

Reacciones con núcleos exóticos: desarrollos teóricos e interpretación de datos experimentales

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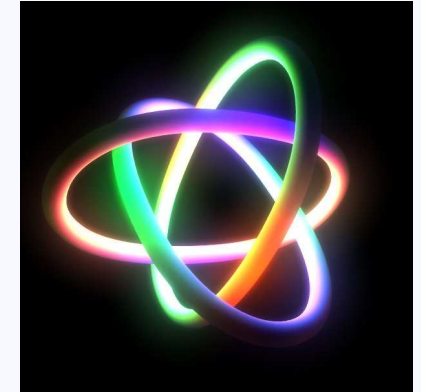
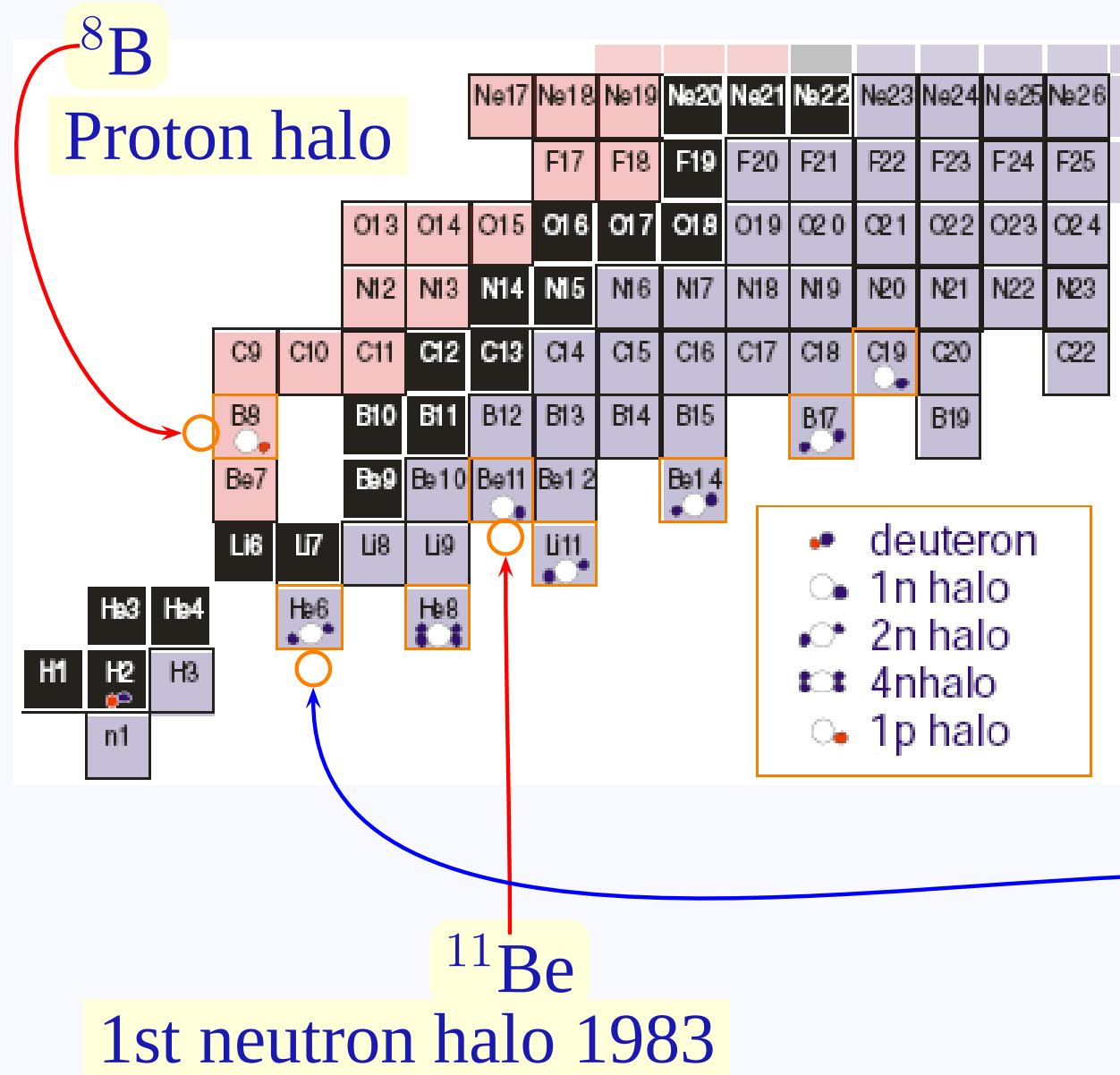
Universidad de Sevilla



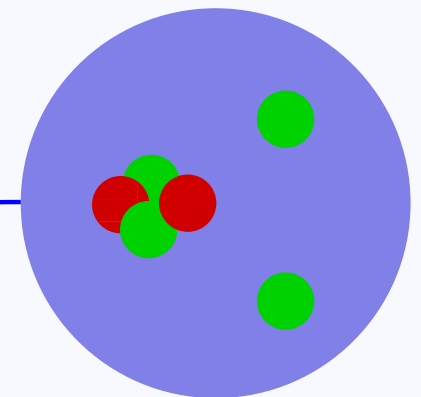
Esquema

- ⇒ Motivación: núcleos halo
- ⇒ Líneas de investigación desarrolladas:
 - ⇒ Estructura de sistemas débilmente ligados
 - ⇒ Reacciones nucleares de 3 y 4 cuerpos: continuum-discretized coupled-channels (CDCC)
 - ➔ Observables de ruptura de 4 cuerpos
 - ✓ Apoyo a grupos experimentales
 - ⇒ Reacciones nucleares de interés astrofísico
 - ⇒ Reacciones nucleares de 3 cuerpos: ecuaciones Faddeev/AGS
 - ★ Reacciones de moléculas débilmente ligadas
- ⇒ Nuevas líneas a investigar

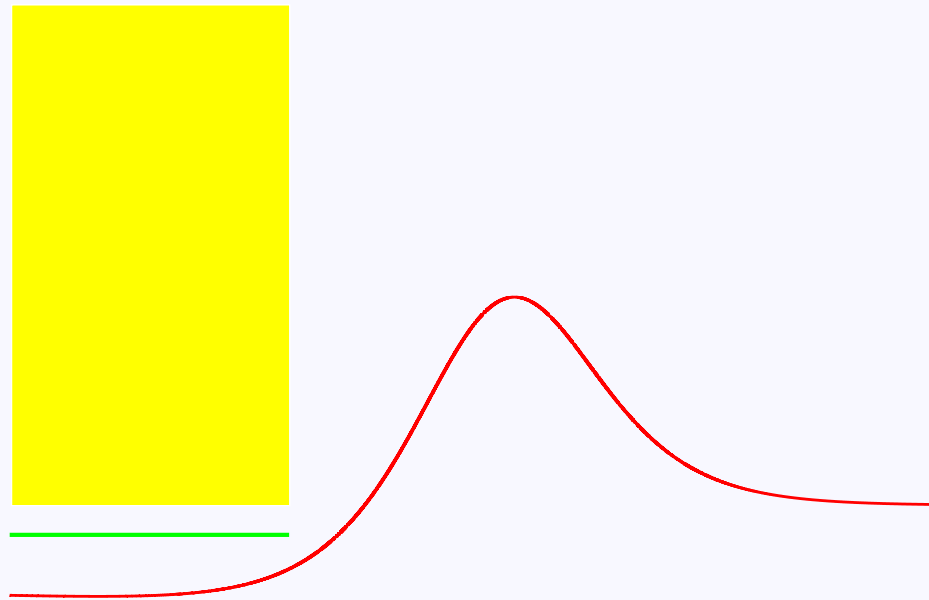
Motivación: Núcleos halo



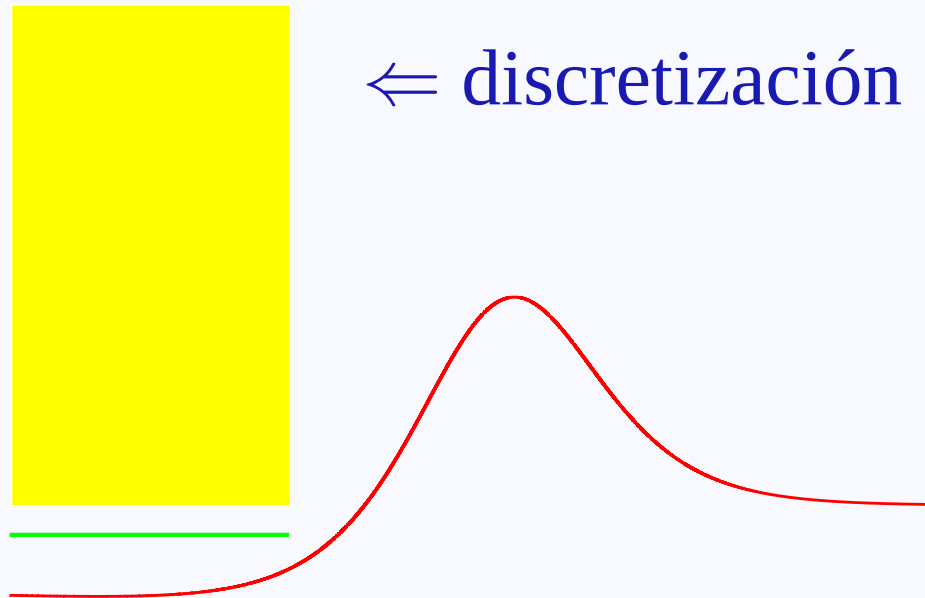
Borromean
2-neutron halo



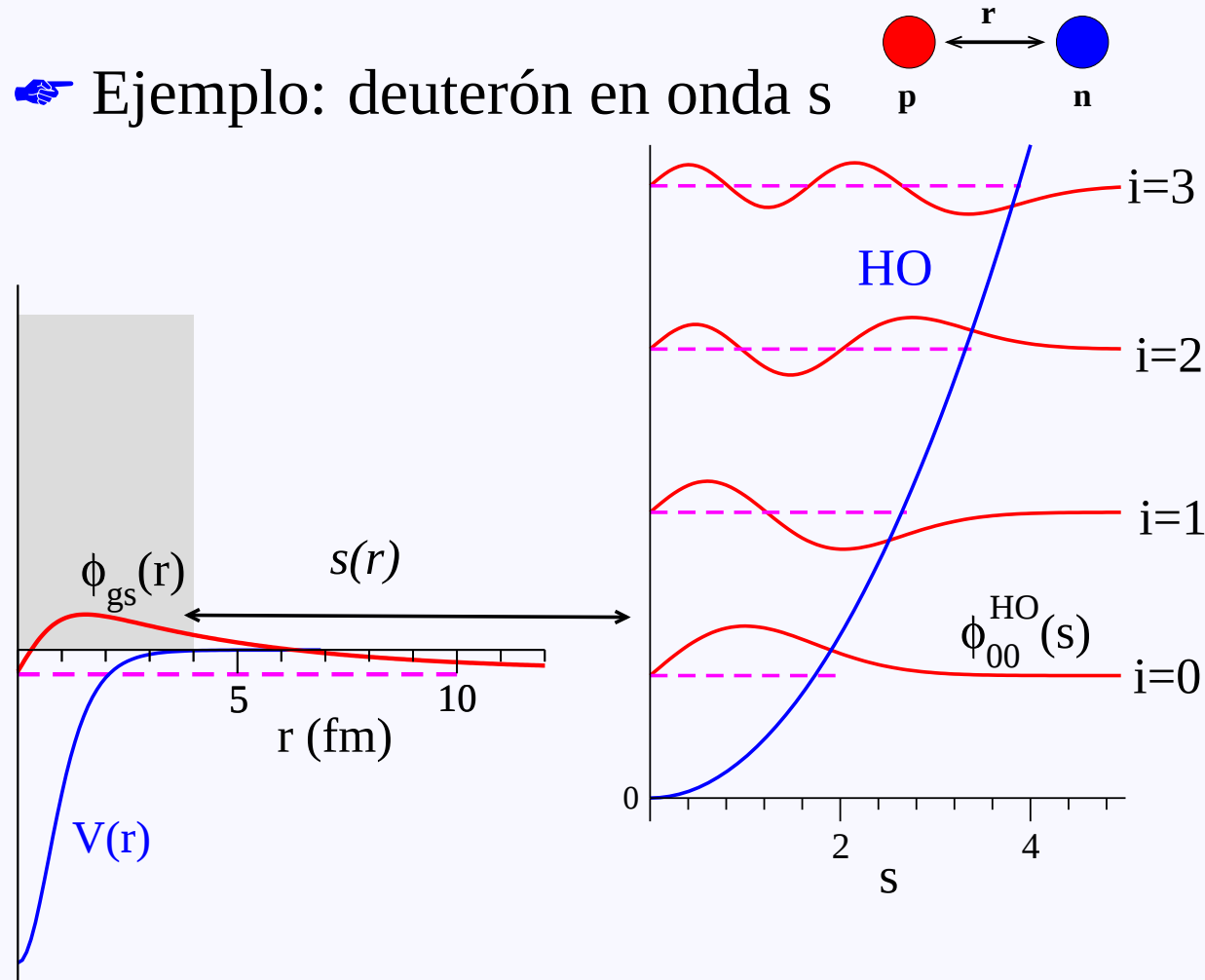
Estructura de sistemas débilmente ligados



Estructura de sistemas débilmente ligados



Método THO

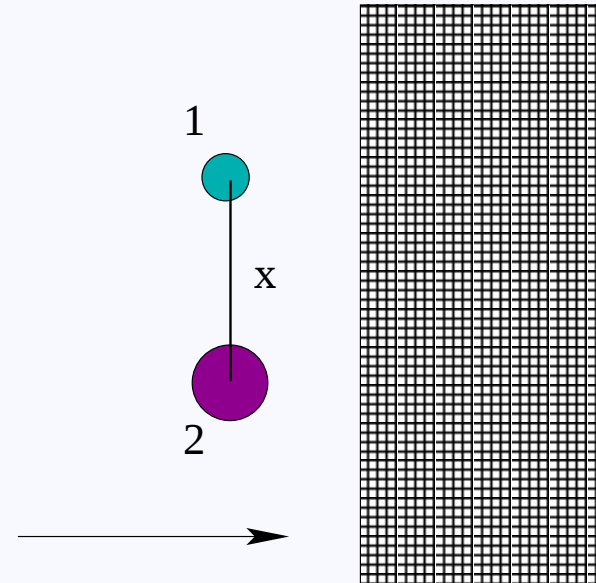


$$\int_0^r dr' r'^2 |\phi_{gs}(r')|^2 = \int_0^s ds' s'^2 |\phi_{00}^{HO}(s')|^2$$

