

Hirschfest, Valencia, January 24 2024

# The minimally flipped “you-know-what”

Michal Malinský

IPNP, Charles University in Prague

based on [arXiv:2312.08357](https://arxiv.org/abs/2312.08357) [hep-ph]

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Thou shalt be careful about vanilla “you-know-what”  
because almost anything is possible there, the correct  
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PHYSICAL REVIEW D **75**, 011701(R) (2007)

### Thermal leptogenesis in extended supersymmetric seesaw model

M. Hirsch<sup>\*</sup> and J. W. F. Valle<sup>†</sup>

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U. Sarkar<sup>||</sup>

*Physical Research Laboratory, Ahmedabad 380 009, India*

(Received 10 August 2006; published 29 January 2007)

We consider an extended supersymmetric SO(10) seesaw model with only doublet Higgs scalars, in which neutrino masses are suppressed by the scale of  $D$ -parity violation. Leptogenesis can occur at the TeV scale through the decay of a singlet  $\Sigma$ , thereby avoiding the gravitino crisis. Washout of the asymmetry can be effectively suppressed by the absence of direct couplings of  $\Sigma$  to leptons.

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# A bit of HEP-centric etymology & a pictogram

## Leptogenesis

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Lep togenesis

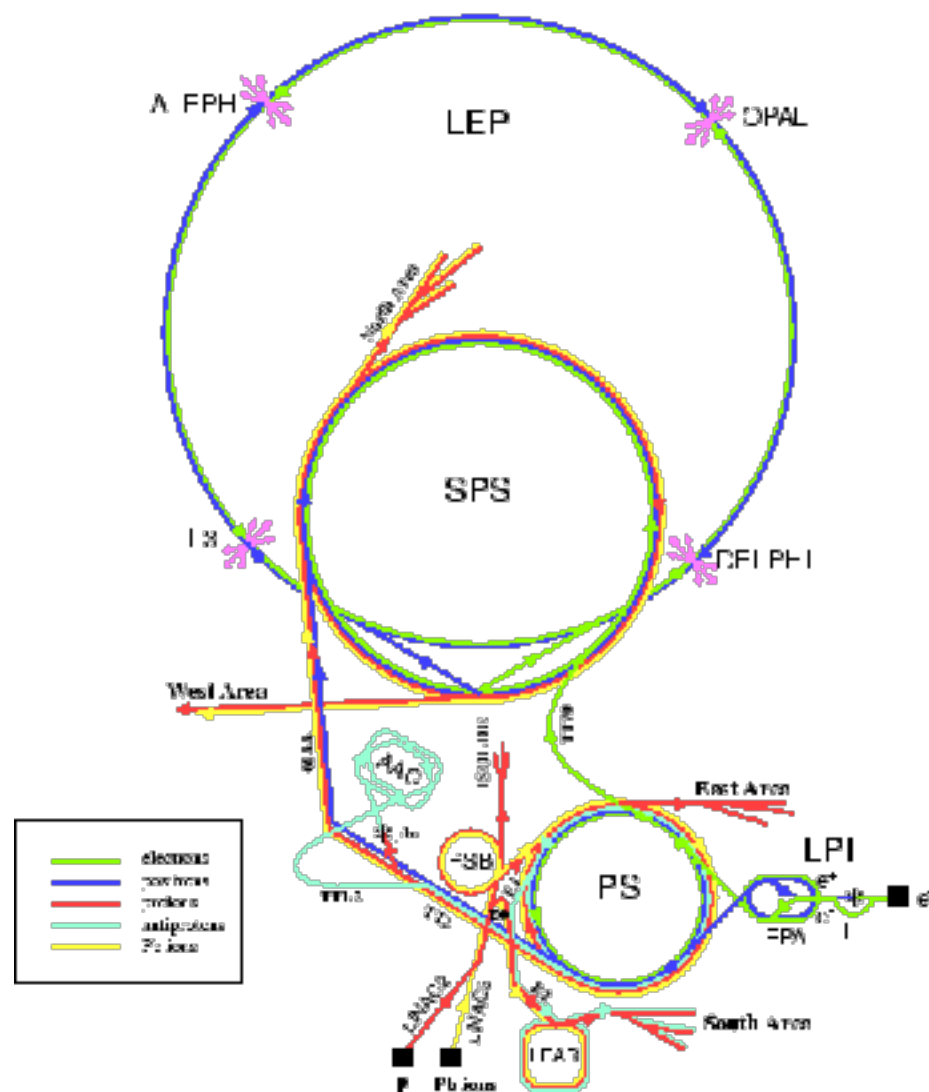
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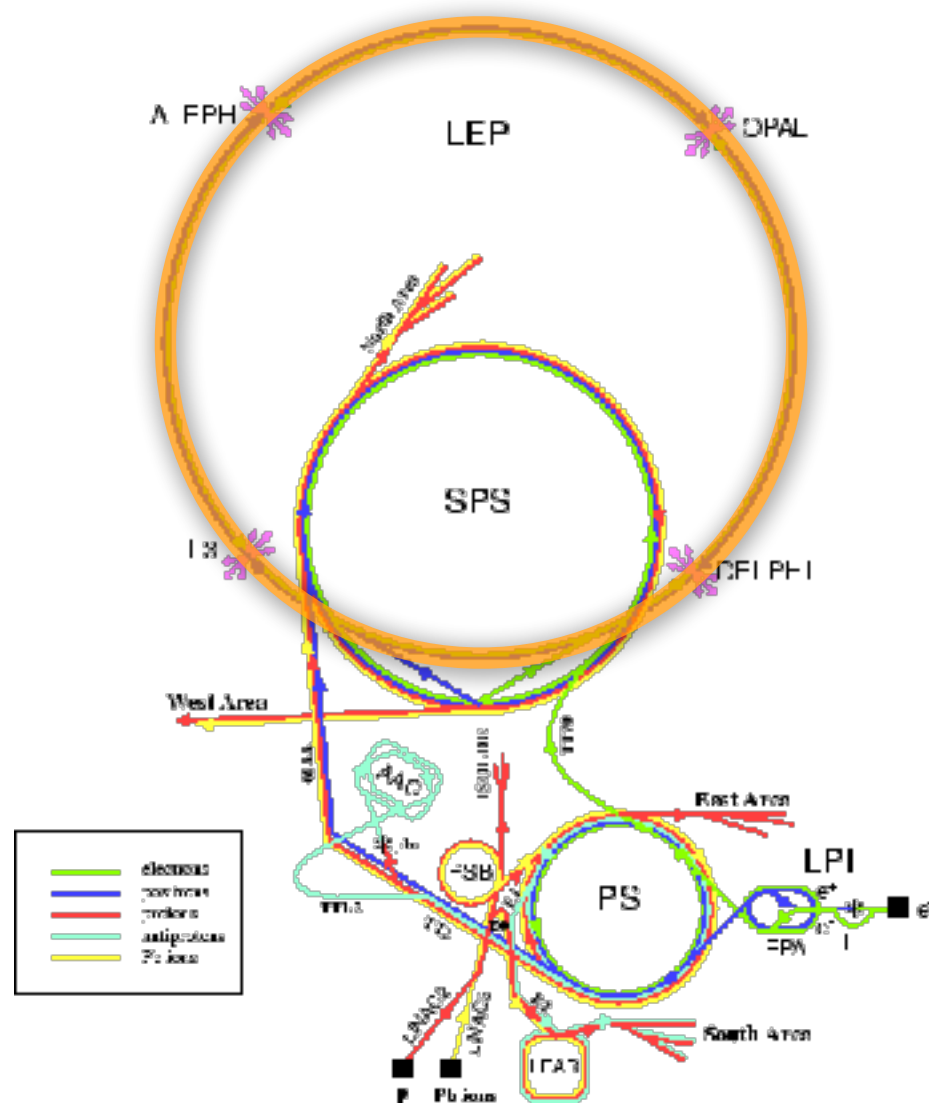
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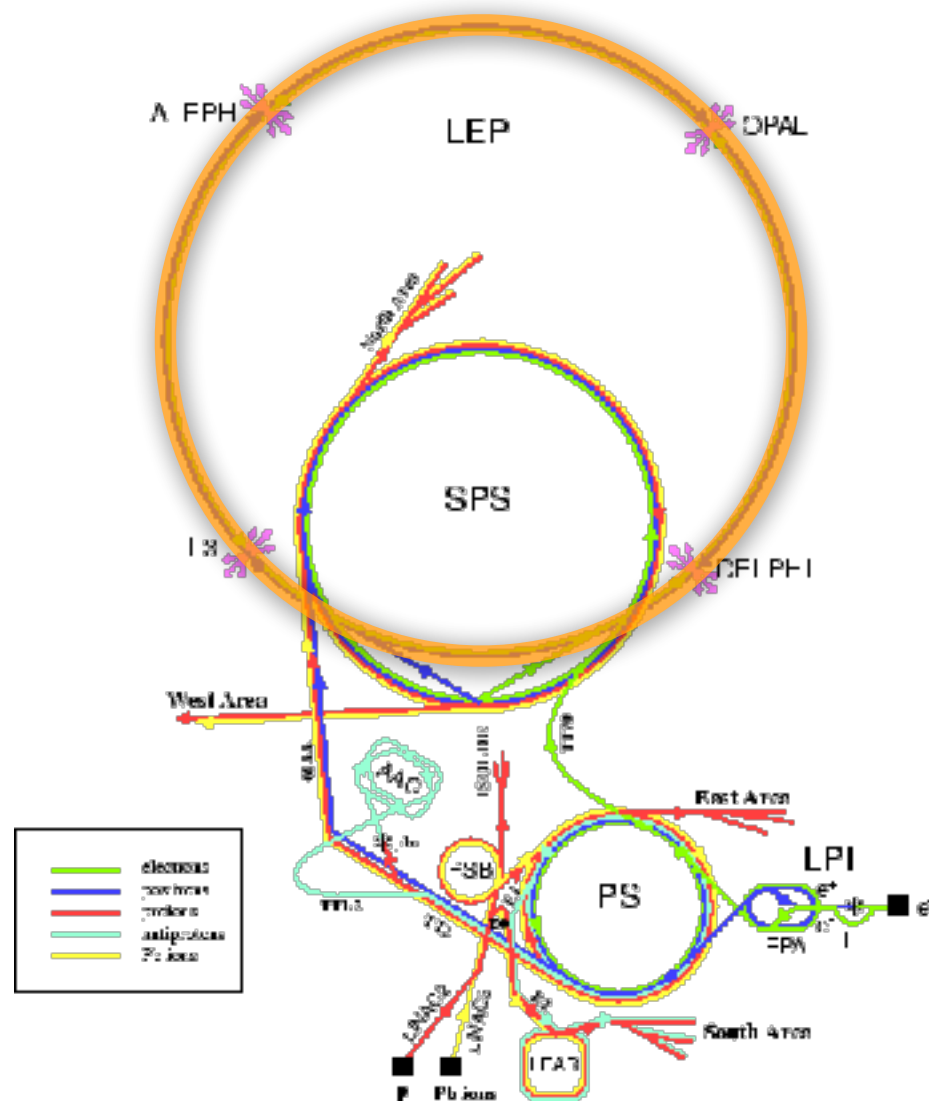
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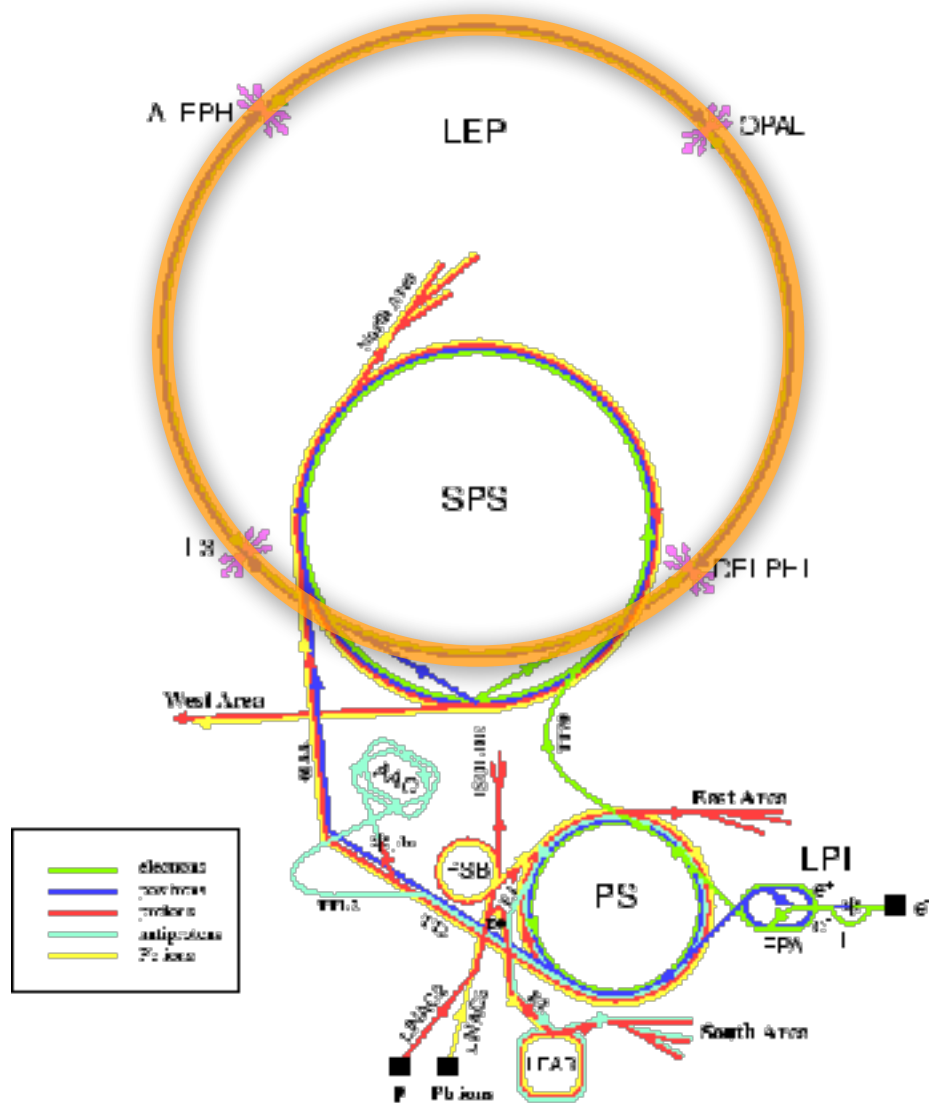
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## LEP to genesis



