



# Higgs Physics at Future $e^+e^-$ Colliders

*Sven Heinemeyer, IFT/IFCA (CSIC, Madrid/Santander)*

zoom only, 10/2020

- Motivation
- Higgs precision measurements and BSM Physics scales
- The Higgs selfcoupling(s) at  $e^+e^-$  colliders
- BSM Higgs bosons below 125 GeV
- Conclusions

# Higgs Physics at Future $e^+e^-$ Colliders in Spain

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# 1. Motivation

## Two Facts:

We have an SM-like Higgs discovery!

The SM cannot be the ultimate theory!

**Conclusion: It cannot be “the SM Higgs”!**

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**Q:** Does the BSM physics have any (relevant) impact on the Higgs?

**Q':** Which model?

# 1. Motivation

## Two Facts:

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The SM cannot be the ultimate theory!

**Conclusion: It cannot be “the SM Higgs”!**

**Q:** Does the BSM physics have any (relevant) impact on the Higgs?

**Q':** Which model?

**A1:** check changed properties

**A2:** check for additional Higgs bosons

**A2':** check for additional Higgs bosons above and below 125 GeV

## Higgs physics at future $e^+e^-$ colliders:

- Measure precisely the  $h_{125}$  couplings to SM particles
  - consistency test of the SM
  - deviations from the SM
  - establish/measure new physics scales
- Measure precisely the Higgs selfcoupling(s)
  - deviations from the SM
  - performance if  $\lambda_{hhh} \neq \lambda_{hhh}^{\text{SM}}$ ?
  - effects of additional Higgs bosons, enhanced triple Higgs couplings?
- Discovery of light BSM Higgs bosons
  - indirect discovery potential
  - direct discovery potential
  - precision measurements of BSM Higgs bosons

⇒ one example for each (currently investigated in Spain)

## 2. Higgs precision measurements and BSM Physics scales

### What to expect from future colliders

⇒ focus on Higgs searches and measurements

#### HL-LHC:

- will improve direct search limits
- will improve rate measurements (production  $\times$  decay)  
systematic/theory uncertainties: S2 scenario

[*M. Cepeda et al. '19 – YR18*]

#### ILC:

- will improve rate measurements (no theory assumptions!)
  - $250 \text{ fb}^{-1}$  at ILC250  $\oplus$   $500 \text{ fb}^{-1}$  at ILC500
  - polarization:  $P(e^-, e^+) = (-80\%, +30\%)$

[*T. Barklow et al. '17, '19*]

(roughly similar results at FCC-ee, CEPC, CLIC)

## The MSSM Higgs sector:

Enlarged Higgs sector: Two Higgs doublets

$$H_1 = \begin{pmatrix} H_1^1 \\ H_1^2 \end{pmatrix} = \begin{pmatrix} v_1 + (\phi_1 + i\chi_1)/\sqrt{2} \\ \phi_1^- \end{pmatrix}$$
$$H_2 = \begin{pmatrix} H_2^1 \\ H_2^2 \end{pmatrix} = \begin{pmatrix} \phi_2^+ \\ v_2 + (\phi_2 + i\chi_2)/\sqrt{2} \end{pmatrix}$$

$$V = m_1^2 H_1 \bar{H}_1 + m_2^2 H_2 \bar{H}_2 - m_{12}^2 (\epsilon_{ab} H_1^a H_2^b + \text{h.c.})$$
$$+ \underbrace{\frac{g'^2 + g^2}{8}}_{\text{gauge couplings, in contrast to SM}} (H_1 \bar{H}_1 - H_2 \bar{H}_2)^2 + \underbrace{\frac{g^2}{2}}_{\text{SM}} |H_1 \bar{H}_2|^2$$

physical states:  $h^0, H^0, A^0, H^\pm$       Goldstone bosons:  $G^0, G^\pm$

Input parameters: (to be determined experimentally)

$$\tan \beta = \frac{v_2}{v_1}, \quad M_A^2 = -m_{12}^2 (\tan \beta + \cot \beta)$$

## Search for the MSSM Higgs bosons:

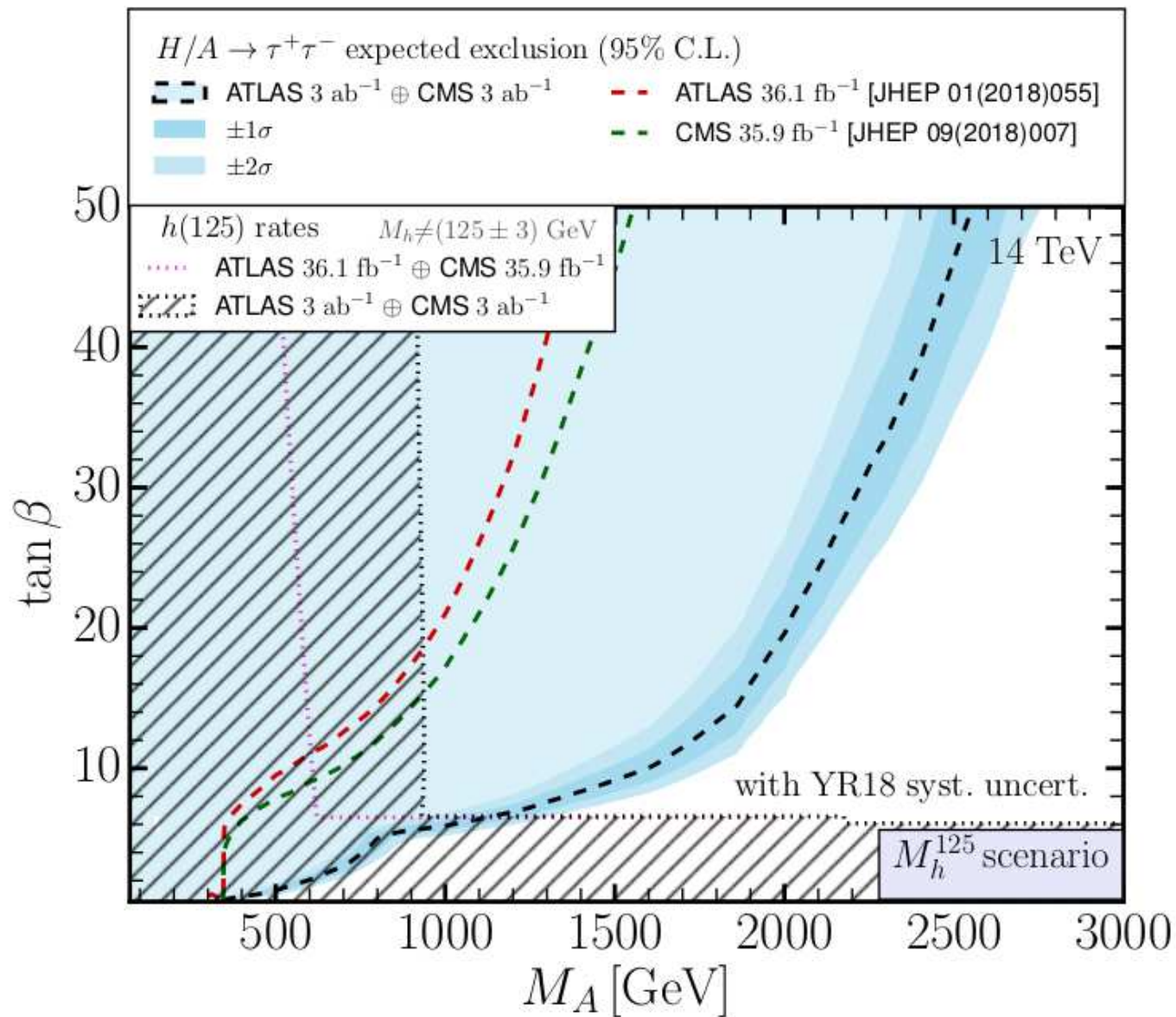
### Smart choice of MSSM parameters?

→ investigate benchmark scenarios:

- Vary only  $M_A$  and  $\tan \beta$
- Keep all other SUSY parameters fixed

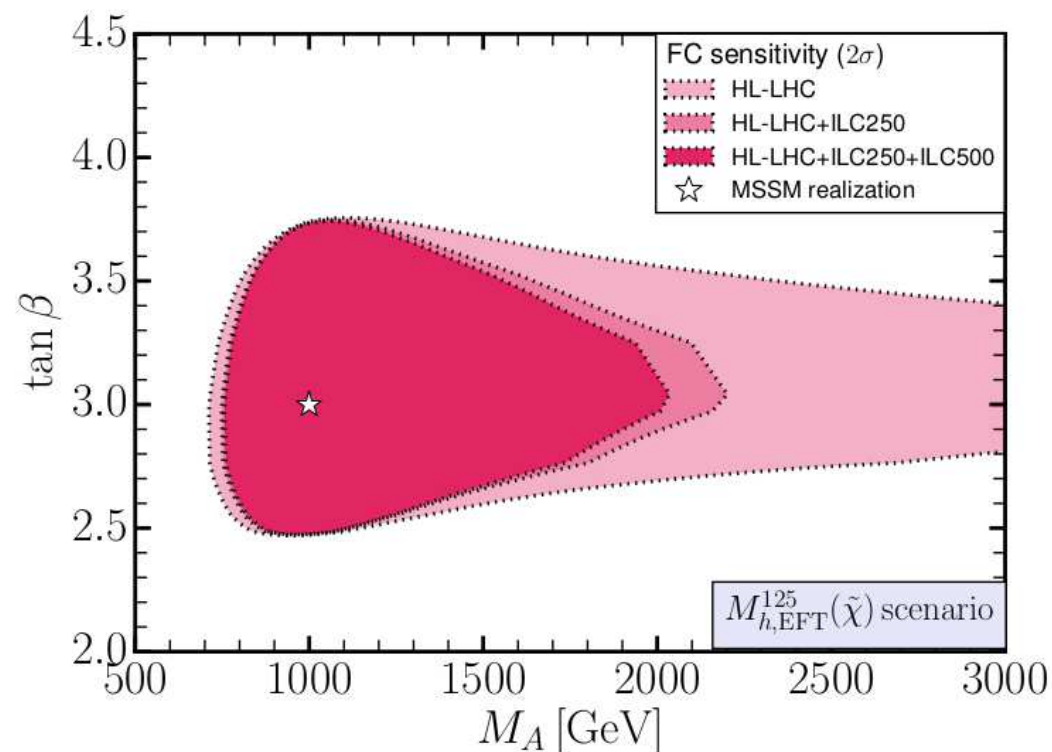
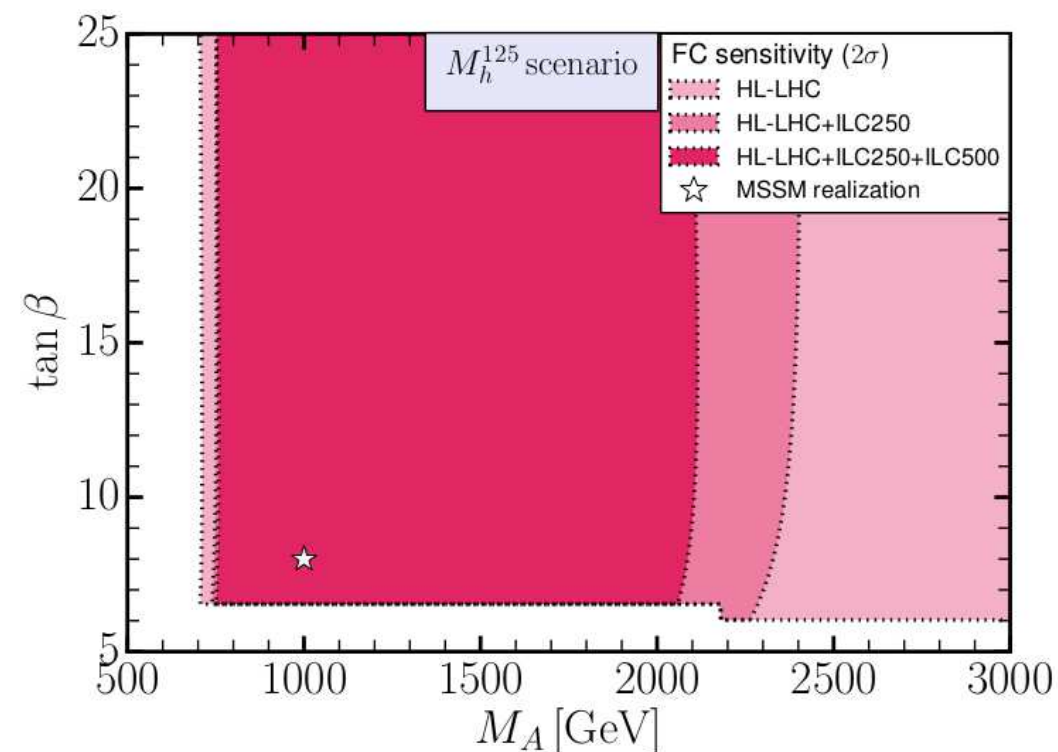
[E. Bagnaschi, H. Bahl, E. Fuchs, T. Hahn, S.H., S. Liebler, S. Patel,  
P. Slavich, T. Stefaniak, C. Wagner, G. Weiglein '18]

1.  $M_h^{125}$  scenario: 2HDM-like model
2.  $M_h^{125}(\tilde{\tau})$  scenario: light staus:  $h \rightarrow \gamma\gamma$ ,  $H/A \rightarrow \tilde{\tau}\tilde{\tau}$
3.  $M_h^{125}(\tilde{\chi})$  scenario: light EW-inos:  $H/A \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0, \tilde{\chi}_k^\pm \tilde{\chi}_l^\mp$
4.  $M_h^{125}$  (alignment) scenario:  $h$  SM-like for very low  $M_A$
5.  $M_H^{125}$  scenario:  $M_H \sim 125$  GeV, all Higgses light
6.  $M_{h_1}^{125}$  (CPV) scenario: complex phases,  $h_2$ - $h_3$  interference



⇒ direct and indirect measurements:  $M_A \gtrsim 1200$  GeV

- Assume a realization of an MSSM point:  $M_A = 1$  TeV,  $\tan \beta = 7/3$
- What limits can be set from rate/coupling measurements?



⇒ only ILC measurements give upper limit on  $M_A$

⇒ limits on  $\tan \beta$  only for small(er)  $\tan \beta$

Let us assume that we do see a deviation

**What do we learn from that?**

**How do we learn something from that?**

⇒ We have to compare the **observed** deviation with **predicted** deviations

⇒ Preferably with the predicted deviations in a **concrete models**  
(A comparison with an EFT result subsequently requires the mapping to concrete models anyway . . .)

⇒ Needed: sufficiently **precise predictions in BSM** model  
close to ready: MSSM, NMSSM  
(I am not aware of uncertainty estimates in other models)

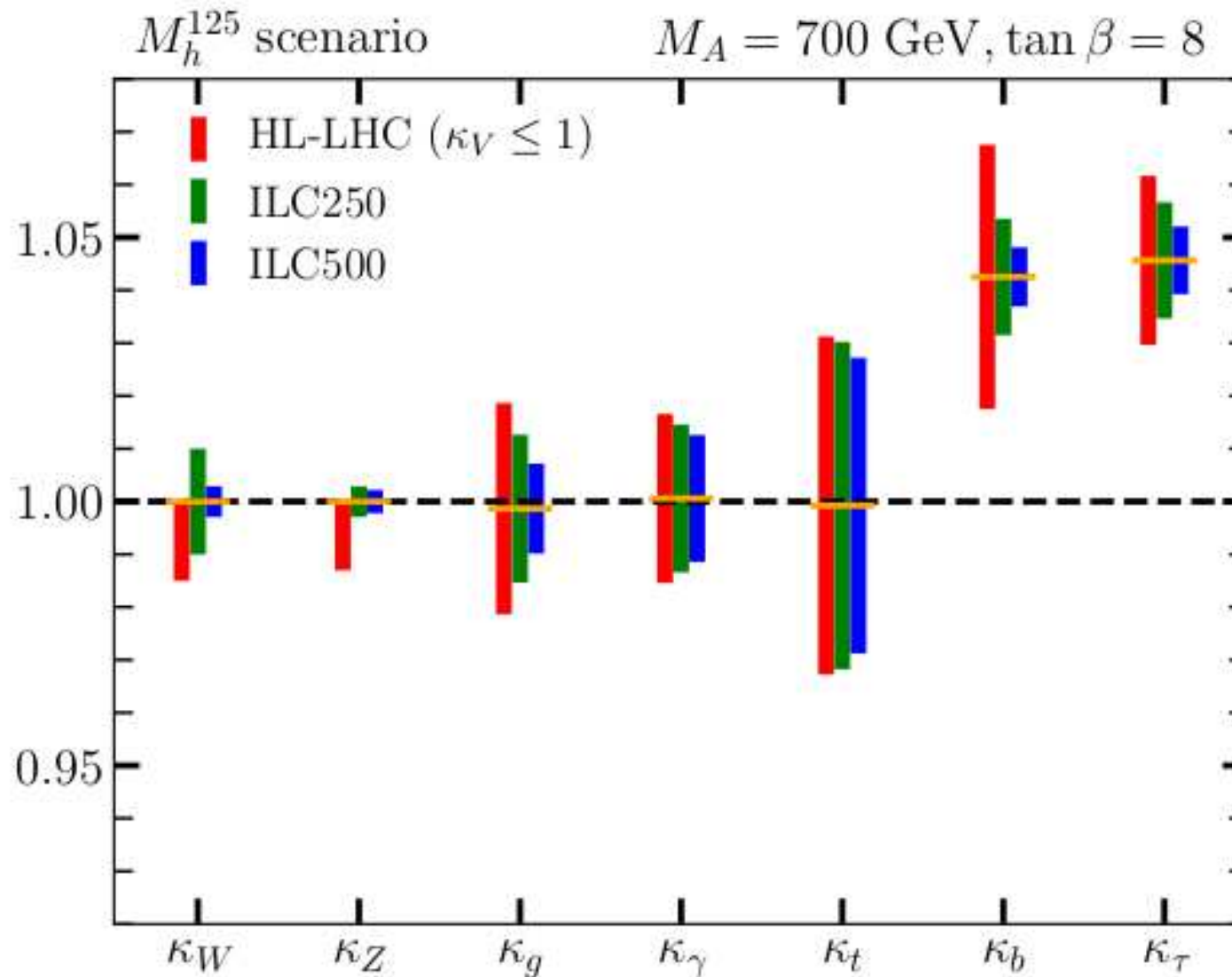
⇒ in the following:

|                                                                                       |
|---------------------------------------------------------------------------------------|
| <b>model prediction</b> (w/o TH unc.) $\Leftrightarrow$ <b>ILC precision</b> (ILC500) |
|---------------------------------------------------------------------------------------|

⇒ **“Wäscheleinen-Plots”** (Non-SUSY models in the back-up!)

# MSSM Wäscheleine I: $e^+e^-$ precision vs. $M_h^{125}$ ( $M_A = 700$ GeV, $\tan \beta = 8$ )

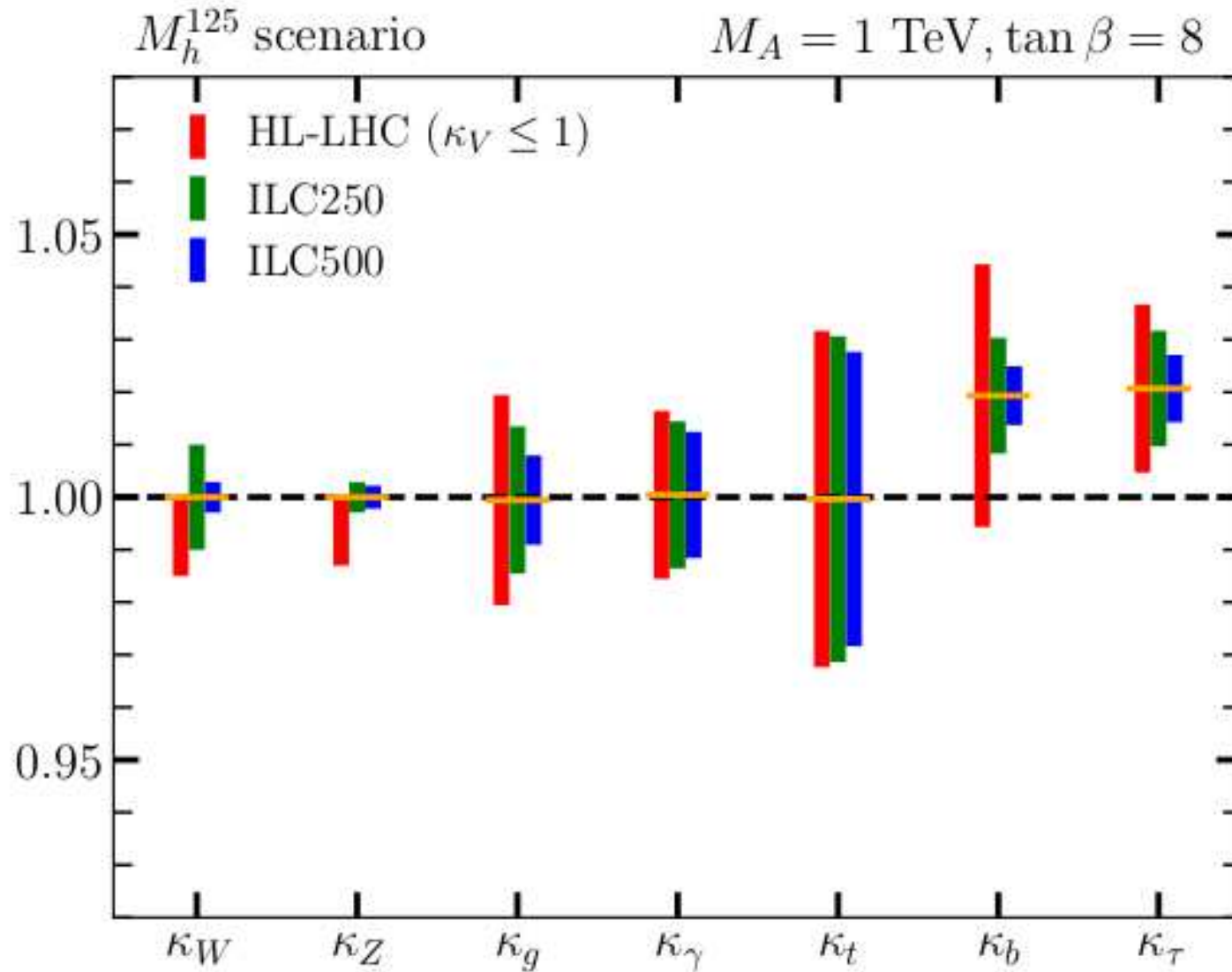
[H. Bahl et al. '20]



⇒ Type II deviations! Distinction from 2HDM possible?