Polarizabilidad sistema 2 cuerpos

$$\alpha(THO) = \sum_n (\langle B | P_2(x) | n \rangle \langle n | P_2(x) | B \rangle) / (\varepsilon_n - \varepsilon_B)$$

i_{max}	α ($e^2 fm^2 / MeV$)
1	0.52155
2	0.70895
3	0.71720
4	0.71721
5	0.71721
exacto	0.71721

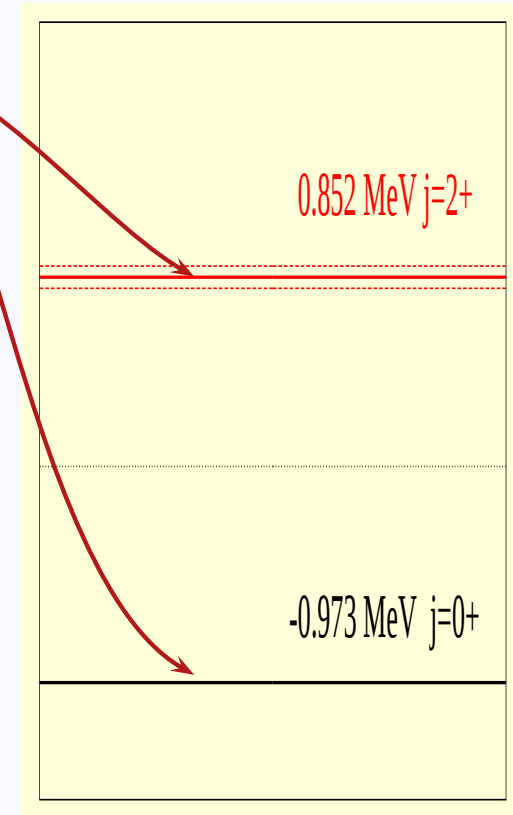


✚ I. Martel, et al., **PRA** 65 (2002) 052708

Propiedades de estructura: ${}^6\text{He}$

$$\hat{H}(\rho, \Omega) = \hat{T}(\rho, \Omega) + \hat{V}(\rho, \Omega)$$

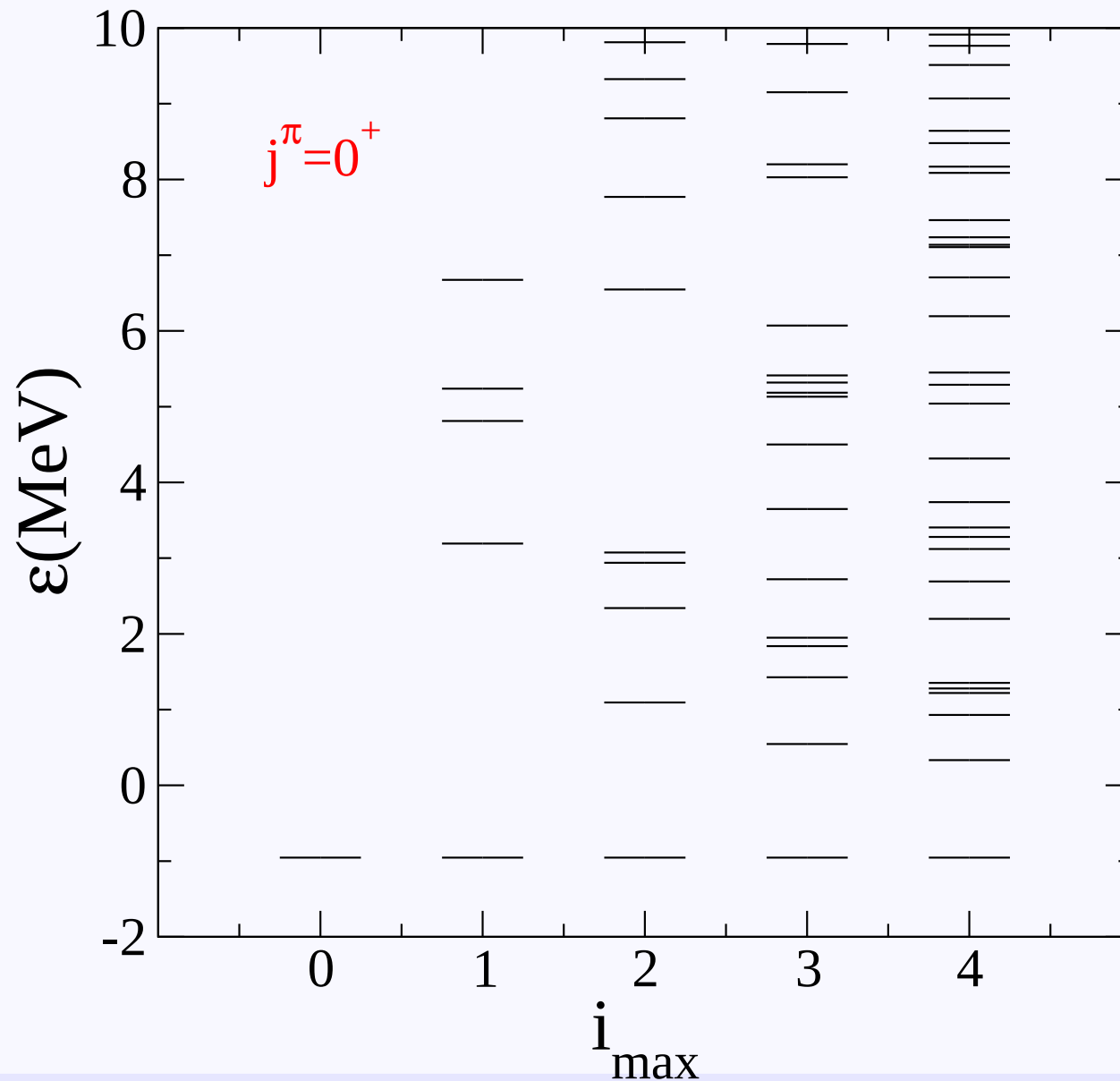
$$V = V_{n\alpha} + V_{n\alpha} + V_{nn} + V_{nn\alpha}$$



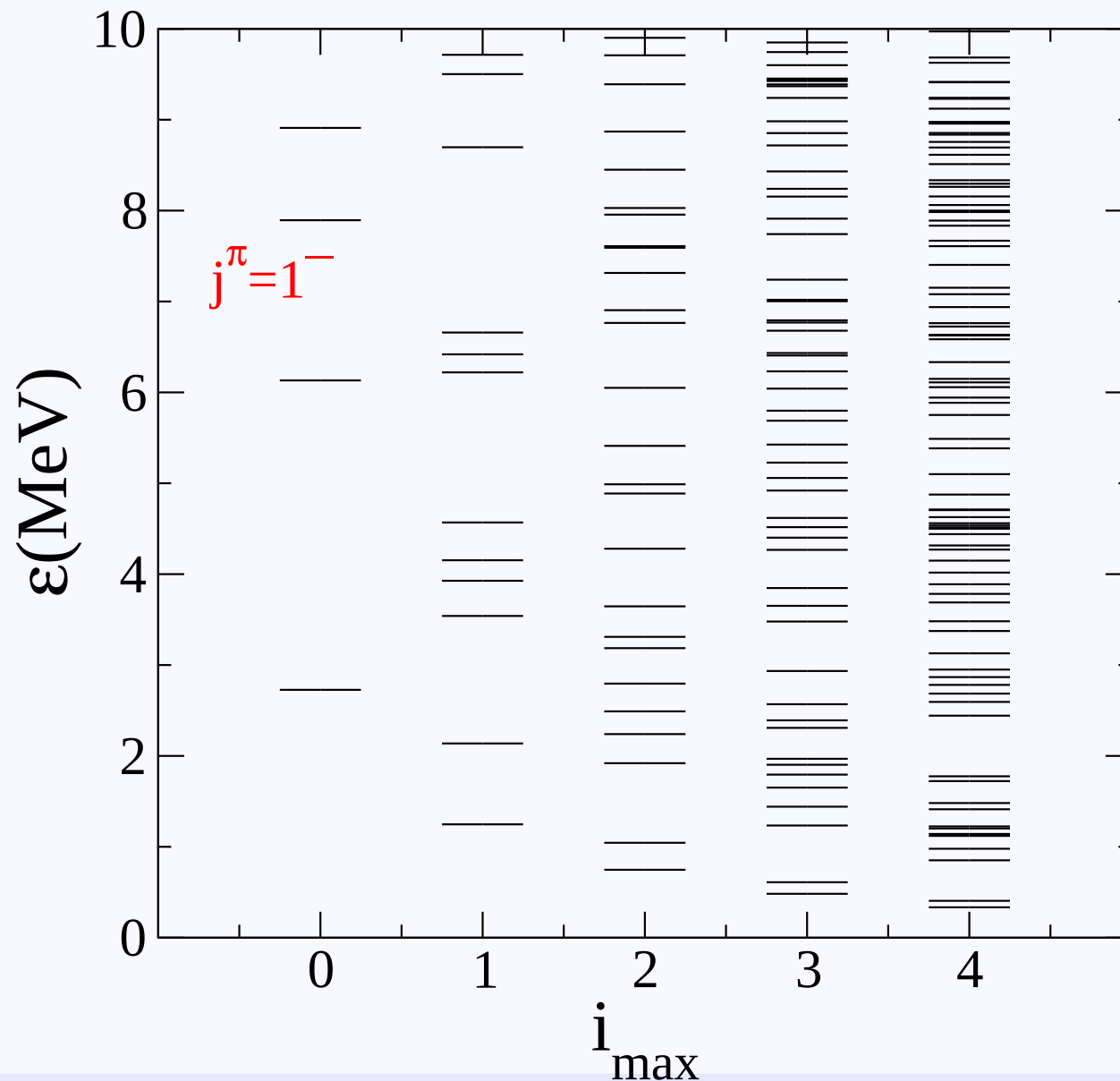
👉 Estados prohibidos de Pauli: V_c repulsivo en onda s

