

# **Z' signals at $e^-e^+$ linear colliders in gauge-Higgs unification**

**Yutaka Hosotani**



S. Funatsu, H. Hatanaka, YH, Y. Orikasa, N. Yamatsu

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**$Z'$  (10 TeV) signals can be seen in**

$$e^- e^+ \rightarrow \mu^- \mu^+ (f \bar{f})$$

**in the early stage of 250 GeV ILC**

The diagram illustrates the interference of two Feynman diagrams for the process  $e^- e^+ \rightarrow f \bar{f}$ . On the left, a vertical red line indicates the squared magnitude of the sum of two amplitudes. The first amplitude shows an incoming  $e^-$  and  $e^+$  (red lines) meeting at a vertex, with a dashed blue line labeled  $Z, \gamma$  connecting to a vertex where an outgoing  $f$  and  $\bar{f}$  (red lines) emerge. The second amplitude is identical but with a dashed blue line labeled  $Z'$ . A plus sign is between the two diagrams. The entire expression is enclosed in large vertical red bars, with a superscript 2 at the top right.

$$\left| e^- e^+ \rightarrow [Z, \gamma] f \bar{f} + e^- e^+ \rightarrow [Z'] f \bar{f} \right|^2$$

**Interference terms : large enough**

# Gauge-Higgs unification

$A_M$

$A_\mu$

$\gamma, W, Z$

$A_y$

125 GeV Higgs boson

AB phase in the 5th dim

$$P \exp \left\{ ig \oint dy A_y \right\} \sim e^{i\Theta_H(x)}$$

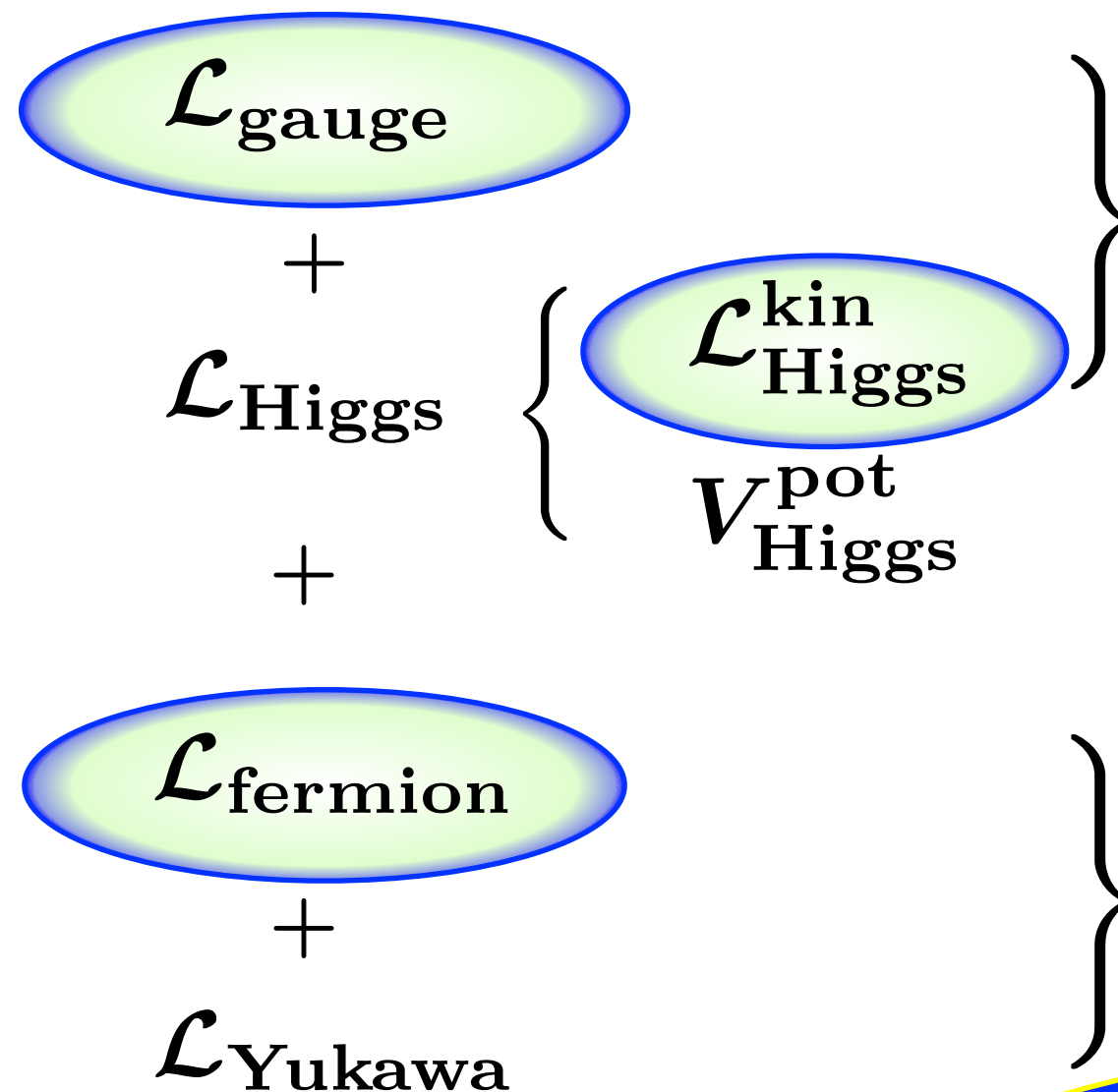
$$\Theta_H(x) = \theta_H + \frac{H(x)}{f_H}$$

$$\theta_H \neq 0$$

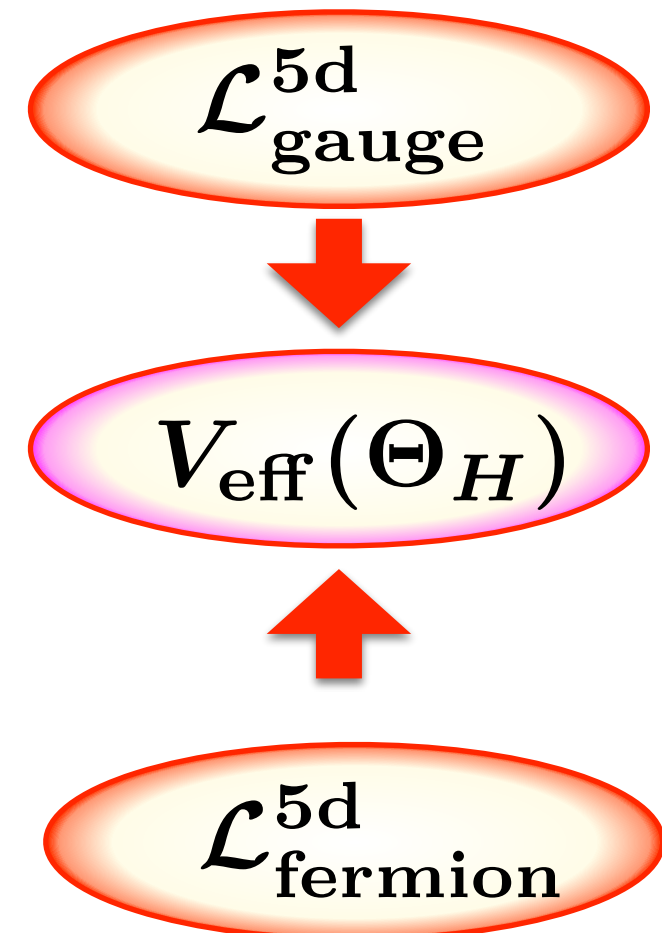
EW sym. breaking

Gauge hierarchy prob. solved

## Standard Model



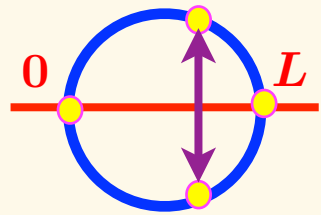
## Gauge-Higgs Unification



gauge principle

# $SU(3) \times SO(5) \times U(1)$ gauge-Higgs on RS

Agashe, Contino, Pomarol 2005  
 Medina, Shah, Wagner 2007  
 YH, Oda, Ohnuma, Sakamura 2008  
 Funatsu, Hatanaka, YH, Orikasa, Shimotani 2013



UV brane

IR brane

AdS  $\Lambda = -6 k^2$

$$P_0 = \begin{pmatrix} -I_4 & \\ & 1 \end{pmatrix}$$

$$ds^2 = e^{-2k|y|} dx^\mu dx_\mu + dy^2$$

$$P_1 = \begin{pmatrix} -I_4 & \\ & 1 \end{pmatrix}$$

$$\longrightarrow SU(3)_C \times SO(4) \times U(1)_X$$

brane scalar

$$\longrightarrow SU(3)_C \times SU(2)_L \times U(1)_Y$$

Hosotani mechanism  $\theta_H \neq 0$

$$\longrightarrow SU(3)_C \times U(1)_{EM}$$

$$A_\mu \sim \left( \begin{array}{c} \boxed{W \ Z \ \gamma} \end{array} \right)$$

$$A_y \sim \left( \begin{array}{c} \text{Higgs} \\ \boxed{\phantom{Higgs}} \end{array} \right)$$

# Matter

|                                                        |               |                                  |                                             |                                             |
|--------------------------------------------------------|---------------|----------------------------------|---------------------------------------------|---------------------------------------------|
| $\begin{pmatrix} u \\ d \\ u' \\ d' \end{pmatrix}$     |               | B-model (GUT inspired)           |                                             |                                             |
|                                                        | Quark         | $(\mathbf{3}, 4)_{\frac{1}{6}}$  | $(\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}^+$ | $(\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}^-$ |
| $\begin{pmatrix} \nu \\ e \\ \nu' \\ e' \end{pmatrix}$ | Lepton        | $(\mathbf{1}, 4)_{-\frac{1}{2}}$ | $D^\pm$                                     |                                             |
|                                                        | Dark fermion  | $(\mathbf{3}, 4)_{\frac{1}{6}}$  | $(\mathbf{1}, \mathbf{5})_0^+$              | $(\mathbf{1}, \mathbf{5})_0^-$              |
|                                                        |               | $(\mathbf{1}, 4)_{-\frac{1}{2}}$ |                                             |                                             |
|                                                        | Brane fermion | $(\mathbf{1}, \mathbf{1})_0$     | $\nu_\chi$                                  |                                             |
|                                                        | Brane scalar  | $(\mathbf{1}, 4)_{\frac{1}{2}}$  | $\hat{\Phi}$                                |                                             |

