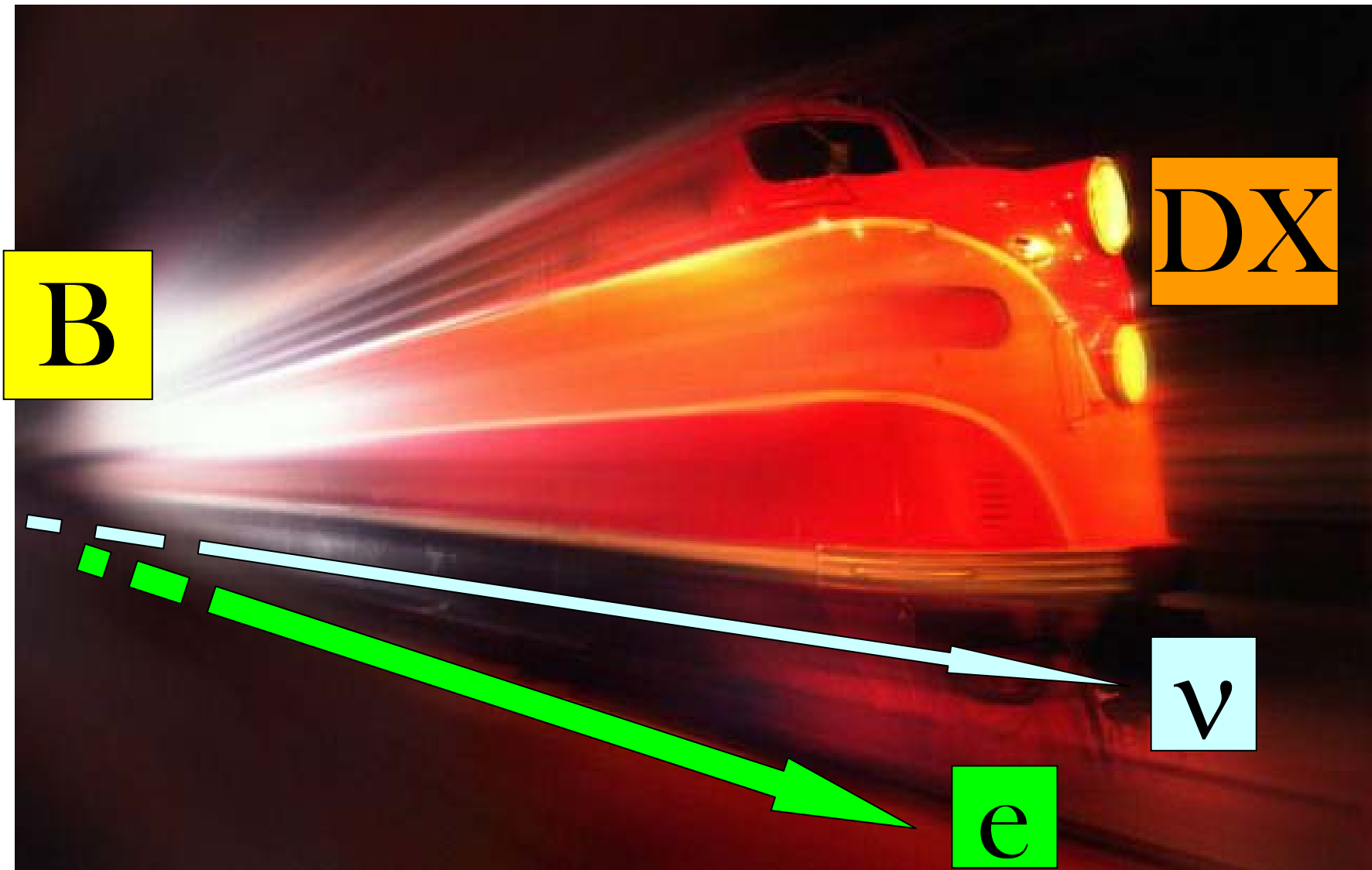


Can we understand $\bar{B} \rightarrow D^{(*)} X l \nu_l$ decays ?



February 4-6, 2013, Valencia

see also: <http://events.lal.in2p3.fr/WorkshopBdecays/>

P. Roudeau (thanks to A. Le Yaouanc and D. Becirevic)


Overall picture

Expt.:

$$\begin{aligned} B(B^0 \rightarrow X_c \mid \nu) &= (10.09 \pm 0.22)\% & \rightarrow B(B^0 \rightarrow D \mid \nu) &= (2.12 \pm 0.06)\% \\ & & \rightarrow B(B^0 \rightarrow D^* \mid \nu) &= (5.11 \pm 0.10)\% \\ & & \rightarrow B(B^0 \rightarrow D_1 \mid \nu) &= (0.58 \pm 0.05)\% \\ & & \rightarrow B(B^0 \rightarrow D_2^* \mid \nu) &= (0.29 \pm 0.03)\% \end{aligned}$$

It remains:

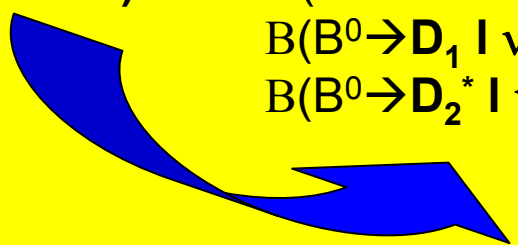
$$\begin{aligned} B(B^0 \rightarrow X_{c,\text{broad}} \mid \nu) &= (2.00 \pm 0.26)\% & \rightarrow B(B^0 \rightarrow D^{(*)} \pi \mid \nu)_{\text{broad}} &= (0.75 \pm 0.09)\% \\ & & \rightarrow B(B^0 \rightarrow D^{(*)} x \mid \nu)_{\text{broad}} &= (1.24 \pm 0.26)\% \\ & & & \ll x \gg \text{ being more than 1 pion} \end{aligned}$$



*About 20% of B-meson
semileptonic decays
are not well understood.*

Remaining questions in $B \rightarrow D^{(*)} \pi \ell \nu_l$

Expt.:

$$\begin{aligned} B(B^0 \rightarrow D \pi \ell \nu)_{\text{broad}} &= (0.42 \pm 0.06)\% & \leftrightarrow & B(B^0 \rightarrow D \pi \ell \nu)_{\text{narrow}} = (0.18 \pm 0.02)\% \\ B(B^0 \rightarrow D^* \pi \ell \nu)_{\text{broad}} &= (0.33 \pm 0.07)\% & \leftrightarrow & B(B^0 \rightarrow D^* \pi \ell \nu)_{\text{narrow}} = (0.50 \pm 0.04)\% \\ & & & B(B^0 \rightarrow D_1 \ell \nu) = (0.58 \pm 0.05)\% \\ & & & B(B^0 \rightarrow D_2^* \ell \nu) = (0.29 \pm 0.03)\% \end{aligned}$$