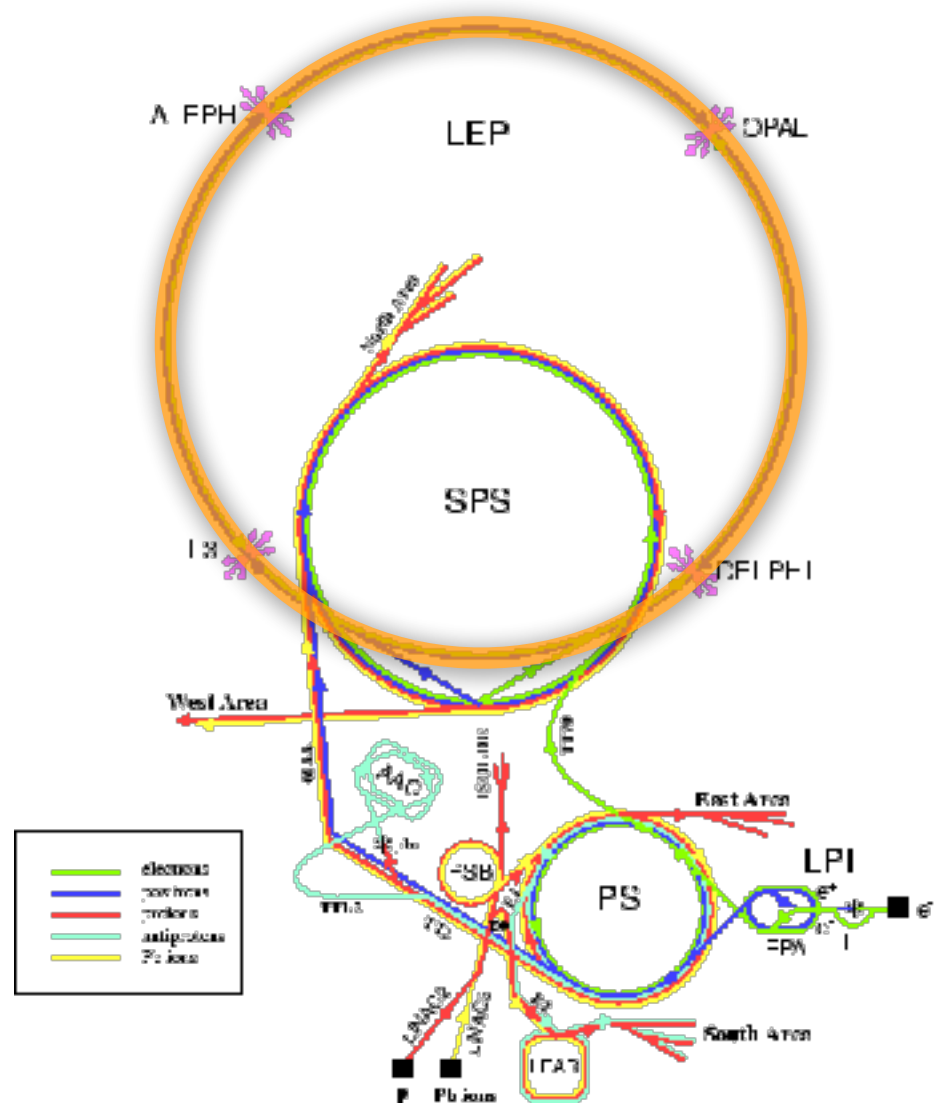
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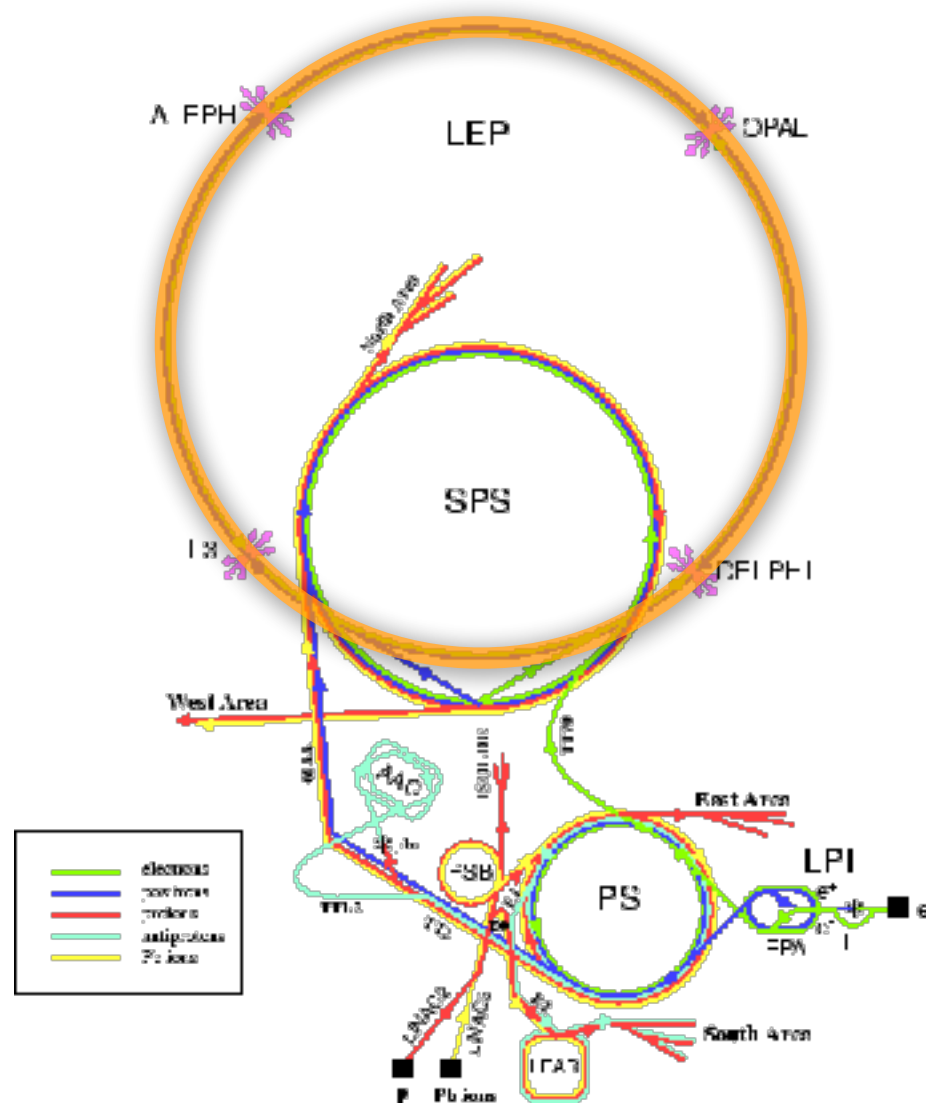
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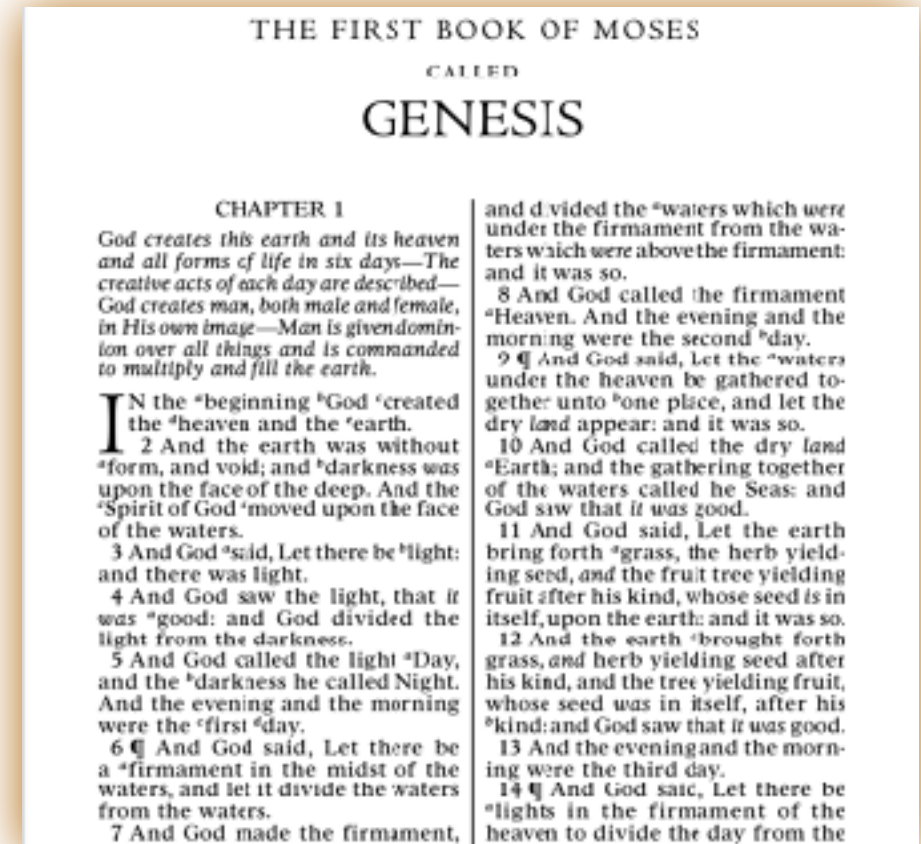
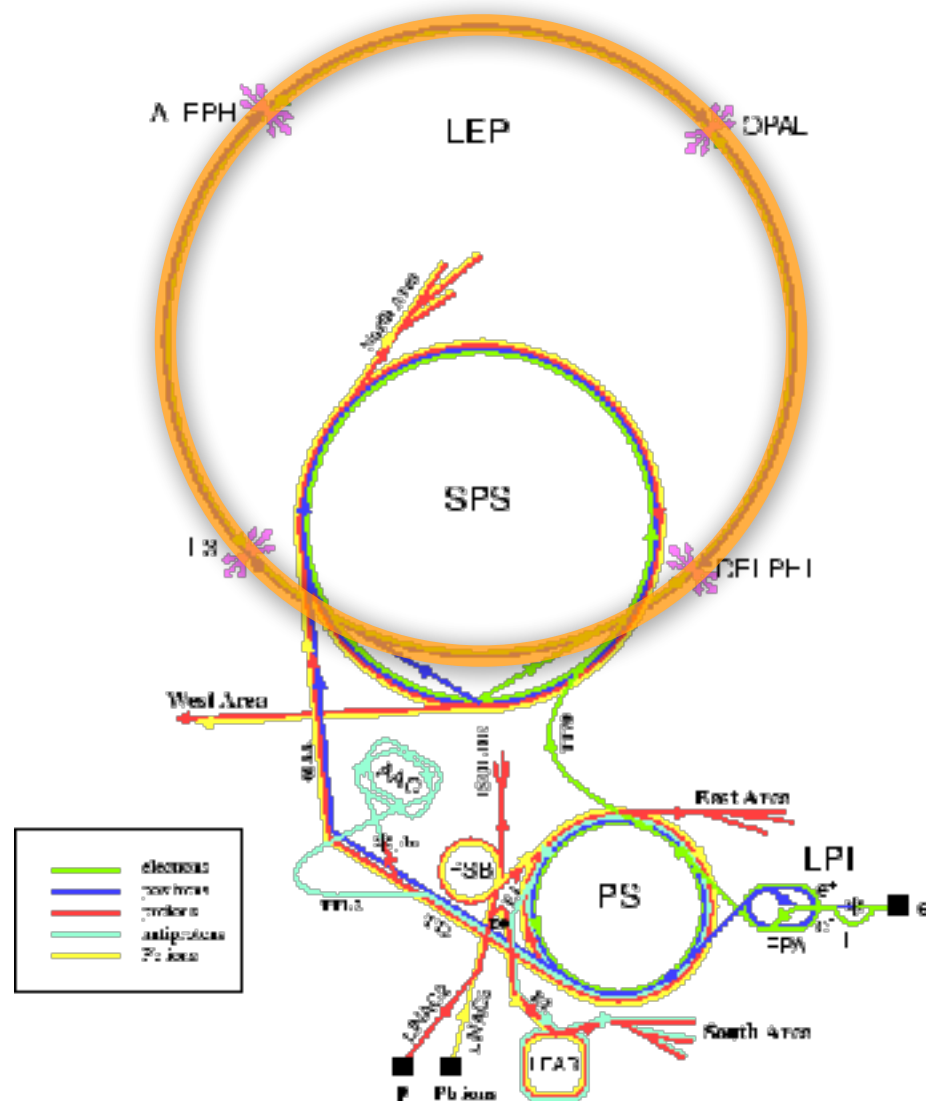
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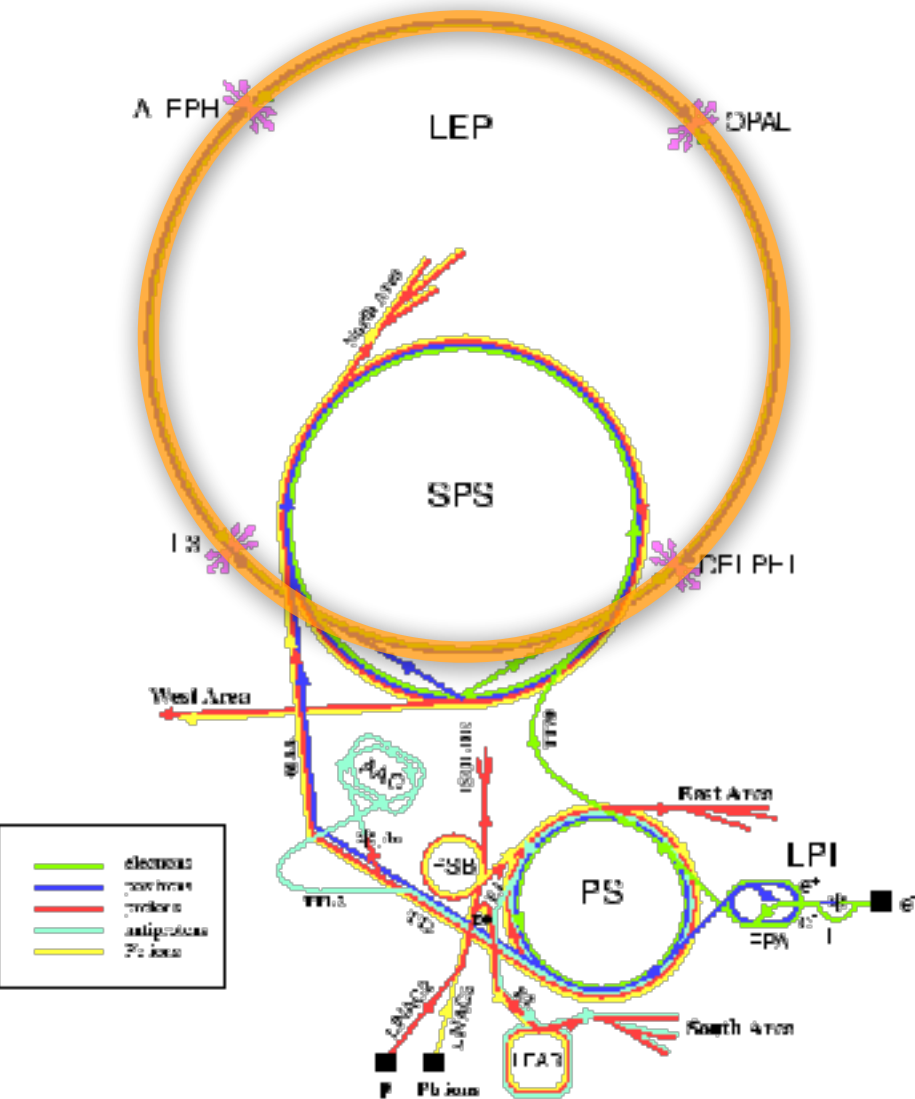
## LEP TO GENESIS





# A bit of HEP-centric etymology & a pictogram

## LEP TO GENESIS



THE FIRST BOOK OF MOSES  
CALLED  
GENESIS

CHAPTER 1

God creates this earth and its heaven and all forms of life in six days—The creative acts of each day are described—God creates man, both male and female, in His own image—Man is given dominion over all things and is commanded to multiply and fill the earth.

**I**N the "beginning" God "created" the "heaven and the "earth."

2 And the earth was without "form, and void; and "darkness was upon the face of the deep. And the "Spirit of God "moved upon the face of the waters.

3 And God "said, Let there be "light: and there was light.

4 And God saw the light, that it was "good: and God divided the light from the darkness.

5 And God called the light "Day, and the "darkness he called Night. And the evening and the morning were the "first "day.

6 ¶ And God said, Let there be a "firmament in the midst of the waters, and let it divide the waters from the waters.

7 And God made the firmament,

and divided the "waters which were under the firmament from the waters which were above the firmament: and it was so.

8 And God called the firmament "Heaven. And the evening and the morning were the second "day.

9 ¶ And God said, Let the "waters under the heaven be gathered together unto "one place, and let the dry land appear: and it was so.

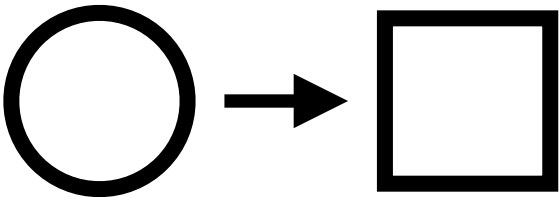
10 And God called the dry land "Earth; and the gathering together of the waters called he Seas: and God saw that it was good.

11 And God said, Let the earth bring forth "grass, the herb yielding seed, and the fruit tree yielding fruit after his kind, whose seed is in itself, upon the earth: and it was so.

12 And the earth "brought forth grass, and herb yielding seed after his kind, and the tree yielding fruit, whose seed was in itself, after his "kind: and God saw that it was good.

13 And the evening and the morning were the third day.

14 ¶ And God said, Let there be "lights in the firmament of the heaven to divide the day from the



# Making things less disturbing for Martin...

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## A trivial optimist's rearrangement:

$\eta_B$  may turn into a strong discriminator if further constraints on Yukawas  
and/or neutrino spectral shape are at place (top-down)

# Take-home message

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**The minimal unified model with flipped hypercharge assignment  
is a perfect illustration of this!**

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The minimal flipped  $\bigcirc \rightarrow \square$

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based on [arXiv:2312.08357 \[hep-ph\]](#)

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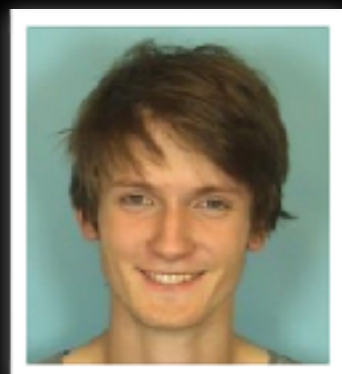
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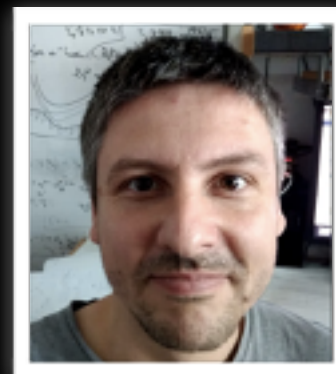
starring :



Václav Miřátský

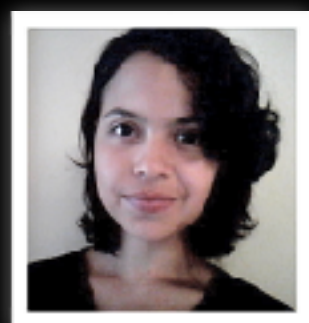


Renato Fonseca

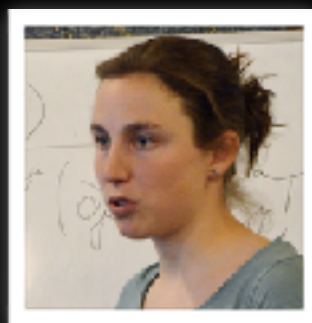


Martin Zdráhal

co-starring :



C. Arbelaez Rodriguez



H. Kolečová



D. Harries



based on arXiv:2312.08357 [hep-ph] , Phys.Rev. D98, 095015 (2018) and Phys.Rev. D89, 055003 (2014)



# Flipped SU(5) one-minute crash course

$$SO(10) \supset SU(5) \times U(1)_Z$$

**Matter:**  $16_M \ni (10, +1)_M \oplus (\bar{5}, -3)_M \oplus (1, +5)_M$

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2 possible  $Y_{\text{SM}}$  assignments:

**Standard:**  $Y = T_{24}$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \\ u^c, Q, e^c & d^c, L & \nu^c \end{array}$$

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**Symmetry breaking:**  $16_H \ni (10, +1)_H$   
 $10_H \ni (5, -2)_H$

SU(5)  $\times$  U(1) to the SM

SM to the QCD  $\times$  QED

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**Gauge sector:**

$$45_G \ni (24, 0)_G \oplus (1, 0)_G \ni \overset{X', Y'}{(3, 2, -\frac{1}{6})}_G + h.c.$$



# BLNV nucleon decays in flipped SU(5) - one $U_\nu$ rules them all

$$\begin{array}{llll}\Gamma(p \rightarrow \pi^0 \ell_\alpha^+) & \Gamma(p \rightarrow \pi^+ \bar{\nu}) & \Gamma(n \rightarrow \pi^- \ell_\alpha^+) & \Gamma(n \rightarrow \pi^0 \bar{\nu}) \\ \Gamma(p \rightarrow K^0 \ell_\alpha^+) & \Gamma(p \rightarrow K^+ \bar{\nu}) & \Gamma(n \rightarrow K^- \ell_\alpha^+) & \Gamma(n \rightarrow K^0 \bar{\nu}) \\ \Gamma(p \rightarrow \eta \ell_\alpha^+) & & & \Gamma(n \rightarrow \eta \bar{\nu})\end{array}$$

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**Charged mesons:**  
(no flavour ambiguity!)

$$\Gamma(p \rightarrow K^+ \bar{\nu}) = 0$$

$$\Gamma(p \rightarrow \pi^+ \bar{\nu}) = \left( \frac{g_G}{M_G} \right)^4 \frac{m_p}{8\pi f_\pi^2} A_L^2 |\alpha|^2 (1 + D + F)^2$$

