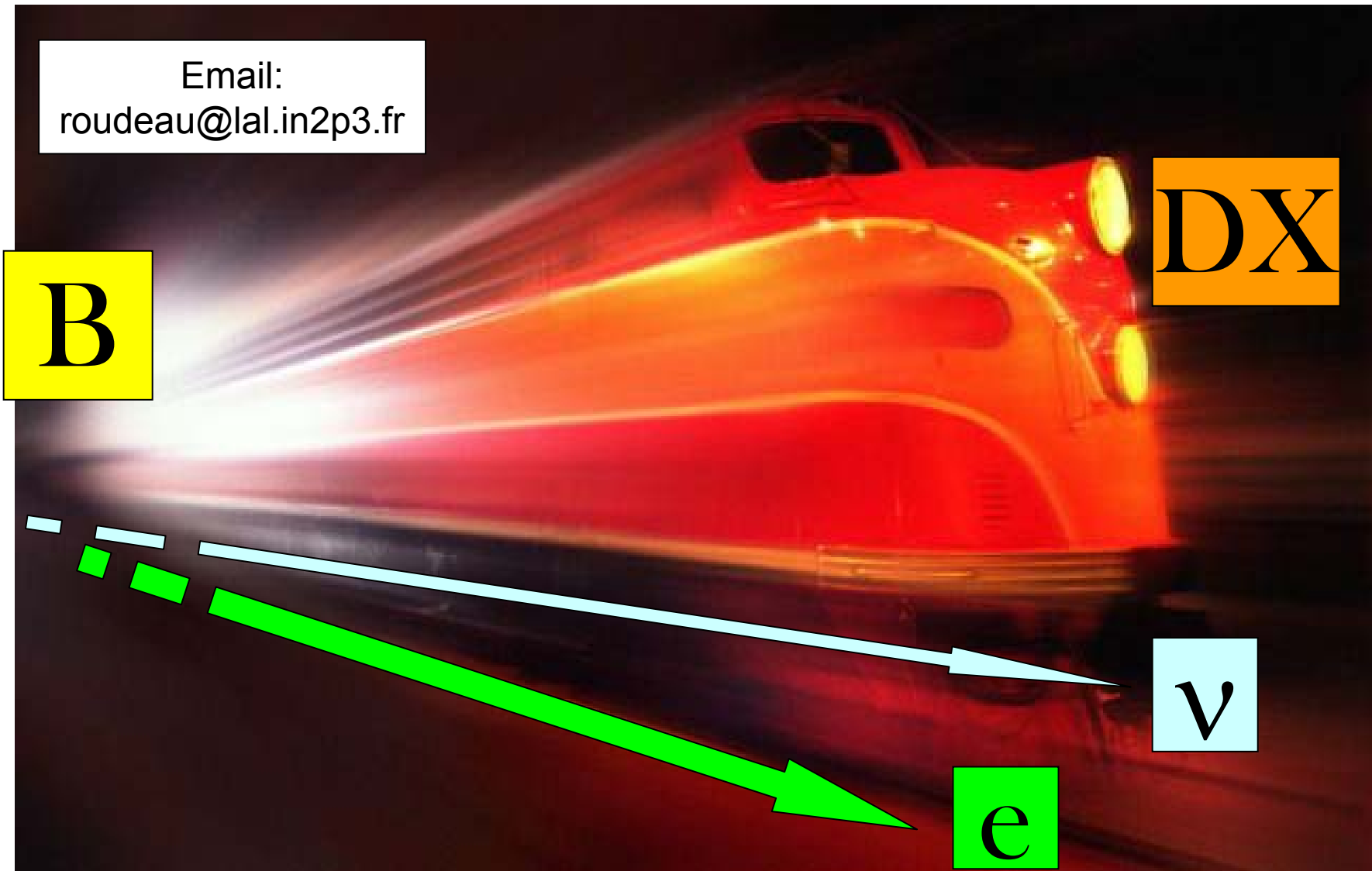


# Can we understand $\bar{B} \rightarrow D^{(*)} X l \nu_l$ decays ?

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February 4-6, 2013, Valencia [see also: http://events.lal.in2p3.fr/WorkshopBdecays/](http://events.lal.in2p3.fr/WorkshopBdecays/)  
P. Roudeau (thanks to A. Le Yaouanc and D. Becirevic)


# Overall picture

Expt.:

$$\begin{aligned} B(B^0 \rightarrow X_c \mid \nu) &= (10.09 \pm 0.22)\% & \rightarrow B(B^0 \rightarrow D \mid \nu) &= (2.12 \pm 0.06)\% \\ & & \rightarrow B(B^0 \rightarrow D^* \mid \nu) &= (5.11 \pm 0.10)\% \\ & & \rightarrow B(B^0 \rightarrow D_1 \mid \nu) &= (0.58 \pm 0.05)\% \\ & & \rightarrow B(B^0 \rightarrow D_2^* \mid \nu) &= (0.29 \pm 0.03)\% \end{aligned}$$

It remains:

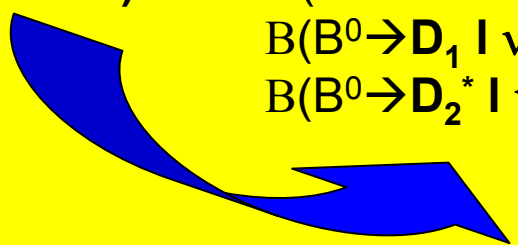
$$\begin{aligned} B(B^0 \rightarrow X_{c,\text{broad}} \mid \nu) &= (2.00 \pm 0.26)\% & \rightarrow B(B^0 \rightarrow D^{(*)} \pi \mid \nu)_{\text{broad}} &= (0.75 \pm 0.09)\% \\ & & \rightarrow B(B^0 \rightarrow D^{(*)} x \mid \nu)_{\text{broad}} &= (1.24 \pm 0.26)\% \\ & & & \ll x \gg \text{ being more than 1 pion} \end{aligned}$$



*About 20% of B-meson  
semileptonic decays  
are not well understood.*

# Remaining questions in $B \rightarrow D^{(*)} \pi \ell \nu_l$

Expt.:

$$\begin{aligned} B(B^0 \rightarrow D \pi \ell \nu)_{\text{broad}} &= (0.42 \pm 0.06)\% & \leftrightarrow & B(B^0 \rightarrow D \pi \ell \nu)_{\text{narrow}} = (0.18 \pm 0.02)\% \\ B(B^0 \rightarrow D^* \pi \ell \nu)_{\text{broad}} &= (0.33 \pm 0.07)\% & \leftrightarrow & B(B^0 \rightarrow D^* \pi \ell \nu)_{\text{narrow}} = (0.50 \pm 0.04)\% \\ & & & B(B^0 \rightarrow D_1 \ell \nu) = (0.58 \pm 0.05)\% \\ & & & B(B^0 \rightarrow D_2^* \ell \nu) = (0.29 \pm 0.03)\% \end{aligned}$$