Theory (naïve):

$$B(B^0 \rightarrow D_0^* \ell \nu) \approx B(B^0 \rightarrow D_1' \ell \nu) \ll B(B^0 \rightarrow D_1 \ell \nu) \approx B(B^0 \rightarrow D_2^* \ell \nu)$$

- If we identify the $(D^{(*)} \pi)_{\text{broad}}$ final states with the D_0^* and D_1' , then there seems to be a contradiction with theory !

$$\tau_{3/2} > \tau_{1/2}$$

- Heavy meson Qq ; $J = j_q \oplus s_Q$, $j_q = L \oplus s_q$, $s_Q = s_q = 1/2$

- For $L = 1$, $j_q = 1/2$ or $3/2$

- The heavy quark spin is decoupled, meson properties depend on j_q

- Adding the heavy quark gives 2 doublets

$j_q = 1/2 \rightarrow J^P = 0^+, 1^+$ broad (D_0^* , D_1), mainly S-wave decays

$j_q = 3/2 \rightarrow J^P = 1^+, 2^+$ narrow (D_1^* , D_2^*), mainly D-wave decays

- Within a doublet, states (are expected) to have similar properties. Production rates in B decays governed by 2 form factors: $\tau_{1/2}(w)$ and $\tau_{3/2}(w)$, $w = v_B \cdot v_D$ (in the infinite mass limit).

$$\tau_{3/2}(1) \simeq 0.54, \quad \tau_{1/2}(1) \simeq 0.22 \quad \text{Quark model}$$

$$\tau_{3/2}(1) = 0.528(23), \quad \tau_{1/2}(1) = 0.297(26) \quad \text{LQCD}$$

$B(B^0 \rightarrow D_{3/2,1/2} \ell \nu)$ depend on: $\tau_{3/2}^2(1) / \tau_{1/2}^2(1) \sim 3 - 6$

slope of ff. versus $w \sim 0.7$

decay rate expression (spin) ~ 2.2

Total: $5 - 9$

-Need better evaluation of uncert. and of other effects as finite mass corrections

The $B \rightarrow D \pi l \nu_l$ decay channel

Expt.:

$$B(B^0 \rightarrow D \pi l \nu)_{\text{broad}} = (0.42 \pm 0.06)\% \leftrightarrow B(B^0 \rightarrow D \pi l \nu)_{\text{narrow}} = (0.18 \pm 0.02)\%$$

Belle analysis:

$$B(B^0 \rightarrow D_0^* l \nu) = (0.30 \pm 0.10 \pm 0.07)\%$$

$$B(B^- \rightarrow D_0^* l \nu) = (0.36 \pm 0.06 \pm 0.09)\%$$

Babar analysis:

$$(0.66 \pm 0.12 \pm 0.09)\%$$

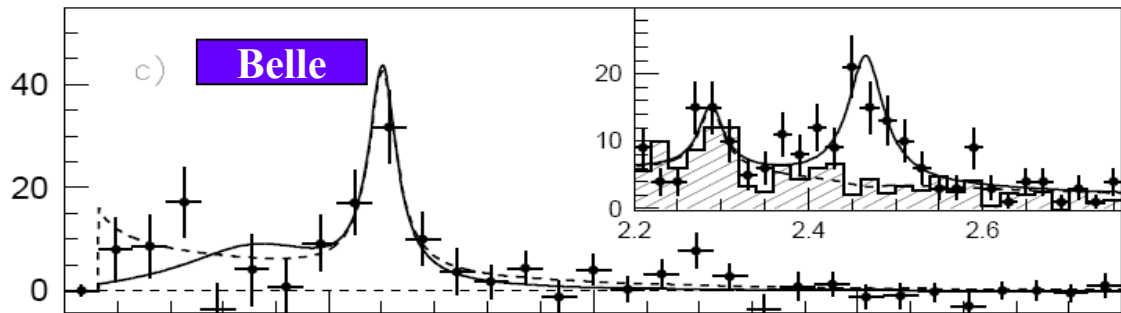
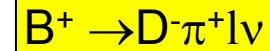
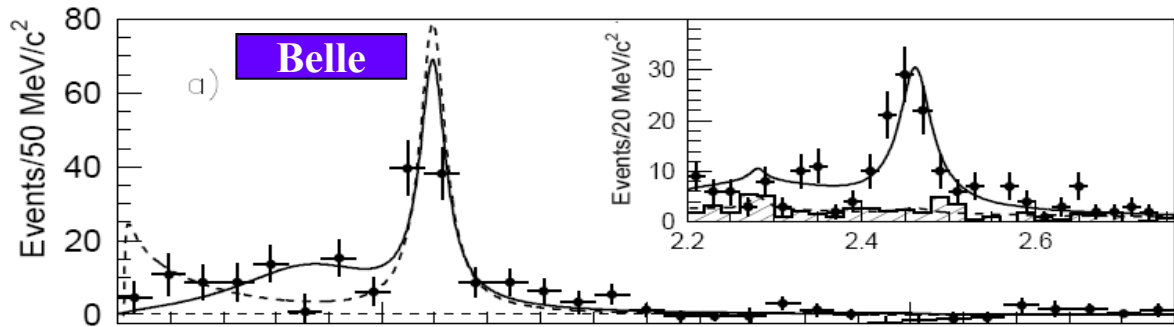
$$(0.39 \pm 0.08 \pm 0.06)\%$$

HFAG average:

$$B(B^0 \rightarrow D_0^* l \nu) = (0.40 \pm 0.08)\%$$

- Compatible results between BaBar and Belle
- The D_0^* can account for all the $(D \pi)_{\text{broad}}$ component but uncert. are large
- In practice there are differences between the 2 analyses.

