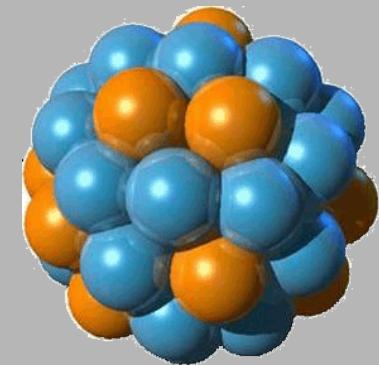


# Nuclear Structure Studies with High-Resolution In-Beam $\gamma$ -Spectroscopy

A.Gadea IFIC-CSIC Valencia

- Introduction to the physics
- Introduction to the in-beam technique
- Reactions for the Spectroscopy
- Measurement capabilities
- Instrumentation

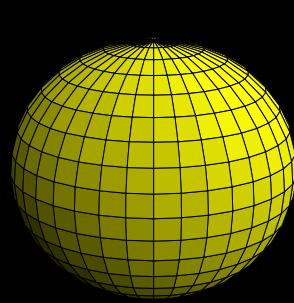


# The Atomic Nucleus

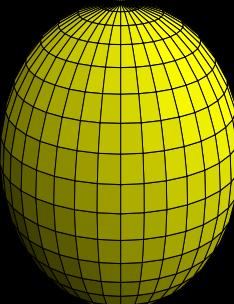
- The atomic nucleus is a complex fermionic system, based on two different particles, interacting via an effective force strongly influenced by in-medium effects.
- Nuclei are small enough that the quantum nature of its constituents determines its properties but large enough that macroscopic features begin to evolve.
- Nuclei have been the traditional objects for studying mesoscopic (many body) phenomena, as well as Open Quantum Systems in the limits of stability.

# Nuclear Collectivity

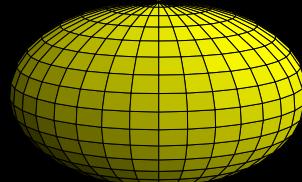
## Examples of Nuclear Shapes



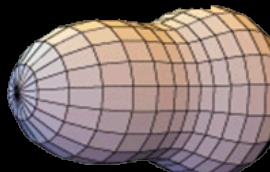
Spherical



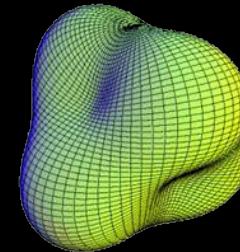
Prolate



Oblate



Octupole



Tetrahedric

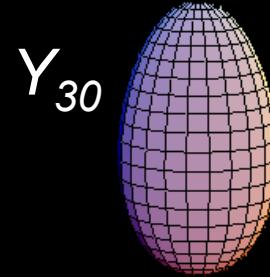
## Examples of Nuclear Shape Vibrations



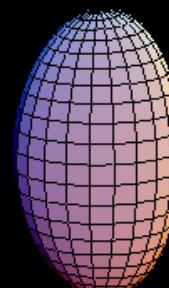
$Y_{20}$



$Y_{22}$



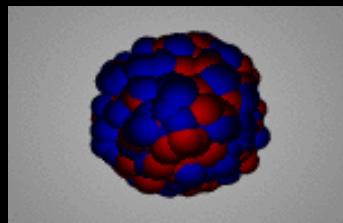
$Y_{30}$



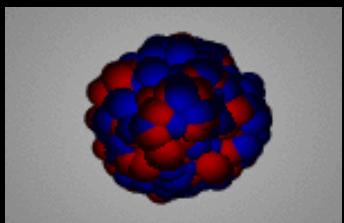
$Y_{31}$

...

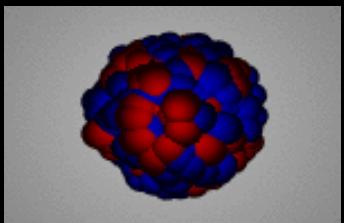
## Examples of Vibrational Collective Nuclei



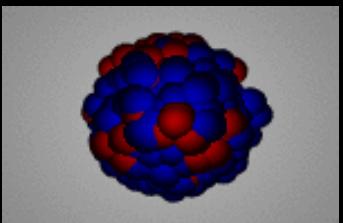
GMR  
(isoscalar)



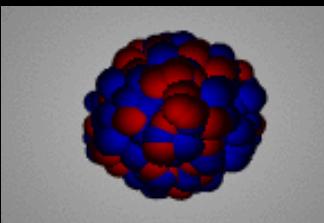
GMR  
(isovector)



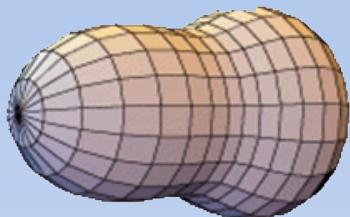
GDR  
(isovector)



GQR  
(isoscalar)

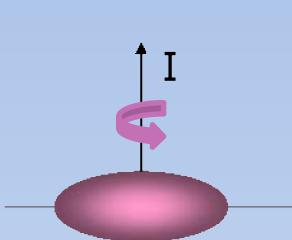
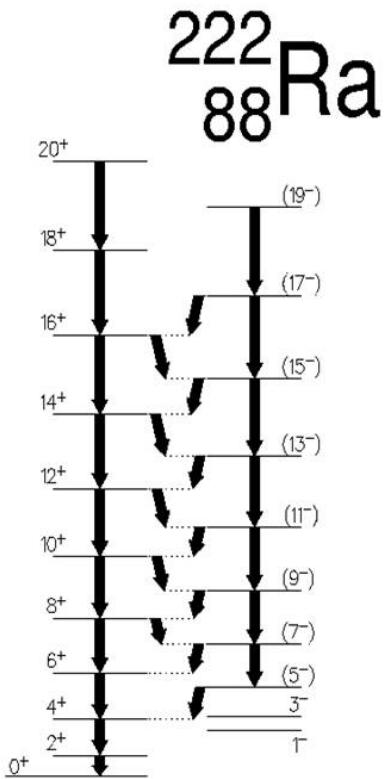


