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Searching new physics in B decays

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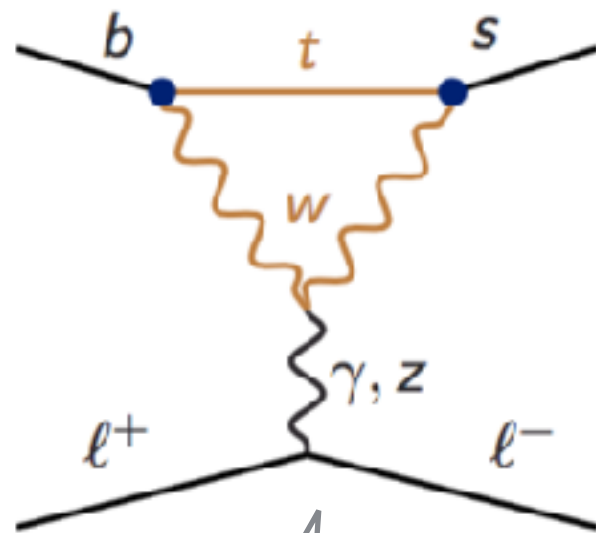


Outline

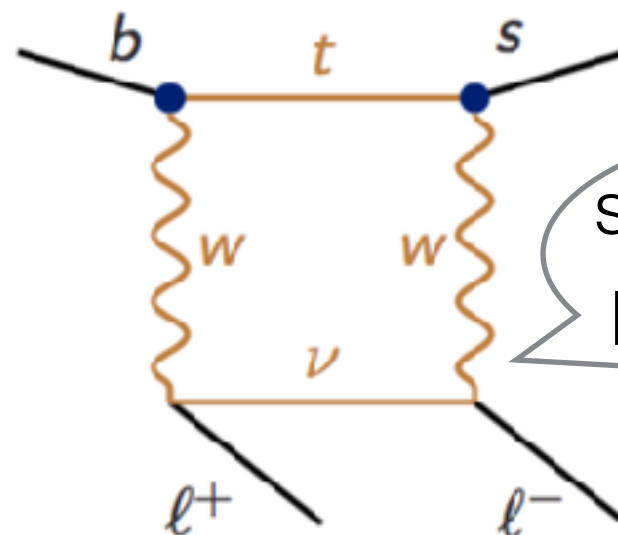
- Introduction
- Rare semileptonic mode $B \rightarrow K^* \ell^+ \ell^-$
 - ▶ Model independent framework
 - ▶ Evidence of new physics
- Lepton flavor non-universality
- Summary

Introduction

loop and CKM suppressed
SM amplitude



large no. of experimentally
accessible observables

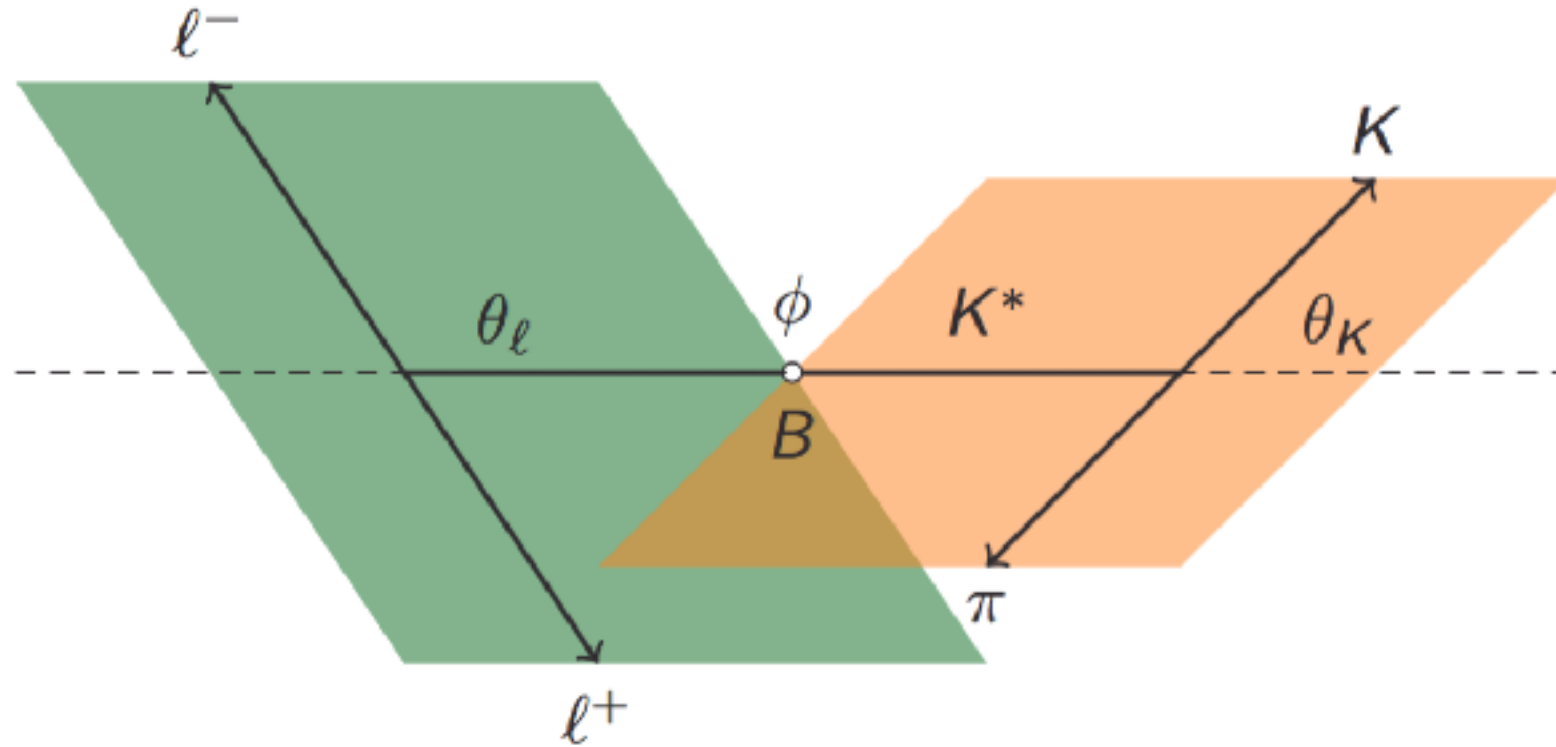


sensitive to new
particle in loop

valuable probe for indirect
search of NP

Introduction

Angular analysis in well known helicity frame [\[Kruger, Sehgal, Sinha, Sinha '99\]](#)



The differential distribution $\frac{d^4\Gamma(B \rightarrow K^* \ell^+ \ell^-)}{dq^2 d\cos\theta_l d\cos\theta_k d\phi}$

$$= \frac{9}{32\pi} \left[I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K + (I_2^s \sin^2 \theta_K + I_2^c \cos^2 \theta_K) \cos 2\theta_l + I_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \right. \\ \left. + I_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + I_5 \sin 2\theta_K \sin \theta_l \cos \phi + I_6^s \sin^2 \theta_K \cos \theta_l \right. \\ \left. + I_7 \sin 2\theta_K \sin \theta_l \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + I_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]$$

Motivation

► $I_i =$ short distance + long distance

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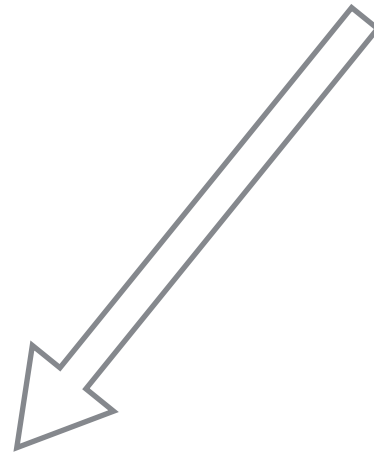
Wilson coefficients:
perturbatively calculable

Motivation

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Wilson coefficients:
perturbatively calculable



Form-factors:
non-perturbative estimates
from LCSR, HQET, Lattice ...
tremendous effort since past

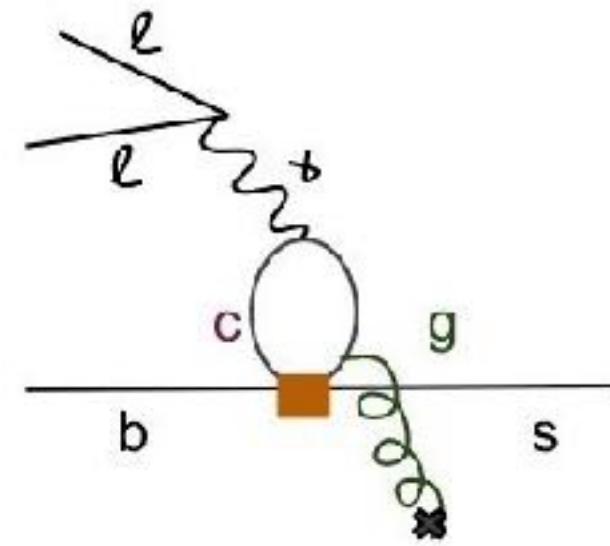
Motivation

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Wilson coefficients:
perturbatively calculable

Form-factors:
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Non-factorizable
contributions:



no quantitative computation

► Challenge: either estimate accurately or eliminate

Model Independent Framework

► The amplitude $\mathcal{A}(B(p) \rightarrow K^*(k)\ell^+\ell^-)$

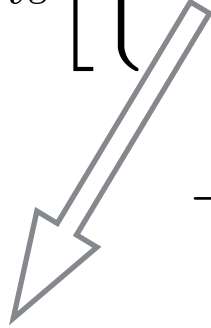
[RM, Sinha, Das '14]

$$= \frac{G_F \alpha}{\sqrt{2}\pi} V_{tb} V_{ts}^* \left[\left\{ C_9 \langle K^* | \bar{s} \gamma^\mu P_L b | \bar{B} \rangle - \frac{2C_7}{q^2} \langle K^* | \bar{s} i \sigma^{\mu\nu} q_\nu (m_b P_R + m_s P_L) b | \bar{B} \rangle \right. \right. \\ \left. \left. - \frac{16\pi^2}{q^2} \sum_{i=\{1-6,8\}} C_i \mathcal{H}_i^\mu \right\} \bar{\ell} \gamma_\mu \ell + C_{10} \langle K^* | \bar{s} \gamma^\mu P_L b | \bar{B} \rangle \bar{\ell} \gamma_\mu \gamma_5 \ell \right]$$

Model Independent Framework

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Wilson coefficients

lorentz & gauge invariance
allow general parametrization
with form-factors $\mathcal{X}_j, \mathcal{Y}_j$

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Wilson coefficients

non-local operator

for non factorization contributions

lorentz & gauge invariance
allow general parametrization
with form-factors $\mathcal{X}_j, \mathcal{Y}_j$

$$\mathcal{H}_i^\mu \sim \left\langle K^* | i \int d^4x e^{iq \cdot x} T \{ j_{em}^\mu(x), \mathcal{O}_i(0) \} | \bar{B} \right\rangle \Rightarrow \text{parametrize with 'new' form-factors } \mathcal{Z}_j^i$$

[Khodjamirian et. al '10]

Model Independent Framework

► Absorbing factorizable & non-factorizable contributions into

$$C_9 \longrightarrow \tilde{C}_9^{(j)} = C_9 + \underbrace{\Delta C_9^{(\text{fac})}(q^2) + \Delta C_9^{(j),(\text{non-fac})}(q^2)}_{\sim \sum_i C_i \mathcal{Z}_j^i / \chi_j}$$

$$\frac{2(m_b + m_s)}{q^2} C_7 \mathcal{Y}_j \longrightarrow \tilde{\mathcal{Y}}_j = \frac{2(m_b + m_s)}{q^2} C_7 \mathcal{Y}_j + \dots$$

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► Most general parametric form of amplitude in SM

$$\mathcal{A}_\lambda^{L,R} = (\tilde{C}_9^\lambda \mp C_{10}) \mathcal{F}_\lambda - \tilde{\mathcal{G}}_\lambda \quad \mathcal{A}_t|_{m_\ell=0} = 0$$

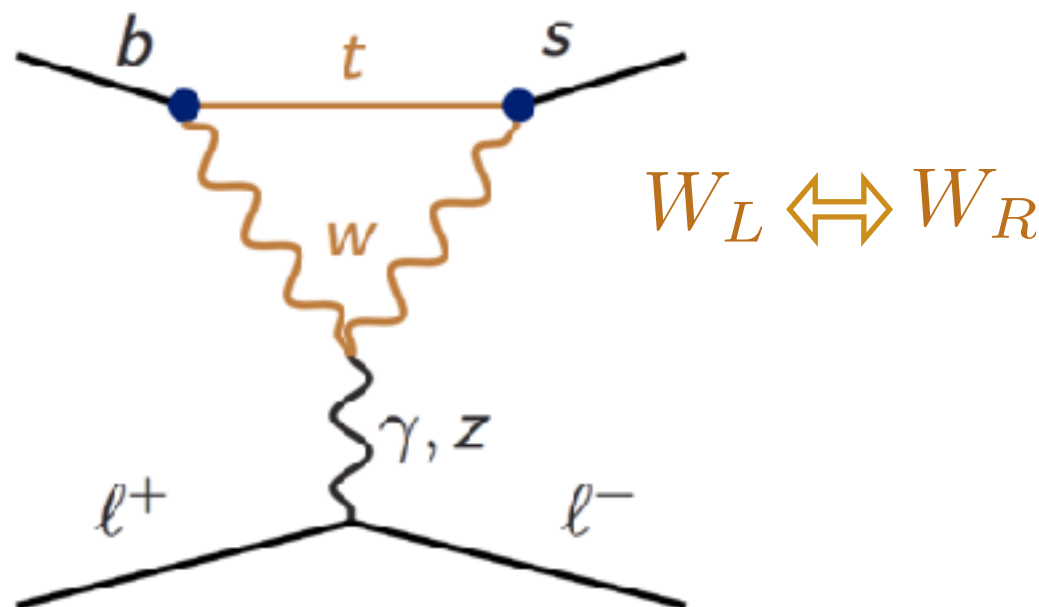
Form-factors: $\mathcal{F}_\lambda \equiv \mathcal{F}_\lambda(\chi_j)$ and $\tilde{\mathcal{G}}_\lambda \equiv \tilde{\mathcal{G}}_\lambda(\tilde{\mathcal{Y}}_j)$

Right-Handed Current

► Chirality flipped operators $\mathcal{O} \leftrightarrow \mathcal{O}'$

$$\bar{s}\gamma_\mu P_L b \quad \longleftrightarrow \quad \bar{s}\gamma_\mu P_R b$$

$$\bar{s}i\sigma_{\mu\nu} P_R b \quad \longleftrightarrow \quad \bar{s}i\sigma_{\mu\nu} P_L b$$



► In presence of right-handed gauge boson or other kind of new particles like leptoquarks etc..

