixel will be smaller
- If there is a significant number of unrecovered avalanches the response will not be linear



SiPM Read-out resistance effect

- Although the read-out resistance is usually small it has an important effect
- It adds a fast component to the SiPM response
- The net effect is to lower the output charge