Theory (naïve):

$$B(B^0 \rightarrow D_0^* \ell \nu) \approx B(B^0 \rightarrow D_1' \ell \nu) \ll B(B^0 \rightarrow D_1 \ell \nu) \approx B(B^0 \rightarrow D_2^* \ell \nu)$$

- If we identify the  $(D^{(*)} \pi)_{\text{broad}}$  final states with the  $D_0^*$  and  $D_1'$ , then there seems to be a contradiction with theory !

$$\tau_{3/2} > \tau_{1/2}$$

- Heavy meson  $Qq$ ;  $J = j_q \oplus s_Q$ ,  $j_q = L \oplus s_q$ ,  $s_Q = s_q = 1/2$

- For  $L = 1$ ,  $j_q = 1/2$  or  $3/2$

- The heavy quark spin is decoupled, meson properties depend on  $j_q$

- Adding the heavy quark gives 2 doublets

$j_q = 1/2 \rightarrow J^P = 0^+, 1^+$  broad ( $D_0^*$ ,  $D_1$ ), mainly S-wave decays

$j_q = 3/2 \rightarrow J^P = 1^+, 2^+$  narrow ( $D_1^*$ ,  $D_2^*$ ), mainly D-wave decays

- Within a doublet, states (are expected) to have similar properties. Production rates in B decays governed by 2 form factors:  $\tau_{1/2}(w)$  and  $\tau_{3/2}(w)$ ,  $w = v_B \cdot v_D$  (in the infinite mass limit).

$$\tau_{3/2}(1) \simeq 0.54, \quad \tau_{1/2}(1) \simeq 0.22 \quad \text{Quark model}$$

$$\tau_{3/2}(1) = 0.528(23), \quad \tau_{1/2}(1) = 0.297(26) \quad \text{LQCD}$$

$B(B^0 \rightarrow D_{3/2,1/2} \ell \nu)$  depend on:  $\tau_{3/2}^2(1) / \tau_{1/2}^2(1) \sim 3 - 6$

slope of ff. versus  $w \sim 0.7$

decay rate expression (spin)  $\sim 2.2$

Total:  $5 - 9$

**-Need better evaluation of uncert. and of other effects as finite mass corrections**

# The $B \rightarrow D \pi l \nu_l$ decay channel

Expt.:

$$B(B^0 \rightarrow D \pi l \nu)_{\text{broad}} = (0.42 \pm 0.06)\% \leftrightarrow B(B^0 \rightarrow D \pi l \nu)_{\text{narrow}} = (0.18 \pm 0.02)\%$$

**Belle analysis:**

$$B(B^0 \rightarrow D_0^* l \nu) = (0.30 \pm 0.10 \pm 0.07)\%$$

$$B(B^- \rightarrow D_0^* l \nu) = (0.36 \pm 0.06 \pm 0.09)\%$$

**Babar analysis:**

$$(0.66 \pm 0.12 \pm 0.09)\%$$

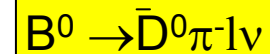
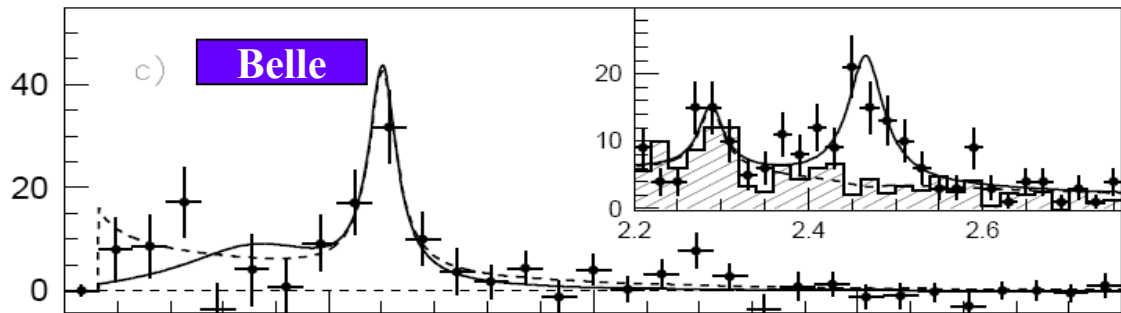
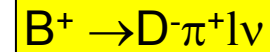
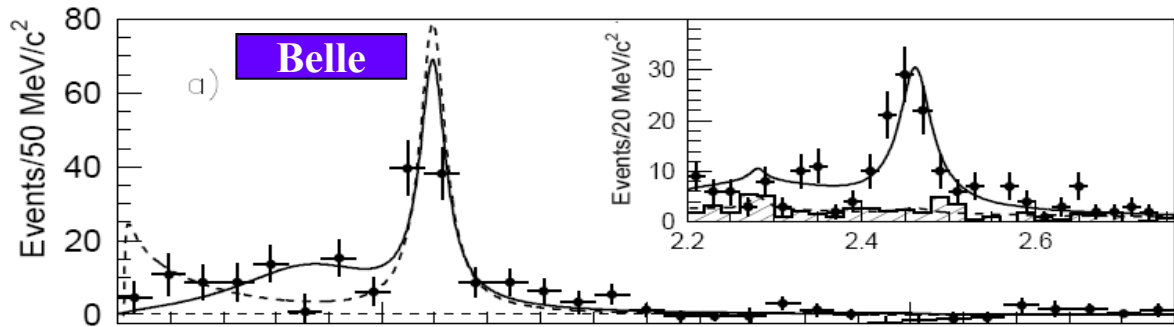
$$(0.39 \pm 0.08 \pm 0.06)\%$$

**HFAG average:**

$$B(B^0 \rightarrow D_0^* l \nu) = (0.40 \pm 0.08)\%$$

- Compatible results between BaBar and Belle
- The  $D_0^*$  can account for all the  $(D \pi)_{\text{broad}}$  component but uncert. are large
- In practice there are differences between the 2 analyses.