✉ Rodríguez-Gallardo et al. PRC 72 (2005) 024007

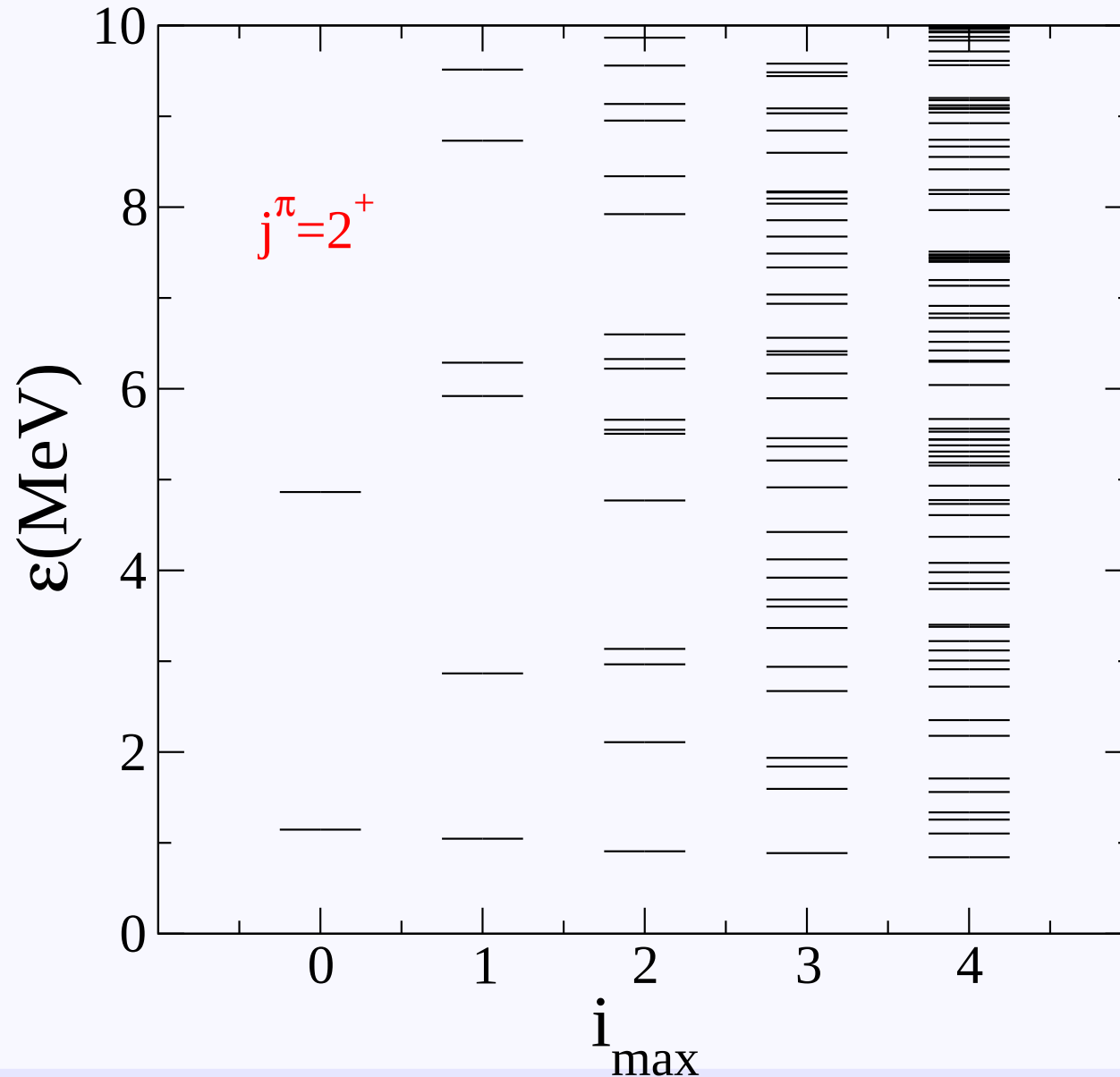
THO: espectros de energía



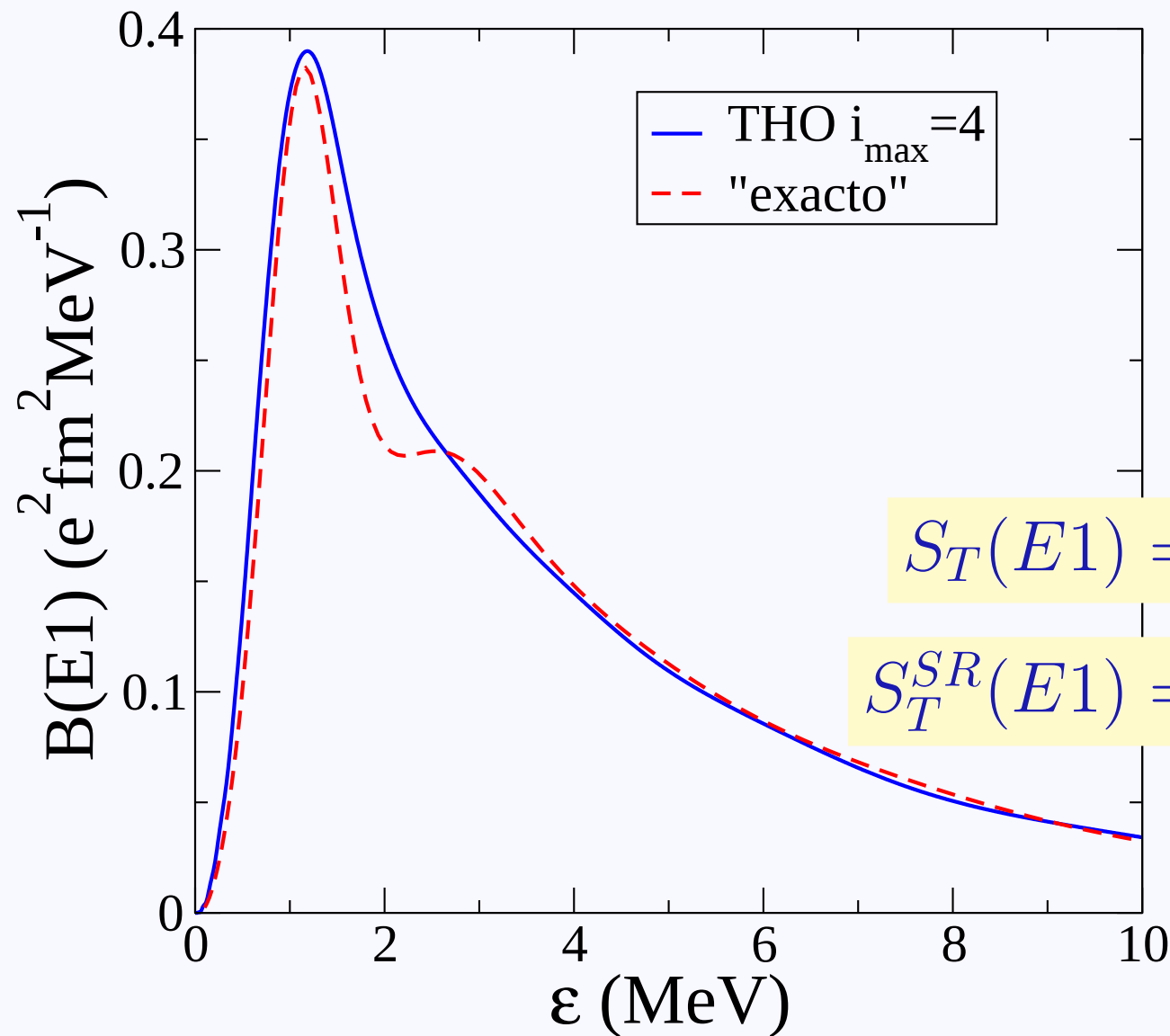
THO: espectros de energía



THO: espectros de energía



Distribución de $B(E1)$



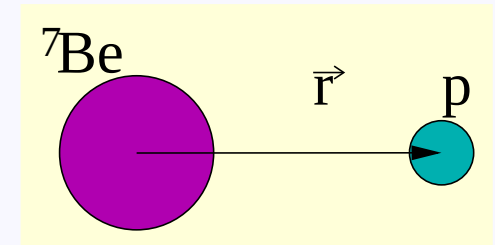
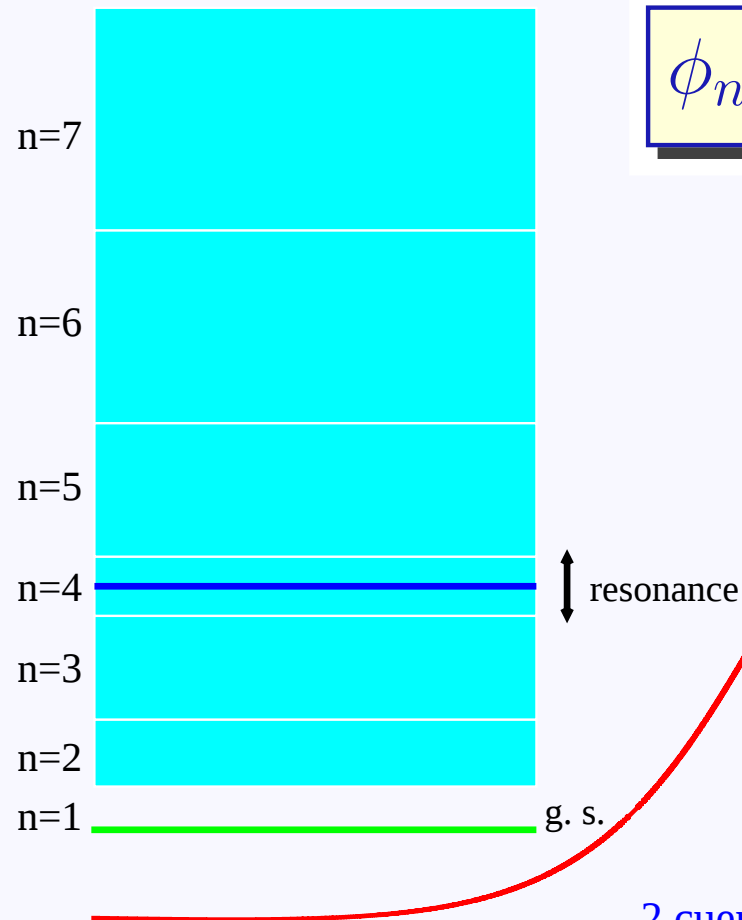
Otro método: *binning*

$\times \beta$

sistema de 2 cuerpos

$$\phi_{n\beta j\mu}(r, \theta, \varphi) = R_{n\beta j}^{bin}(r) \mathcal{Y}_{\beta j\mu}(\theta, \varphi)$$

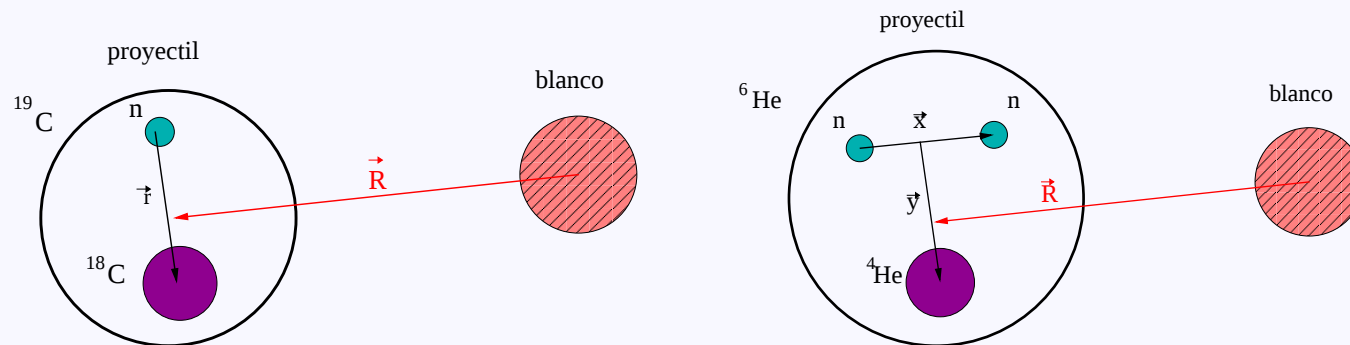
$$\beta \equiv \{l, s\}$$



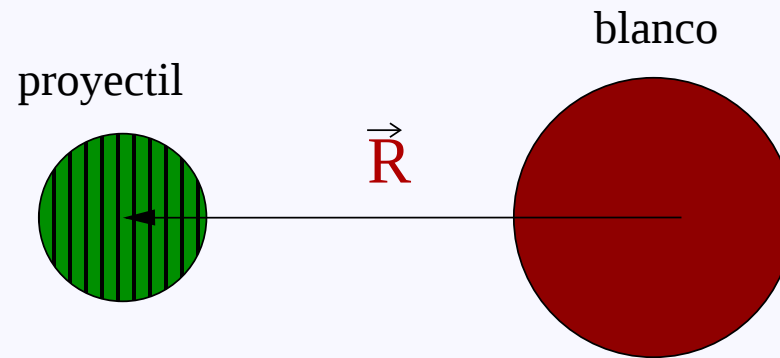
2 cuerpos: Yahiro et al. Prog. Theor. Phys. 89 (1986) 32

3 cuerpos: Rodríguez-Gallardo et al. PRC 80 (2009) 051601(R)

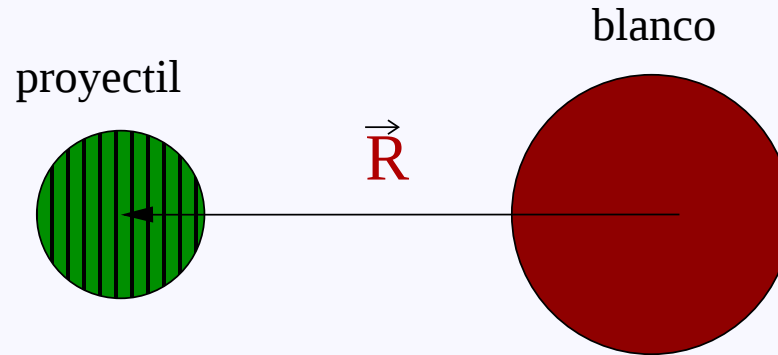
Reacciones nucleares de 3 y 4 cuerpos: formalismo CDCC



Formalismo CDCC

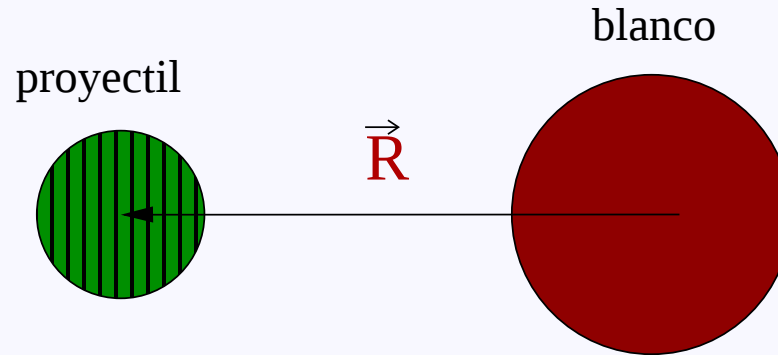


Formalismo CDCC



$$\Psi_J^M(\vec{R}, \xi) = \sum \phi_{jn}^\mu(\xi) \langle LM_L j\mu | JM \rangle \frac{i^L}{R} Y_L^{M_L}(\hat{R}) f_{Lnj}^J(R)$$

Formalismo CDCC

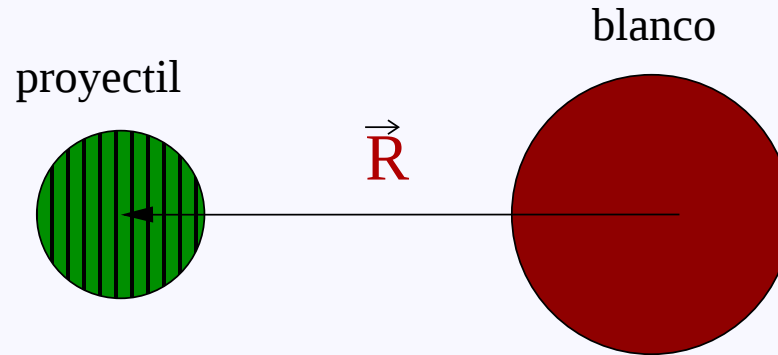


$$\Psi_J^M(\vec{R}, \xi) = \sum \phi_{jn}^\mu(\xi) \langle LM_L j \mu | JM \rangle \frac{i^L}{R} Y_L^{M_L}(\hat{R}) f_{Lnj}^J(R)$$

(sistema de canales acoplados)

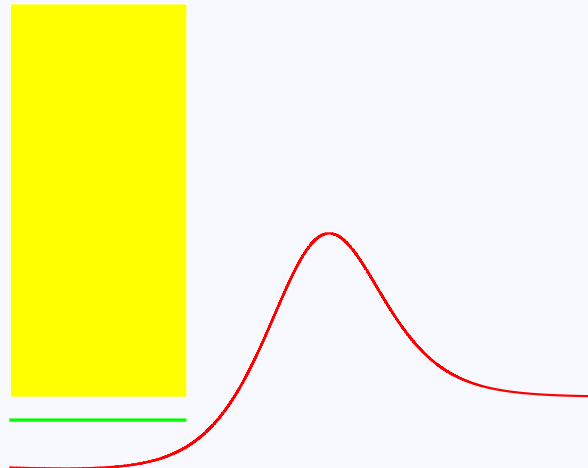
$$\left[-\frac{\hbar^2}{2m_r} \left(\frac{d^2}{dR^2} - \frac{L(L+1)}{R^2} \right) + \varepsilon_{nj} - E \right] f_{Lnj}^J(R) + \sum_{L'n'j'} i^{L'-L} V_{Lnj, L'n'j'}^J(R) f_{L'n'j'}^J(R) = 0$$