## MSSM Wäscheleine II: $e^+e^-$ precision vs. $M_h^{125}$ ( $M_A = 1000$ GeV, $\tan \beta = 8$ )

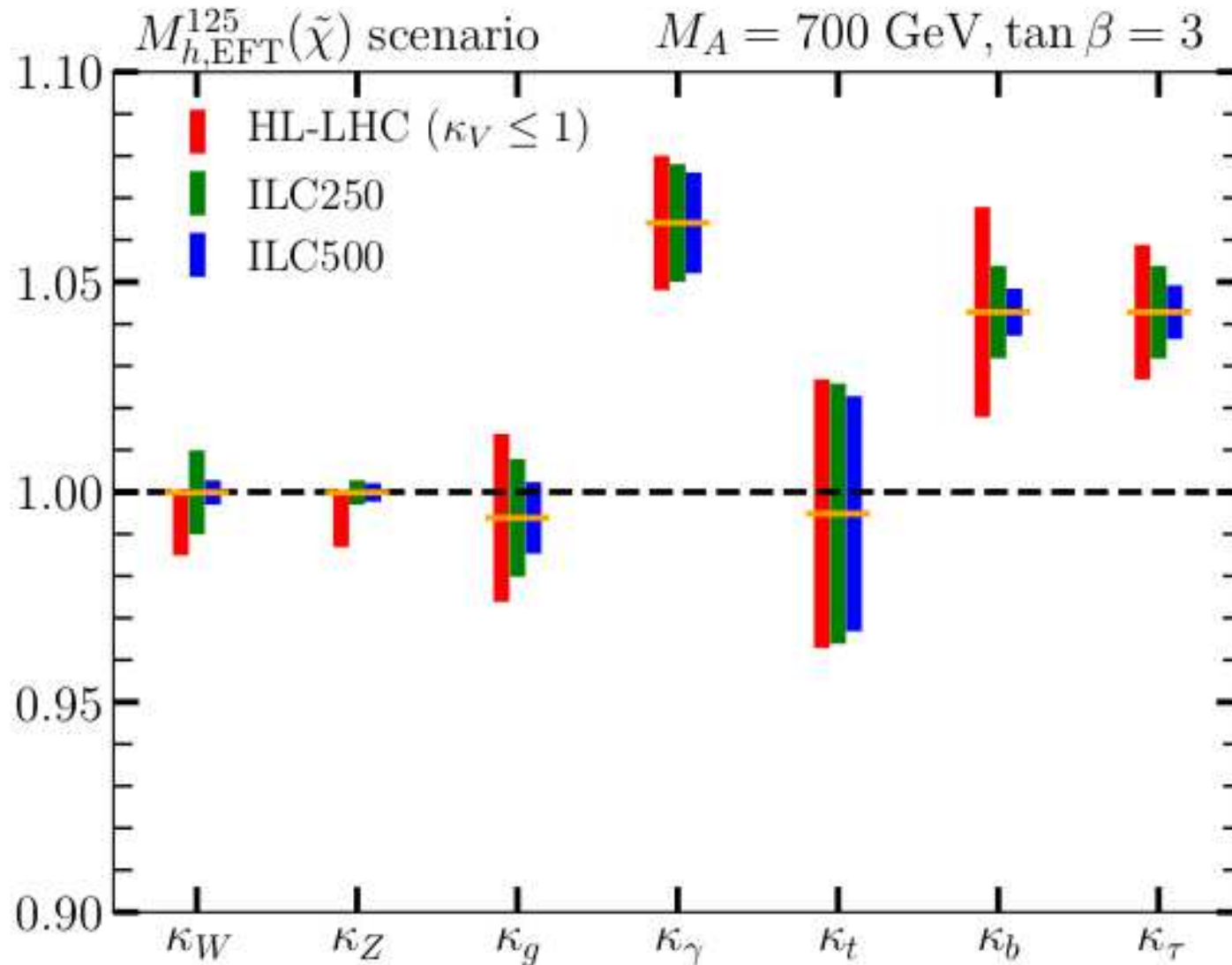
[H. Bahl et al. '20]



$\Rightarrow$  only  $e^+e^-$  measurements allows to set upper limit on  $M_A$

# MSSM Wäscheleine III: $e^+e^-$ vs. $M_h^{125,\text{EFT}}(\tilde{\chi})$ ( $M_A = 700$ GeV, $\tan \beta = 3$ )

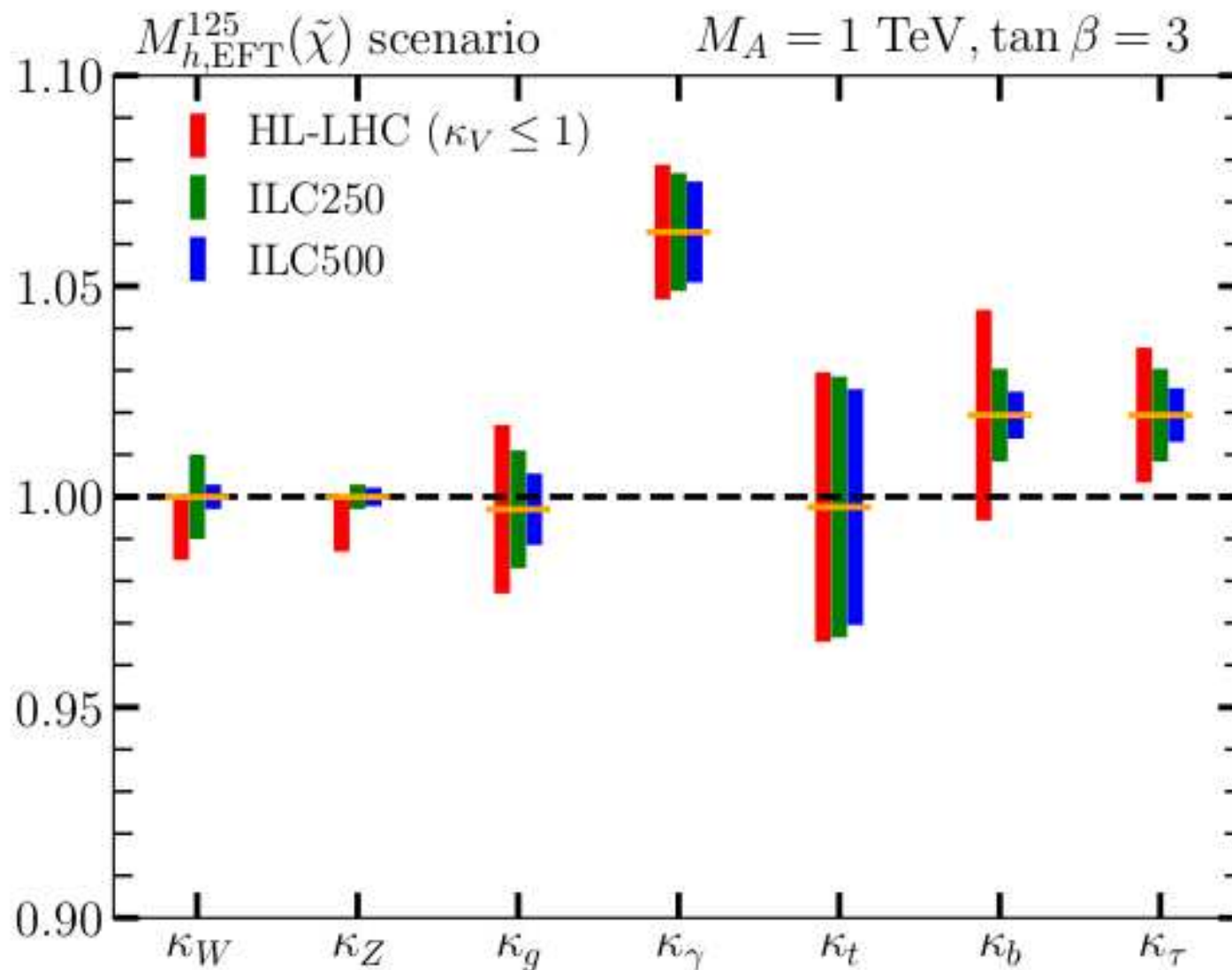
[H. Bahl et al. '20]



⇒ clear effect of light SUSY particles

# MSSM Wäscheleine IV: $e^+e^-$ vs. $M_h^{125,\text{EFT}}(\tilde{\chi})$ ( $M_A = 1000$ GeV, $\tan \beta = 3$ )

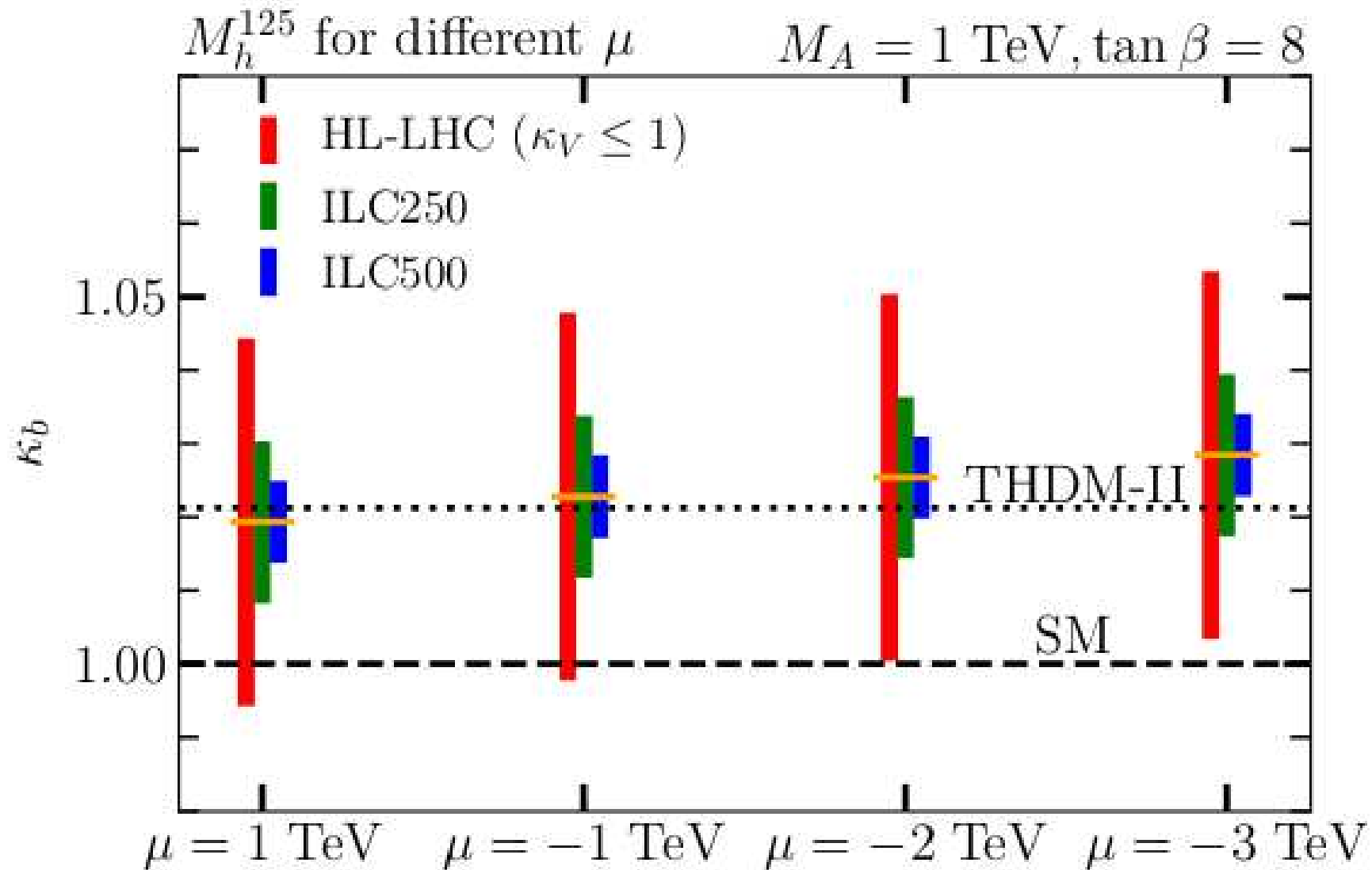
[H. Bahl et al. '20]



$\Rightarrow$  only  $e^+e^-$  measurements allows to set upper limit on  $M_A$

# MSSM Wäscheleine V: $e^+e^-$ vs. $M_h^{125}$ ( $M_A = 1000$ GeV, $\tan \beta = 8$ )

[H. Bahl et al. '20]



⇒ MSSM vs. 2HDM: very challenging!

### 3. The Higgs selfcoupling(s) at $e^+e^-$ colliders

Di-Higgs production:  $\lambda_{hhh}$  or  $\kappa_\lambda := \lambda_{hhh}/\lambda_{hhh}^{\text{SM}}$

- deviations possible in BSM models
- which size is still allowed taking all constraints into account?
- implications for measurements at future colliders?

Di-Higgs production involving heavy Higgses:  $\lambda_{hhH}$ ,  $\lambda_{hHH}$ ,  $\lambda_{hAA}$ ,  $\lambda_{hH+H-}$

- large values of  $\lambda$ 's possible?
- which size is still allowed taking all constraints into account?
- implications for searches at future colliders?

⇒ analysis in the 2HDM

[F. Arco, S.H., M. Herrero '20]

(several slides from F. Arco :-)

# The 2HDM

Two Higgs Doublet Model  $CP$  conserving

The potential: 
$$V = m_{11}^2(\Phi_1^\dagger\Phi_1) + m_{22}^2(\Phi_2^\dagger\Phi_2) - m_{12}^2(\Phi_1^\dagger\Phi_2 + \Phi_2^\dagger\Phi_1) + \frac{\lambda_1}{2}(\Phi_1^\dagger\Phi_1)^2 + \frac{\lambda_2}{2}(\Phi_2^\dagger\Phi_2)^2 \\ + \lambda_3(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_2) + \lambda_4(\Phi_1^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1) + \frac{\lambda_5}{2}[(\Phi_1^\dagger\Phi_2)^2 + (\Phi_2^\dagger\Phi_1)^2]$$

Considerations:

- ★  $CP$  conserving  $\longrightarrow$  all parameters are real
- ★  $\mathbb{Z}_2$  symmetry to avoid FCNC  $\longrightarrow$  softly broken by  $m_{12}^2$  **Very important!**
- ★ Four types of Yukawa structure (we will focus on type I and II)

CP  
odd

7 free parameters + 5 physical states:  $h, H, A, H^+$  and  $H^-$

CP even

Extension of  $\mathbb{Z}_2$  symmetry to fermions  $\Rightarrow$  4 types  
 $\Rightarrow$  analyzed: type I and type II

## The constraints:

→ applied to every point analyzed/scanned/...

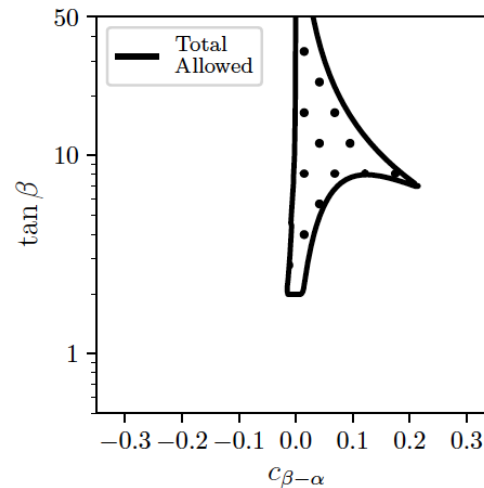
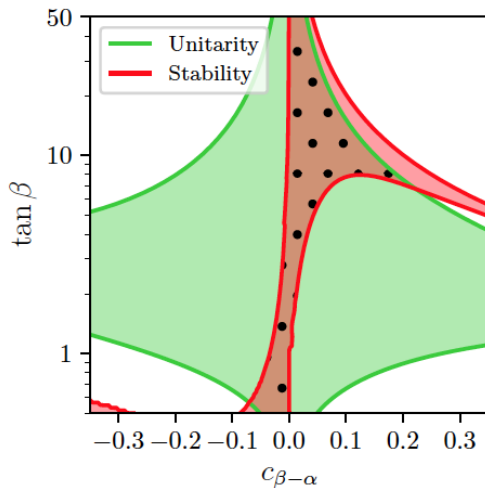
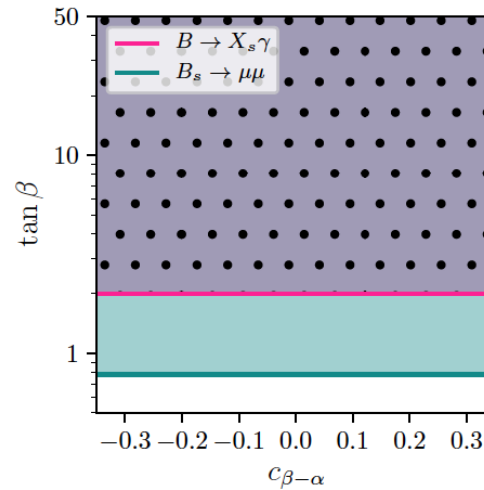
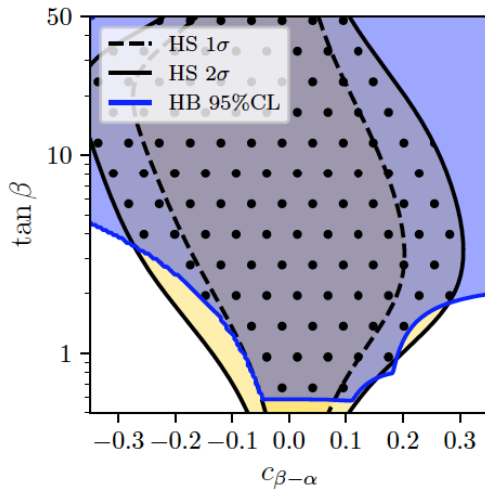
- Tree-level perturbativity
- Stability: potential is bounded from below
- Higgs searches at LEP, Tevatron, LHC  $\Rightarrow$  HiggsBounds (2HDMC)
- SM-like Higgs properties  $\Rightarrow$  HiggsSignals (2HDMC)
- Flavor physics (mainly  $\text{BR}(B_s \rightarrow X_s \gamma)$ ,  $\Delta M_{B_s}$ )  $\Rightarrow$  SuperIso
- Electroweak precision data ( $S$ ,  $T$  and  $U$ )  $\Rightarrow$  2HDMC

## 2HDM type I, scenario C

$$m_H = m_A = m_{H^\pm} = 1000 \text{ GeV (scenario C)}$$

$$m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$$

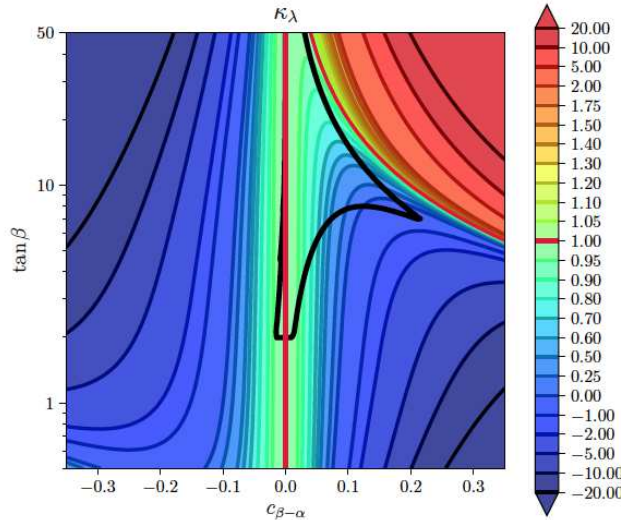
- ★ Collider searches imposes  $|c_{\beta-\alpha}| \lesssim 0.3$
- ★ Low  $\tan \beta$  disallowed by  $B \rightarrow X_s \gamma$
- ★ Most stringent bounds from theoretical constraints, but helped by  $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$



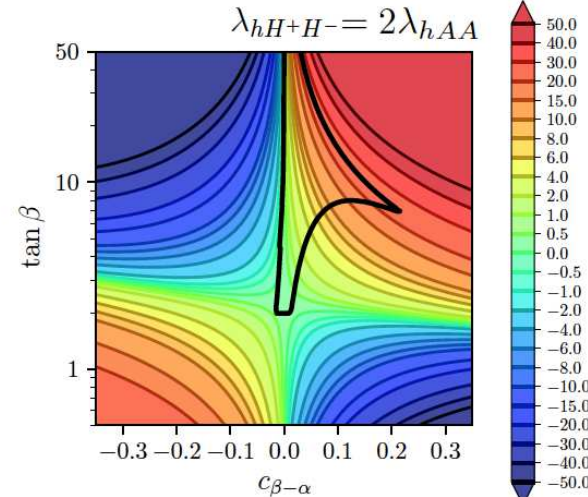
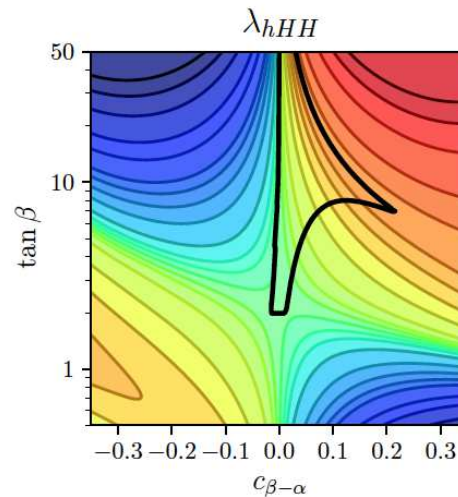
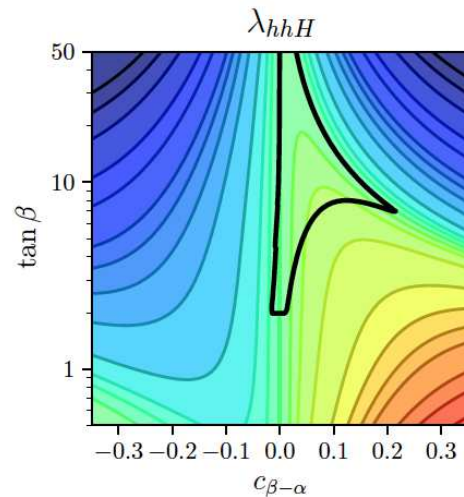
## 2HDM type I, scenario C

$$m_H = m_A = m_{H^\pm} = 1000 \text{ GeV (scenario C)}$$

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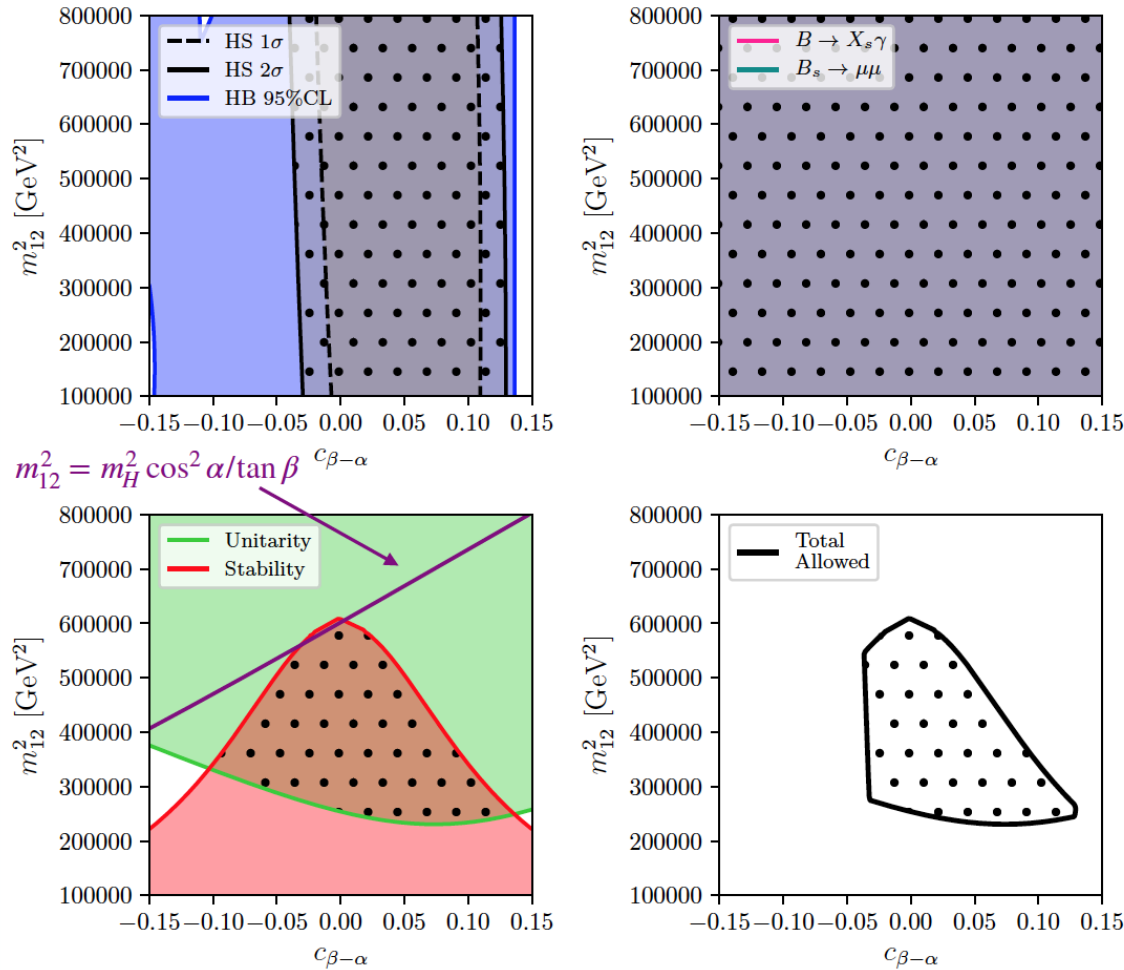
- ★ Min  $\kappa_\lambda \sim -0.4$  in the “tip” with  $\tan \beta \sim 7$  and  $c_{\beta-\alpha} \sim 0.2$
- ★ Max  $\lambda_{hhH} \sim 1.2$  for  $c_{\beta-\alpha} \sim 0.1$
- ★ Max  $\lambda_{hHH} \sim 12$  and  $\lambda_{hH+H^-} = 2\lambda_{hAA} \sim 24$  in the unitarity border