Nath, Fileviez-Perez, Phys.Rept.441

Dorsner, Fileviez-Perez, PLB605

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**Neutral mesons:**

$$\Gamma(p \rightarrow \pi^0 \ell_\alpha^+) = \frac{1}{2} \Gamma(p \rightarrow \pi^+ \bar{\nu}) |(V_{CKM})_{11}|^2 |(V_{PMNS} U_\nu)_{\alpha 1}|^2$$

$$m_\nu = U_\nu^T D_\nu U_\nu$$

Constraining  $U_\nu$  yields **constraints for ALL 2-body BNV channels!!!**

# RH neutrino masses in the flipped SU(5)

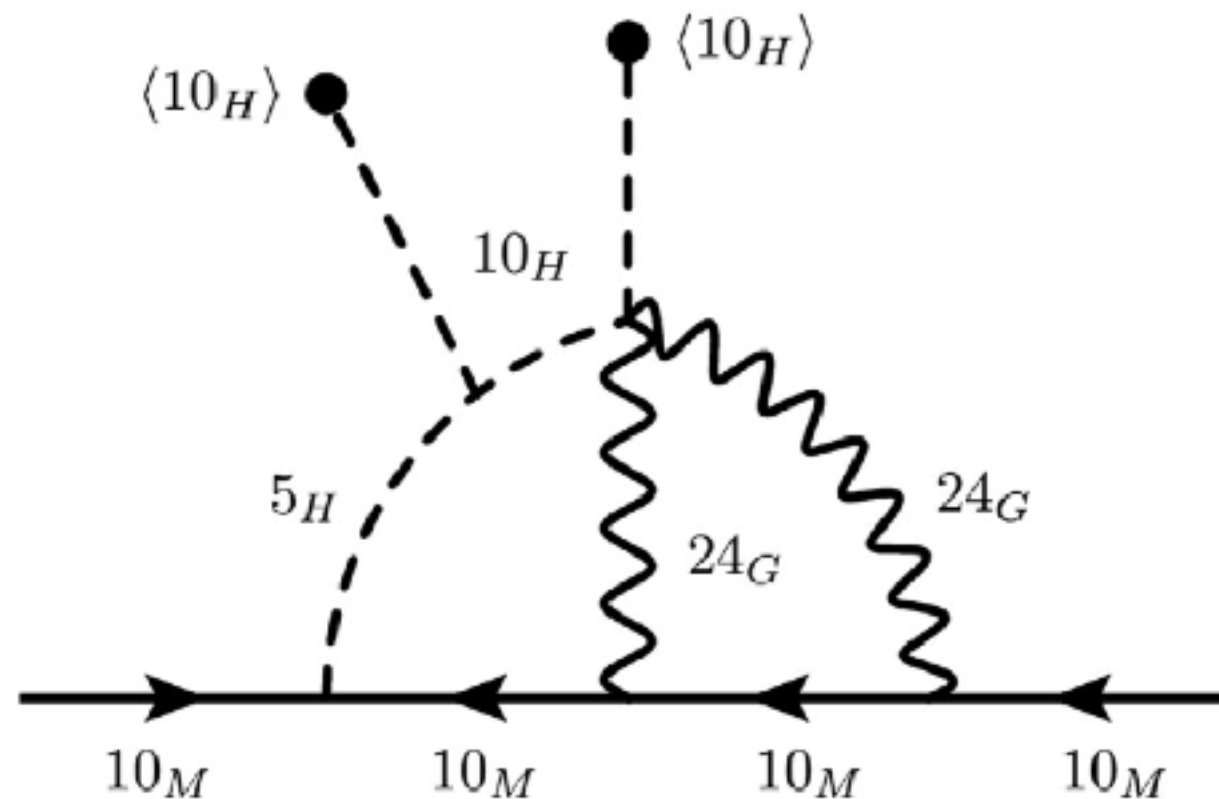
Tree level:  $10_M Y_{50} 10_M \langle 50_H \rangle$       OK in principle but overkill

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Witten's loop option:

C.Arbelaez-Rodriguez, H. Kolečová, MM PRD89 (2014)



NB first brief mention of this option in flipped SU(5) : Leontaris, Vergados, PLB 258 (1991)

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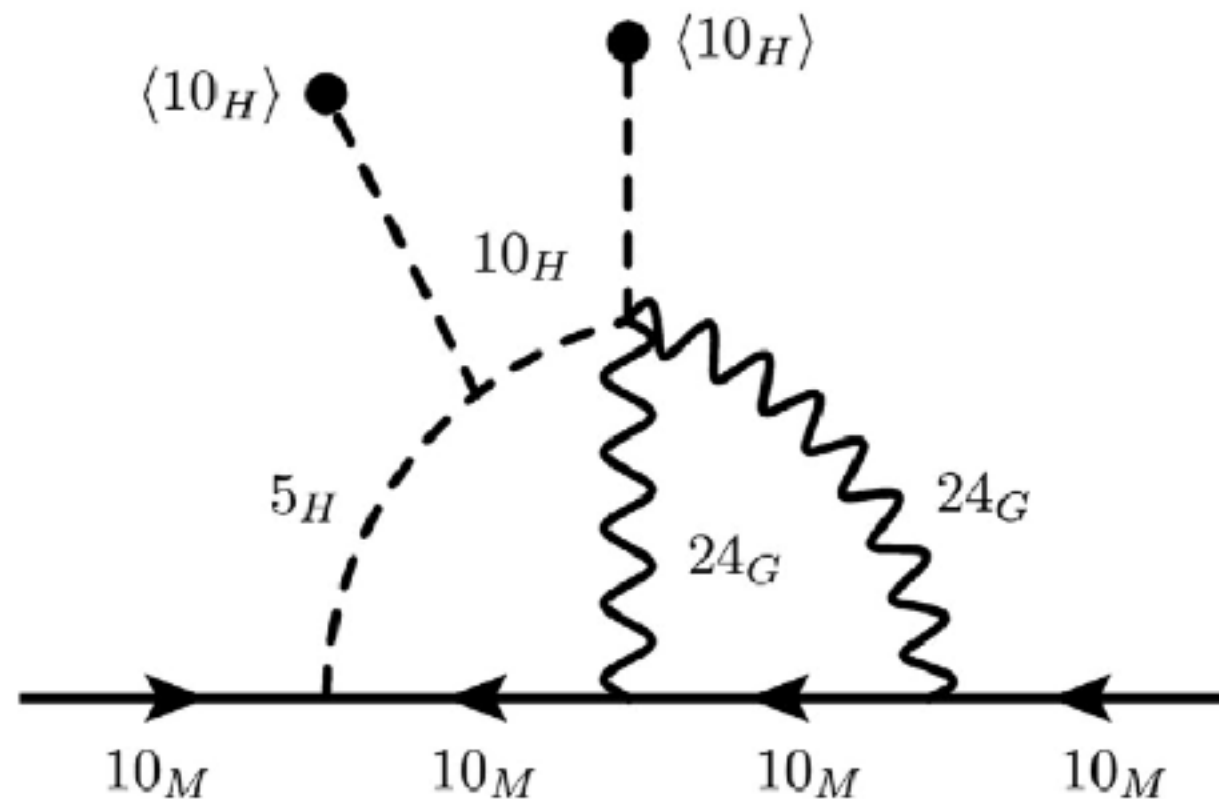


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# The Witten's loop

## NEUTRINO MASSES IN THE MINIMAL $O(10)$ THEORY <sup>☆</sup>

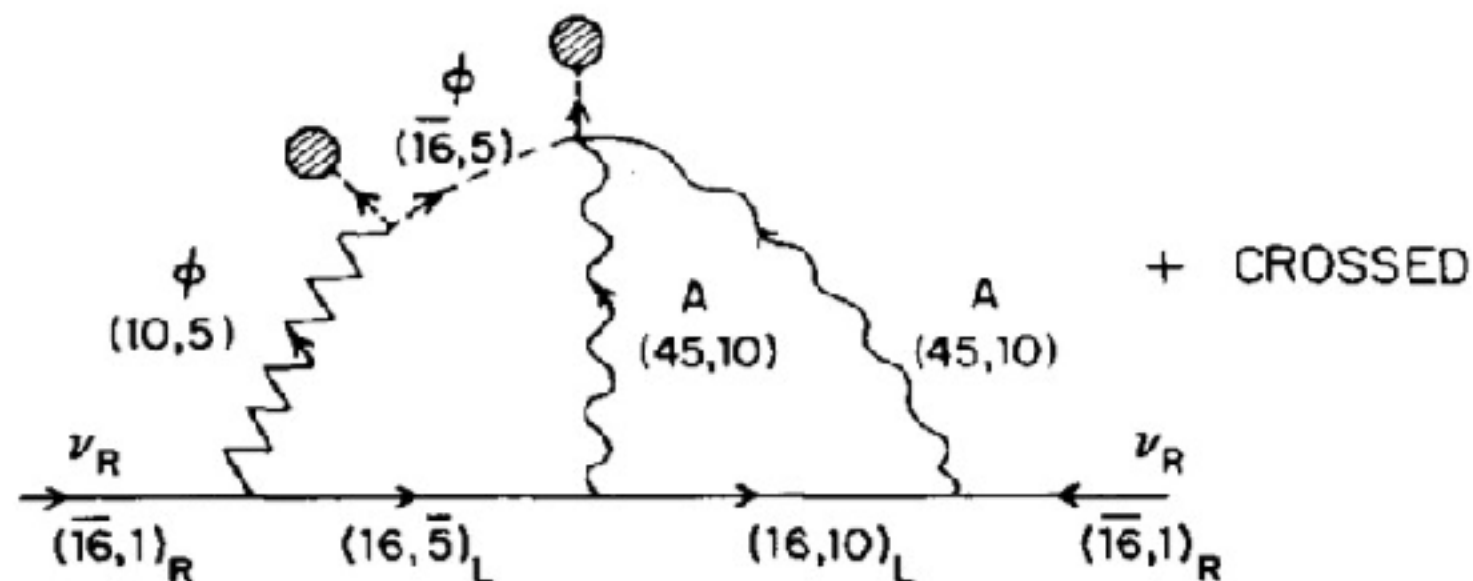
Phys. Lett. B91 (1980) 81

Edward WITTEN <sup>1</sup>

Lyman Laboratory of Physics, Harvard University, Cambridge, MA 02138, USA

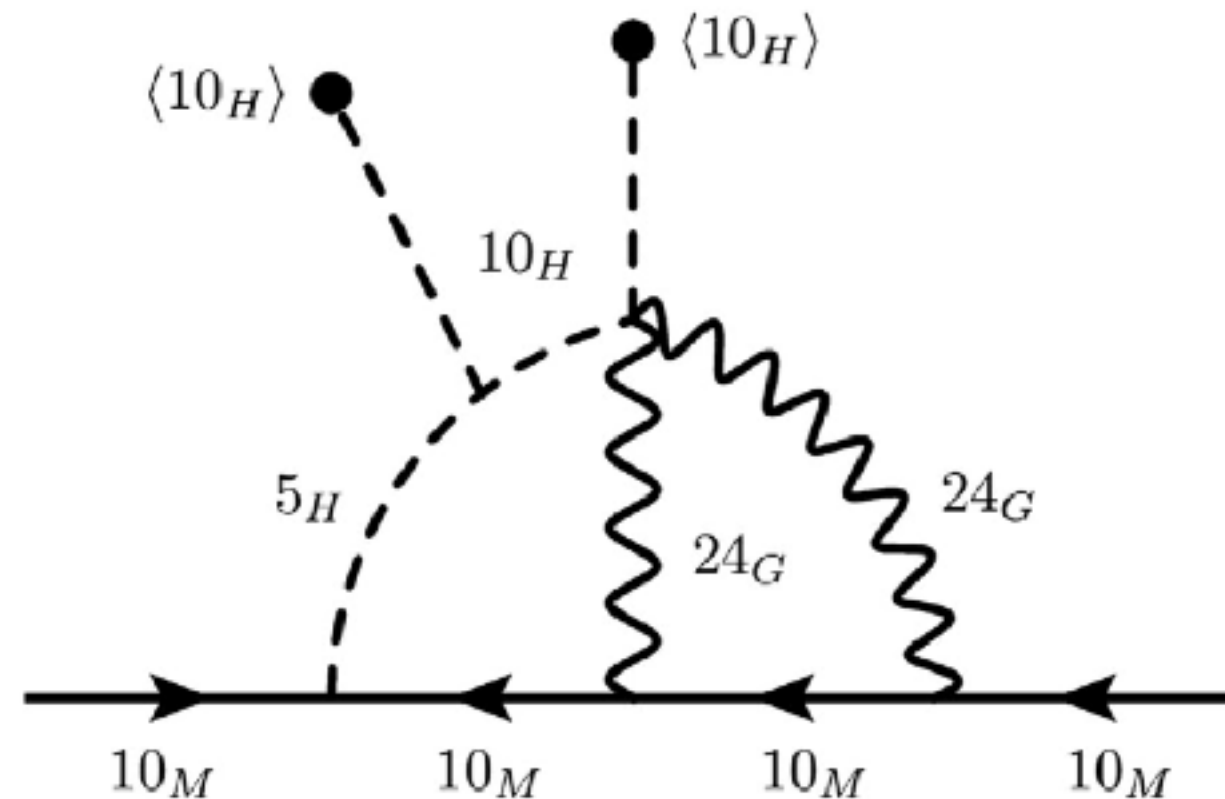
Received 6 December 1979

Neutrino masses are discussed in the context of the  $O(10)$  grand unified theory. In the “minimal” form of this theory, with minimal Higgs and fermion content, the right-handed neutrinos acquire masses at the two loop level. The left-handed neutrino masses are correspondingly *larger* by a factor roughly  $(\alpha/\pi)^{-2}$  than they would be if the right-handed neutrino could acquire mass at the tree level. In the simplest form of this theory, the neutrino mass matrix is proportional to the up quark mass matrix, and the neutrino mixing angles equal the usual Cabibbo angles. The neutrino masses will be roughly in the range  $10^{0\pm 2}$  eV depending on the strength of  $O(10)$  symmetry breaking, and on certain unknown ratios of masses and couplings of superheavy particles.



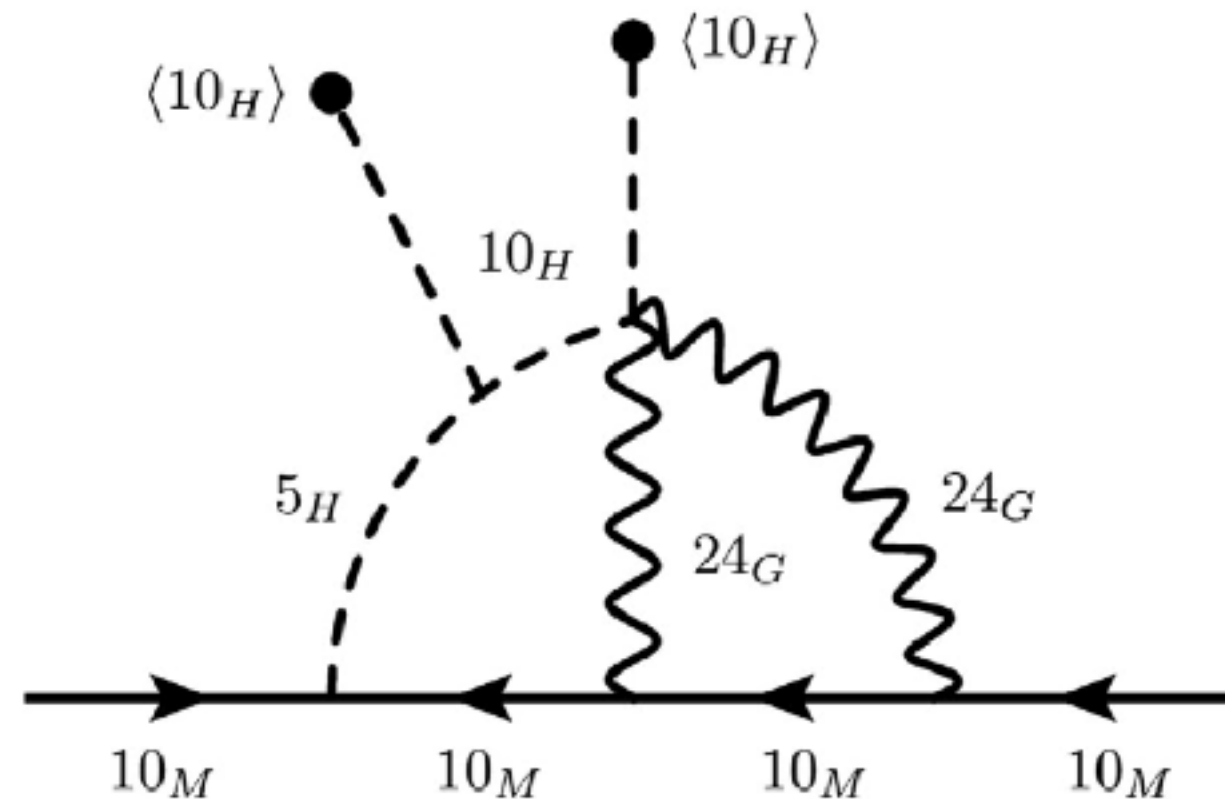
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Flipped SU(5) Witten's loop anatomy: C.Arbelaez-Rodriguez, H. Kolečová, MM PRD89(2014)