RH Current

► Amplitudes $\mathcal{A}_{\perp}^{L,R} = ((\tilde{C}_9^{\perp} + C'_9) \mp (C_{10} + C'_{10}))\mathcal{F}_{\perp} - \tilde{\mathcal{G}}_{\perp}$
 $\mathcal{A}_{\parallel,0}^{L,R} = ((\tilde{C}_9^{\parallel,0} - C'_9) \mp (C_{10} - C'_{10}))\mathcal{F}_{\parallel,0} - \tilde{\mathcal{G}}_{\parallel,0}$

► Notation $r_{\lambda} = \frac{\text{Re}(\tilde{\mathcal{G}}_{\lambda})}{\mathcal{F}_{\lambda}} - \text{Re}(\tilde{C}_9^{\lambda}) \quad \xi = \frac{C'_{10}}{C_{10}} \quad \xi' = \frac{C'_9}{C_{10}}$

► Variables $R_{\perp} = \frac{\frac{r_{\perp}}{C_{10}} - \xi'}{1 + \xi}, \quad R_{\parallel} = \frac{\frac{r_{\parallel}}{C_{10}} + \xi'}{1 - \xi}, \quad R_0 = \frac{\frac{r_0}{C_{10}} + \xi'}{1 - \xi}.$

► HQET limit $\frac{\tilde{\mathcal{G}}_{\parallel}}{\mathcal{F}_{\parallel}} = \frac{\tilde{\mathcal{G}}_{\perp}}{\mathcal{F}_{\perp}} = \frac{\tilde{\mathcal{G}}_0}{\mathcal{F}_0} = -\kappa \frac{2m_b m_B C_7}{q^2},$ [Grinstein, Pijol '04]
[Bobeth et. al '10]

⇒ $r_0 = r_{\parallel} = r_{\perp} \equiv r$ ignoring non-factorisable corrections

⇒ $R_0 = R_{\parallel} \neq R_{\perp}$ in presence of RH currents

RH Current

At kinematic endpoint   exact HQET limit
 polarization independent
non-factorisable correction

► Observables $F_L(q_{\text{max}}^2) = \frac{1}{3}, F_{\parallel}(q_{\text{max}}^2) = \frac{2}{3}, A_4(q_{\text{max}}^2) = \frac{2}{3\pi},$
 $F_{\perp}(q_{\text{max}}^2) = 0, A_{\text{FB}}(q_{\text{max}}^2) = 0, A_{5,7,8,9}(q_{\text{max}}^2) = 0.$

[Hiller, Zwicky '14]

► Taylor series expansion around $\delta \equiv q_{\text{max}}^2 - q^2$

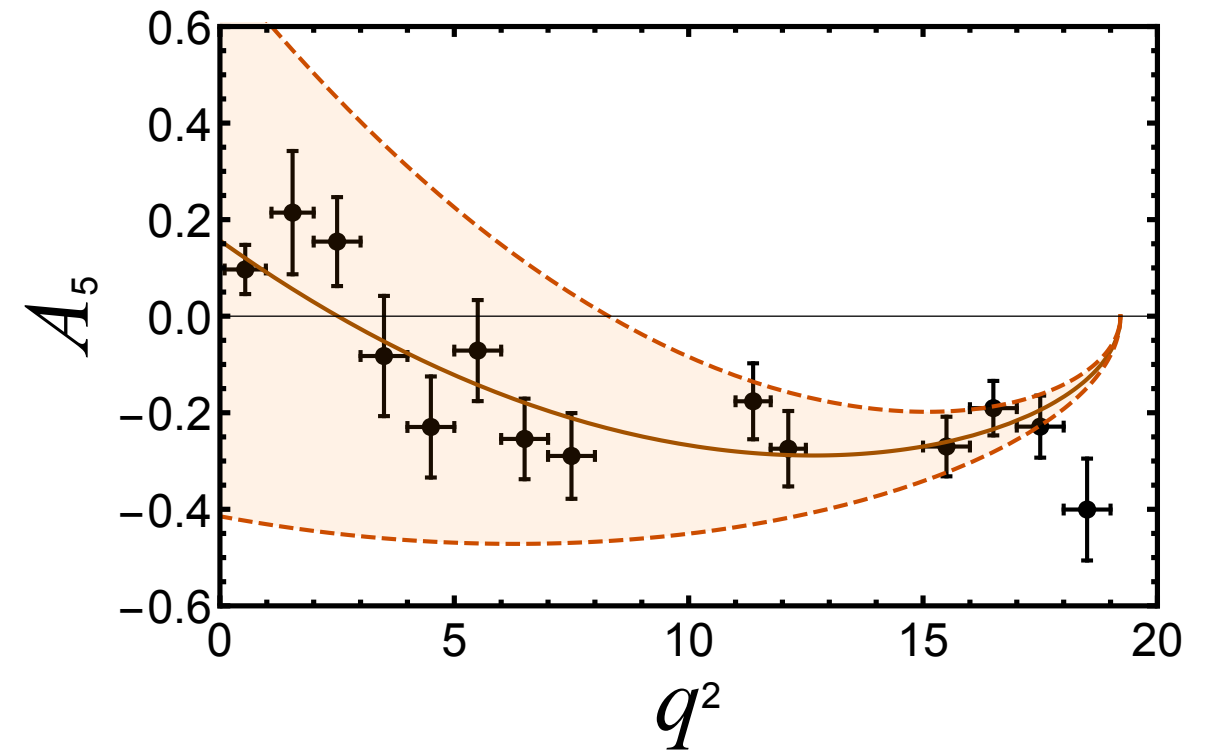
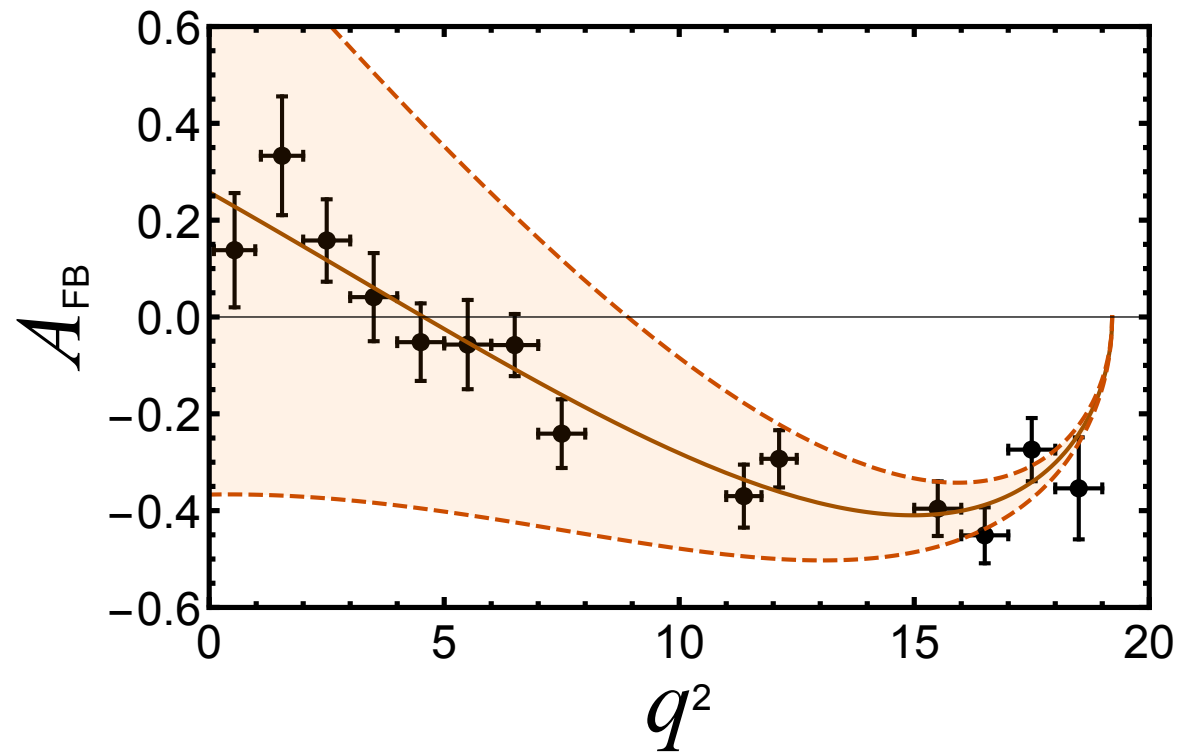
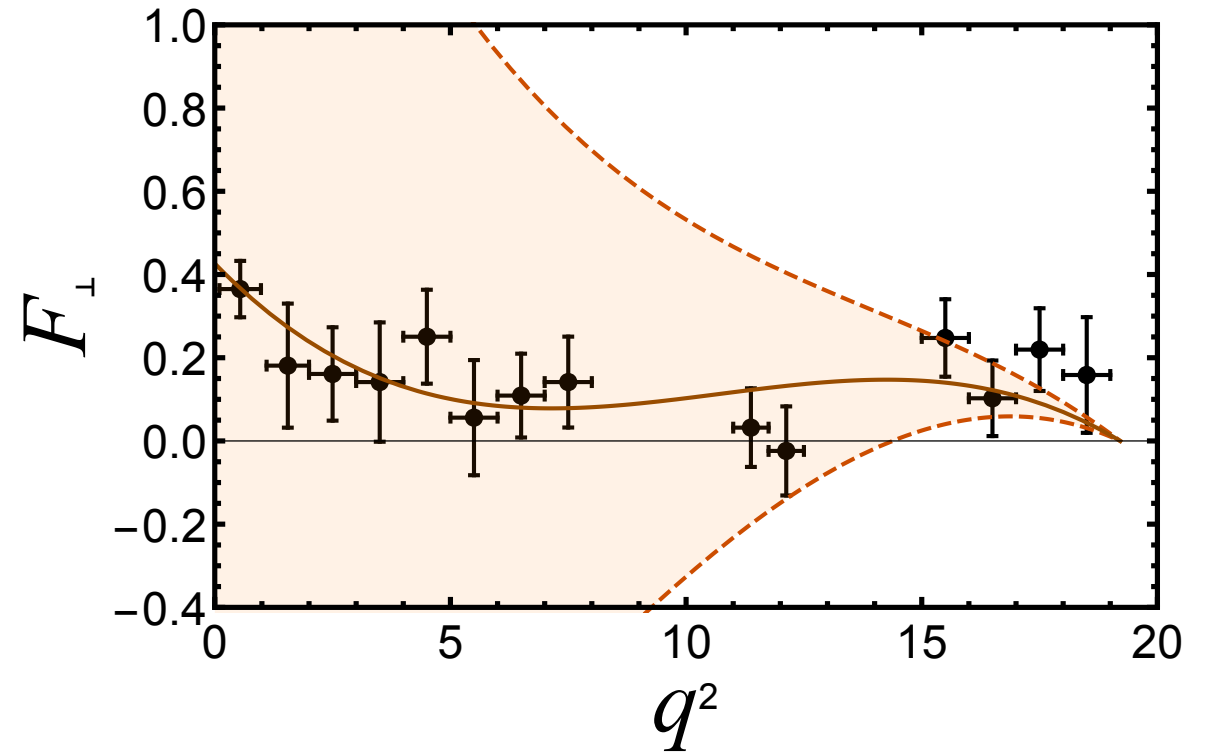
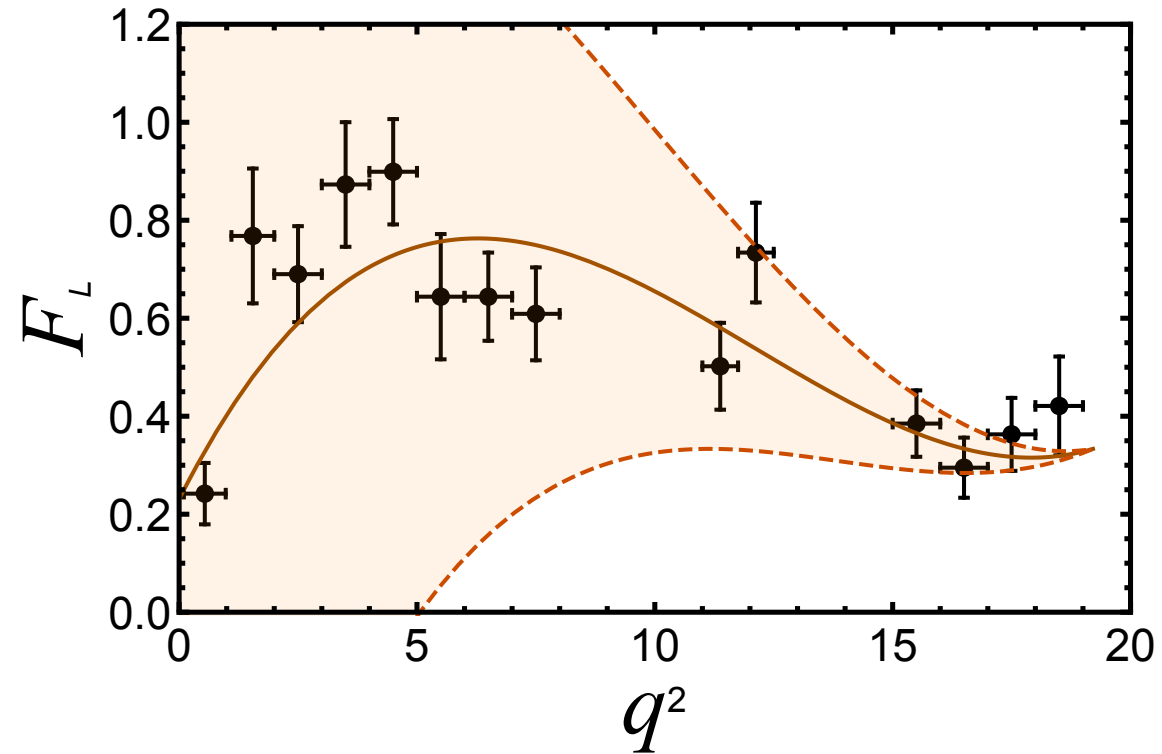
$$F_L = \frac{1}{3} + F_L^{(1)}\delta + F_L^{(2)}\delta^2 + F_L^{(3)}\delta^3$$

$$F_{\perp} = F_{\perp}^{(1)}\delta + F_{\perp}^{(2)}\delta^2 + F_{\perp}^{(3)}\delta^3$$

$$A_{\text{FB}} = A_{\text{FB}}^{(1)}\delta^{\frac{1}{2}} + A_{\text{FB}}^{(2)}\delta^{\frac{3}{2}} + A_{\text{FB}}^{(3)}\delta^{\frac{5}{2}}$$

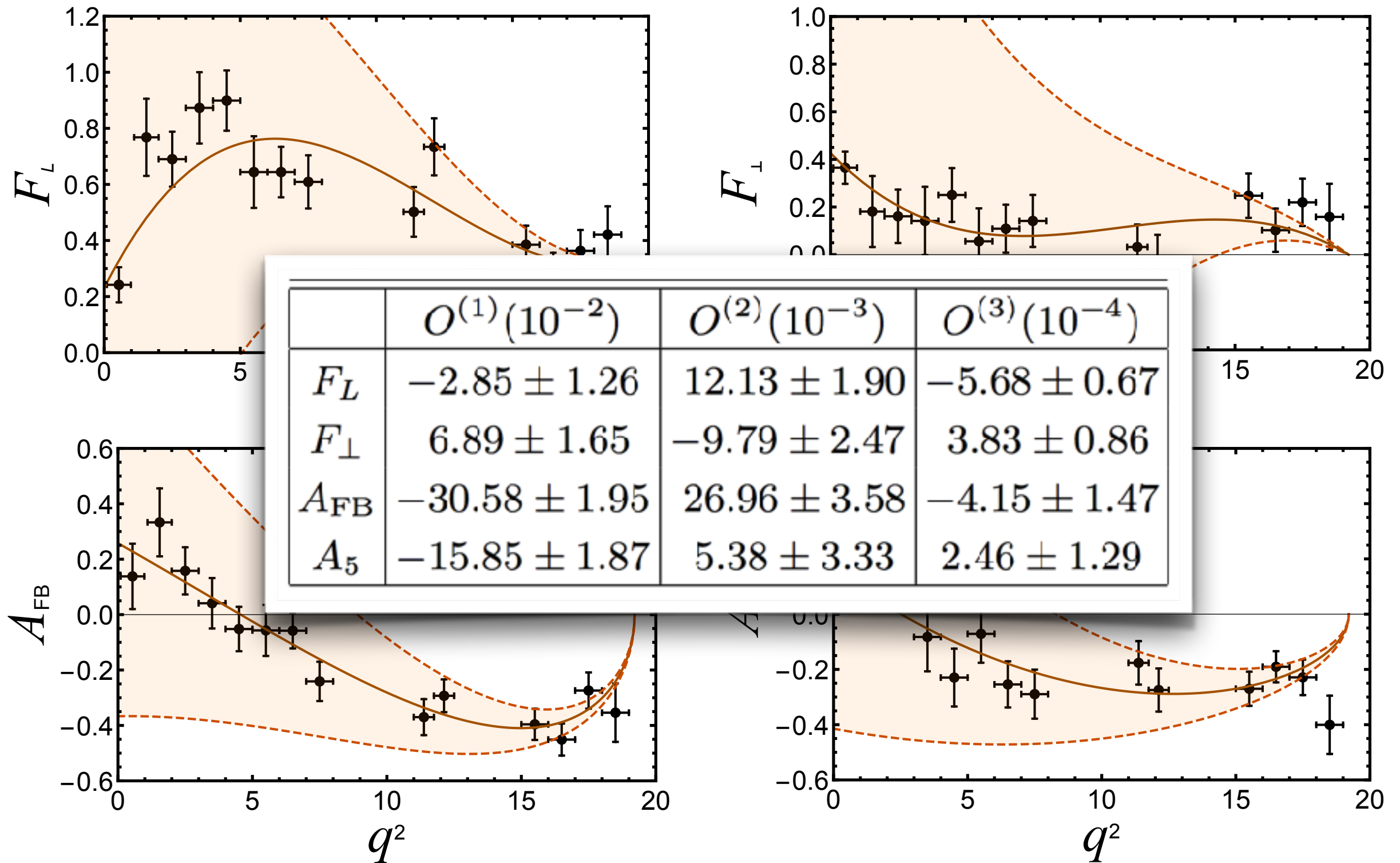
$$A_5 = A_5^{(1)}\delta^{\frac{1}{2}} + A_5^{(2)}\delta^{\frac{3}{2}} + A_5^{(3)}\delta^{\frac{5}{2}},$$

