



# Hirsch FEST



Enrico Nardi



HEP Group



Istituto Nazionale di Fisica Nucleare  
Laboratori Nazionali di Frascati

[Subtle effects in high precision physics: the  $(g-2)_\mu$  anomalies]

*IFIC (Valencia)*

--

*January 23-24, 2024*

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In those years I was holding a professorship position at the UdeA in Medellín, Colombia.

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Index	Domain	Meaning
Hirsch-0	Only applicable to Martin	No. of papers authored by Martin
Hirsch-1	Anyone	No. of papers coauthored with Martin by the researcher
Hirsch-2	Anyone	No. of papers coauthored with Martin by coauthors of the researcher
Hirsch-3	Anyone	No. of papers coauthored with Martin by coauthors of coauthors of the researcher
....		

E. Nardi:      Hirsch-1 Index = 2

Quasi-Dirac neutrinos at the LHC #1

G. Anamiati (Valencia U., IFIC), M. Hirsch (Valencia U., IFIC), E. Nardi (Frascati) (Jul 19, 2016)

Published in: JHEP 10 (2016) 010 • e-Print: 1607.05641 [hep-ph]

pdf    DOI    cite    claim    reference search    96 citations

Bounds on the tau and muon neutrino vector and axial vector charge radius #2

Martin Hirsch (Valencia U., IFIC), Enrico Nardi (Frascati and Antioquia U.), Diego Restrepo (Antioquia U.) (Oct, 2002)

Published in: Phys.Rev.D 67 (2003) 033005 • e-Print: hep-ph/0210137 [hep-ph]

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However, my **Hirsch-2** index is remarkable:

E. Nardi: Hirsch-2 Index (partial, only UdeA) > 23

and there is a good explanation also for this...



At the end of the past millenium/beginning of the new one, in Colombia scientific isolation was affecting heavily scientific research, and high level formation of young researchers (Ph.D.)

- Internet seemed to run on a 56Kb modem for the whole UdeA (arXiv download only in the night)
- Only a few and outdated physics books in the Library
- Fragmentary collections of scientific journals (several years missing - almost useless)
- Administrative apparatus mainly oriented to handle teaching (unsuited for research needs)

[Example of a typical objections: 1 month leave of the absence to visit CERN = 1 month vacation in the Swiss ALPs]

- Because of dangerous social conditions, very few colleagues willing to pay a visit to UdeA

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- [Example of a typical objections: 1 month leave of the absence to visit CERN = 1 month vacation in the Swiss ALPs]
- Because of dangerous social conditions, very few colleagues willing to pay a visit to UdeA

Martin was one of those very few colleagues. From a backup CD, I have been able to trace:

- A 1st visit: 25 Nov - 11 Dec, 2000, during which he also acted as evaluator of the 1st thesis in HEP at UdeA.
- A 2nd visit: 10 Aug - 4 Sept 2002, during which I became **Hirsch-1 Index** = 1
- A 3rd visit: 26 Jan - 14 Feb 2004

Martin was always ready to comply with unusual requests:

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```
INBOX-NEW- From enardi@naima.udea.edu.co Mon Nov 13 07:03:19 2000 -0500
INBOX-NEW: Return-Path: <mahirsch@hep.phys.soton.ac.uk>
INBOX-NEW->
INBOX-NEW-> [...] would it be possible that
INBOX-NEW-> I will ask amazon.co.uk to ship the
INBOX-NEW-> books to you, before November 25, and you will
INBOX-NEW-> bring them to us ?
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```
INBOX-NEW- Hi Enrico,
INBOX-NEW- Today I received 2 books from Amazon for you.
INBOX-NEW- a.) Bailin and Love, Introduction to gauge field theory
INBOX-NEW- b.) Gaisser, Cosmic Rays and Particle Physics.

INBOX-NEW- Hi Enrico,
INBOX-NEW-
INBOX-NEW- I received 5 more books from Amazon:
INBOX-NEW- 1. Lattice Gauge Theories: An introduction
INBOX-NEW- 2. Mathematical methods for physicists
INBOX-NEW- 3. Instantons in gauge theories
INBOX-NEW- 4. Modern Differential Geometry for Physicists
INBOX-NEW- 5. Dynamics of the SM
```

And also rather unusual non-academic requests (like importing coffee to Colombia !):



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```
Received-Feb-2004: From mahirsch@ific.uv.es Fri Jan 23 10:52:06 2004
Received-Feb-2004- Delivered-To: enardi@naima.udea.edu.co
Received-Feb-2004- Hi Enrico,
Received-Feb-2004-
Received-Feb-2004- > My Italian espresso coffee is finished :-(
Received-Feb-2004- > And here in Medellin it is impossible
Received-Feb-2004- > to find it, and therefore I am not sure
Received-Feb-2004- > that I can make it until your arrival.
Received-Feb-2004-
Received-Feb-2004- Hold on! Don't give up! Rescue is only a bit more than
Received-Feb-2004- a week away...
Received-Feb-2004-
Received-Feb-2004- > I order of preference, the brand could be :
Received-Feb-2004- >
Received-Feb-2004- > Illy
Received-Feb-2004- > Lavazza Oro
Received-Feb-2004- > Lavazza Rosso
Received-Feb-2004-
Received-Feb-2004- ...I'll try to do my best.
```

Around mid 2000 a vacancy for a professorship position became available in UdeA. Martin responded positively to an inquiry about his possible interest in that position

NaimaInbox- On Mon, 14 Aug 2000, Diego Restrepo wrote:

NaimaInbox-

NaimaInbox-> Hola Martin,

NaimaInbox->

NaimaInbox-> Enrico me encomendo el preguntarte si tu estarias interesado en postular a

NaimaInbox-> una plaza vacante que hay en este momento en la Universidad de Antioquia o

NaimaInbox-> si conoces de alguien que podria estar interesado.

NaimaInbox->

NaimaInbox-> Hasta luego

NaimaInbox-> Diego

NaimaInbox- Date: Wed, 16 Aug 2000 00:04:57 +0200 (CET)

NaimaInbox: From: Martin Hirsch <mahirsch@nac11.ific.uv.es>

NaimaInbox- To: Diego Restrepo <restrepo@naima.udea.edu.co>

NaimaInbox- Subject: Re: Question

NaimaInbox-

NaimaInbox- Hola Diego,

NaimaInbox-

NaimaInbox- en principio puede ser que tengo interes. Sabes, que voy a inglaterra

NaimaInbox- on octubre, pero eso es solamente una position postdoctoral. Si tienes

NaimaInbox- mas informaciones puedes enviar me lo? Si no, por favour, me escribiras

NaimaInbox- el Email de Enrico...Gracias!