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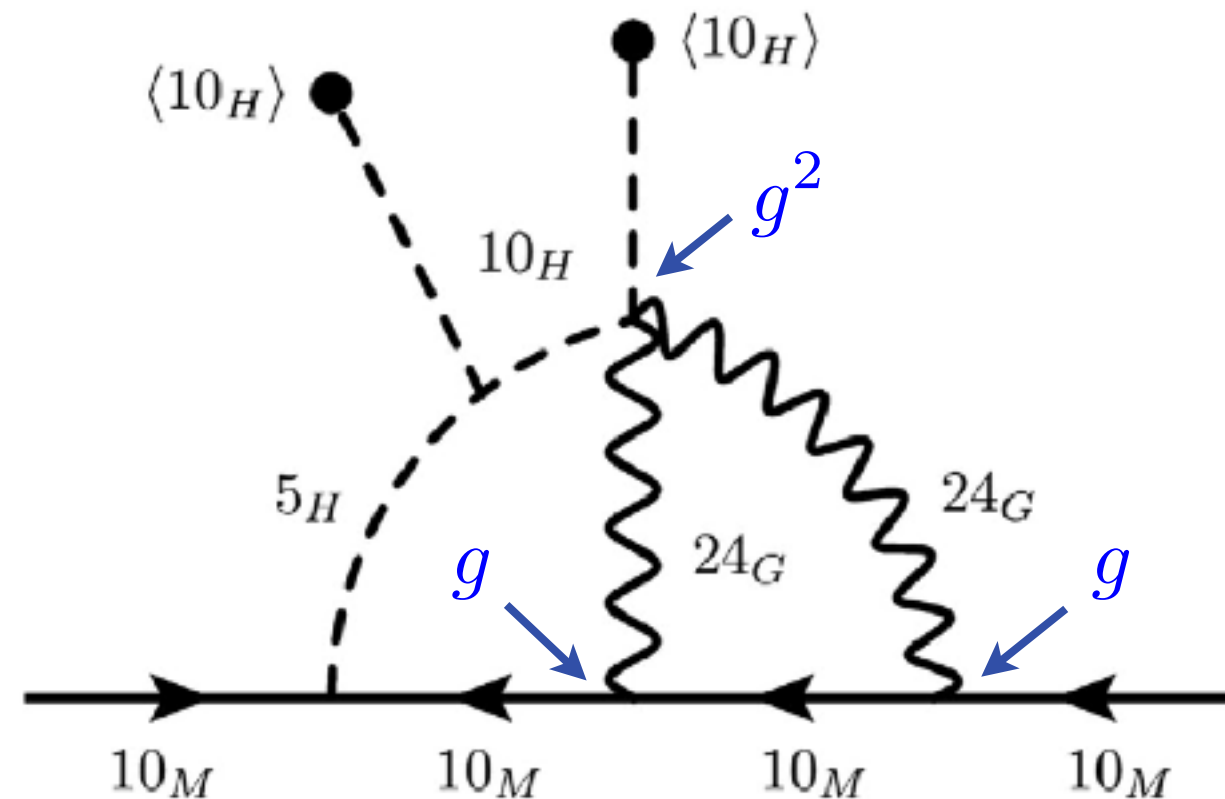
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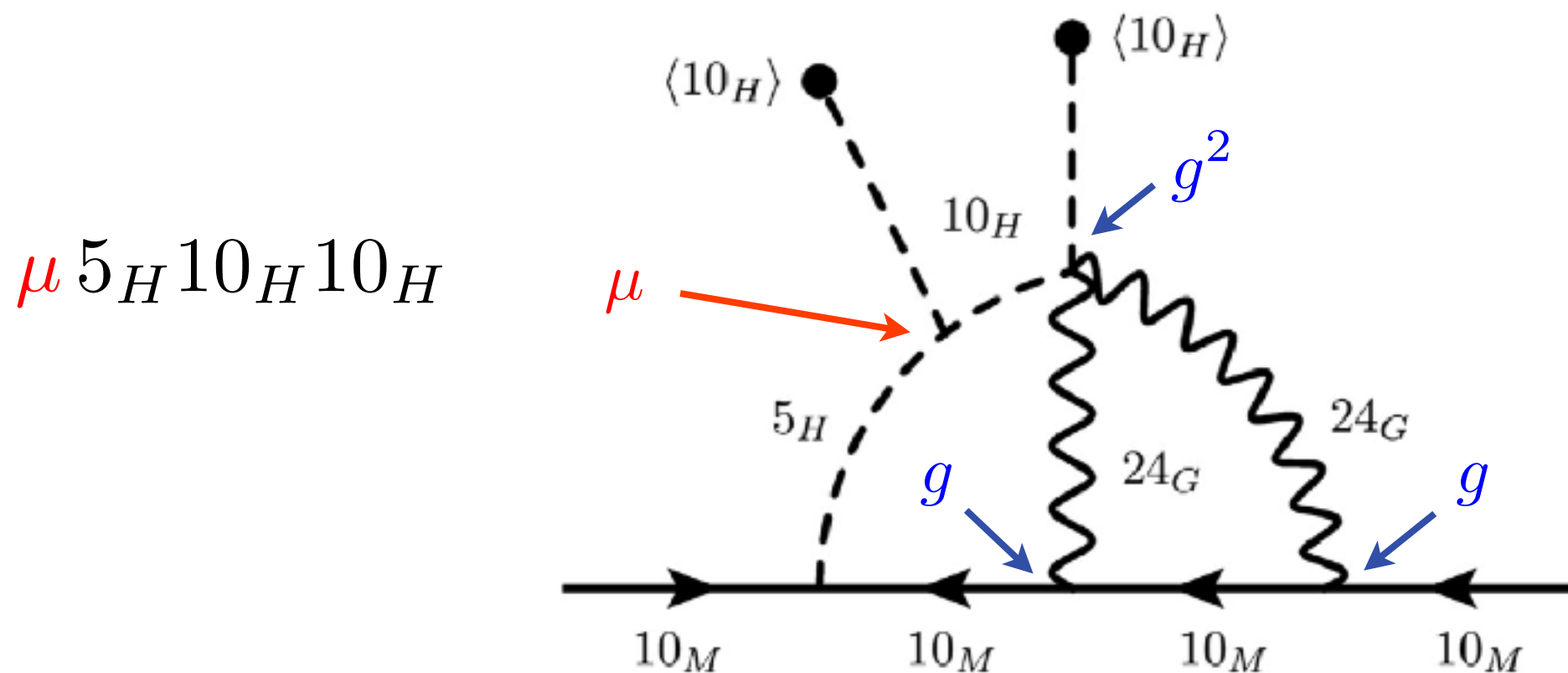
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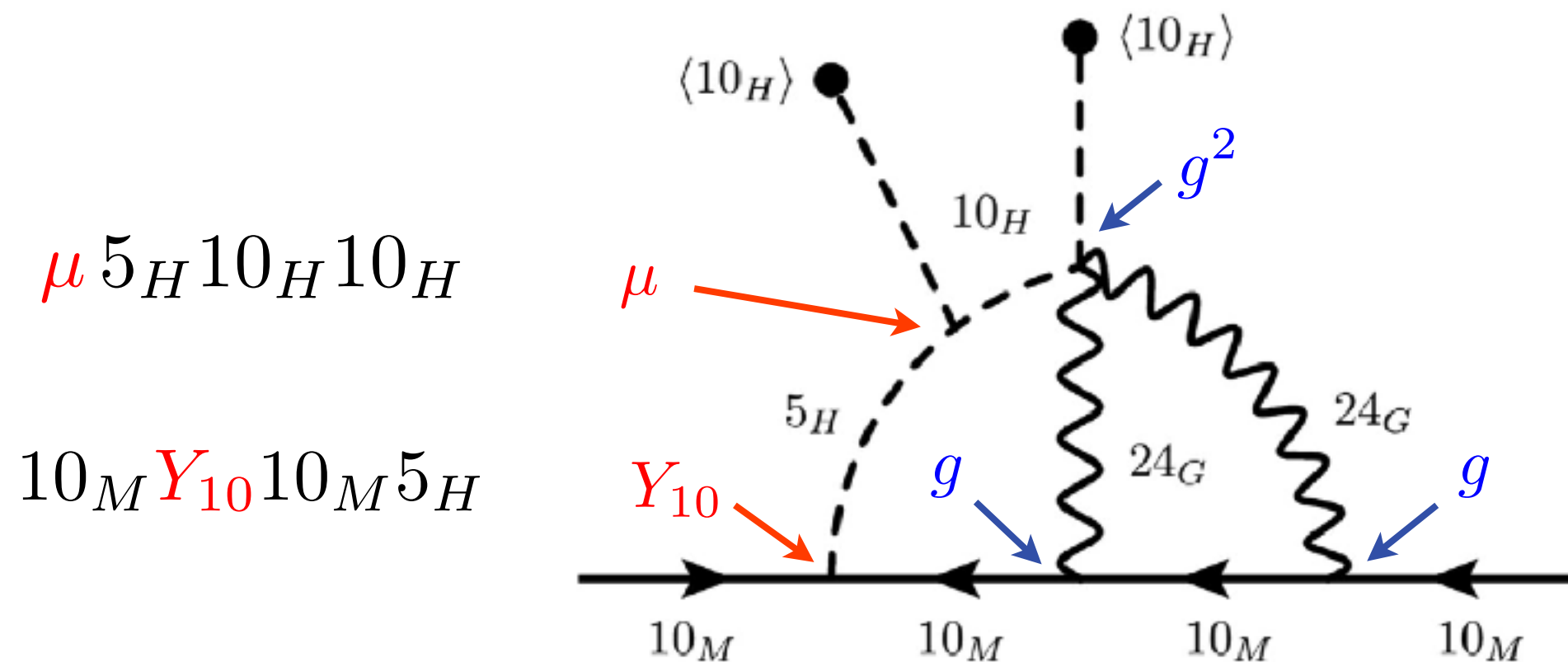
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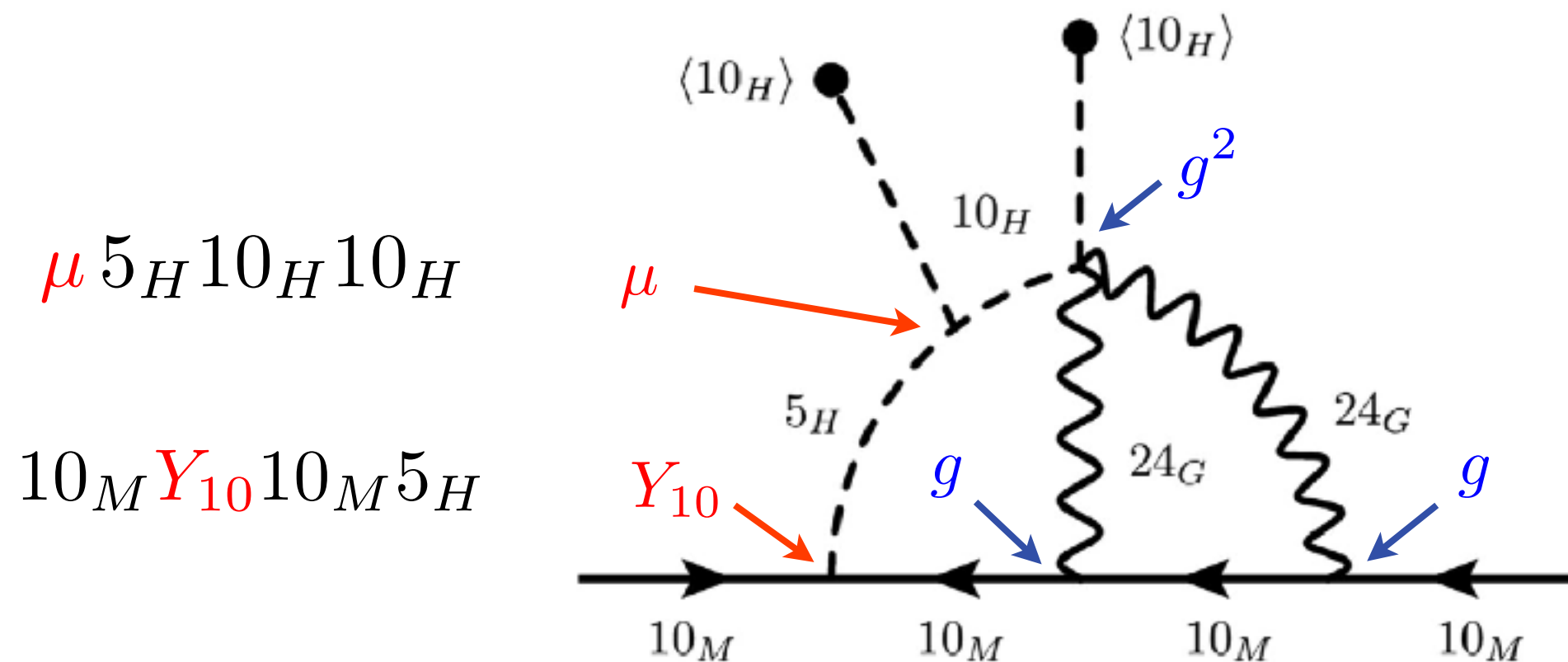
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$$M_M = \frac{1}{(16\pi^2)^2} g^4 \mu Y_{10}$$

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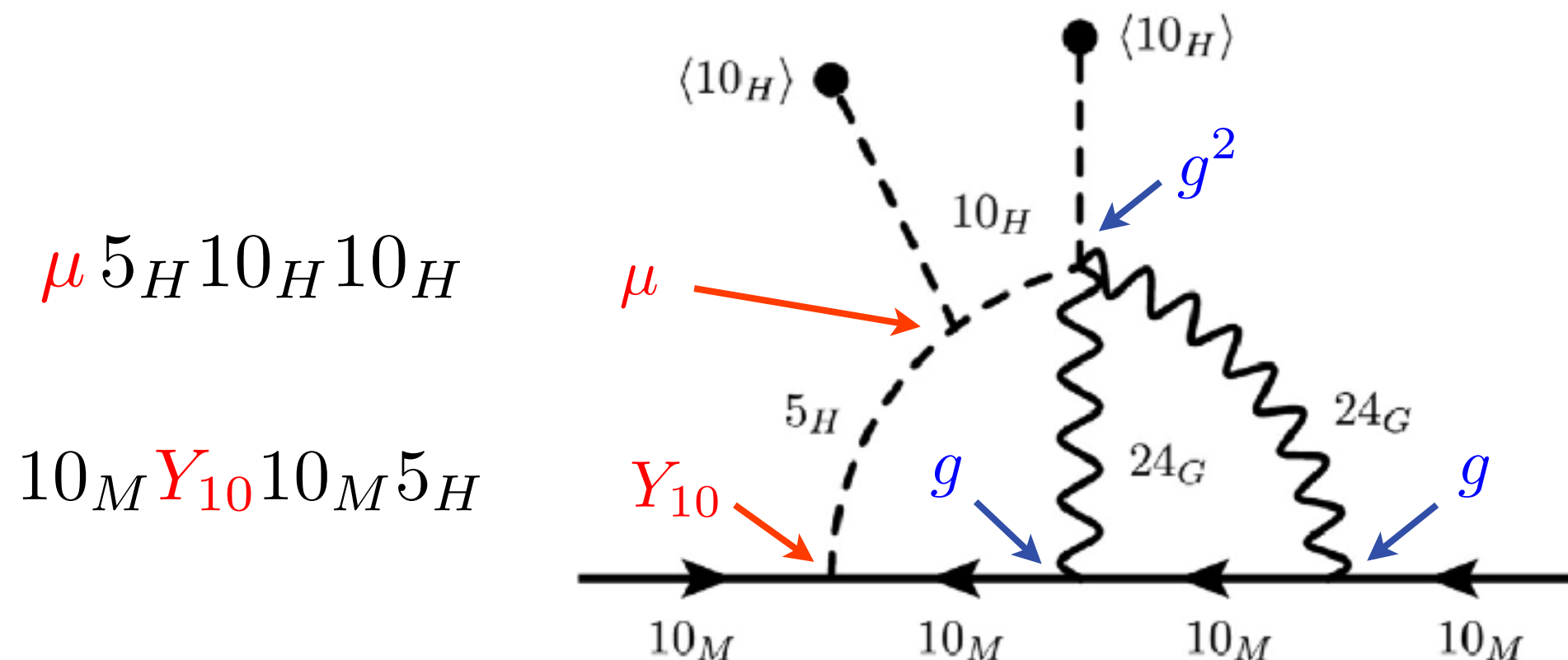


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O(1) factor depending on the details of the heavy spectrum



# Seesaw formula - the key to phenomenology

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**$U_\nu$  structure is strongly constrained !**

$$D_\nu^{-1} \text{ looks like } \begin{pmatrix} 10^{10-\infty} & 0 & 0 \\ 0 & 10^{10-11} & 0 \\ 0 & 0 & 10^{10} \end{pmatrix} \text{ GeV}^{-1} \quad D_u \sim \begin{pmatrix} 10^{-3} & 0 & 0 \\ 0 & 10^0 & 0 \\ 0 & 0 & 10^2 \end{pmatrix} \text{ GeV}$$

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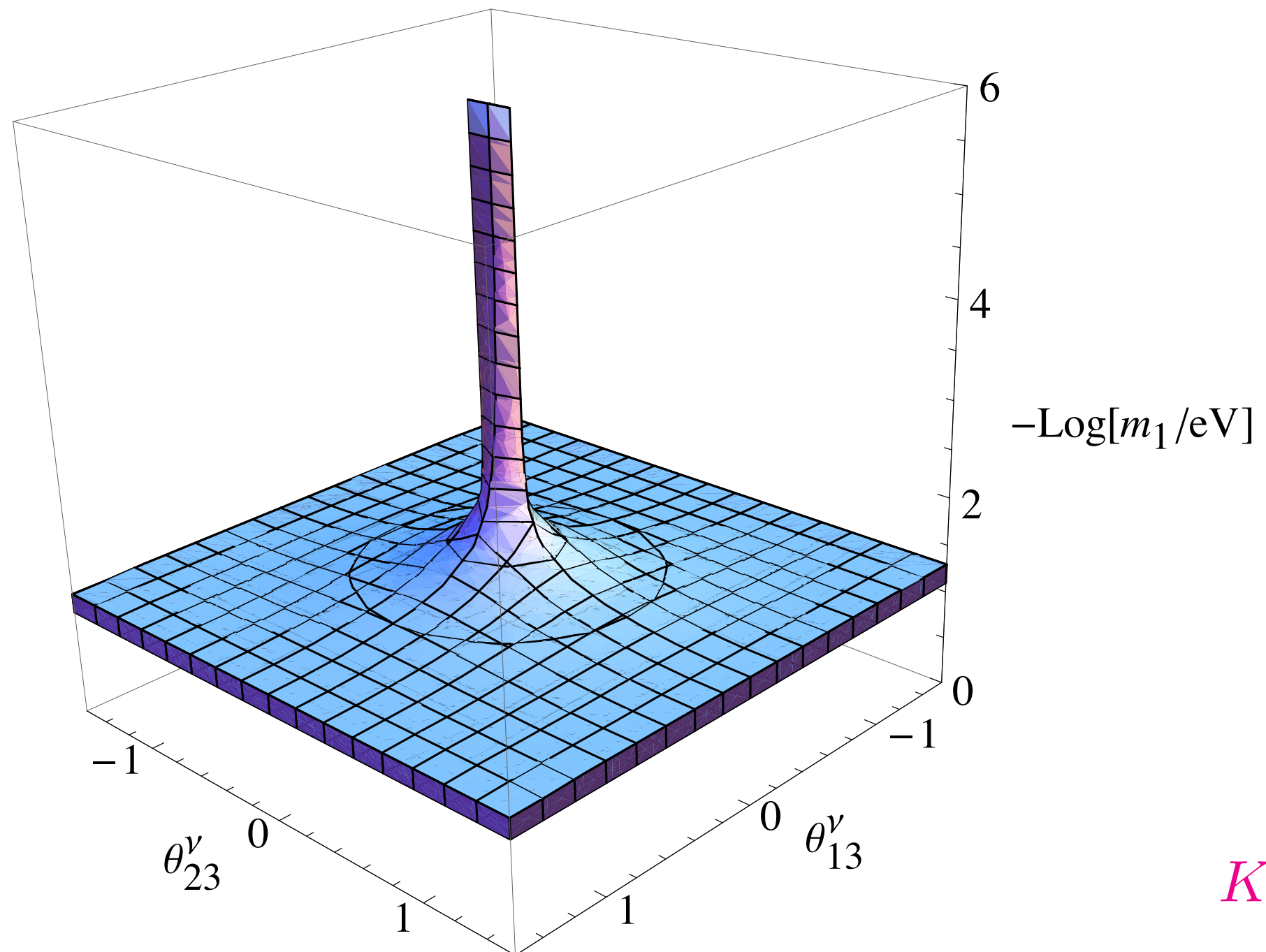
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Severity of these constraints depends on  $U_\nu$  and the lightest neutrino mass  $m_1$ ...