⇒ large deviations for  $\kappa_\lambda$

⇒ large values for BSM  $\lambda$ 's

## 2HDM type II, scenario C



$$m_H = m_A = m_{H^\pm} = 1100 \text{ GeV (scenario C)}$$

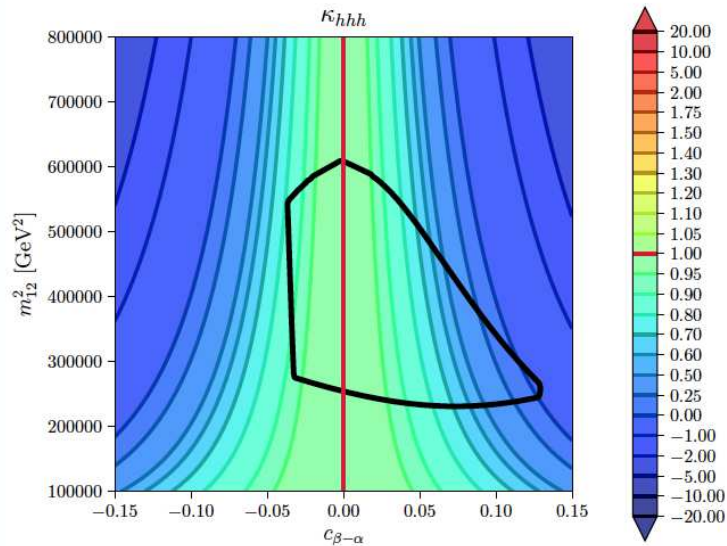
$$\tan \beta = 0.9$$

- ★ Collider measurements  
 $c_{\beta-\alpha} \in [-0.05, 0.13]$  nearly independent of  $m_{12}^2$
- ★ No bounds from flavor
- ★ Overlapped allowed region by unitarity and stability  
 $(m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta \text{ does not work here})$

## 2HDM type II, scenario C

$$m_H = m_A = m_{H^\pm} = 1100 \text{ GeV (scenario C)}$$

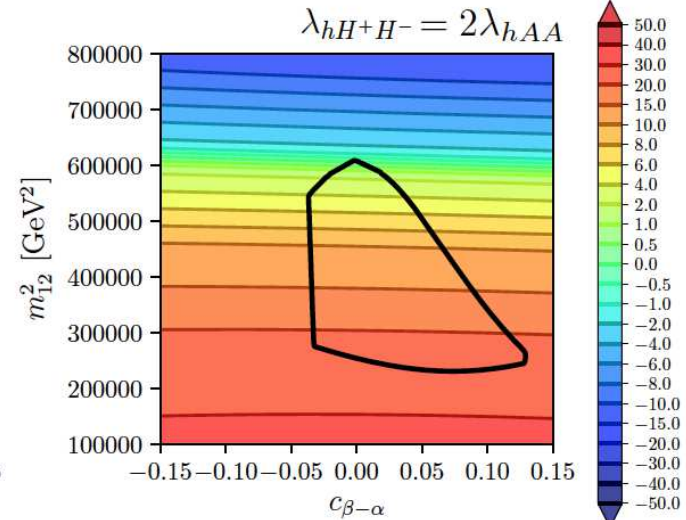
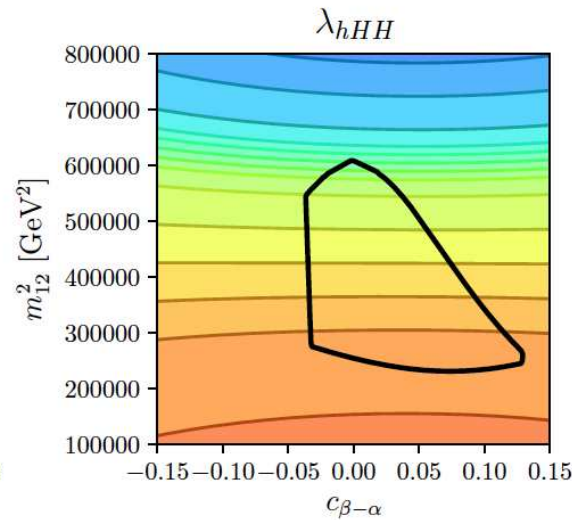
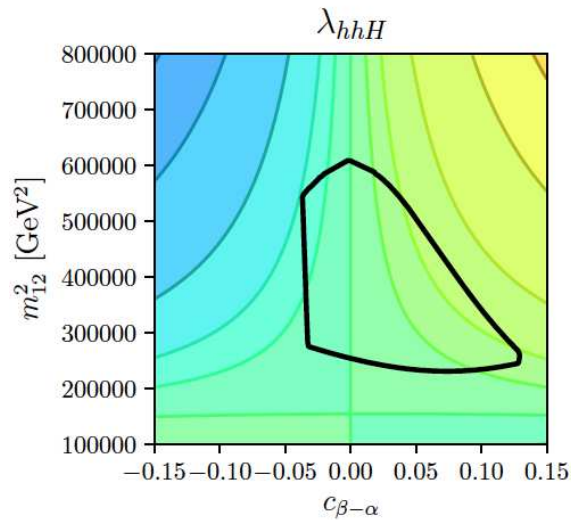
$$\tan \beta = 0.9$$



★ Min  $\kappa_\lambda \sim -1.0$  for max  $c_{\beta-\alpha} \sim 0.13$

★ Allowed  $\lambda_{hhH} \in [-1, 1.4]$

★ Max  $\lambda_{hHH} \sim 12$  and  $\lambda_{hH^+H^-} = 2\lambda_{hAA} \sim 24$  for min  $m_{12}^2 \sim 2 \times 10^5 \text{ GeV}^2$



⇒ large deviations for  $\kappa_\lambda$

⇒ large values for BSM  $\lambda$ 's

## Final allowed ranges

### Type I

$$\kappa_\lambda \in [-0.5, 1.5]$$

$$\lambda_{hhH} \in [-1.4, 1.5]$$

$$\lambda_{hHH} \in [0, 15]$$

$$\lambda_{hAA} \in [0, 16]$$

$$\lambda_{hH^+H^-} \in [0, 32]$$

### Type II

$$\kappa_\lambda \in [0.0, 1.0]$$

$$\lambda_{hhH} \in [-1.6, 1.8]$$

$$\lambda_{hHH} \in [0, 15]$$

$$\lambda_{hAA} \in [0, 16]$$

$$\lambda_{hH^+H^-} \in [0, 32]$$



Far from the alignment limit  
and playing with  $m_{12}^2$



For  $c_{\beta-\alpha} \sim \pm 0.05$

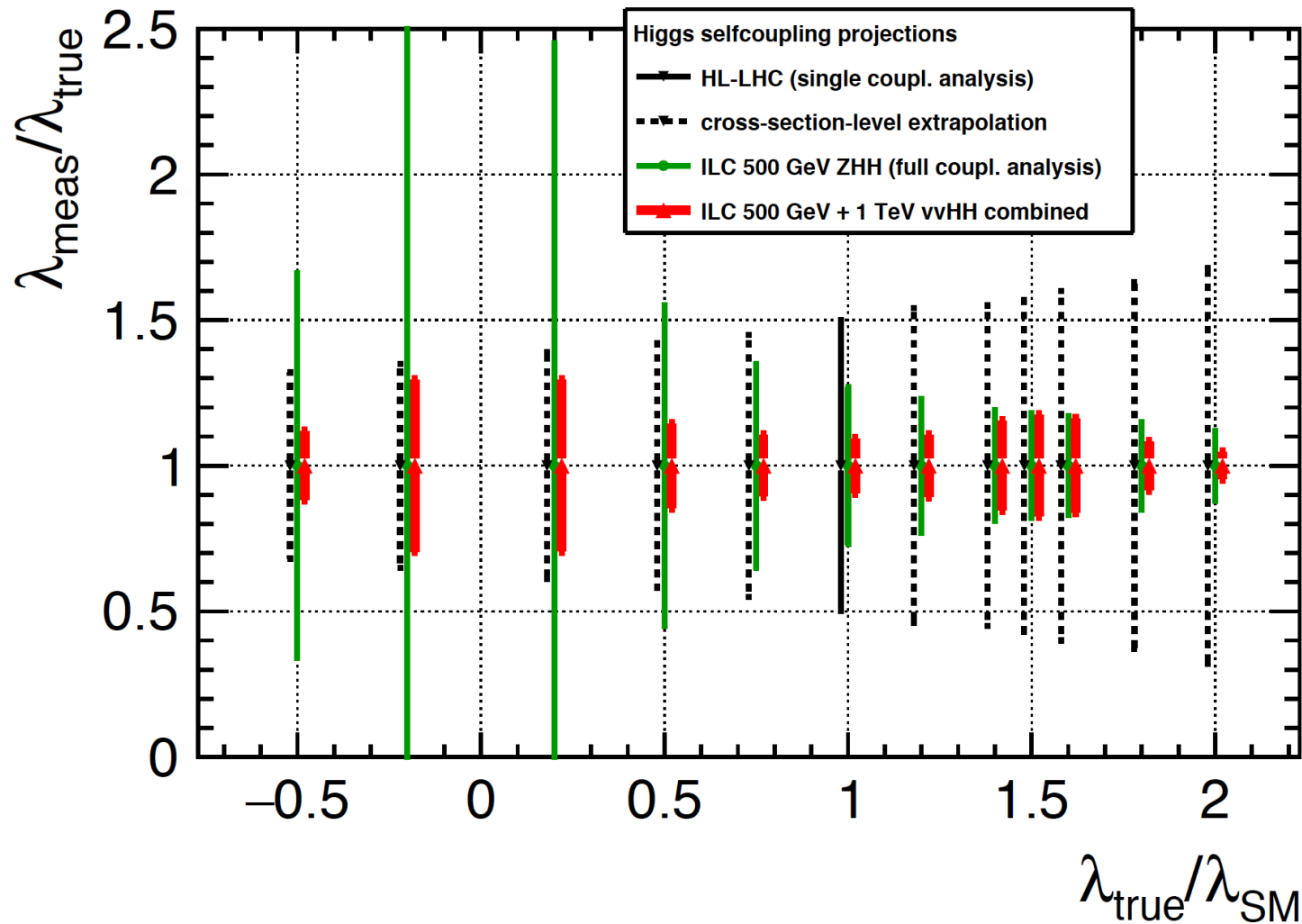


Large masses and nearly  
independent of  $c_{\beta-\alpha}$  and  
scenario A or B

✨ Interesting points are shown in our paper [arXiv:2005.10576] ✨

# Measurement of the triple Higgs selfcoupling

[J. List et al. – PRELIMINARY]



⇒ over most of the parameter space ILC is clearly superior to HL-LHC

## Production cross sections at (high-energy) $e^+e^-$ colliders

[F. Arco, S.H., M. Herrero – PRELIMINARY]

⇒ many benchmark points proposed ⇒ example “point 6”:

Proposed benchmark point: 2HDM type I

Input:

$$m_h = 125 \text{ GeV}$$

$$m_H = m_A = m_{H^\pm} = 600 \text{ GeV}$$

$$\tan \beta = 10$$

$$\cos(\beta - \alpha) = 0.2$$

$$m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta \simeq 36000 \text{ GeV}^2$$

Output:

$$\kappa_\lambda := \lambda_{hhh} / \lambda_{hhh}^{SM} \simeq 1$$

$$\lambda_{hhH} = -0.5$$

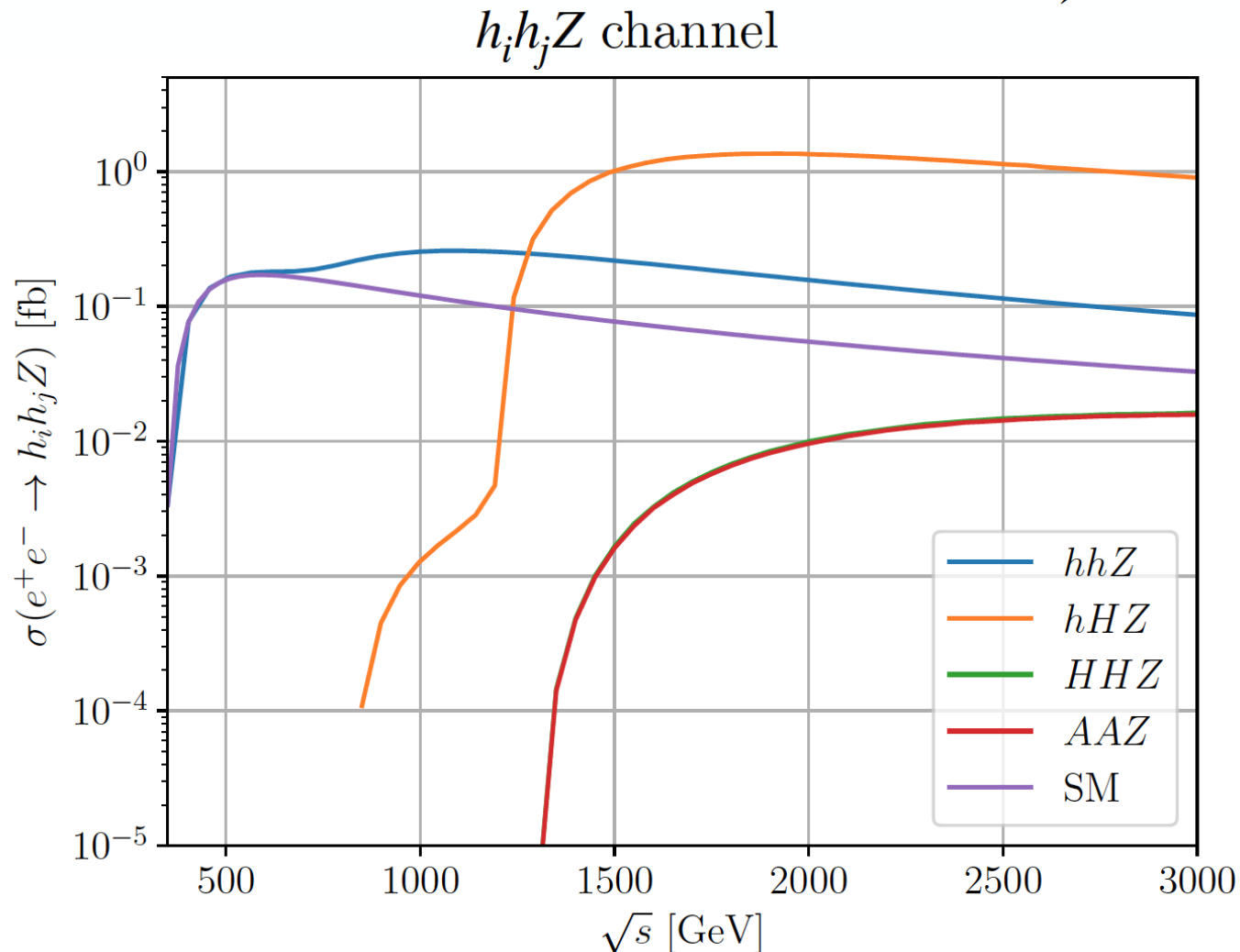
$$\lambda_{hHH} = \lambda_{hAA} = 6$$

$$\lambda_{hH^+H^-} = 12$$

⇒ contribution to new Snowmass  $HH$  initiative

## Various di-Higgs production cross sections I: (P6)

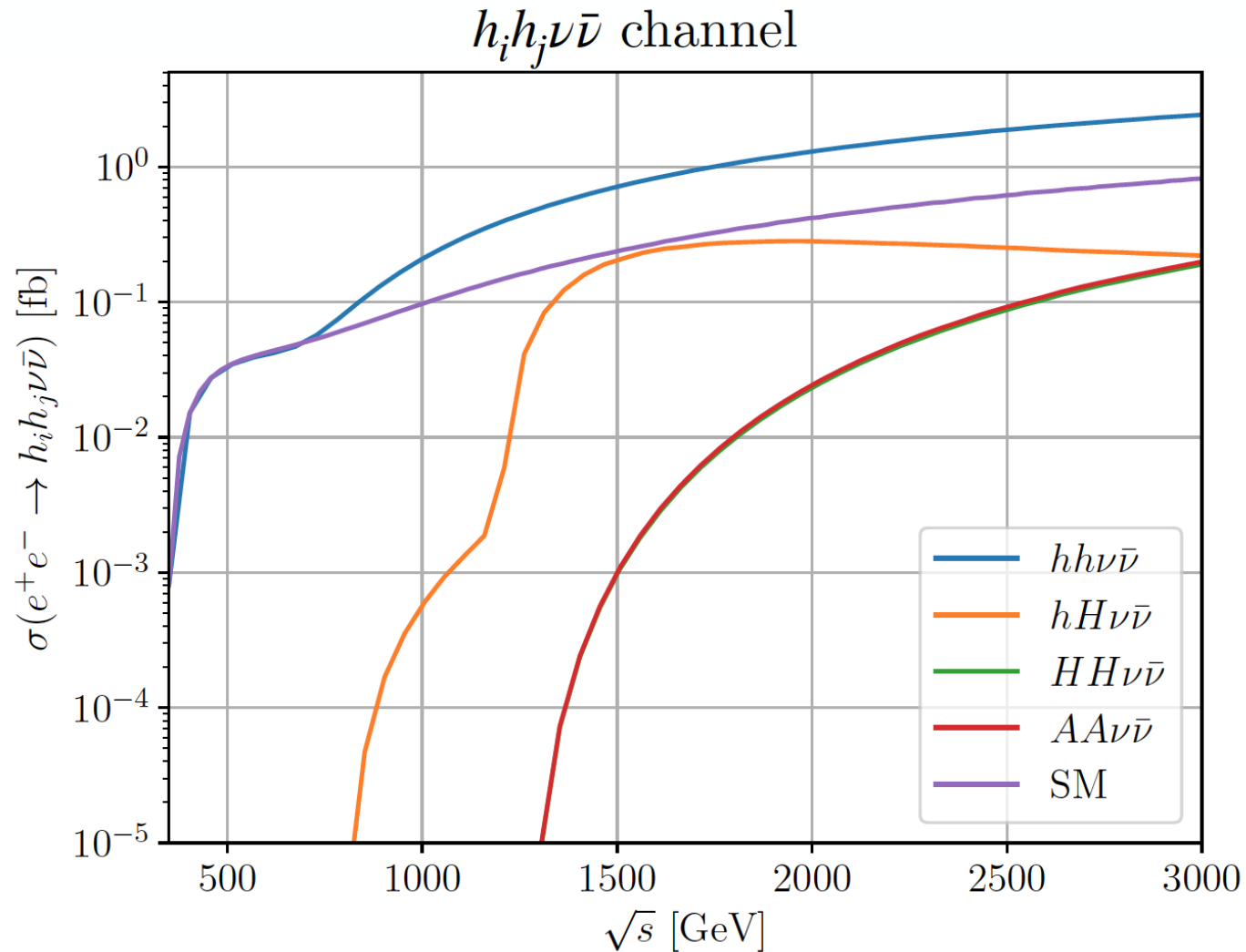
[F. Arco, S.H., M. Herrero – PRELIMINARY]



⇒ strong enhancement w.r.t. SM XS, large BSM XS's

## Various di-Higgs production cross sections II: (P6)

[F. Arco, S.H., M. Herrero – PRELIMINARY]