# Belle analysis

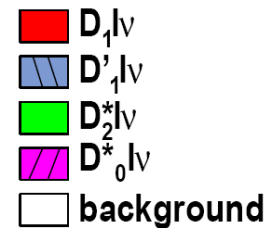
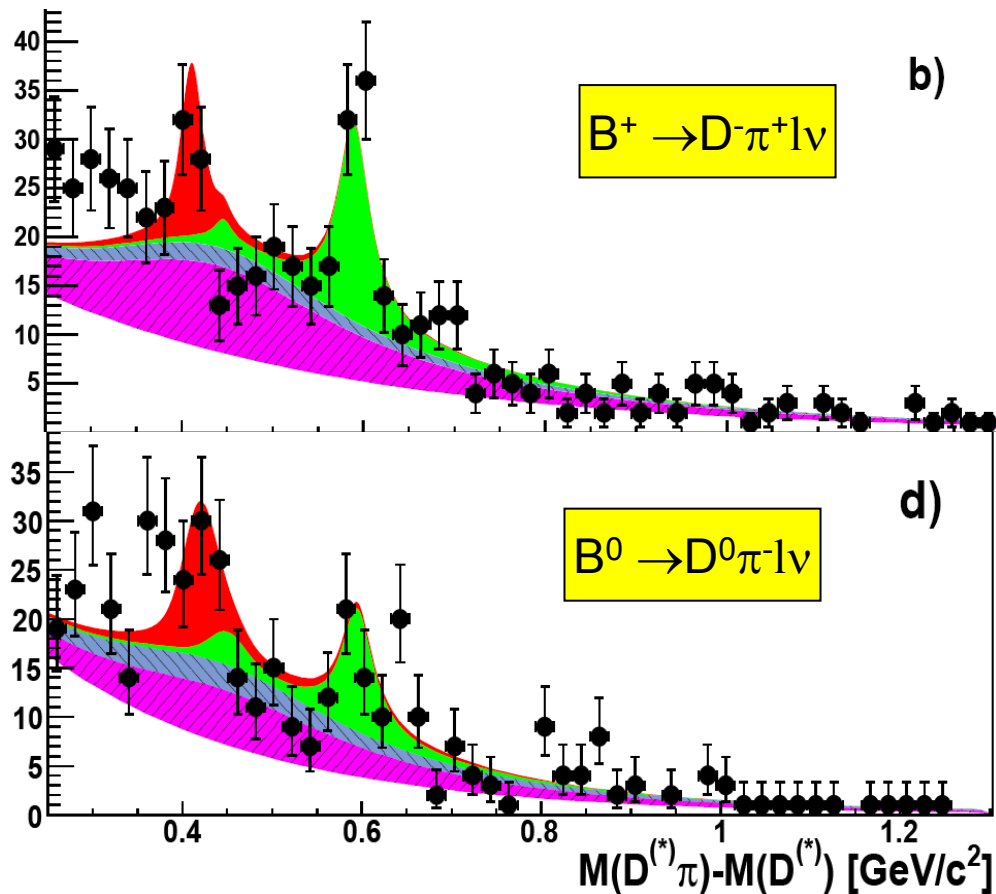


2 2.4 2.8 3.2 3.6  $D\pi$  mass

**$-D_0^* + D_2^*$  favoured over  $D_V + D_2^*$  by 2.8 sigmas**

and background  $D^{(*)}\pi$  mass spectra. The signal function includes all orbitally excited  $D^{**}$  contributing to the given final state ( $D_0$  and  $D_2^*$  to  $D\pi$  and  $D_1, D_1', D_2^*$  to  $D^*\pi$ ), each of which is described by a relativistic Breit-Wigner function for a known orbital momenta, and a non-resonant part described by the Goity-Roberts model [16].  $D^{**}$  masses and widths are

# Babar analysis



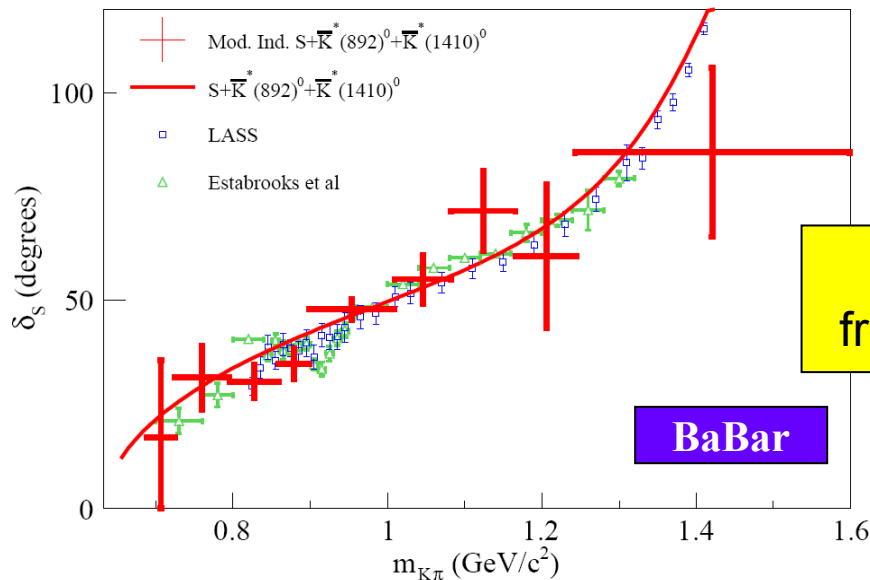
Larger window on  $m_{\pi l \nu}$  than in Belle (keeps soft  $\pi$ ).

Excess of evts at low mass attributed to  $D \pi l \nu_1$  not included in the simulation.

- resonances do not include « Goity-Roberts » effects
- fitted model assumes only  $D^{**}$  states

# Comments on present analyses

- Agreement between BaBar and Belle is a bit « artificial »
- There seems to be an excess of evts at low mass :  
“à la Goity-Roberts”?  $D_V^*$ ?
- Most probably the  $D_0^*$  is only a fraction of the  $(D \pi)_{\text{broad}}$
- What is the equivalent of the  $K_0^*(800)$  for charm ?
- Radial excitations?

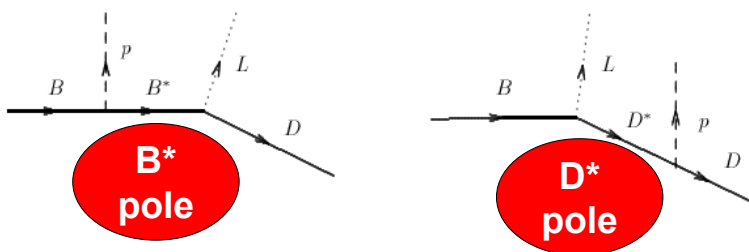


S-wave phase  
from  $D^+ \rightarrow K^- \pi^+ e^+ \nu_e$

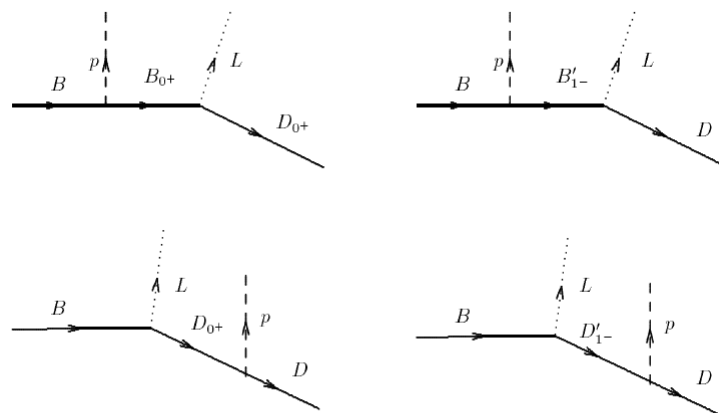


# What can be done ?

- Get expressions from theorists for  $d\mathcal{B}(B^0 \rightarrow D \pi | \nu) / dx^5$  (tests can be done on  $D^+ \rightarrow K^- \pi^+ e^+ \nu_e$  ?)
- Can one normalize the  $D^*$  ( $B^*$ ) pole contribution(s) ?
- Use  $B^0 \rightarrow D \pi \pi$ , which has larger statistics, to understand the  $(D \pi)_{\text{broad}}$  components
- Use  $B^- \rightarrow D^+ \pi^- \pi^-$  to measure the phase of the  $D_0^* \rightarrow D \pi$  versus the  $D \pi$  mass.
- Have new spectra from BaBar with similar cuts as in Belle