# The parameter space ( $m_1, U_\nu$ )

C.Arbelaez-Rodriguez, H.Kolešová, MM, PRD89 (2014)

$U_\nu$  angular behaviour:

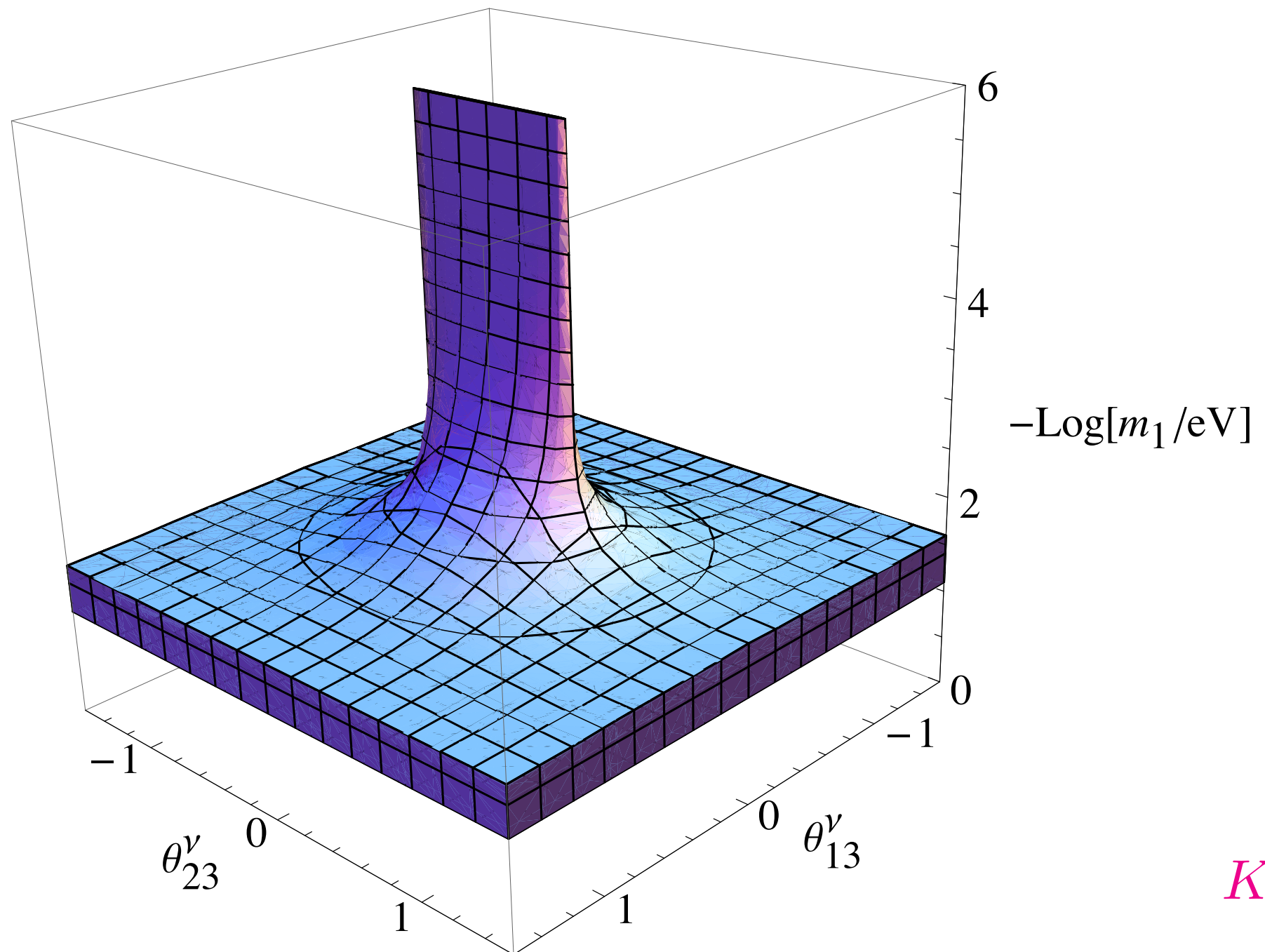


$K = 1$

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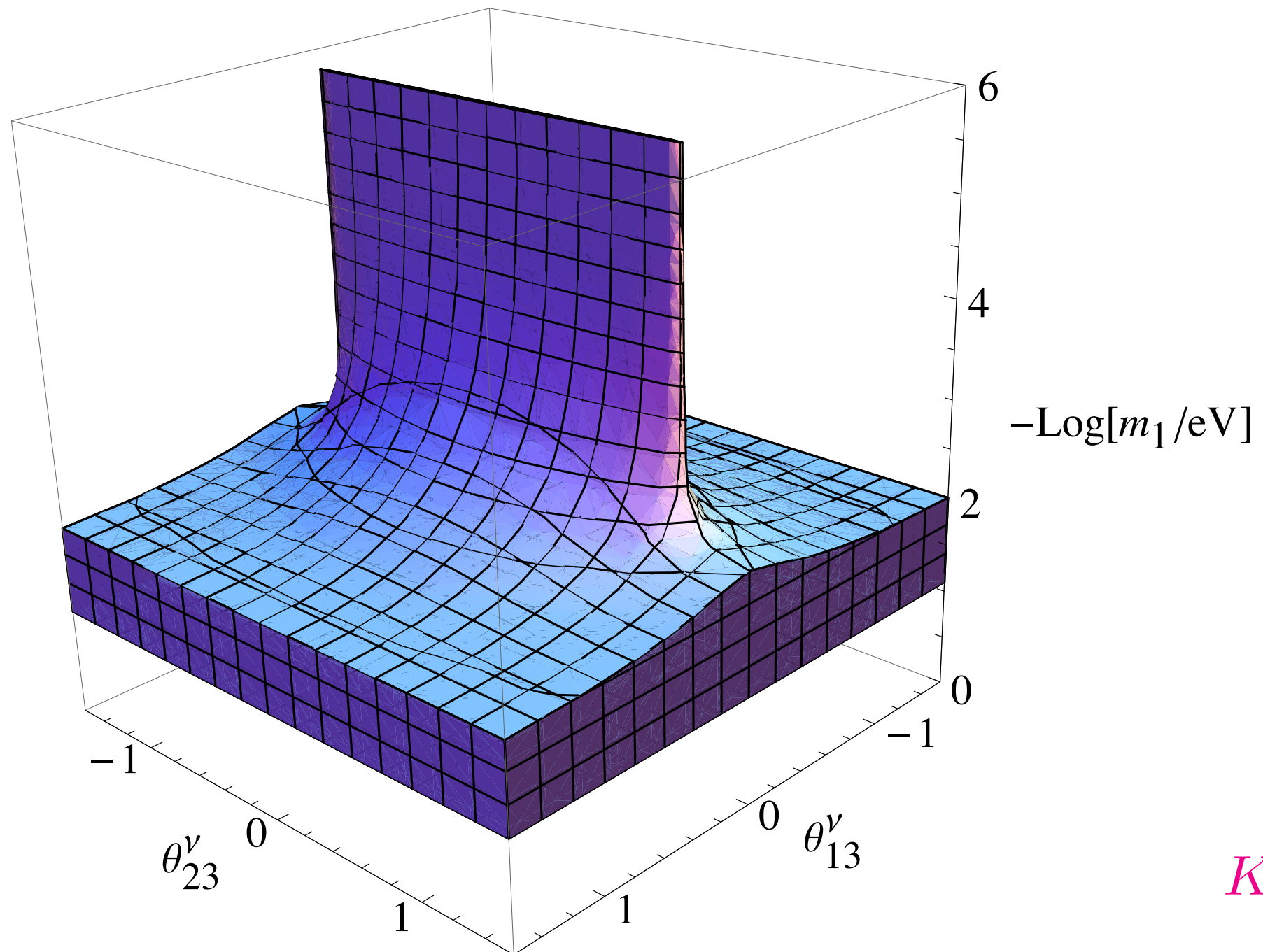
$K = 2$



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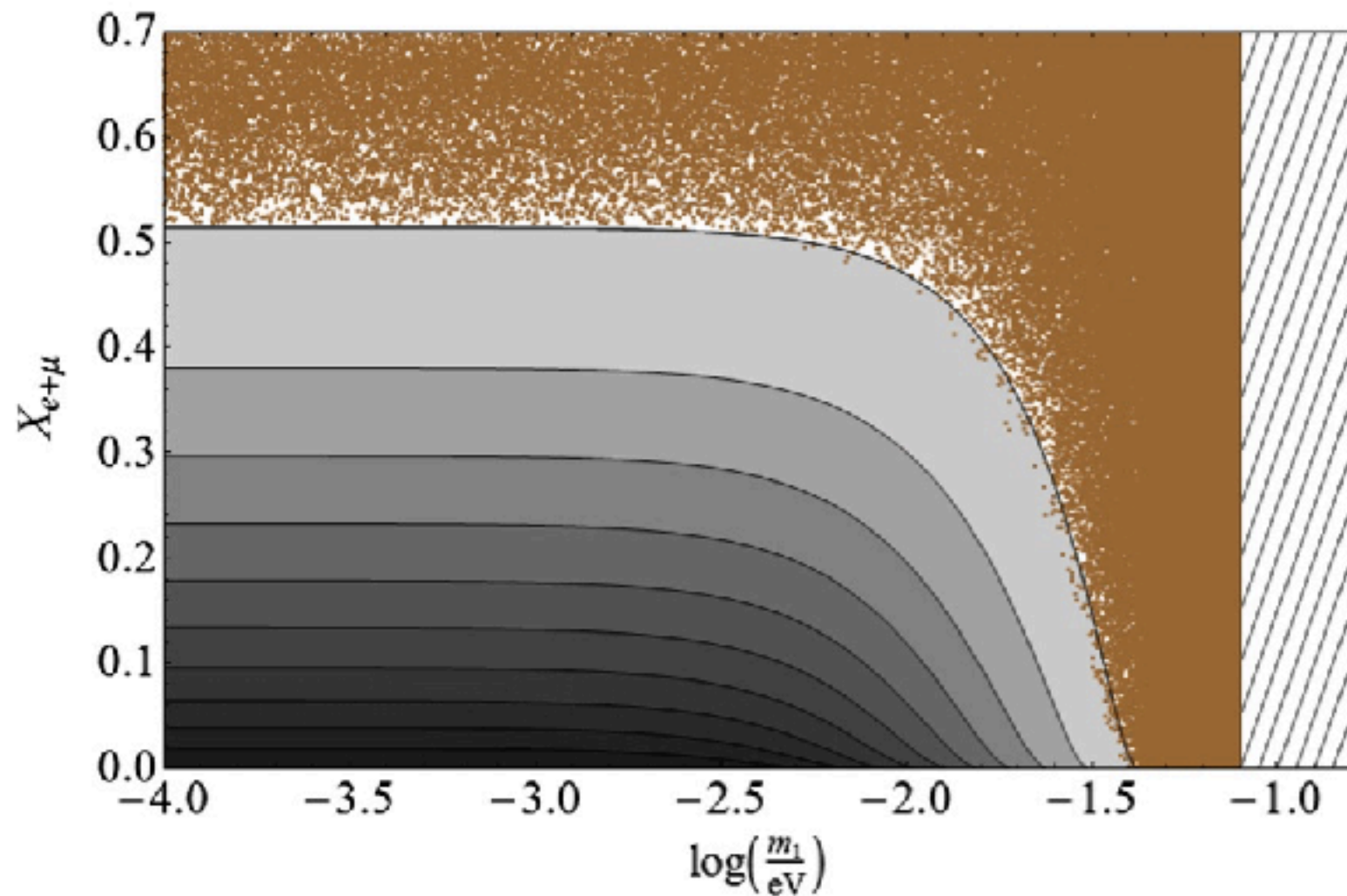
$K = 5$



# $U_\nu$ features in proton decay rates

Unlikely to have both  $\Gamma(p \rightarrow \pi^0 e^+)$  and  $\Gamma(p \rightarrow \pi^0 \mu^+)$  arbitrarily suppressed  
(in the small  $m_1$  regime)