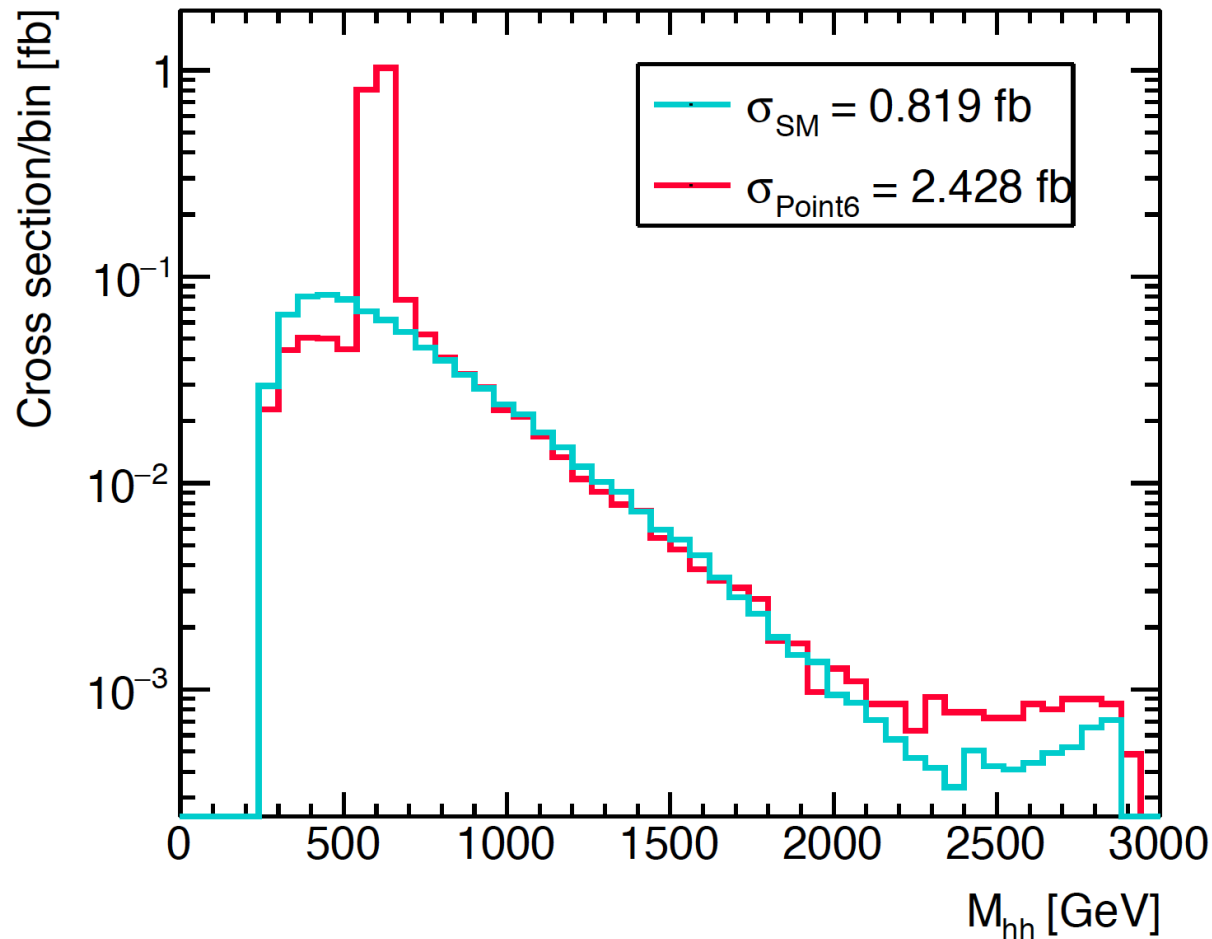


⇒ strong enhancement w.r.t. SM XS, large BSM XS's

## Invariant mass distribution: (P6)

[F. Arco, S.H., M. Herrero – PRELIMINARY]

$$\sigma(e^-e^+ \rightarrow hh\nu\bar{\nu}), \sqrt{s} = 3000\text{GeV}$$



⇒ heavy Higgs boson in the  $s$ -channel strongly contributes

## 4. BSM Higgs bosons below 125 GeV

- Is there an excess?  
There are 2.5!
- Can this be explained?
- indirect HL-LHC/**ILC** opportunities  
(Similar for **FCC-ee**, **CEPC**! **CLIC**?)
- direct ILC opportunities

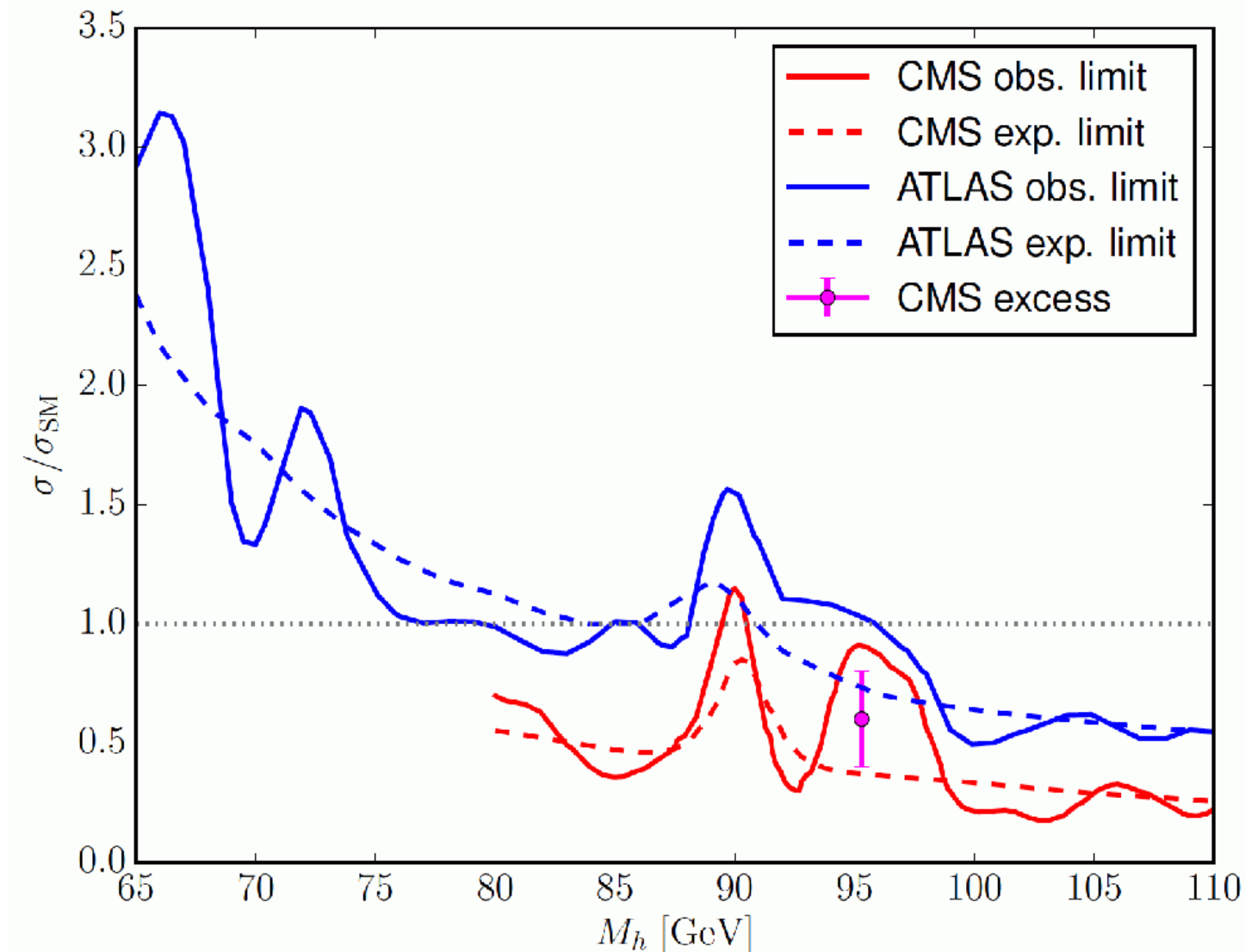


## What was seen at CMS and ATLAS?

[CMS '17, ATLAS '18, S.H., T. Stefaniak '18]

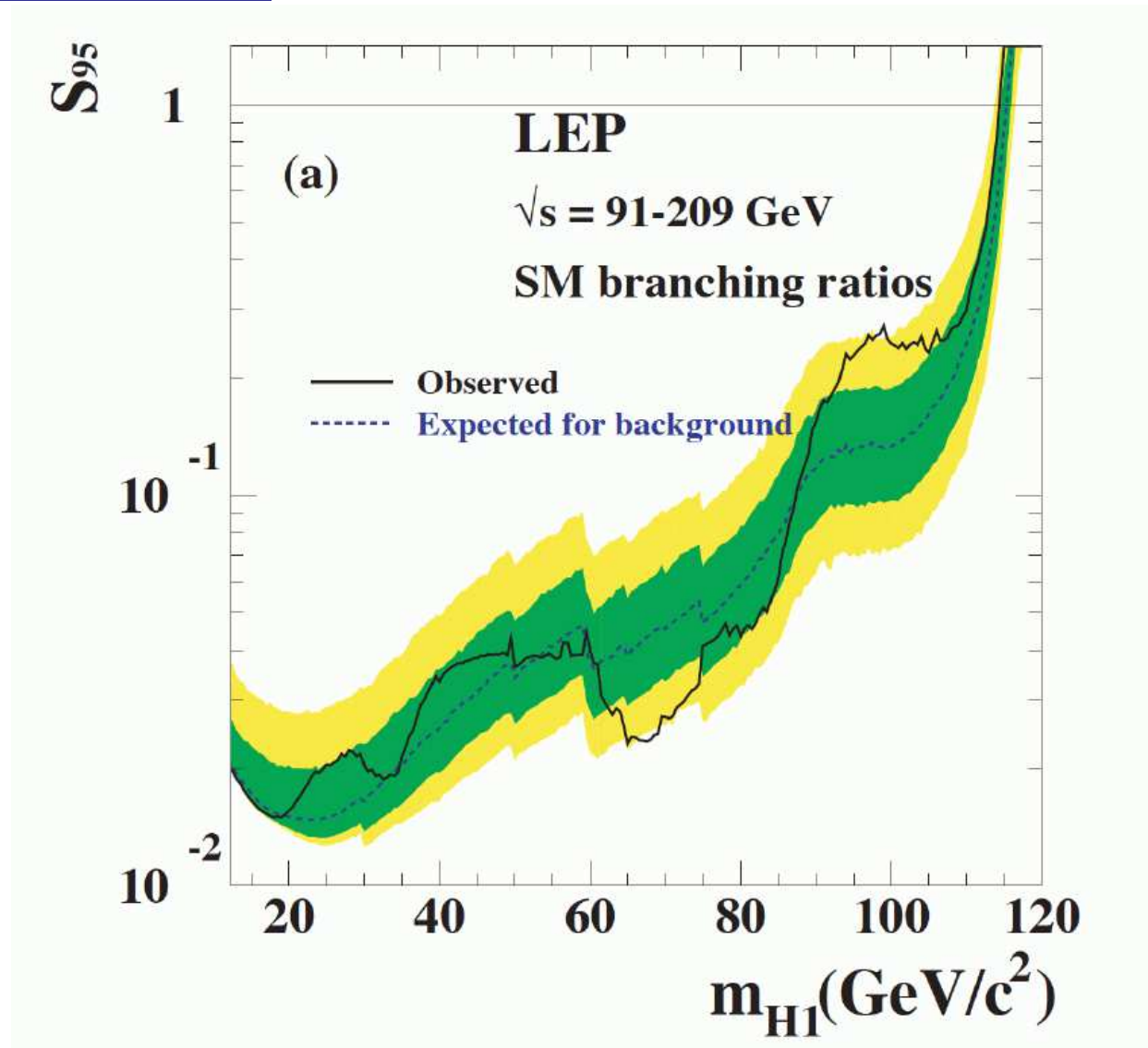
Search for  $pp \rightarrow \phi \rightarrow \gamma\gamma$  with  $m_\phi \leq 125$  GeV

$\mu_{\text{CMS}} = 0.6 \pm 0.2$



⇒ if there is something, it would look exactly like this!

## What was seen at LEP?



$$\mu_{\text{LEP}}(98 \text{ GeV}) = \left[ \sigma(e^+e^- \rightarrow Zh_1) \times \text{BR}(h_1 \rightarrow b\bar{b}) \right]_{\text{exp/SM}} = 0.117 \pm 0.057$$

## Investigation in BSM Higgs models: N2HDM

[*T. Biekötter, M. Chakraborti, S.H. '19*]

Fields:

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \rho_1 + i\eta_1) \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \rho_2 + i\eta_2) \end{pmatrix}, \quad \Phi_S = v_S + \rho_S$$

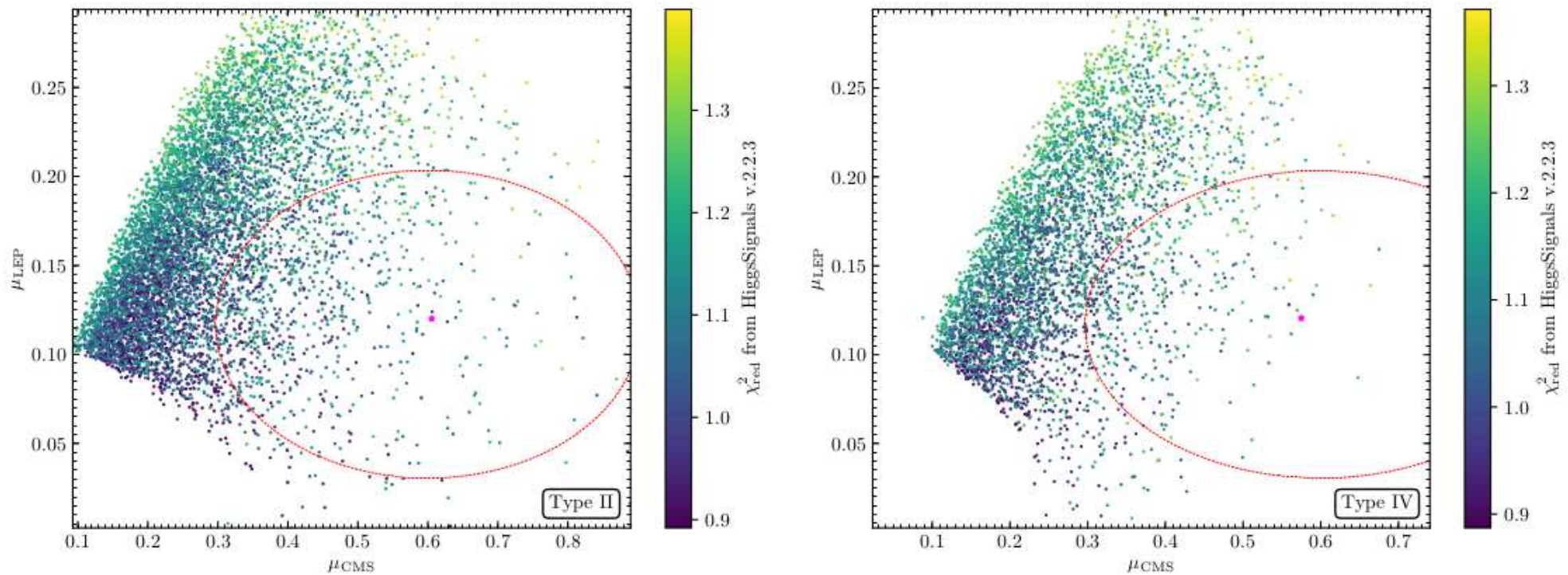
Physical states:  $h_1, h_2, h_3$  ( $\mathcal{CP}$ -even),  $A$  ( $\mathcal{CP}$ -odd),  $H^\pm$  (charged)

|                            | $u$ -type | $d$ -type | leptons  |
|----------------------------|-----------|-----------|----------|
| type I                     | $\Phi_2$  | $\Phi_2$  | $\Phi_2$ |
| type II                    | $\Phi_2$  | $\Phi_1$  | $\Phi_1$ |
| type III (lepton-specific) | $\Phi_2$  | $\Phi_2$  | $\Phi_1$ |
| type IV (flipped)          | $\Phi_2$  | $\Phi_1$  | $\Phi_2$ |

$\Rightarrow$  exactly as in 2HDM

## Fitting the excesses:

[*T. Biekötter, M. Chakraborti, S.H. '19*]



⇒ excesses well fitted, with good  $\chi^2_{\text{red}}$ : 0.9 – 1.3

⇒ preferred  $M_{H^\pm}$ : 650 GeV – 950 GeV (lower limit: flavor constr.)

⇒ preferred  $\tan \beta$ : 0.8 – 3.8

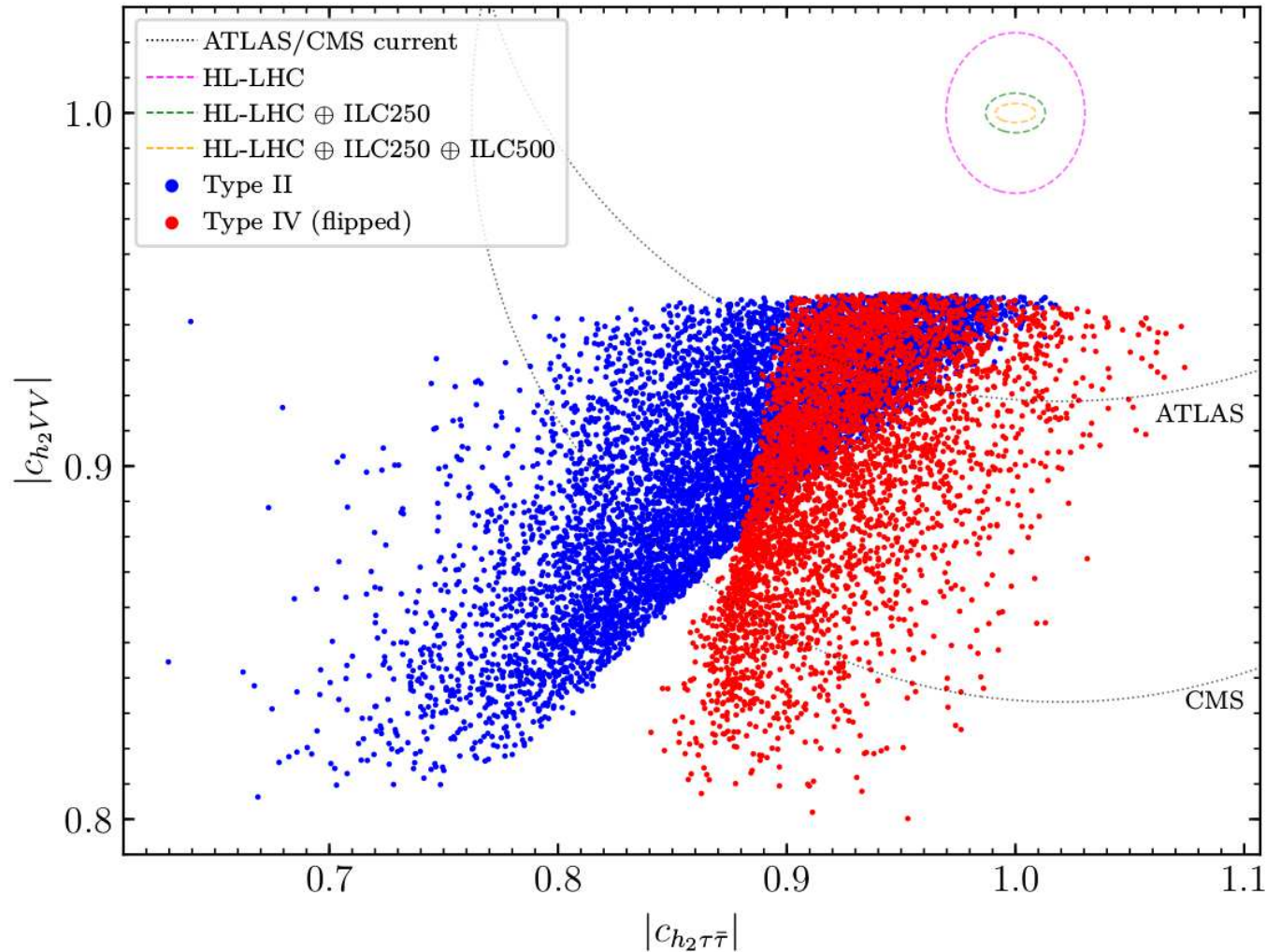
## What can we learn from future measurements?

- LHC  $h_{125}$  coupling measurements
- HL-LHC  $h_{125}$  coupling measurements
- ILC (or other  $e^+e^-$  coll.)  $h_{125}$  coupling measurements
- **NEW:** ILC (or other  $e^+e^-$  coll.)  $\phi_{96}$  coupling measurements  
[S.H., P. Toledo '20]
- direct production of  $\phi_{96}$  at the LHC
- direct production of  $\phi_{96}$  at the HL-LHC
- direct production of  $\phi_{96}$  at the ILC (or other  $e^+e^-$  coll.)
- production of other BSM Higgs bosons at the LHC/HL-LHC/ILC/...

## What can we learn from future measurements?

- LHC  $h_{125}$  coupling measurements  $\Leftarrow$  focus
- HL-LHC  $h_{125}$  coupling measurements  $\Leftarrow$  focus
- ILC (or other  $e^+e^-$  coll.)  $h_{125}$  coupling measurements  $\Leftarrow$  focus
- **NEW:** ILC (or other  $e^+e^-$  coll.)  $\phi_{96}$  coupling measurements  $\Leftarrow$  focus  
[S.H., P. Toledo '20]
- direct production of  $\phi_{96}$  at the LHC
- direct production of  $\phi_{96}$  at the HL-LHC
- direct production of  $\phi_{96}$  at the ILC (or other  $e^+e^-$  coll.)  $\Leftarrow$  focus
- production of other BSM Higgs bosons at the LHC/HL-LHC/ILC/...

Future measurements:  $\Rightarrow$  HL-LHC/ILC Higgs coupling measurements



$\Rightarrow$  type II and IV show strong deviations from SM

$\Rightarrow$  N2HDM can always be distinguished from SM!