RH Current



Fit to 14 bin LHCb data including correlation among observables

RH Current



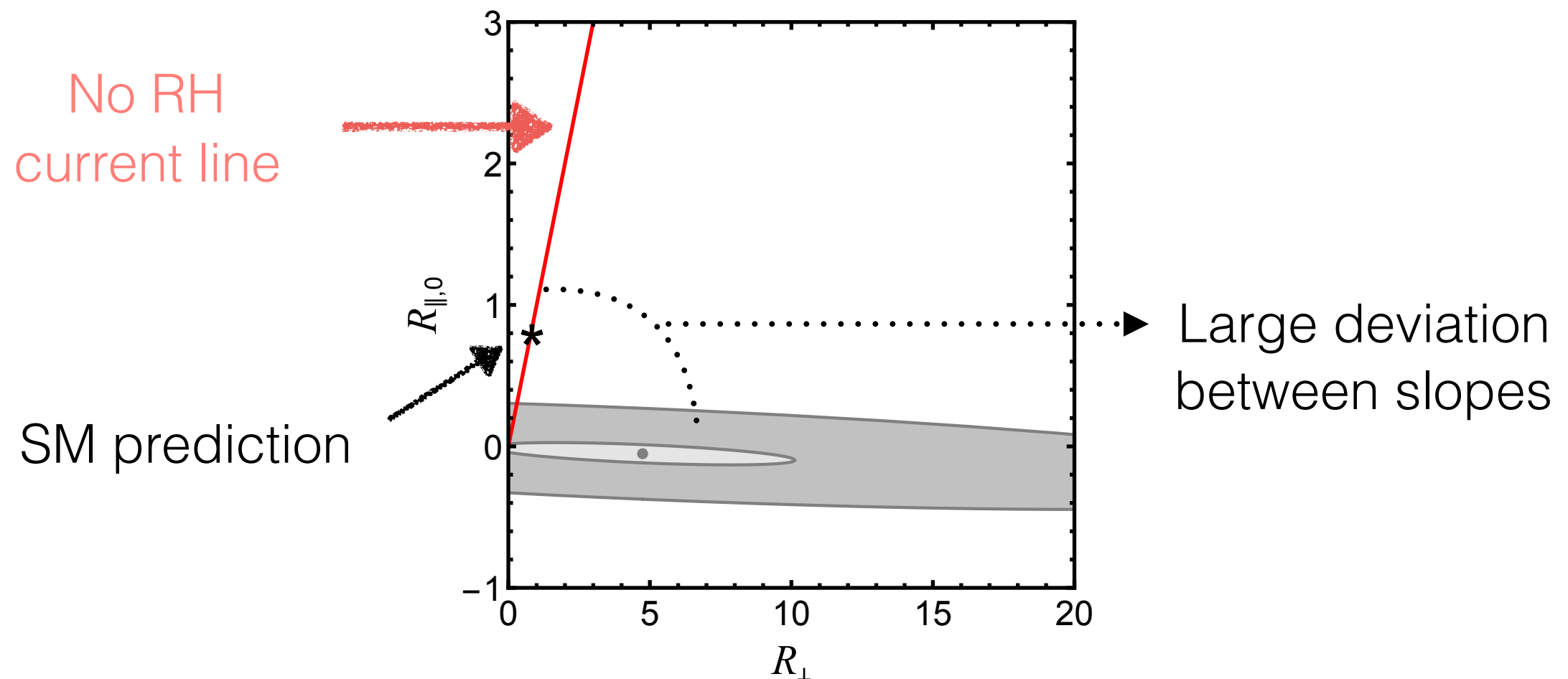
Fit to 14 bin LHCb data including correlation among observables

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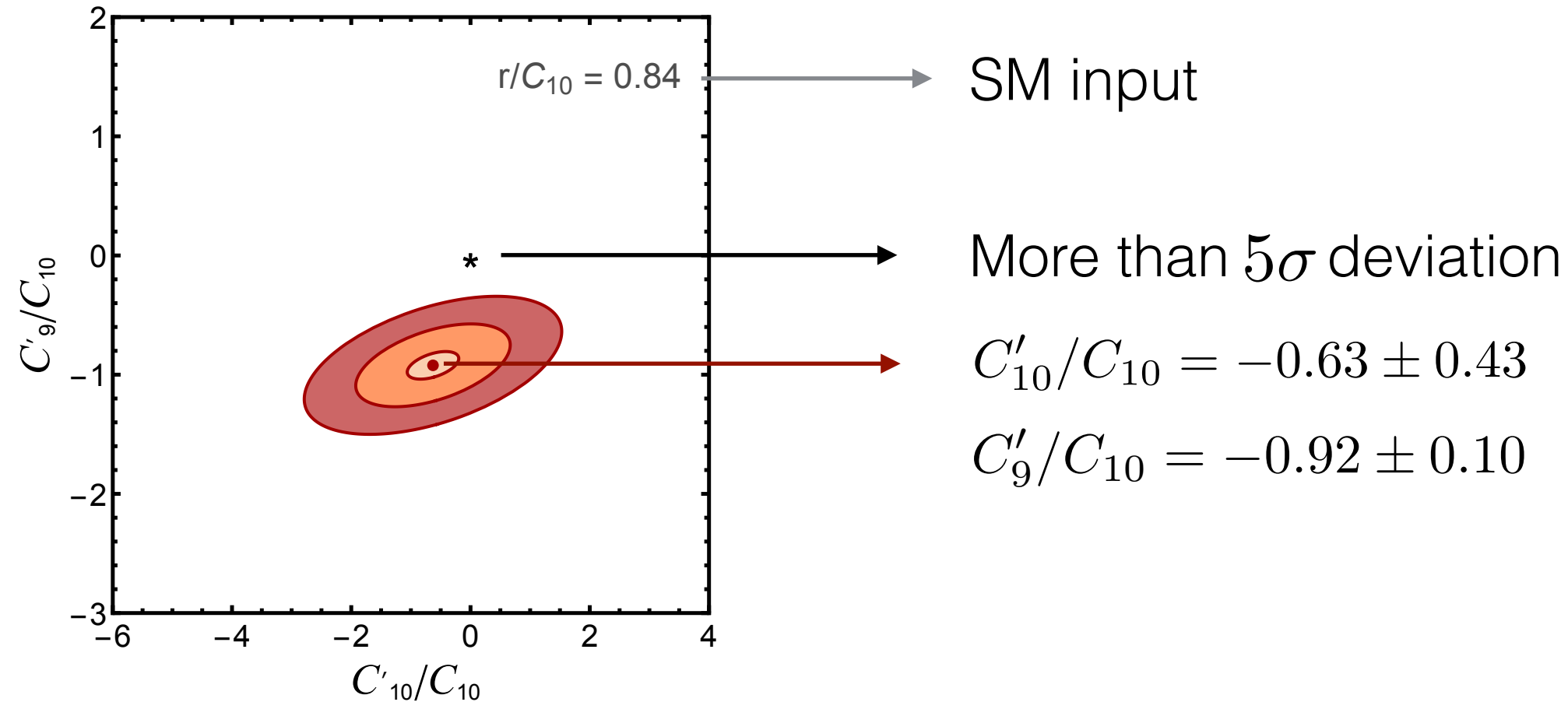
► Limiting analytic expressions

$$R_{\perp}(q_{\max}^2) = \frac{\omega_2 - \omega_1}{\omega_2 \sqrt{\omega_1 - 1}}, \quad R_{\parallel}(q_{\max}^2) = \frac{\sqrt{\omega_1 - 1}}{\omega_2 - 1} = R_0(q_{\max}^2)$$

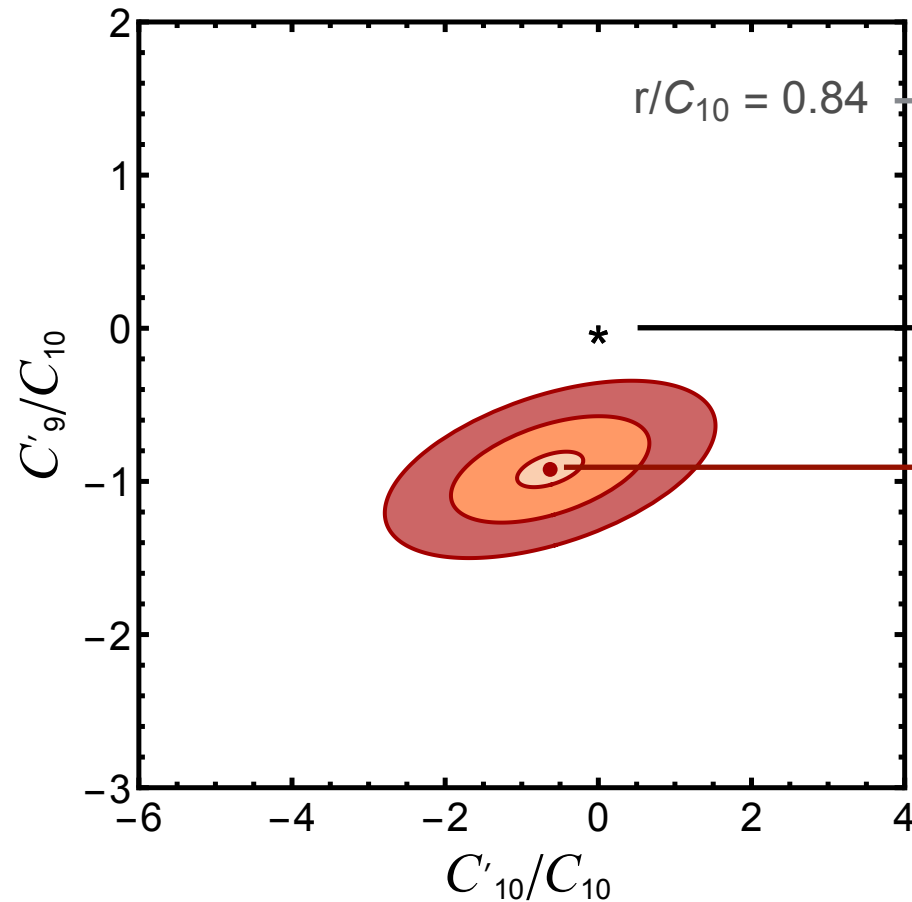
$$\omega_1 = \frac{3}{2} \frac{F_{\perp}^{(1)}}{A_{\text{FB}}^{(1)2}} \quad \text{or} \quad \frac{3}{8} \frac{F_{\perp}^{(1)}}{A_5^{(1)2}} \quad \text{and} \quad \omega_2 = \frac{4 \left(2A_5^{(2)} - A_{\text{FB}}^{(2)} \right)}{3 A_{\text{FB}}^{(1)} \left(3F_L^{(1)} + F_{\perp}^{(1)} \right)} \quad \text{or} \quad \frac{4 \left(2A_5^{(2)} - A_{\text{FB}}^{(2)} \right)}{6 A_5^{(1)} \left(3F_L^{(1)} + F_{\perp}^{(1)} \right)}$$