NaimaInbox-

NaimaInbox- Hasta luego,

NaimaInbox- Martin

UdeA colleagues were very excited to hear that Martin was willing to join the UdeA HEP group. But someone also moved some critiques...

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INBOX-NEW- Date: Mon, 13 Nov 2000 22:44:53 +0100  
INBOX-NEW- From: Tatiana Fernandez Maya <taferma@alumni.uv.es>  
INBOX-NEW- To: [enardi@naima.udea.edu.co](mailto:enardi@naima.udea.edu.co)  
INBOX-NEW-  
INBOX-NEW- Me contaron por ahi las malas lenguas que dentro de unos dias llegara  
INBOX-NEW- alli Martin Hirsch (o algo asi) y que al parecer piensan ofrecerle el  
INBOX-NEW- puesto que dejo Luis Alberto; como puedes ser tan miserable que quieres  
INBOX-NEW- que Martin sufra todo lo que has sufrido? Que tienes contra el pobre  
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INBOX-NEW- Date: Mon, 12 Feb 2001 02:30:10 +0000 (GMT)  
INBOX-NEW- From: Martin Hirsch <mahirsch@hep.phys.soton.ac.uk>  
INBOX-NEW- To: Enrico Nardi <enardi@naima.udea.edu.co>  
INBOX-NEW- Subject: Re: Time scale  
INBOX-NEW-  
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So we opened the UdeA call, and Martin won it. (With his academic records, basically no competitors)

But in the end Martin got a Ramon&Cajal and declined the UdeA position  
(I guess, luckily for him, but in a sense also for us... you will see why...)

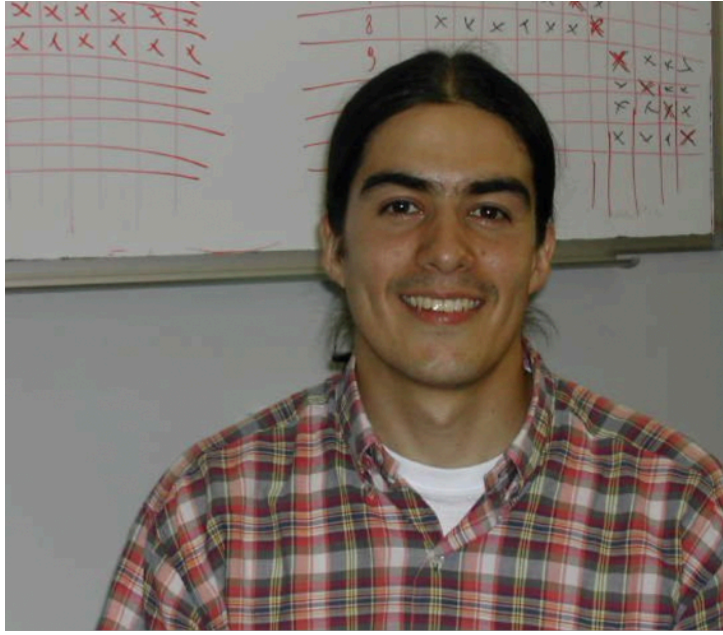


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Received-Sep-2001-  
Received-Sep-2001- Hi Enrico,  
Received-Sep-2001-  
Received-Sep-2001- this is going to be a bit difficult. I am in Valencia  
Received-Sep-2001- now for a short visit and news have just appeared that  
Received-Sep-2001- **my name is on the list of eligible candidates for the**  
Received-Sep-2001- **Ramon y Cajal program. As I understand it right this**  
Received-Sep-2001- **moment this means that I have it,** barring some unforeseen  
Received-Sep-2001- bureaucratic obstacle.  
Received-Sep-2001-  
Received-Sep-2001- I hope you understand my situation and I am sorry if  
Received-Sep-2001- I caused trouble in Medellin. I will write to Nelson  
Received-Sep-2001- to explain the situation, because **at present it seems**  
Received-Sep-2001- **that I will most likely not be able to accept the offer**  
Received-Sep-2001- **by the University of Antioquia.**  
Received-Sep-2001-  
Received-Sep-2001- It is really an embarrassing situation. For years I have  
Received-Sep-2001- tried to find something more permanent than a simple  
Received-Sep-2001- postdoc, and everything failed in the end.

We have been lucky to have a contact in a strong HEP group in Europe, always ready to help: inviting students, helping with Ph.D. scholarships, supervising Ph.D. thesis:

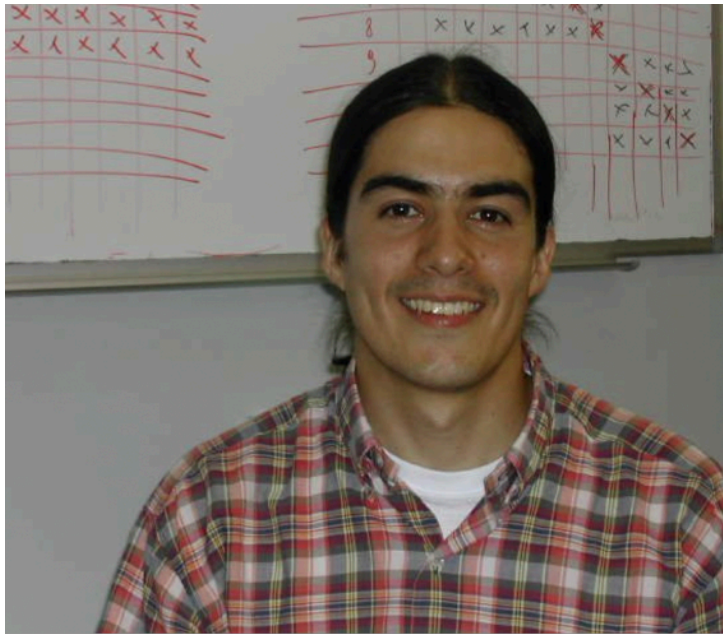
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Diego Aristizabal Sierra (M.Sc. UdeA) Ph.D. U. Valencia 2007