GQR  
(isovector)

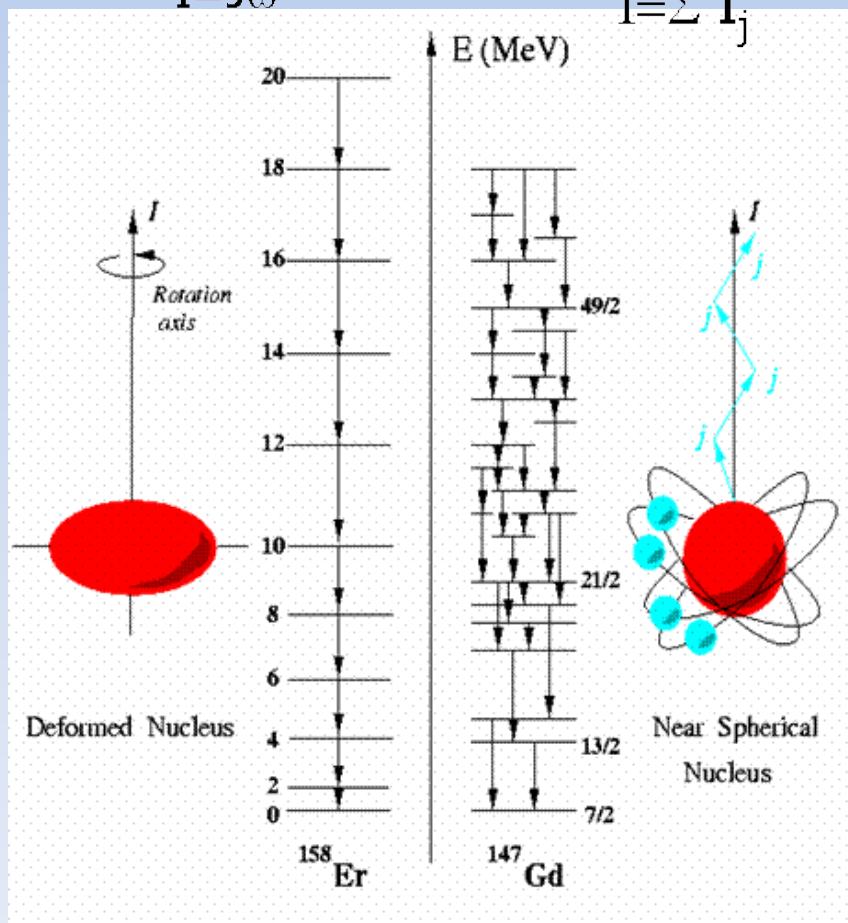


$$|\Psi\rangle = |\text{apple}\rangle$$

$$P|\Psi\rangle \neq |\Psi\rangle$$



$$I=J\oplus$$



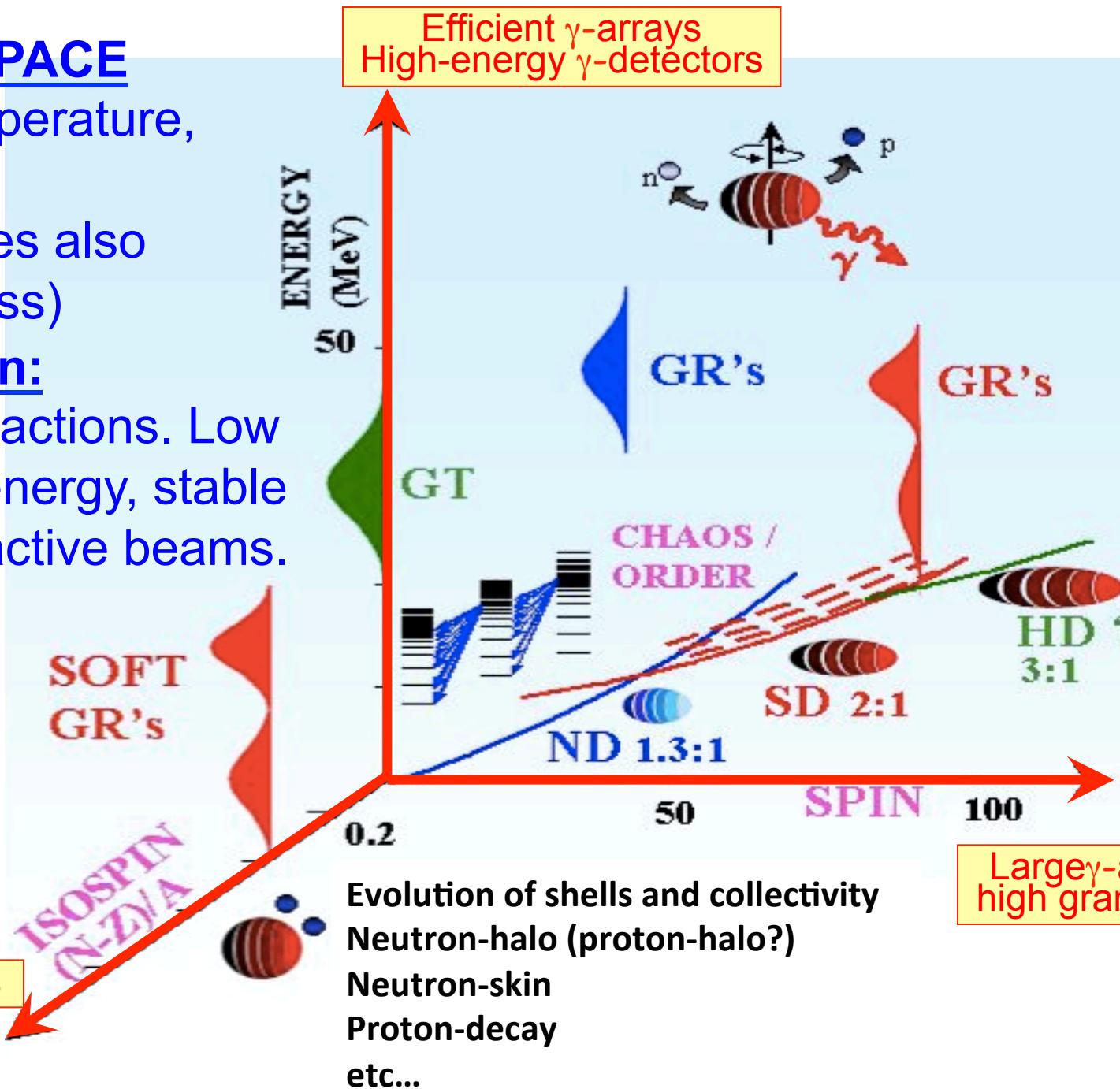
# PHASE SPACE

Spin, Temperature, Isospin.  
(Sometimes also strangeness)

## Population:

Nuclear reactions. Low and high energy, stable and radioactive beams.

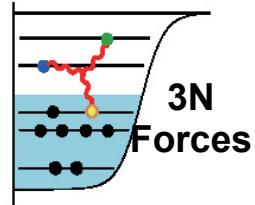
Exotic beams



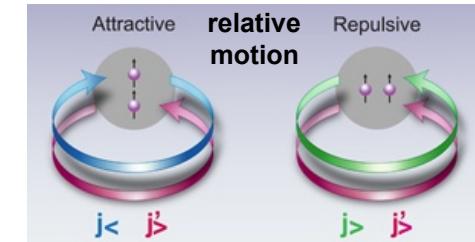
# Some Scientific Topics

## Organization of Nuclear Matter and Emerging Phenomena. In-media Fundamental Interactions, Origin and Evolution of Nuclear Matter

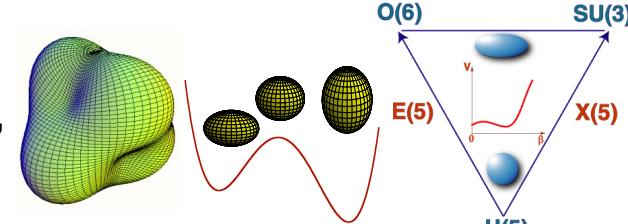
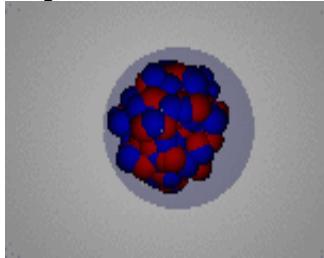
- **Shell Structure Far From Stability:** large nucleon asymmetry lead to shell modifications driven by the spin-isospin nucleon-nucleon interaction and close to the drip-line by the weakening of the spin-orbit interaction



- **Three Body Forces:** testing the role of three nucleon (3N) forces in the microscopic description of the atomic nucleus. Indications of important role in the vicinity of proton as well as neutron drip-lines.



- **Nuclear Shapes:** coexistence of different nuclear shapes, Large deformation, high-rank symmetries, phase transition, dynamic and critical point symmetries.



- **Spin-isospin Response Of Nuclei:** out-of-phase density oscillations of the neutron and proton fluids provided information on macroscopic nuclear properties associated with isovector fields.