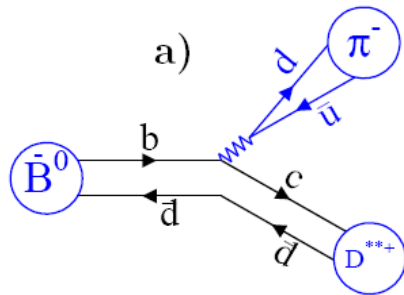


NR contributions in  $B \rightarrow D \pi | \nu$  decays



Resonant contributions

# $\bar{B}^0 \rightarrow D^0 \pi^+ \pi^-$

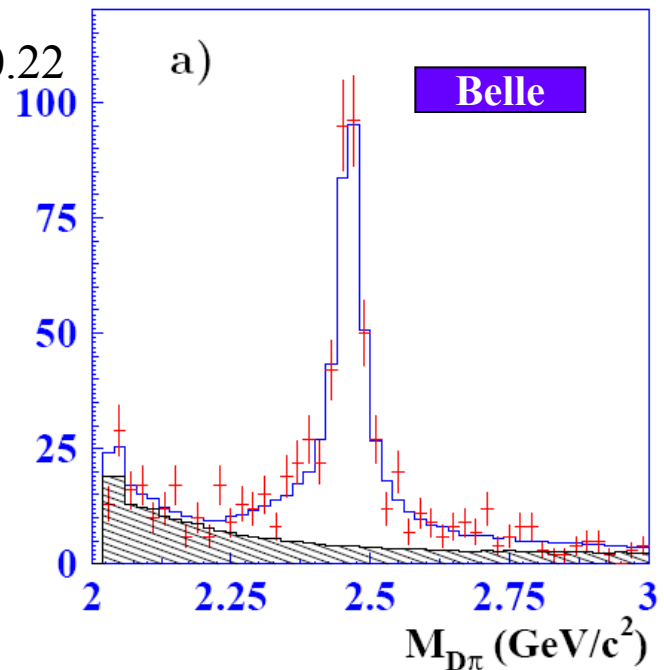


Type I decay, can be related to sl. decay at  $q^2 = m_\pi^2 \sim 0$ , using factorization

Results from Belle (published) and BaBar (prelim.) are not in nice agreement.

| Belle   |                                   |
|---|-----------------------------------|
| $\mathcal{B}_{B \rightarrow D_0^* \pi} \mathcal{B}_{D_0^* \rightarrow D \pi} (10^{-4})$ | $0.60 \pm 0.13 \pm 0.15 \pm 0.22$ |
| $\phi_{D_0^*}$  | $-3.00 \pm 0.13$                  |
| $M_{D_0^*}, (MeV/c^2)$  | 2308.0                            |
| $\Gamma_{D_0^*}, (MeV/c^2)$   | 276.0                             |
| $\mathcal{B}_{B \rightarrow D_v^* \pi} \mathcal{B}_{D_v^* \rightarrow D \pi} (10^{-4})$ | $0.88 \pm 0.13$                   |
| $\phi_{D_v^*}$  | $-2.62 \pm 0.15$                  |

- significant  $D_v^*$  component
- LHCb can improve the accuracy
- difficult analysis



# $\bar{B}^0 \rightarrow D^{0(*)} \pi^+ \pi^-$

| $B_d^0 \rightarrow \bar{D}^{**} \pi^+$ | theory               | expt.                                |
|--|----------------------|--------------------------------------|
| $\bar{D}_2^*$                          | $1.1 \times 10^{-3}$ | $(0.49 \pm 0.07) \times 10^{-3}$     |
| $\bar{D}_1$                            | $1.3 \times 10^{-3}$ | $(8.2_{-1.7}^{+2.5}) \times 10^{-4}$ |
| $\bar{D}'_1$                           | $1.1 \times 10^{-4}$ | $< 10^{-4} (90\% C.L.)$              |
| $\bar{D}_0^*$                          | $1.3 \times 10^{-4}$ | $[0.3, 3.4] \times 10^{-4}$          |

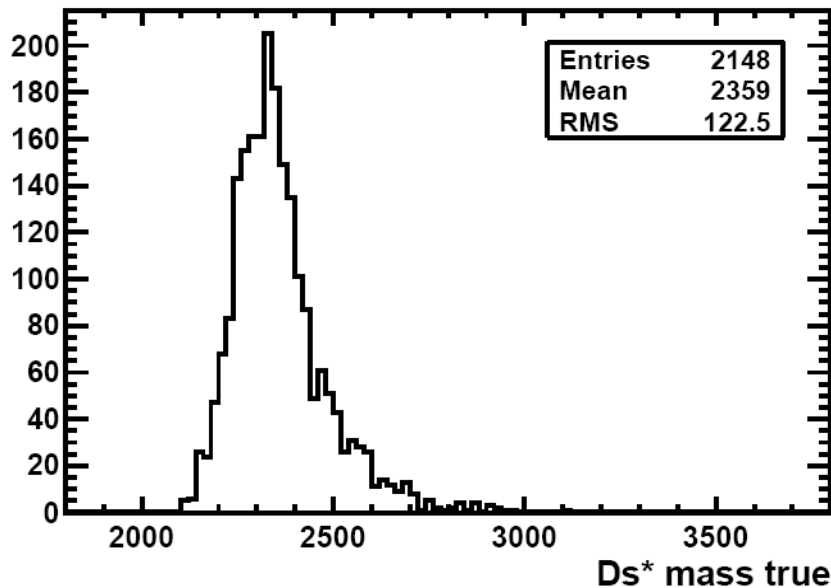
| $B_d^0 \rightarrow \bar{D}^{**} e^+ \nu_e$ |                       |                                  |
|--|-----------------------|----------------------------------|
| $\bar{D}_2^*$                              | $0.7 \times 10^{-2}$  | $(0.29 \pm 0.03) \times 10^{-2}$ |
| $\bar{D}_1$                                | $0.45 \times 10^{-2}$ | $(0.58 \pm 0.05) \times 10^{-2}$ |
| $\bar{D}'_1$                               | $0.7 \times 10^{-3}$  | $[0., 3.2] \times 10^{-3}$       |
| $\bar{D}_0^*$                              | $0.6 \times 10^{-3}$  | $(3.5 \pm 0.7) \times 10^{-3}$   |