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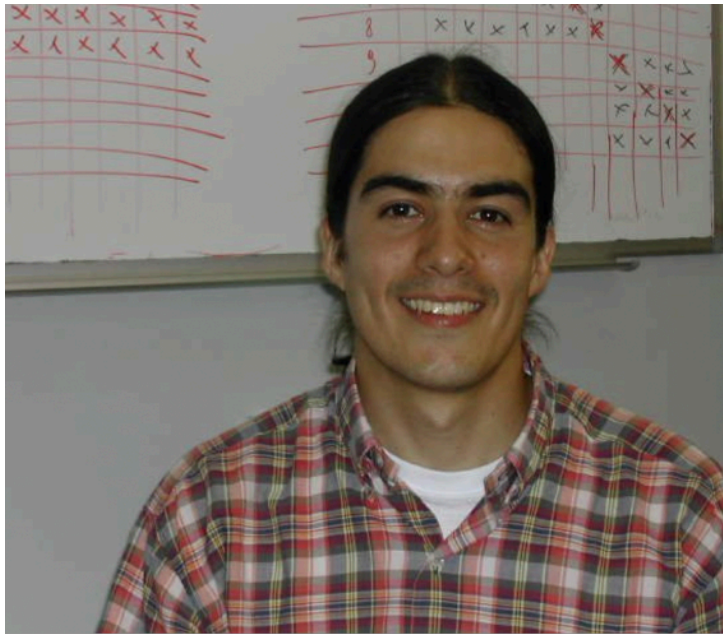
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Gaetana Animati (B.Sc. Unical) Ph.D. U. Valencia 2018

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Therefore, for all the episodes listed above, and for many more contributions not listed because of time/space constraints



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Thank you Martin !



# Subtle effects in high precision physics: the $(g-2)_\mu$ anomalies

Based on:

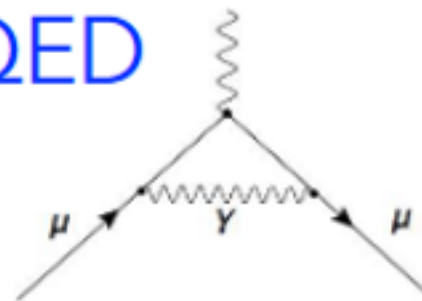
[L. Darmé, G. Grilli di Cortona, E. Nardi,](#)

[hep-ph/2112.09139 \(JHEP\)](#)

[hep-ph/2212.03877 \(PRD\)](#)

SM WP20 prediction from the TI White Paper (0.37 ppm)

QED

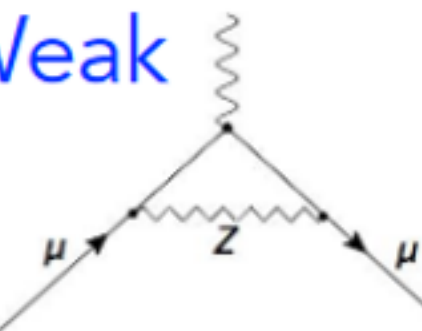


+ ...

$$116\,584\,718.9(1) \times 10^{-11}$$

0.001 ppm

Weak



+ ...

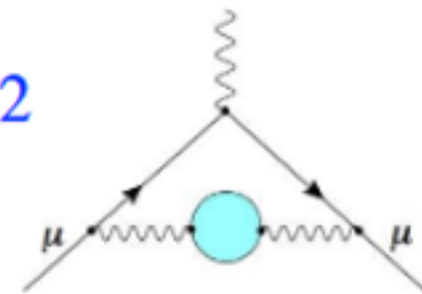
$$153.6(1.0) \times 10^{-11}$$

0.01 ppm

Hadronic...

...Vacuum Polarization (HVP)

$\alpha^2$



+ ...

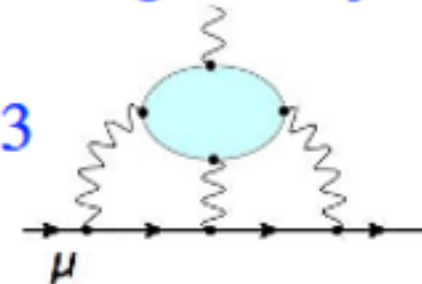
$$6845(40) \times 10^{-11}$$

[0.6%]

0.34 ppm

...Light-by-Light (HLbL)

$\alpha^3$



+ ...

$$92(18) \times 10^{-11}$$

[20%]

0.15 ppm

➤ Uncertainty dominated by hadronic contributions, now  $\delta \text{HVP} > \delta \text{HLbL}$

# Subtle effects in high precision physics: the $(g-2)_\mu$ anomalies

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hep-ph/2112.09139 (JHEP)

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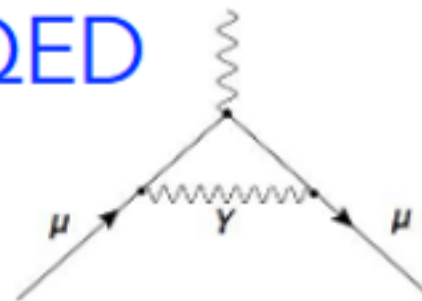
HPV is a non-perturbative contribution.

It can be estimated from data  
(via dispersion relations)

or via non-perturbative methods  
(lattice QCD)

SM WP20 prediction from the TI White Paper (0.37 ppm)

QED

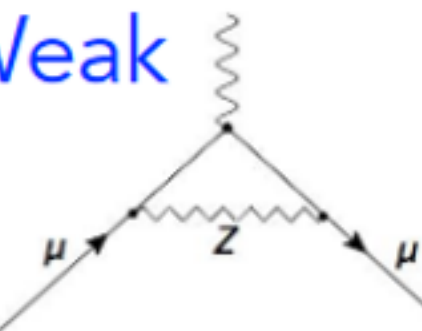


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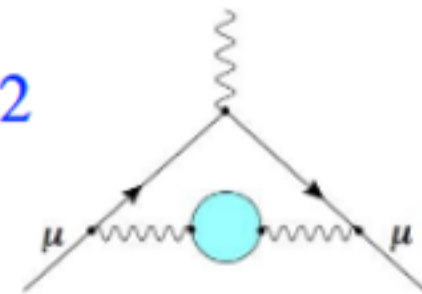
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+...