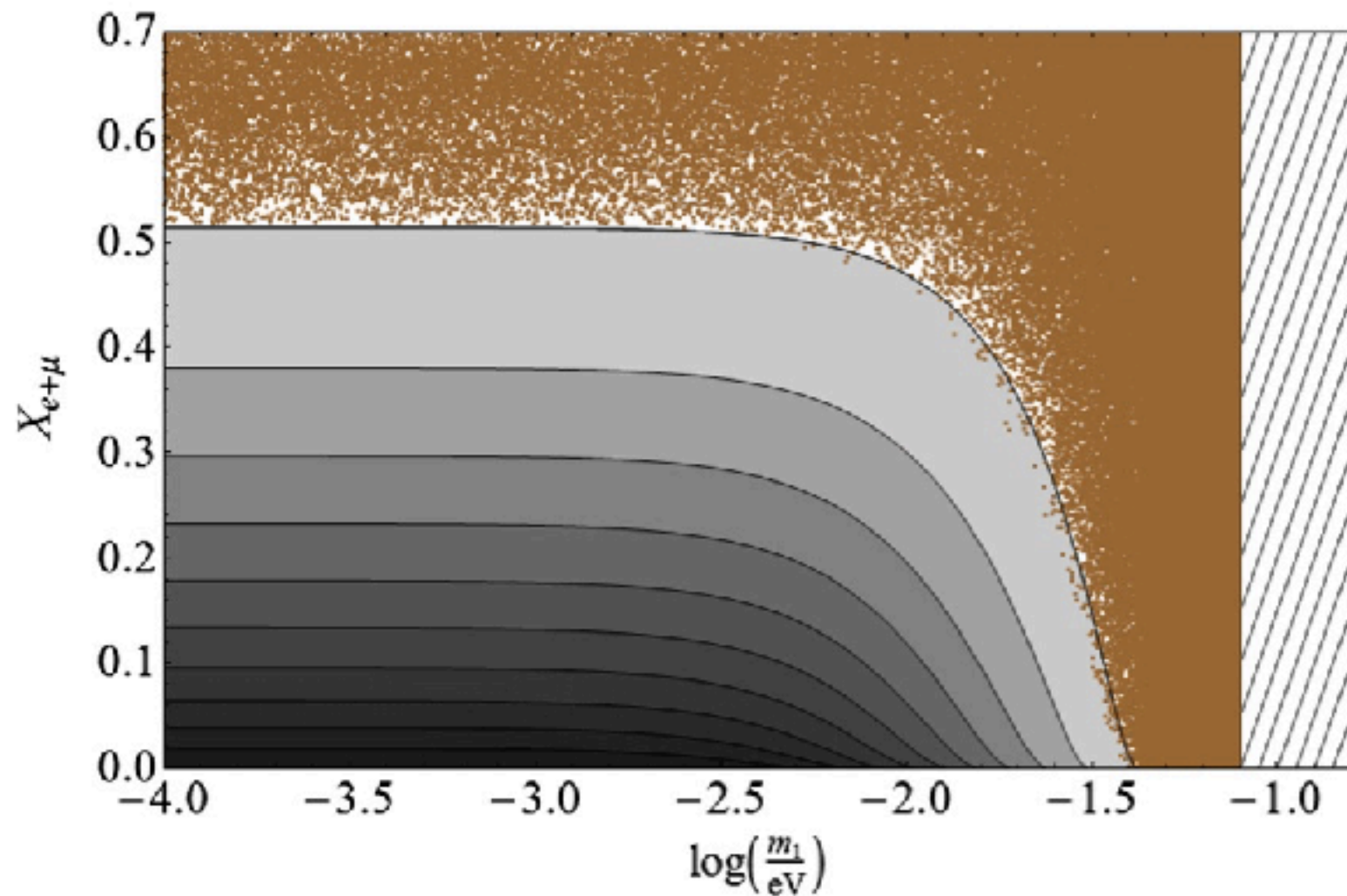
$K$   
growing  
↓



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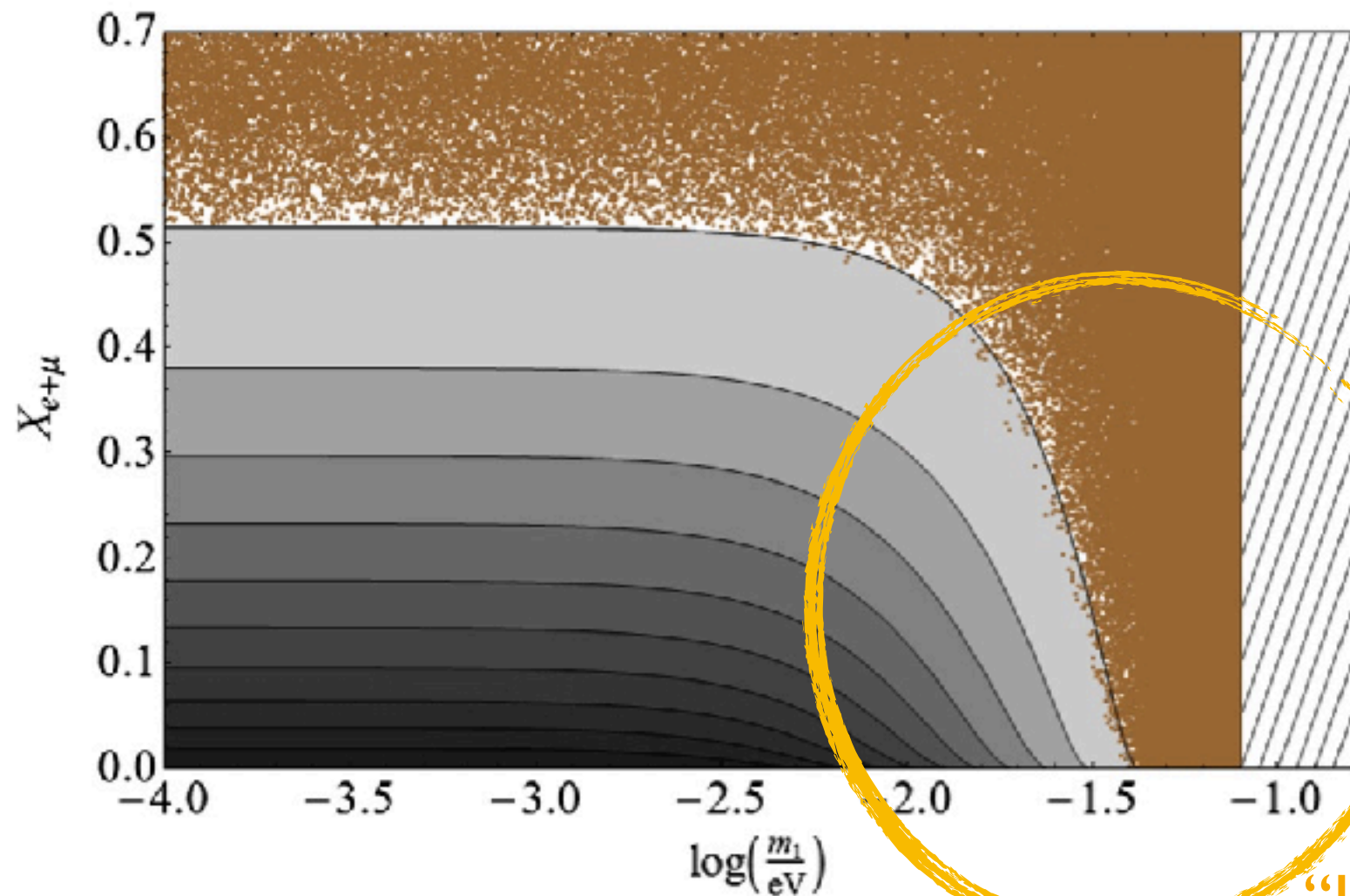
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“Large  $m_1$ ” regime

C.Arbelaez-Rodriguez, H.Kolešová, MM, PRD89 (2014)



# K ?



D. Harries, MM, M. Zdráhal PRD98 (2018)

Broken phase massive PE, unitary gauge:

$$M_M = \Sigma_{1\text{-loop}}(0) + \dots$$

NB. Zero-momentum two-loop integrals: M.J.G.Veltman, J.Van der Bij, Nucl. Phys. B231, 205 (1984)

- Each graph is **UV divergent** but no  $d=4$  counterterm -  $\Sigma(0)$  must be finite

UV divergences (d. reg.):

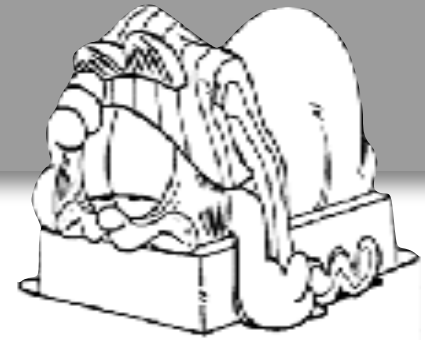
$$-\frac{M_\Delta^4}{4M_X^4\epsilon^2} - \frac{3M_\Delta^4}{4M_X^4\epsilon} + \frac{M_\Delta^4 \log(M_\Delta^2)}{2M_X^4\epsilon} + \frac{3}{2\epsilon}$$

Exactly cancel among the three topologies

$$M_M \lesssim 10^{-2} M_X \times 10^{-1} \times 3 \sum_{i=1,2} (U_\Delta)_{i1} (U_\Delta^*)_{i2} I \left( \frac{m_{\Delta_i}^2}{m_X^2} \right)$$

# How about the “large $m_1$ ” regime?

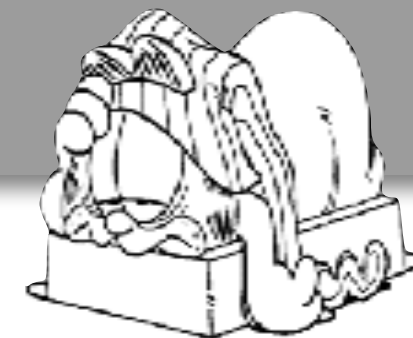
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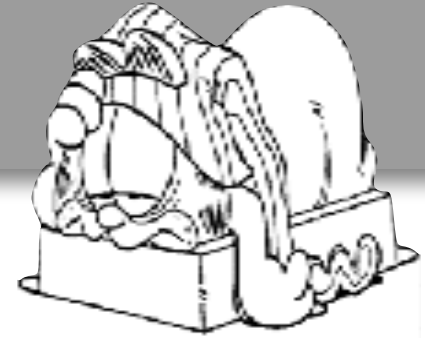
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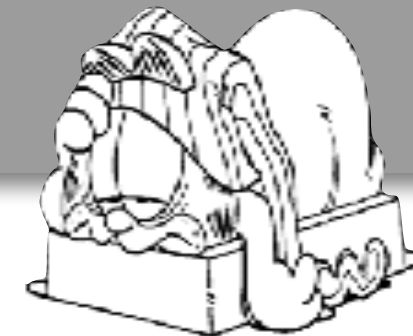
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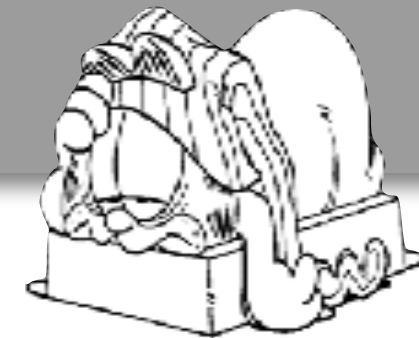
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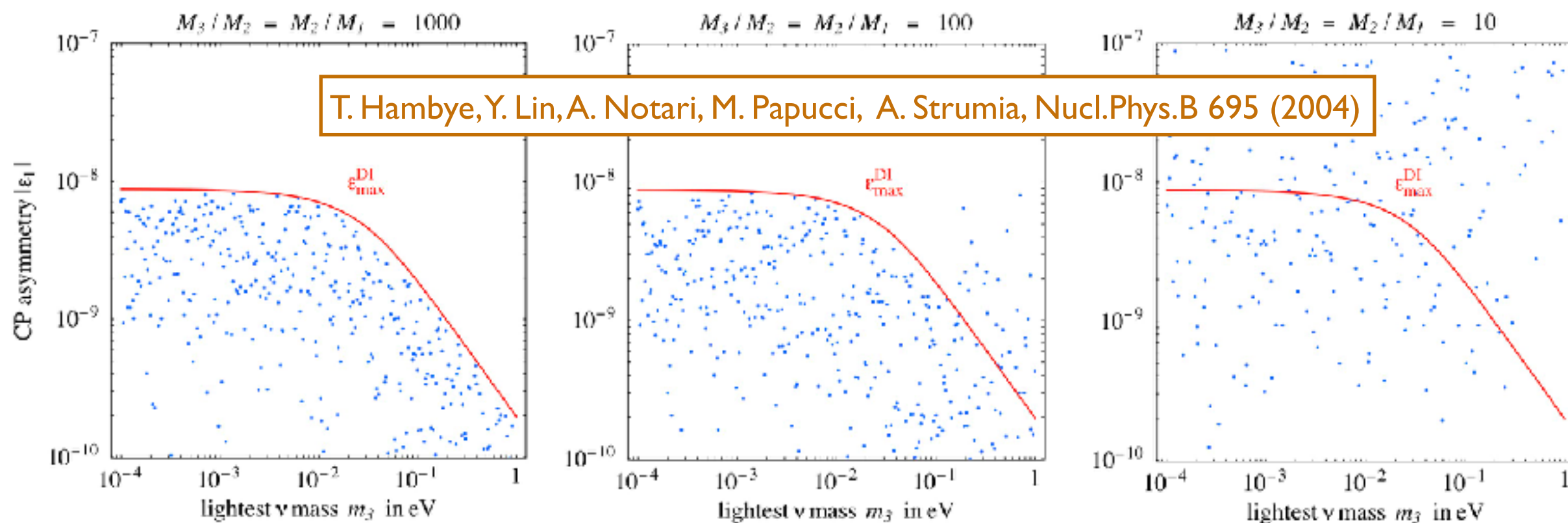


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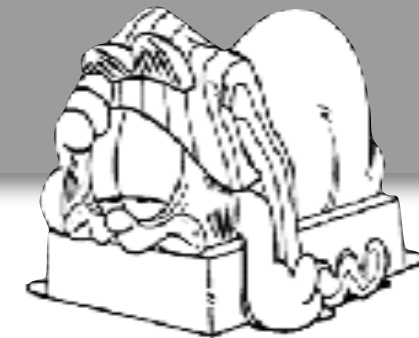
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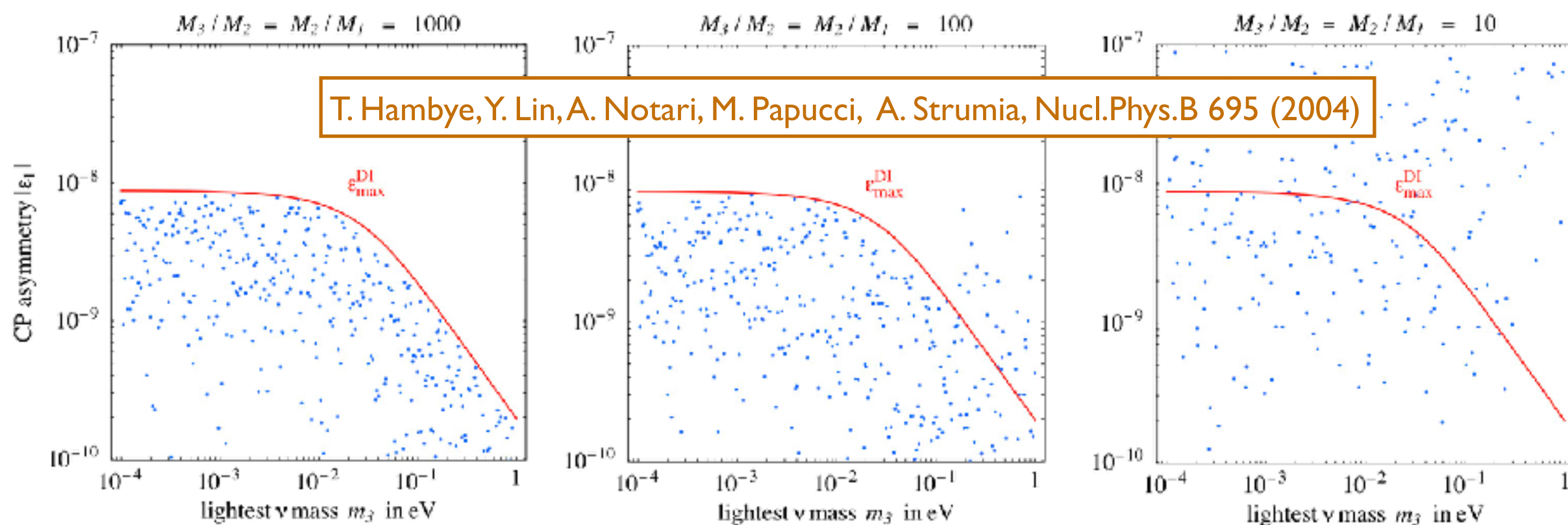


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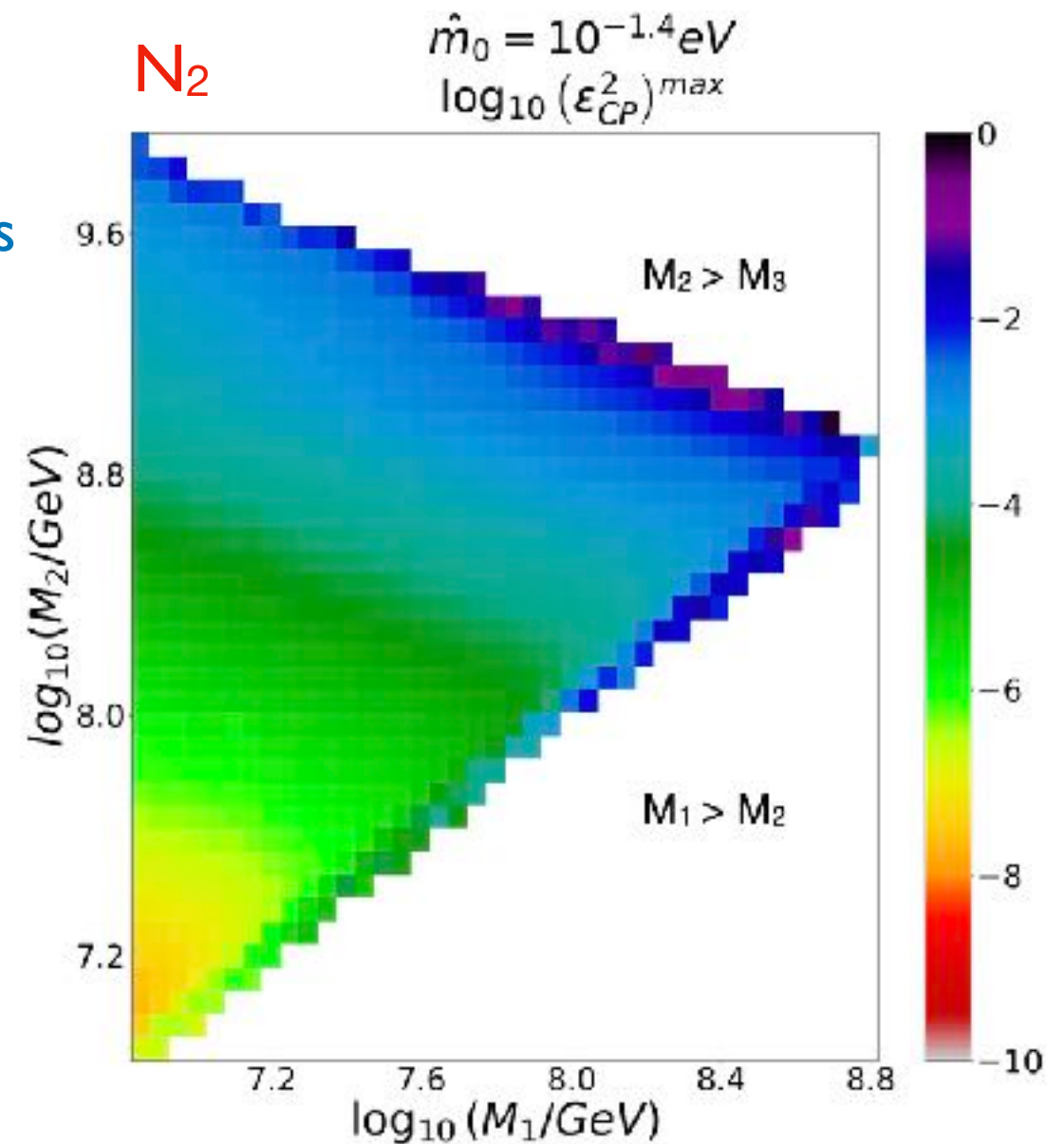
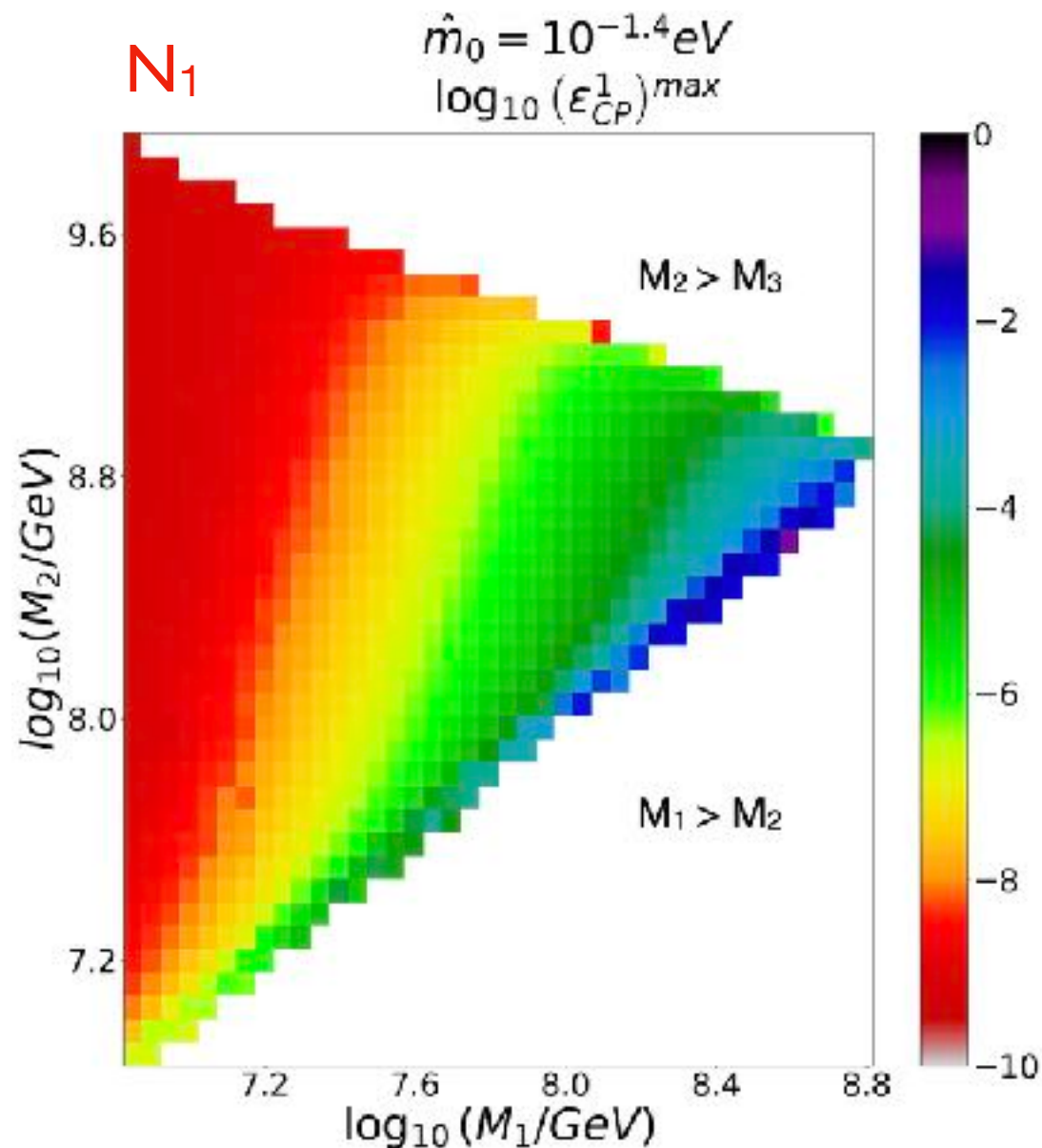