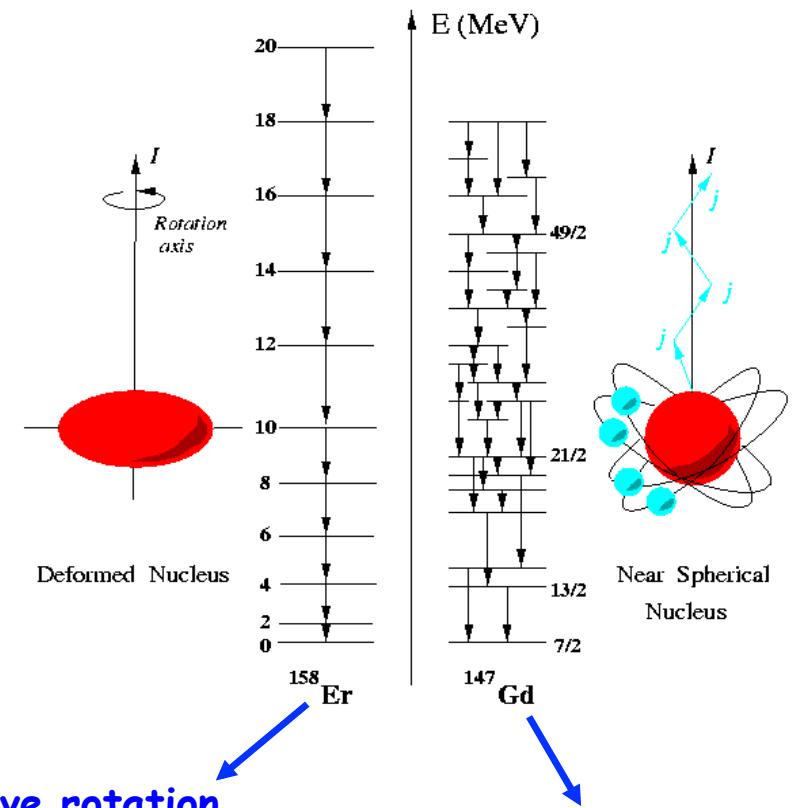
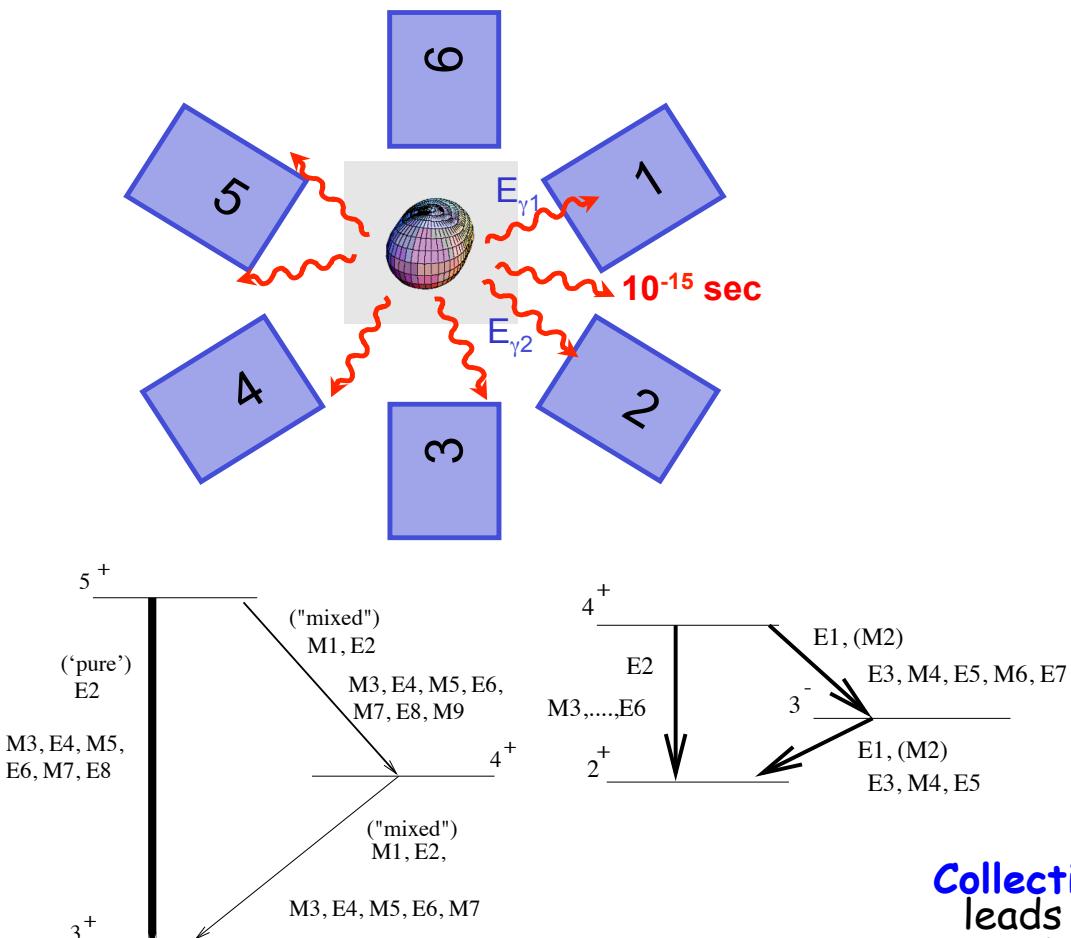
- **Nuclear Matter Appearance and Evolution:** nuclear astrophysics, explosive scenarios and the rp-process, the origin of the elements heavier than Iron and the r-process

- **and Clustering in Nuclei, New forms of nuclear pairing, In-Media isospin breaking interactions, Study of Open Quantum Systems, etc ...**

# In-Beam Spectroscopy Key Aspects

- Direct detection of the “prompt” de-excitation  $\gamma$ -rays emitted by the nucleus of interest
- The nucleus to be studied “must” be in a excited state:
  - The nucleus can be created in a excited state or
  - The nucleus must be excited during the reaction process
- The detection system are installed around the reaction point
  - Key factors are Efficiency, Peak-to-Total, i.e. signal-to-noise and Selectivity.
  - Reaction rates could by limited by the detector counting rates limit.
- In addition to the  $\gamma$ -ray detector, frequently, complementary detectors and devices are necessary to improve selectivity or to perform a particular measurement.

# In-beam Experiments and Nuclear Structure



**Collective rotation**  
leads to **regular**  
band structures

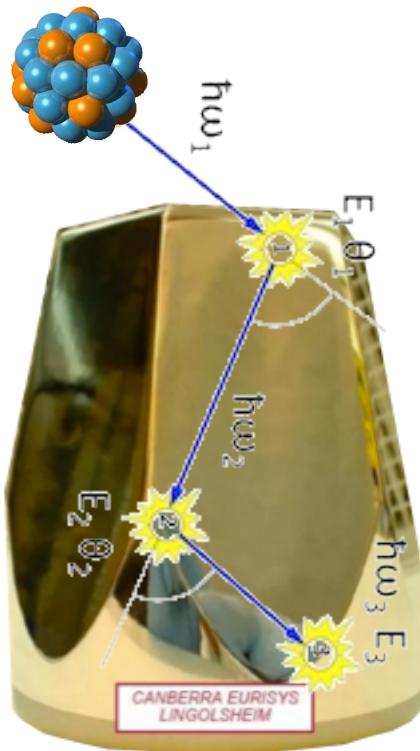
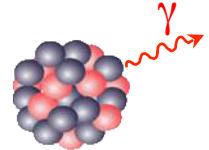
**Single-particle** generation  
of spin leads to an  
**irregular** level structure