Results in $C'_{10}/C_{10} - C'_9/C_{10}$



Results in $C'_{10}/C_{10} - C'_9/C_{10}$



SM input

More than 5σ deviation

$$C'_{10}/C_{10} = -0.63 \pm 0.43$$

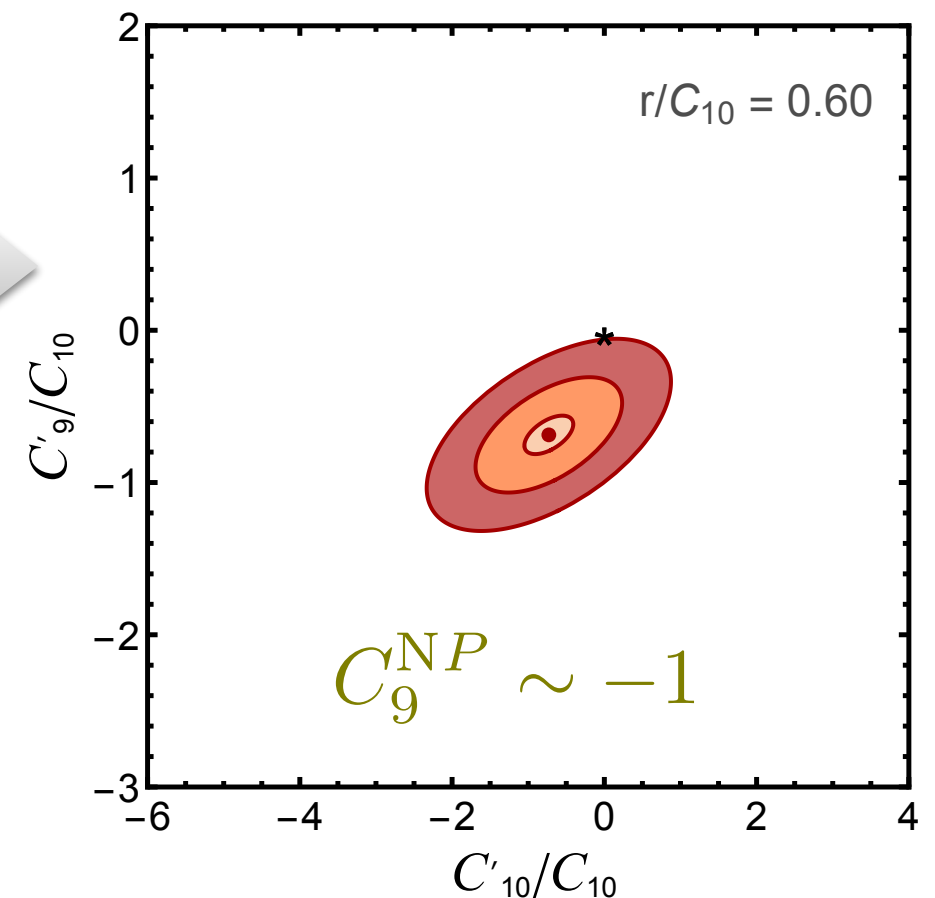
$$C'_9/C_{10} = -0.92 \pm 0.10$$

reduced significance of deviation
for lowered r/C_{10} value

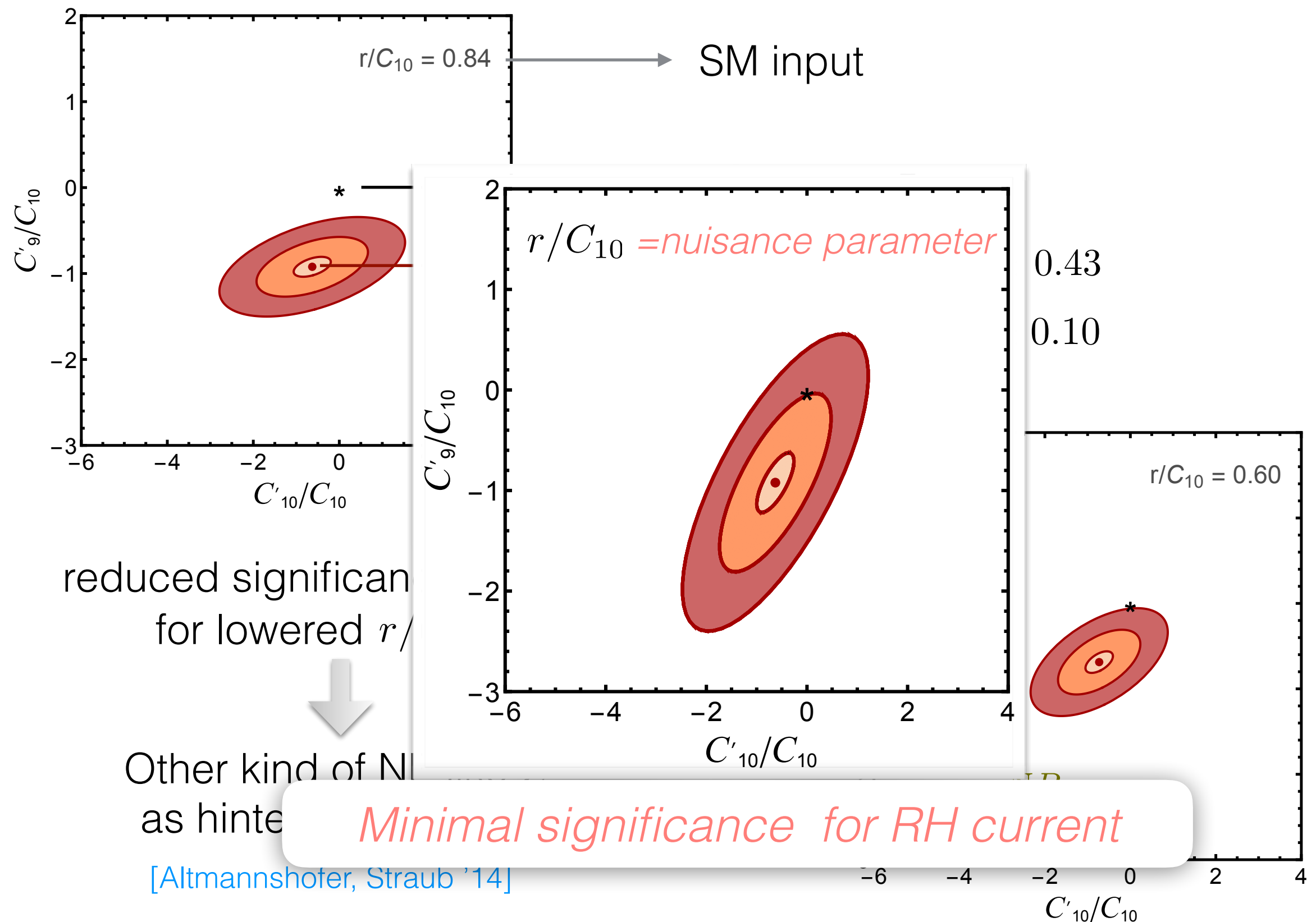


Other kind of NP like Z'
as hinted in global fits

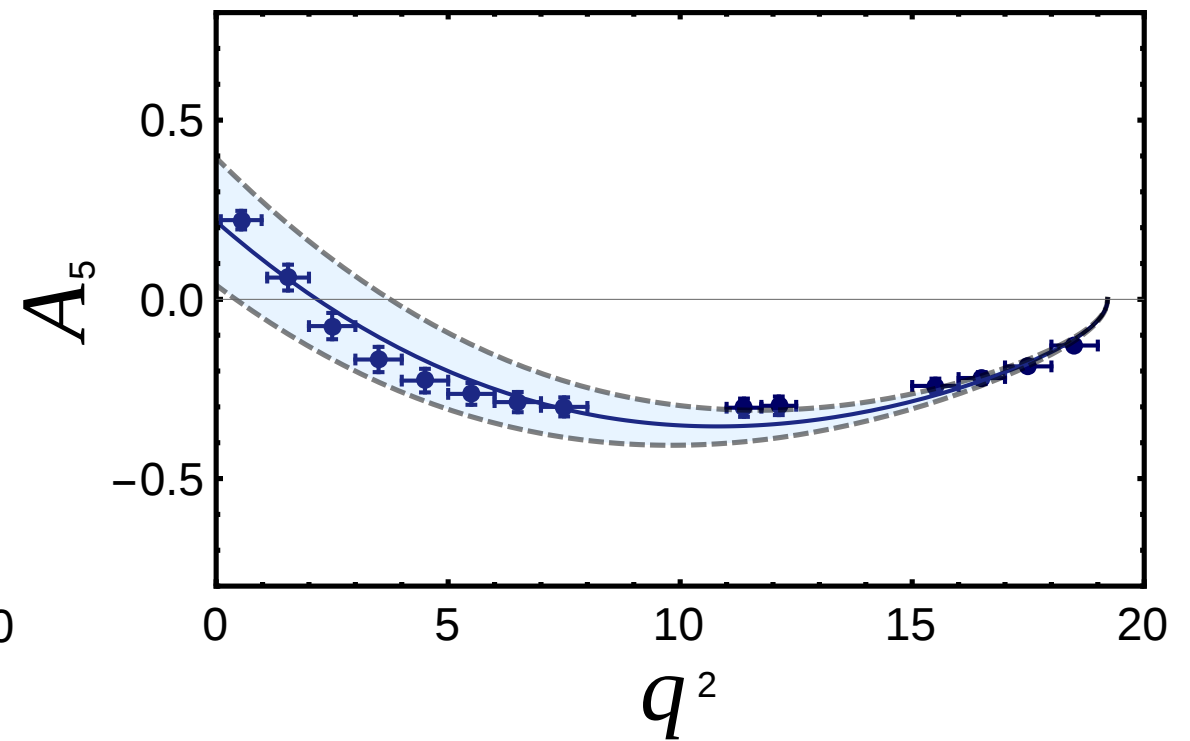
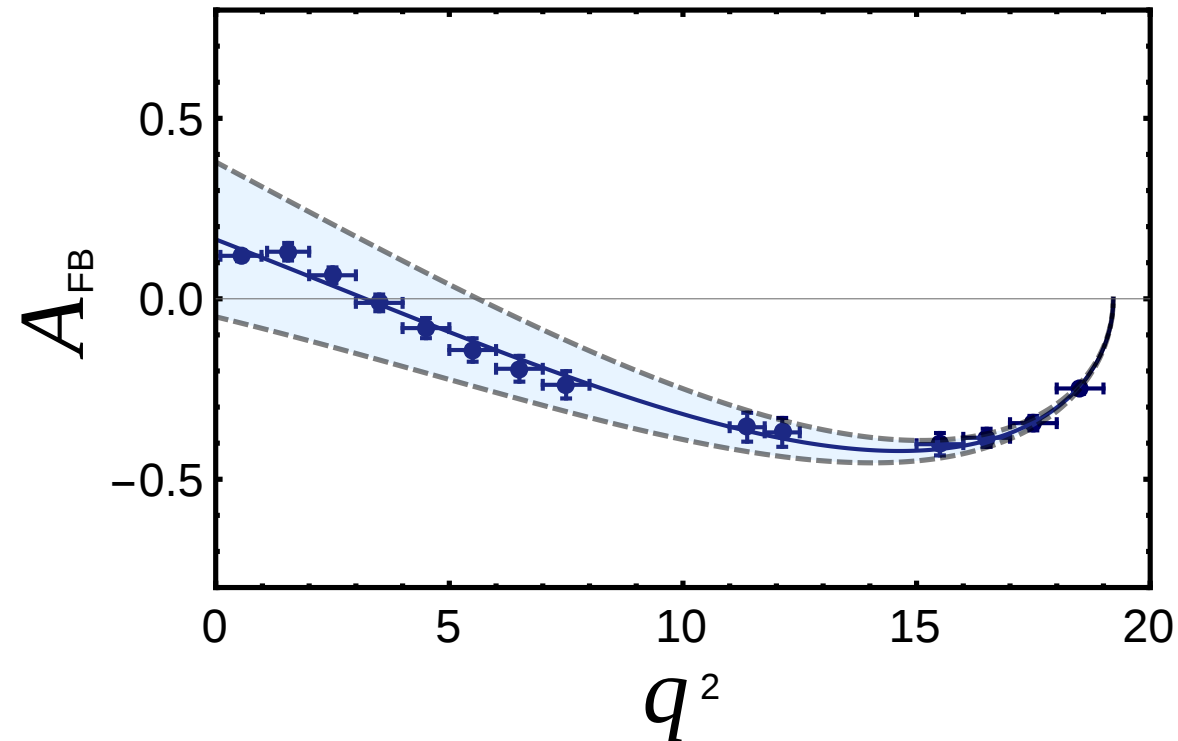
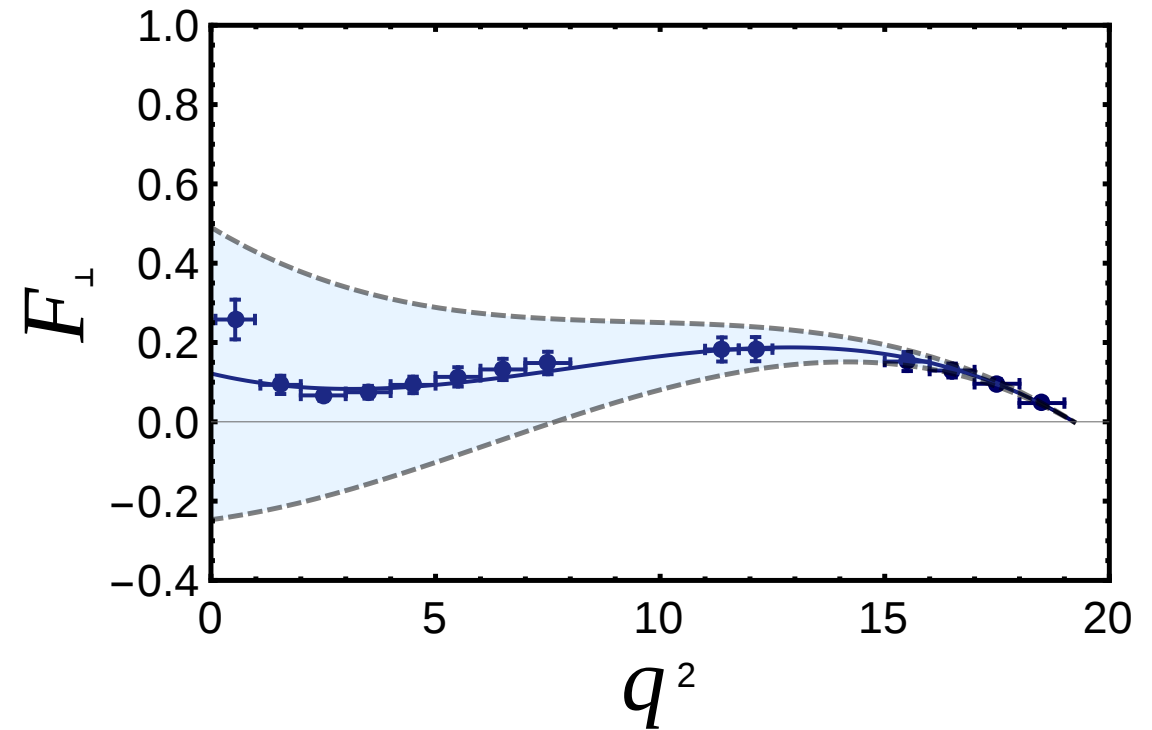
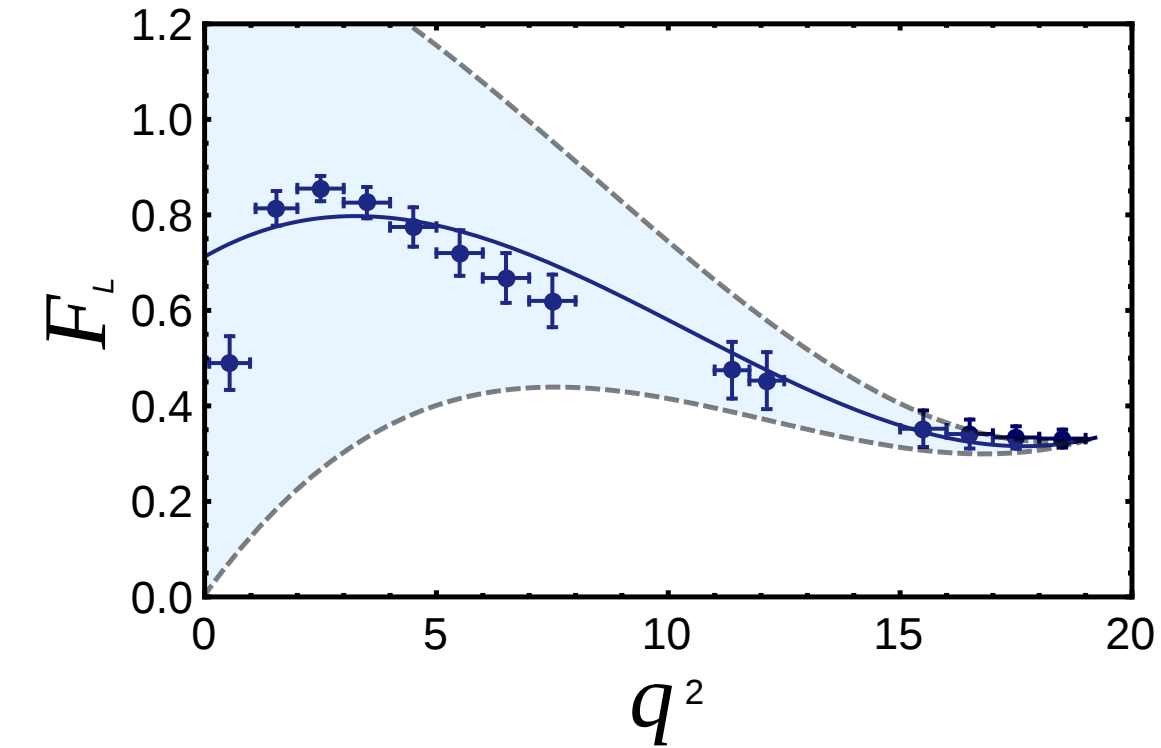
[Altmannshofer, Straub '14]



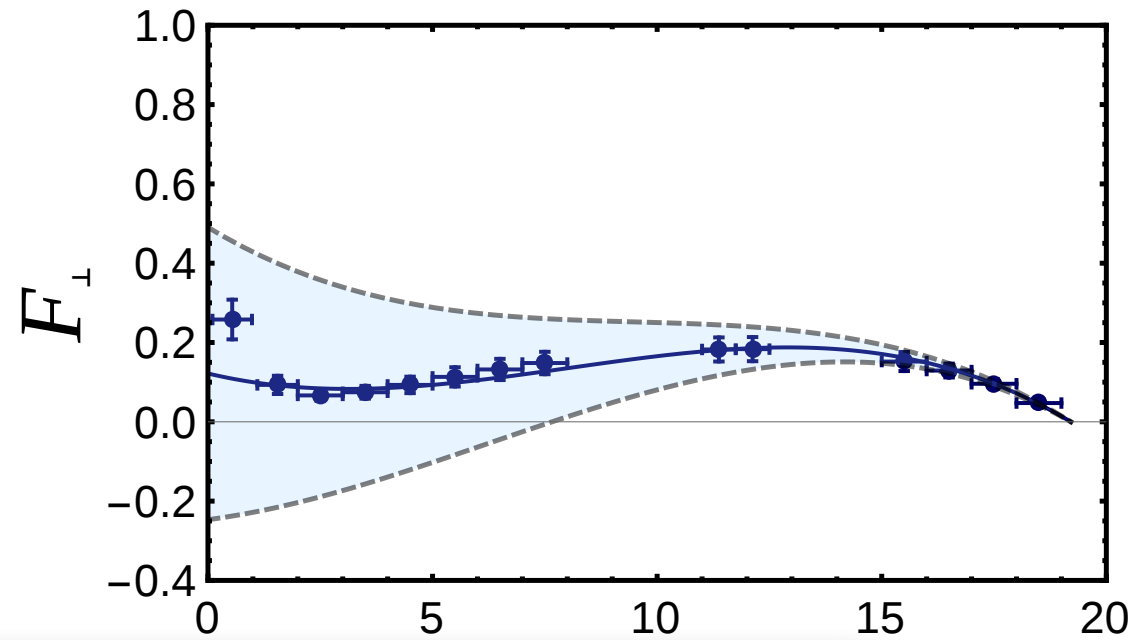
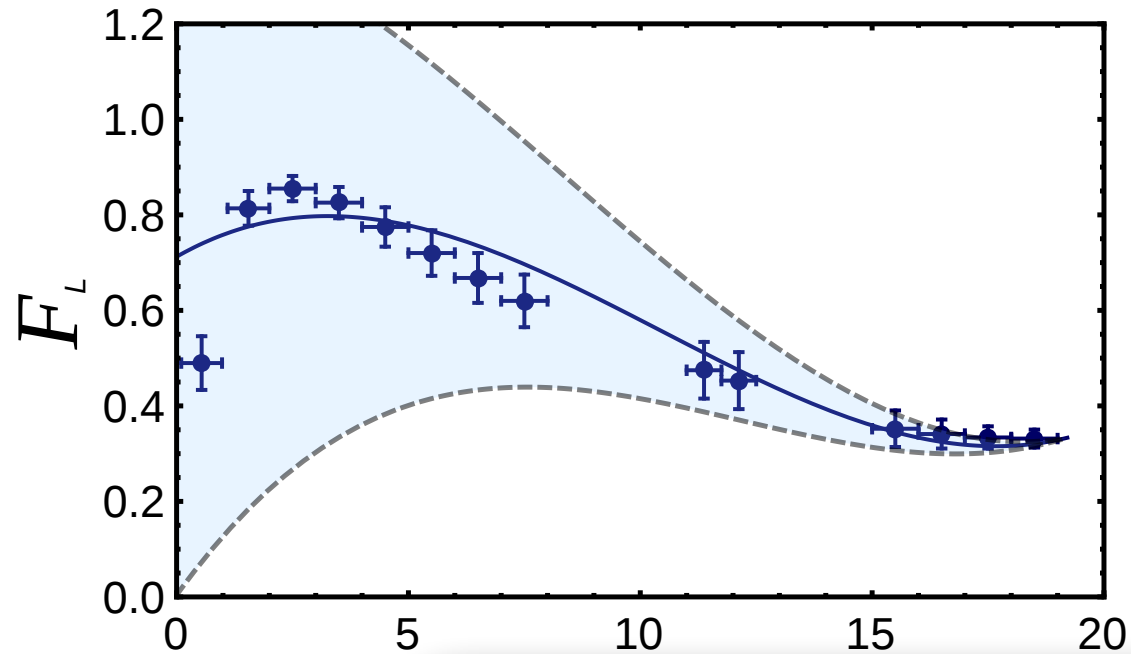
Results in $C'_{10}/C_{10} - C'_9/C_{10}$