## Probes of the 96 GeV Higgs at the ILC

- Direct production at the ILC

Uses work by:

*[P. Drechsel, G. Moortgat-Pick, G. Weiglein '18]*

*[Y. Wang, M. Berggren, J. List '20]*

- Coupling measurements at the ILC *[S.H., P. Toledo '20]*

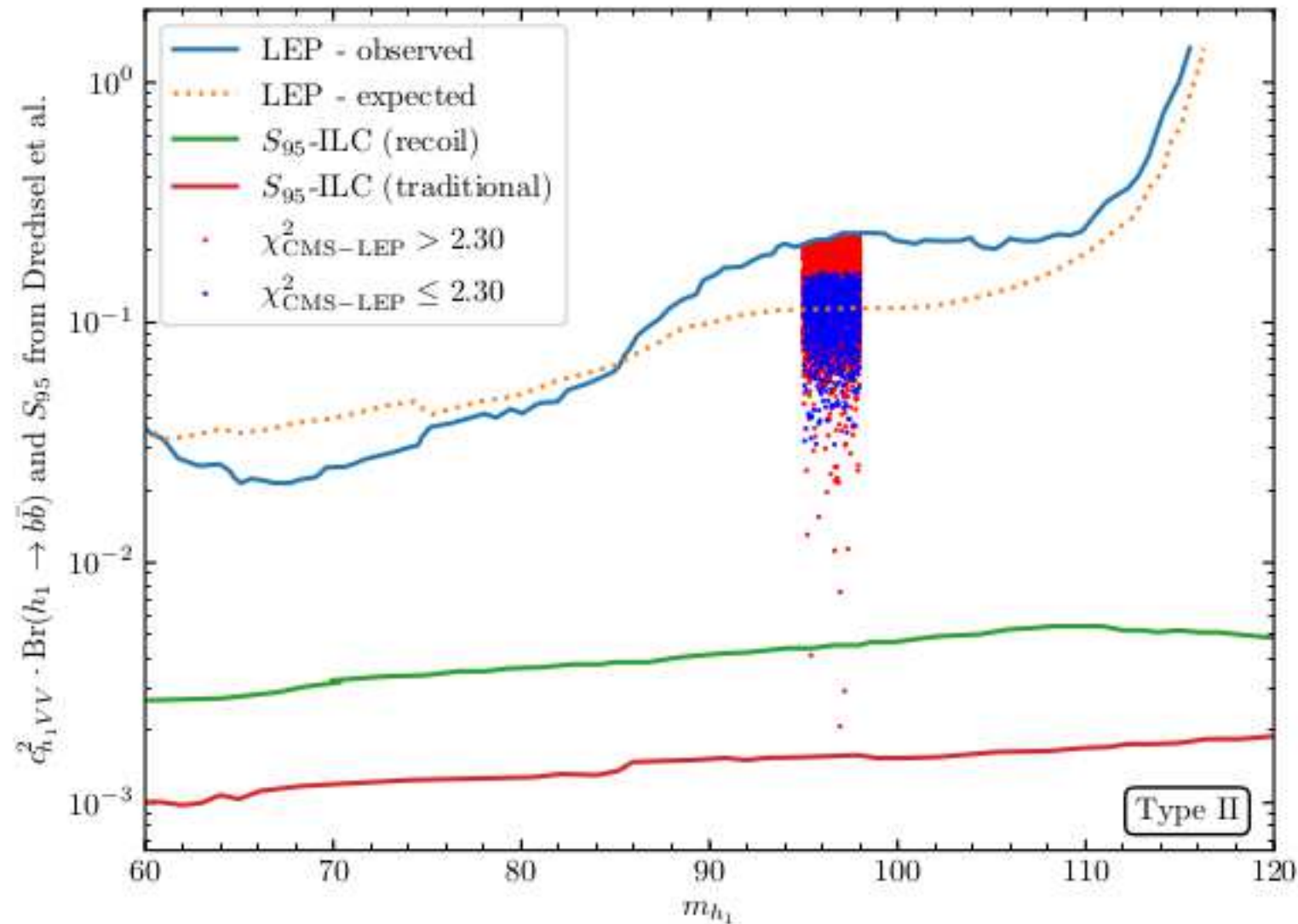
Thanks go to:

- T. Biekötter (for the data and discussions)
- M. Cepeda (for her help with the formulas)
- J. List (for help on  $S/B$  in BSM models)
- J. Tian (for help on  $S/B$  in the SM)
- C. Schappacher (for some production cross sections)

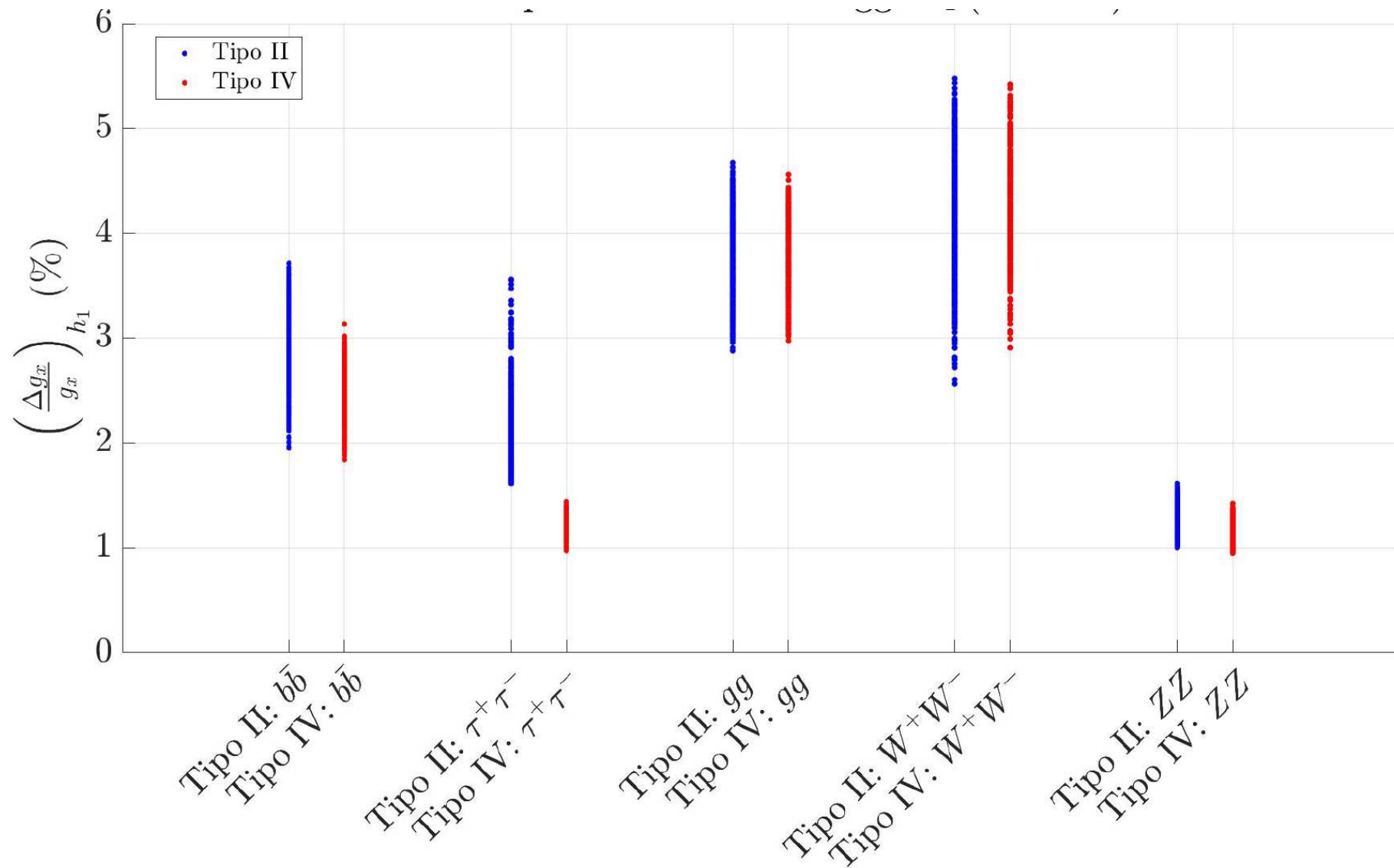
⇒ focus on “good” points with  $\chi^2_{\text{CMS-LEP}} < 2.3$

Next project?  $\Rightarrow$  ILC production of the light scalar

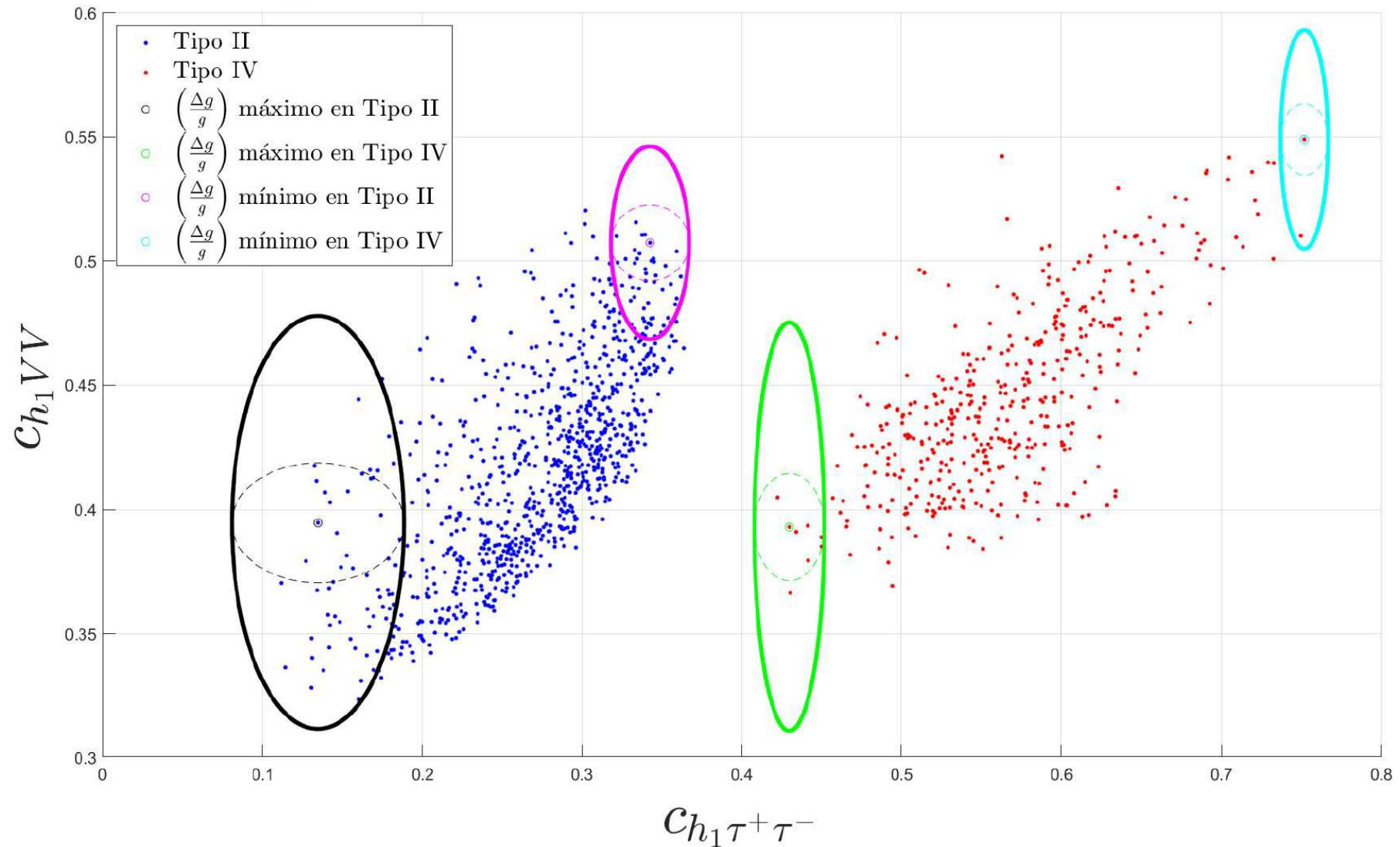
[*T. Biekötter, M. Chakraborti, S.H. '19*]



$\Rightarrow$  new state easily in the reach of the ILC  $\Rightarrow$  coupling measurements



$\Rightarrow \mathcal{O}(1 - 5\%)$ :  $g_Z$  best from production,  $g_\tau$  very precise in type IV



⇒ model distinction possible via coupling measurements

## 5. Conclusions:      There is BSM physics! Extended Higgs sector likely?!

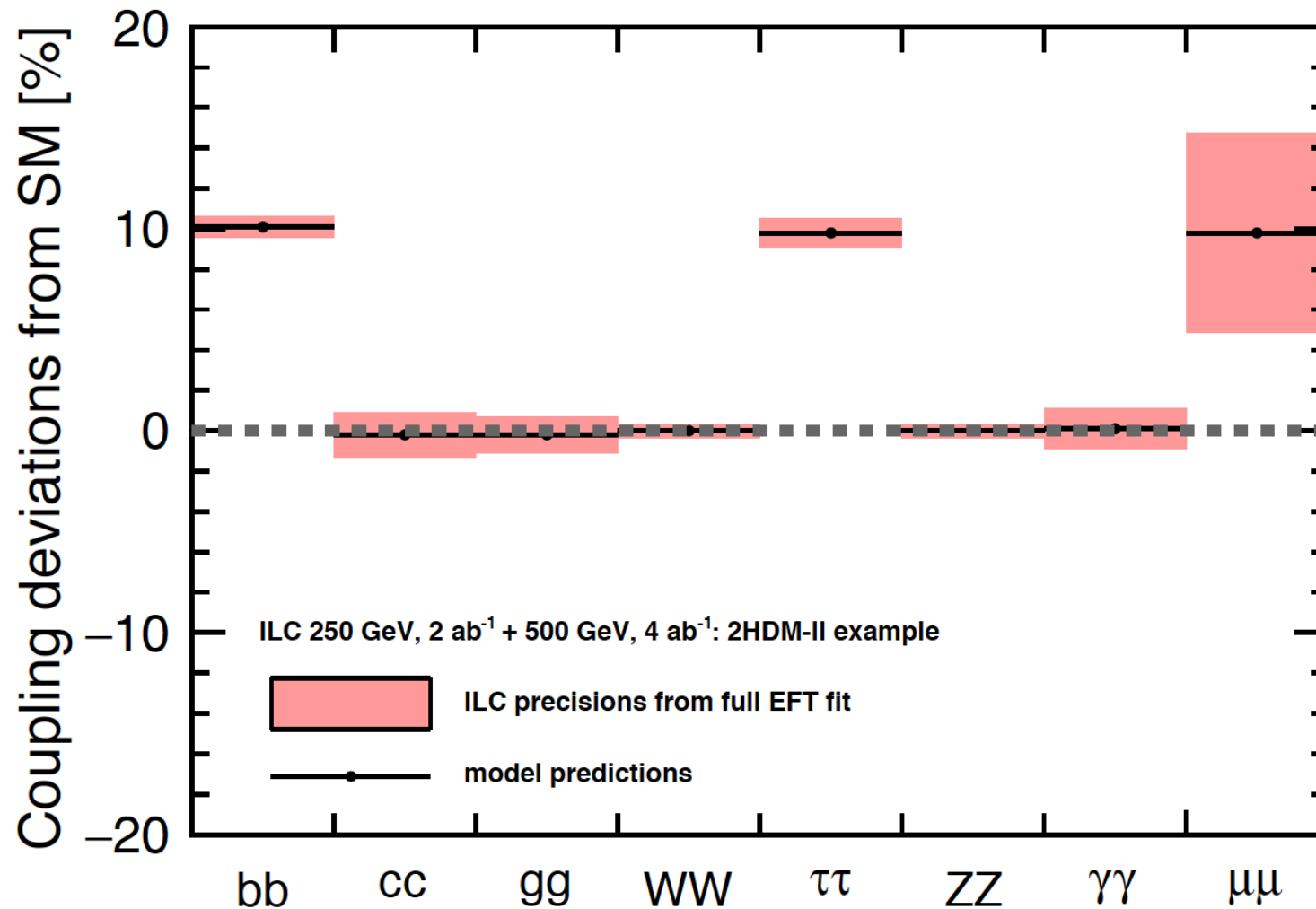
- Higgs precision meas. and BSM physic (ILC, CLIC, FCC-ee, CEPC)
  - **MSSM** is taken as a showcase
  - HL-LHC can test  $M_A$  up to  $\sim 1.2$  TeV
  - ILC can set **upper limit** on undiscovered mass scales
  - light SUSY particles can have a strong impact  $\Rightarrow$  parameter det.?!
  - difficult to disentangle SUSY effects from Higgs effects
- Higgs selfcoupling(s) at  $e^+e^-$  colliders (ILC, CLIC)
  - Analysis in the **2HDM type I, II**
  - all constraints (theo/exp) are taken into account
  - **large deviations in  $\lambda_{hhh}$**  still possible (more in type I)
  - over most of the parameter space ILC is clearly superior to HL-LHC
  - large BSM triple Higgs couplings possible
  - large SM-like and BSM di-Higgs production cross sections
- BSM Higgs bosons below 125 GeV (ILC, FCC-ee, CEPC; CLIC?)
  - analysis of a **96 GeV Higgs** within the **N2HDM**
  - $pp \rightarrow \phi_{96} \rightarrow \gamma\gamma$  excess at CMS, not excluded by ATLAS
  - $e^+e^- \rightarrow Z \phi_{96} \rightarrow Z b\bar{b}$  excess at LEP
  - **$\phi_{96}$  can be produced at the ILC abundantly**
  - coupling measurements can distinguish various BSM solutions



Further Questions?

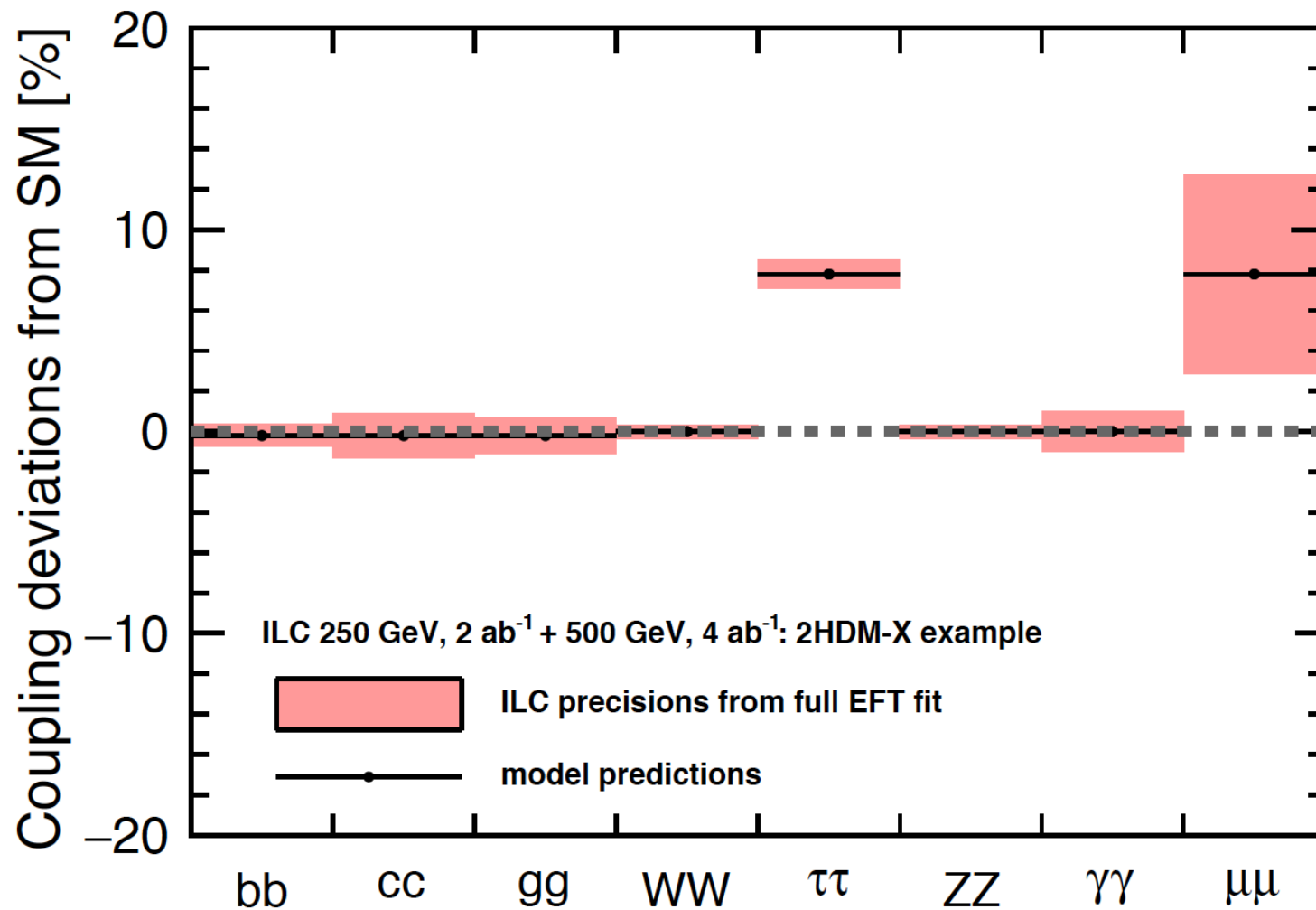
## BSM Wäscheleine I: ILC precision vs. 2HDM type II prediction:

[*T. Barklow et al., '17*]



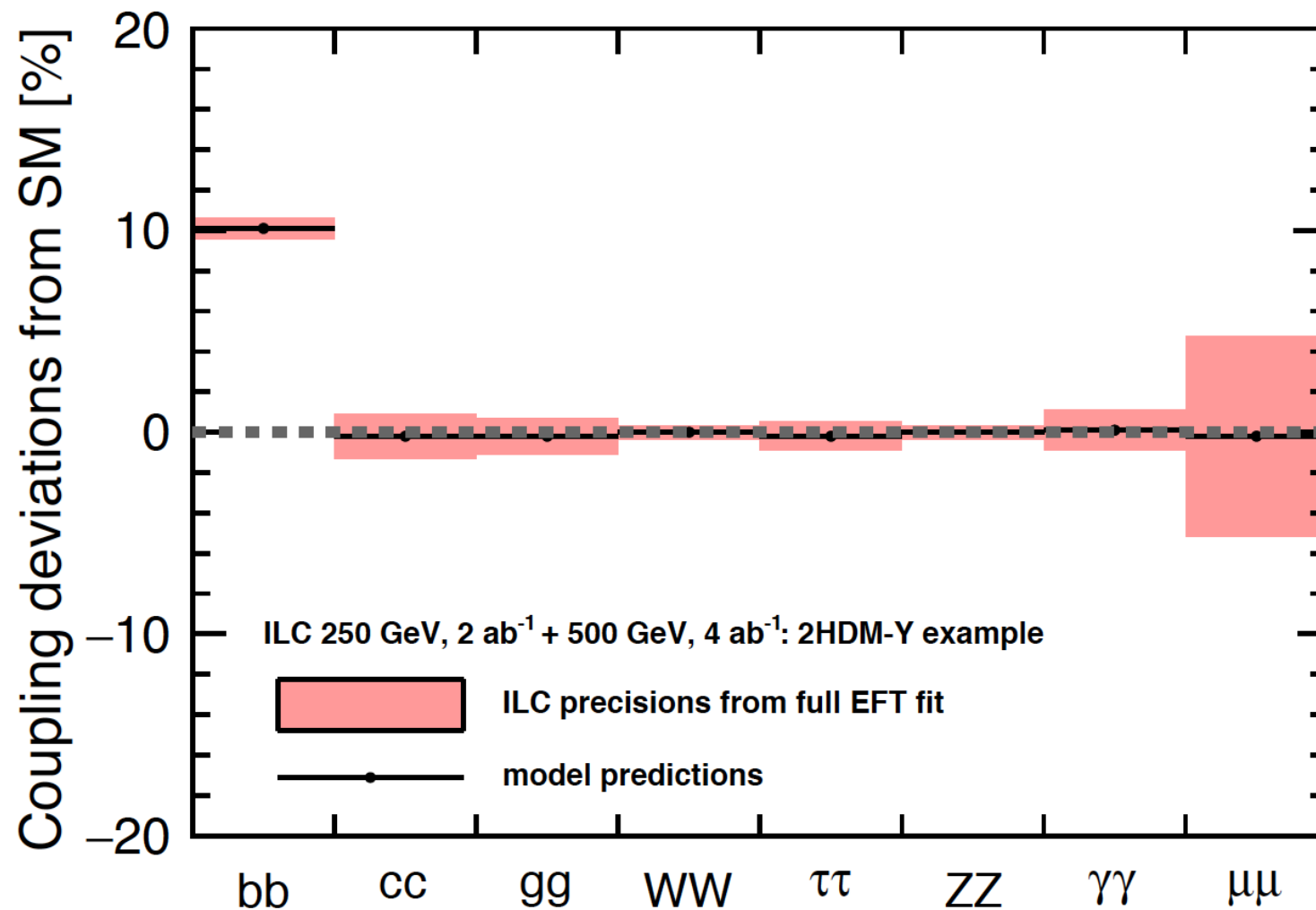
## BSM Wäscheleine II: ILC precision vs. 2HDM type X prediction:

[*T. Barklow et al., '17*]