**Need better accuracy**

- theory uncertainties ?
- rough agreement between th. and expt. in nl decays and for narrow states in sl. decays
- disagreement for broad states in sl. decays

$$B^0_s \rightarrow D_{0s}^{*-} \pi^+, D_{0s}^{*-} \rightarrow D_s^- \pi^0$$

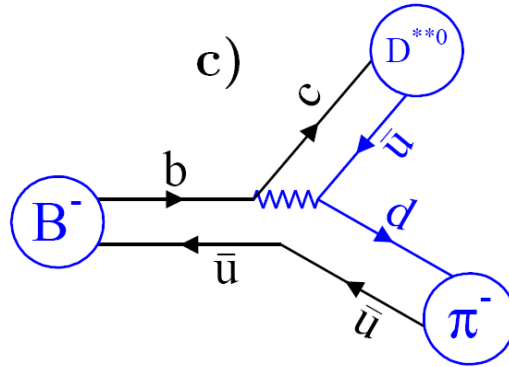
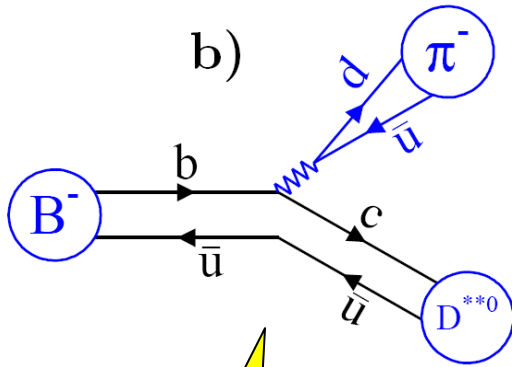
- This is a type I diagram
- The  $D_{0s}^{*-}$  is very narrow (avoid the problem of measuring broad states)
- ... unfortunately needs to reconstruct a soft  $\pi^0$  (missed ?)
- so ... signal expected to be relatively broad (use of kinematic constraints at LHCb)



- expect few hundred evts/ fb<sup>-1</sup>
- background level ?

[c.f. arXiv:1206.5869 [hep-ph]]

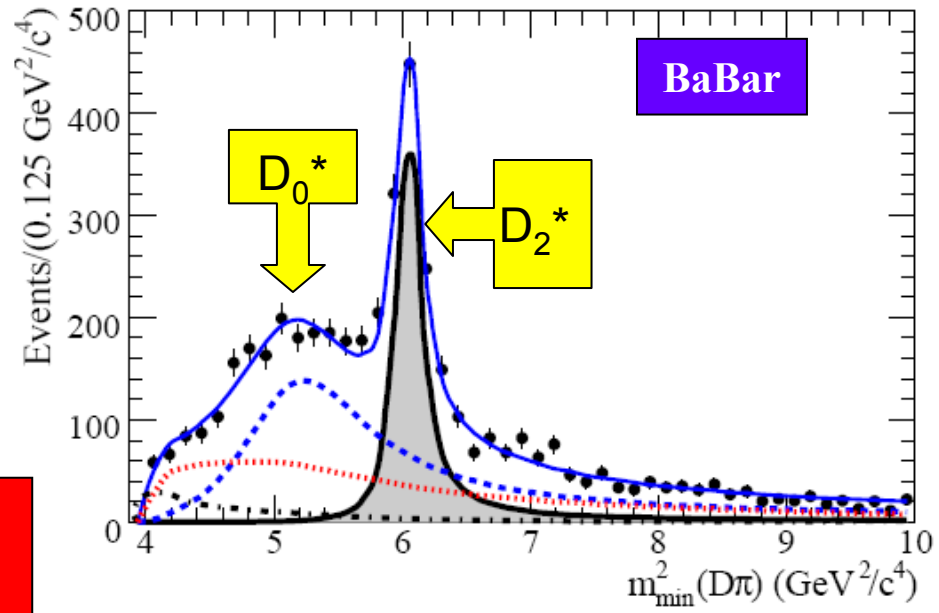
# $B^- \rightarrow D^+ \pi \pi$



Type III decay, can be used to measure the  $D\pi$  S-wave phase

*Is the  $D_0^*$  a simple Breit-Wigner?*

- large signal, rather small backg.
- LHCb can improve the accuracy



LHCb

# The $B \rightarrow D^* \pi l \nu_l$ decay channel

Expt.:

$$B(B^0 \rightarrow D^* \pi l \nu)_{\text{broad}} = (0.33 \pm 0.07)\% \leftrightarrow B(B^0 \rightarrow D^* \pi l \nu)_{\text{narrow}} = (0.50 \pm 0.04)\%$$