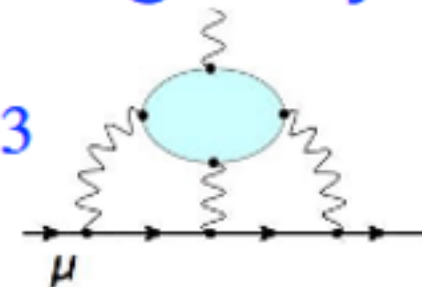
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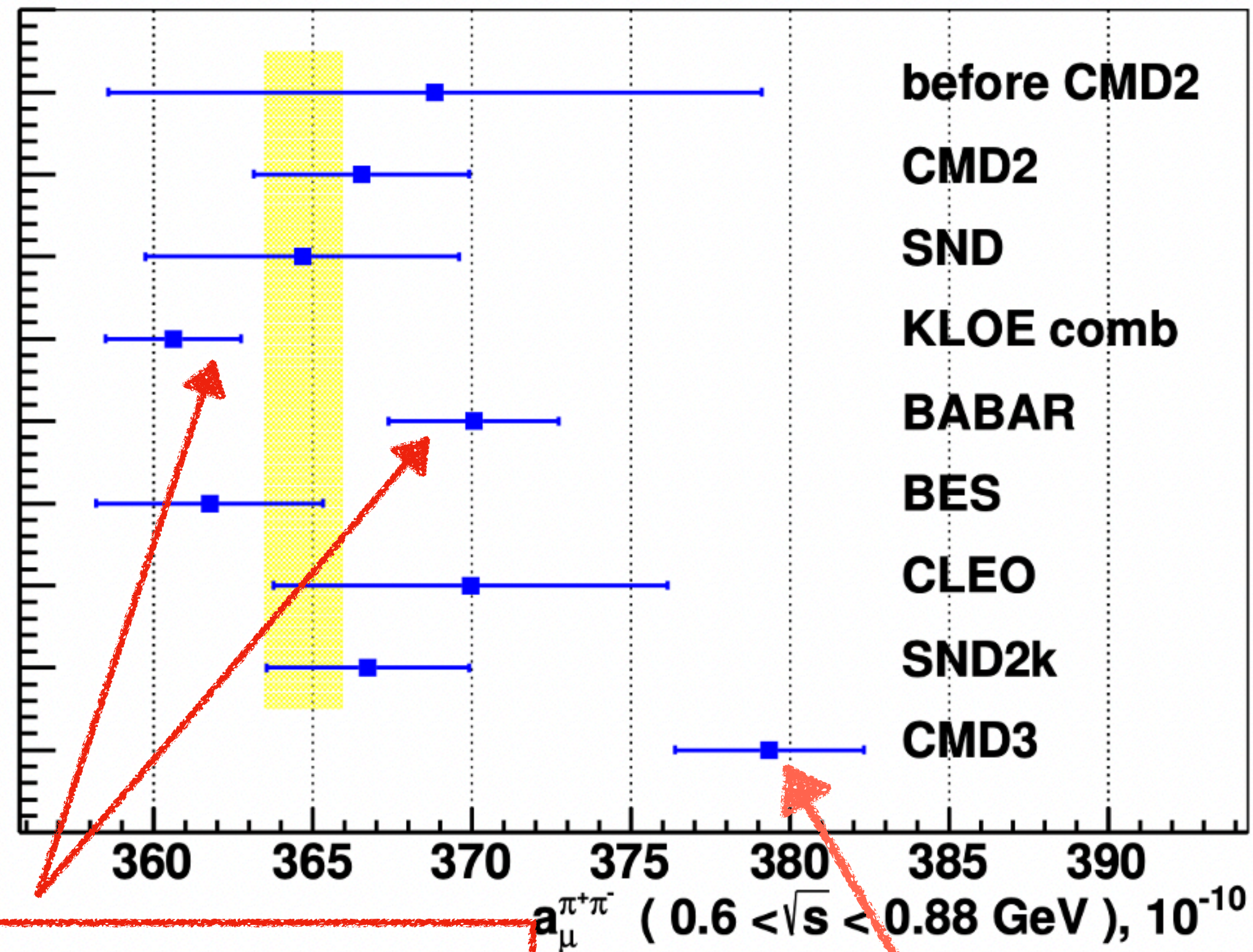
0.15 ppm

➤ Uncertainty dominated by hadronic contributions, now  $\delta \text{HVP} > \delta \text{HLbL}$



# Discrepancies in the different estimates of $a_\mu^{\text{HVP}}$

$\sigma(e^+e^- \rightarrow \pi^+ \pi^-)$  data



$\sim 3\sigma$  tension between  
KLOE and BaBaR

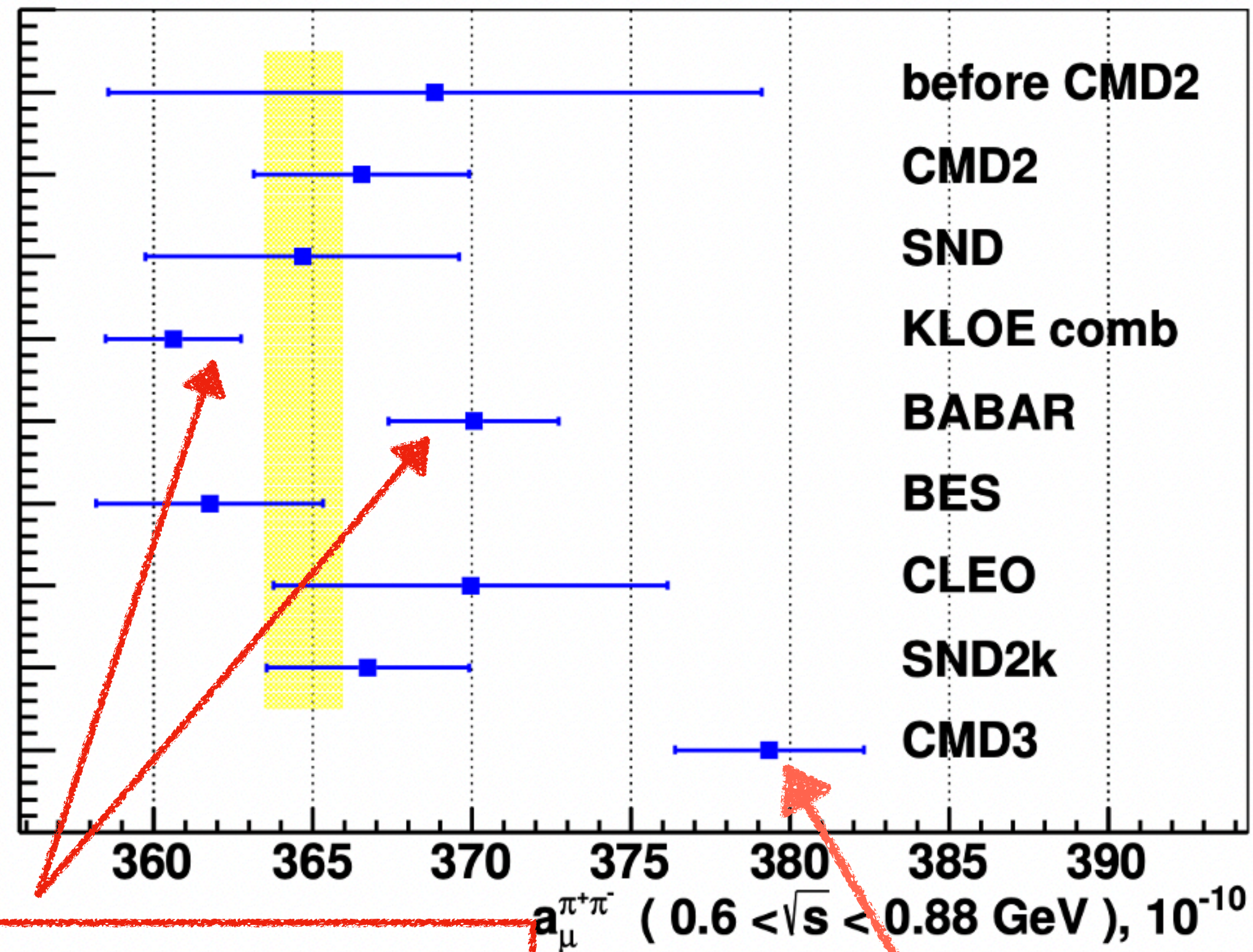
$\sim 5\sigma$  with CMD3 (2023)