$SU(3)_C \times SO(5) \times U(1)_X$  content

# GUT inspired B-model

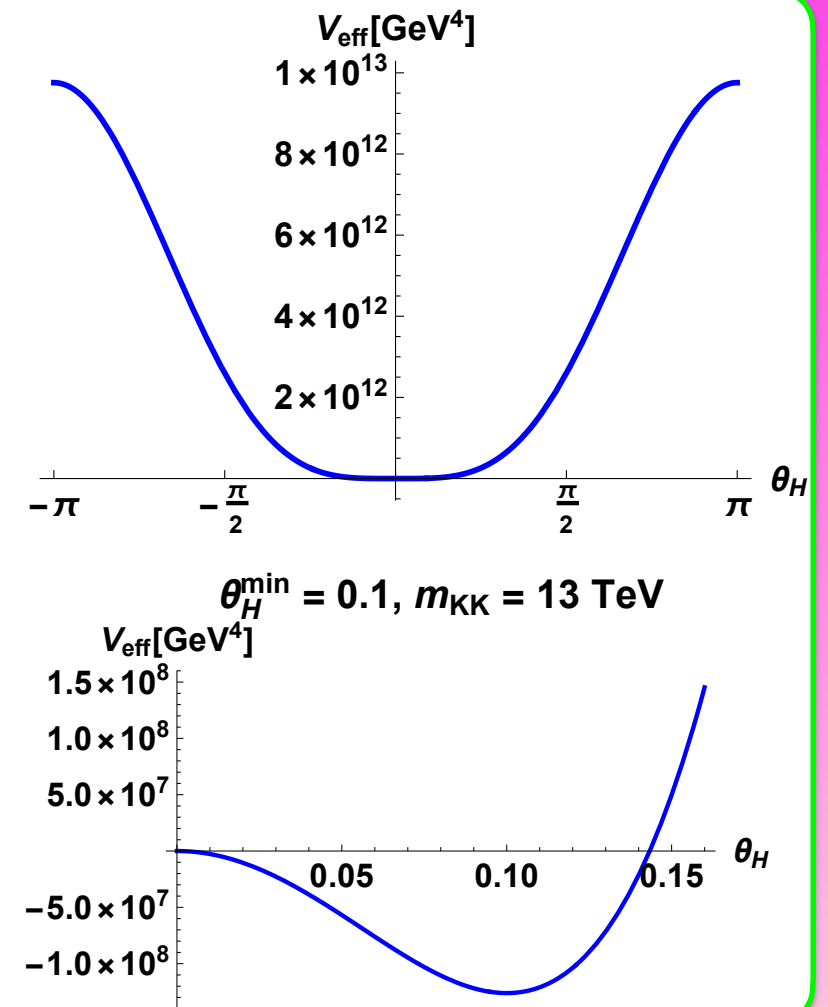
**EW sym breaking**

$$\theta_H \sim 0.1, m_H = 125.1 \text{ GeV}$$

**Mass spectrum**

**CKM**

**FCNC naturally suppressed**



# W, Z couplings of quarks/leptons

– nearly the same as in the SM

$$\frac{1}{g_{L\text{ lepton}}^W} \begin{pmatrix} g_{Luu}^Z \\ g_{Ruu}^Z \\ g_{Ldd}^Z \\ g_{Rdd}^Z \end{pmatrix} = \begin{matrix} \theta_H = 0.10 \\ \begin{pmatrix} 0.34588 \\ -0.15413 \\ -0.42295 \\ 0.07707 \end{pmatrix} \end{matrix}, \begin{matrix} \theta_H = 0.15 \\ \begin{pmatrix} 0.34591 \\ -0.15411 \\ -0.42298 \\ 0.07706 \end{pmatrix} \end{matrix} \Leftrightarrow \begin{matrix} SM \\ \begin{pmatrix} 0.3458 \\ -0.1541 \\ -0.4229 \\ 0.0771 \end{pmatrix} \end{matrix}$$

## GHU : signals (deviation from SM)



**KK states**  $Z^{(n)}, \gamma^{(n)}, W^{(n)}, gluon^{(n)}, q^{(n)}, \dots$

# Higgs couplings

**WWH, ZZH**

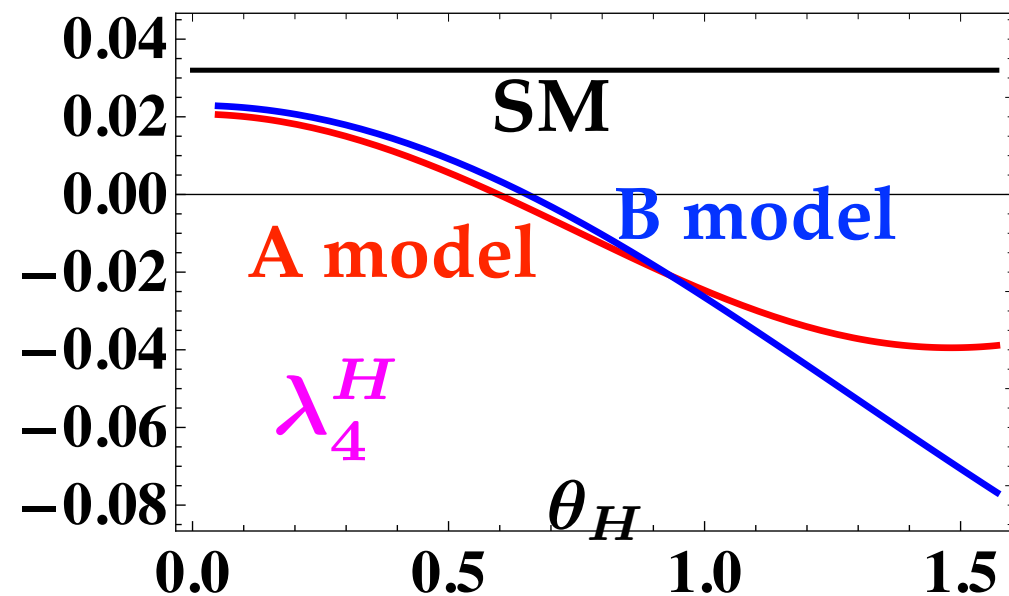
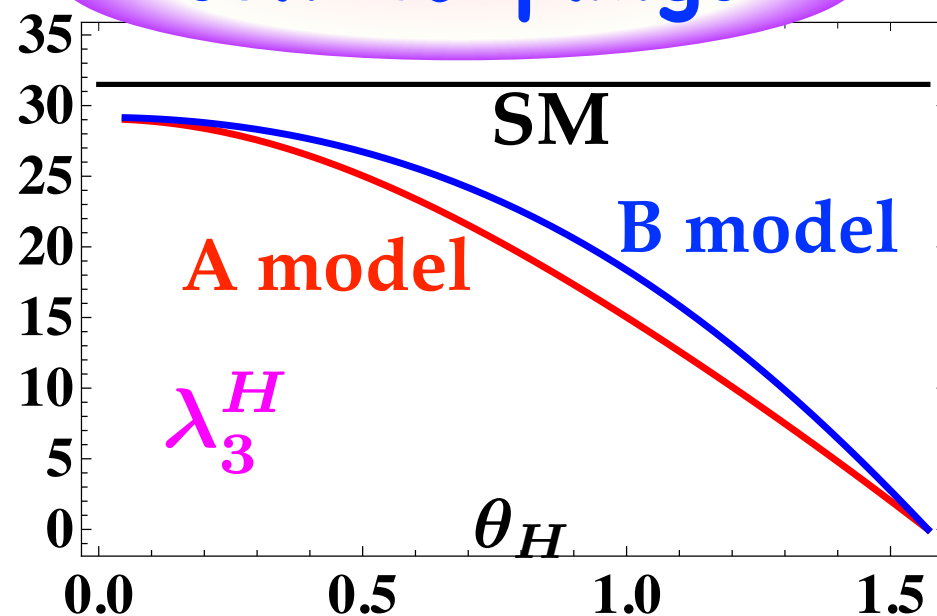
$$\sim (\text{SM}) \times \cos \theta_H$$

**Yukawa couplings**

$$\sim \begin{cases} (\text{SM}) \times \cos \theta_H & \text{A model} \\ (\text{SM}) \times \cos^2 \frac{1}{2} \theta_H & \text{B model} \end{cases}$$

**Deviation from SM is small for  $\theta_H \sim 0.1$**

## self-couplings



# New Particles

## Kaluza-Klein excitation modes

|                | $\theta_H$<br>[rad.] | $m_{KK}$<br>[TeV] | $z_L$                  | $k$<br>[GeV]           | $m_{\gamma^{(1)}}$<br>[TeV] | $\Gamma_{\gamma^{(1)}}$<br>[TeV] | $m_{Z^{(1)}}$<br>[TeV] | $\Gamma_{Z^{(1)}}$<br>[TeV] | $m_{Z_R^{(1)}}$<br>[TeV] | $\Gamma_{Z_R^{(1)}}$<br>[TeV] |
|----------------|----------------------|-------------------|------------------------|------------------------|-----------------------------|----------------------------------|------------------------|-----------------------------|--------------------------|-------------------------------|
| B <sup>L</sup> | 0.10                 | 11.00             | $1.980 \times 10^8$    | $6.933 \times 10^{11}$ | 8.715                       | 2.080                            | 8.713                  | 4.773                       | 8.420                    | 0.603                         |
| B              | 0.10                 | 13.00             | $3.865 \times 10^{11}$ | $1.599 \times 10^{15}$ | 10.20                       | 3.252                            | 10.20                  | 7.840                       | 9.951                    | 0.816                         |
| B <sup>H</sup> | 0.10                 | 15.00             | $2.667 \times 10^{15}$ | $1.273 \times 10^{19}$ | 11.69                       | 4.885                            | 11.69                  | 11.82                       | 11.48                    | 1.253                         |

$$Z' : Z^{(1)} \quad \gamma^{(1)} \quad Z_R^{(1)}$$

$$\sim 10 \text{ TeV}$$

# $Z'$ couplings in RS

$Z'$  :  $Z^{(1)}$   $\gamma^{(1)}$   $Z_R^{(1)}$   $m \sim 0.8 m_{\text{KK}}$   
localized **near IR**

|                                | $c_\ell$ , $c_q$ | left-handed<br>$\ell_L$ , $q_L$       | right-handed<br>$\ell_R$ , $q_R$      |
|--------------------------------|------------------|---------------------------------------|---------------------------------------|
| <b>A model</b>                 | $> 0$            | near UV                               | <b>near IR</b><br>large $Z'$ coupling |
| <b>B model</b><br>GUT inspired | $< 0$            | <b>near IR</b><br>large $Z'$ coupling | near UV                               |

$$\mathcal{M} = \begin{array}{c} e^- \\ e^+ \end{array} \begin{array}{c} \diagup \\ \diagdown \end{array} \begin{array}{c} Z, \gamma \\ \text{---} \\ \mathcal{M}_0 \end{array} \begin{array}{c} \diagdown \\ \diagup \end{array} \begin{array}{c} \mu^- \\ \mu^+ \end{array} + \begin{array}{c} e^- \\ e^+ \end{array} \begin{array}{c} \diagup \\ \diagdown \end{array} \begin{array}{c} Z' \\ Z_R^{(1)}, Z^{(1)}, \gamma^{(1)} \\ \text{---} \\ \mathcal{M}_{Z'} \end{array} \begin{array}{c} \diagdown \\ \diagup \end{array} \begin{array}{c} \mu^- \\ \mu^+ \end{array}$$