Formalismo CDCC

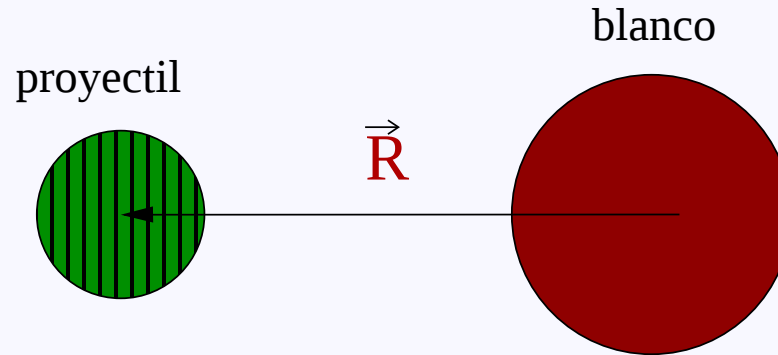


$$\Psi_J^M(\vec{R}, \xi) = \sum \phi_{jn}^{\mu}(\xi) \langle LM_L j\mu | JM \rangle \frac{i^L}{R} Y_L^{M_L}(\hat{R}) f_{Lnj}^J(R)$$

$\phi_n^{j\mu}(\xi)?$

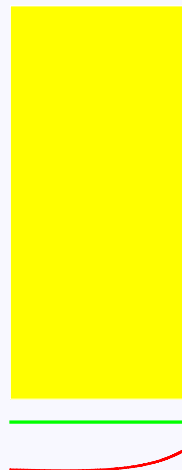


Formalismo CDCC

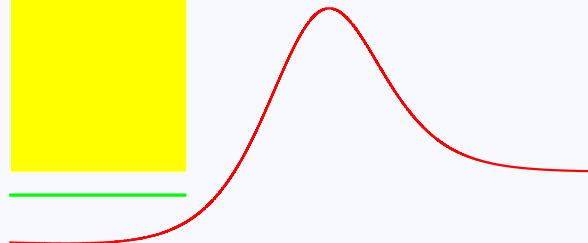


$$\Psi_J^M(\vec{R}, \xi) = \sum \phi_{jn}^{j\mu}(\xi) \langle LM_L j\mu | JM \rangle \frac{i^L}{R} Y_L^{M_L}(\hat{R}) f_{Lnj}^J(R)$$

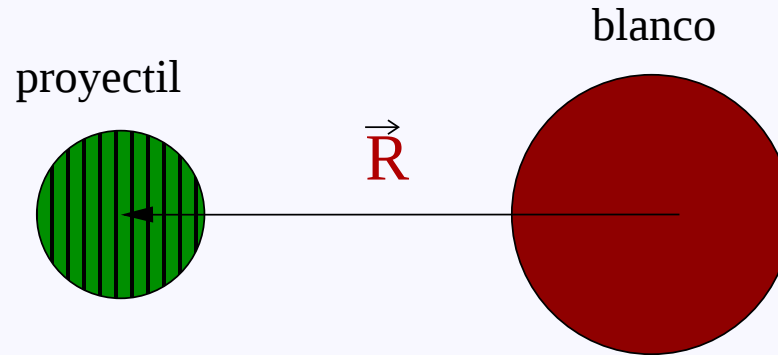
$\phi_n^{j\mu}(\xi)?$



① THO [MRG et al. PRC 77 (2008) 064609]

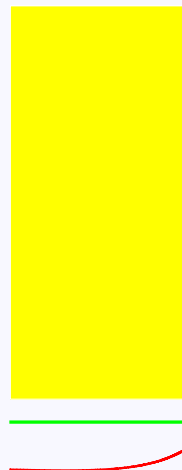


Formalismo CDCC

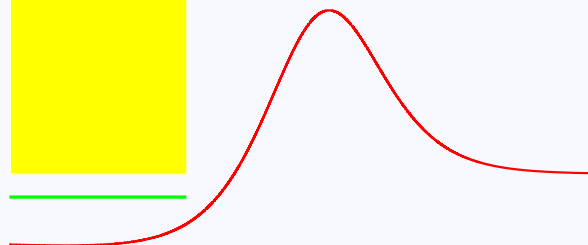


$$\Psi_J^M(\vec{R}, \xi) = \sum \phi_{jn}^{\mu}(\xi) \langle LM_L j \mu | JM \rangle \frac{i^L}{R} Y_L^{M_L}(\hat{R}) f_{Lnj}^J(R)$$

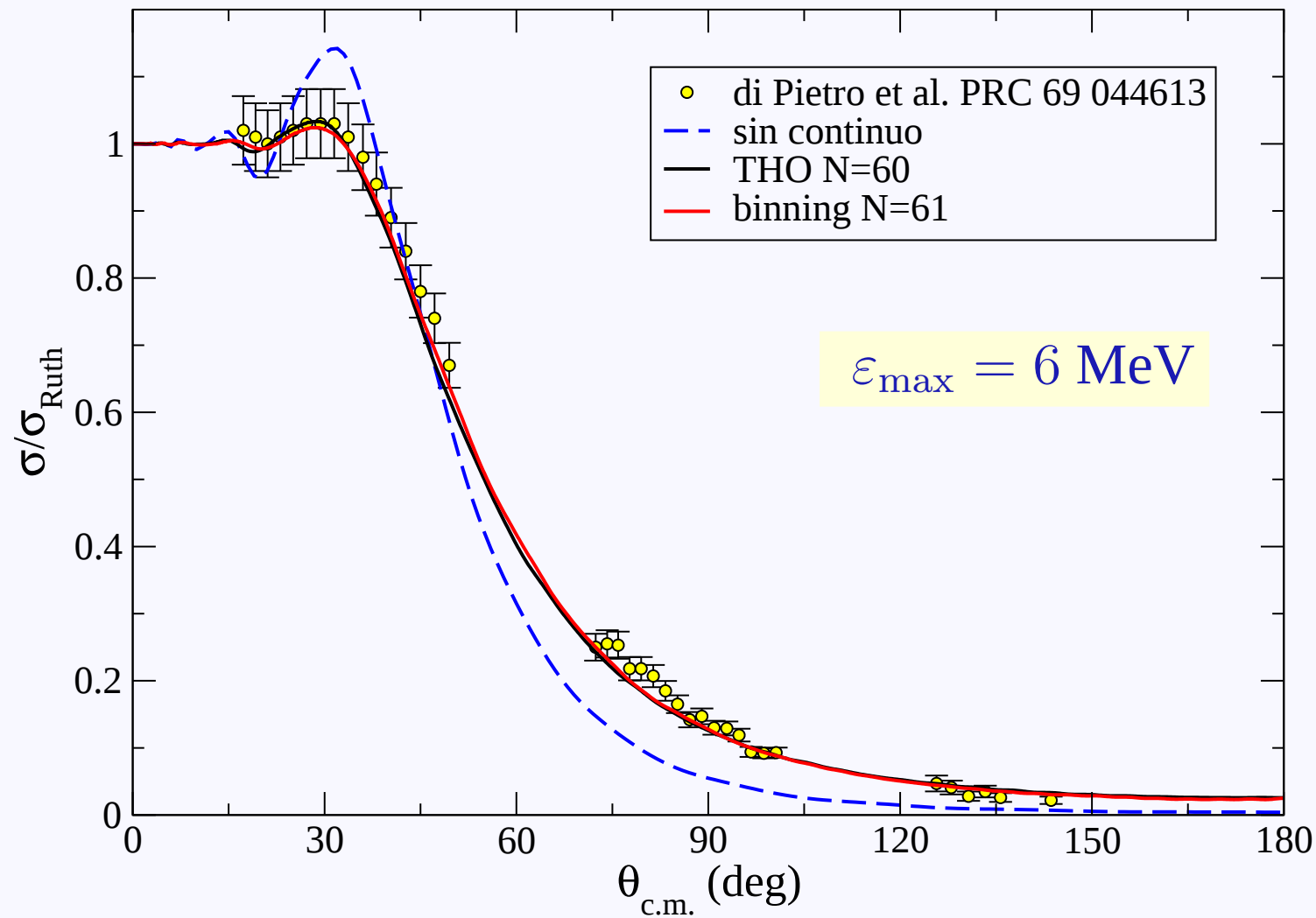
$\phi_n^{j\mu}(\xi)?$



- ① THO [MRG et al. PRC 77 (2008) 064609]
- ② binning [MRG et al. PRC 80 (2009) 051601(R)]



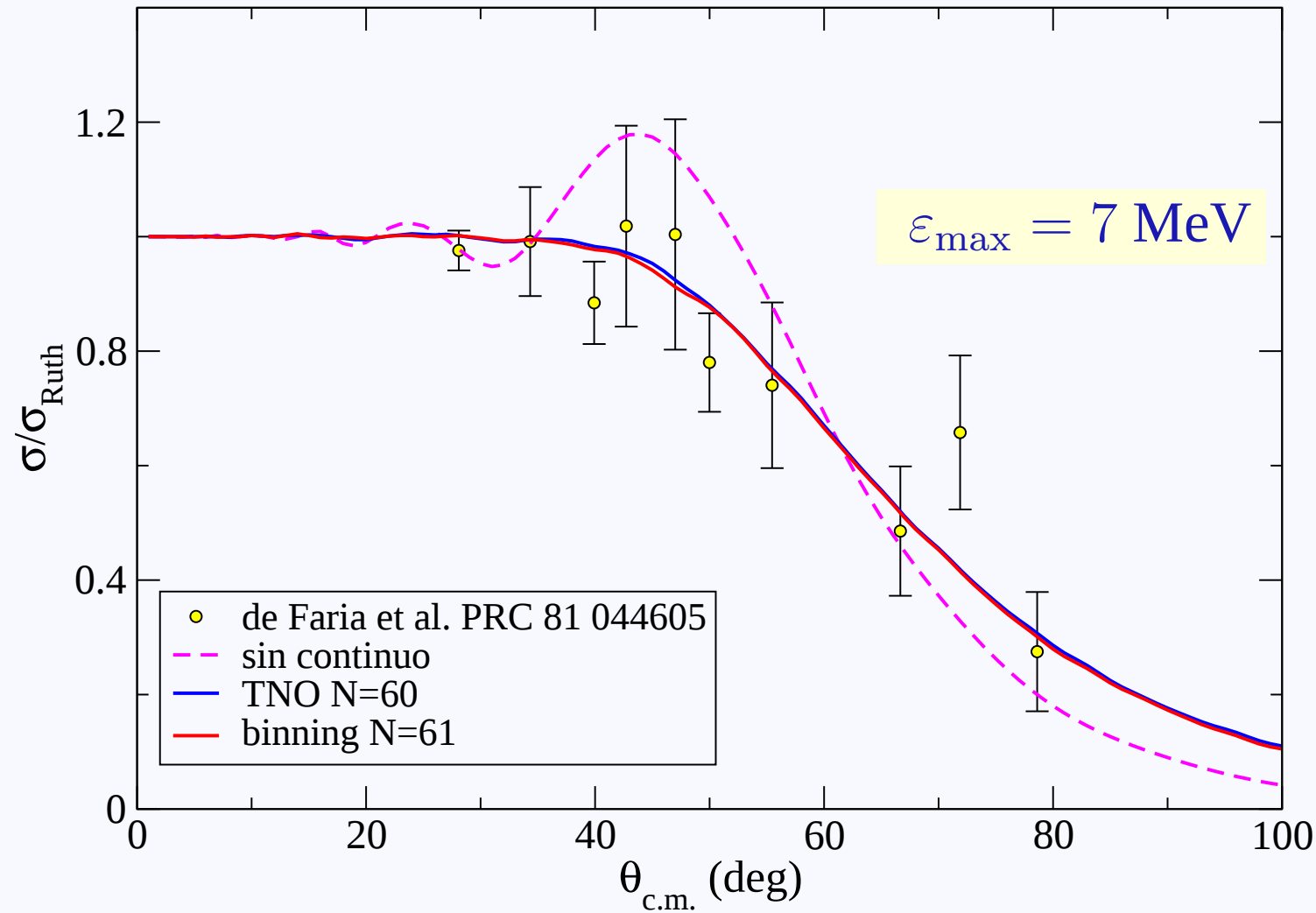
${}^6\text{He} + {}^{64}\text{Zn}$ @ 13.6 MeV: elástico



☒ THO: Rodríguez-Gallardo et al., PRC 77 (2008) 064609

☒ bin: Rodríguez-Gallardo et al., AIPCP 1231 (2010) 235-236

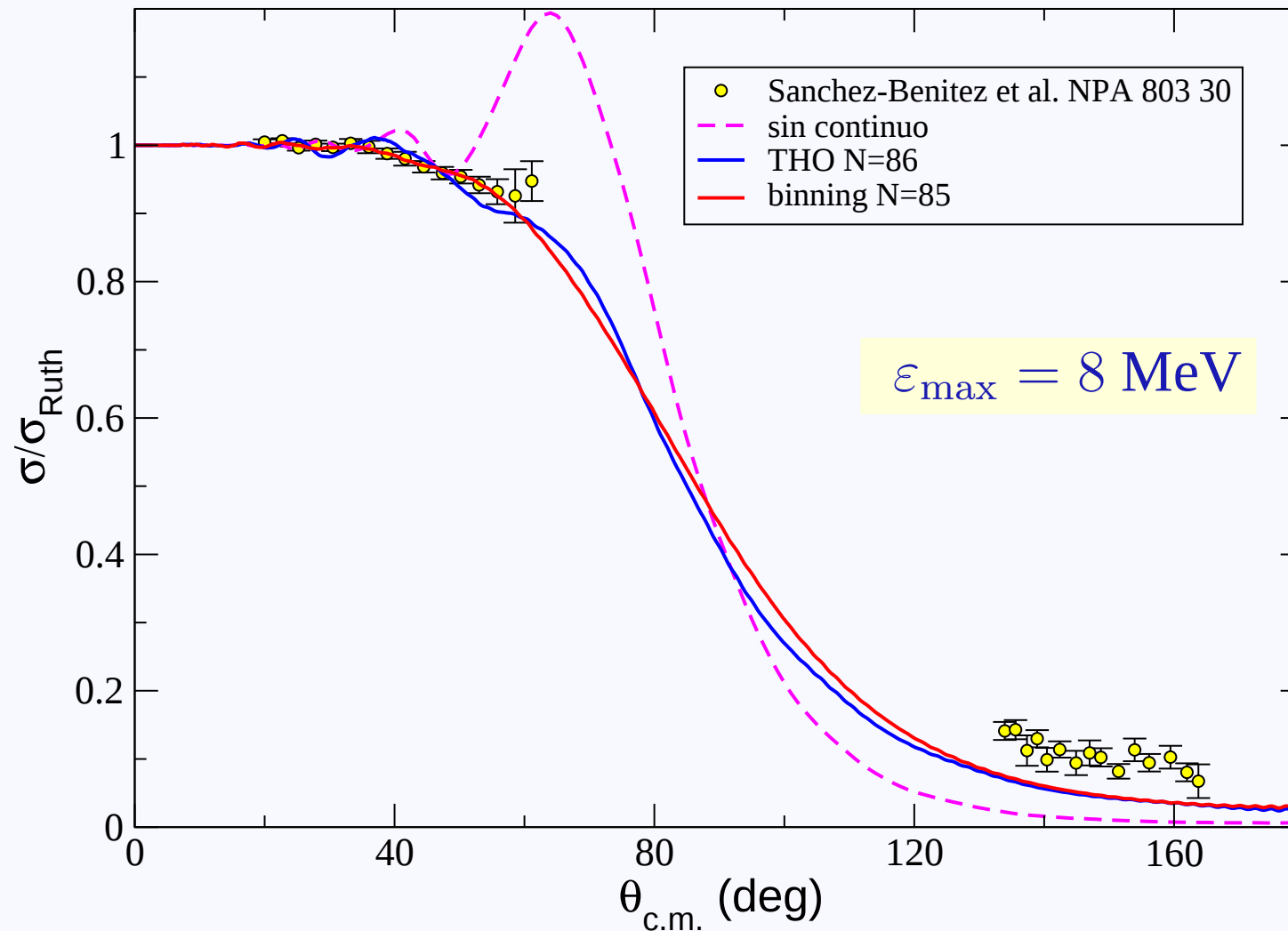
${}^6\text{He} + {}^{120}\text{Sn}$ @ 17.4 MeV: elástico