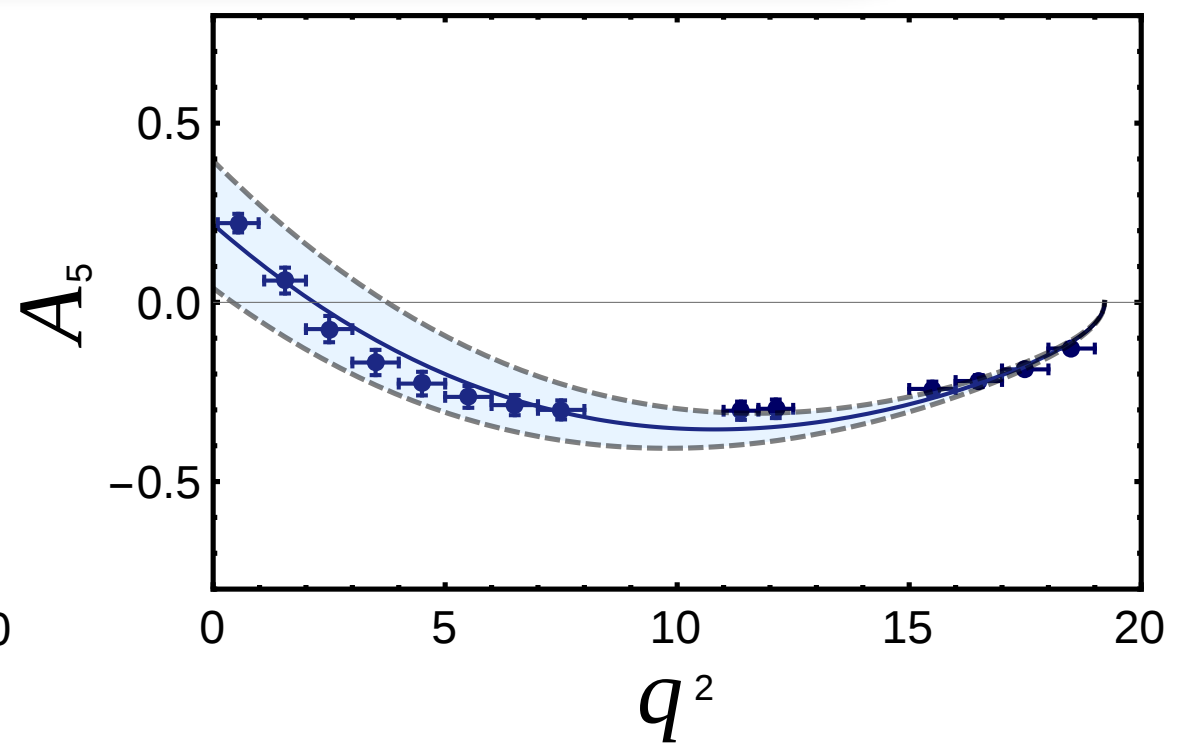
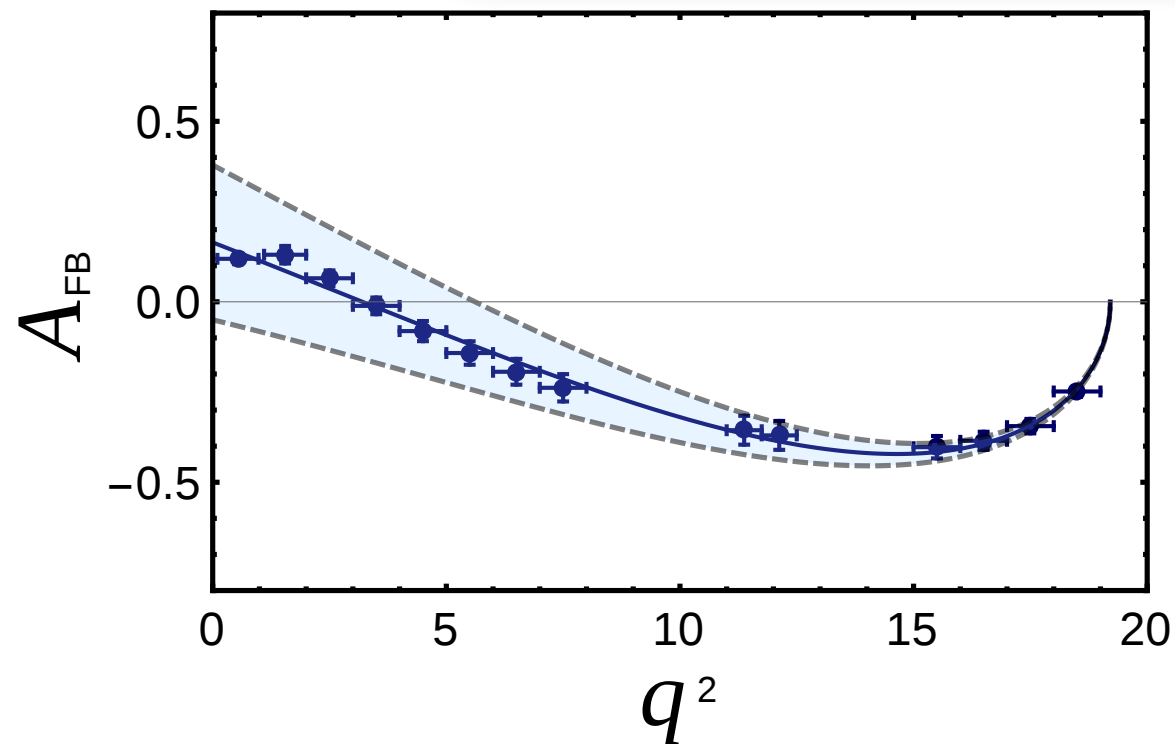
Fit to form factor observables



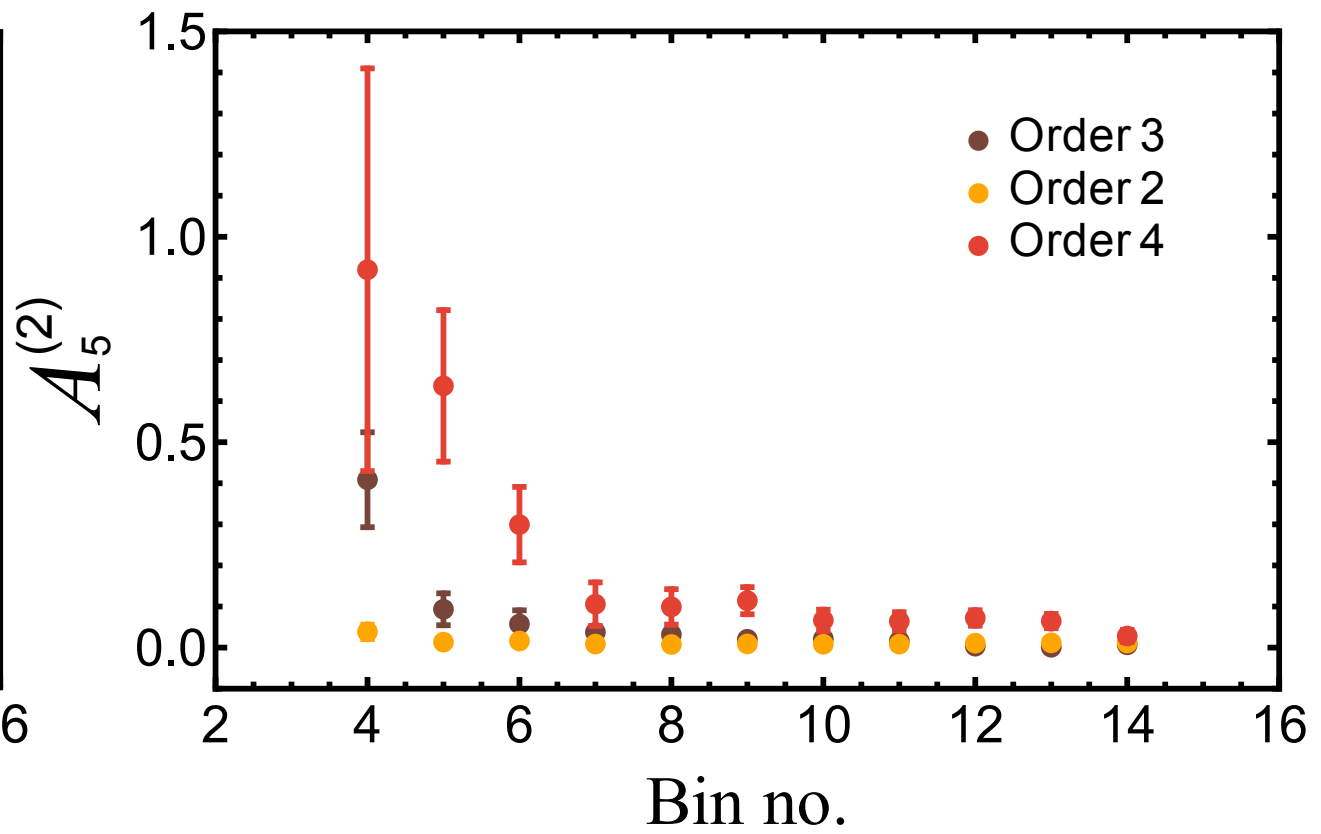
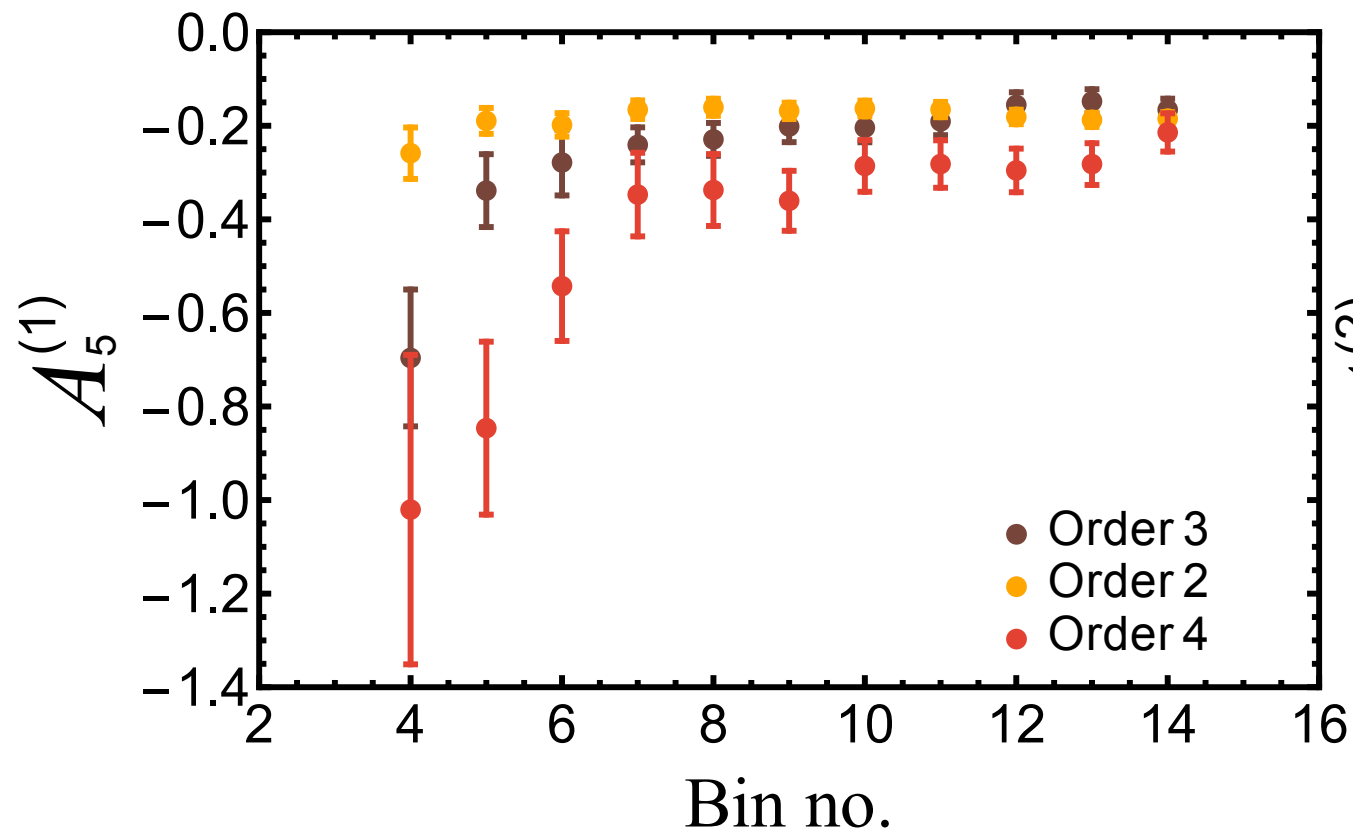
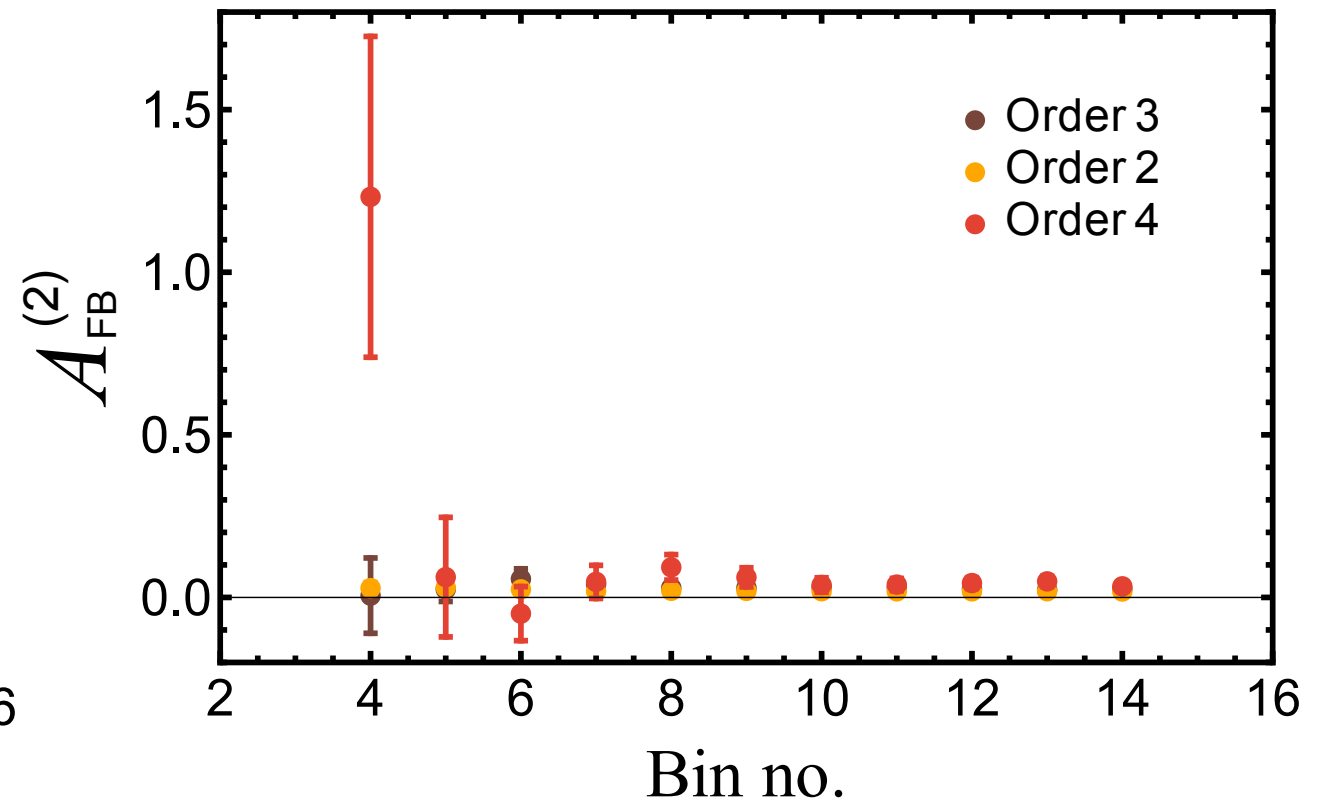
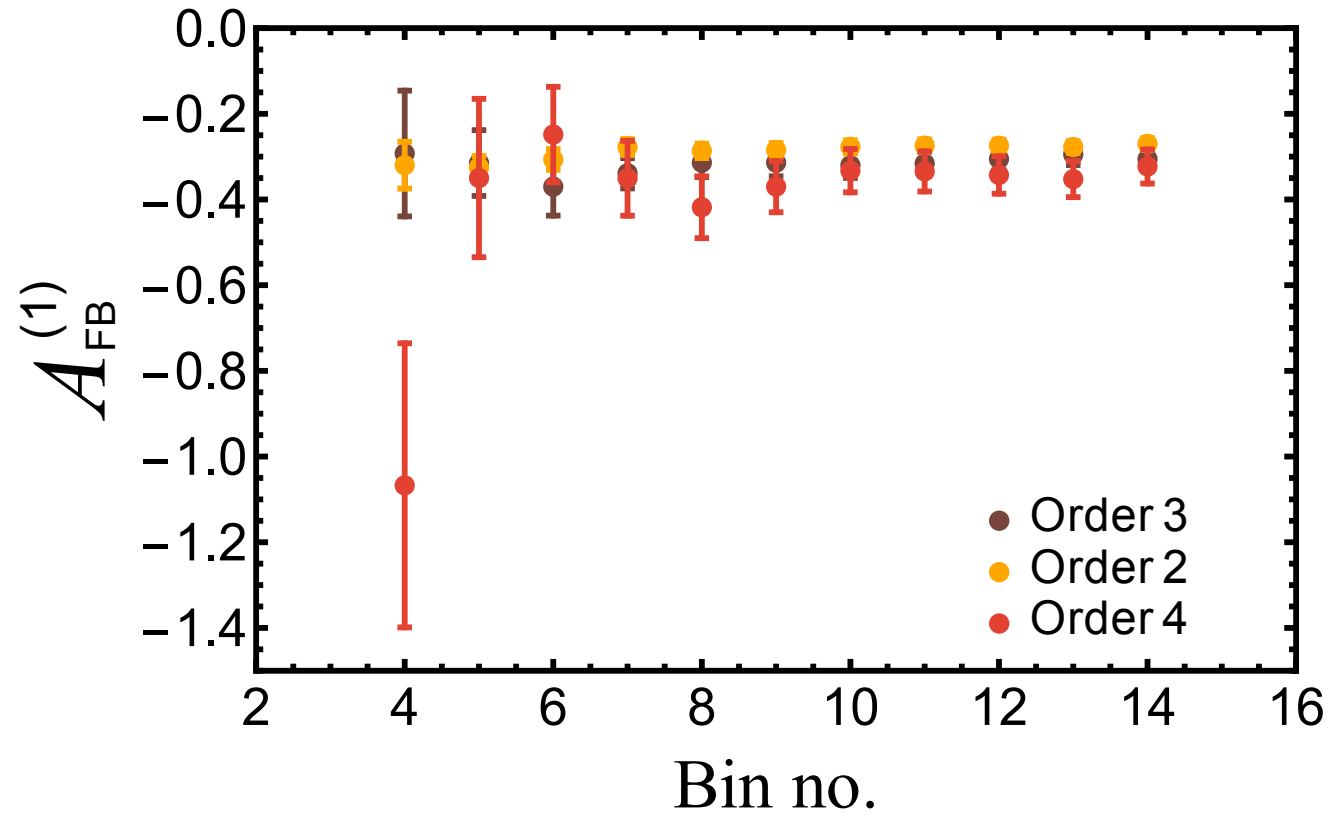
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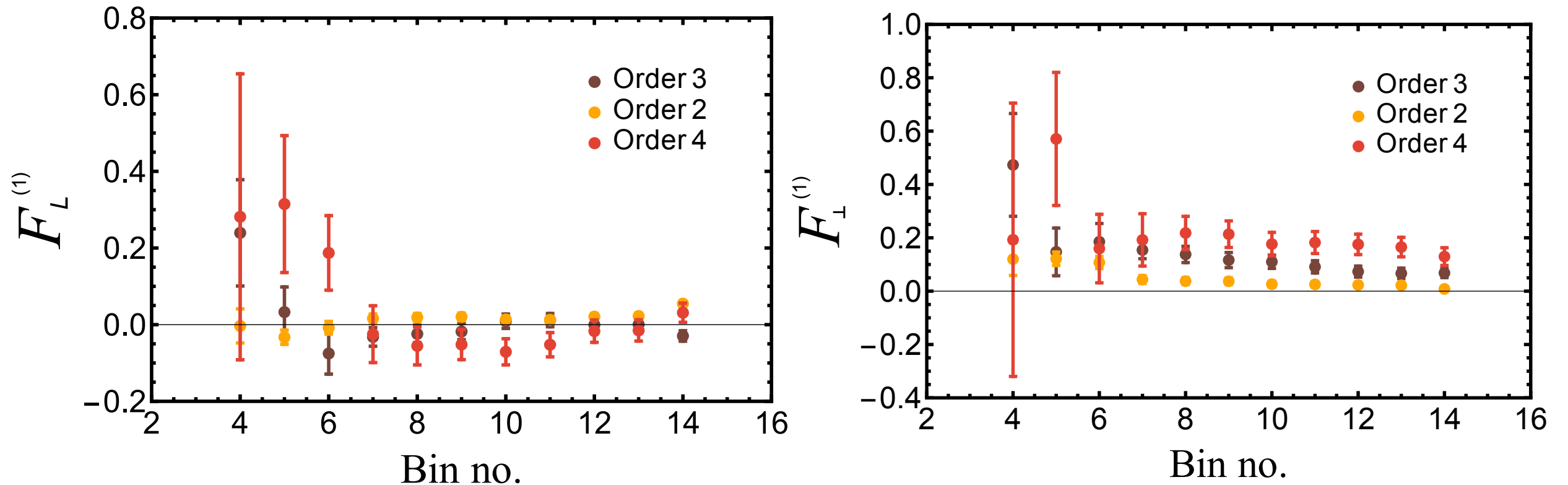
nicely explained by 3rd order polynomial