# Z' couplings in RS

$$\theta_H = 0.1, m_{KK} = 13 \text{ TeV}$$

| $f$        | $g_{Zf}^L$ <b>Z</b> | $g_{Zf}^R$ | $g_{Z^{(1)}f}^L$ <b>Z<sup>(1)</sup></b> | $g_{Z^{(1)}f}^R$ | $g_{Z_R^{(1)}f}^L$ <b>Z<sup>(1)</sup><sub>R</sub></b> | $g_{Z_R^{(1)}f}^R$ | $g_{\gamma^{(1)}f}^L$ <b>γ<sup>(1)</sup></b> | $g_{\gamma^{(1)}f}^R$ |
|------------|---------------------|------------|-----------------------------------------|------------------|-------------------------------------------------------|--------------------|----------------------------------------------|-----------------------|
| $\nu_e$    | 0.5687              | 0          | 3.2774                                  | 0                | -1.0322                                               | 0                  | 0                                            | 0                     |
| $\nu_\mu$  | 0.5687              | 0          | 3.1207                                  | 0                | -0.9852                                               | 0                  | 0                                            | 0                     |
| $\nu_\tau$ | 0.5687              | 0          | 3.0165                                  | 0                | -0.9539                                               | 0                  | 0                                            | 0                     |
| $e$        | -0.3058             | 0.2629     | -1.7621                                 | -0.0584          | -1.0444                                               | 0                  | -2.7587                                      | 0.1071                |
| $\mu$      | -0.3058             | 0.2629     | -1.6778                                 | -0.0584          | -0.9969                                               | 0                  | -2.6268                                      | 0.1071                |
| $\tau$     | -0.3058             | 0.2629     | -1.6218                                 | -0.0584          | -0.9652                                               | 0.0001             | -2.5391                                      | 0.1070                |
| $u$        | 0.3934              | -0.1753    | 2.1951                                  | 0.0390           | 0.3415                                                | 0                  | 1.7807                                       | -0.0714               |
| $c$        | 0.3934              | -0.1753    | 2.1147                                  | 0.0389           | 0.3296                                                | 0                  | 1.7154                                       | -0.0714               |
| $t$        | 0.3938              | -0.1749    | 1.7406                                  | -0.3269          | 0.2740                                                | -0.7395            | 1.4121                                       | 0.6017                |
| $d$        | -0.4811             | 0.0876     | -2.6842                                 | 0.1162           | 0.3297                                                | -0.1801            | -0.8904                                      | -0.2113               |
| $s$        | -0.4811             | 0.0876     | -2.5858                                 | 0.1460           | 0.3182                                                | -0.2197            | -0.8577                                      | -0.2657               |
| $b$        | -0.4811             | 0.0876     | -2.1284                                 | 0.2900           | 0.2646                                                | -0.4096            | -0.7059                                      | -0.5279               |

large

in units of  $g_w$

$$\mathcal{M} = \begin{array}{c} e^- \\ e^+ \end{array} \begin{array}{c} \diagup \\ \diagdown \end{array} \begin{array}{c} \gamma, Z, Z' \\ \text{---} \end{array} \begin{array}{c} \diagdown \\ \diagup \end{array} \begin{array}{c} f \\ \bar{f} \end{array}$$

$$\frac{d\sigma^{f\bar{f}}}{d\cos\theta} = \frac{1 - P_{e^-}P_{e^+}}{4} \left\{ (1 - P_{\text{eff}}) \frac{d\sigma_{LR}^{f\bar{f}}}{d\cos\theta} + (1 + P_{\text{eff}}) \frac{d\sigma_{RL}^{f\bar{f}}}{d\cos\theta} \right\}$$

$$\sigma_{LR}^{f\bar{f}} : e_L^- e_R^+ \rightarrow f\bar{f}$$

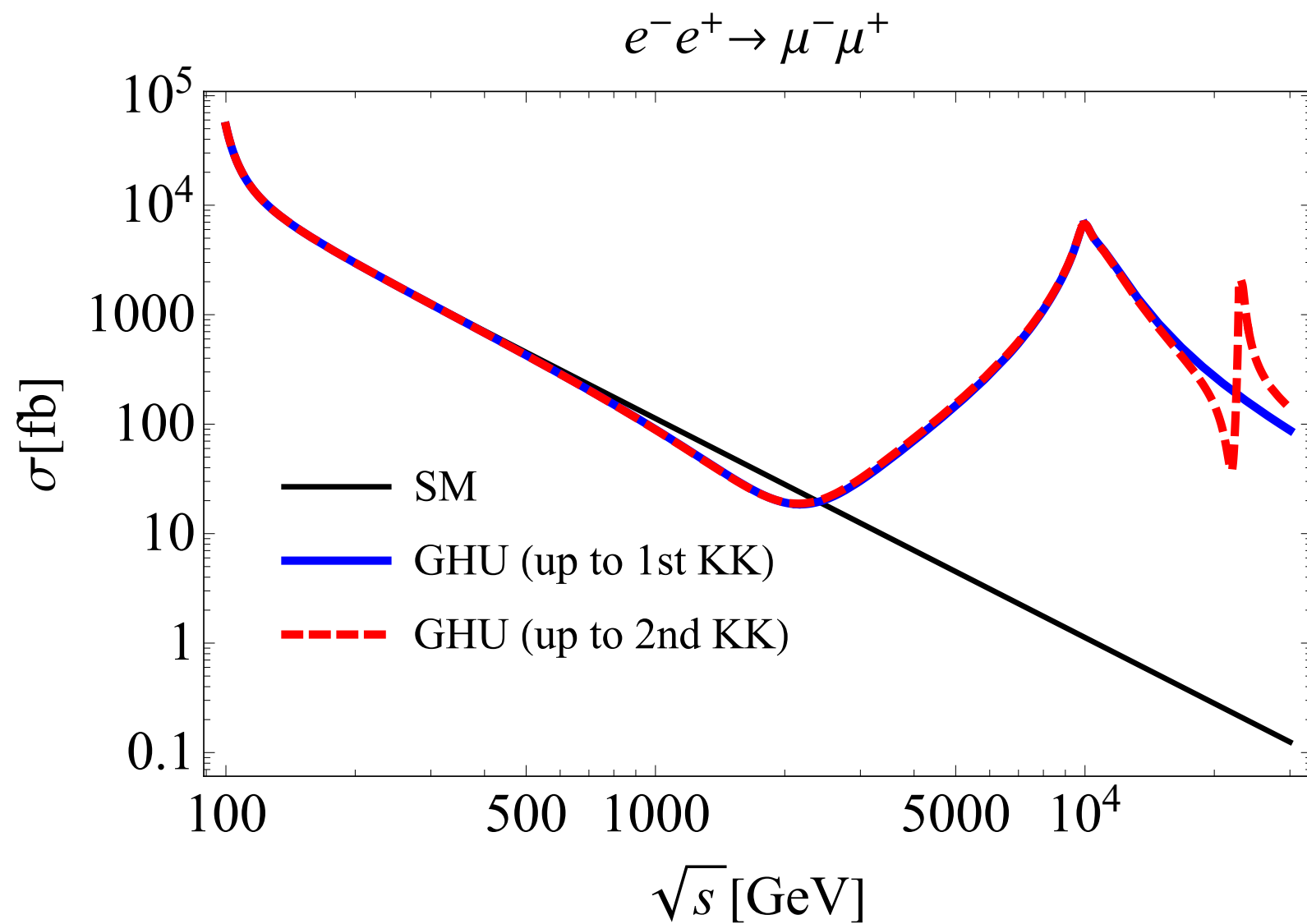
$$\sigma_{RL}^{f\bar{f}} : e_R^- e_L^+ \rightarrow f\bar{f}$$

$$P_{\text{eff}} \equiv \frac{P_{e^-} - P_{e^+}}{1 - P_{e^-}P_{e^+}} \quad \begin{array}{l} |P_{e^-}| \leq 0.8 \\ |P_{e^+}| \leq 0.3 \end{array} \quad \text{at ILC}$$

$$\frac{d\sigma_{LR}^{f\bar{f}}}{d\cos\theta} \overset{\text{RL}}{\simeq} \frac{s}{32\pi} \left\{ (1 + \cos\theta)^2 |Q_{e_L f_L}|^2 + (1 - \cos\theta)^2 |Q_{e_L f_R}|^2 \right\}$$

$$Q_{e_L f_L} \overset{\substack{\text{R} \\ \uparrow}}{\equiv} \sum_i \frac{g_{V_i e}^L \overset{\substack{\text{R} \\ \downarrow}}{g_{V_i f}^L}}{(s - m_{V_i}^2) + im_{V_i}\Gamma_{V_i}}, \quad |Q_{e_L f_L}| : \text{large}$$

$$e^+e^- \rightarrow \mu^+\mu^-$$



$$\theta_H = 0.1, \quad m_{\text{KK}} = 13 \text{ TeV}$$

**Contributions from 2nd KK modes  
small for  $\sqrt{s} < 3 \text{ TeV}$**

# ILC

$$\mathcal{M} = \begin{array}{c} e^- \\ e^+ \end{array} \begin{array}{c} \diagup \\ \diagdown \end{array} \begin{array}{c} Z, \gamma \\ \text{---} \end{array} \begin{array}{c} \diagdown \\ \diagup \end{array} \begin{array}{c} \mu^- \\ \mu^+ \end{array} \mathcal{M}_0 + \begin{array}{c} e^- \\ e^+ \end{array} \begin{array}{c} \diagup \\ \diagdown \end{array} \begin{array}{c} Z'^{(1)}, Z^{(1)}, \gamma^{(1)} \\ \text{---} \end{array} \begin{array}{c} \diagdown \\ \diagup \end{array} \begin{array}{c} \mu^- \\ \mu^+ \end{array} \mathcal{M}_{Z'}$$