**Belle analysis:**

$$B(B^- \rightarrow D_1' l \nu) = (-0.04 \pm 0.08 \pm 0.10)\%$$

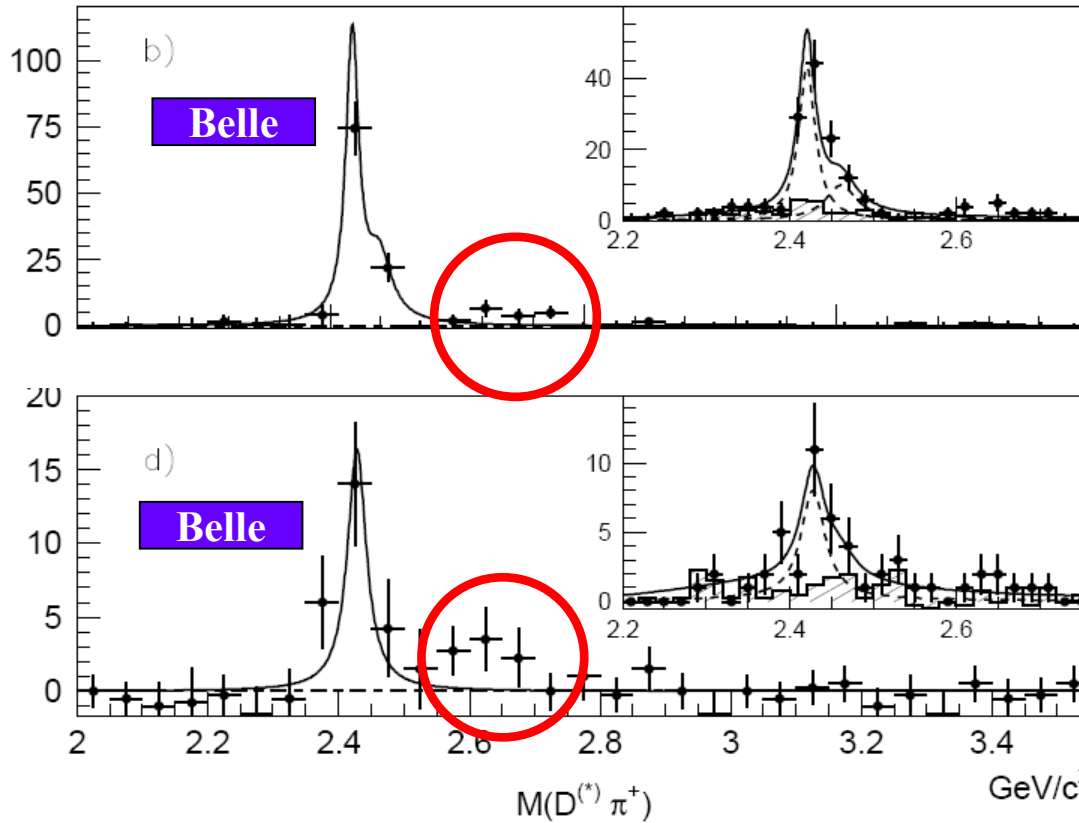
**Babar analysis:**

$$(0.38 \pm 0.06 \pm 0.06)\%$$

**HFAG average: ??**

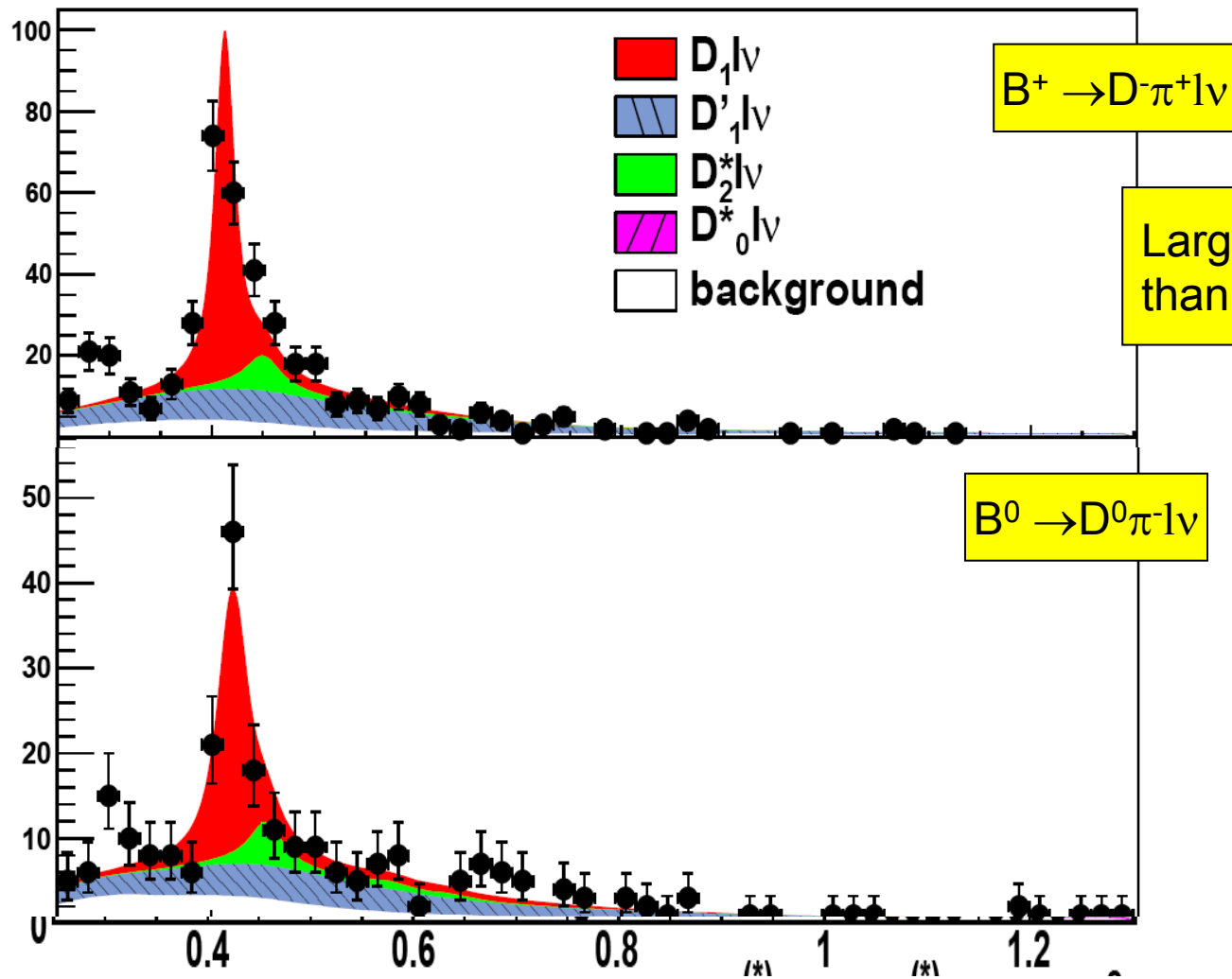
- BaBar and Belle not in « good » agreement ( $\sim 3 \sigma$ )
- Can BaBar tighten the cuts on  $m_{\text{min}}^2(\nu)$  ?

# Belle analysis



- no evidence for  $D_1'$
- some « excess » around 2.6 GeV ?