THO: de Faria et al. PRC 81 (2010) 044605

bin: Rodríguez-Gallardo and Moro. AIP Conf. Proc. 1351 (2011) 29-38

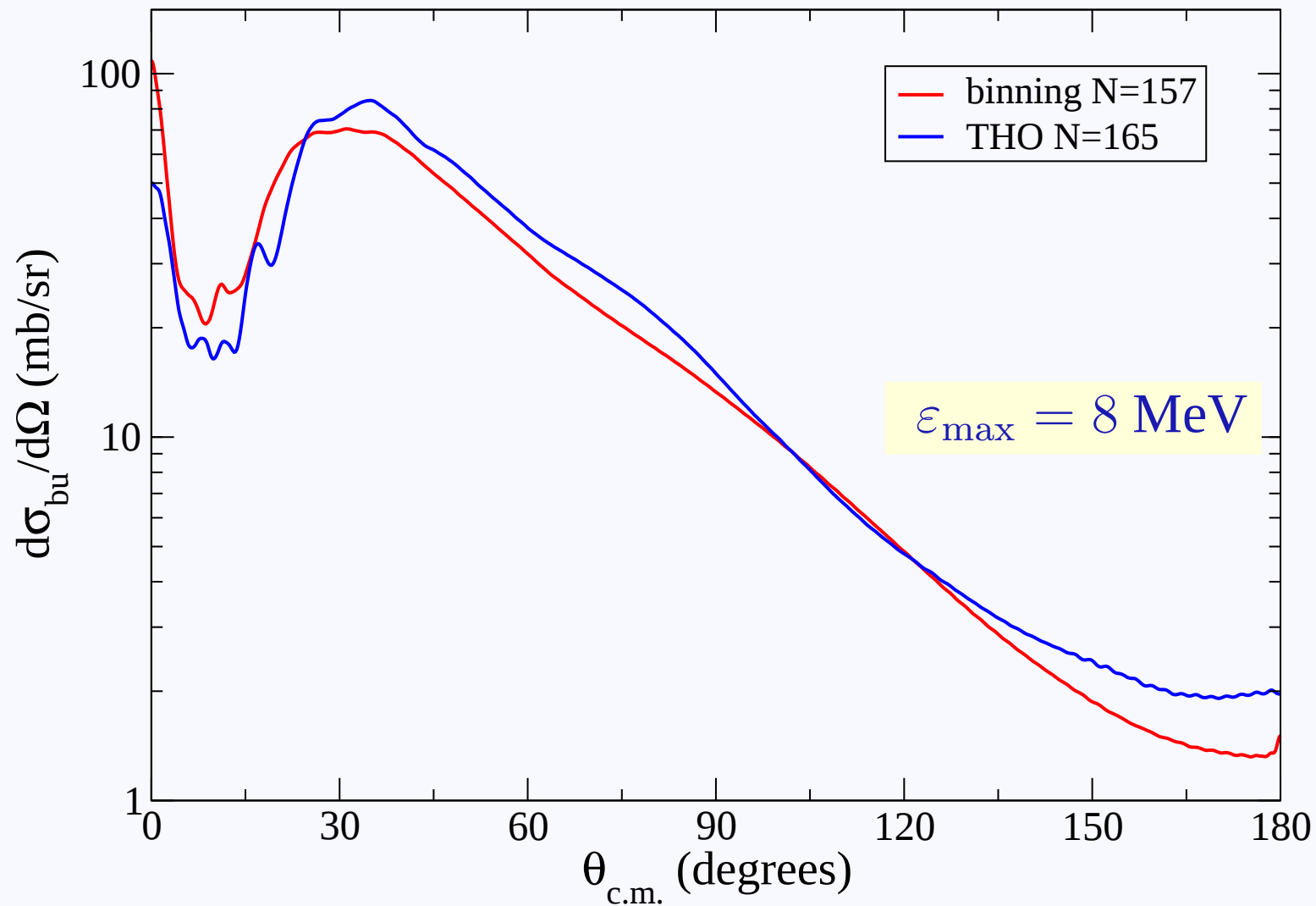
${}^6\text{He} + {}^{208}\text{Pb}$ @ 22 MeV: elástico



✠ THO: Rodríguez-Gallardo et al., PRC 77 064609 (2008)

✠ bin: Rodríguez-Gallardo et al. PRC 80 (2009) 051601(R)

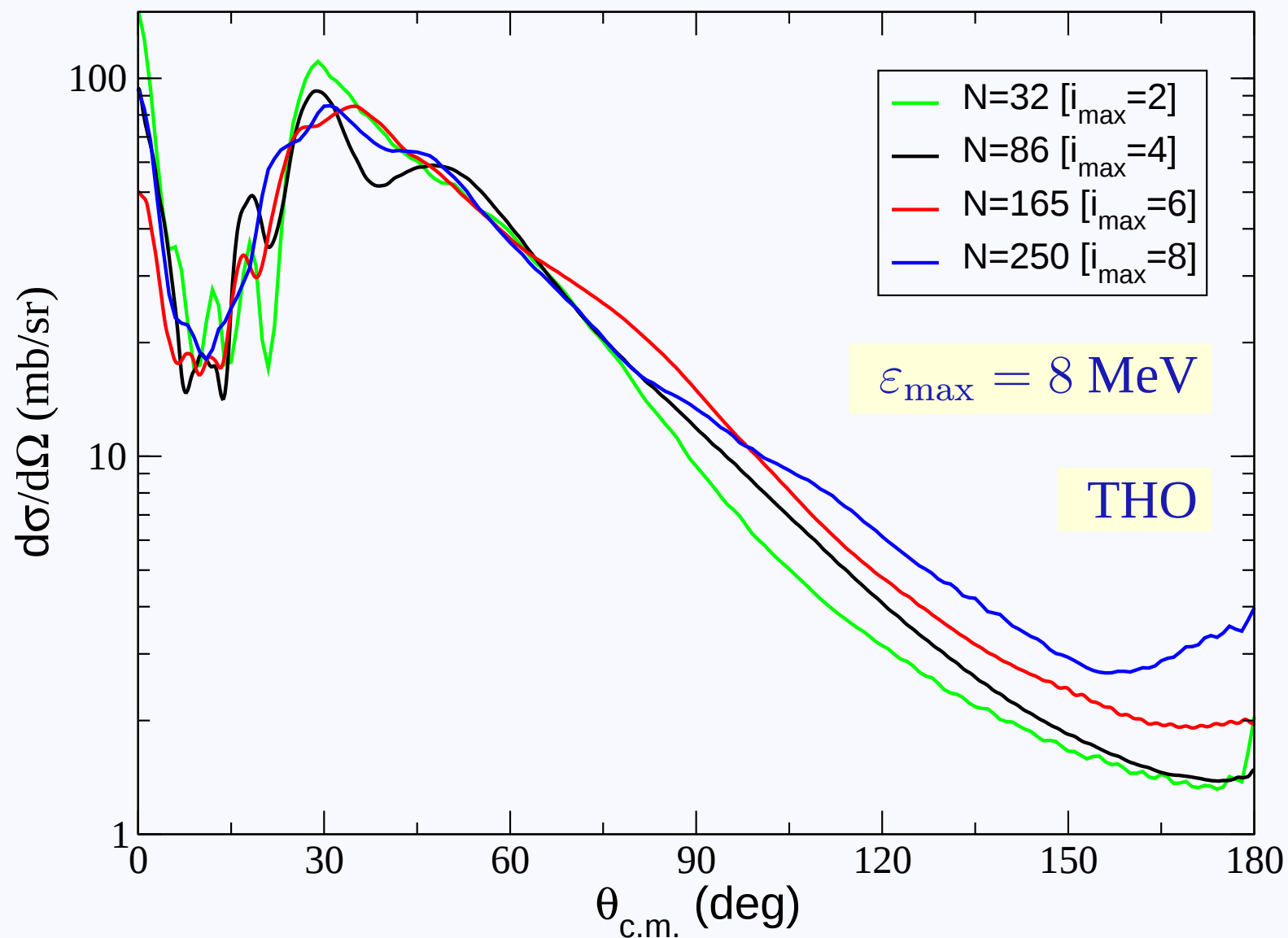
${}^6\text{He} + {}^{208}\text{Pb}$ @ 22 MeV: breakup



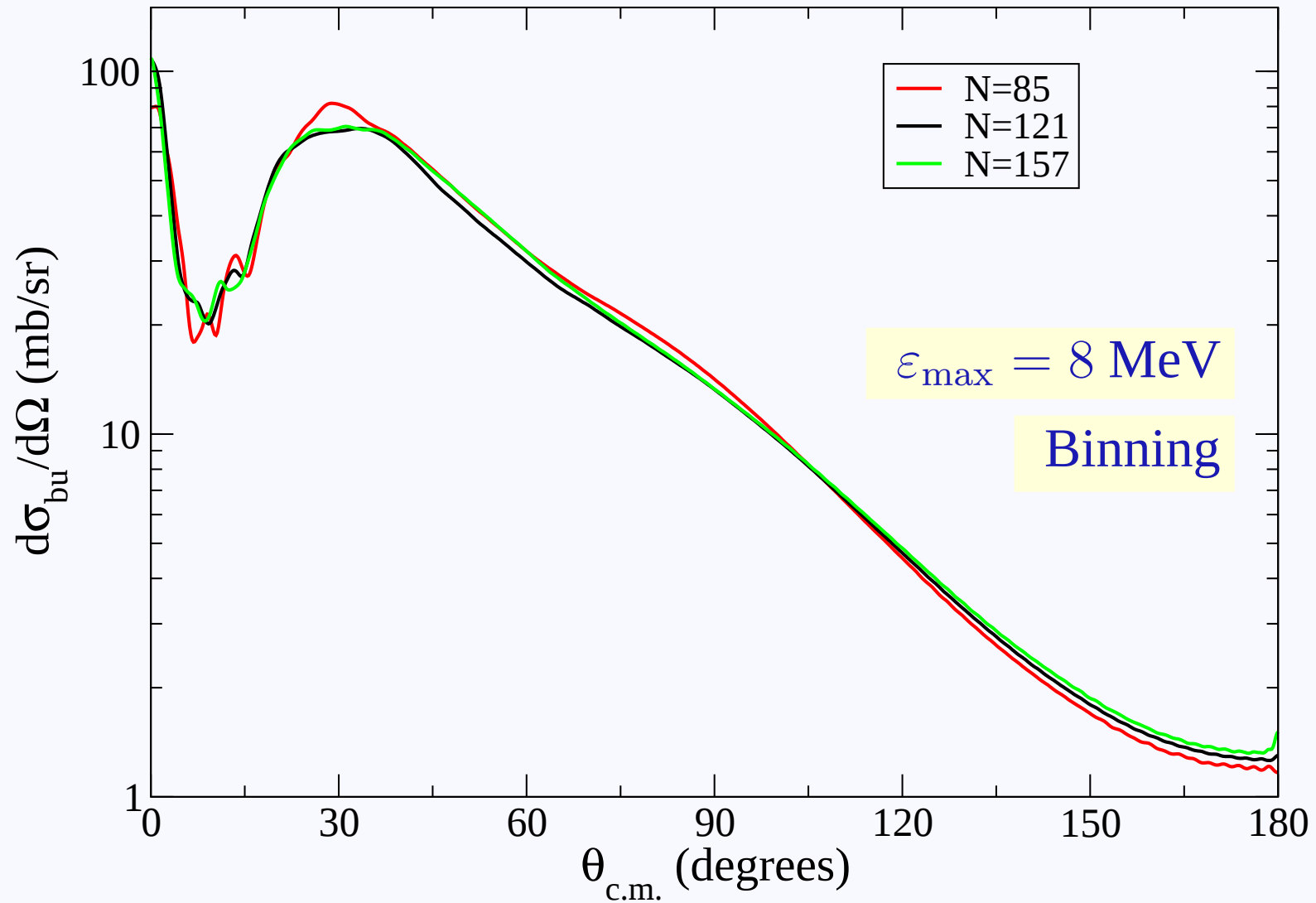
✠ bin: Rodríguez-Gallardo and Moro. AIP Conf. Proc. 1351 (2011) 29-38