$$m_Z^2 \ll s \ll m_{Z'}^2$$

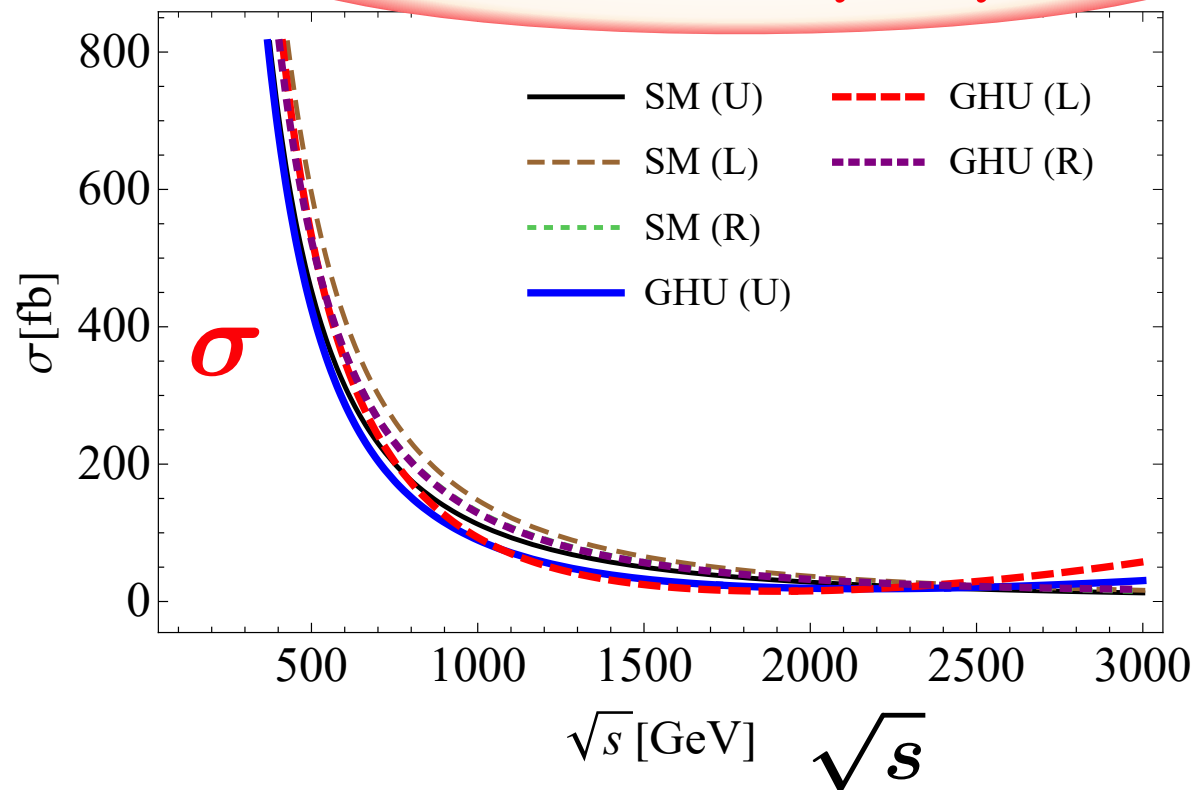
$$(250 \text{ GeV})^2 \sim (1 \text{ TeV})^2$$

## interference effects

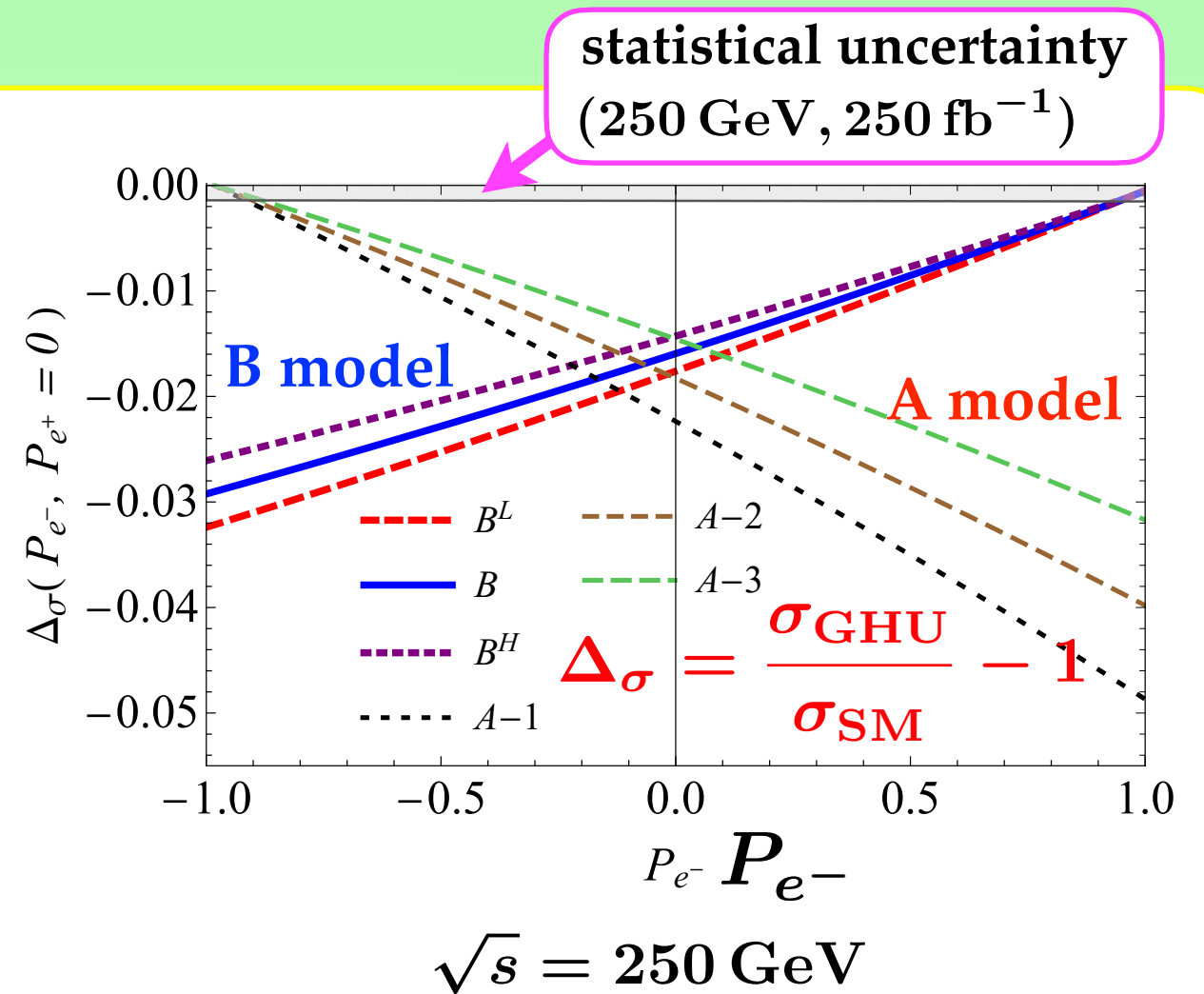
$$\frac{\mathcal{M}_0 \mathcal{M}_{Z'}^*}{|\mathcal{M}_0|^2} \sim -15 \frac{s}{m_{Z'}^2}$$

$$\sim -0.02 \quad \text{at } \sqrt{s} = 250 \text{ GeV}$$

$$e^+e^- \rightarrow \mu^+\mu^-$$



$$\theta_H = 0.1, m_{KK} = 13 \text{ TeV}$$



|   | $(P_{e^-}, P_{e^+})$ |
|---|----------------------|
| U | (0, 0)               |
| L | (-0.8, +0.3)         |
| R | (+0.8, -0.3)         |

|       | B model    |          | A model    |              |
|-------|------------|----------|------------|--------------|
|       | $\theta_H$ | $m_{KK}$ | $\theta_H$ | $m_{KK}$     |
| $B^L$ | 0.10       | 11 TeV   | $A_1$      | 0.10 8.1 TeV |
| $B$   | 0.10       | 13 TeV   | $A_2$      | 0.09 8.7 TeV |
| $B^H$ | 0.10       | 15 TeV   | $A_3$      | 0.08 9.5 TeV |