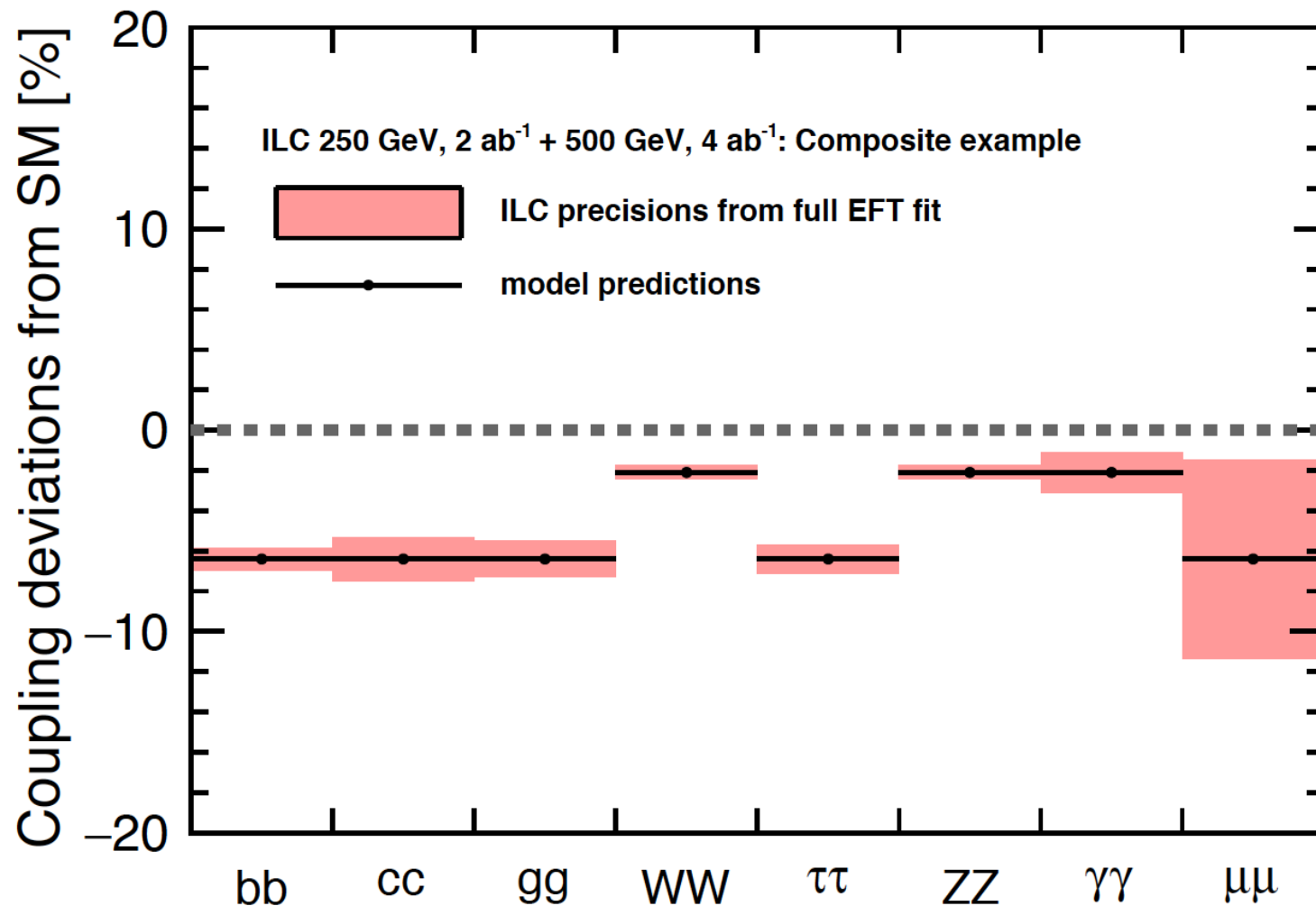
## BSM Wäscheleine III: ILC precision vs. 2HDM type Y prediction:

[*T. Barklow et al., '17*]



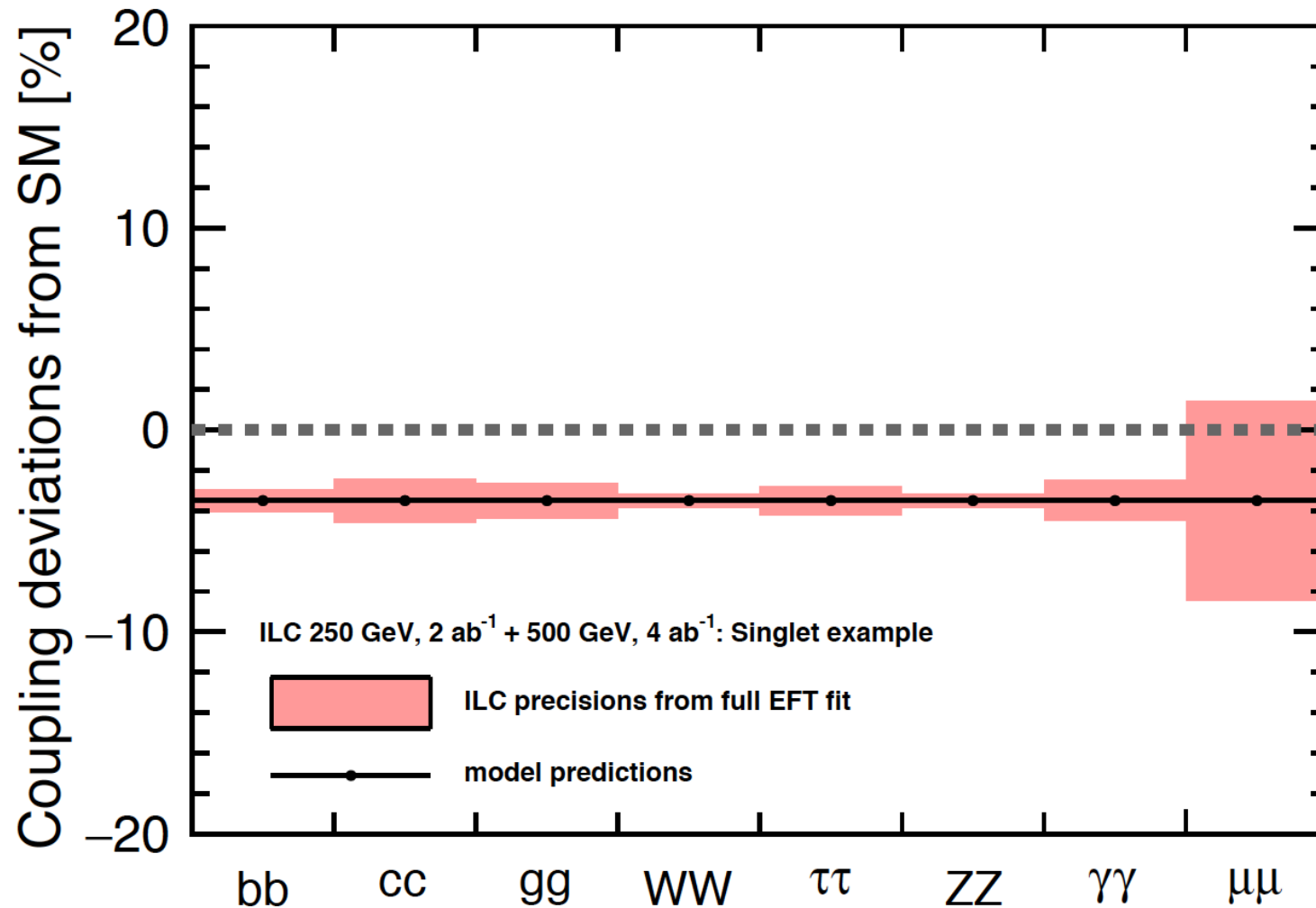
## BSM Wäscheleine IV: ILC precision vs. Composite Higgs prediction:

[*T. Barklow et al., '17*]



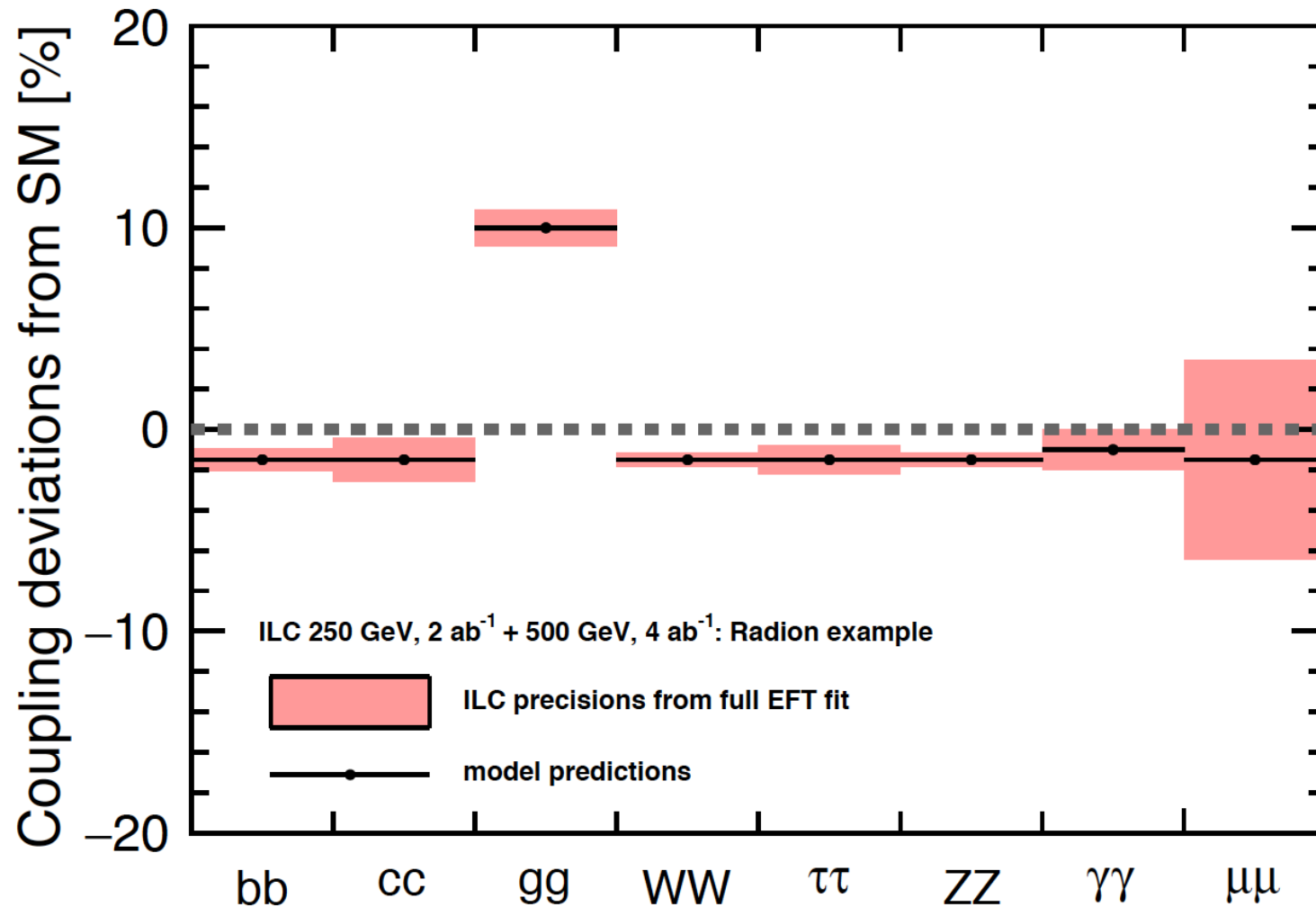
## BSM Wäscheleine V: ILC precision vs. HxSM prediction:

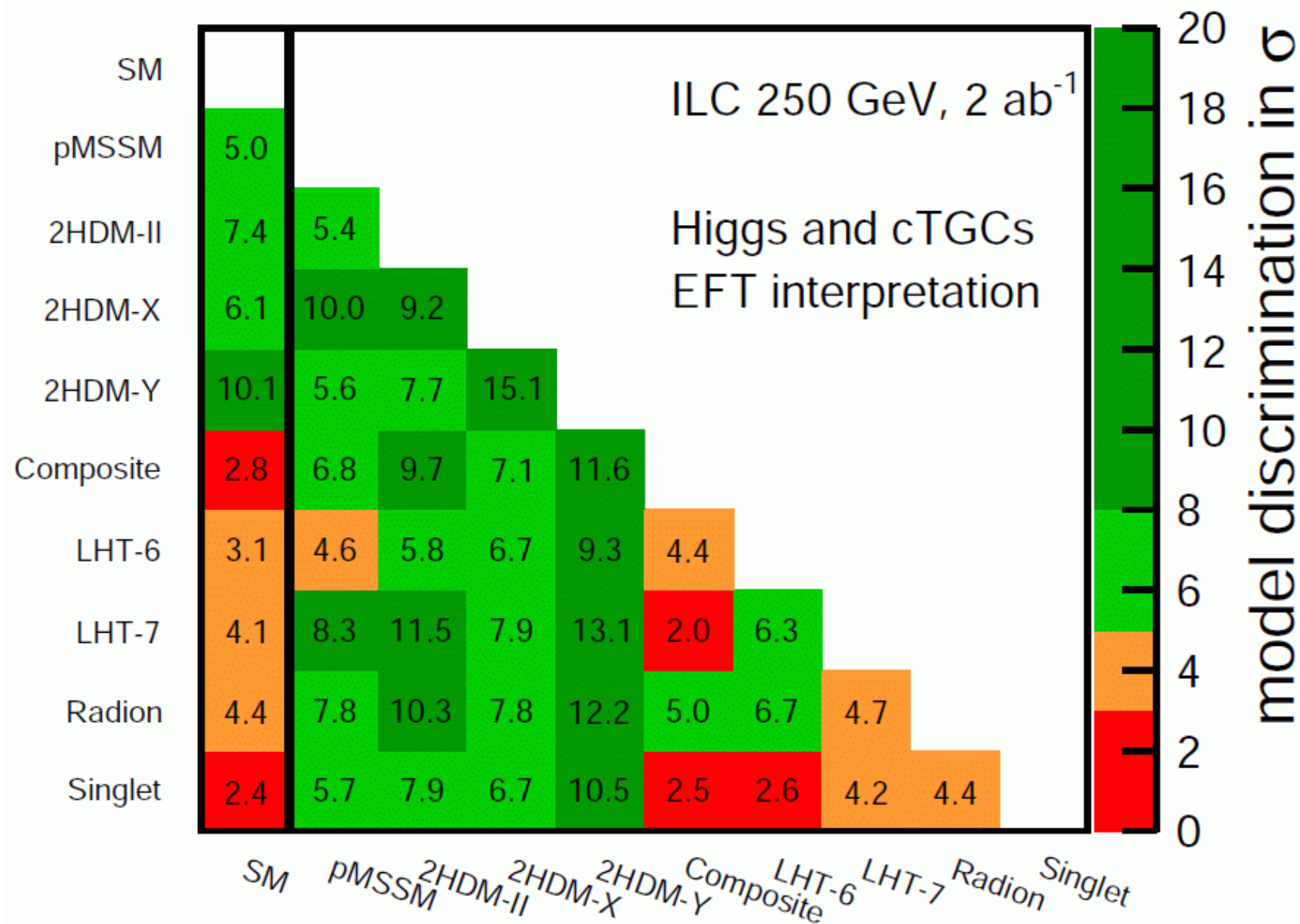
[*T. Barklow et al., '17*]

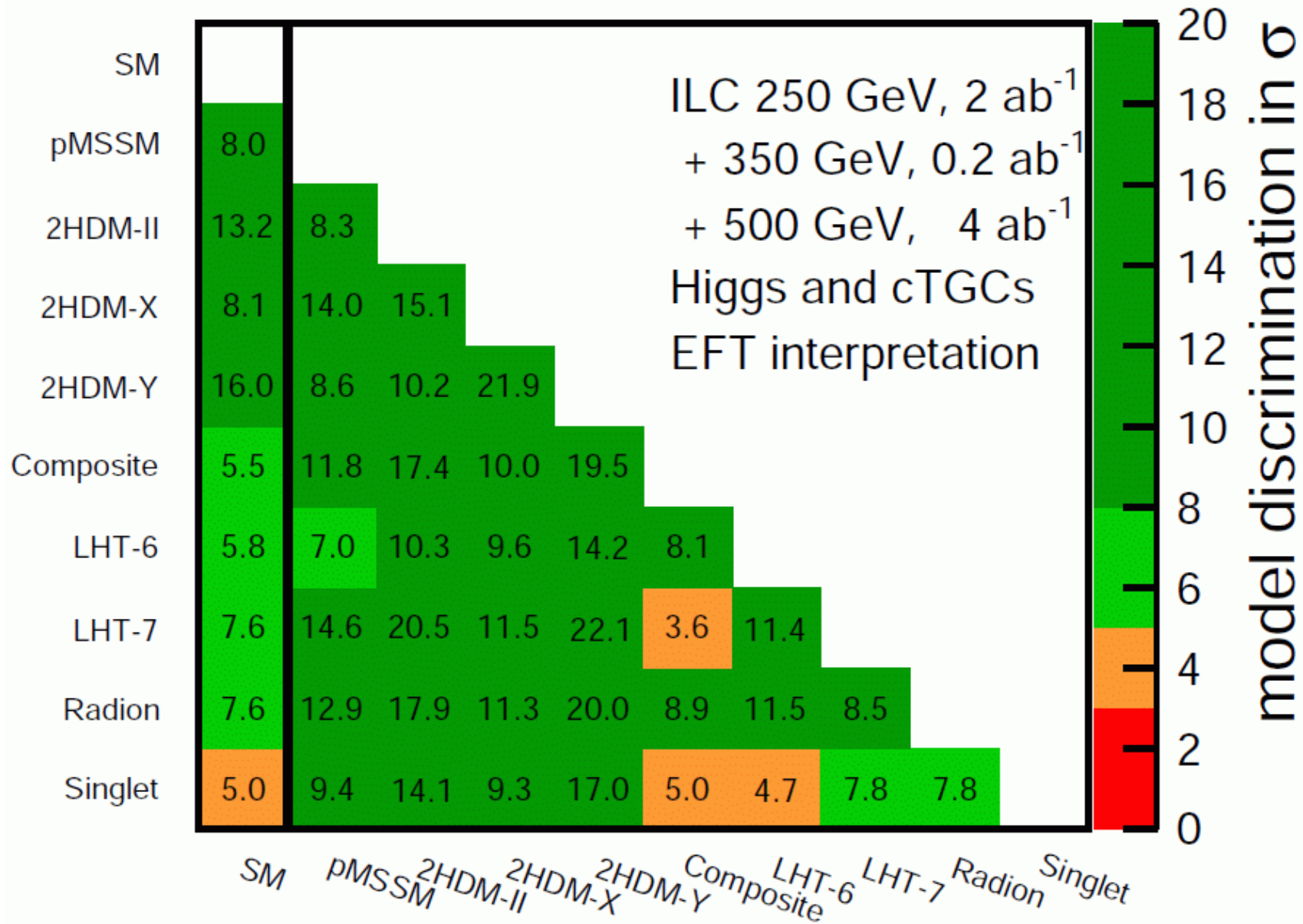


## BSM Wäscheleine VI: ILC precision vs. Higgs-Radion prediction:

[*T. Barklow et al., '17*]







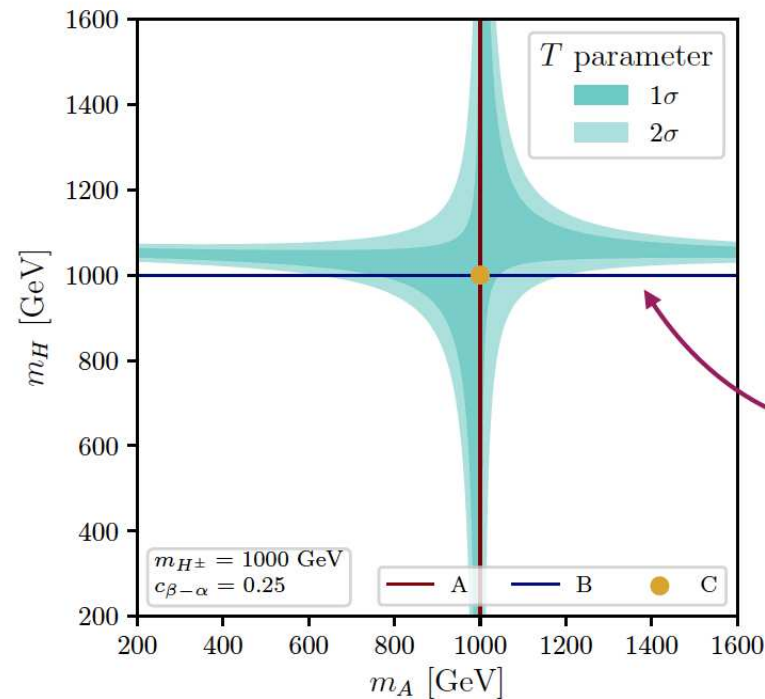
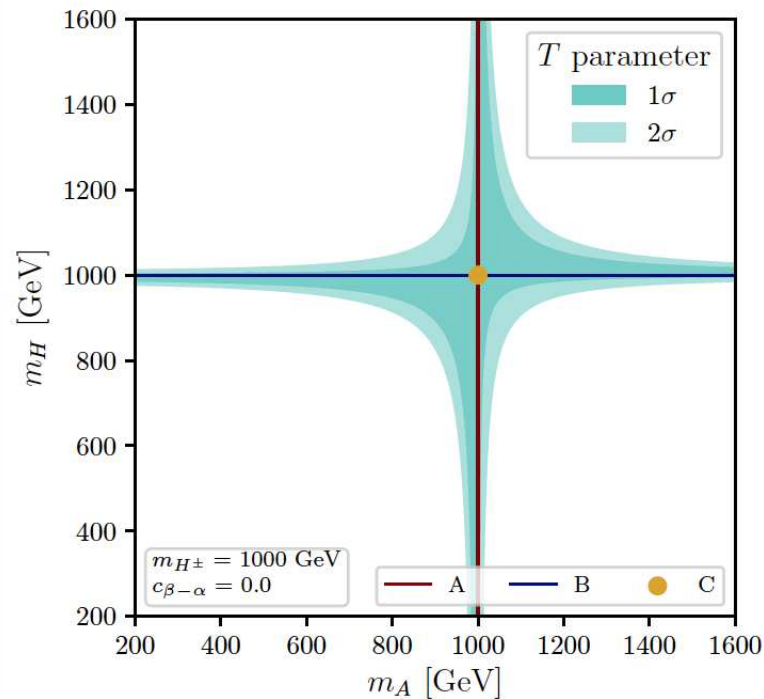
## $T$ parameter

$T$  is sensitive to the mass splitting of the Higgs bosons  $\Rightarrow$  3 simplified scenarios!