- $U_\nu$  may need to be special though  $\longrightarrow$  **further constraints on BLNV rates (?)**



# Thermal $\bigcirc \rightarrow \square$ in the minimal flipped SU(5) à la Witten

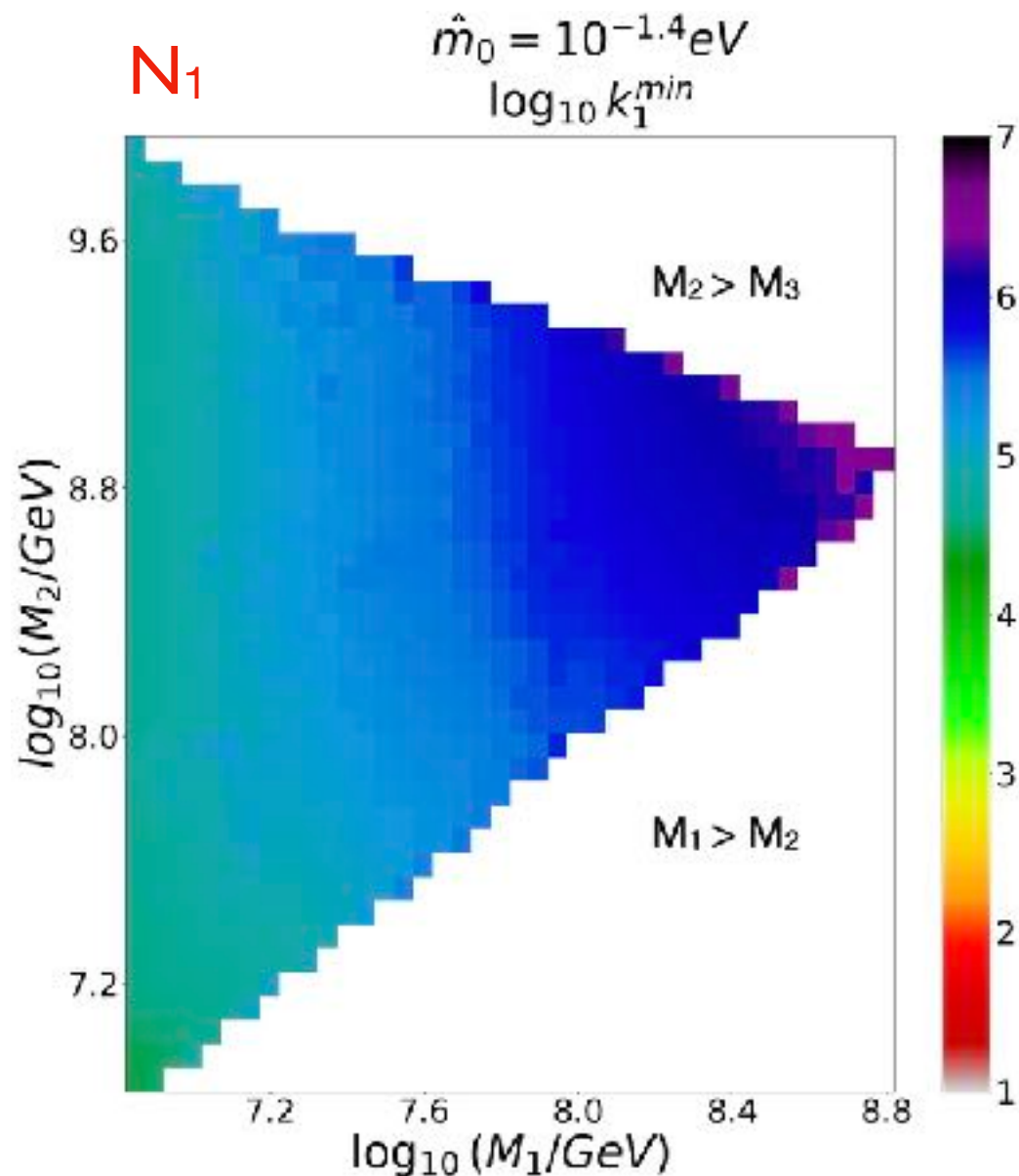
“Large  $m_1$ ” regime : CP asymmetries OK, washout typically large



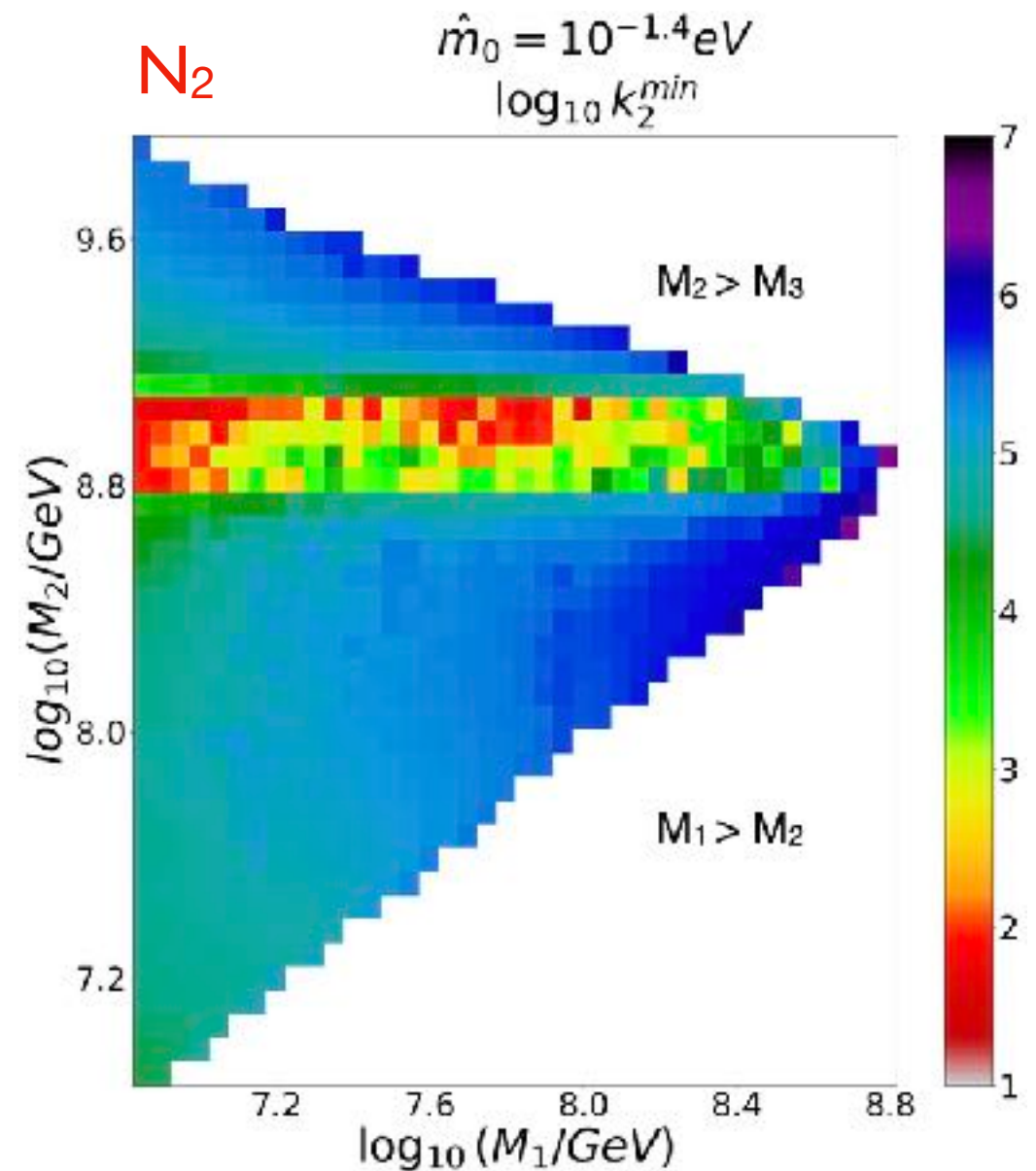
Miřátský, Fonseca, Zdráhal, MM, arXiv:2312.08357

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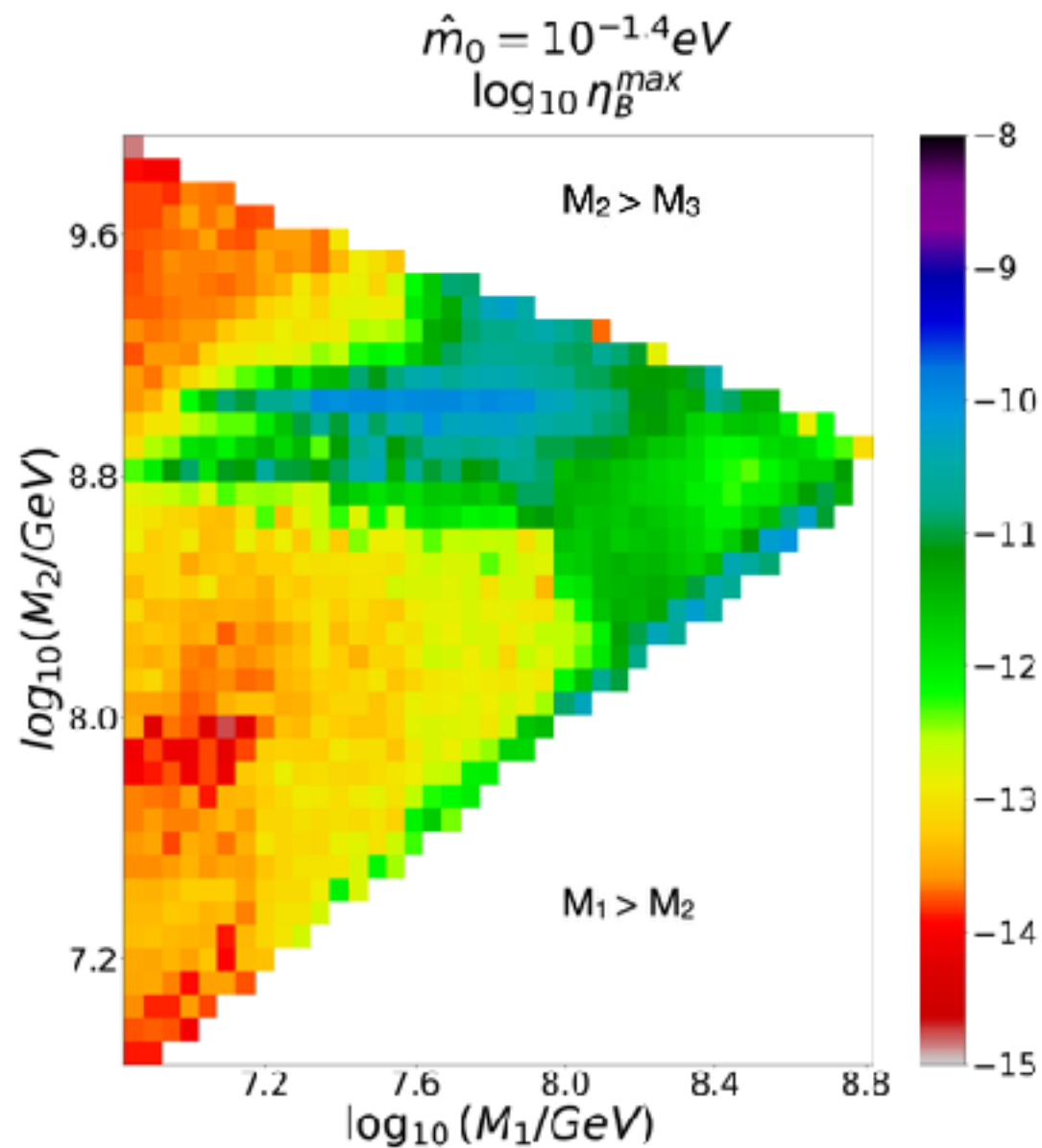
Washout



Miřátský, Fonseca, Zdráhal, MM, arXiv:2312.08357

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Detailed numerical analysis (ULYSSES)