Belle analysis

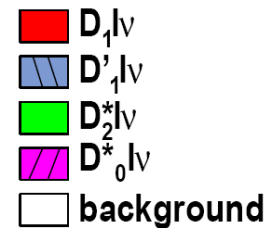
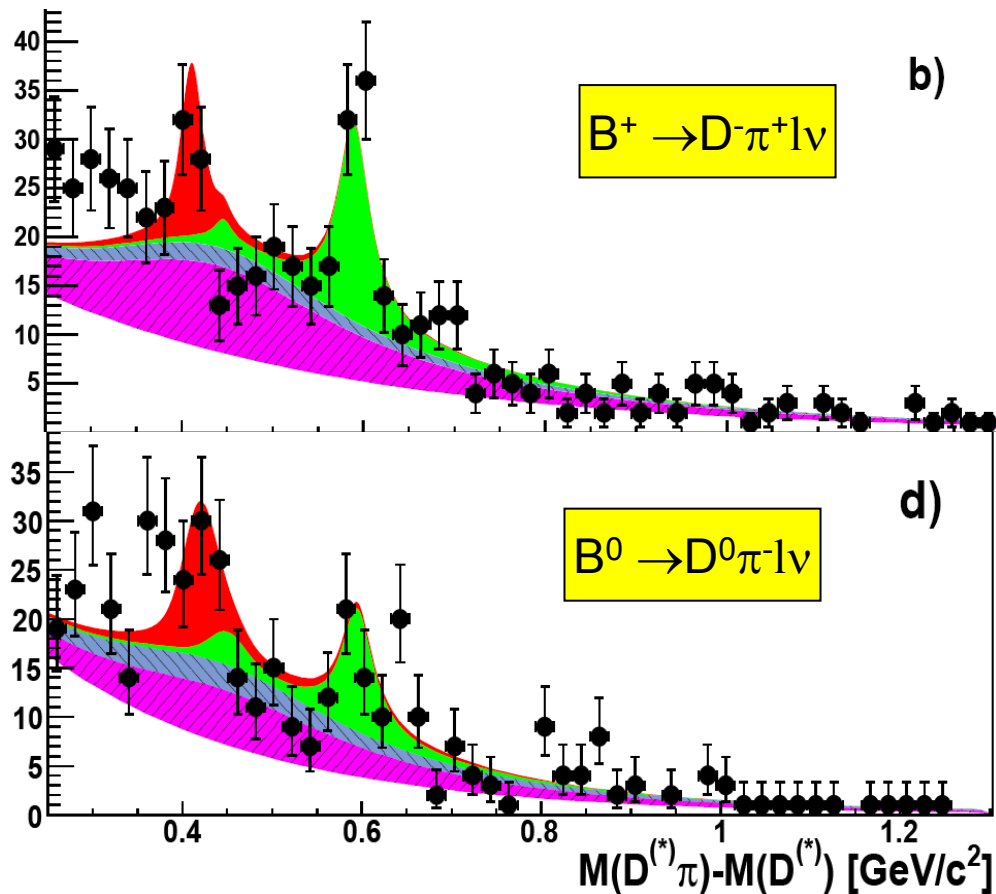


2 2.4 2.8 3.2 3.6 $D\pi$ mass

$-D_0^* + D_2^*$ favoured over $D_V + D_2^*$ by 2.8 sigmas

and background $D^{(*)}\pi$ mass spectra. The signal function includes all orbitally excited D^{**} contributing to the given final state (D_0 and D_2^* to $D\pi$ and D_1, D_1', D_2^* to $D^*\pi$), each of which is described by a relativistic Breit-Wigner function for a known orbital momenta, and a non-resonant part described by the Goity-Roberts model [16]. D^{**} masses and widths are

Babar analysis



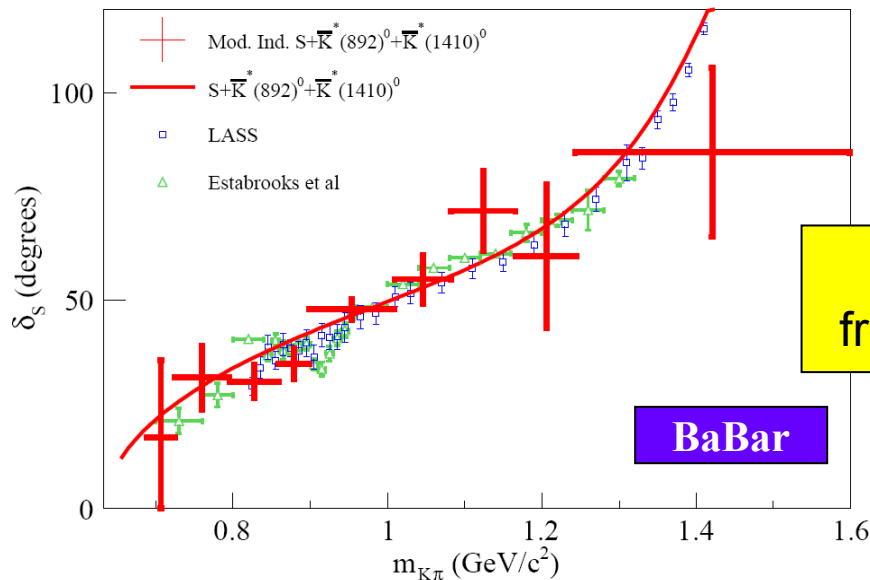
Larger window on $m_{\pi l \nu}$ than in Belle (keeps soft π).

Excess of evts at low mass attributed to $D \pi l \nu_1$ not included in the simulation.

- resonances do not include « Goity-Roberts » effects
- fitted model assumes only D^{**} states

Comments on present analyses

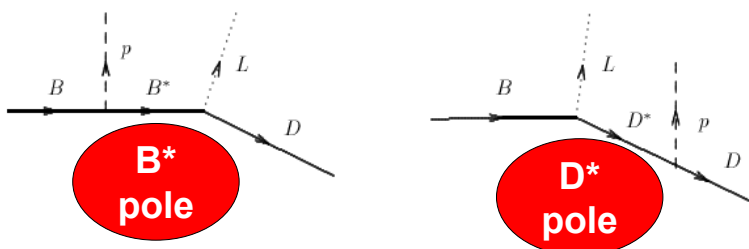
- Agreement between BaBar and Belle is a bit « artificial »
- There seems to be an excess of evts at low mass :
“à la Goity-Roberts”? D_V^* ?
- Most probably the D_0^* is only a fraction of the $(D \pi)_{\text{broad}}$
- What is the equivalent of the $K_0^*(800)$ for charm ?
- Radial excitations?