Scenario A:  $m_A = m_{H^\pm}$

Scenario B:  $m_H = m_{H^\pm}$

Scenario C:  $m_H = m_A = m_{H^\pm}$



Scenario B may be in conflict with data outside the alignment limit

Predictions of  $T$  obtained with 2HDMC [[arXiv:0902.0851](https://arxiv.org/abs/0902.0851)]

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$\Rightarrow$  definition of Scenario A, B, C

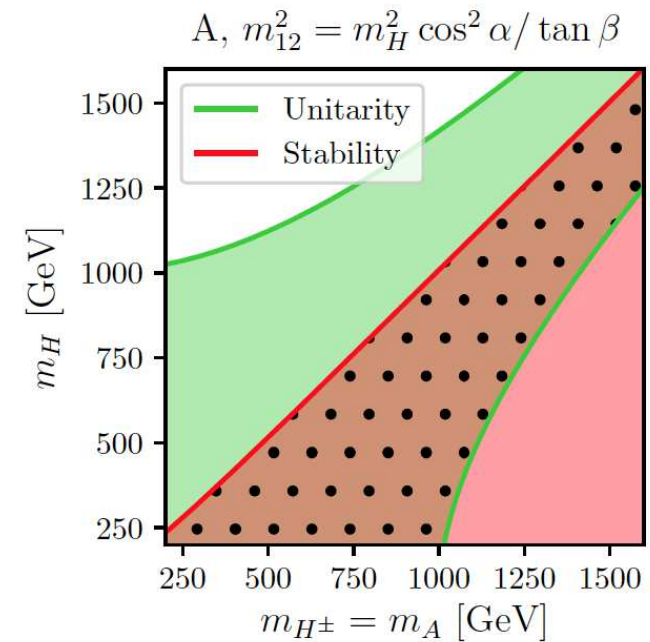
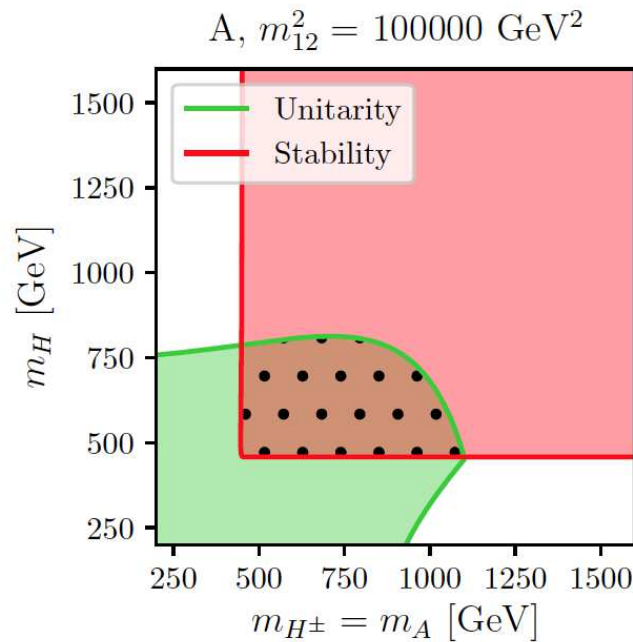
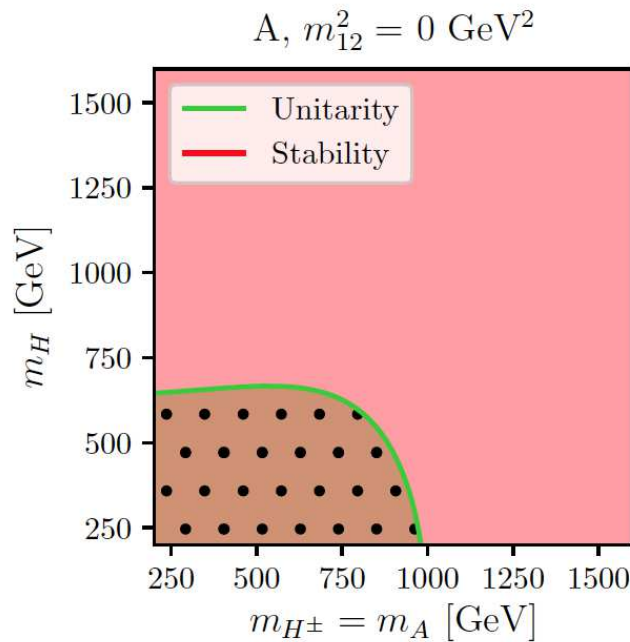
$\Rightarrow$  Once  $T$  is satisfied, also  $S$  and  $U$  are satisfied

# Unitarity + Stability

$$\tan \beta = 1.5$$

$$c_{\beta-\alpha} = 0$$

*dotted region are  
allowed regions*



★  $m_{12}^2$  controls the overlapping region between unitarity and stability

★  $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$  enlarges the allowed region!

*Similar for  
scenario B... 12*

⇒ special condition for  $m_{12}^2$  helps

## SUSY realizations

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- $\mu\nu$ SSM
- ...

## SUSY realizations

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- NMSSM
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- ...

**Q:** Can the models fit the excesses **despite** the additional SUSY constraints on the Higgs sector **???**

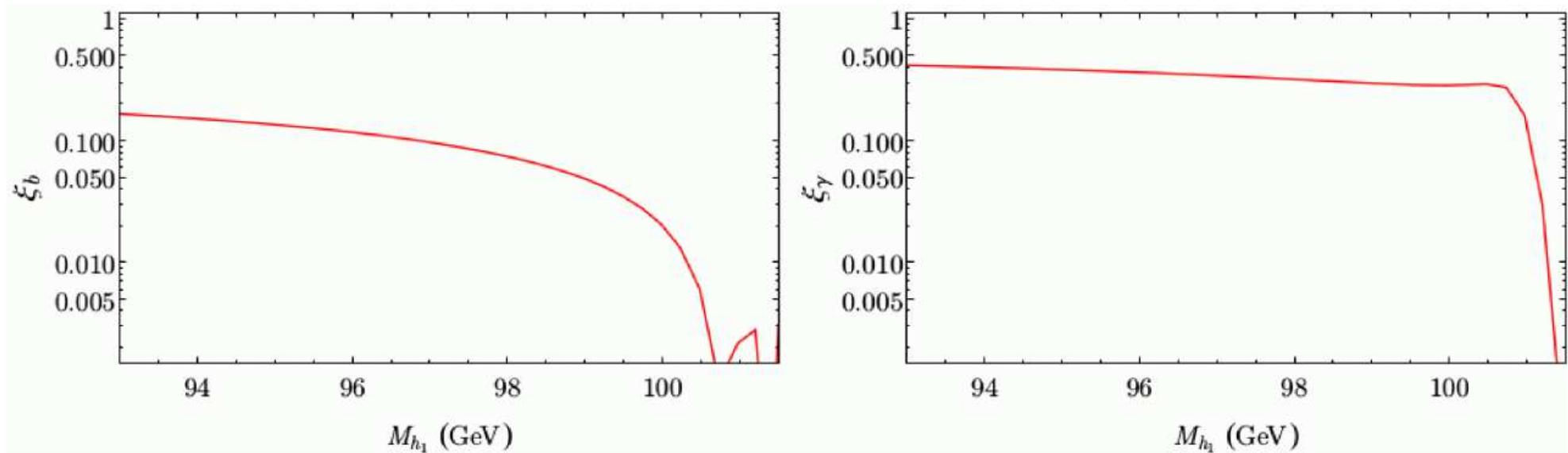
## What about the NMSSM?

[F. Domingo, S.H., S. Passehr, G. Weiglein '18]

### Parameters:

$\lambda = 0.6$ ,  $\kappa = 0.035$ ,  $\tan \beta = 2$ ,  $\mu_{\text{eff}} = (397 + 15x)$  GeV,  $M_{H^\pm} = 1$  TeV,  $A_\kappa = -325$  GeV,  $M_{\text{SUSY}} = 1$  TeV,  $A_t = A_b = 0$

$$\xi_b \equiv \frac{\Gamma[h_1 \rightarrow ZZ] \cdot \text{BR}[h_1 \rightarrow b\bar{b}]}{\Gamma[H_{\text{SM}}(M_{h_1}) \rightarrow ZZ] \cdot \text{BR}[H_{\text{SM}}(M_{h_1}) \rightarrow b\bar{b}]} \sim \frac{\sigma[e^+e^- \rightarrow Z(h_1 \rightarrow b\bar{b})]}{\sigma[e^+e^- \rightarrow Z(H_{\text{SM}}(M_{h_1}) \rightarrow b\bar{b})]}$$
$$\xi_\gamma \equiv \frac{\Gamma[h_1 \rightarrow gg] \cdot \text{BR}[h_1 \rightarrow \gamma\gamma]}{\Gamma[H_{\text{SM}}(M_{h_1}) \rightarrow gg] \cdot \text{BR}[H_{\text{SM}}(M_{h_1}) \rightarrow \gamma\gamma]} \sim \frac{\sigma[gg \rightarrow h_1 \rightarrow \gamma\gamma]}{\sigma[gg \rightarrow H_{\text{SM}}(M_{h_1}) \rightarrow \gamma\gamma]}.$$



⇒ both excesses can be fitted simultaneously (at  $1 - 1.5 \sigma$ )!

## What about the $\mu\nu$ SSM?

$\mu\nu$ SSM: [D. Lopez-Fogliani, C. Muñoz '06]

$\mu\nu$ SSM: NMSSM + well motivated RPV (in simple terms)  
 $\Rightarrow$  EW scale seesaw to reproduce the neutrino data

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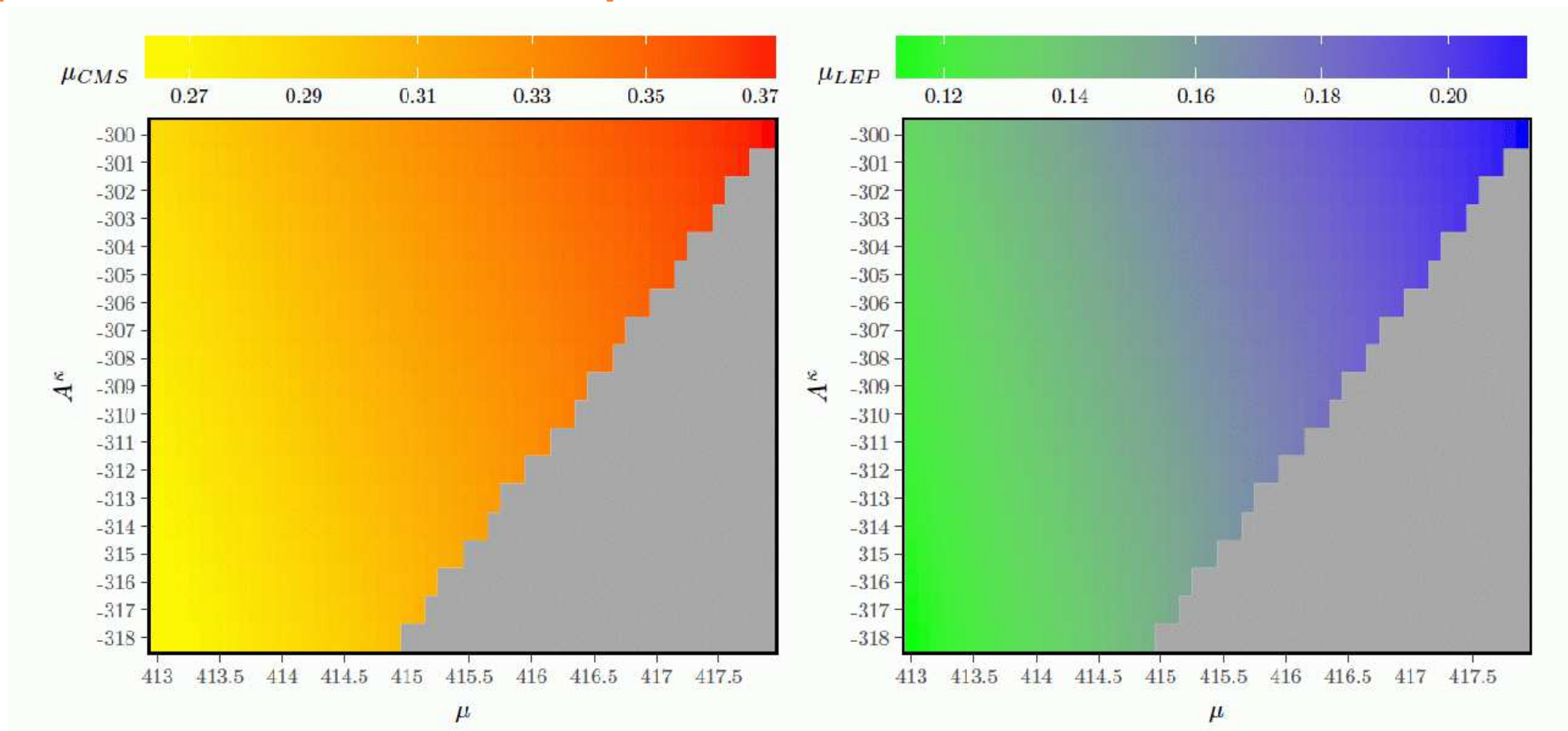
Can the  $\mu\nu$ SSM explain the two excesses?

[T. Biekötter, S.H., C. Muñoz '17]

| $v_{iL}$                 | $Y_i^\nu$ | $A_i^\nu$              | $\tan\beta$            | $\mu$                  | $\lambda$ | $A^\lambda$     | $\kappa$       | $A^\kappa$   | $M_1$         |
|--------------------------|-----------|------------------------|------------------------|------------------------|-----------|-----------------|----------------|--------------|---------------|
| $\sqrt{2} \cdot 10^{-5}$ | $10^{-7}$ | -1000                  | 2                      | [413; 418]             | 0.6       | 956.035         | 0.035          | [-300; -318] | 100           |
| $M_2$                    | $M_3$     | $m_{\tilde{Q}_{iL}}^2$ | $m_{\tilde{u}_{iR}}^2$ | $m_{\tilde{d}_{iR}}^2$ | $A_1^u$   | $A_{2,3}^{u,d}$ | $(m_e^2)_{ii}$ | $A_{33}^e$   | $A_{11,22}^e$ |
| 200                      | 1500      | $800^2$                | $800^2$                | $800^2$                | 0         | 0               | $800^2$        | 0            | 0             |

# Can the $\mu\nu$ SSM explain the two excesses?

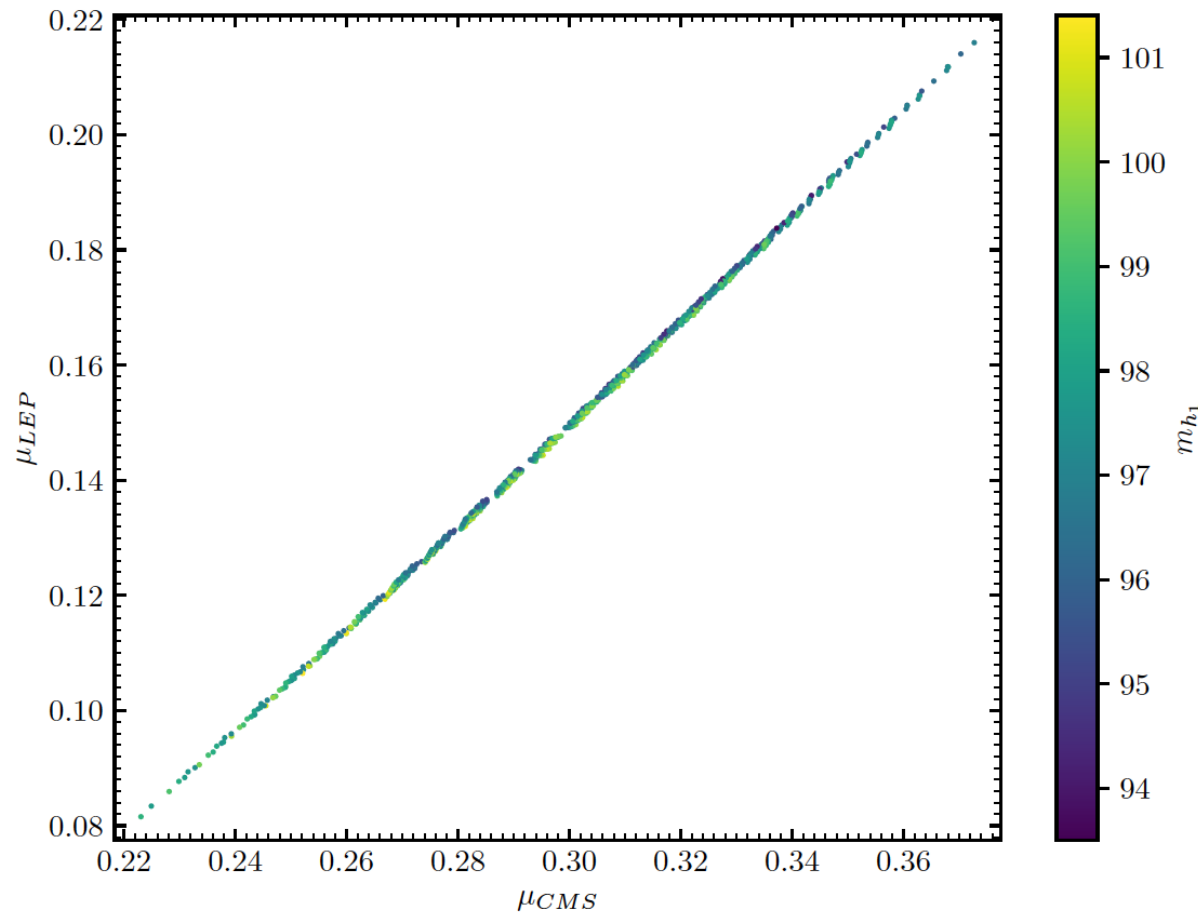
[*T. Biekötter, S.H., C. Muñoz '17*]



⇒ YES, WE CAN! :-)  
at the  $1 - 1.5\sigma$  level

## Why can SUSY explain the excesses only at $1 - 1.5 \sigma$ ?

[*T. Biekötter, S.H., C. Muñoz '19*]



⇒ SUSY enforces strong correlation!

⇒ note: ATLAS limits and CMS “observation”  
will likely result in a lower  $\mu_{LHC}$ !

Fitting the excesses:

$$\mu_{\text{LEP}} = 0.117 \pm 0.057, \quad \mu_{\text{CMS}} = 0.6 \pm 0.2$$

$$\begin{aligned}\mu_{\text{LEP}} &= \frac{\sigma_{\text{N2HDM}}(e^+e^- \rightarrow Zh_1)}{\sigma_{\text{SM}}(e^+e^- \rightarrow ZH)} \cdot \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow b\bar{b})}{\text{BR}_{\text{SM}}(H \rightarrow b\bar{b})} \\ &= |c_{h_1VV}|^2 \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow b\bar{b})}{\text{BR}_{\text{SM}}(H \rightarrow b\bar{b})}\end{aligned}$$

$$\begin{aligned}\mu_{\text{CMS}} &= \frac{\sigma_{\text{N2HDM}}(gg \rightarrow h_1)}{\sigma_{\text{SM}}(gg \rightarrow H)} \cdot \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow \gamma\gamma)}{\text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma)} \\ &= |c_{h_1tt}|^2 \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow \gamma\gamma)}{\text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma)}\end{aligned}$$

$$\chi_{\text{CMS-LEP}}^2 = \frac{(\mu_{\text{LEP}} - 0.117)^2}{(0.057)^2} + \frac{(\mu_{\text{CMS}} - 0.6)^2}{(0.2)^2}$$

⇒ “best-fit point”

Needed to fit the two excesses:  $m_{h_1} \sim 96 \text{ GeV}$ ,  $m_{h_2} \sim 125 \text{ GeV}$

- $c_{h_1 VV}^2$  strongly reduced for  $\mu_{\text{LEP}}$
- $c_{h_1 bb}$  reduced to enhance  $\text{BR}(h_1 \rightarrow \gamma\gamma)$
- $c_{h_1 tt}$  not reduced for  $\mu_{\text{CMS}}$
- $c_{h_1 \tau\tau}$  possibly reduced to enhance  $\text{BR}(h_1 \rightarrow \gamma\gamma)$

|          | Decrease $c_{h_1 b\bar{b}}$    | No decrease $c_{h_1 t\bar{t}}$            | No enhancement $c_{h_1 \tau\bar{\tau}}$   |
|----------|--------------------------------|-------------------------------------------|-------------------------------------------|
| type I   | $(\frac{R_{12}}{s_\beta}) :-)$ | $(\frac{R_{12}}{s_\beta}) :-(\text{red})$ | $(\frac{R_{12}}{s_\beta}) :-)$            |
| type II  | $(\frac{R_{11}}{c_\beta}) :-)$ | $(\frac{R_{12}}{s_\beta}) :-)$            | $(\frac{R_{11}}{c_\beta}) :-)$            |
| type III | $(\frac{R_{12}}{s_\beta}) :-)$ | $(\frac{R_{12}}{s_\beta}) :-(\text{red})$ | $(\frac{R_{11}}{c_\beta}) :-(\text{red})$ |
| type IV  | $(\frac{R_{11}}{c_\beta}) :-)$ | $(\frac{R_{12}}{s_\beta}) :-)$            | $(\frac{R_{12}}{s_\beta}) :-(\text{red})$ |

**Type II and IV:**  $c_{h_1 bb}$  and  $c_{h_1 tt}$  independent

**Type II bonus:**  $c_{h_1 \tau\tau}$  can be suppressed (together with  $c_{h_1 bb}$ )

$\Rightarrow$  only type II and IV can fit CMS and LEP excesses

## Best-fit point in type II:

| $m_{h_1}$              | $m_{h_2}$              | $m_{h_3}$                    | $m_A$                            | $M_{H^\pm}$            |                        |  |
|------------------------|------------------------|------------------------------|----------------------------------|------------------------|------------------------|--|
| 96.5263                | 125.09                 | 535.86                       | 712.578                          | 737.829                |                        |  |
| $\tan \beta$           | $\alpha_1$             | $\alpha_2$                   | $\alpha_3$                       | $m_{12}^2$             | $v_S$                  |  |
| 1.26287                | 1.26878                | -1.08484                     | -1.24108                         | 80644.3                | 272.72                 |  |
| $\text{BR}_{h_1}^{bb}$ | $\text{BR}_{h_1}^{gg}$ | $\text{BR}_{h_1}^{\tau\tau}$ | $\text{BR}_{h_1}^{\gamma\gamma}$ | $\text{BR}_{h_1}^{WW}$ | $\text{BR}_{h_1}^{ZZ}$ |  |
| 0.5048                 | 0.2682                 | $5.09 \cdot 10^{-2}$         | $2.582 \cdot 10^{-3}$            | $1.37 \cdot 10^{-2}$   | $1.753 \cdot 10^{-3}$  |  |
| $\text{BR}_{h_2}^{bb}$ | $\text{BR}_{h_2}^{gg}$ | $\text{BR}_{h_2}^{\tau\tau}$ | $\text{BR}_{h_2}^{\gamma\gamma}$ | $\text{BR}_{h_2}^{WW}$ | $\text{BR}_{h_2}^{ZZ}$ |  |
| 0.5916                 | 0.0771                 | $6.36 \cdot 10^{-2}$         | $2.153 \cdot 10^{-3}$            | 0.2087                 | $2.610 \cdot 10^{-3}$  |  |