✠ THO: sin publicar

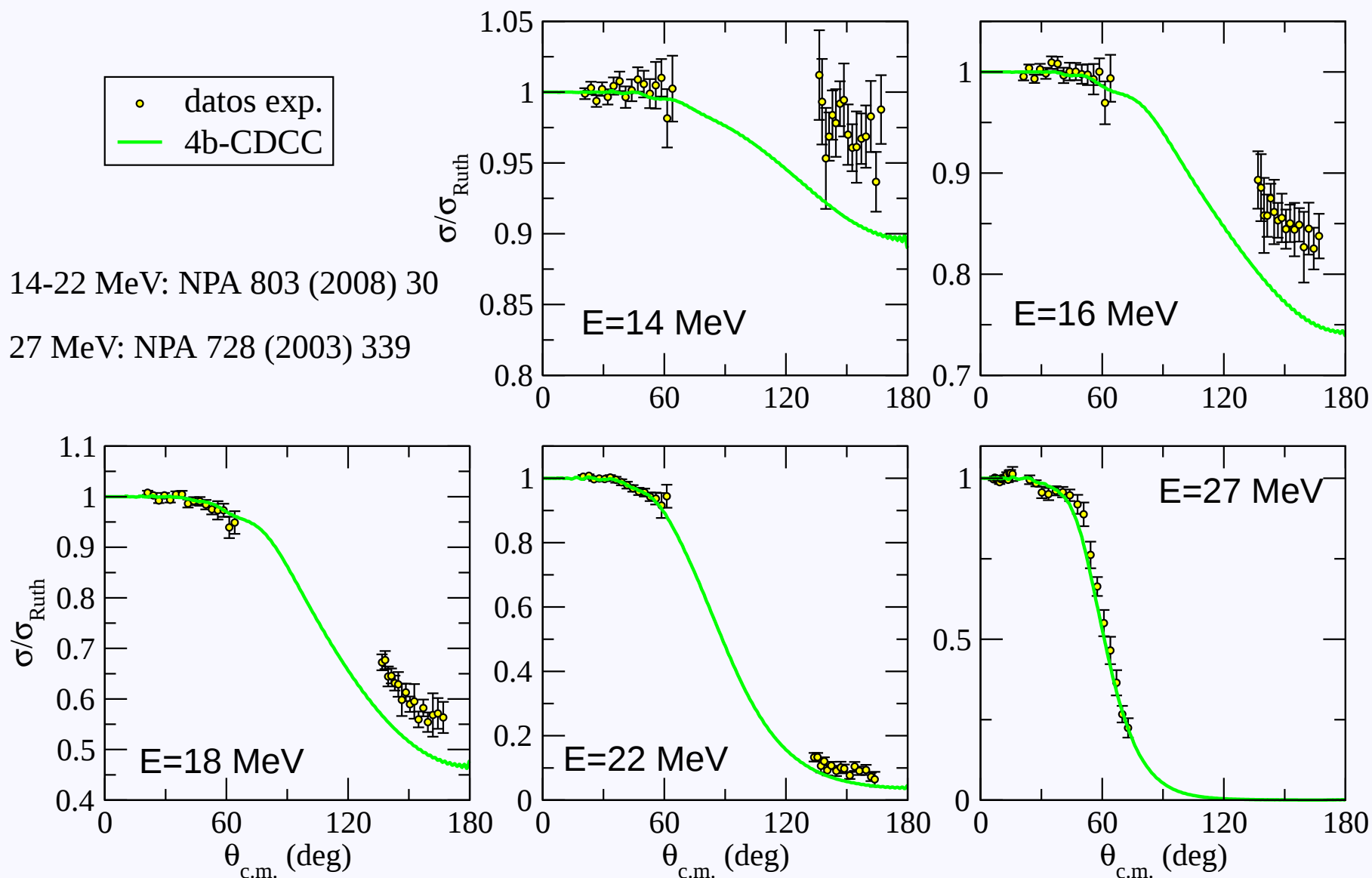
${}^6\text{He} + {}^{208}\text{Pb}$ @ 22 MeV: breakup



${}^6\text{He} + {}^{208}\text{Pb}$ @ 22 MeV: breakup



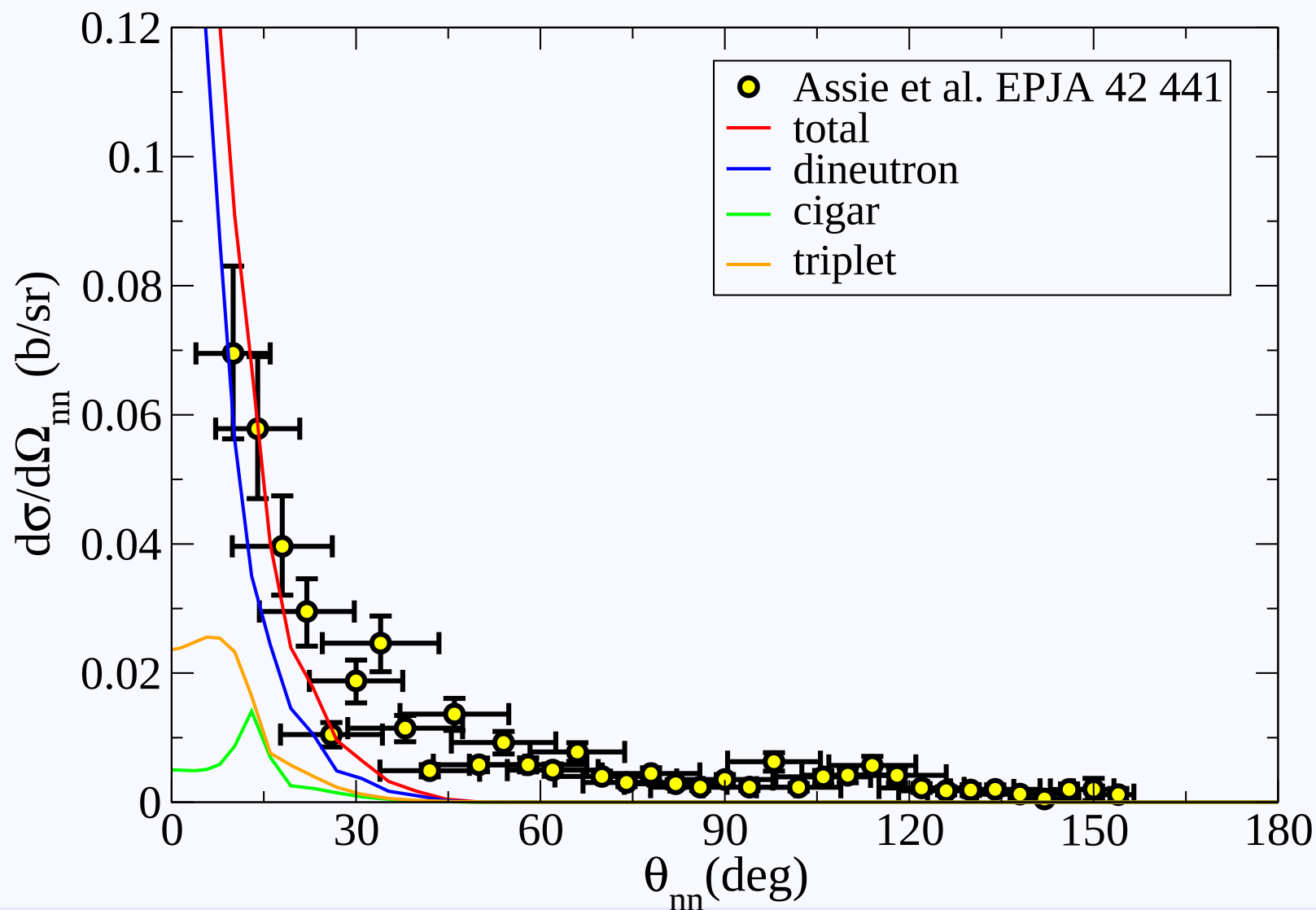
${}^6\text{He} + {}^{208}\text{Pb}$ @ 14, 16, 18, 22, 27 MeV



✉ Fernández-García et al. NPA 840 (2010) 19-38; PLB 693 (2010) 310-315

Observables de ruptura de 4 cuerpos

${}^6\text{He} + {}^{208}\text{Pb} @ 120\text{MeV}$

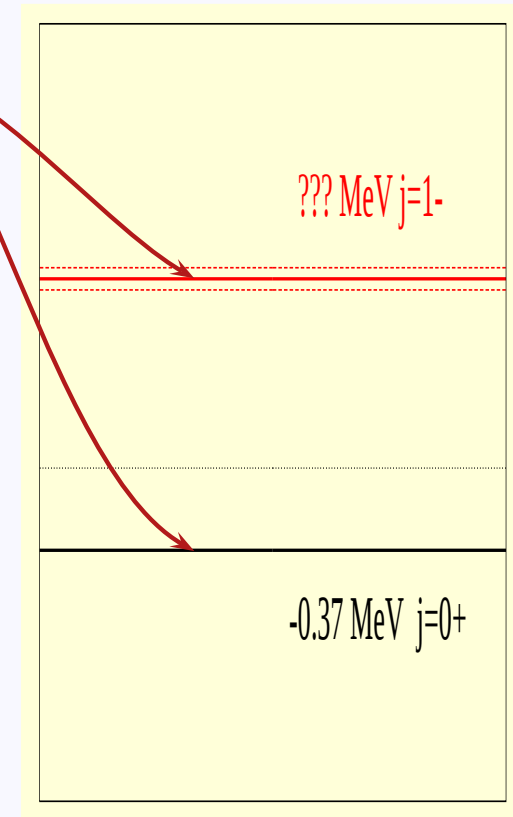


^{11}Li : ¿qué sabemos?