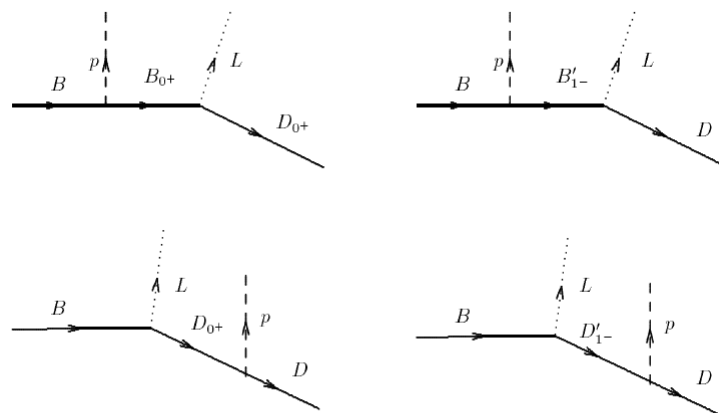
S-wave phase
from $D^+ \rightarrow K^- \pi^+ e^+ \nu_e$

What can be done ?

- Get expressions from theorists for $d\mathcal{B}(B^0 \rightarrow D \pi | \nu) / dx^5$ (tests can be done on $D^+ \rightarrow K^- \pi^+ e^+ \nu_e$?)
- Can one normalize the D^* (B^*) pole contribution(s) ?
- Use $B^0 \rightarrow D \pi \pi$, which has larger statistics, to understand the $(D \pi)_{\text{broad}}$ components
- Use $B^- \rightarrow D^+ \pi^- \pi^-$ to measure the phase of the $D_0^* \rightarrow D \pi$ versus the $D \pi$ mass.
- Have new spectra from BaBar with similar cuts as in Belle

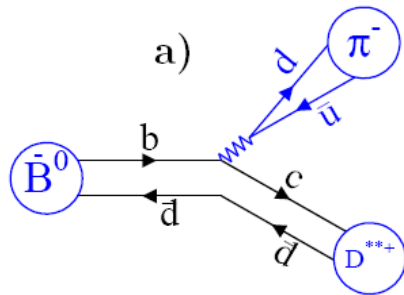


NR contributions in $B \rightarrow D \pi | \nu$ decays



Resonant contributions

$\bar{B}^0 \rightarrow D^0 \pi^+ \pi^-$

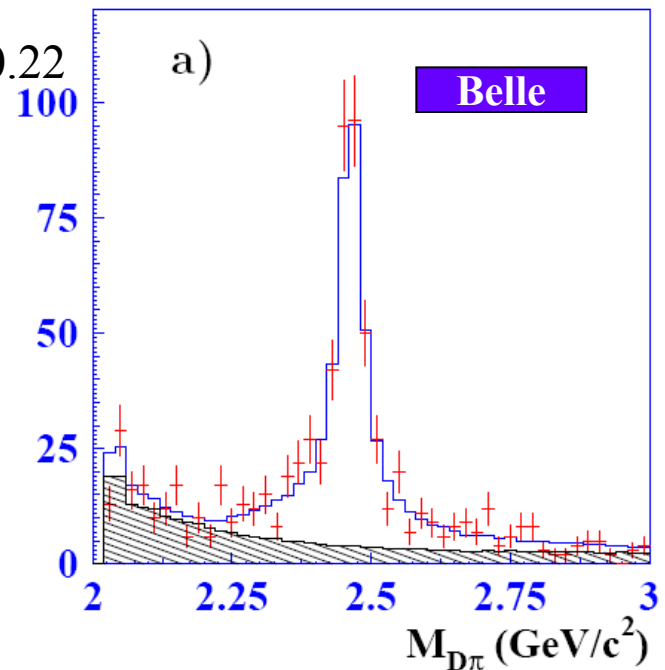


Type I decay, can be related to sl. decay at $q^2 = m_\pi^2 \sim 0$, using factorization

Results from Belle (published) and BaBar (prelim.) are not in nice agreement.

Belle	
$\mathcal{B}_{B \rightarrow D_0^* \pi} \mathcal{B}_{D_0^* \rightarrow D \pi} (10^{-4})$	$0.60 \pm 0.13 \pm 0.15 \pm 0.22$
$\phi_{D_0^*}$	-3.00 ± 0.13
$M_{D_0^*}, (MeV/c^2)$	2308.0
$\Gamma_{D_0^*}, (MeV/c^2)$	276.0
$\mathcal{B}_{B \rightarrow D_v^* \pi} \mathcal{B}_{D_v^* \rightarrow D \pi} (10^{-4})$	0.88 ± 0.13
$\phi_{D_v^*}$	-2.62 ± 0.15

- significant D_v^* component
- LHCb can improve the accuracy
- difficult analysis



$\bar{B}^0 \rightarrow D^{0(*)} \pi^+ \pi^-$

$B_d^0 \rightarrow \bar{D}^{**} \pi^+$	theory	expt.
\bar{D}_2^*	1.1×10^{-3}	$(0.49 \pm 0.07) \times 10^{-3}$
\bar{D}_1	1.3×10^{-3}	$(8.2_{-1.7}^{+2.5}) \times 10^{-4}$
\bar{D}'_1	1.1×10^{-4}	$< 10^{-4} (90\% C.L.)$
\bar{D}_0^*	1.3×10^{-4}	$[0.3, 3.4] \times 10^{-4}$

$B_d^0 \rightarrow \bar{D}^{**} e^+ \nu_e$		
\bar{D}_2^*	0.7×10^{-2}	$(0.29 \pm 0.03) \times 10^{-2}$
\bar{D}_1	0.45×10^{-2}	$(0.58 \pm 0.05) \times 10^{-2}$
\bar{D}'_1	0.7×10^{-3}	$[0., 3.2] \times 10^{-3}$
\bar{D}_0^*	0.6×10^{-3}	$(3.5 \pm 0.7) \times 10^{-3}$