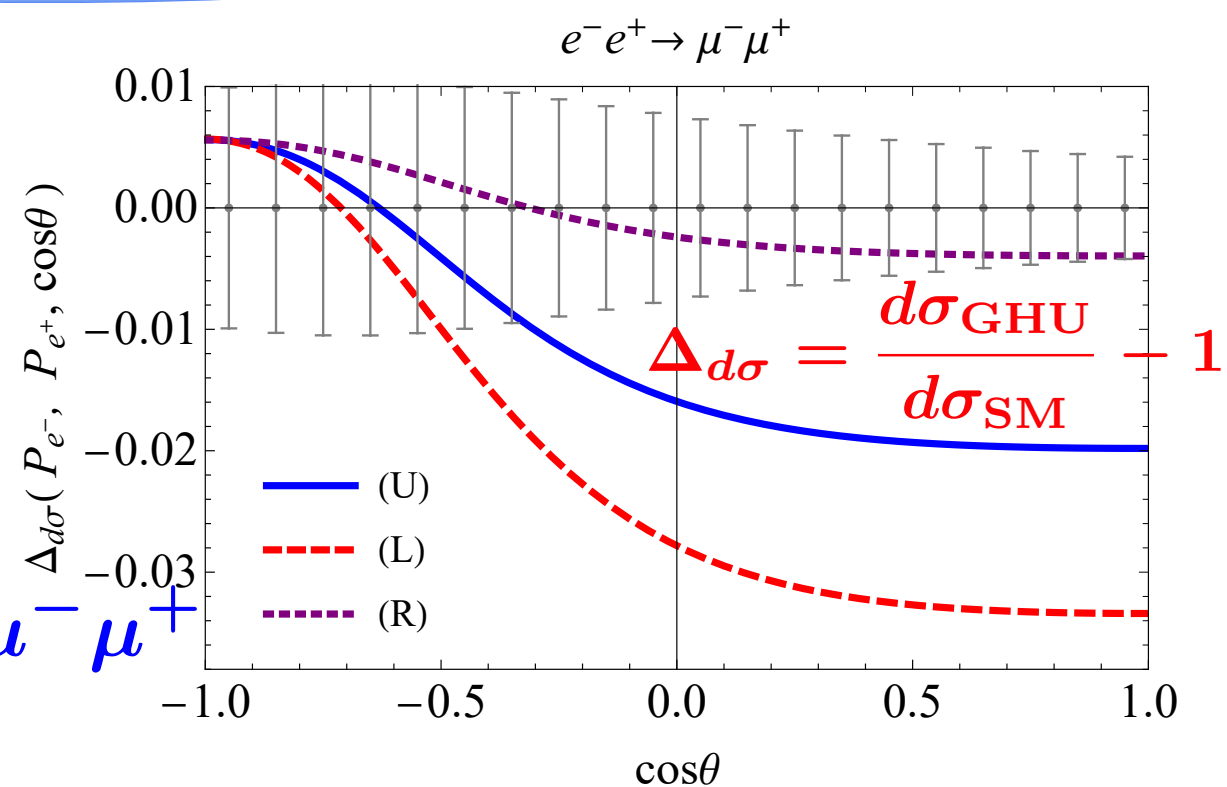
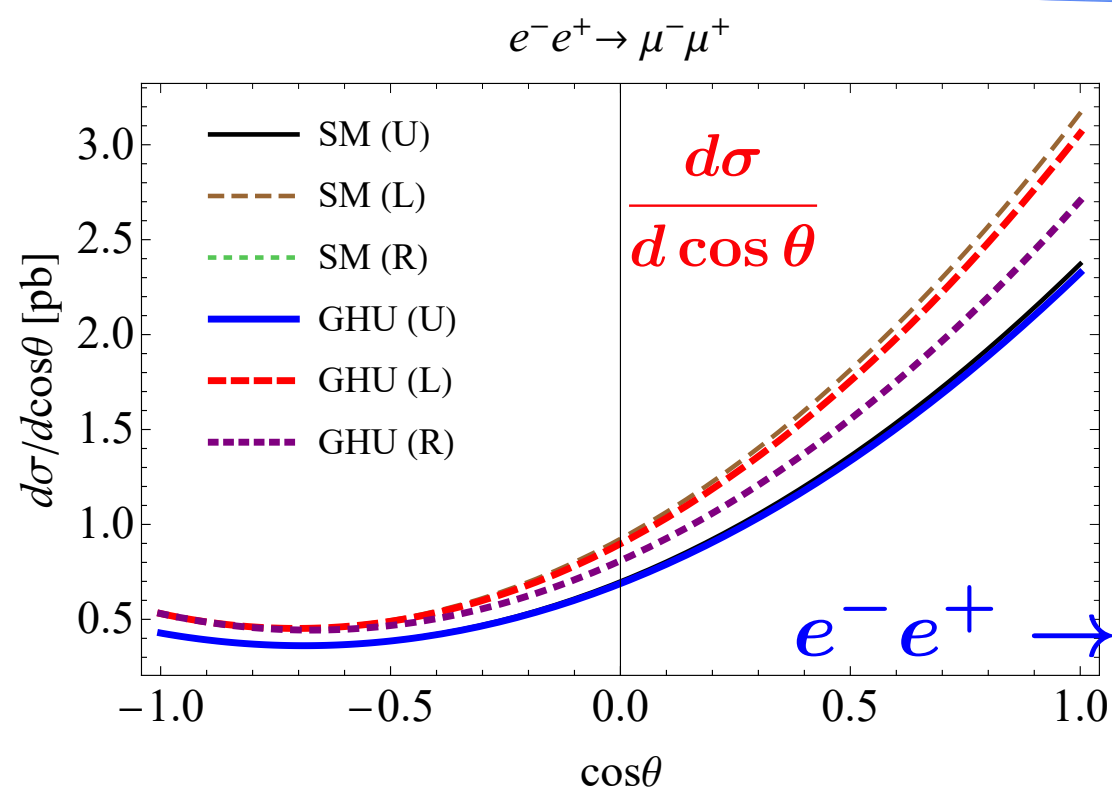
Distinguish

A model

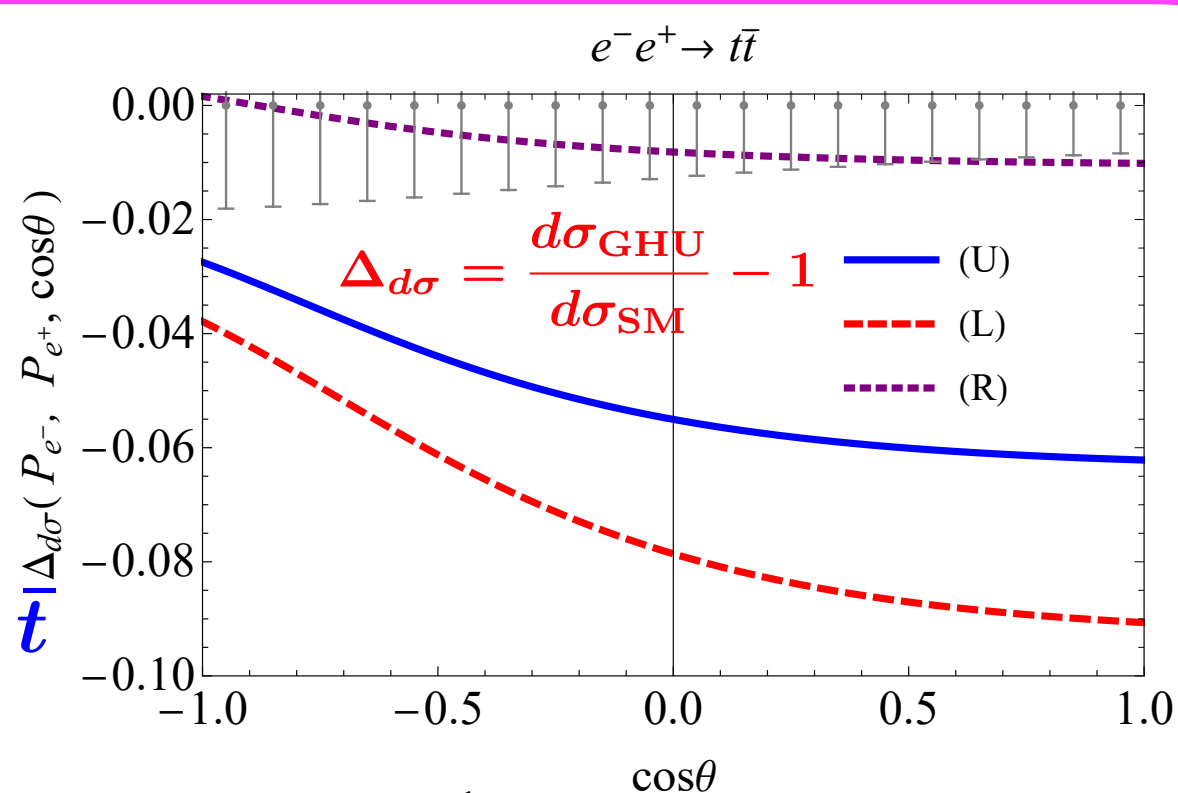
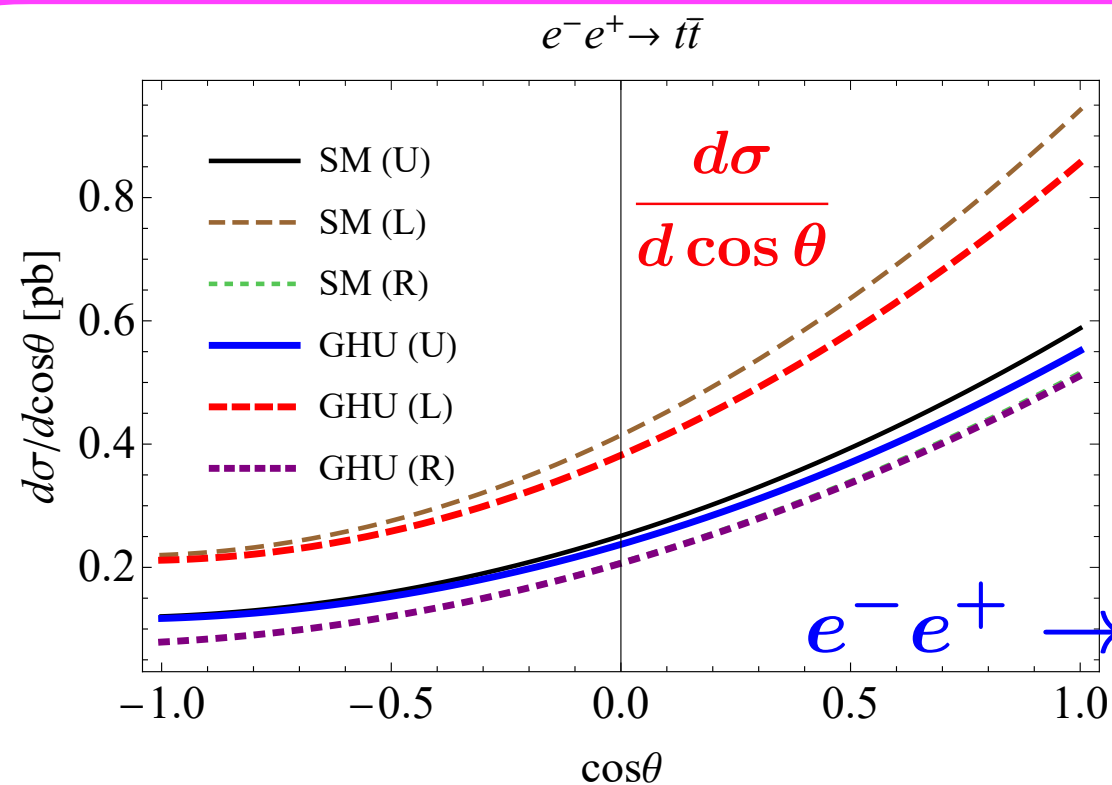
B model