Embarrassing disagreement



# Discrepancies in the different estimates of $a_\mu^{\text{HVP}}$

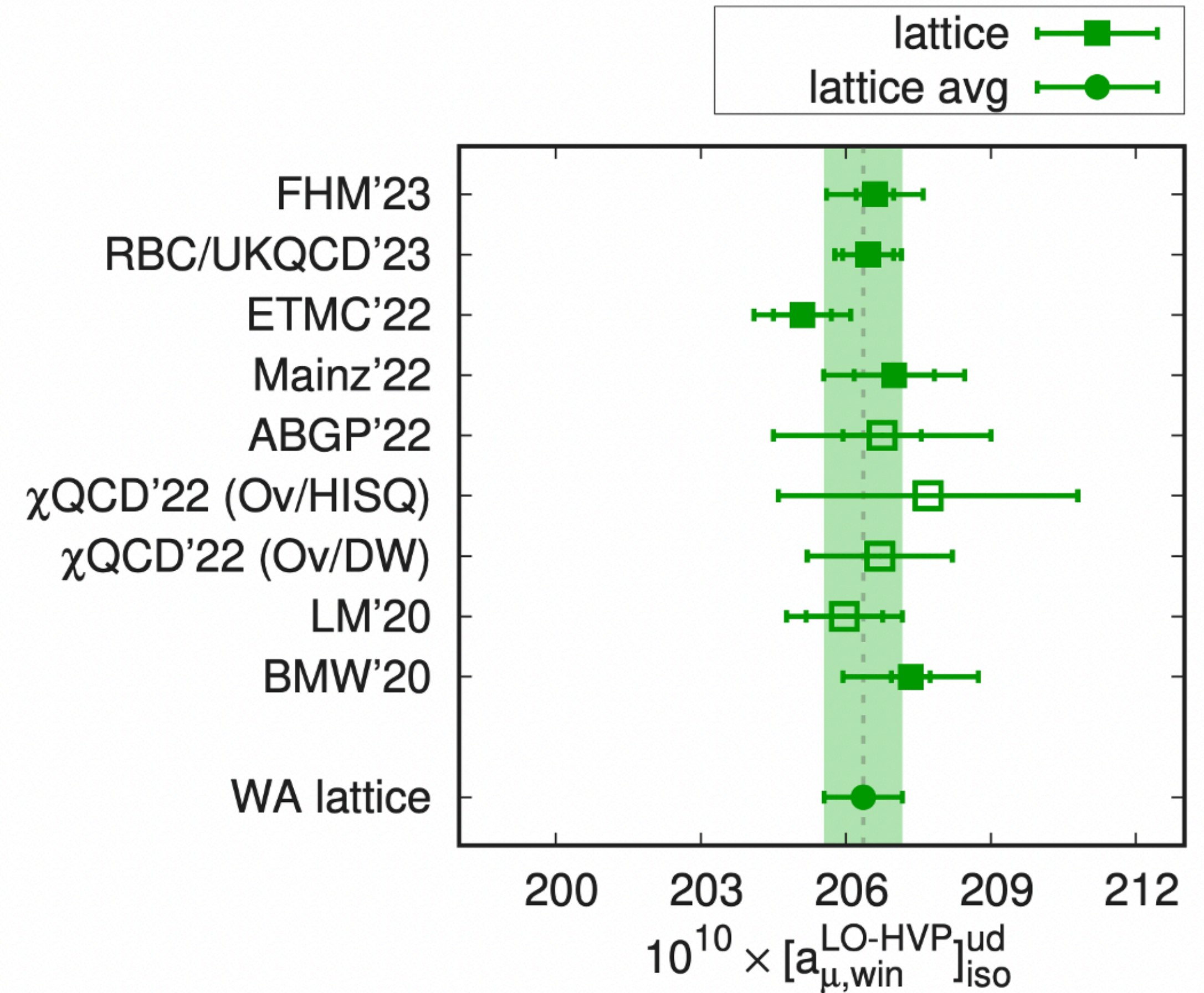
$\sigma(e^+e^- \rightarrow \pi^+ \pi^-)$  data



$\sim 3\sigma$  tension between KLOE and BaBaR

$\sim 5\sigma$  with CMD3 (2023)