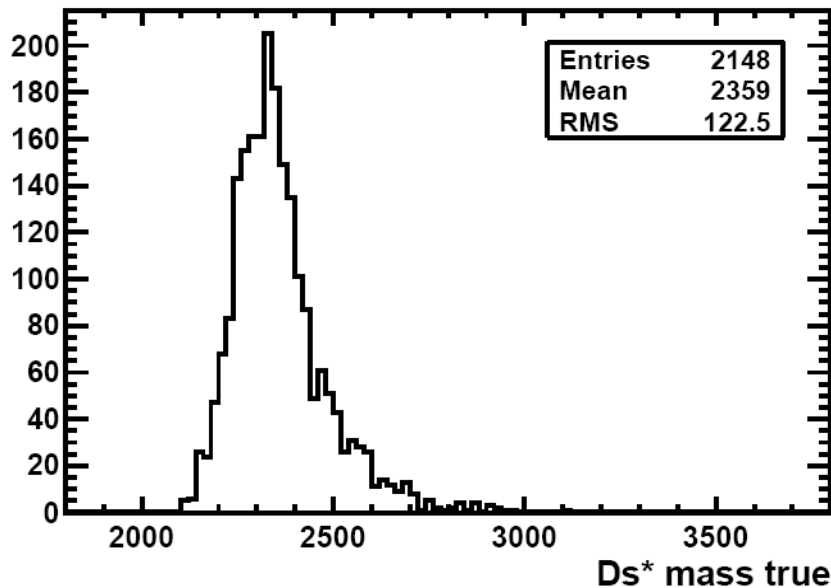
Need better accuracy

- theory uncertainties ?
- rough agreement between th. and expt. in nl decays and for narrow states in sl. decays
- disagreement for broad states in sl. decays

$$B^0_s \rightarrow D_{0s}^{*-} \pi^+, D_{0s}^{*-} \rightarrow D_s^- \pi^0$$

- This is a type I diagram
- The D_{0s}^{*-} is very narrow (avoid the problem of measuring broad states)
- ... unfortunately needs to reconstruct a soft π^0 (missed ?)
- so ... signal expected to be relatively broad (use of kinematic constraints at LHCb)

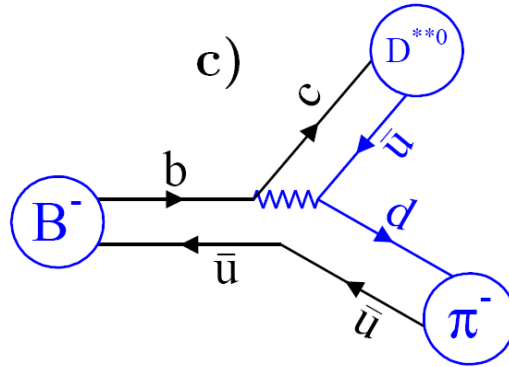
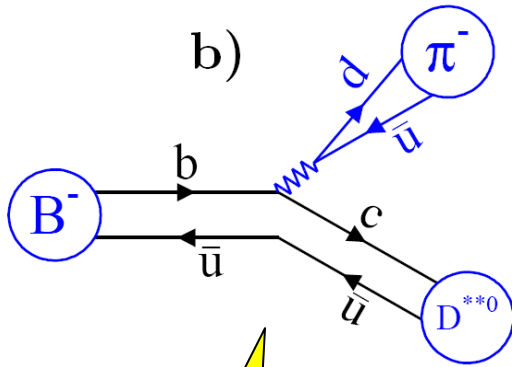
← LHCb



- expect few hundred evts/ fb⁻¹
- background level ?

[c.f. arXiv:1206.5869 [hep-ph]]

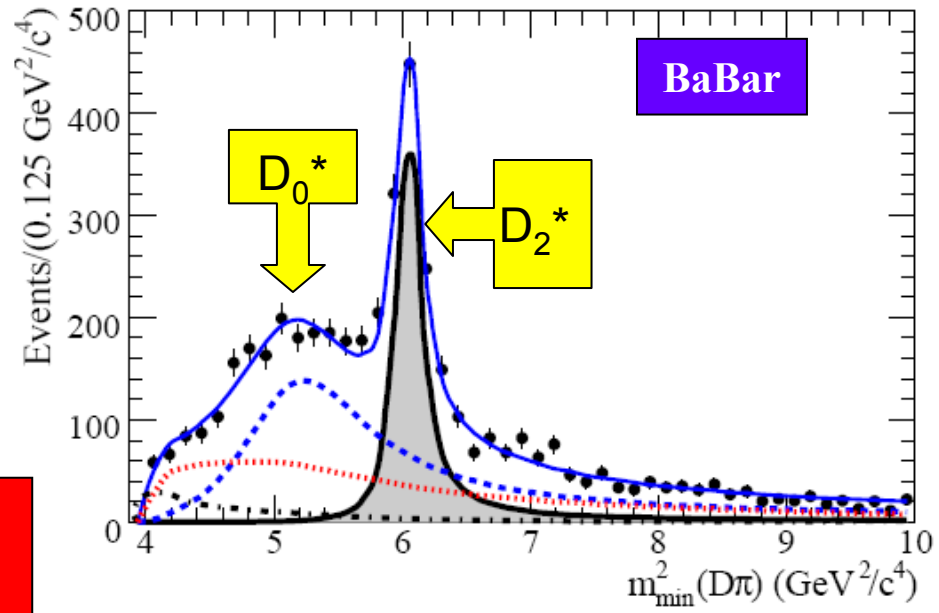
$B^- \rightarrow D^+ \pi \pi$



Type III decay, can be used to measure the $D\pi$ S-wave phase

Is the D_0^ a simple Breit-Wigner?*

- large signal, rather small backg.
- LHCb can improve the accuracy



LHCb

The $B \rightarrow D^* \pi l \nu_l$ decay channel

Expt.:

$$B(B^0 \rightarrow D^* \pi l \nu)_{\text{broad}} = (0.33 \pm 0.07)\% \leftrightarrow B(B^0 \rightarrow D^* \pi l \nu)_{\text{narrow}} = (0.50 \pm 0.04)\%$$