by polarization dependence

# Angular distribution



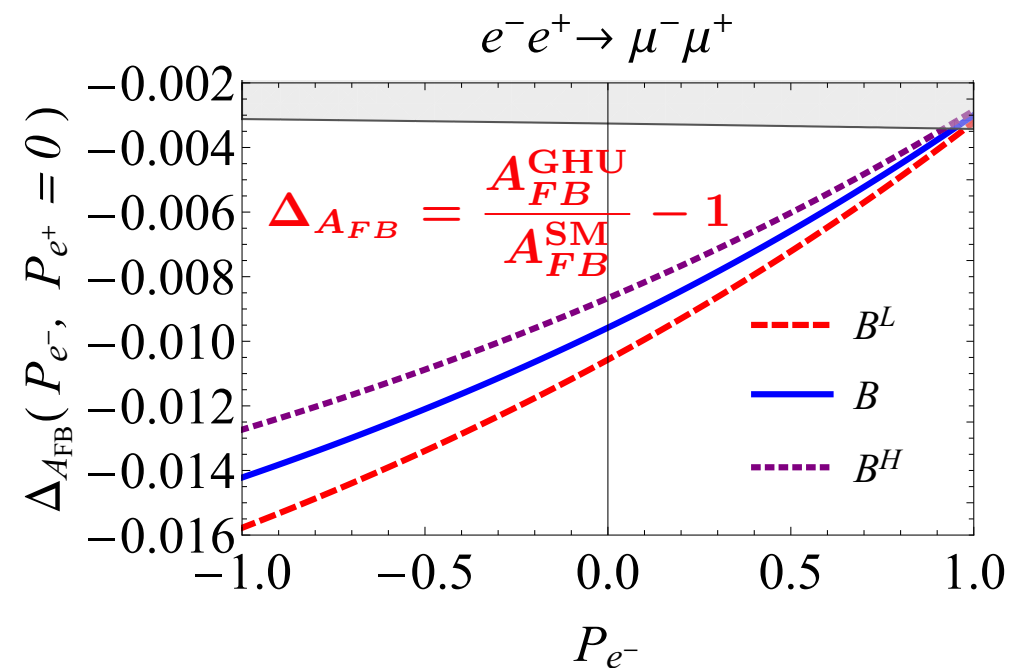
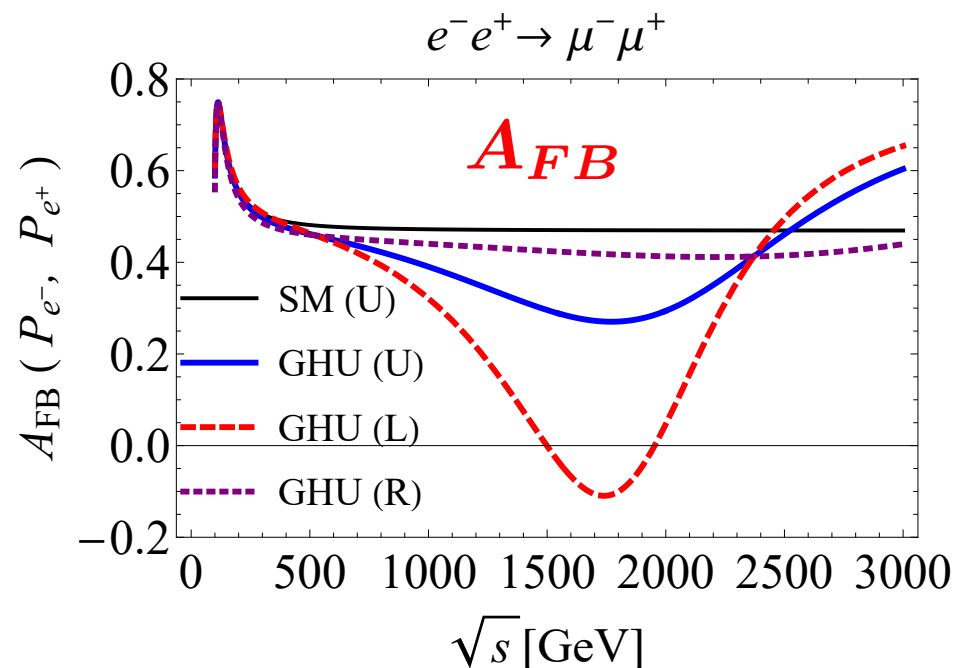
$\theta_H = 0.1$  ,  $m_{\text{KK}} = 13 \text{ TeV}$  (250 GeV, 250 fb<sup>-1</sup>)



$\theta_H = 0.1$  ,  $m_{\text{KK}} = 13 \text{ TeV}$  (500 GeV, 500 fb<sup>-1</sup>)

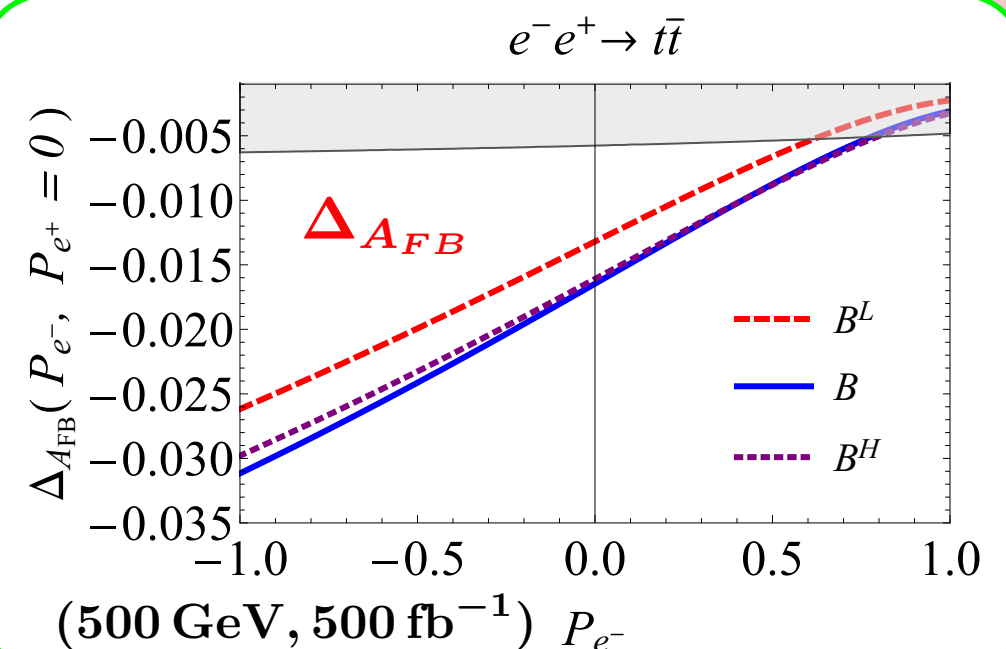
# Forward-backward asymmetry

$$A_{FB} = \frac{\sigma_{\text{forward}} - \sigma_{\text{backward}}}{\sigma_{\text{forward}} + \sigma_{\text{backward}}}$$



$\theta_H = 0.1$ ,  $m_{KK} = 13$  TeV (250 GeV, 250 fb $^{-1}$ )

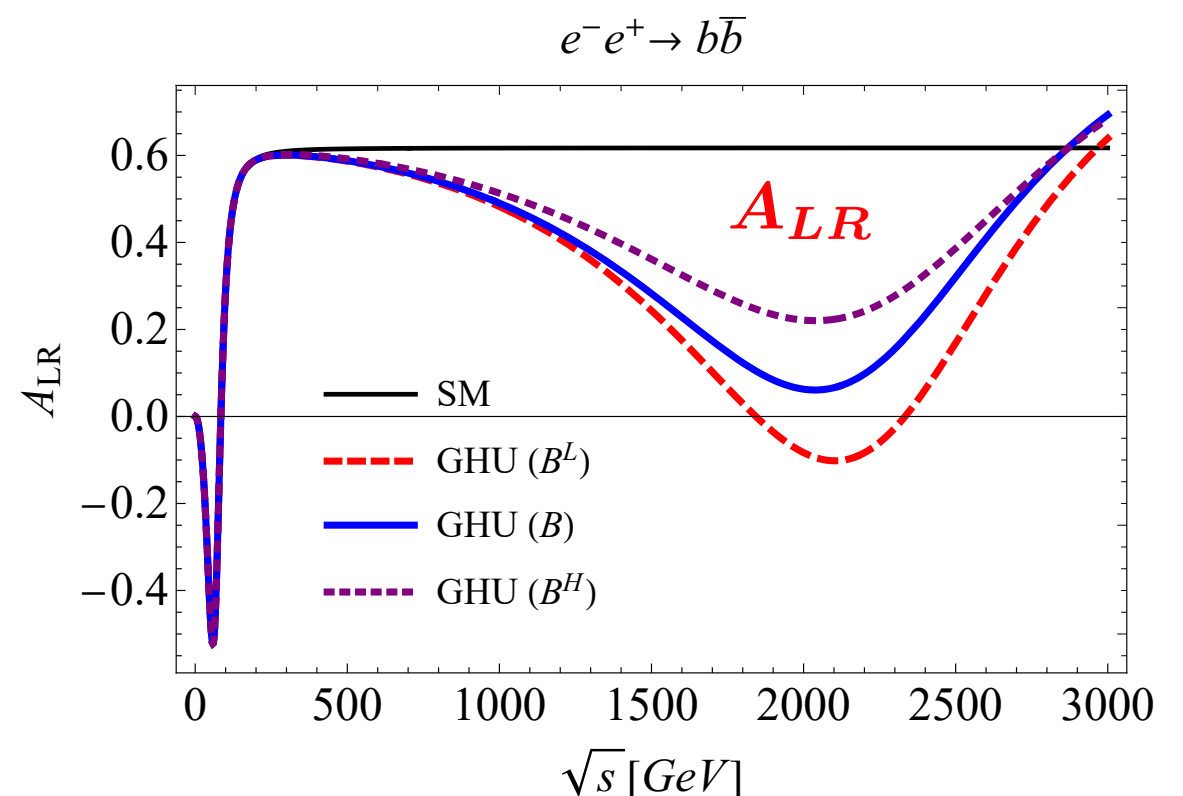
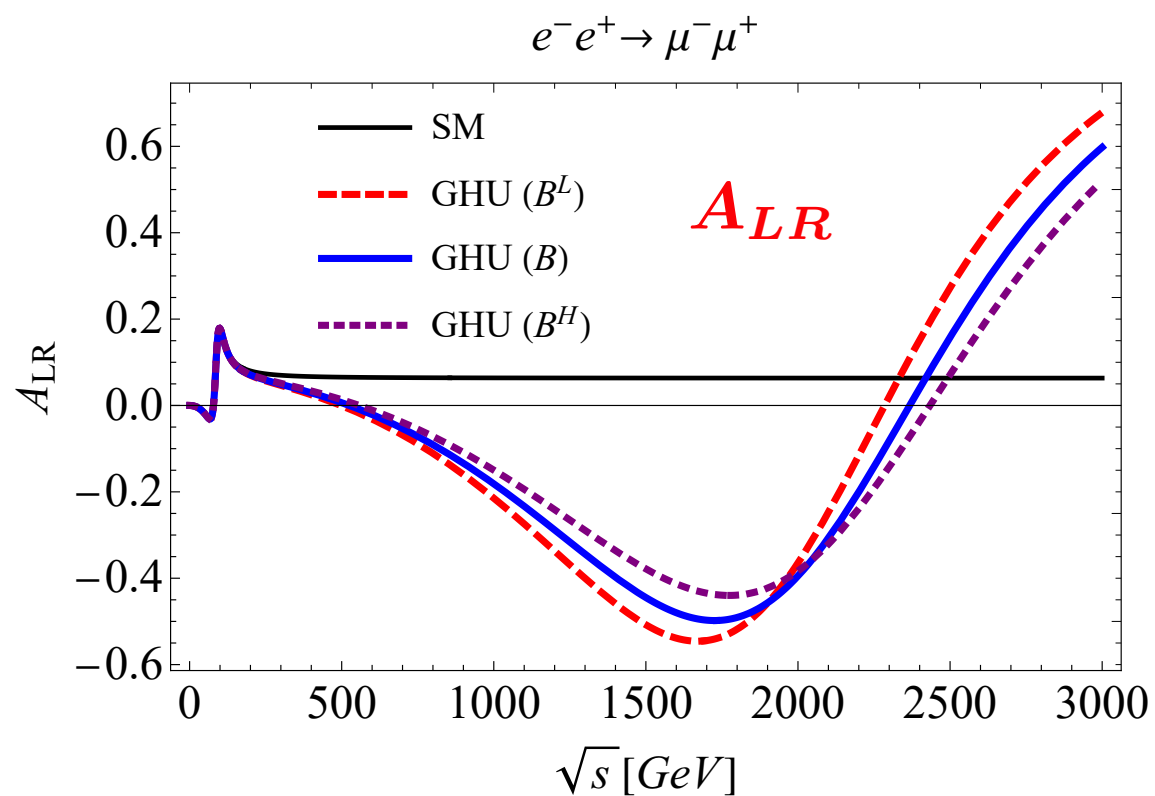
|     | $(P_{e^-}, P_{e^+})$ |
|-----|----------------------|
| $U$ | (0, 0)               |
| $L$ | (-0.8, +0.3)         |
| $R$ | (+0.8, -0.3)         |