$B(E/M\lambda)$

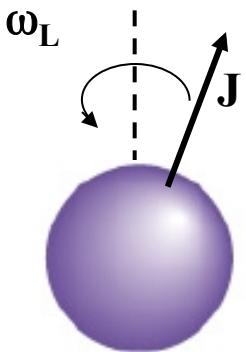
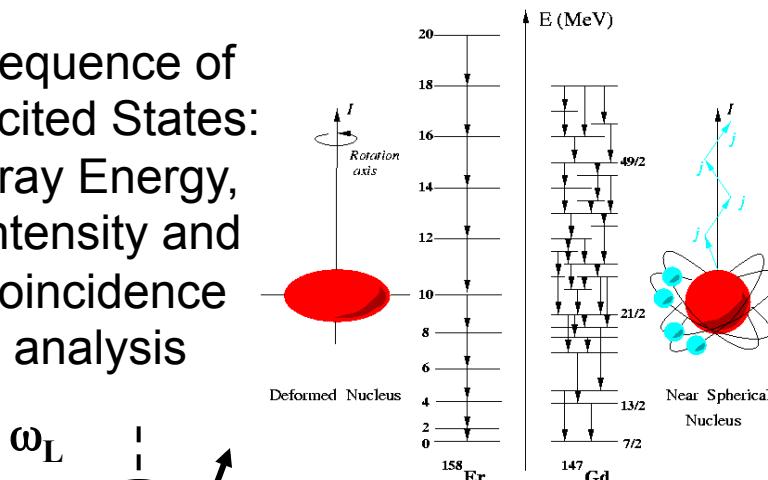
The decay probability is governed by the matrix element of the multipole operator

$$m_{fi}(\sigma L) = \int \Psi_f^* m(\sigma L) \Psi_i dv$$

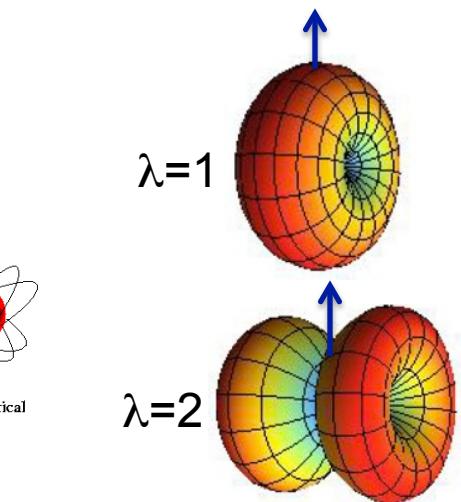
# High Resolution $\gamma$ -ray Spectroscopy



Sequence of  
Excited States:  
 $\gamma$ -ray Energy,  
intensity and  
coincidence  
analysis

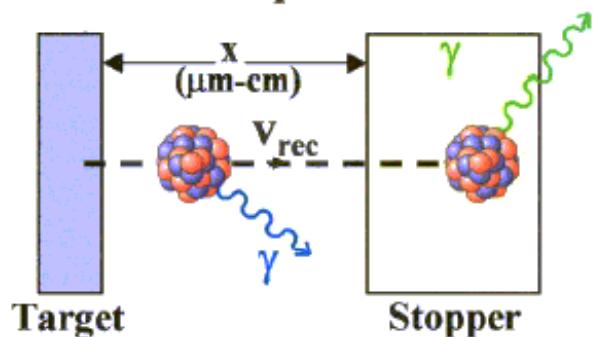


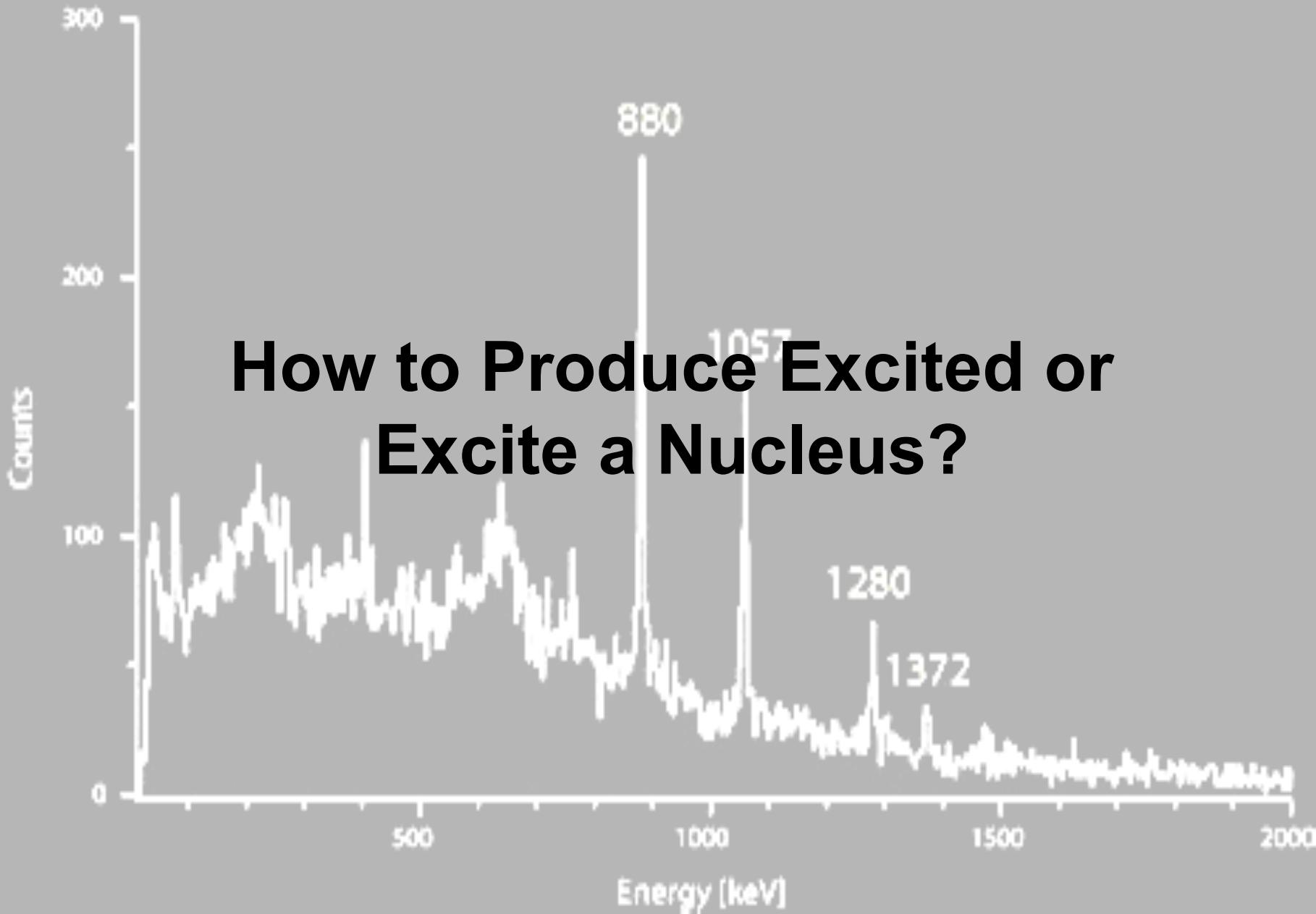
Nuclear  
Moments  
(e.g.: g-factors  
magnetic field)