Belle analysis:

$$B(B^- \rightarrow D_1' l \nu) = (-0.04 \pm 0.08 \pm 0.10)\%$$

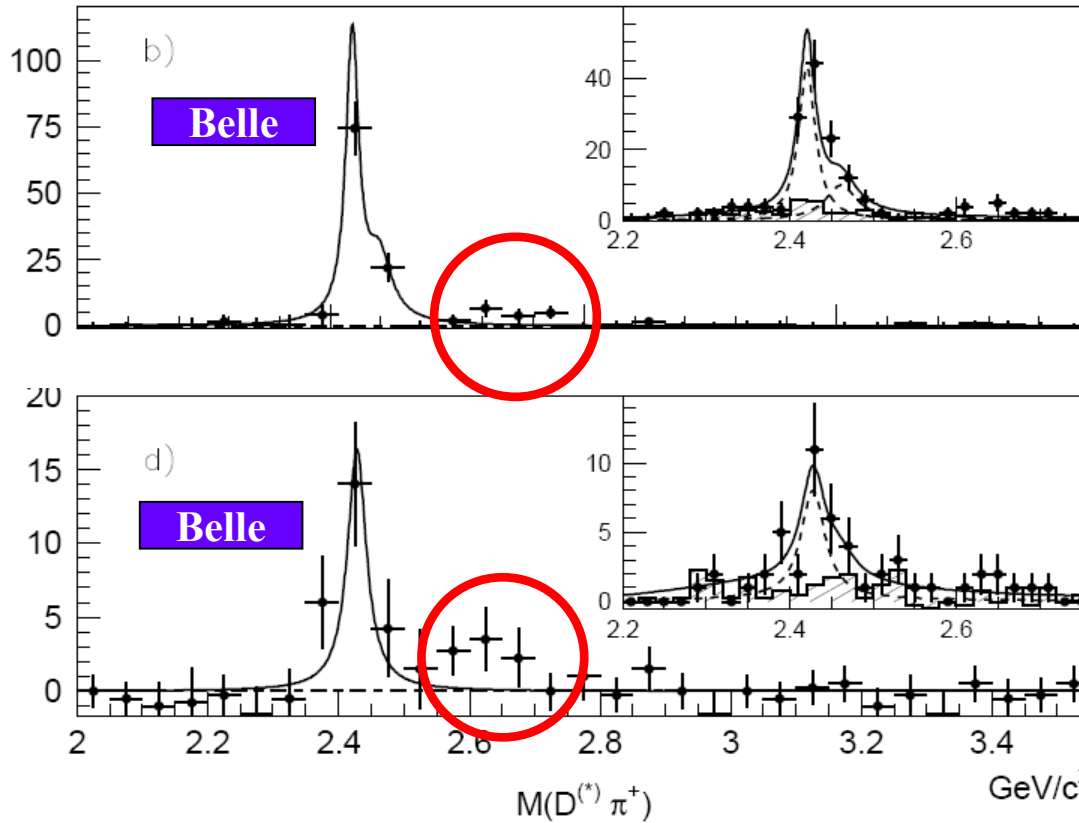
Babar analysis:

$$(0.38 \pm 0.06 \pm 0.06)\%$$

HFAG average: ??

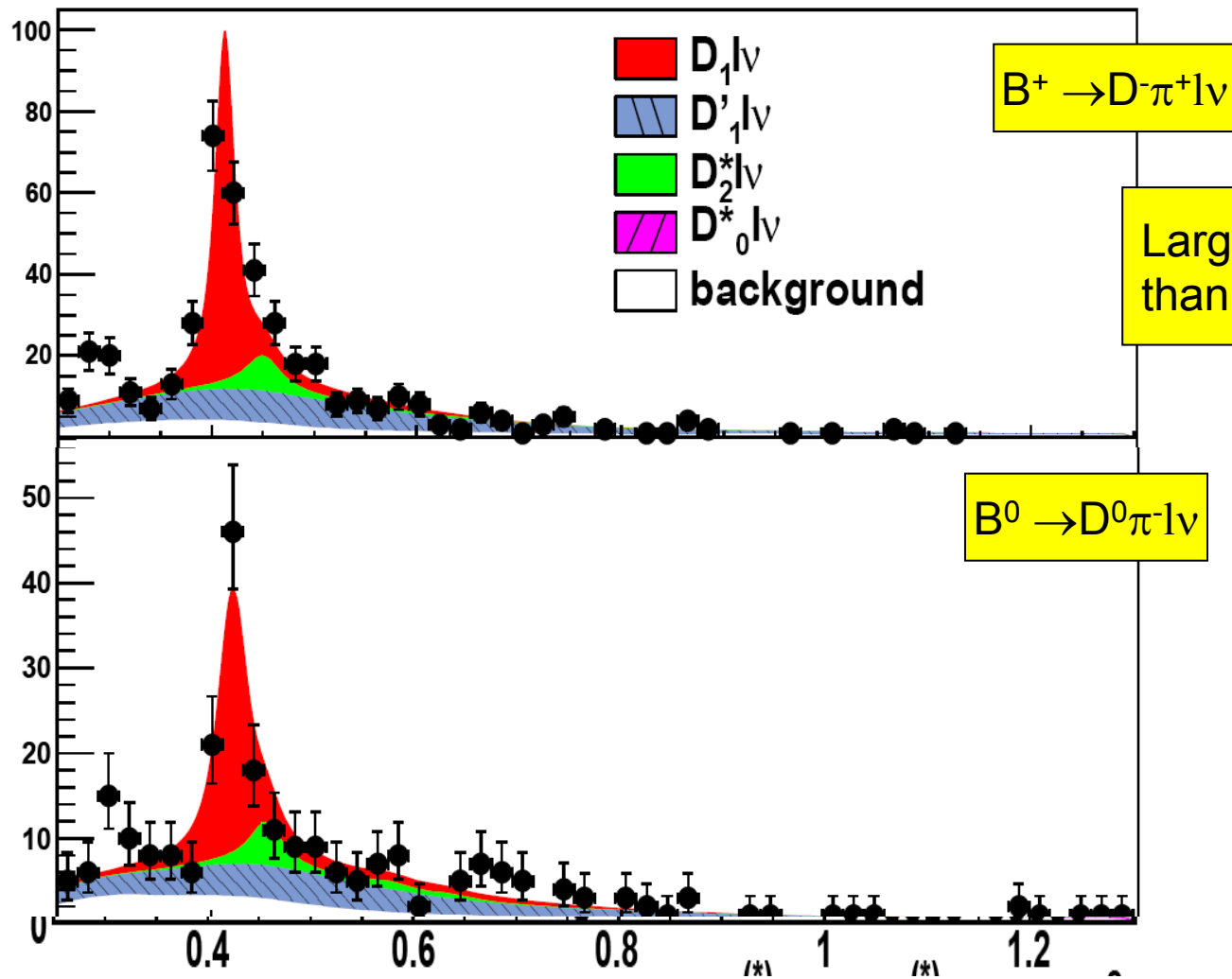
- BaBar and Belle not in « good » agreement ($\sim 3 \sigma$)
- Can BaBar tighten the cuts on $m_{\text{min}}^2(\nu)$?