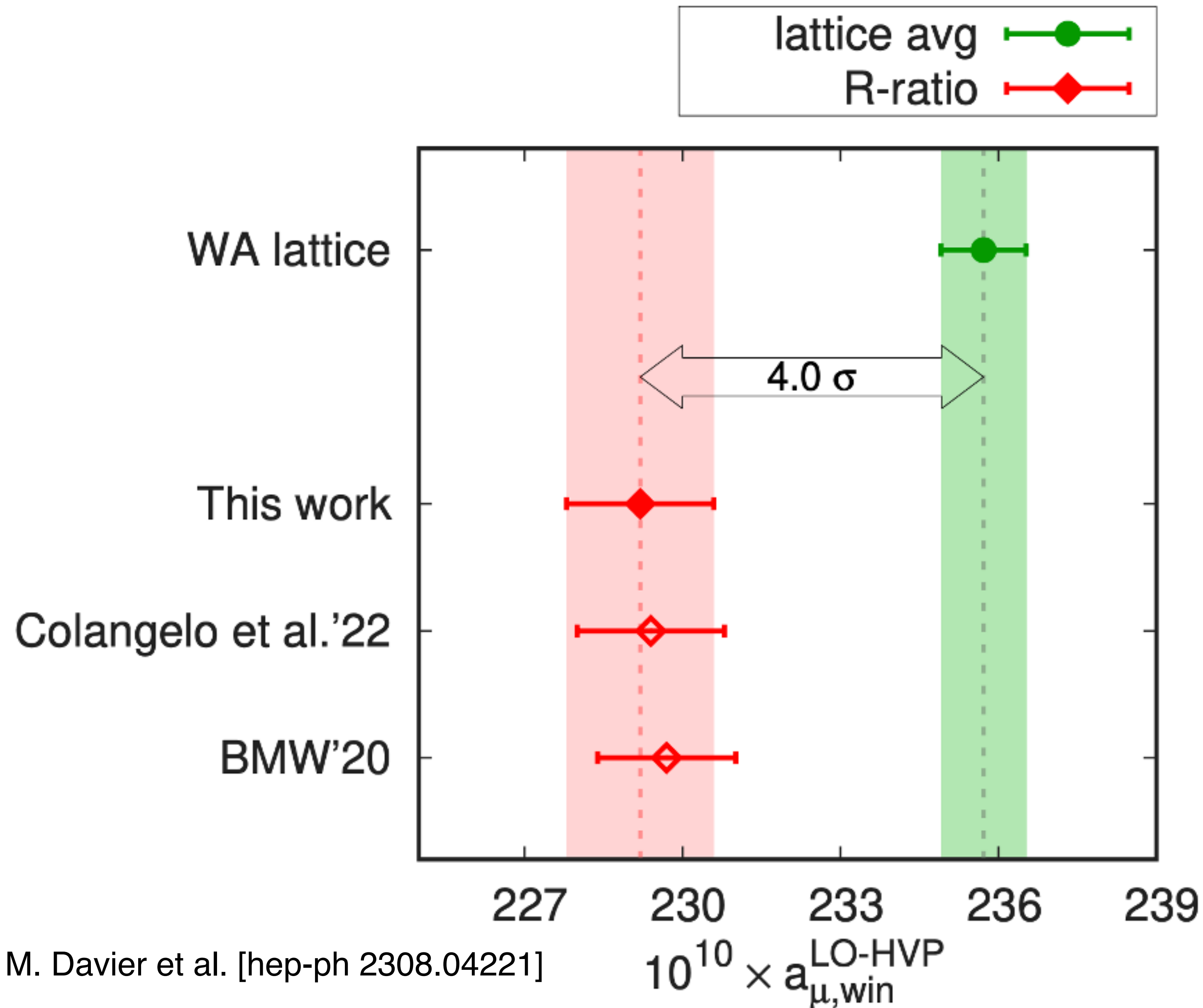
Embarrassing disagreement



Very good agreement



# Discrepancies in the different estimates of $a_\mu^{\text{HVP}}$



Can it be possible to reconcile KLOE with BaBar with CMD3, Data driven  $a_\mu^{\text{HVP}}$  with lattice, and explain  $(g-2)^{\text{exp}}$  vs.  $(g-2)^{\text{th}}$ ?



Measuring the Energy Dependence of the hadronic cross section  $\sigma_{\text{had}}(s)$ . Two strategies:

Radiative technique  
(KLOE, BaBar, BES)

$$[e^+e^-](s) \rightarrow [e^+e^-](s') + \gamma_{\text{ISR}} \rightarrow \text{had}(s') + \gamma_{\text{ISR}}$$

$$\text{beams: } s = (E_{b^+} + E_{b^-})^2 \text{ fixed}$$

Scanning technique  
(KLOE, BaBar, BES)

$$[e^+e^-](s) \rightarrow \text{had}(s)$$

$$\text{beams: } s = (E_{b^+} + E_{b^-})^2 \text{ variable}$$

# A Measurement of the hadronic cross section requires theoretical input

Luminosity dependent:

$$\sigma_{\text{had}} \propto N_{\text{had}} / \mathcal{L}_{e^+e^-}$$

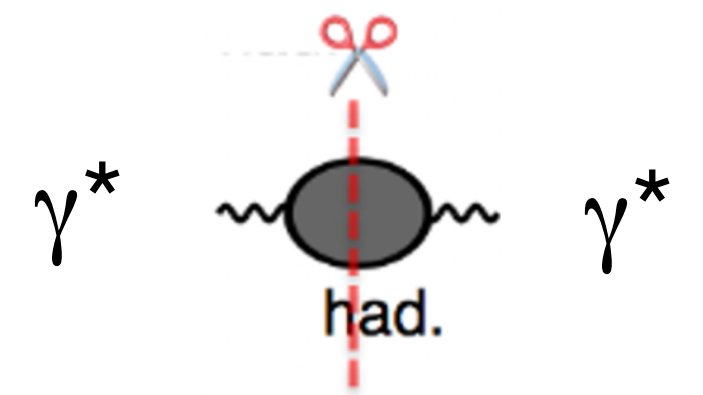
KLOE08, KLOE10

The luminosity is estimated by comparing high statistics measurements of  $e^+e^- \rightarrow e^+e^-$  events with the SM prediction for Bhabha scattering:

$$\mathcal{L}_{e^+e^-}^{\text{SM}} = \frac{N_{\text{Bha}}}{\sigma_{\text{eff}}^{\text{SM}}} \quad \leftarrow \text{Theory QED}$$

If there are additional  $e^+e^-$  events from some NP:  $\mathcal{L}_{e^+e^-} = \mathcal{L}_{e^+e^-}^{\text{SM}} \frac{\sigma_{\text{eff}}^{\text{SM}}}{\sigma_{\text{eff}}} < \mathcal{L}_{e^+e^-}^{\text{SM}} \Rightarrow$

$$\sigma_{\text{eff}} = \sigma_{\text{eff}}^{\text{SM}} (1 + \delta_R)$$



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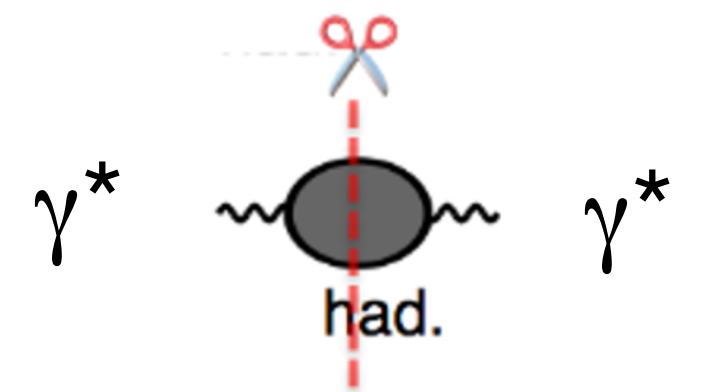
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Luminosity independent:

$$\sigma_{\pi^+\pi^-}^0 = \frac{N_{\pi^+\pi^-\gamma_{\text{ISR}}}}{N_{\mu^+\mu^-\gamma_{\text{ISR}}}} \sigma_{\mu^+\mu^-}^0$$