$$\hat{H}(\rho, \Omega) = \hat{T}(\rho, \Omega) + \hat{V}(\rho, \Omega)$$

$$V = V_{n\alpha} + V_{n\alpha} + V_{nn} + V_{nn\alpha}$$

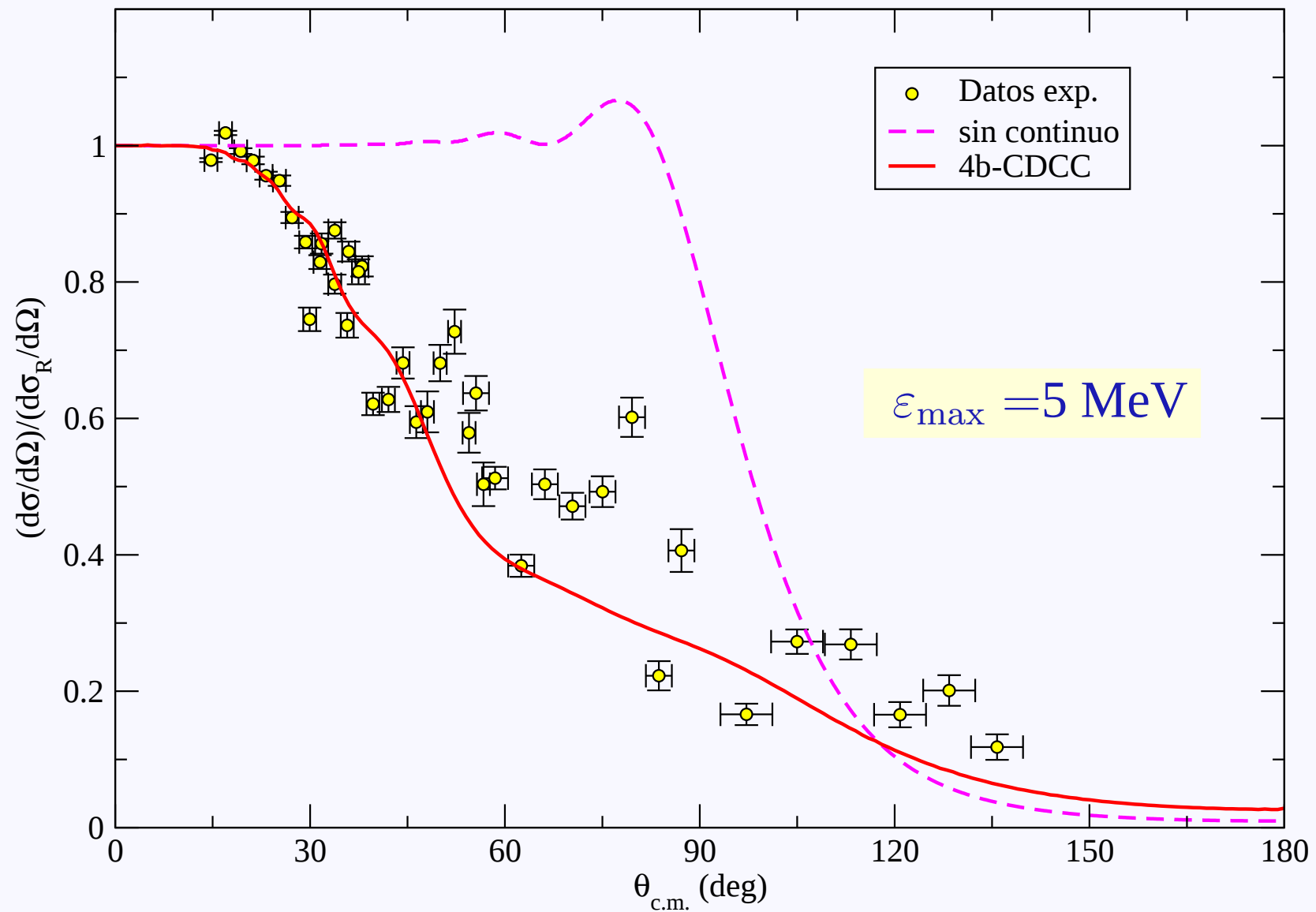
sin espín del core



✋ estados prohibidos de Pauli: método PA

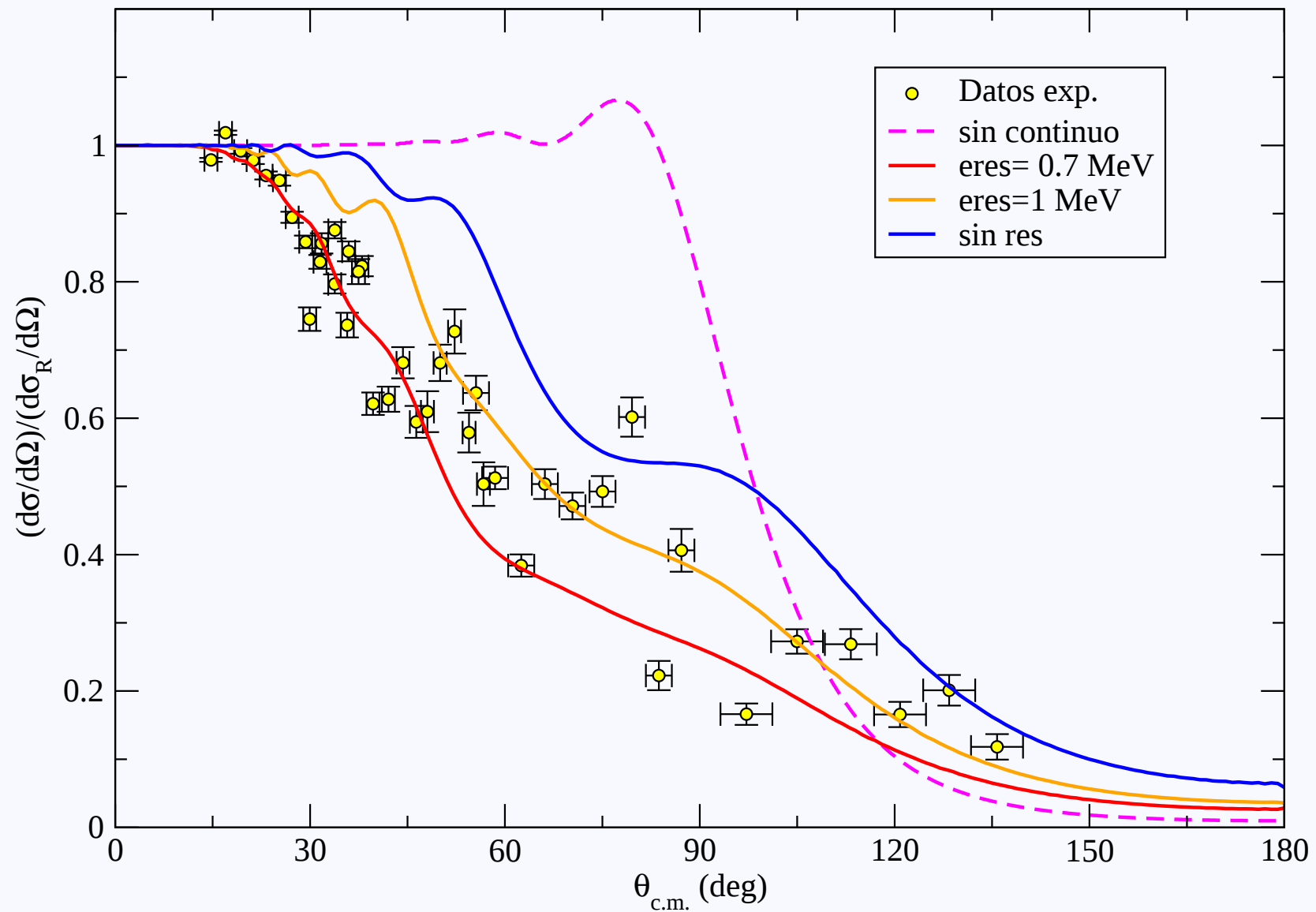
🚩 Cubero et al. PRL 2012; Fernández-García et al. enviado a PRL 2012

$^{11}\text{Li} + ^{208}\text{Pb} @ 29.8 \text{ MeV}$: elástico

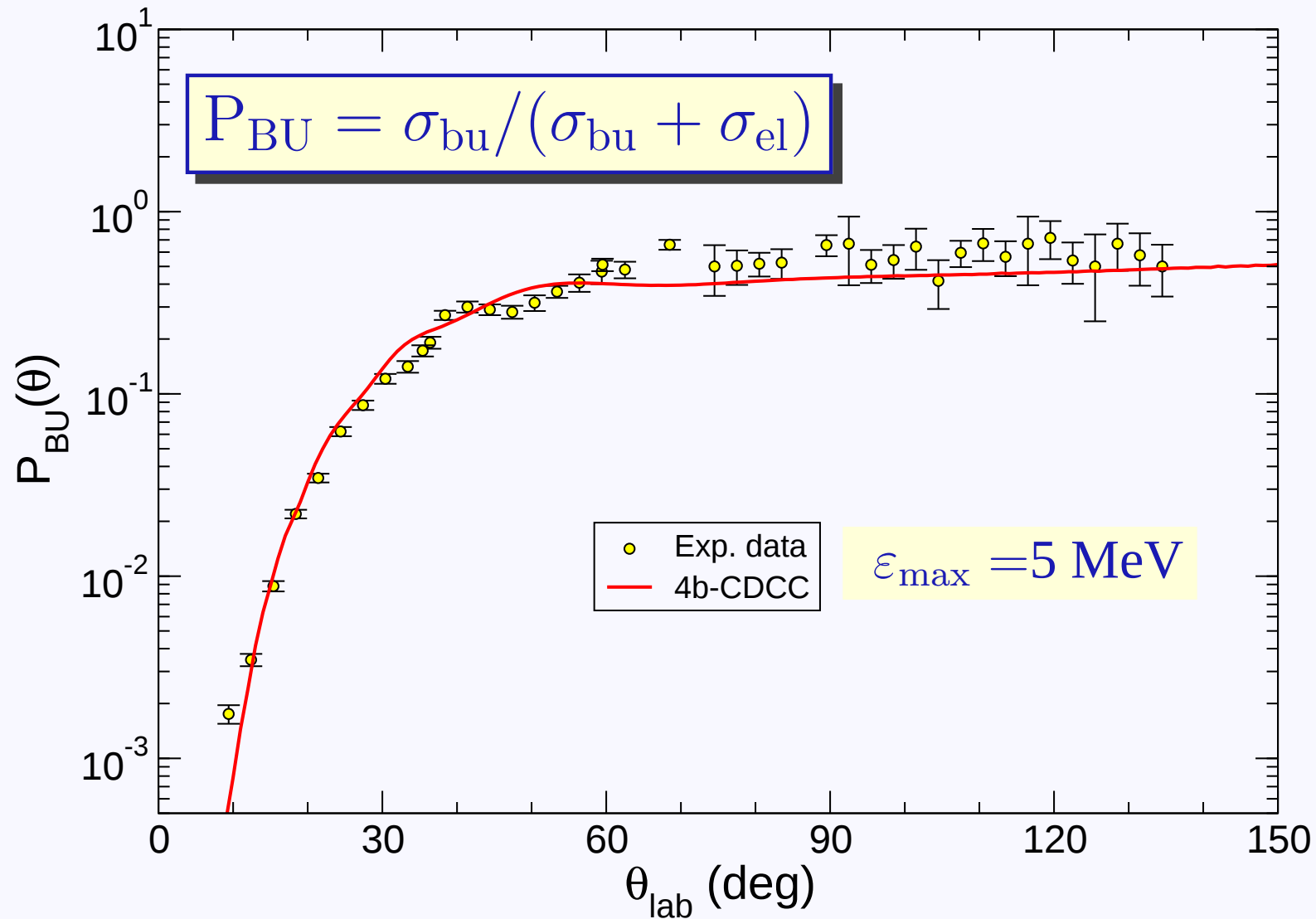


✠ Cubero et al., PRL 2012

$^{11}\text{Li} + ^{208}\text{Pb} @ 29.8 \text{ MeV}$: elástico

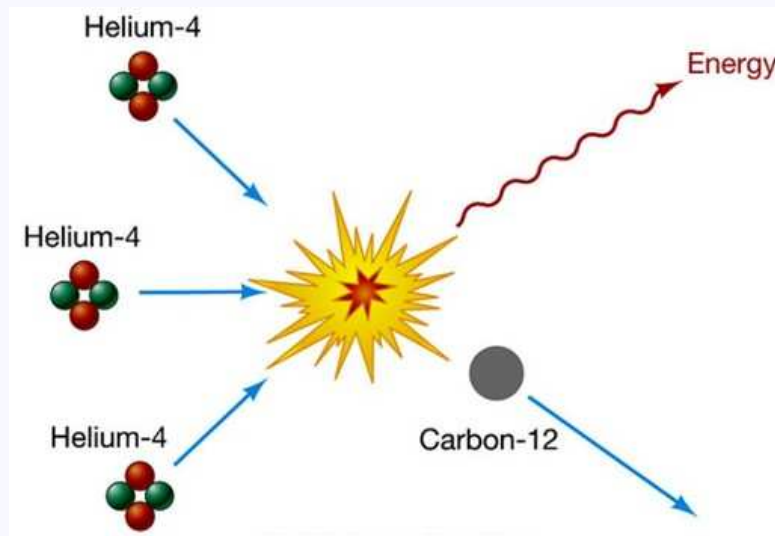


$^{11}\text{Li} + ^{208}\text{Pb} @ 29.8 \text{ MeV}$: prob. breakup



✉ Fernández-García et al., enviado a PRL 2012

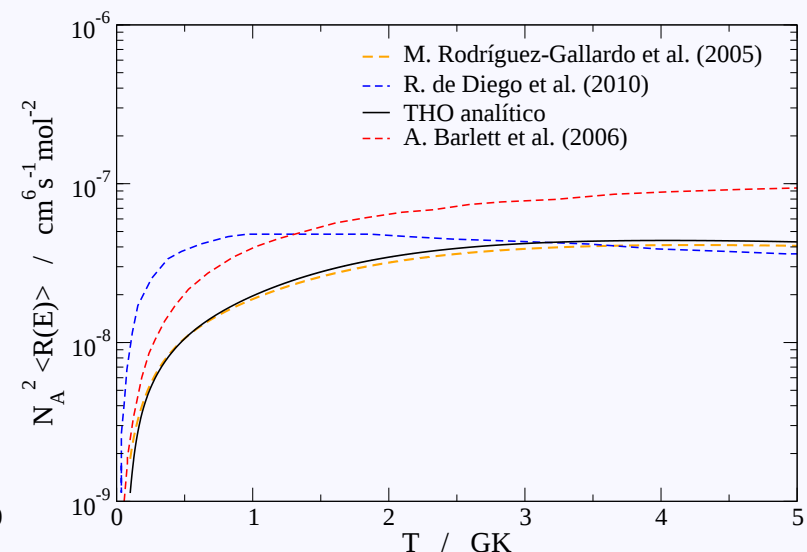
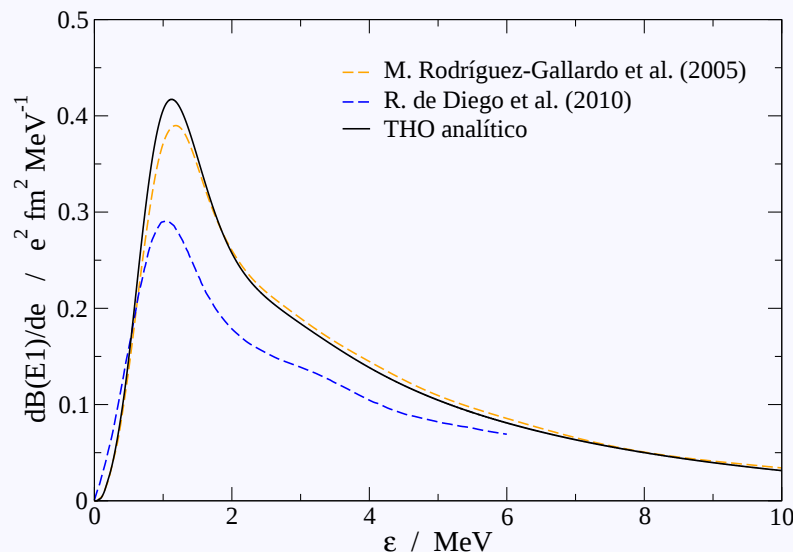
Reacciones nucleares de interés astrofísico:



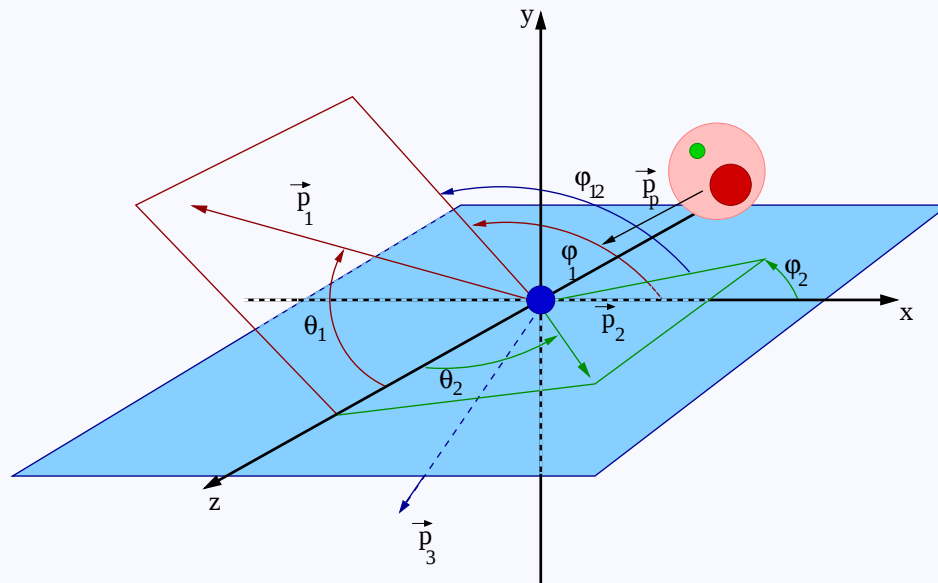
Reac. nucleares de interés astrofísico

✉ Trabajo Fin de Máster de Jesús Casal Berbel

- ⇒ Método THO analítico para calcular las propiedades de estructura
- ⇒ Cálculo de las **tasa de reacción** a partir de las transiciones eléctricas y magnéticas
- ⇒ Aplicación a ${}^6\text{He}(\alpha+n+n)$:



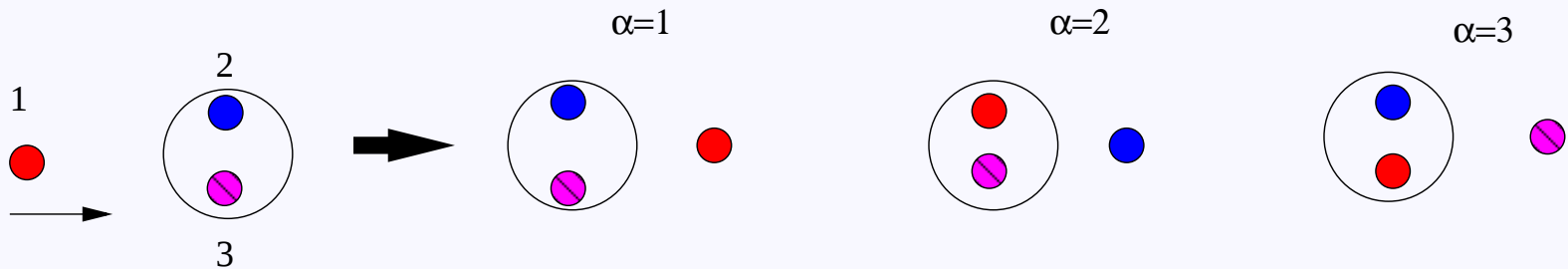
Reacciones nucleares de 3 cuerpos: ecuaciones de Faddeev