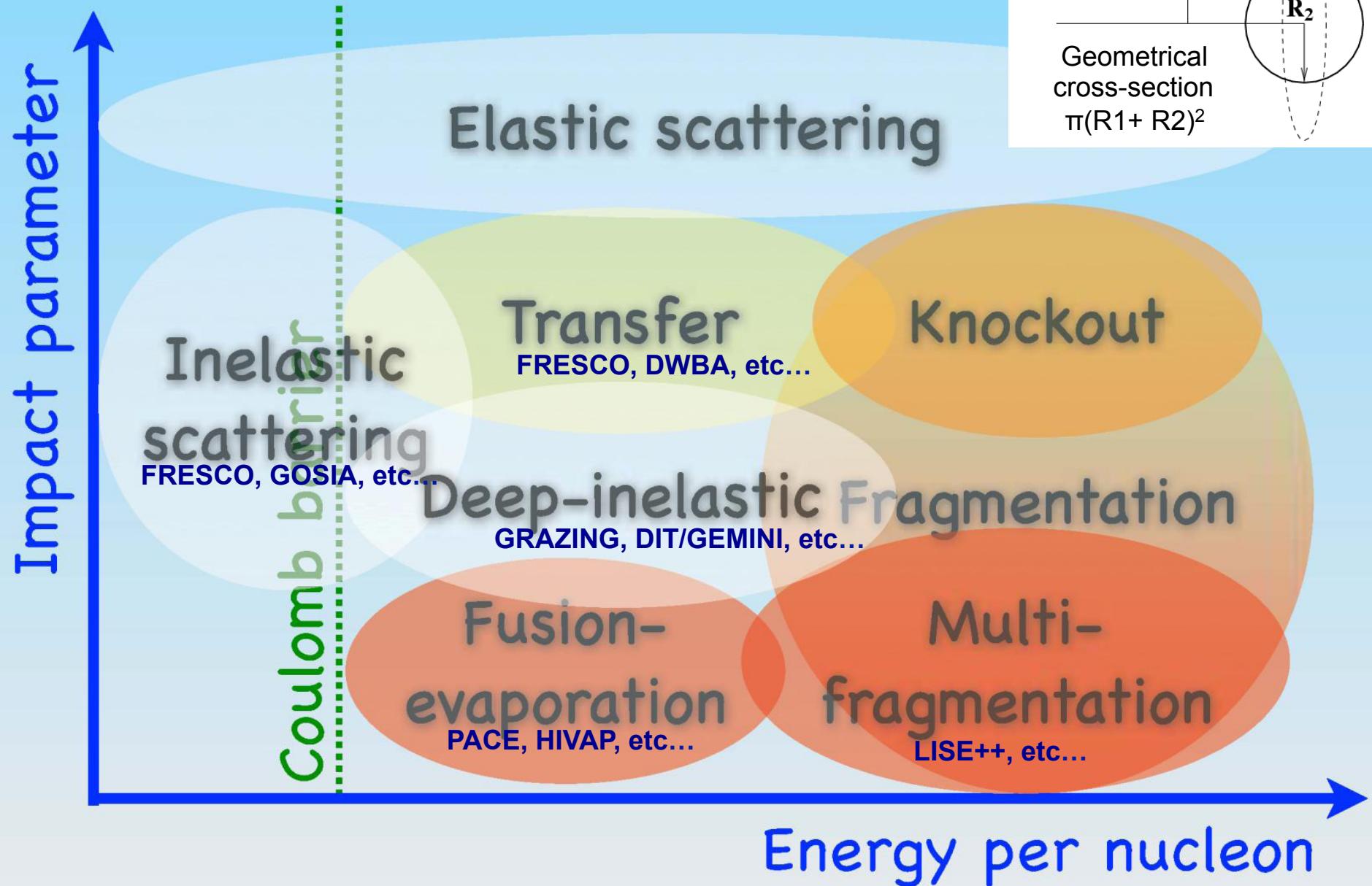
State Quantum  
numbers  $J^\pi$   
 $\gamma$ -ray angular  
distribution,  
correlations and linear  
polarization