BaBar, BESIII, KLOE12

Theory QED





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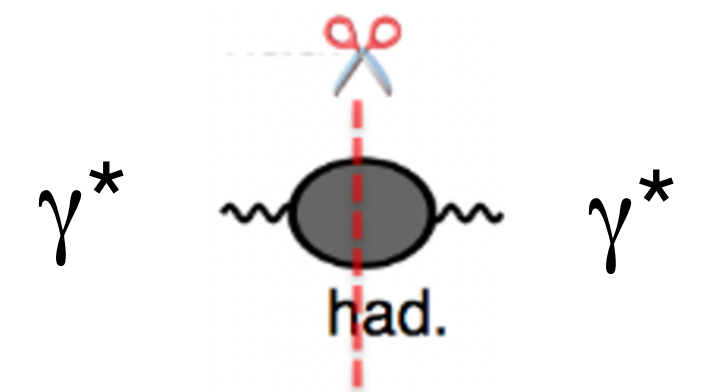
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$$\sigma_{\pi^+\pi^-}^0 = \frac{N_{\pi^+\pi^- \gamma_{\text{ISR}}}}{N_{\mu^+\mu^- \gamma_{\text{ISR}}}} \sigma_{\mu^+\mu^-}^0$$

BaBar, BESIII, KLOE12

Theory QED



If there are additional  $\mu^+\mu^-$   $\times$  events from some NP (i.e. not from  $e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-$ ) mimicking  $\mu^+\mu^- \gamma_{\text{ISR}}$  ( $\times$  invisible) they must be subtracted out

$$\sigma_{\pi^+\pi^-}^0 \longrightarrow \sigma_{\pi^+\pi^-}^{0(\gamma^*)} \simeq \sigma_{\pi^+\pi^-}^0 [1 + \delta_\mu(s')]$$

$$\delta_\mu(s') \equiv \frac{\sigma_{\mu\mu X}^{\text{NP}}(s')}{\sigma_{\mu\mu}(s')} \frac{\epsilon^{\text{NP}}}{\epsilon^{\text{SM}}}$$



Now, which could be a useful model ? We need NP at 1 GeV !!

We have borrowed an iDM model

$X = V$  Dark Photon

FEYNRULES

MadGraph5\_aMC@NLO

Shifts:  $\delta_R^{\text{KLOE08}}$  ,  $\delta_\mu^{\text{BESIII}}$  ,  $\delta_\mu^{\text{KLOE12}}$

For KLOE08

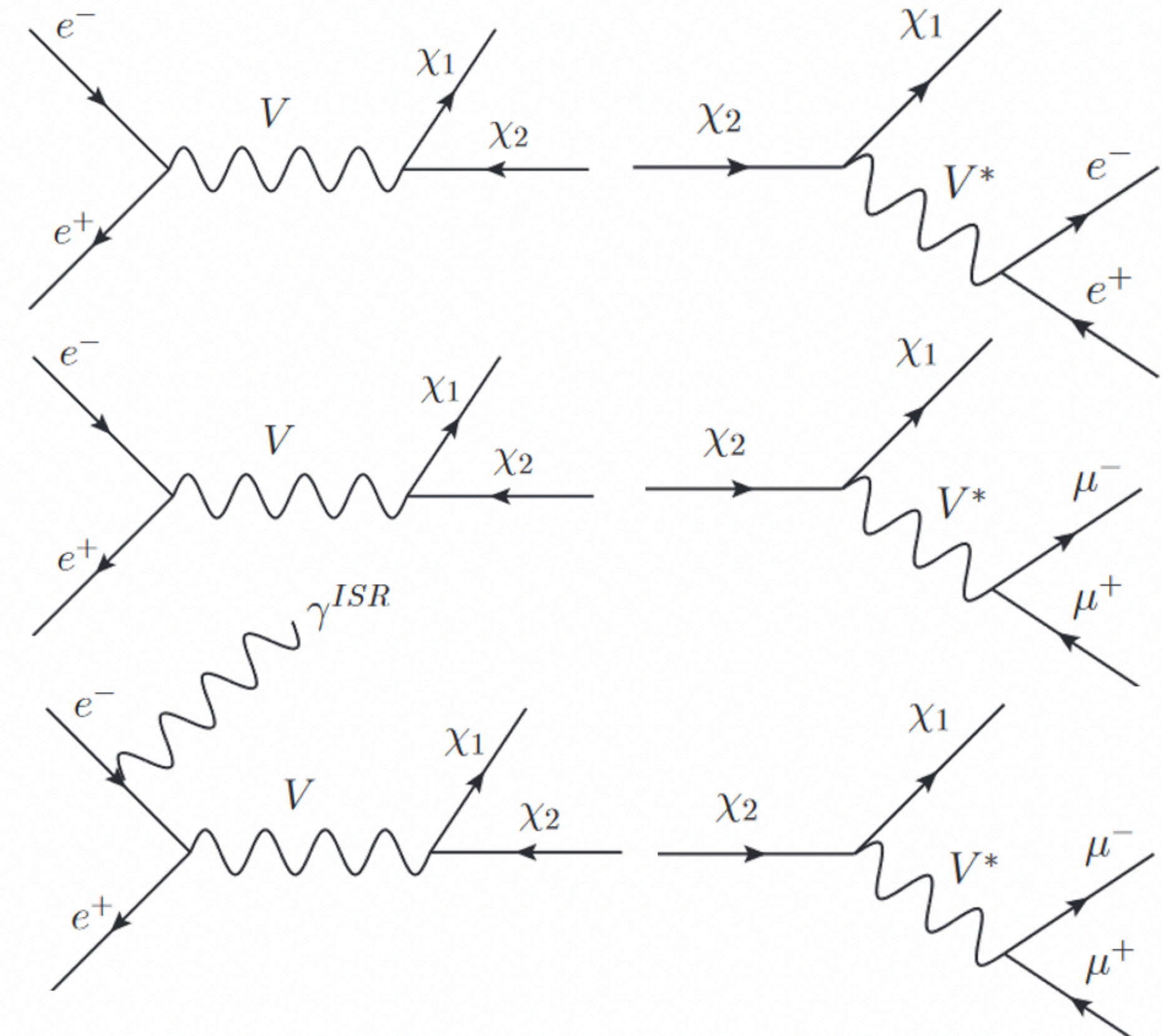
$$e^+e^- \rightarrow e^+e^- \chi_1 \chi_1$$