Ecuaciones de Faddeev/AGS

$$U^{\beta\alpha} = \bar{\delta}_{\beta\alpha} G_0^{-1} + \sum_{\gamma} U^{\beta\gamma} G_0 t_{\gamma} \bar{\delta}_{\gamma\alpha}$$

⇒ Trata las 3 partículas de igual manera



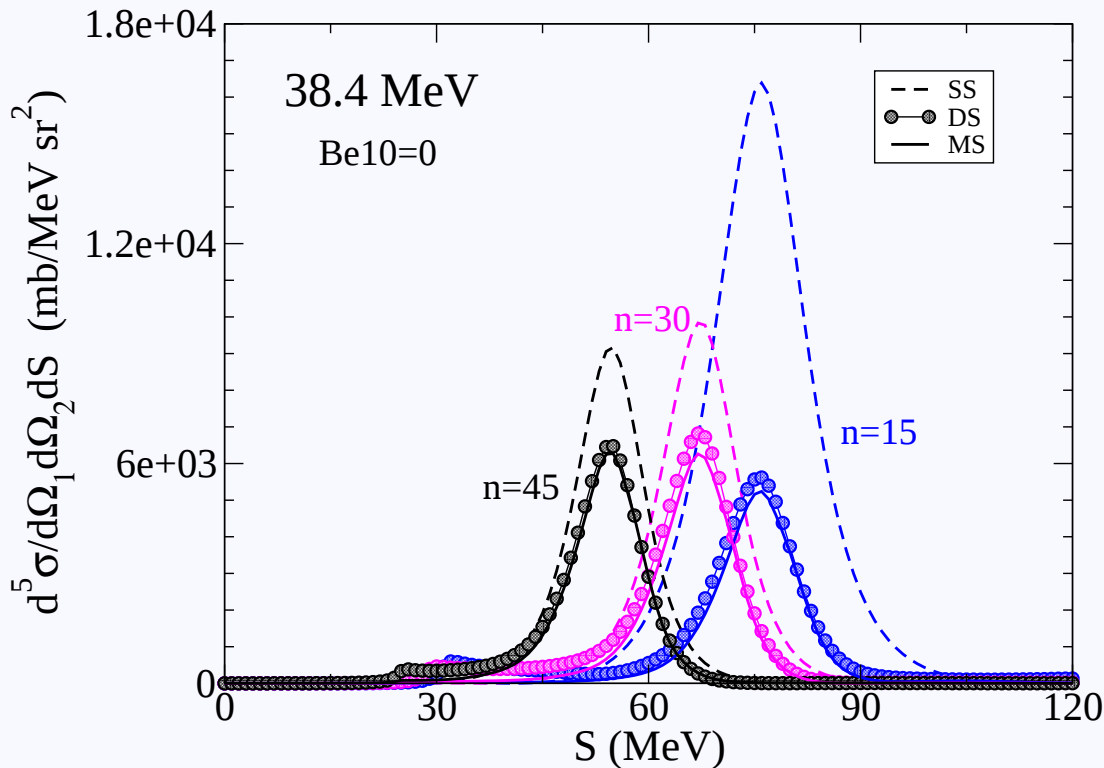
⇒ Resolución en el espacio de momentos:

⇒ Se elimina el problema del continuo

⇒ Surge el problema de Coulomb -> solución:
potencial apantallado suavizado

$$V(r) = V_R(r) e^{-(r/R)^n}$$

Algunas aplicaciones: $p+^{11}\text{Be}$



✉ Crespo et al.,

PRC 77 (2008) 024601

$$S = \int \sqrt{dE_1^2 + dE_2^2}$$

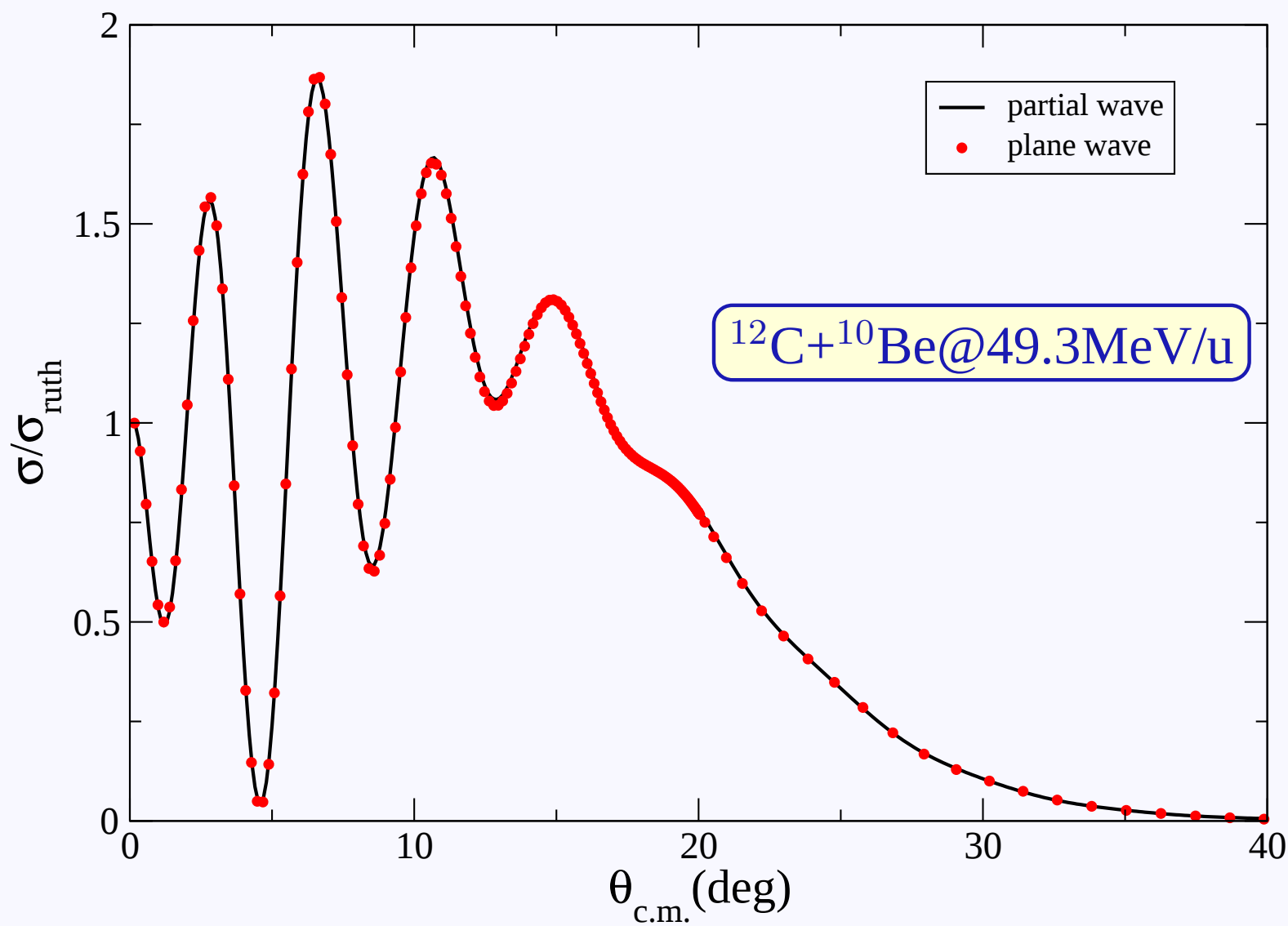
partícula 1: ^{10}Be

partícula 2: n

Otras aplicaciones:

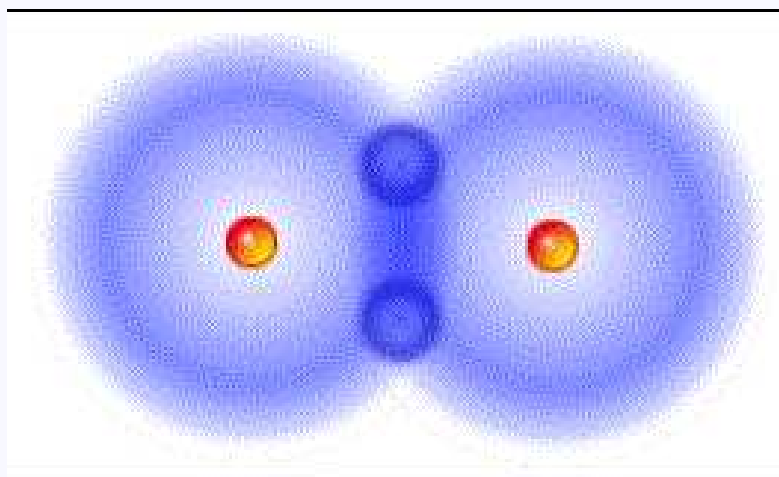
- ⇒ Crespo et al., PRC 76 (2007) 014620: $p+^{11}\text{Be}$ a 100, 150 y 200 MeV (test de la aproximación de Glauber)
- ⇒ Crespo et al., PRC 79 (2009) 014609: $p+^{14}\text{Be}$ a 69 MeV (1n-knockout)
- ⇒ Crespo et al., EPJA 42 (2009) 609-611: $p+^{11}\text{Be}$ a 38.4 y 200 MeV (comparación con PWIA)
- ⇒ Crespo et al., PRC 83 (2011) 054613: $p+^{19}\text{C}$ a 70 MeV (comparación con 3b-CDCC)

Onda plana vs onda parcial

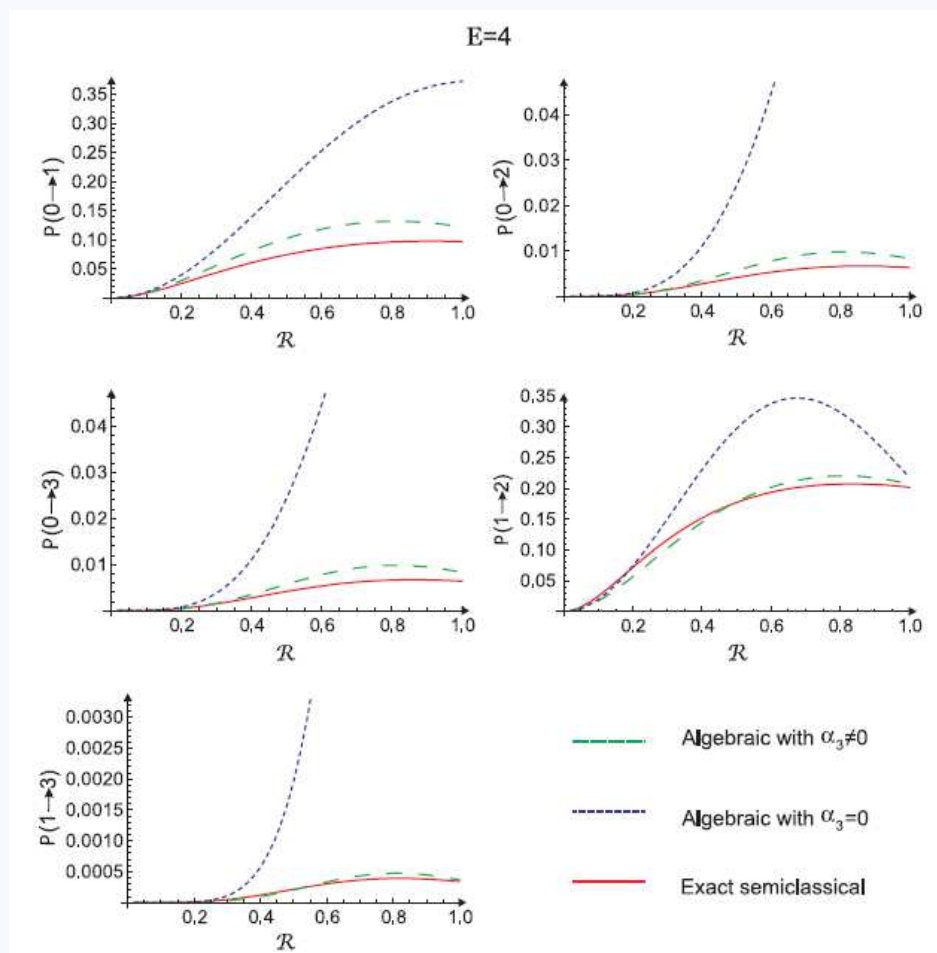
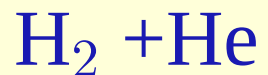


✉ Rodríguez-Gallardo et al, PRC 78 (2008) 034602; EPJA 42 (2009) 609-611

Reacciones moleculares



Reacciones moleculares



- ➡ H_2 : pot. Morse
- ➡ $E = 4\hbar\omega$
(unidades características)
- ➡ $P(i \rightarrow j)$:
probabilidad de pasar del estado i al j
- ➡ R : parámetro que controla la intensidad de la interacción

✉ Álvarez-Bajo et al, JPB 40 (2007) 4513-4527

Nuevas líneas a investigar

- ⇒ Cálculos de transferencia y knockout
- ⇒ Cálculos preliminares para grandes instalaciones
- ⇒ Aplicación a Física Atómica de los modelos desarrollados



- ⇒ Reacciones nucleares de interés astrofísico:
 ${}^9\text{Be}(\alpha+\alpha+n)$, ${}^{17}\text{Ne}({}^{15}\text{O}+p+p)$, ${}^{12}\text{C}(\alpha+\alpha+\alpha)$
- ⇒ 4b-CDCC para reacciones ${}^{17}\text{Ne}+\text{target}$ (GSI)
- ⇒ Códigos para observables de ruptura de 4 cuerpos
- ⇒ Completar el programa de Faddeev en onda plana