# Babar analysis



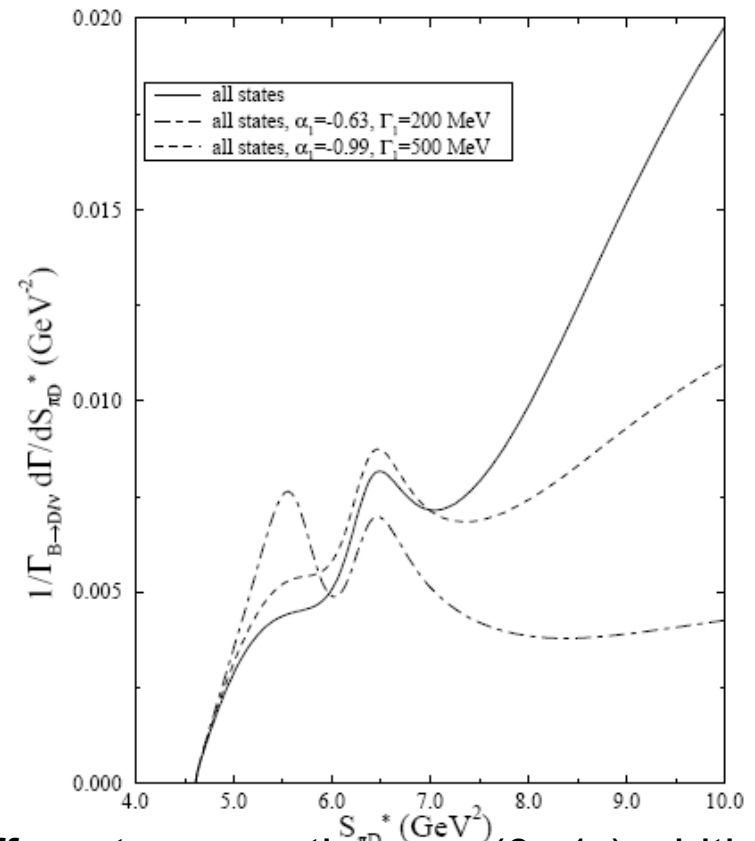
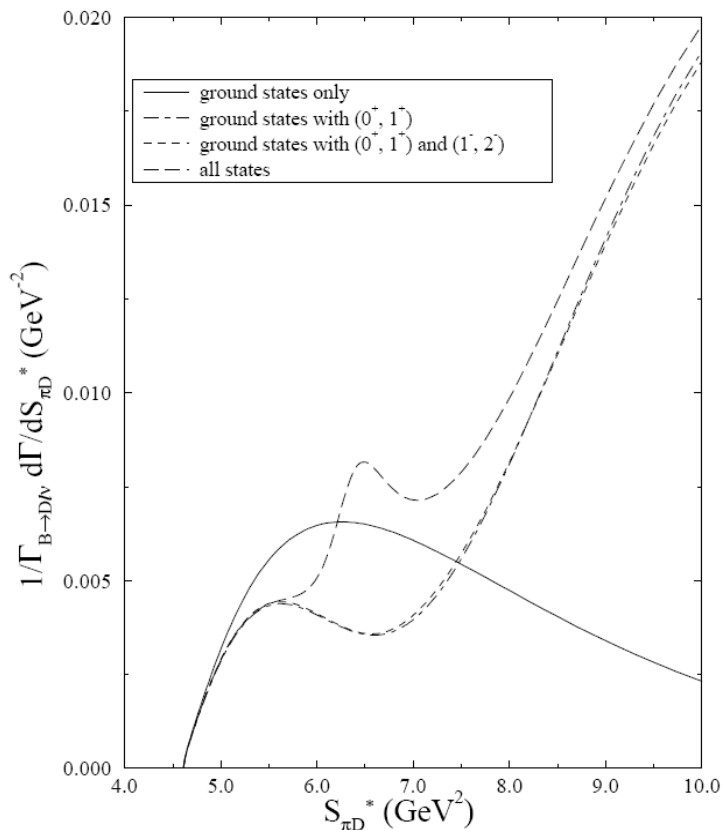
- no spectacular excess around  $m(D^*) + 0.6$  GeV



# Comments on present analyses

- Poor agreement between BaBar and Belle

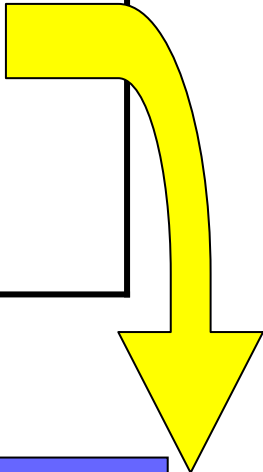
-The “Goity-Roberts” model predicts contributions at high masses (validity?), what about  $(1^-, 2^-)$ ? The non-resonant component is expected to be large ... normally it can be absolutely normalized!



With different assumptions on  $(0^+, 1^+)$  width

# Radial excitations

| State  | decay                         |            | Final state       | Angular mom. |
|--|-------------------------------|------------|-------------------|--------------|
| <b>D'(2550)</b><br><b>J<sup>P</sup>=0<sup>-</sup></b><br><b>M=2540 MeV</b><br><b>Γ=130 MeV</b> | <b>Dπ</b>                     | <b>No</b>  |                   |              |
|  | <b>D*π</b>                    | <b>Yes</b> | <b>D*π</b>        | <b>L=1</b>   |
|  | <b>D<sub>0</sub>* (2400)π</b> | <b>Yes</b> | <b>Dππ</b>        | <b>L=0</b>   |
|  | <b>D<sub>1</sub>π</b>         | <b>No</b>  |                   |              |
|  | <b>D<sub>2</sub>* (2460)π</b> | <b>Yes</b> | <b>Dππ, D*ππ</b>  | <b>L=2</b>   |
| <b>D*(2600)</b><br><b>J<sup>P</sup>=1<sup>-</sup></b><br><b>M=2610 MeV</b><br><b>Γ=93 MeV</b>  | <b>Dπ</b>                     | <b>Yes</b> | <b>Dπ</b>         | <b>L=1</b>   |
|  | <b>D*π</b>                    | <b>Yes</b> | <b>D*π</b>        | <b>L=1</b>   |
|  | <b>D<sub>0</sub>* (2400)π</b> | <b>No</b>  |                   |              |
|  | <b>D<sub>1</sub>π</b>         | <b>Yes</b> | <b>D*ππ, Dπππ</b> | <b>L=0</b>   |
|  | <b>D<sub>2</sub>* (2460)π</b> | <b>Yes</b> | <b>Dππ, D*ππ</b>  | <b>L=2</b>   |



- Relatively narrow  
 - L=0 or 1 presumably dominant

BaBar  
 $B(D\pi) / B(D^*\pi) = 0.32 \pm 0.02 \pm 0.09$

# Production rates in cc events

| State            | Efficiency (%)                    | BaBar Yield ( $\times 10^{-3}$ )          | Yield corrected ( $\times 10^{-7}$ )               |
|------------------|-----------------------------------|---|--|
| $D_1(2420)^0$    | <b><math>1.09 \pm 0.03</math></b> | <b><math>214.6 \pm 1.2 \pm 6.4</math></b> | <b><math>4.38 \pm 0.13 \pm 0.19</math></b>         |
| $D_2^*(2460)^0$  | <b><math>1.12 \pm 0.04</math></b> | <b><math>136 \pm 2 \pm 13</math></b>      | <b><math>4.67 \pm 0.45 \pm 0.36</math></b>         |
| $D'(2550)^0$     | <b><math>1.14 \pm 0.04</math></b> | <b><math>98.4 \pm 8.2 \pm 38</math></b>   | <b><math>(1.3 \pm 0.5) / \alpha(D')</math></b>     |
| $D^{*'}(2600)^0$ | <b><math>1.18 \pm 0.05</math></b> | <b><math>71.4 \pm 1.7 \pm 7.3</math></b>  | <b><math>(0.9 \pm 0.1) / \alpha(D^{*'})</math></b> |