Convergence of coefficients



Convergence of coefficients

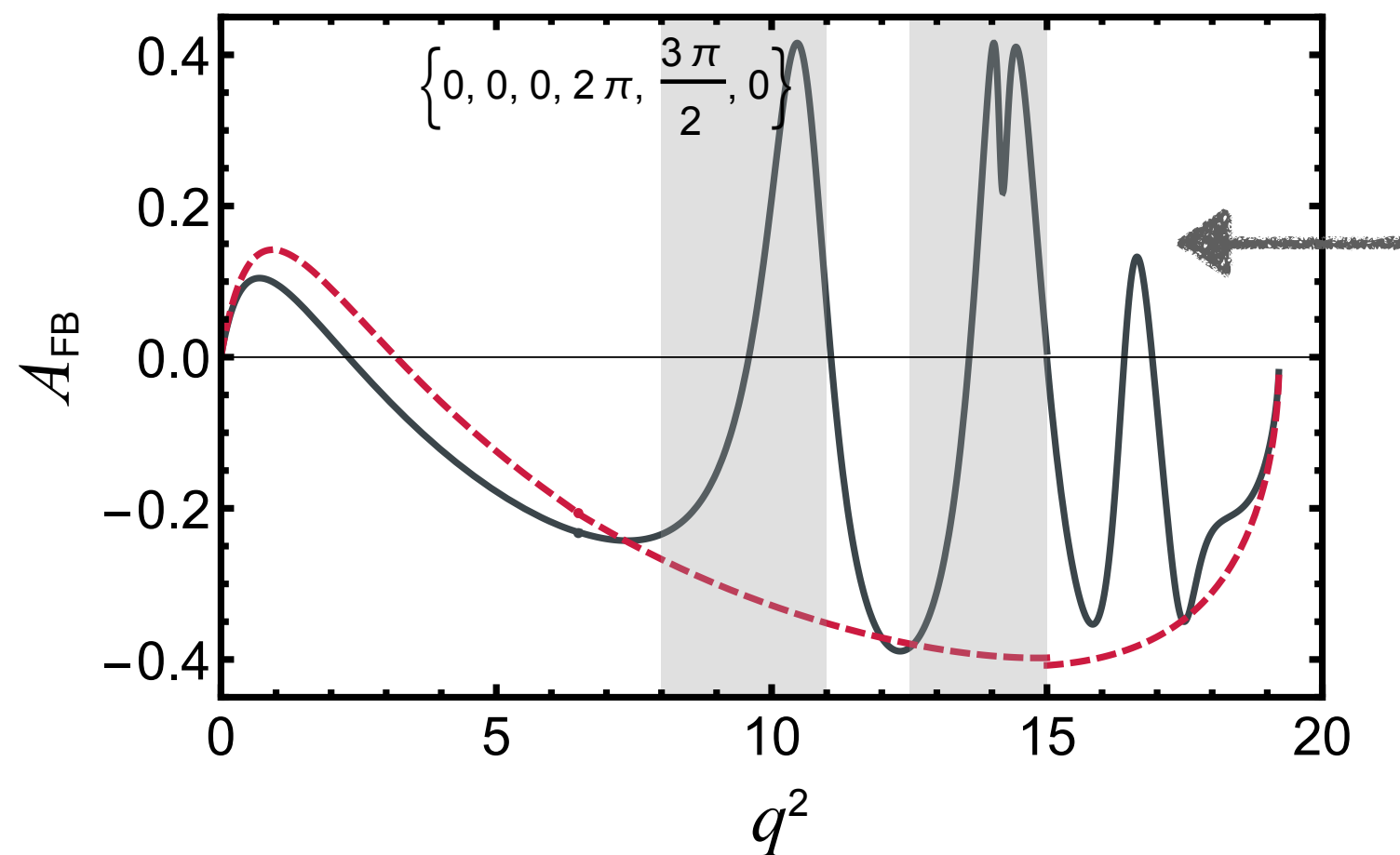


Shows a good convergence with variation in polynomial order & no. of bins used for the data fit

Resonances

$c\bar{c}$ bound states added: J/ψ , $\psi(2S)$, $\psi(3770)$, $\psi(4040)$, $\psi(4160)$, $\psi(4415)$.