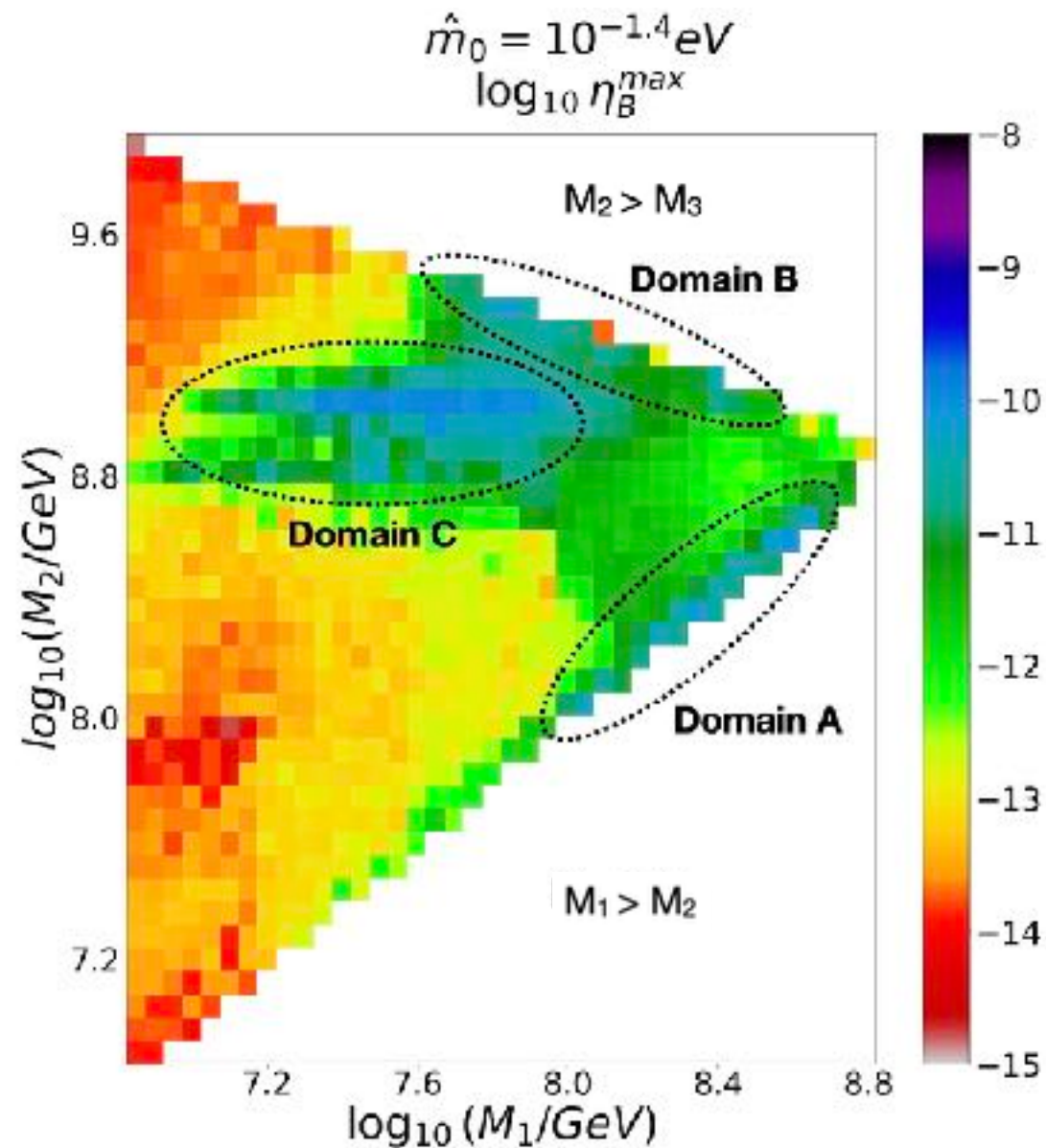
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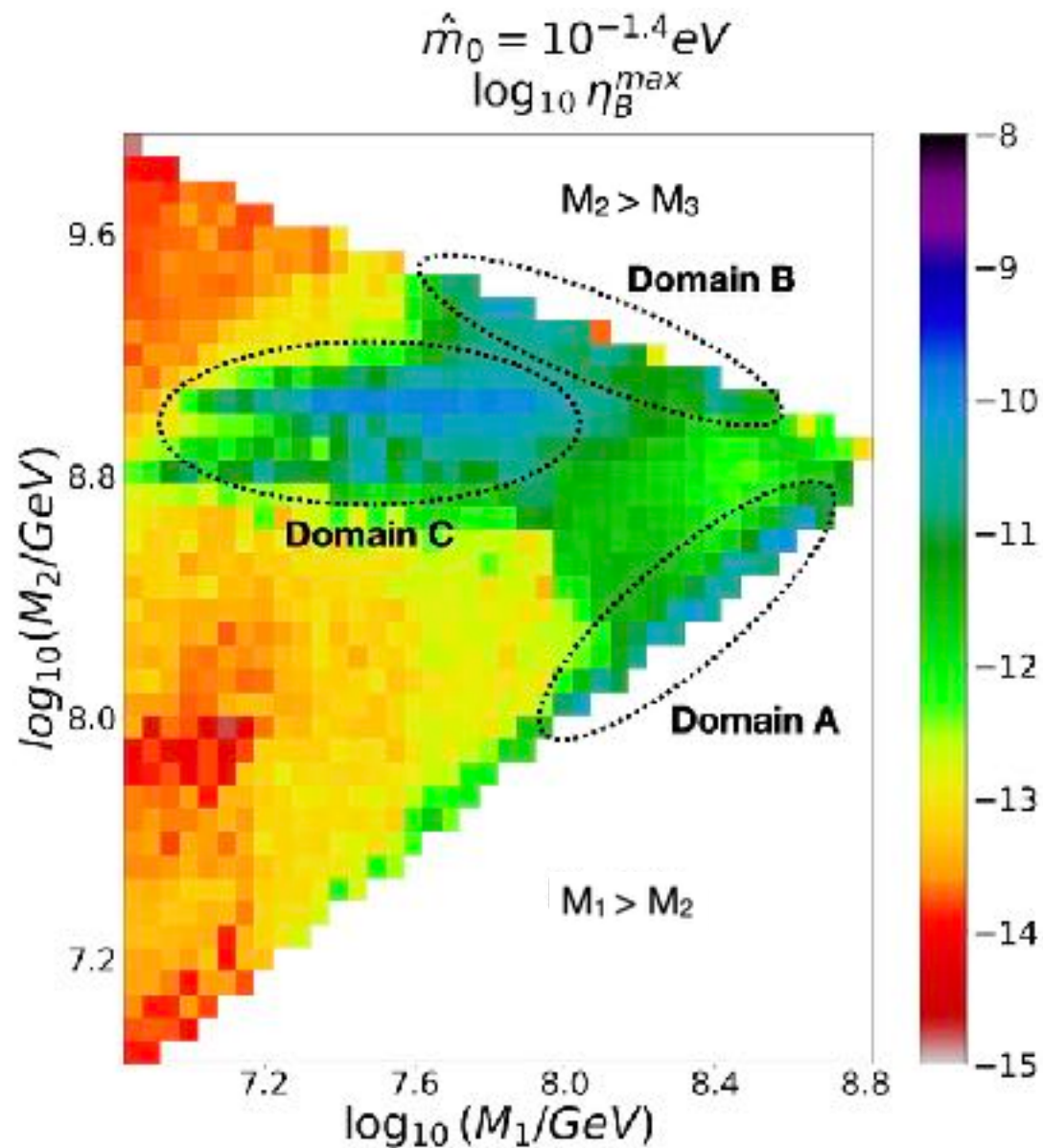
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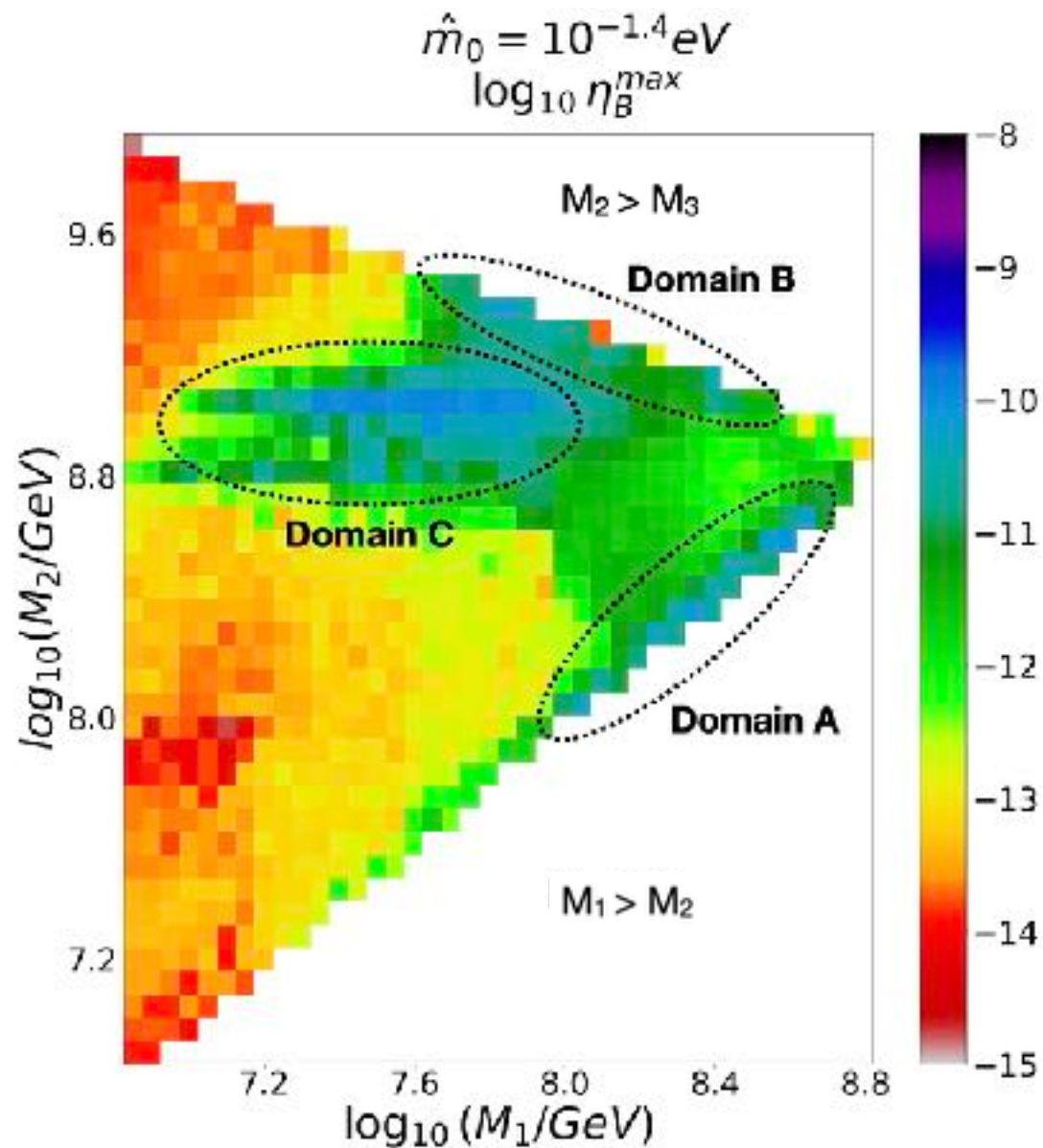
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(several tens of millions generated)

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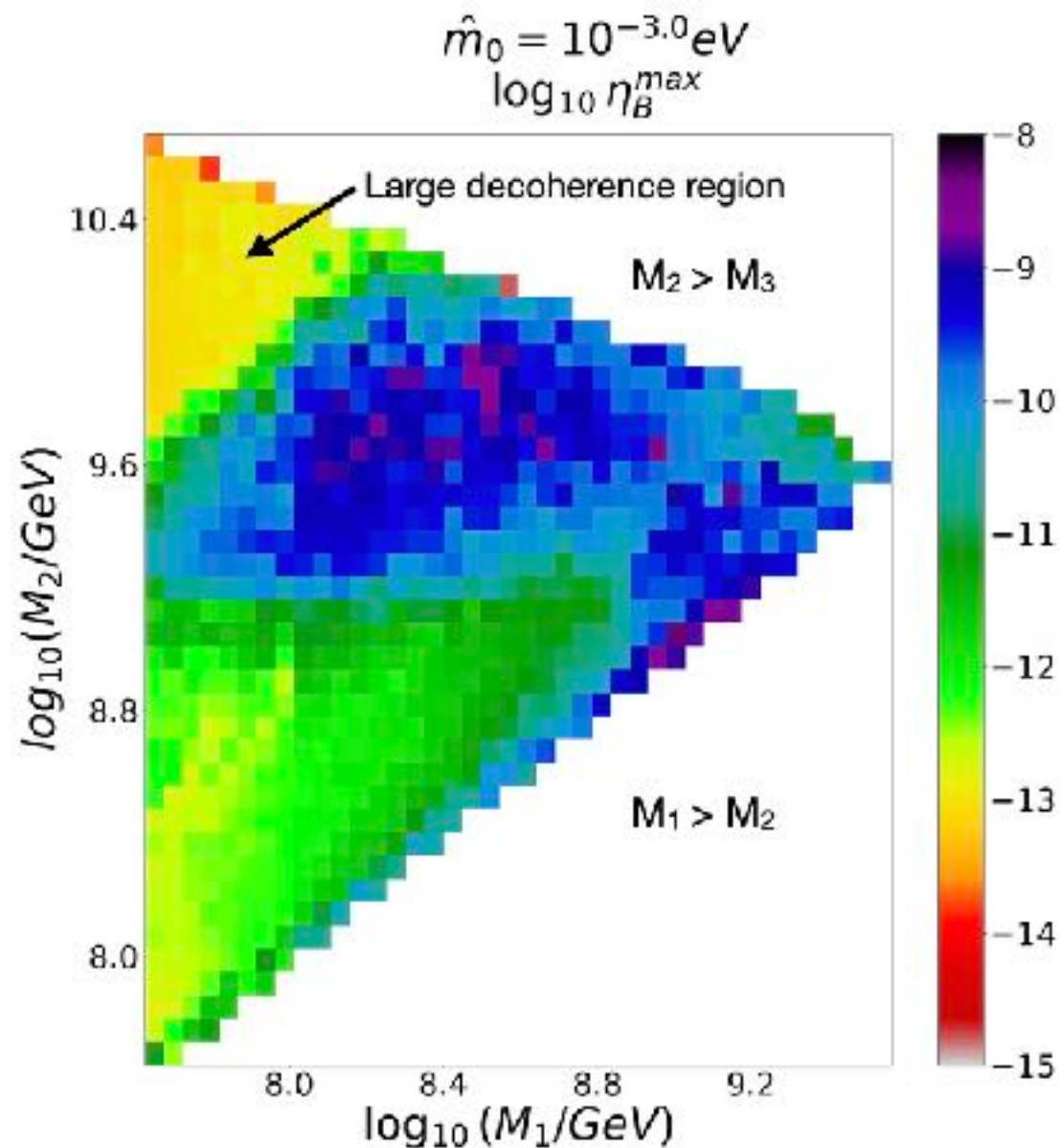
“Large  $m_1$ ” regime sterile

**No signal in KATRIN**

Miřátský, Fonseca, Zdráhal, MM, arXiv:2312.08357

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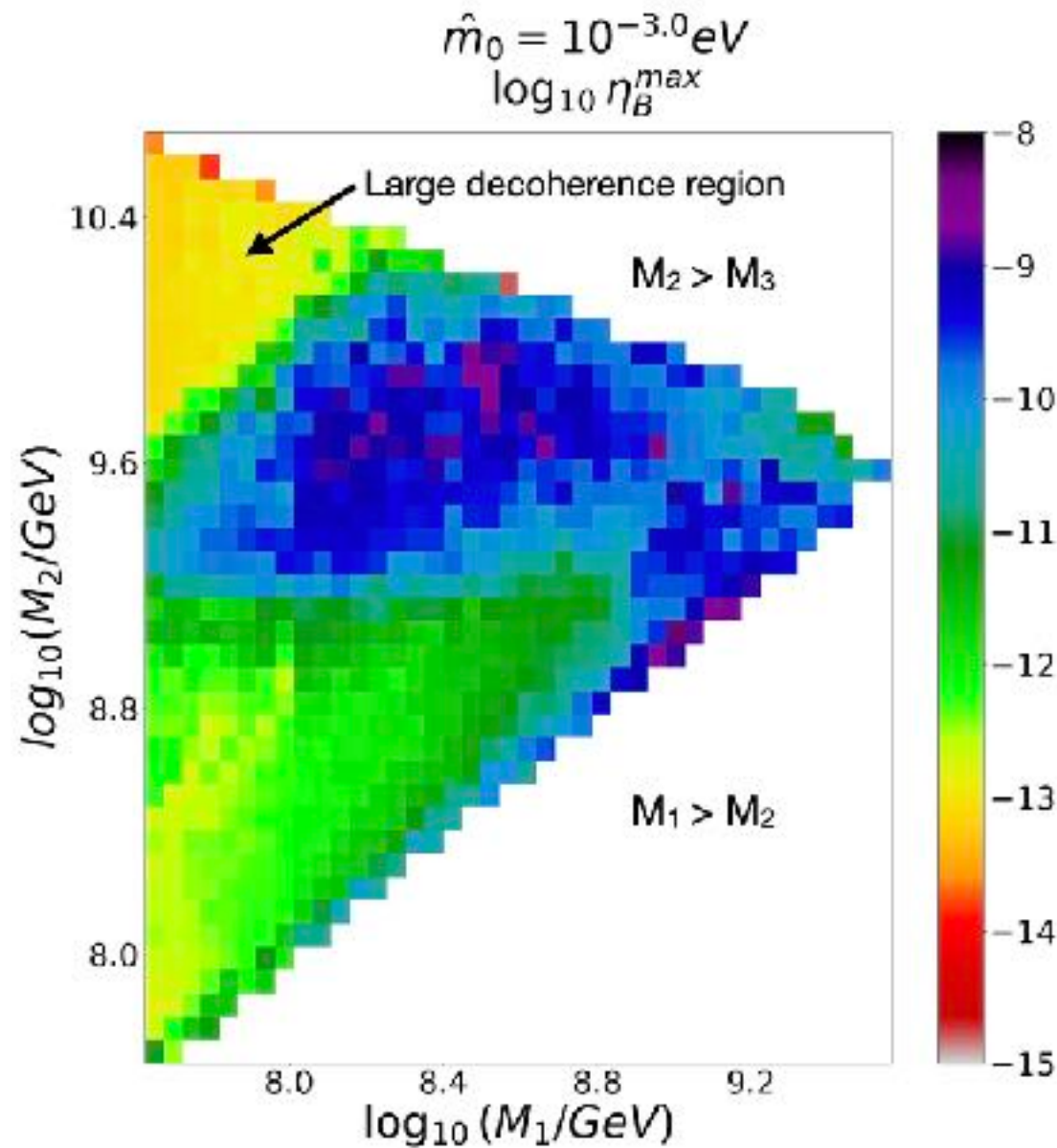
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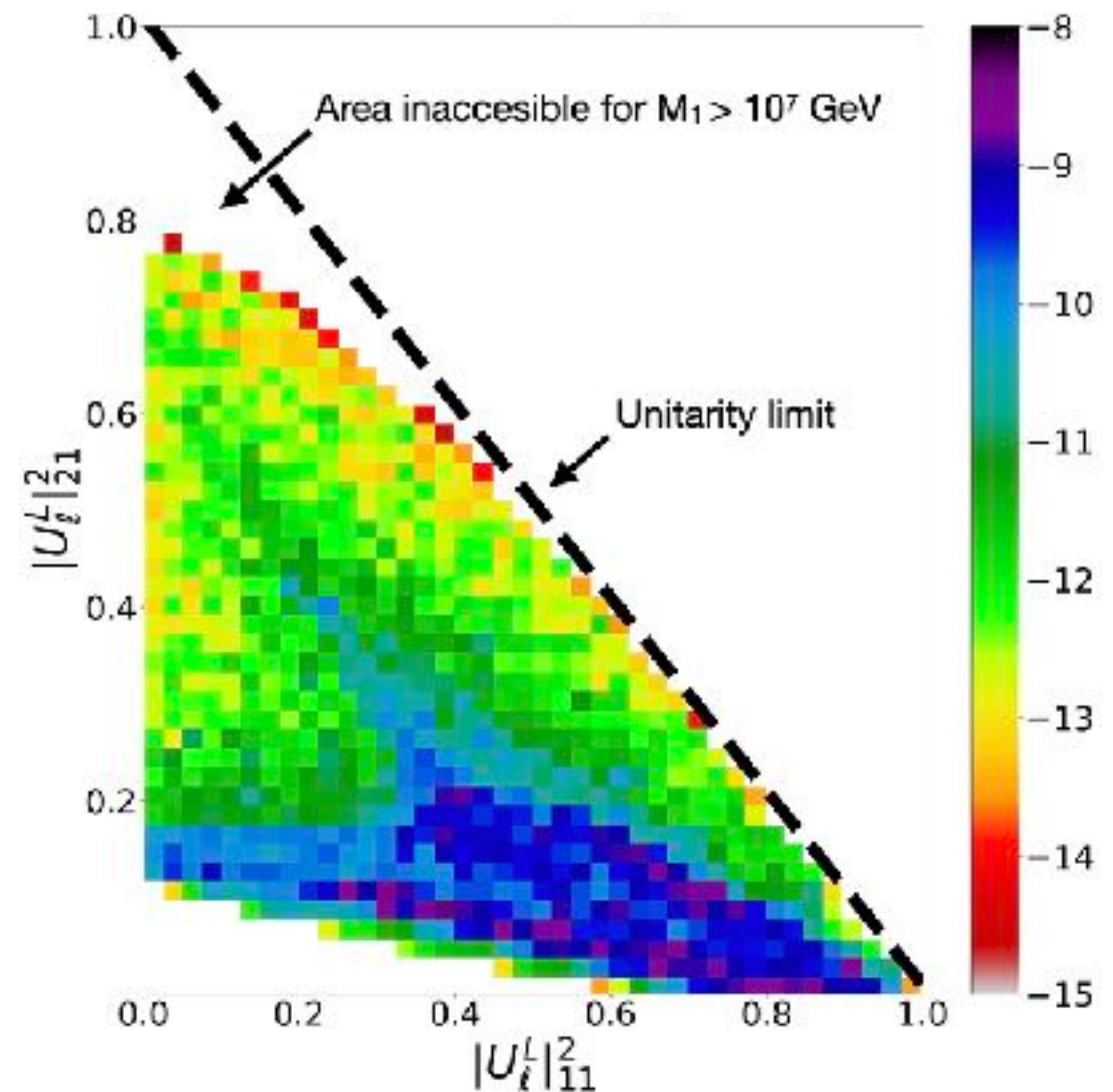


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Further constraints on p-decay!



Miřátský, Fonseca, Zdráhal, MM, arXiv:2312.08357

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