Final state measured:  $D^{*+}\pi^-$

Yield corrected values assume:

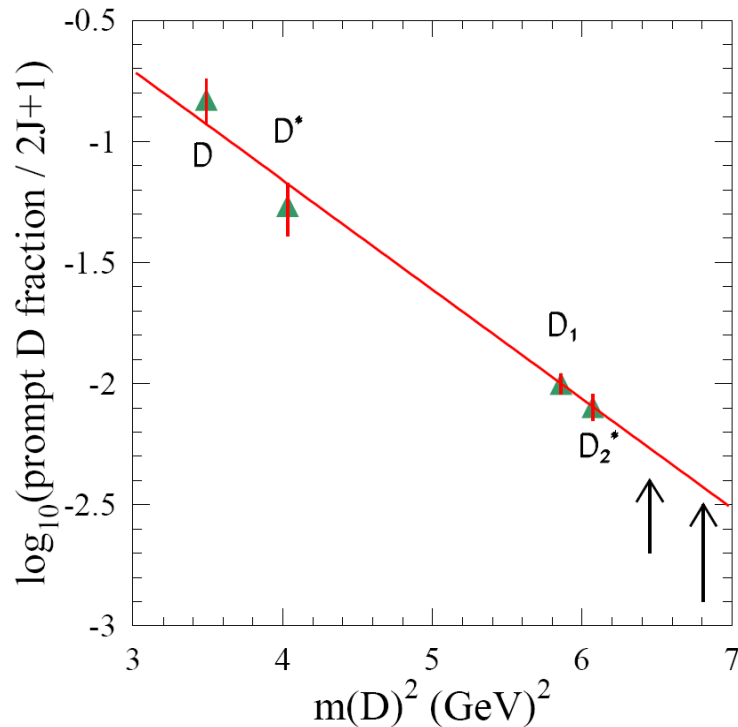
- $B(D_1(2420)^0 \rightarrow D^{*+}\pi^-) = 0.45 \pm 0.02$
- $B(D_2^*(2460)^0 \rightarrow D^{*+}\pi^-) = 0.26 \pm 0.02$
- $B(D' / D^{*'} )^0 \rightarrow D^{*+}\pi^- = 2/3 \times \alpha$

$-\alpha$  is the fraction of decays into the  $D^*\pi$  final state.

# LEP recollections ...

Particle prod. in jets can be described using:  
 $(2J + 1) \times \exp(-b m^2)$

$P(c \rightarrow D_1(2420)) \sim 3\%$



-  $P(c \rightarrow D') \sim 0.5\%$

-  $P(c \rightarrow D^{*'}) \sim 1.1\%$

-  $\alpha(D') = 1.6 \pm 0.6$  .. rather uncertain

-  $\alpha(D^{*'}) = 0.5 \pm 0.1$

*Rather large decay rates of  
D' and D\*' into D\* $\pi$ !*

# What about $B$ sl decays ?

Can we explain broad  $D^{(*)}\pi$  components in  $B^0 \rightarrow D^{(*)}\pi l \nu_l$  by the  $D^{(*)}'$  ?

|  | (%)             |
|--|-----------------|
| $B_d^0 \rightarrow D_1^- l^+ \nu_l$                        | $0.58 \pm 0.05$ |
| $B_d^0 \rightarrow D_2^{*-} l^+ \nu_l$                     | $0.29 \pm 0.03$ |
| $B_d^0 \rightarrow [\overline{D}\pi]_{broad} l^+ \nu_l$    | $0.42 \pm 0.06$ |
| $B_d^0 \rightarrow [\overline{D}^* \pi]_{broad} l^+ \nu_l$ | $0.33 \pm 0.07$ |

One expects that  $D^{(*)}'$  states are less abundant than narrow  $D^{**}$  because they have a higher mass (to be checked: decay rate expressions, form factors, ...)

- only the  $D^{*}'$  can contribute to  $D\pi$  (broad)
- upper limit:  $0.6\% \times \frac{1}{2} \times 0.3 \sim 0.1\%$

*The  $D^{*}'$  has a negligible effect in  $D\pi$  broad.*

- for  $D^*\pi$  (broad) there could be  $D^{(*)}'$  contributions.
- my guess estimate:  $<0.1\%$  from  $D'$ ,  $\sim 0.1\%$  from  $D^{*}'$  ... could be enough

- for  $D^{(*)}\pi\pi$  (broad) my guess estimate:  $<0.1\%$  from  $D'$ ,  $\sim 0.1\%$  from  $D^{*}'$  ... this cannot explain the  $1.25 \pm 0.25\%$


# $B \rightarrow D^{(*)} X l \nu_l, X \neq \pi$

Expt.:

$B(B^0 \rightarrow D^{(*)} X l \nu)_{\text{broad}} = (1.24 \pm 0.26)\%$  ; « x » being more than 1 pion

$B(B^0 \rightarrow D \pi \pi l \nu)_{\text{narrow}} = (0.19 \pm 0.02)\%$  ; from  $D_1$

$B(B^0 \rightarrow D_s^{(*)} K^0 l \nu) = (0.06 \pm 0.01)\%$



*What are these states?*

- Can be explained by radial excitations?

**Yes** → **Phys.Rev. D85 (2012) 094033**

**No** → see previous discussion, expect 0.1% contribution

**?** → large signal expected in nl: **arXiv:1301.7336**

- NR contributions ? (1-,2-) resonances ? « à la Goity-Roberts »

-  $X = \eta$  : expect small rates

- Decays of broad  $D^{**}$  states into  $D^{(*)}\pi\pi$  ? (small)

# Conclusions

- from nl  $B^0$  decays, broad  $D^{**}$  are disfavoured relative to narrow states (uncert. are still large)
- in  $B^0 \rightarrow D \pi |_{\text{broad}} | \nu$  :  $D_0^*$  is non negligible and a NR component at low mass is likely Seems to contradict a large (factor 10) suppression of  $j=1/2$ .
- in  $B^0 \rightarrow D^* \pi |_{\text{broad}} | \nu$  :  $D1'$  is expected to be similar as the  $D_0^*$  (?), possibly a small radial excit. component is present?

- need evaluation of theory uncertainties ...

- need ideas and theory input to describe  $B^0 \rightarrow D \pi \pi |_{\text{broad}} | \nu$  decays (NR, radial excitations?, D-waves, ....)

LHCb can provide informations analyzing nl.  $B^- \rightarrow D^{(*)} \pi^- \pi^+$ ,  $B^0 \rightarrow D^{0(*)} \pi^+ \pi^-$  and  $B_s^0 \rightarrow D_{0s}^{*} \pi^+$ .

Maybe also LHCb can analyze sl. B decays to search for radial excitations mass peaks in  $D^{(*)} \pi$  mass distributions.