Observable = Form-factors + Kruger & Sehgal parametrization



Asymmetries decrease
in high q^2 region

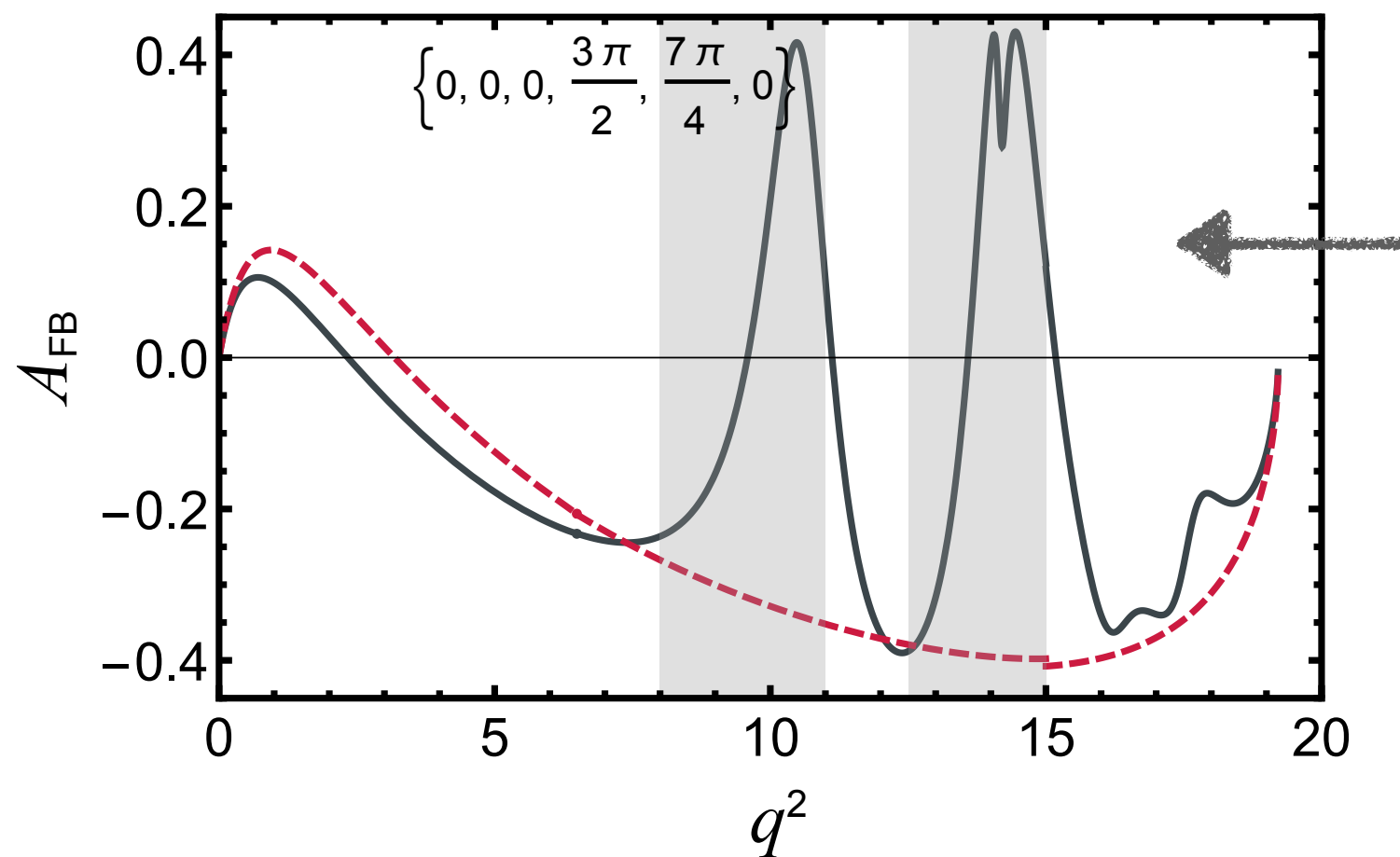
makes observable
 ω_1 unphysical

Random variation of each strong phases

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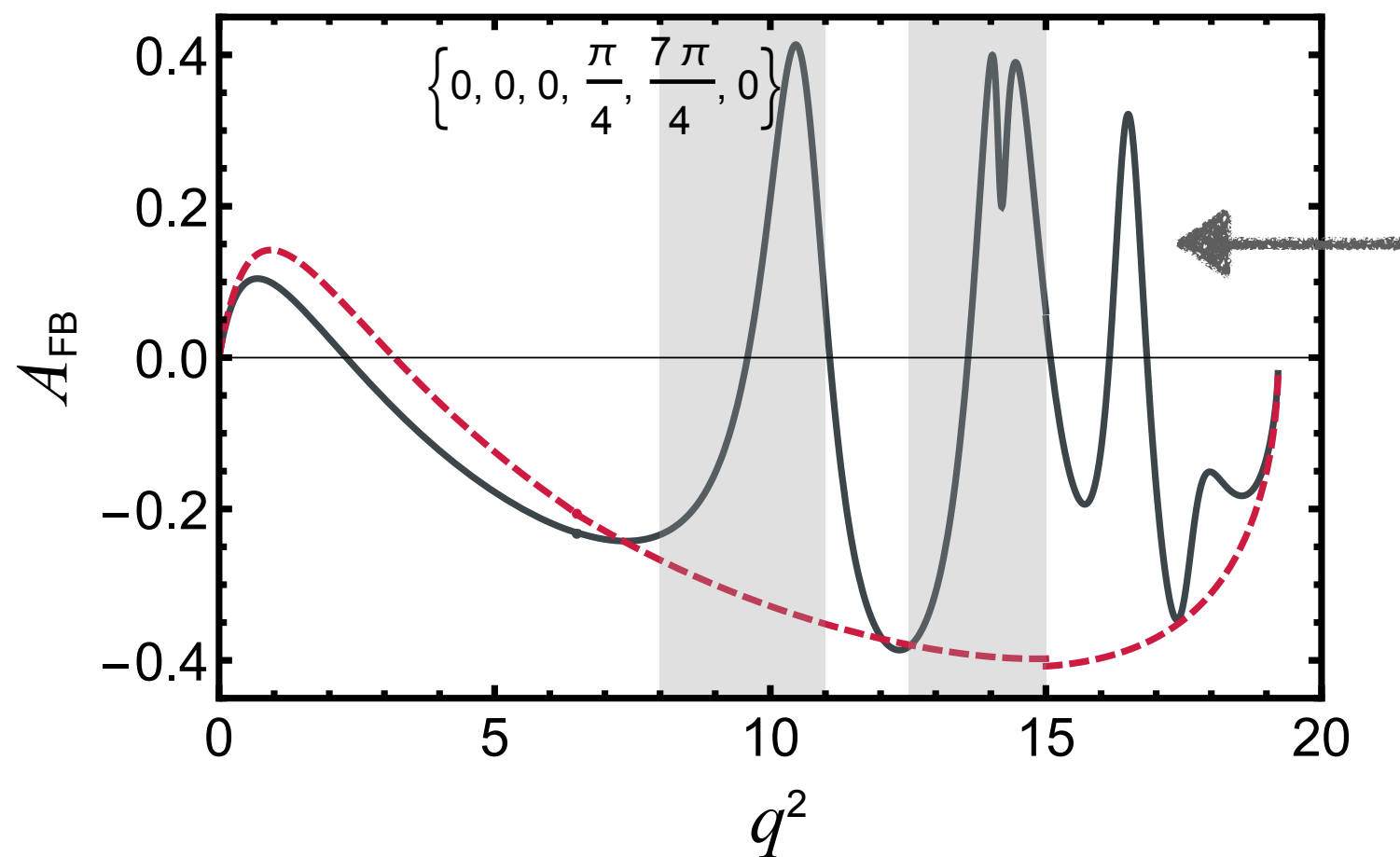
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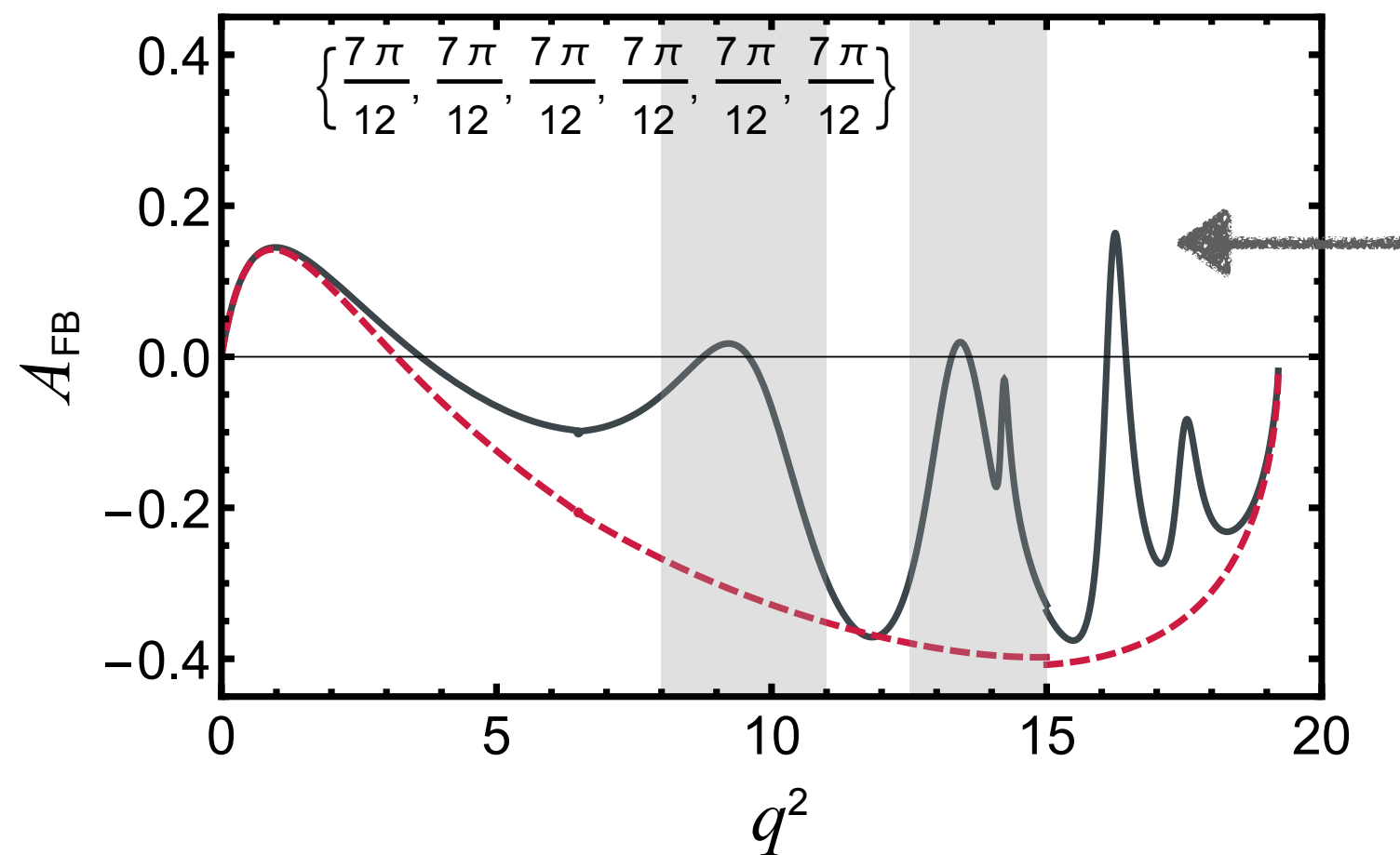
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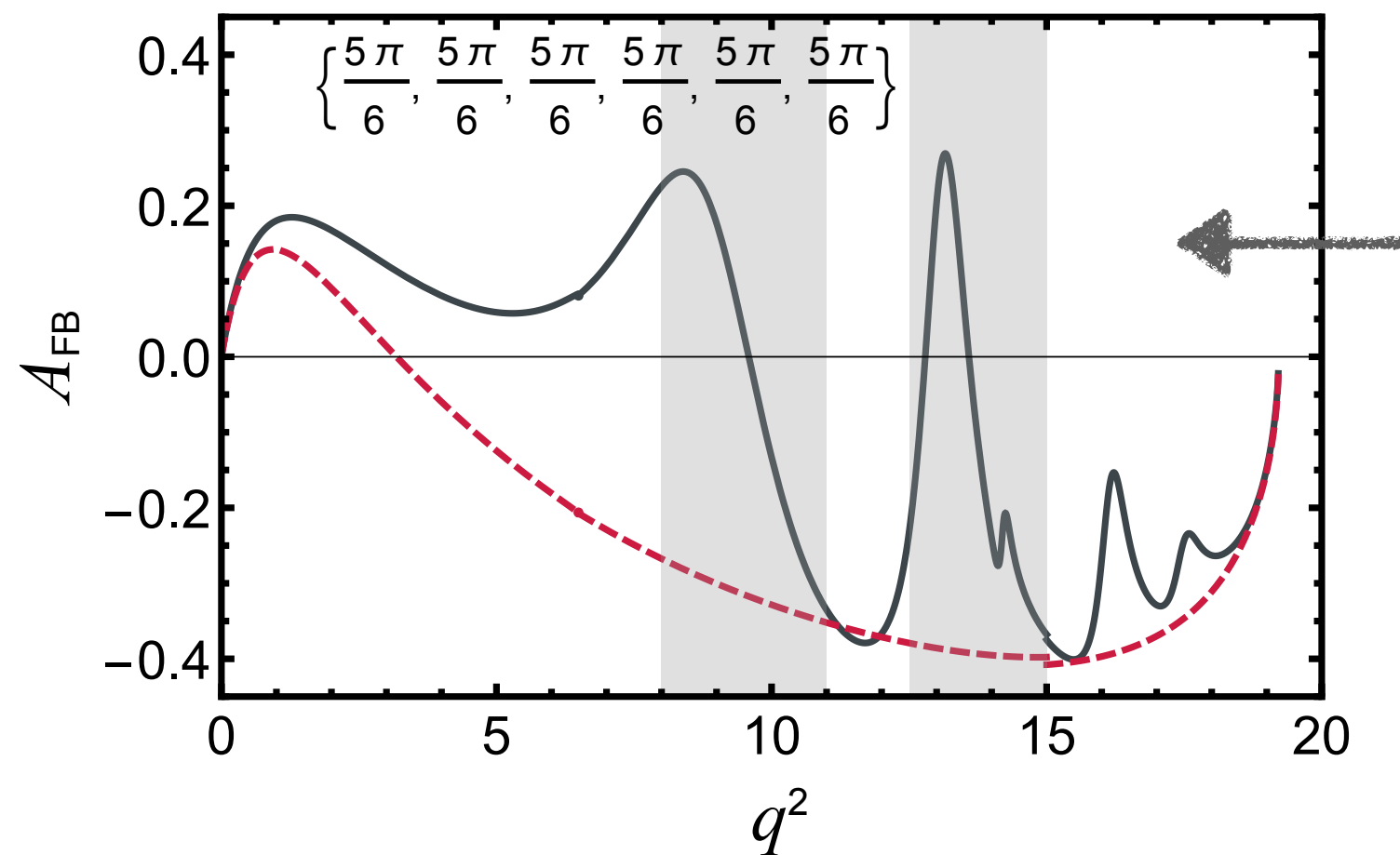
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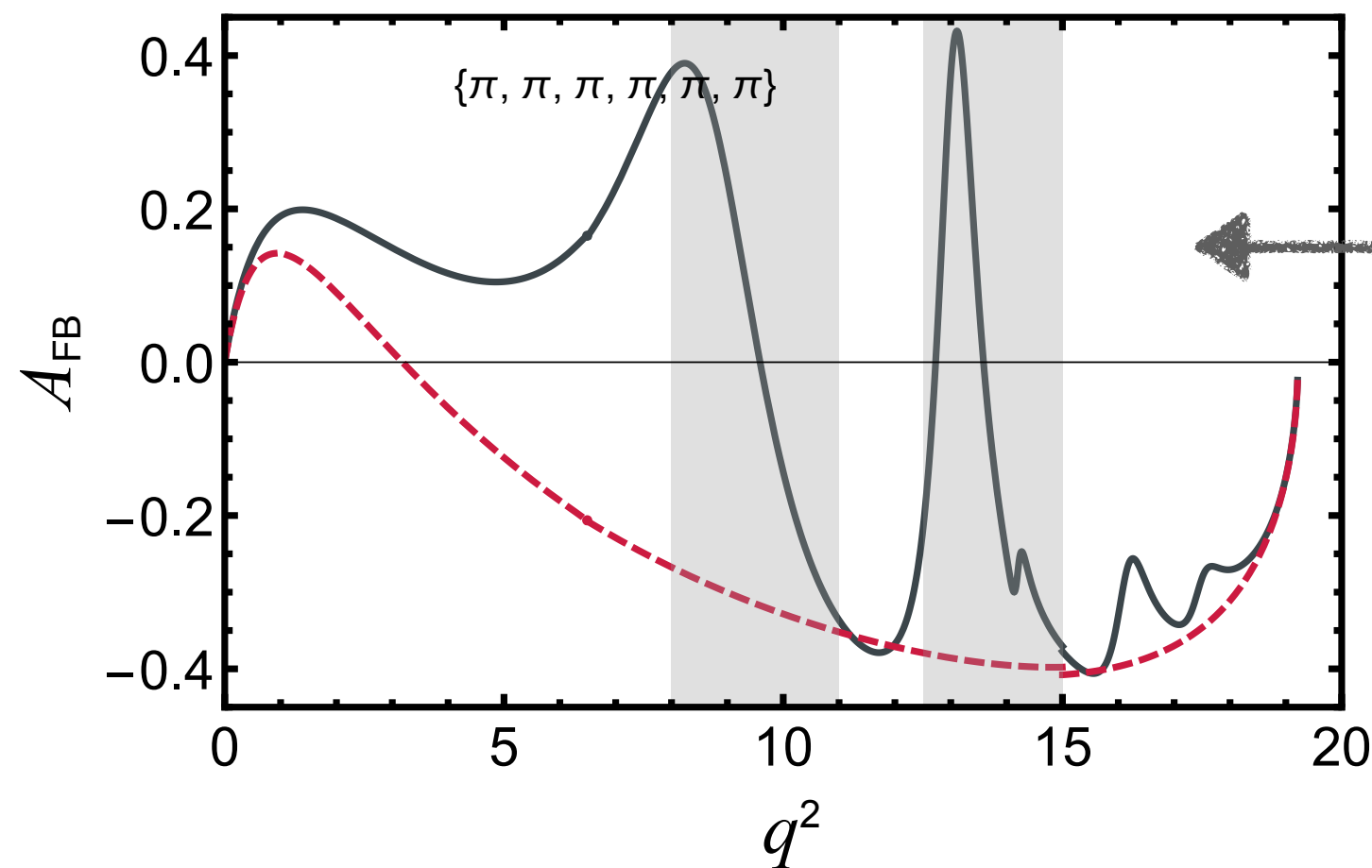
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in high q^2 region

makes observable
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Random variation of each strong phases

Lepton non-universality

► Discrepancies in neutral current B decays

$$R_{K^{(*)}} \equiv \frac{\text{BR}(B \rightarrow K^{(*)} \mu \mu)}{\text{BR}(B \rightarrow K^{(*)} e e)} = 1 \text{ in SM}$$

[LHCb '14,'17]

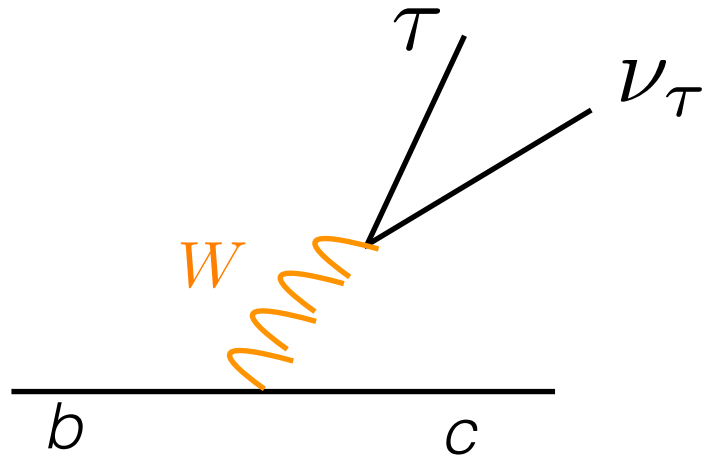
$R_K = 0.745_{-0.074}^{+0.090} \pm 0.036$	$q^2 \in [1 : 6] \text{ GeV}^2$	$\longrightarrow 2.6\sigma$
$R_{K^*}^{\text{low}} = 0.660_{-0.070}^{+0.110} \pm 0.024$	$q^2 \in [0.045 : 1.1] \text{ GeV}^2$	$\longrightarrow 2.1\sigma$
$R_{K^*}^{\text{cntr}} = 0.685_{-0.069}^{+0.113} \pm 0.047$	$q^2 \in [1.1 : 6] \text{ GeV}^2$	$\longrightarrow 2.4\sigma$

$$\begin{aligned} \Phi &\equiv d \text{BR}(B_s \rightarrow \phi \mu \mu) / dq^2 \Big|_{q^2 \in [1:6] \text{ GeV}^2} && [\text{LHCb '15}] \\ &= (2.58_{-0.31}^{+0.33} \pm 0.08 \pm 0.19) \times 10^{-8} \text{ GeV}^{-2} && (\text{exp}) \\ &= (4.81 \pm 0.56) \times 10^{-8} \text{ GeV}^{-2} && (\text{SM}) \end{aligned}$$

3σ

Lepton non-universality

► Exciting discrepancies observed in charged current B decays



$$\mathcal{H}^{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{cb} (1 + C^{\text{NP}}) (\bar{c}_L \gamma_\mu b_L) (\bar{\tau}_L \gamma^\mu \nu_{\tau L})$$

$$R(D^{(*)}) \equiv \frac{\text{BR}(B \rightarrow D^{(*)} \tau \nu)}{\text{BR}(B \rightarrow D^{(*)} \ell \nu)}, \quad \ell \in \{e, \mu\}$$

$$R(D) = (1.34 \pm 0.17) \times R(D)_{\text{SM}}, \quad R(D^*) = (1.23 \pm 0.07) \times R(D^*)_{\text{SM}}$$

2.2σ

3.3σ

[HFAG]

combined deviation

$\sim 4\sigma$

Lepton non-universality

► Constraints from other modes

[LHCb '17]

$$\text{BR}(B_s \rightarrow \mu\mu) = \begin{array}{l} (3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9} \quad (\text{exp.}) \\ \underline{(3.65 \pm 0.23) \times 10^{-9}} \quad (\text{SM}) \end{array}$$

well in agreement

$$\text{BR}(B \rightarrow K^{(*)} \nu \bar{\nu}) < 1.6 \text{ (2.7)} \times 10^{-5}$$

$$\text{BR}(B^+ \rightarrow K^+ \mu^\pm \tau^\mp) < 4.5 \text{ (2.8)} \times 10^{-5}$$

$$\text{BR}(B_s \rightarrow \tau\tau) < 6.8 \times 10^{-3}$$

$$\text{BR}(B_c^- \rightarrow \tau^- \bar{\nu}) \lesssim 5\% \quad [\text{Grinstein et.al '16}]$$

Quite challenging to explain all anomalies together by evading all the bounds.

Lepton non-universality

► NP operators with 2nd & 3rd generation fields

$$\mathcal{H}^{\text{NP}} = A_1 (\bar{Q}_{2L} \gamma_\mu L_{3L}) (\bar{Q}_{3L} \gamma^\mu L_{3L}) + A_2 (\bar{Q}_{2L} \gamma_\mu Q_{3L}) (\bar{\tau}_R \gamma^\mu \tau_R)$$