# Left-right asymmetry

$$A_{LR} = \frac{\sigma_{LR} - \sigma_{RL}}{\sigma_{LR} + \sigma_{RL}}$$

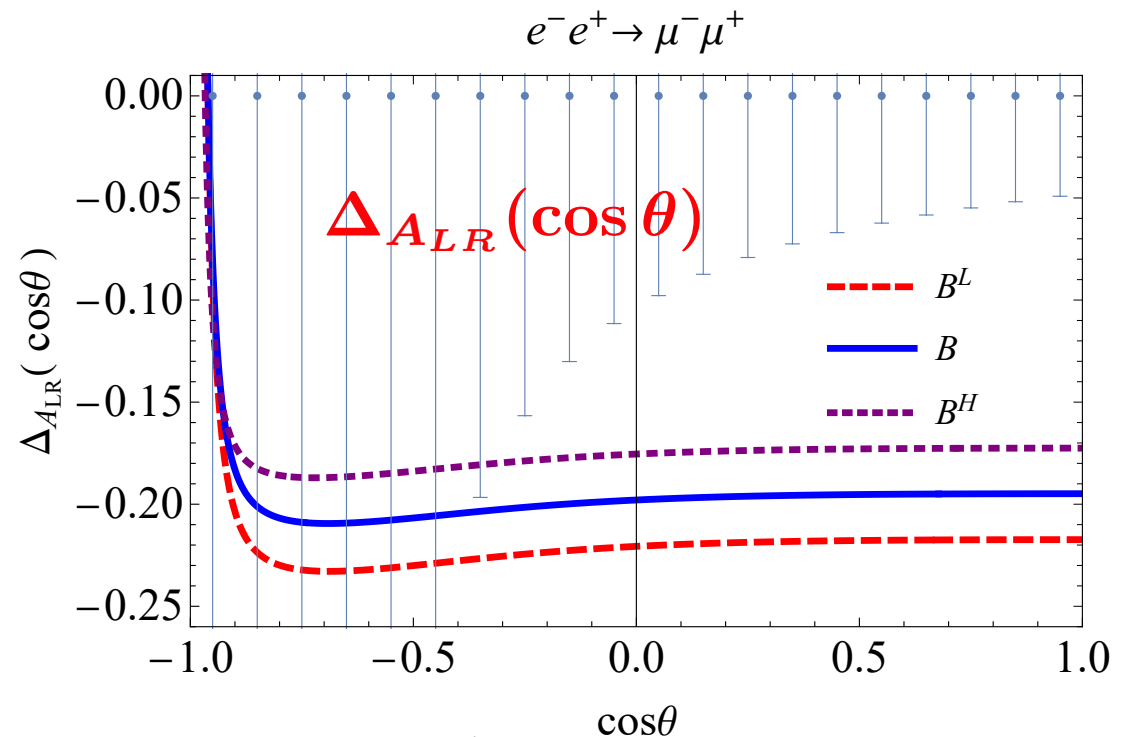
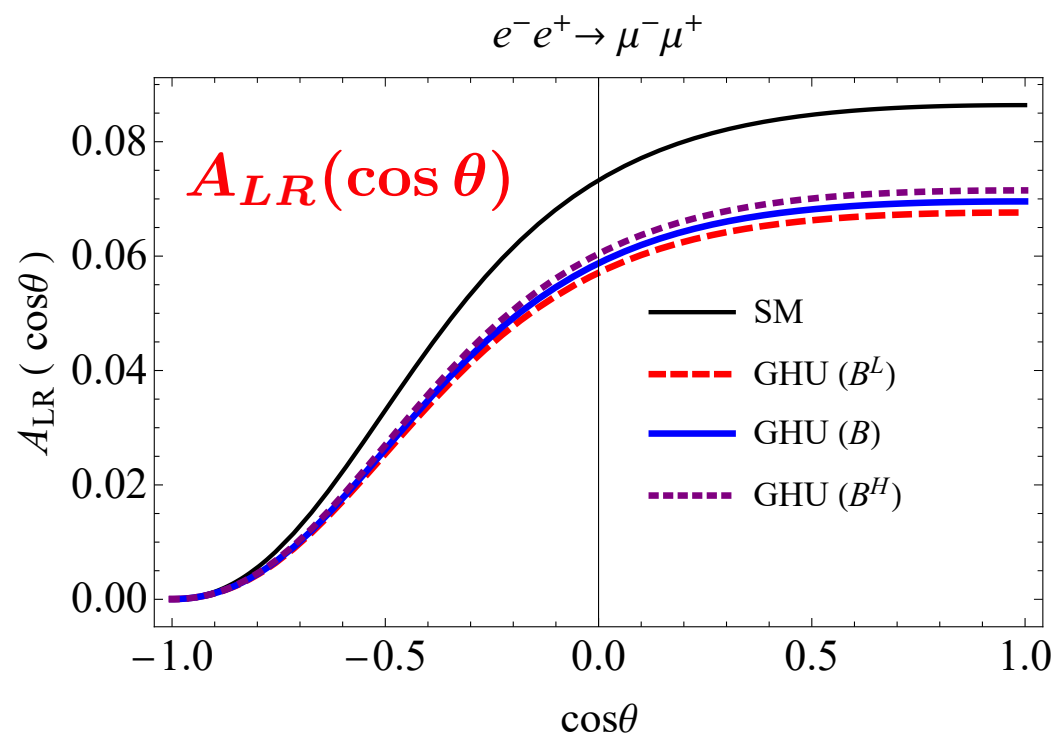
$$= \frac{1}{P_{\text{eff}}} \frac{\sigma(P_{e-}, P_{e+}) - \sigma(-P_{e-}, -P_{e+})}{\sigma(P_{e-}, P_{e+}) + \sigma(-P_{e-}, -P_{e+})}$$



# Differential left-right asymmetry

$$A_{LR}(\cos \theta) = \frac{d\sigma_{LR} - d\sigma_{RL}}{d\sigma_{LR} + d\sigma_{RL}} \Leftrightarrow d\sigma_{LR} \equiv \frac{d\sigma_{LR}}{d\cos \theta}$$

$$= \frac{1}{P_{\text{eff}}} \frac{d\sigma(P_{e-}, P_{e+}) - d\sigma(-P_{e-}, -P_{e+})}{d\sigma(P_{e-}, P_{e+}) + d\sigma(-P_{e-}, -P_{e+})} \Leftrightarrow d\sigma(P_{e-}, P_{e+}) \equiv \frac{d\sigma(P_{e-}, P_{e+})}{d\cos \theta}$$