⇒ surprisingly large  $\text{BR}_{h_1}^{\gamma\gamma}$

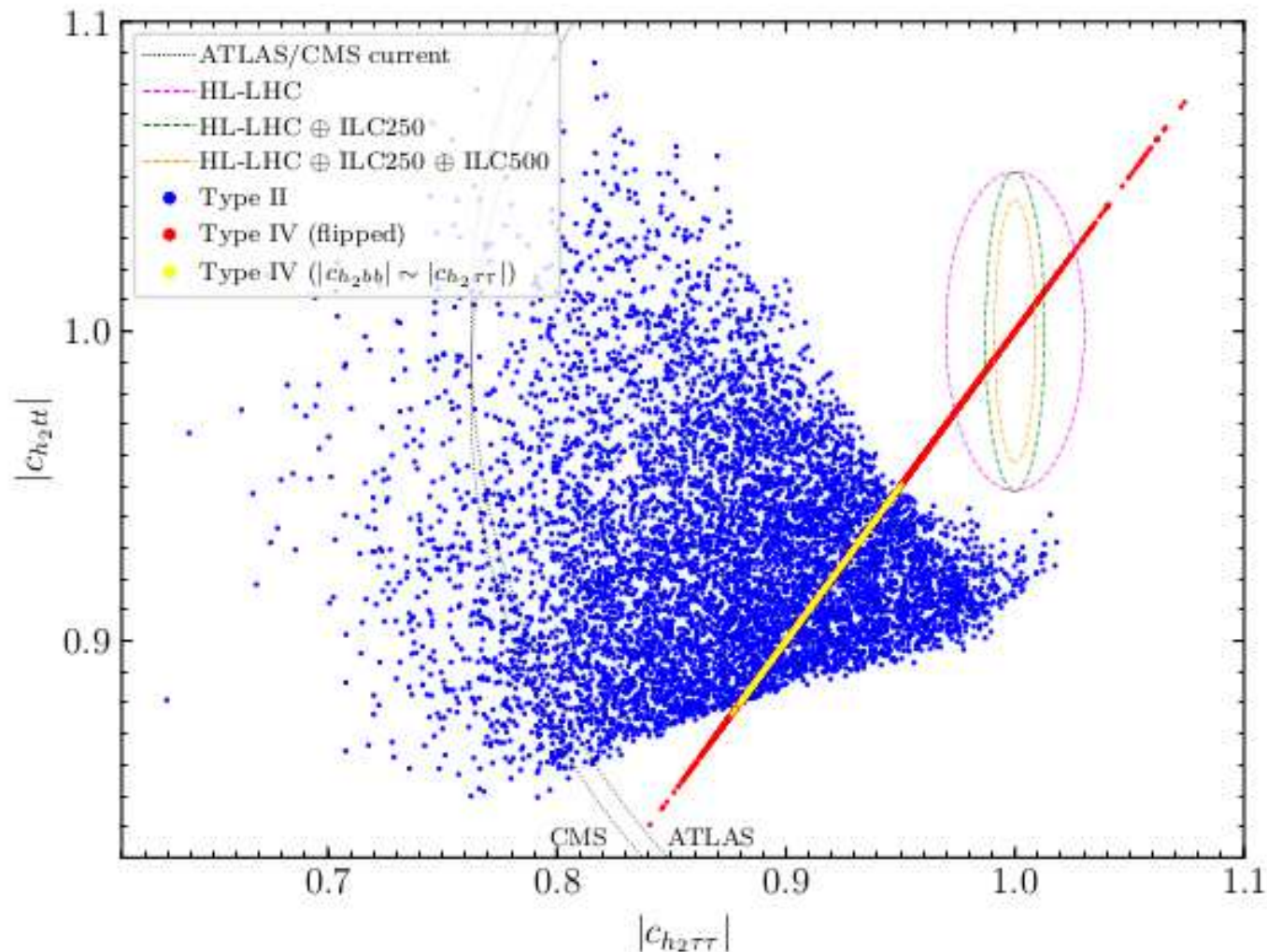
## Best-fit point in type IV:

| $m_{h_1}$              | $m_{h_2}$              | $m_{h_3}$                    | $m_A$                            | $M_{H^\pm}$            |                        |
|------------------------|------------------------|------------------------------|----------------------------------|------------------------|------------------------|
| 97.8128                | 125.09                 | 485.998                      | 651.502                          | 651.26                 |                        |
| $\tan \beta$           | $\alpha_1$             | $\alpha_2$                   | $\alpha_3$                       | $m_{12}^2$             | $v_S$                  |
| 1.3147                 | 1.27039                | -1.02829                     | -1.32496                         | 41034.1                | 647.886                |
| $\text{BR}_{h_1}^{bb}$ | $\text{BR}_{h_1}^{gg}$ | $\text{BR}_{h_1}^{\tau\tau}$ | $\text{BR}_{h_1}^{\gamma\gamma}$ | $\text{BR}_{h_1}^{WW}$ | $\text{BR}_{h_1}^{ZZ}$ |
| 0.4074                 | 0.20714                | 0.248324                     | $2.139 \cdot 10^{-3}$            | $1.347 \cdot 10^{-2}$  | $1.579 \cdot 10^{-3}$  |
| $\text{BR}_{h_2}^{bb}$ | $\text{BR}_{h_2}^{gg}$ | $\text{BR}_{h_2}^{\tau\tau}$ | $\text{BR}_{h_2}^{\gamma\gamma}$ | $\text{BR}_{h_2}^{WW}$ | $\text{BR}_{h_2}^{ZZ}$ |
| 0.5363                 | 0.09388                | $7.58 \cdot 10^{-2}$         | $2.247 \cdot 10^{-3}$            | 0.2267                 | $2.836 \cdot 10^{-2}$  |

⇒ substantially larger  $\text{BR}_{h_1}^{\tau\tau}$  than in type II

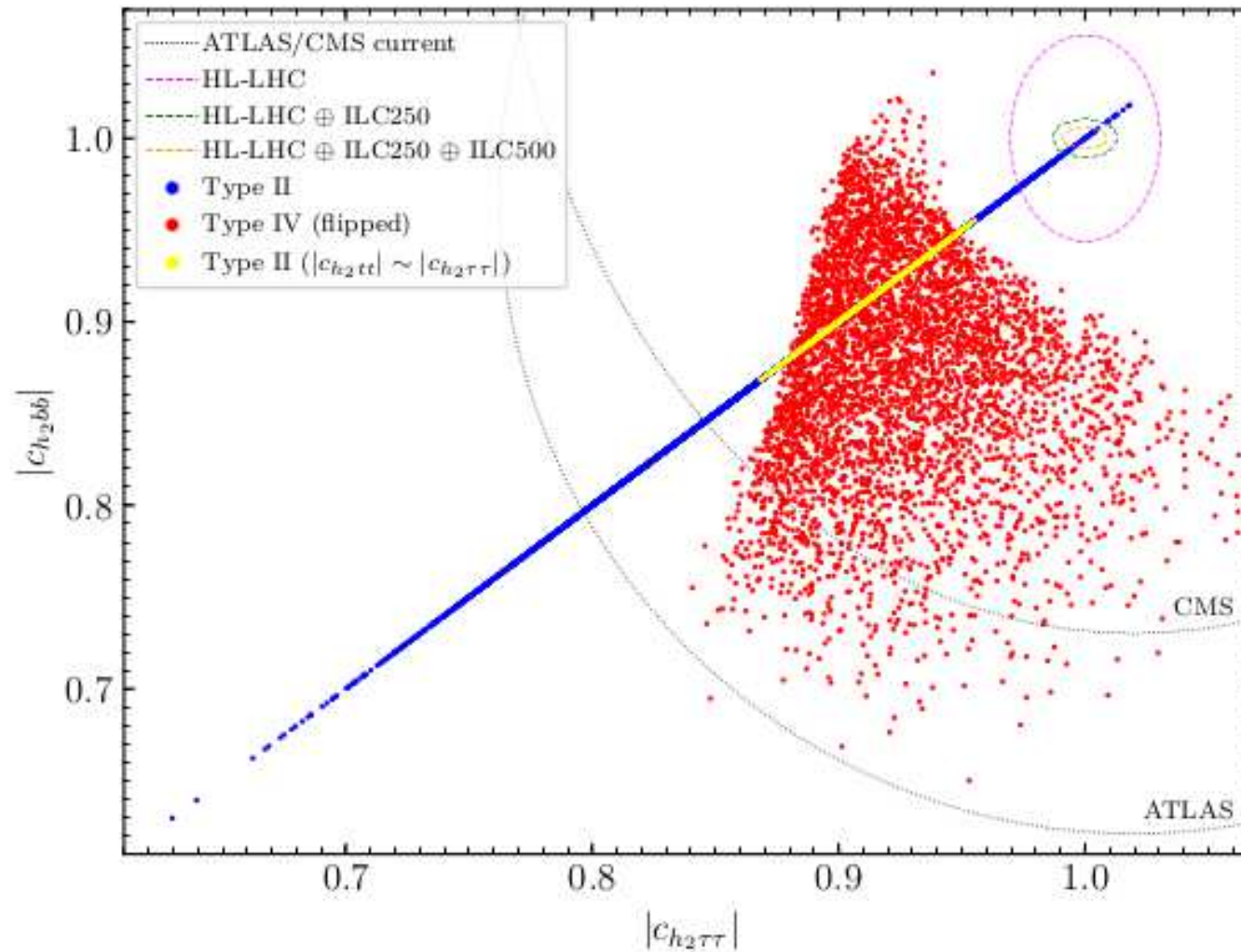
## Probes of the 125 GeV Higgs

Future measurements:  $\Rightarrow$  HL-LHC/ILC Higgs coupling measurements



$\Rightarrow$  type II shows deviation from SM

Future measurements:  $\Rightarrow$  HL-LHC/ILC Higgs coupling measurements



$\Rightarrow$  type IV shows deviations from SM

$\Rightarrow$  N2HDM can always be distinguished from SM!

## How to evaluate the precision of $\phi_{96}$ coupling measurements?

Start with **data of the SM Higgs**:

SM Higgs **BRs**:

[YR4 LHCHXSWG]

| final state | $b\bar{b}$ | $gg$  | $\tau^+\tau^-$ | $WW^*$ | $\sigma_{ZH}$ |
|-------------|------------|-------|----------------|--------|---------------|
| BR          | 0.582      | 0.082 | 0.063          | 0.214  | 206 fb        |

SM Higgs coupling **uncertainties**:

ILC,  $\mathcal{L}_{\text{int}} = 2 \text{ ab}^{-1}$  at  $\sqrt{s} = 250 \text{ GeV}$

[T. Barklow et al. '17]

| coupling      | $b\bar{b}$ | $gg$ | $\tau^+\tau^-$ | $WW$ | $ZZ$ |
|---------------|------------|------|----------------|------|------|
| rel. unc. [%] | 1.04       | 1.60 | 1.16           | 0.65 | 0.66 |

SM Higgs  **$S/B$** :

[S. Dawson et al. '13] [J. Tian, priv. commun.]

| coupling | $H \rightarrow b\bar{b}$ | $H \rightarrow gg$ | $H \rightarrow \tau^+\tau^-$ | $H \rightarrow WW$ | $\sigma_{ZH}$ |
|----------|--------------------------|--------------------|------------------------------|--------------------|---------------|
| $S/B$    | 1/0.89                   | 1/13               | 1/0.44                       | 1/0.96             | 1/1.65        |

## Some more basics:

$$f := S/B \equiv N_S/N_B$$

$$\frac{\Delta N_S}{N_S} = \frac{1}{\sqrt{N_S}} \sqrt{1 + 1/f}$$

Holds if background is known perfectly and the overall uncertainty is dominated by statistical precision

Uncertainty improves with  $1/\sqrt{N_S}$  for  $f = S/B \gg 1$

## Cross section for $\phi_{96}$ :

$$\sigma(e^+e^- \rightarrow \phi Z) = \sigma_{\text{SM}}(e^+e^- \rightarrow Z H_{\text{SM}}^{\phi_{96}}) \times |c_{\phi VV}|^2$$

$$\sigma_{\text{SM}}(e^+e^- \rightarrow Z H_{\text{SM}}^{\phi_{96}}) = 0.332 \text{ pb}$$

$\Rightarrow \mathcal{O}(10^5)$   $\phi$ 's can be produced at  $\sqrt{s} = 250 \text{ GeV}$  and  $\mathcal{L}_{\text{int}} = 2 \text{ ab}^{-1}$

## Evaluating uncertainties:

- Coupling is measured via decay

A new Higgs boson  $\phi$  couples with  $g_x$  to  $xx$

$$\Gamma(\phi \rightarrow xx) \propto g_x^2$$

$$\text{BR}(\phi \rightarrow xx) =: 1/p$$

$$\frac{\Delta N_S}{N_S} = 2 \frac{\Delta g_x}{g_x} \left(1 - \frac{1}{p}\right)$$

- Coupling is measured via production:  $g_Z$

$$\sigma(e^+e^- \rightarrow Z\phi) \propto g_Z^2$$

$$\frac{\Delta N_S}{N_S} = 2 \frac{\Delta g_x}{g_x}$$

- Final assumption:  $\left(\frac{N_S}{N_B}\right)_H / \left(\frac{N_S}{N_B}\right)_\phi = f_H/f_\phi =: D$

with  $D = 2$  as starting point

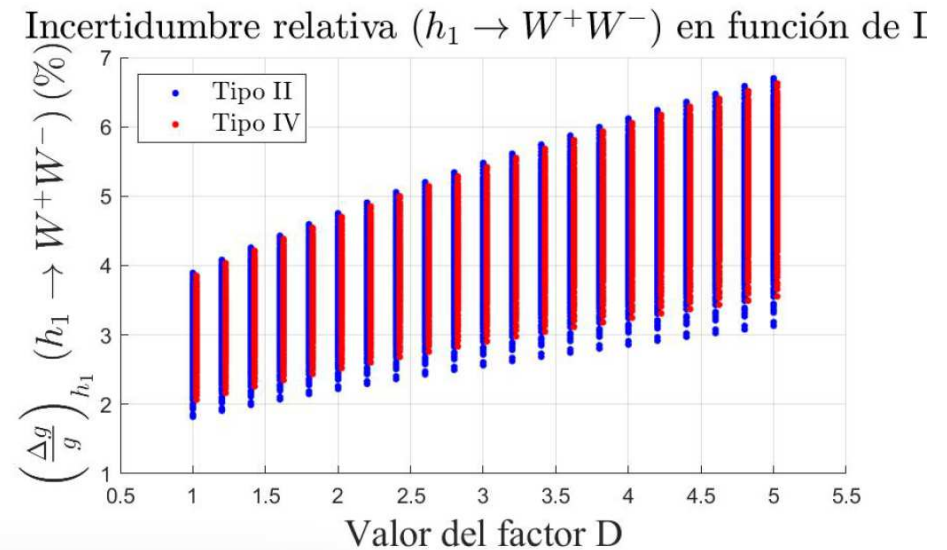
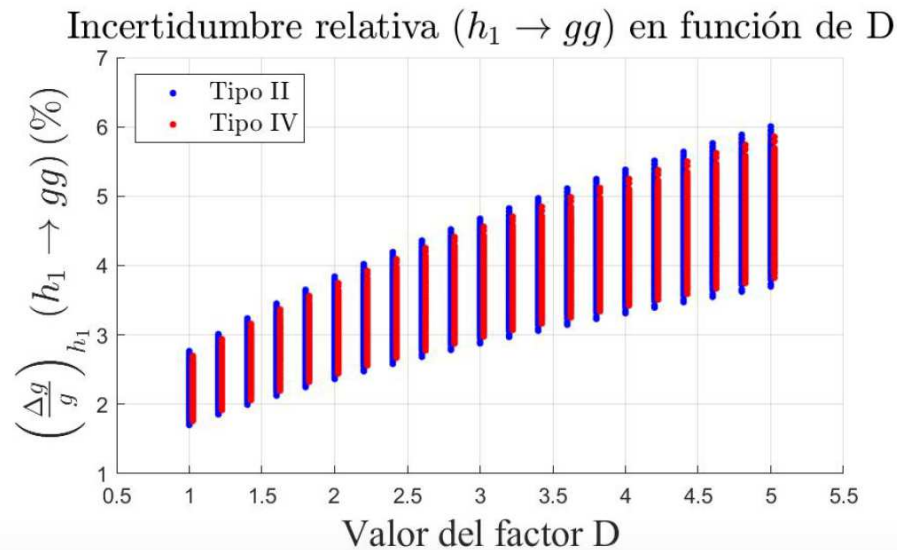
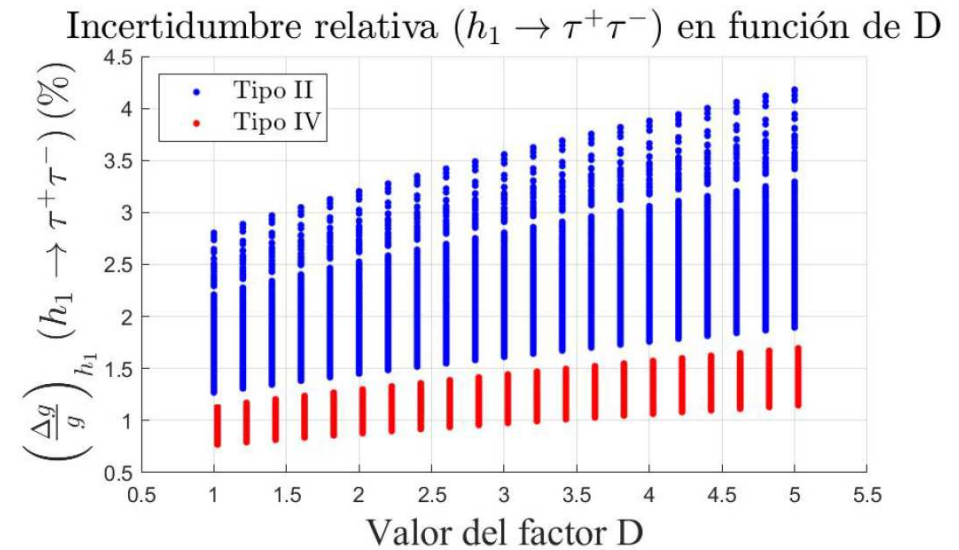
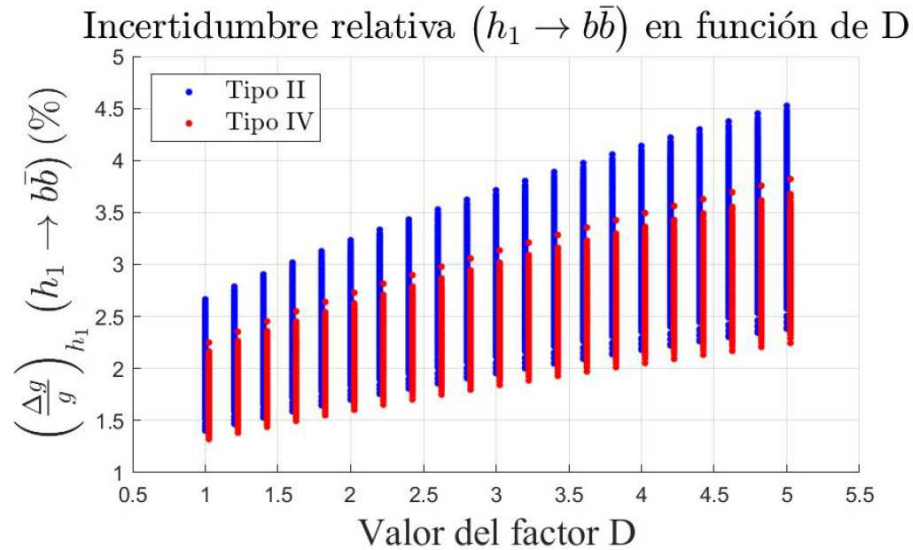
## Evaluating uncertainties of $\phi_{96}$ :

- Coupling is measured via decay

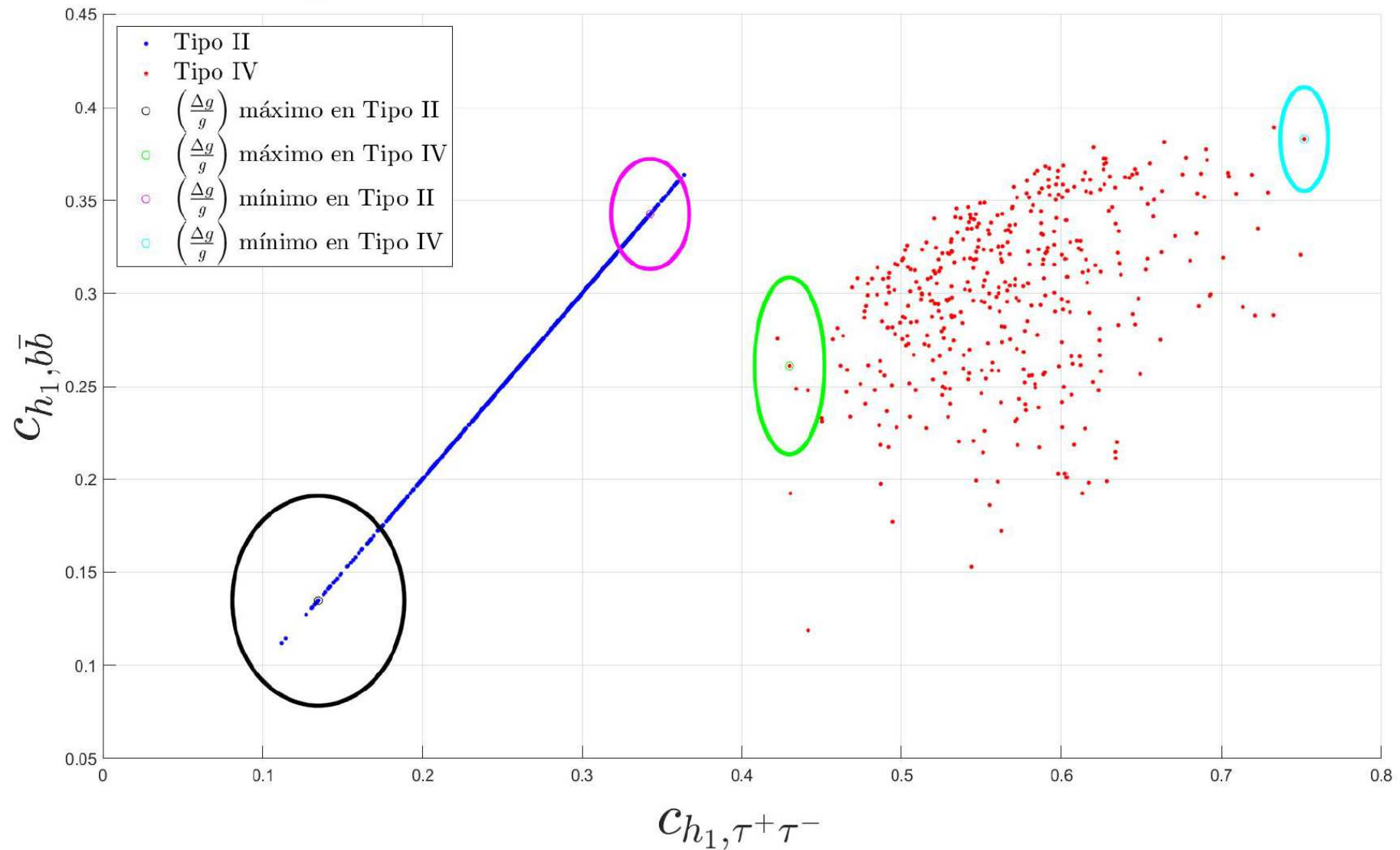
$$\begin{aligned} \left( \frac{\Delta g_x}{g_x} \right)_\phi &= \left( \frac{\Delta g_x}{g_x} \right)_H \times \frac{\left( \frac{\Delta N_S}{N_S} \right)_\phi}{\left( \frac{\Delta N_S}{N_S} \right)_H} \times \frac{\left( 1 - \frac{1}{p_H} \right)}{\left( 1 - \frac{1}{p_\phi} \right)} \\ &\rightarrow \sqrt{\frac{D + f_H}{1 + f_H}} \times \sqrt{\frac{\sigma(e^+e^- \rightarrow ZH)}{\sigma(e^+e^- \rightarrow Z\phi)}} \times \sqrt{\frac{\text{BR}(H \rightarrow xx)}{\text{BR}(\phi \rightarrow xx)}} \times \frac{(1 - \text{BR}(H \rightarrow xx))}{(1 - \text{BR}(\phi \rightarrow xx))} \end{aligned}$$

- Coupling is measured via production:  $g_Z$  ( $S/B$  does not change)

$$\begin{aligned} \left( \frac{\Delta g_Z}{g_Z} \right)_\phi &= \left( \frac{\Delta g_Z}{g_Z} \right)_H \times \frac{\left( \frac{\Delta N_S}{N_S} \right)_\phi}{\left( \frac{\Delta N_S}{N_S} \right)_H} \\ &\rightarrow \sqrt{\frac{\sigma(e^+e^- \rightarrow ZH)}{\sigma(e^+e^- \rightarrow Z\phi)}} \end{aligned}$$



⇒ non-negligible, but small ⇒ “robust” result



⇒ model distinction possible via coupling measurements