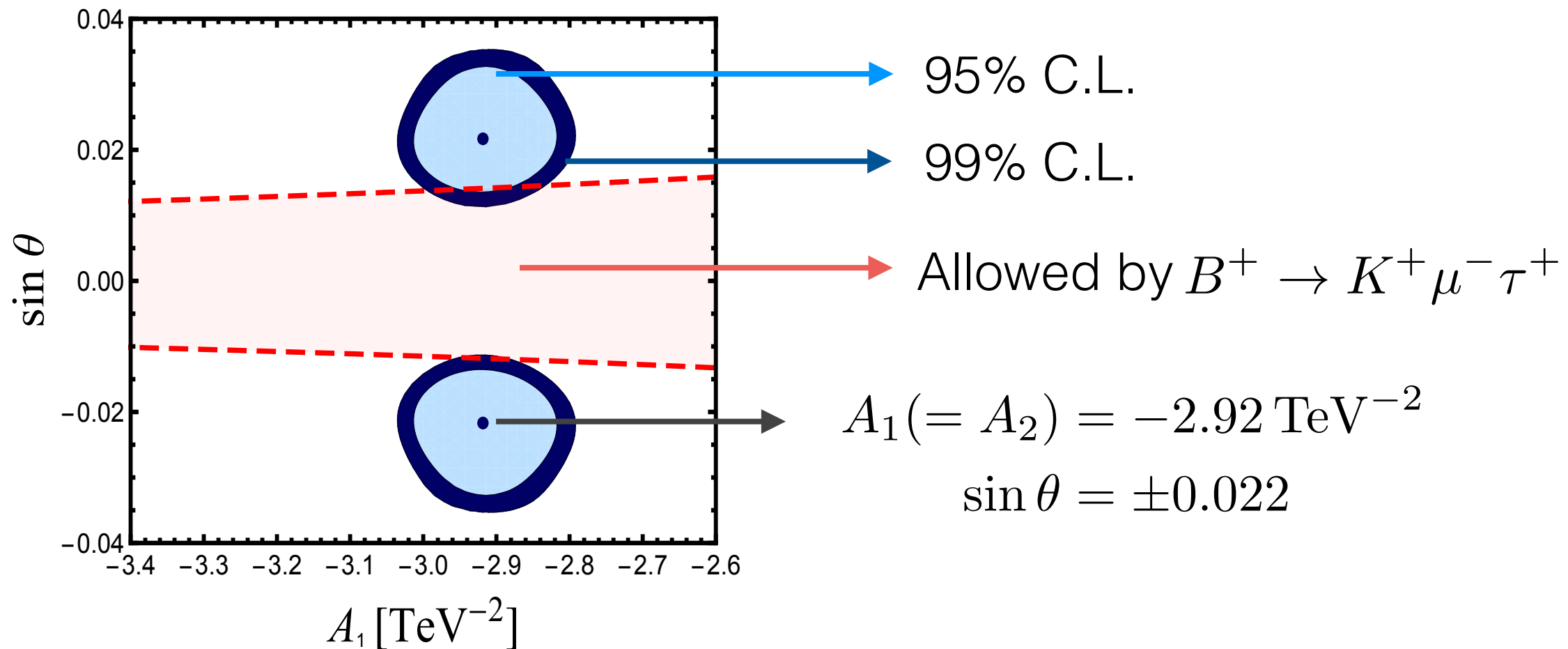
► Directly contributes to $R(D^{(*)})$

► Diagonalisation of Hamiltonian for lepton part through small mixing angle θ : interaction basis  mass basis

$$\tau = \cos \theta \tau' + \sin \theta \mu'$$

Contribution to $b \rightarrow s \mu \mu$ is generated

Lepton non-universality



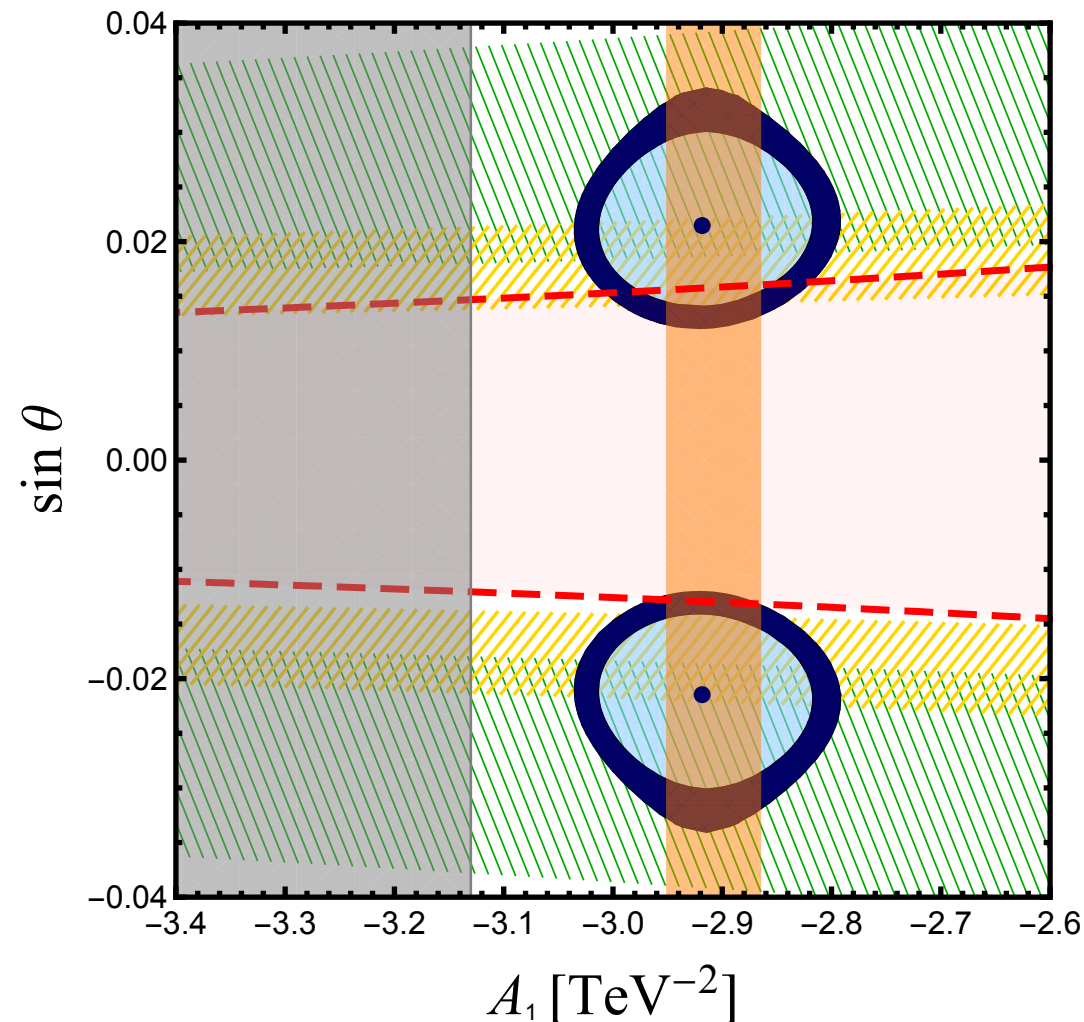
$$\chi^2_{\text{SM}}/\text{d.o.f} \simeq 6.6 \quad \longrightarrow \quad \chi^2_{\text{allowed region}}/\text{d.o.f} \simeq 3$$

✓
 agreement
 within
 2σ level

$$R_K \simeq 0.86, \quad R_{K^*}^{\text{cntr}} \simeq 0.88, \quad R_{K^*}^{\text{low}} \simeq 0.90,$$

$$R(D^{(*)}) \simeq 1.25 \times R(D^{(*)})_{\text{SM}}, \quad \Phi \simeq 4.1 \times 10^{-8} \text{ GeV}^{-2}.$$

Lepton non-universality



Allowing 20% breaking

$$A_2 = 4A_1/5$$

from quantum corrections
or unknown dynamics of the
UV completion of the model

- $R_{K^*}^{\text{cntr}}$
- R_K
- $R_{D^{(*)}}$
- $B^+ \rightarrow K^+ \mu^- \tau^+$
(allowed)
- $B_s \rightarrow \tau \tau$
(disallowed)

$$\chi_{\text{SM}}^2/\text{d.o.f} \simeq 6.6 \quad \longrightarrow \quad \chi_{\text{allowed region}}^2/\text{d.o.f} \simeq 2$$

✓
agreement
within
 1σ level

$$R_K \simeq 0.80, \quad R_{K^*}^{\text{cntr}} \simeq 0.83, \quad R_{K^*}^{\text{low}} \simeq 0.88,$$

$$R(D^{(*)}) \simeq 1.24 \times R(D^{(*)})_{\text{SM}}, \quad \Phi \simeq 3.8 \times 10^{-8} \text{GeV}^{-2}$$

Lepton non-universality

► Another discrepancy at $b \rightarrow c$ charged current

[LHCb '17]

$$R_{J/\psi} \equiv \frac{\text{BR}(B_c \rightarrow J/\psi \tau \nu)}{\text{BR}(B_c \rightarrow J/\psi \mu \nu)}$$
$$= (2.5 \pm 0.97) \times R_{J/\psi}^{\text{SM}} \longrightarrow < 2\sigma$$



In the same direction as of $R(D^{(*)})$



considered operators can also explain

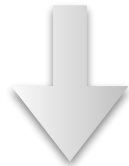
► $SU(2)_L$ triplet type operators are also explored

[1712.01593]

Summary

Popular approaches

✓ Combine all $b \rightarrow s$ transitions



many decay modes i.e. **observables**

+

more **hadronic uncertainties**

+

conservative assumption of
non-factorisable contributions

✓ Focusing on low q^2 region

Our approach

✓ Most general parametric form of
SM amplitude

+

$B \rightarrow K^* \ell^+ \ell^-$ **observables**

+

eliminate **hadronic uncertainties**



no/minimal dependency on
form-factors & independent of
non-factorisable contributions

✓ Conclusion derived at endpoint

Summary

- ☑ Formalism developed to include all possible effects within SM

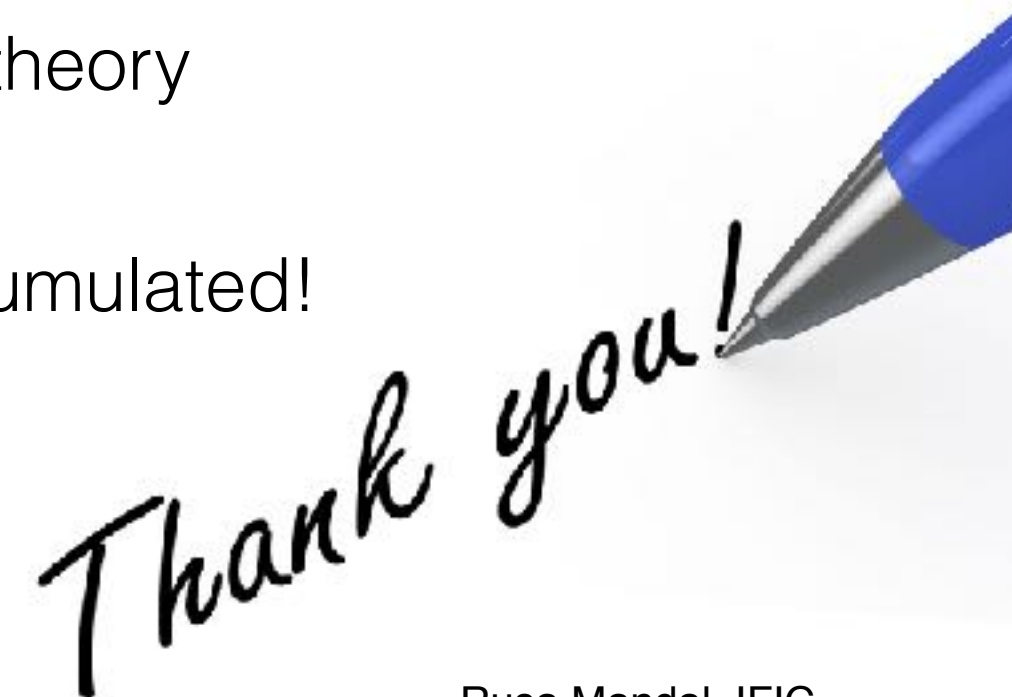
- ☑ Strong evidence of RH currents derived at endpoint limit —
 - ▶ systematics studied by varying polynomial order & bin no.
 - ▶ finite K^* width effect is considered
 - ▶ resonance effects increase the deviation

Summary

- ☑ Several hints of lepton non universality are observed by various experimental groups
- ☑ In terms of effective operators we show a possible explanation to all the anomalies together
 - ▶ The model has only two new parameters
 - ▶ It predicts some interesting signatures in the context of B decays such as $B_s \rightarrow \tau\tau$, $B \rightarrow K^{(*)}\mu\tau$
- ☑ Opens up way to construct UV complete theory
- ☑ Fluctuation? Wait for more data to be accumulated!

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Thank you!

Back Up

Complex part of amplitudes

► SM amplitude $\mathcal{A}_\lambda^{L,R} = (\tilde{C}_9^\lambda \mp C_{10})\mathcal{F}_\lambda - \tilde{\mathcal{G}}_\lambda$

► Complex part $\varepsilon_\lambda \equiv \text{Im}(\tilde{C}_9^\lambda)\mathcal{F}_\lambda - \text{Im}(\tilde{\mathcal{G}}_\lambda)$

► Iterative solutions

$$\varepsilon_\perp = \frac{\sqrt{2}\pi\Gamma_f}{(r_0 - r_\parallel)\mathcal{F}_\perp} \left[\frac{A_9\mathbf{P}_1}{3\sqrt{2}} + \frac{A_8\mathbf{P}_2}{4} - \frac{A_7\mathbf{P}_1\mathbf{P}_2r_\perp}{3\pi\hat{C}_{10}} \right],$$

$$\varepsilon_\parallel = \frac{\sqrt{2}\pi\Gamma_f}{(r_0 - r_\parallel)\mathcal{F}_\perp} \left[\frac{A_9r_0}{3\sqrt{2}r_\perp} + \frac{A_8\mathbf{P}_2r_\parallel}{4\mathbf{P}_1r_\perp} - \frac{A_7\mathbf{P}_2r_\parallel}{3\pi\hat{C}_{10}} \right],$$

$$\varepsilon_0 = \frac{\sqrt{2}\pi\Gamma_f}{(r_0 - r_\parallel)\mathcal{F}_\perp} \left[\frac{A_9\mathbf{P}_1r_0}{3\sqrt{2}\mathbf{P}_2r_\perp} + \frac{A_8r_\parallel}{4r_\perp} - \frac{A_7\mathbf{P}_1r_0}{3\pi\hat{C}_{10}} \right].$$

Complex part of amplitudes

q^2 range in GeV^2	$\varepsilon_{\perp}/\sqrt{\Gamma_f}$	$\varepsilon_{\parallel}/\sqrt{\Gamma_f}$	$\varepsilon_0/\sqrt{\Gamma_f}$
$0.1 \leq q^2 \leq 0.98$	-0.048 ± 0.116	-0.047 ± 0.103	0.020 ± 0.111
$1.1 \leq q^2 \leq 2.5$	-0.010 ± 0.078	-0.010 ± 0.078	0.078 ± 0.172
$2.5 \leq q^2 \leq 4.0$	-0.009 ± 0.079	-0.008 ± 0.080	-0.025 ± 0.212
$4.0 \leq q^2 \leq 6.0$	-0.026 ± 0.097	0.014 ± 0.093	0.032 ± 0.234
$6.0 \leq q^2 \leq 8.0$	-0.011 ± 0.088	-0.046 ± 0.078	-0.132 ± 0.129
$11.0 \leq q^2 \leq 12.5$	-0.011 ± 0.050	0.038 ± 0.074	-0.078 ± 0.114
$15.0 \leq q^2 \leq 17.0$	-0.0003 ± 0.067	-0.027 ± 0.071	0.020 ± 0.072
$17.0 \leq q^2 \leq 19.0$	0.006 ± 0.076	-0.090 ± 0.090	-0.040 ± 0.088

$\frac{\varepsilon_{\lambda}}{\sqrt{\Gamma_f}}$ values with errors are consistent with zero

Resonances

Parametrization in Wilson coefficient C_9

[Kruger, Sehgal '96]

$$g(m_c, q^2) = -\frac{8}{9} \ln \frac{m_c}{m_b} - \frac{4}{9} + \frac{q^2}{3} P \int_{4\hat{m}_D^2}^{m_b^2} \frac{R_{\text{had}}^{c\bar{c}}(x)}{x(x - q^2)} dx + i \frac{\pi}{3} R_{\text{had}}^{c\bar{c}}(q^2)$$

$$R_{\text{had}}^{c\bar{c}}(q^2) = R_{\text{cont}}^{c\bar{c}}(q^2) + \sum_{V=J/\psi, \psi' \dots} \frac{9q^2}{\alpha} \frac{\text{Br}(V \rightarrow l^+ l^-) \Gamma_{\text{total}}^V \Gamma_{\text{had}}^V}{(q^2 - m_V^2)^2 + m_V^2 \Gamma_{\text{total}}^V} e^{i\delta_V}$$

Solutions

$$\begin{aligned}
 R_{\perp} &= \pm \frac{3}{2} \frac{\left(\frac{1-\xi}{1+\xi}\right) F_{\perp} + \frac{1}{2} P_1 Z_1}{P_1 A_{\text{FB}}} & F_{\perp} &= 2\zeta (1+\xi)^2 (1+R_{\perp}^2) \\
 R_{\parallel} &= \pm \frac{3}{2} \frac{\left(\frac{1+\xi}{1-\xi}\right) P_1 F_{\parallel} + \frac{1}{2} Z_1}{A_{\text{FB}}} & F_{\parallel} P_1^2 &= 2\zeta (1-\xi)^2 (1+R_{\parallel}^2) \\
 R_0 &= \pm \frac{3}{2\sqrt{2}} \frac{\left(\frac{1+\xi}{1-\xi}\right) P_2 F_L + \frac{1}{2} Z_2}{A_5} & F_L P_2^2 &= 2\zeta (1-\xi)^2 (1+R_0^2) \\
 P_2 &= \frac{\left(\frac{1-\xi}{1+\xi}\right) 2P_1 A_{\text{FB}} F_{\perp}}{\sqrt{2} A_5 \left(\left(\frac{1-\xi}{1+\xi}\right) 2F_{\perp} + Z_1 P_1 \right) - Z_2 P_1 A_{\text{FB}}} & A_{\text{FB}} P_1 &= 3\zeta (1-\xi^2) (R_{\parallel} + R_{\perp}) \\
 & & \sqrt{2} A_5 P_2 &= 3\zeta (1-\xi^2) (R_0 + R_{\perp})
 \end{aligned}$$

$$Z_1 = \sqrt{4F_{\parallel} F_{\perp} - \frac{16}{9} A_{\text{FB}}^2} \quad Z_2 = \sqrt{4F_L F_{\perp} - \frac{32}{9} A_5^2}$$

Effective operators

► Hamiltonian and relevant operators for $b \rightarrow s\mu\mu$

$$\mathcal{H}^{\text{eff}} = \frac{-4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i(\mu) \mathcal{O}_i(\mu) ,$$

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu}$$

$$\mathcal{O}_9 = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\mu} \gamma^\mu \mu)$$

$$\mathcal{O}_{10} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\mu} \gamma^\mu \gamma_5 \mu)$$

New contribution to
(axial)vector currents

$$C_9 \rightarrow C_9 + C_9^{\text{NP}}$$

$$C_{10} \rightarrow C_{10} + C_{10}^{\text{NP}}$$