For KLOE12

$$e^+e^- \rightarrow \mu^+\mu^- \chi_1 \chi_1$$

For BESIII

$$e^+e^- \rightarrow \mu^+\mu^- \gamma \chi_1 \chi_1$$



To hide NP at the GeV **make the NP signature look like background** of standard searches:

- No bumps in  $(m_{e^+e^-})^2$  or  $(m_{\mu^+\mu^-})^2$  invariant mass (multi-body final state)
- Evade searches based on missing energy with charged particles in the final state



The largest shift needed is in KLOE data. So assume new  $X$  resonance with  $m_X \sim m_\phi$  (we also assume  $\Gamma_X \sim \Gamma_\phi$ ). Three KLOE measurements

KLOE08:  $\sqrt{s} = m_\phi$  *Luminosity method*

KLOE10:  $\sqrt{s} = m_\phi - 4.5 \Gamma_\phi$  *Luminosity method (in our model not affected by NP)*

KLOE12:  $\sqrt{s} = m_\phi$  *Luminosity **independent** method. Data fully correlated with KLOE08*

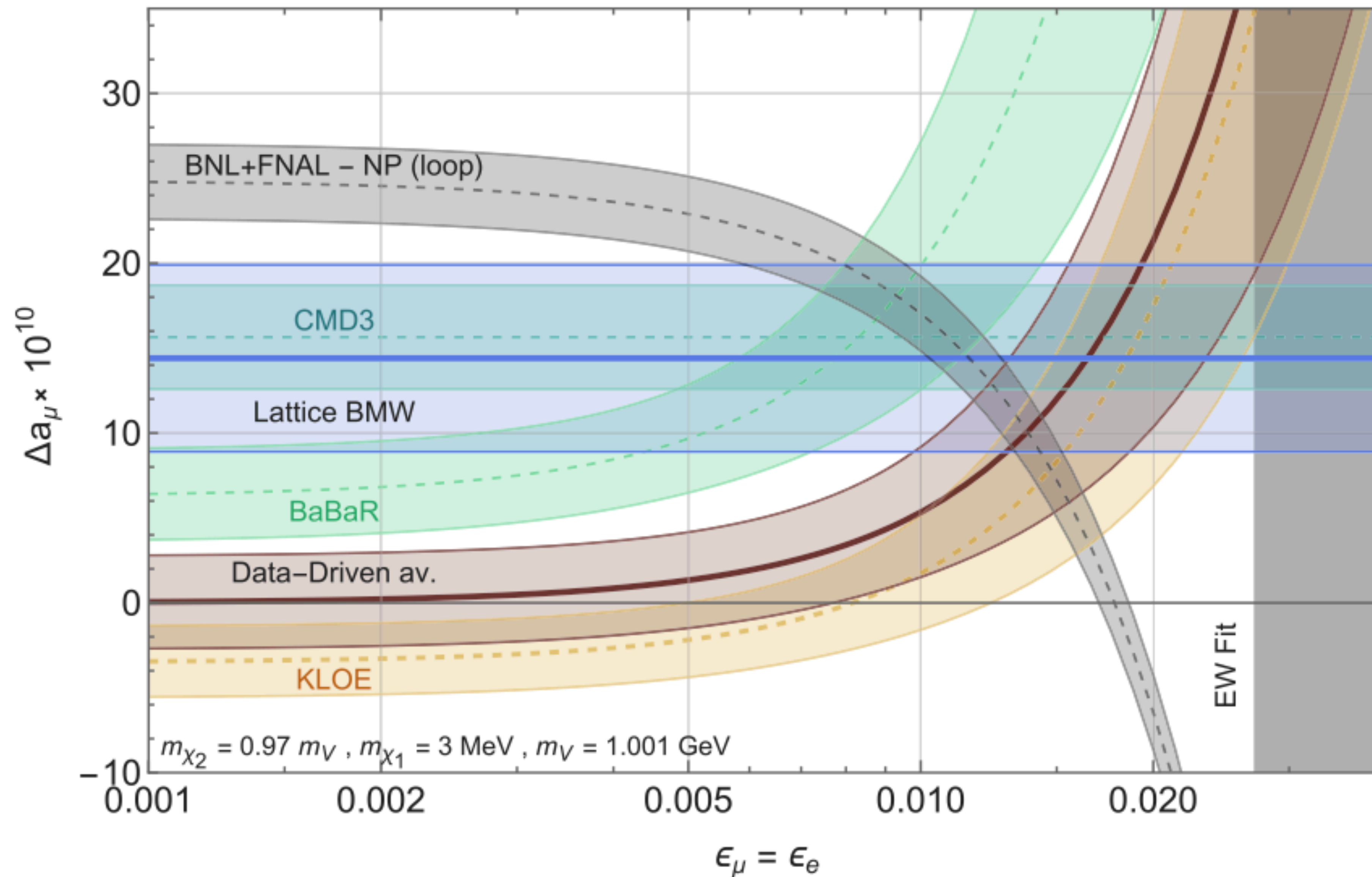
Although CoM far above  $m_\phi$ , BaBar and BESIII also receive corrections

BaBar12:  $\sqrt{s} = 10.6 \text{ GeV}$  *Luminosity independent ( $\mu$ ) method.*

BESIII:  $\sqrt{s} = 3.8 \text{ GeV}$  *Luminosity independent ( $\mu$ ) method.*

Experiments that exploit the ISR method to scan  $s'$  will generally be affected whenever the CoM energy is above the resonance even if not particularly close to the pole. This is because ISR photon emission can downgrade the effective  $e^+e^-$  collision energy to the right value to excite the resonance. (In our analysis: Included in BESIII but not in BaBar)

# Shifts in the prediction of the data-driven results



This idea was first put forth in

L. Darmé, G. Grilli di Cortona, E. Nardi, [hep-ph/2112.09139 \(JHEP\)](#)

The scenario (2021) predicted:

- No effects in scanning-method experiments  $\sqrt{s} \lesssim 1 \text{ GeV}$
- Lattice-Data driven discrepancy should not arise from the so called "short-distance window" (very roughly, for  $\sqrt{s} \gtrsim 1 \text{ GeV}$ )

This is in nice agreement with (2023) results: [[see hep-ph:2212.03877 \(PRD\)](#)]

- The CMD3 result (Feb. 2023) [[F.V. Ignatov et al., hep-ex:2302.08834.](#)]
- The Fermilab Latt., HPQCD, and MILC; RBC/UKQCD (Jan. 2023) Lattice results [[A. Bazavov et al. hep-lat:2301.08274 \(PRD\)](#); [T. Blum et al. \[hep-lat:2301.08696\] \(PRD\)](#)]

Thanks for your attention !