Belle analysis



- no evidence for D_1'
- some « excess » around 2.6 GeV ?

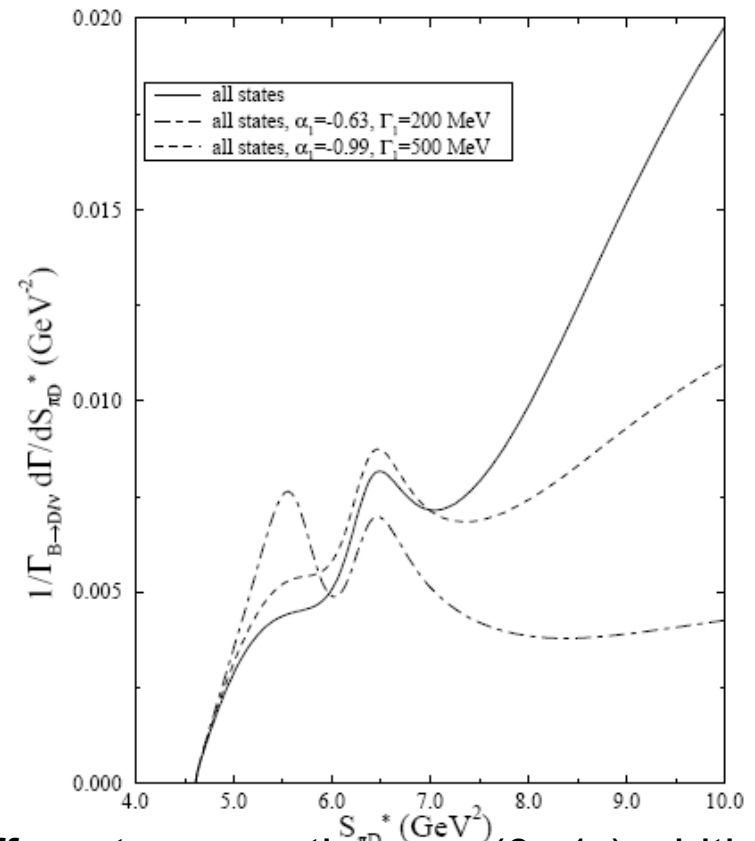
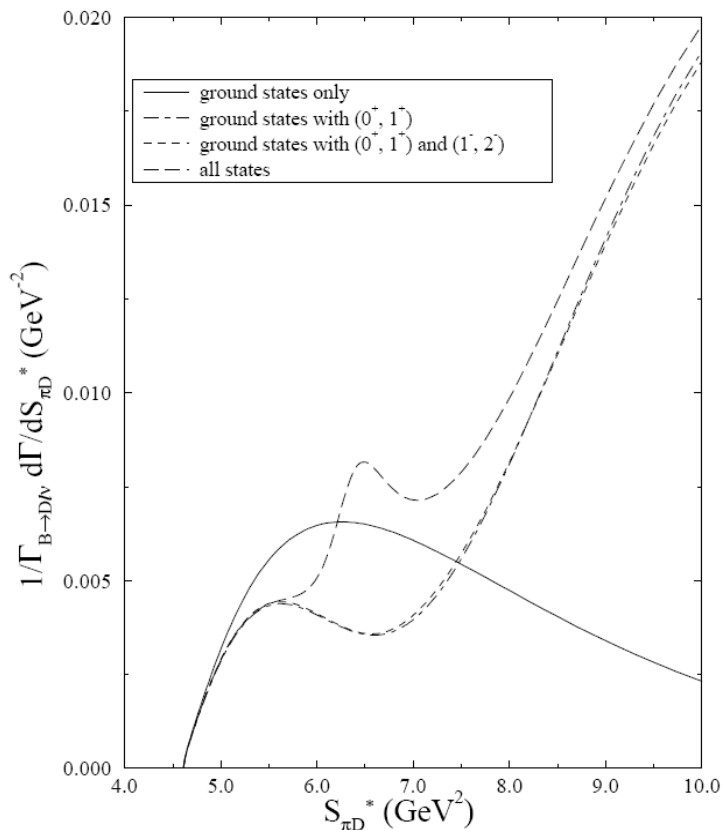
Babar analysis



Comments on present analyses

- Poor agreement between BaBar and Belle

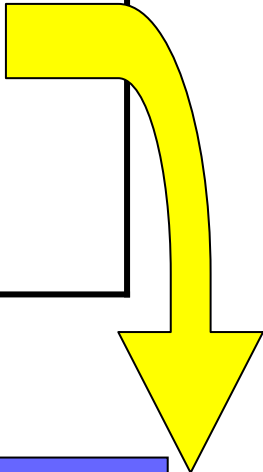
-The “Goity-Roberts” model predicts contributions at high masses (validity?), what about $(1^-, 2^-)$? The non-resonant component is expected to be large ... normally it can be absolutely normalized!



With different assumptions on $(0^+, 1^+)$ width

Radial excitations

State	decay		Final state	Angular mom.
D'(2550) J^P=0⁻ M=2540 MeV Γ=130 MeV	Dπ	No		
	D*π	Yes	D*π	L=1
	D₀* (2400)π	Yes	Dππ	L=0
	D₁π	No		
	D₂* (2460)π	Yes	Dππ, D*ππ	L=2
D*(2600) J^P=1⁻ M=2610 MeV Γ=93 MeV	Dπ	Yes	Dπ	L=1
	D*π	Yes	D*π	L=1
	D₀* (2400)π	No		
	D₁π	Yes	D*ππ, Dπππ	L=0
	D₂* (2460)π	Yes	Dππ, D*ππ	L=2



- Relatively narrow
 - L=0 or 1 presumably dominant

BaBar
 $B(D\pi) / B(D^*\pi) = 0.32 \pm 0.02 \pm 0.09$

Production rates in cc events

State	Efficiency (%)	BaBar Yield ($\times 10^{-3}$)	Yield corrected ($\times 10^{-7}$)
$D_1(2420)^0$	1.09 ± 0.03	$214.6 \pm 1.2 \pm 6.4$	$4.38 \pm 0.13 \pm 0.19$
$D_2^*(2460)^0$	1.12 ± 0.04	$136 \pm 2 \pm 13$	$4.67 \pm 0.45 \pm 0.36$
$D'(2550)^0$	1.14 ± 0.04	$98.4 \pm 8.2 \pm 38$	$(1.3 \pm 0.5) / \alpha(D')$
$D^{*'}(2600)^0$	1.18 ± 0.05	$71.4 \pm 1.7 \pm 7.3$	$(0.9 \pm 0.1) / \alpha(D^{*'})$