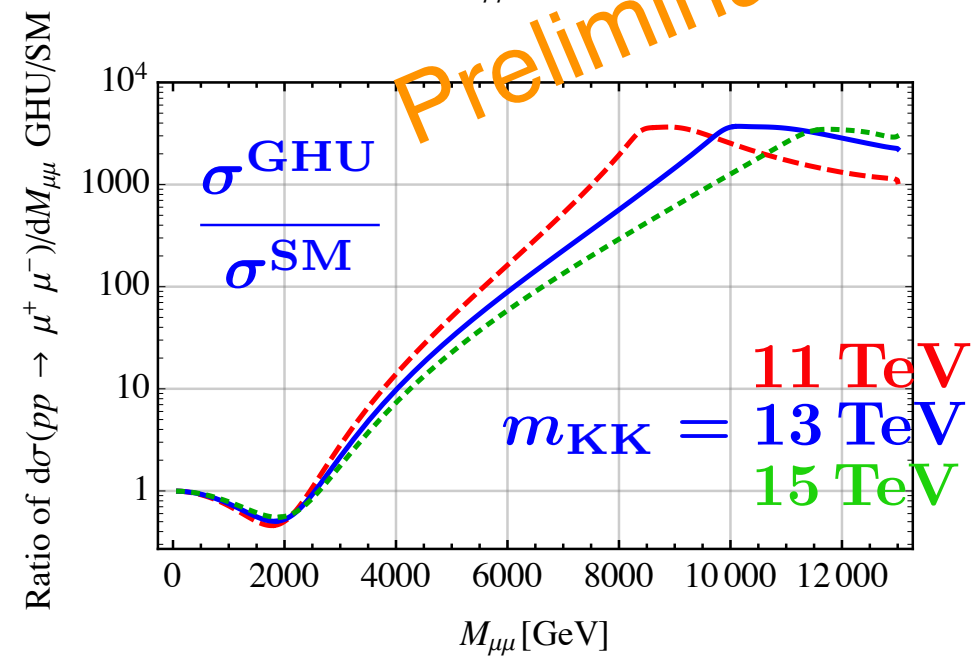
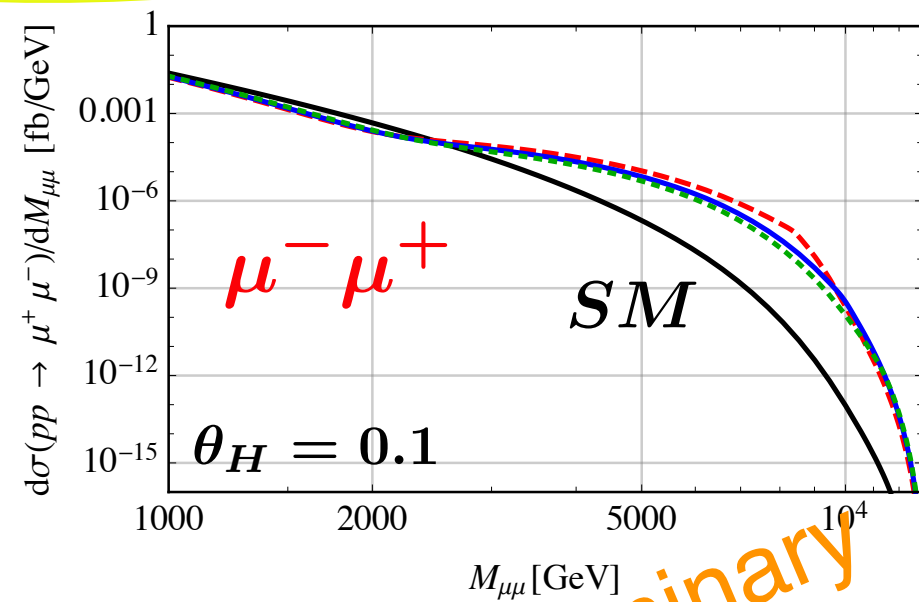
$$\theta_H = 0.10, \sqrt{s} = 250 \text{ GeV}, 250 \text{ fb}^{-1}$$

# LHC signals

$$p p \xrightarrow{Z'} e^- e^+, \mu^- \mu^+$$

$$p p \xrightarrow{g^{(1)}} t \bar{t}$$

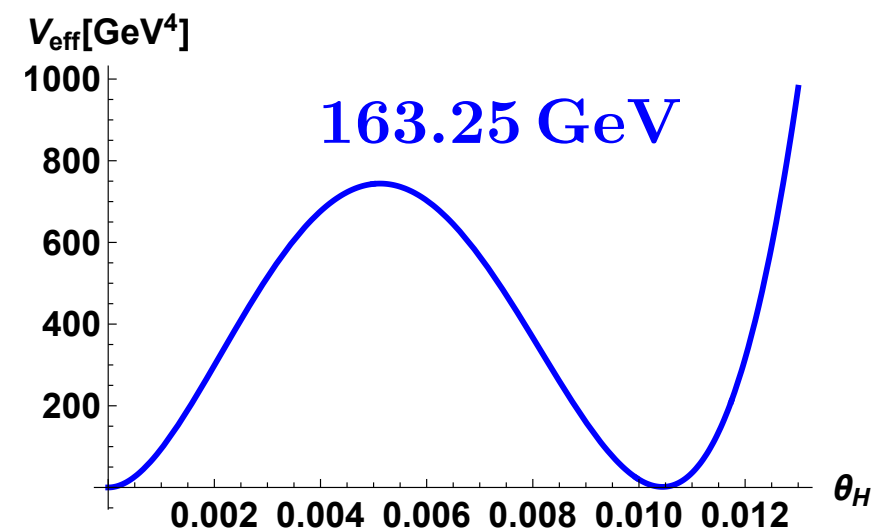
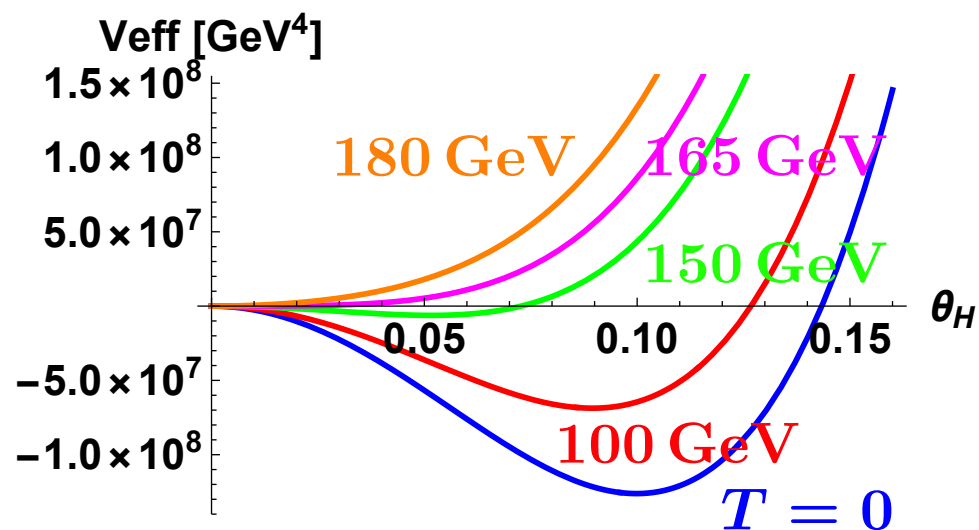
$$p p \xrightarrow{W'} t \bar{b}$$



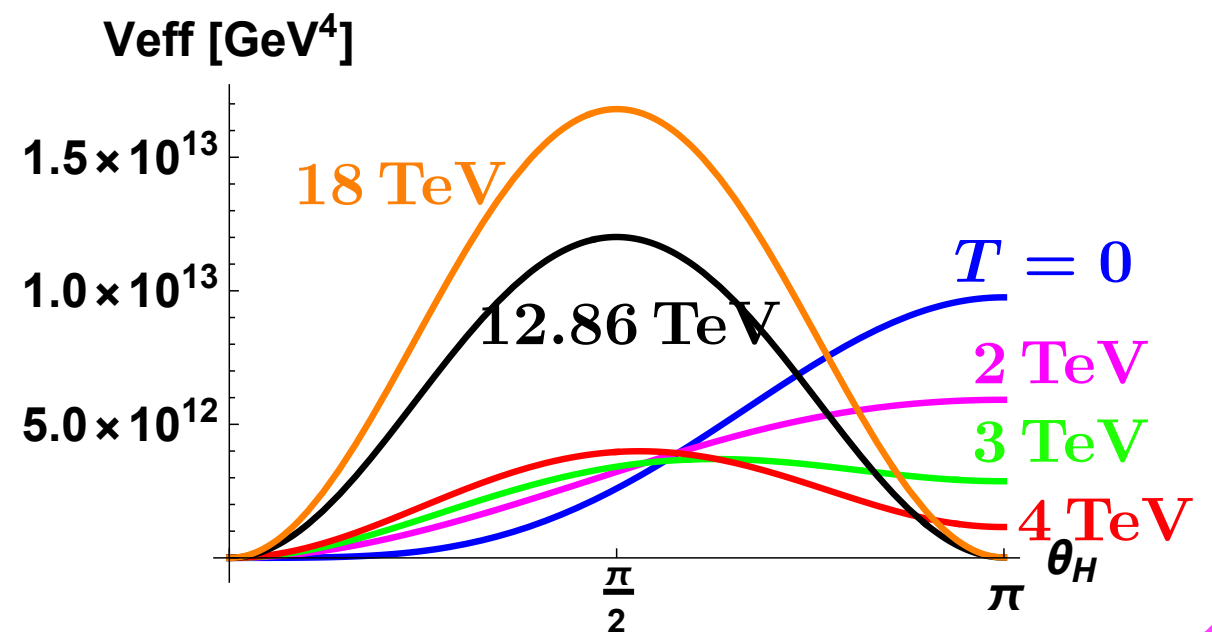
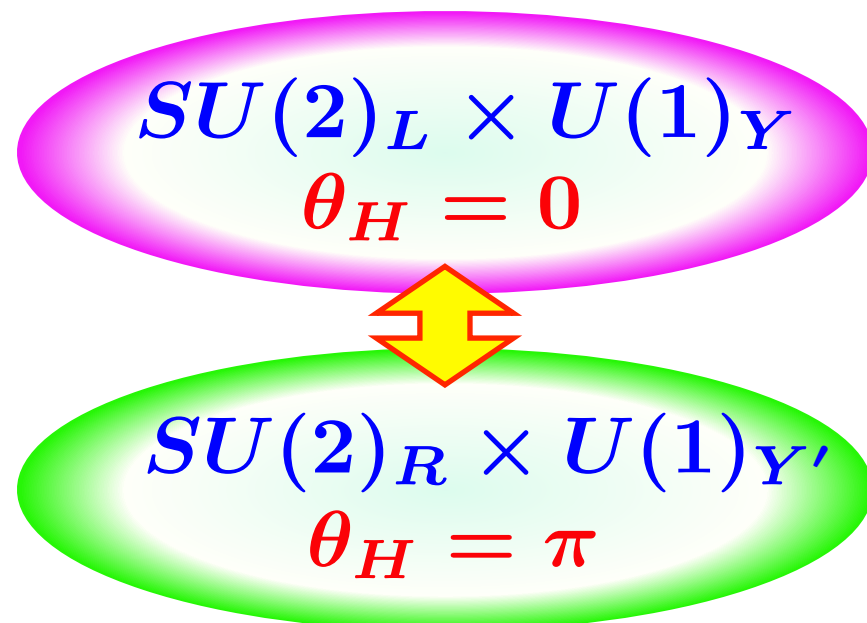
# Phase transitions

[arXiv: 2103.16320]

## Electroweak transition: similar to SM



## Left-right transition:



## Summary

GUT inspired gauge-Higgs unification

New particles  $Z'$  & extra dimensions  
can be explored

$$\left| e^- e^+ \rightarrow Z, \gamma \rightarrow f \bar{f} + e^- e^+ \rightarrow Z_R^{(1)}, Z^{(1)}, \gamma^{(1)} \rightarrow f \bar{f} \right|^2$$

in the early stage of **ILC 250**