Final state measured: $D^{*+}\pi^-$

Yield corrected values assume:

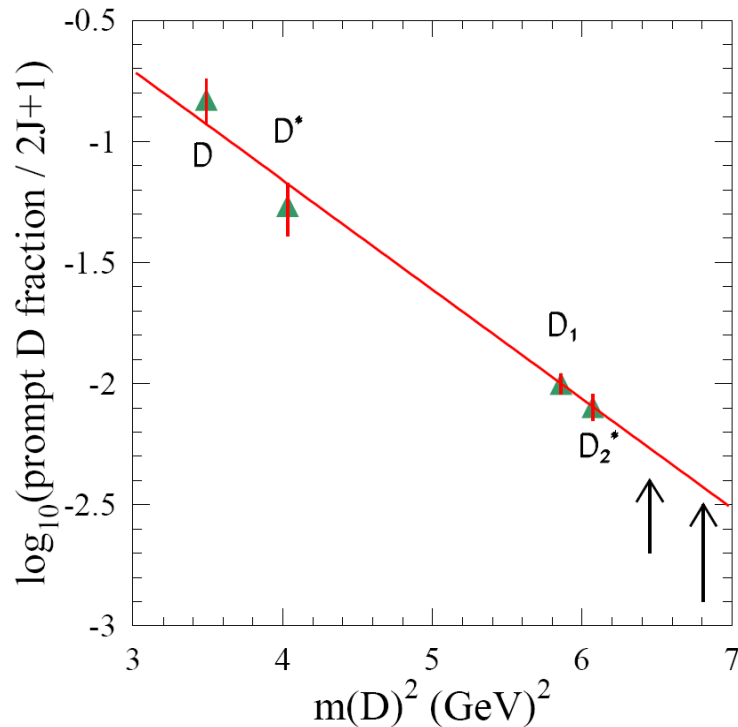
- $B(D_1(2420)^0 \rightarrow D^{*+}\pi^-) = 0.45 \pm 0.02$
- $B(D_2^*(2460)^0 \rightarrow D^{*+}\pi^-) = 0.26 \pm 0.02$
- $B(D' / D^{*'})^0 \rightarrow D^{*+}\pi^- = 2/3 \times \alpha$

$-\alpha$ is the fraction of decays into the $D^*\pi$ final state.

LEP recollections ...

Particle prod. in jets can be described using:
 $(2J+1) \times \exp(-b m^2)$

$P(c \rightarrow D_1(2420)) \sim 3\%$



- $P(c \rightarrow D') \sim 0.5\%$

- $P(c \rightarrow D^{*'}) \sim 1.1\%$

- $\alpha(D') = 1.6 \pm 0.6$.. rather uncertain

- $\alpha(D^{*'}) = 0.5 \pm 0.1$

*Rather large decay rates of
 D' and $D^{*'}$ into $D^*\pi$!*

What about B sl decays ?

Can we explain broad $D^{(*)}\pi$ components in $B^0 \rightarrow D^{(*)}\pi l \nu_l$ by the $D^{(*)}'$?

	(%)
$B_d^0 \rightarrow D_1^- l^+ \nu_l$	0.58 ± 0.05
$B_d^0 \rightarrow D_2^{*-} l^+ \nu_l$	0.29 ± 0.03
$B_d^0 \rightarrow [\overline{D}\pi]_{broad} l^+ \nu_l$	0.42 ± 0.06
$B_d^0 \rightarrow [\overline{D}^* \pi]_{broad} l^+ \nu_l$	0.33 ± 0.07

One expects that $D^{(*)}'$ states are less abundant than narrow D^{**} because they have a higher mass (to be checked: decay rate expressions, form factors, ...)

- only the D^{*}' can contribute to $D\pi$ (broad)
- upper limit: $0.6\% \times \frac{1}{2} \times 0.3 \sim 0.1\%$

The D^{}' has a negligible effect in $D\pi$ broad.*

- for $D^*\pi$ (broad) there could be $D^{(*)}'$ contributions.
- my guess estimate: $<0.1\%$ from D' , $\sim 0.1\%$ from D^{*}' ... could be enough

- for $D^{(*)}\pi\pi$ (broad) my guess estimate: $<0.1\%$ from D' , $\sim 0.1\%$ from D^{*}' ... this cannot explain the $1.25 \pm 0.25\%$


$B \rightarrow D^{(*)} X l \nu_l, X \neq \pi$

Expt.:

$B(B^0 \rightarrow D^{(*)} X l \nu)_{\text{broad}} = (1.24 \pm 0.26)\%$; « x » being more than 1 pion

$B(B^0 \rightarrow D \pi \pi l \nu)_{\text{narrow}} = (0.19 \pm 0.02)\%$; from D_1

$B(B^0 \rightarrow D_s^{(*)} K^0 l \nu) = (0.06 \pm 0.01)\%$



What are these states?

- Can be explained by radial excitations?

Yes → **Phys.Rev. D85 (2012) 094033**

No → see previous discussion, expect 0.1% contribution

? → large signal expected in nl: **arXiv:1301.7336**

- NR contributions ? (1-,2-) resonances ? « à la Goity-Roberts »

- $X = \eta$: expect small rates

- Decays of broad D^{**} states into $D^{(*)}\pi\pi$? (small)

Conclusions

- from nl B^0 decays, broad D^{**} are disfavoured relative to narrow states (uncert. are still large)
 - in $B^0 \rightarrow D \pi |_{\text{broad}} | \nu$: D_0^* is non negligible and a NR component at low mass is likely
 - in $B^0 \rightarrow D^* \pi |_{\text{broad}} | \nu$: $D1'$ is expected to be similar as the D_0^* (?), possibly a small radial component
- need ideas and theory input to describe $B^0 \rightarrow D \pi \pi |_{\text{broad}} | \nu$ decays (NR, radial excitations?, D-waves,)

LHCb can provide informations analyzing nl. $B^- \rightarrow D^{(*)} \pi^- \pi^+$, $B^0 \rightarrow D^{0(*)} \pi^+ \pi^-$ and $B_s^0 \rightarrow D_{0s}^{*} \pi^+$.

Maybe also LHCb can analyze sl. B decays to search for radial excitations mass peaks in $D^{(*)} \pi$ mass distributions.