Transition  
probabilities  
by Doppler or  
indirect methods  
 $B(E/M\lambda)$

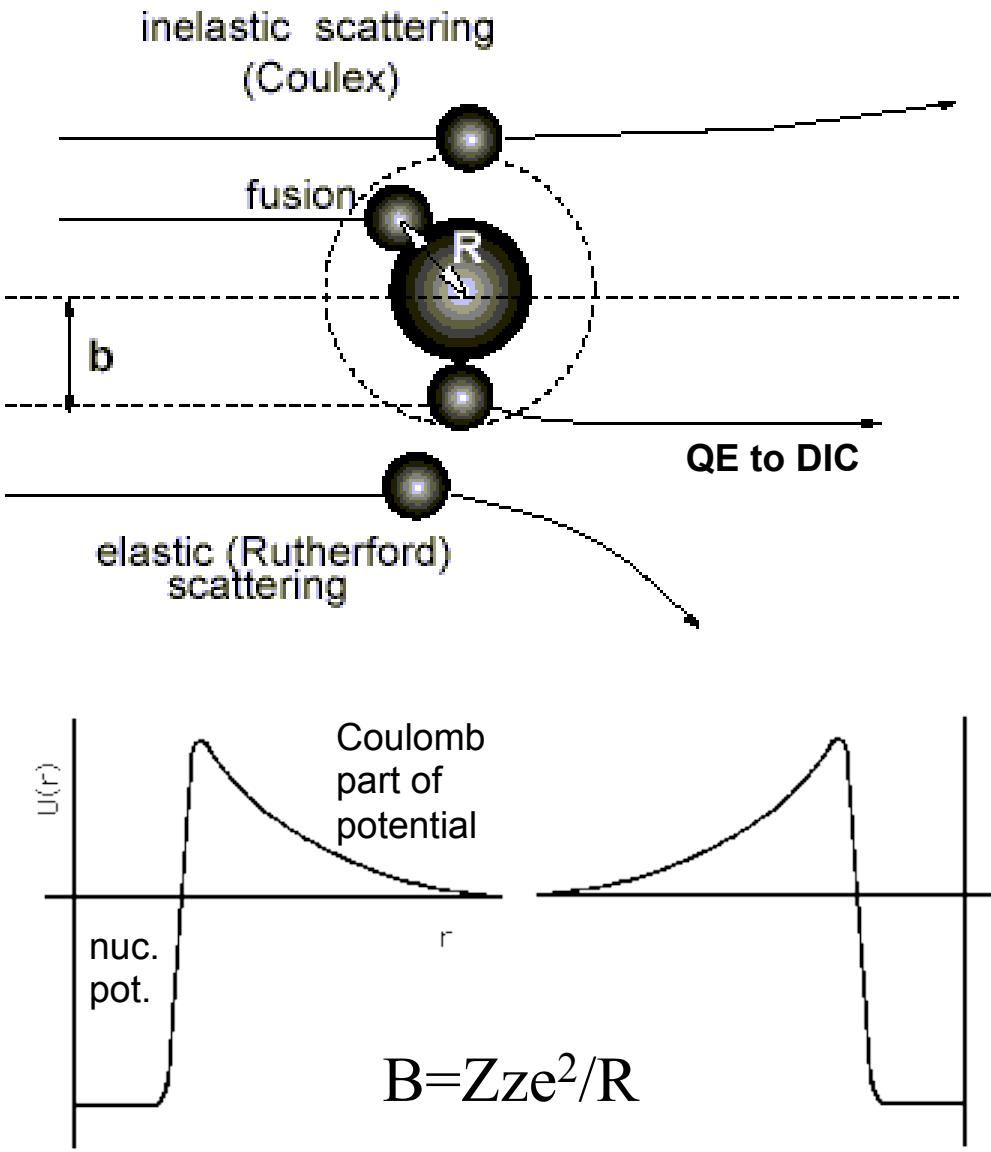




# Types of Nuclear Reactions



# Low Energy reaction mechanisms used for $\gamma$ -Spectroscopy (up to $\sim 10$ MeV.A)

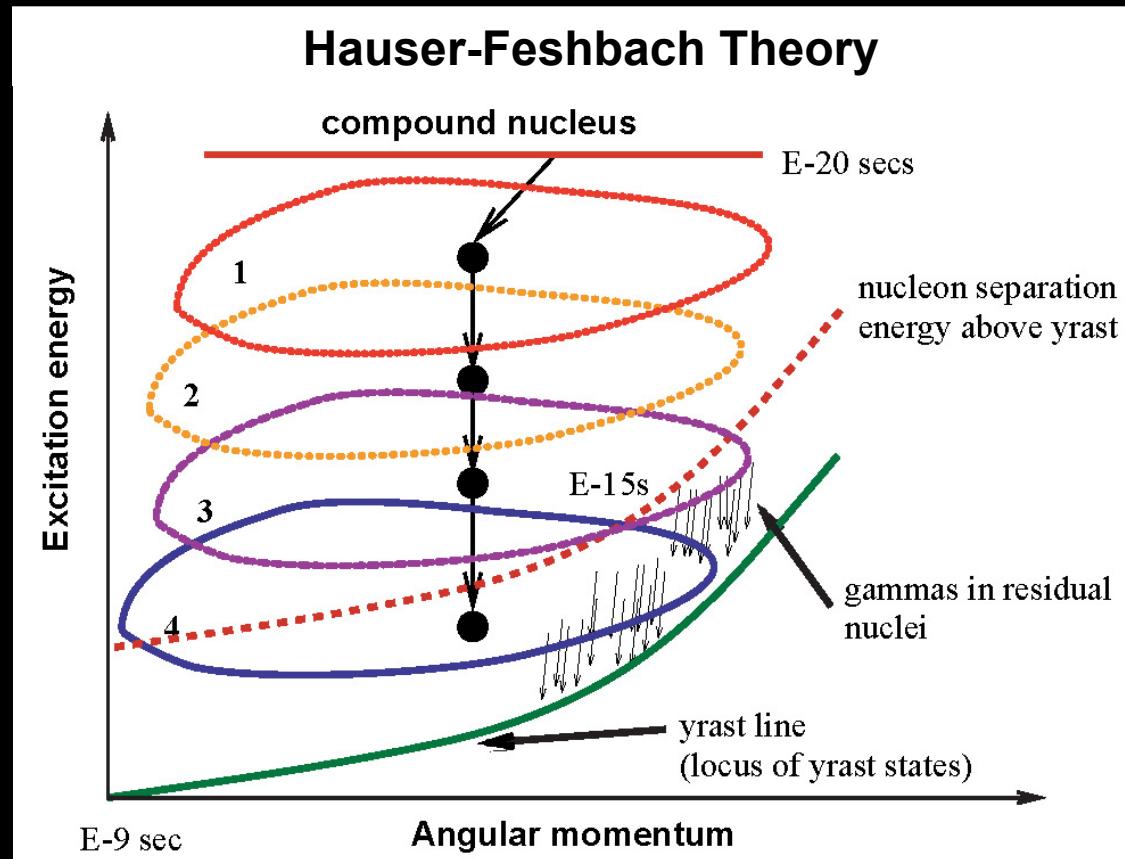
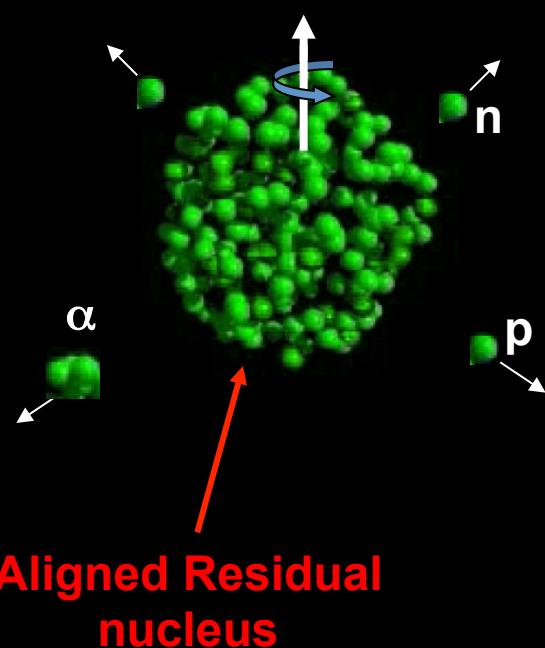
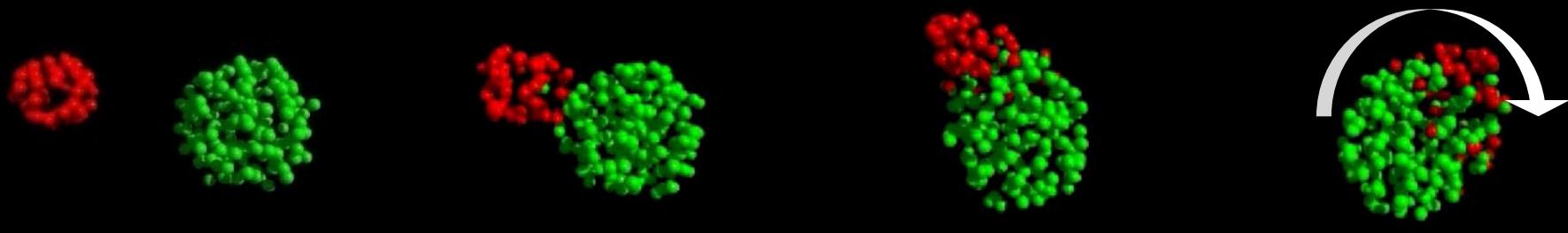


Smaller impact parameter "b"

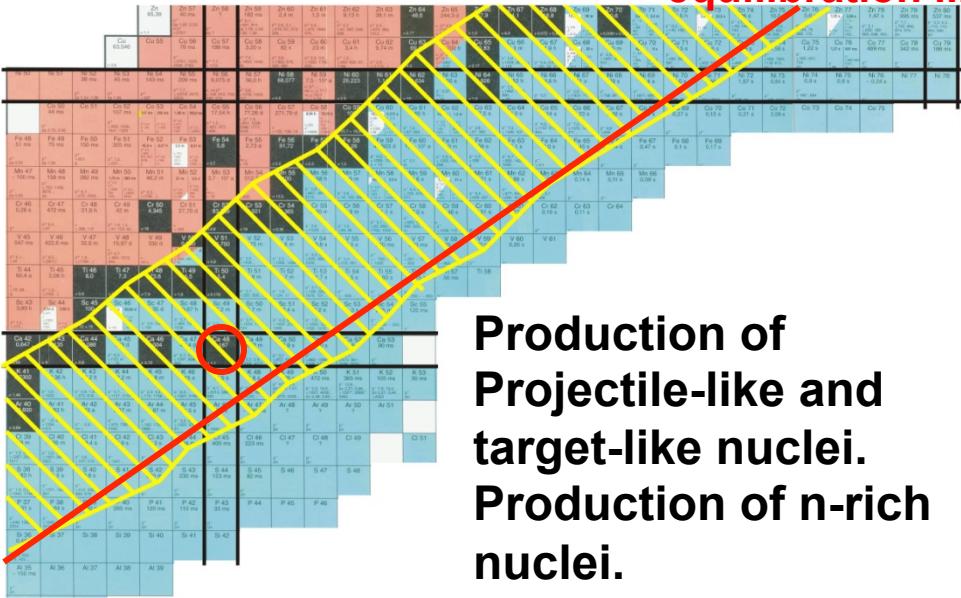
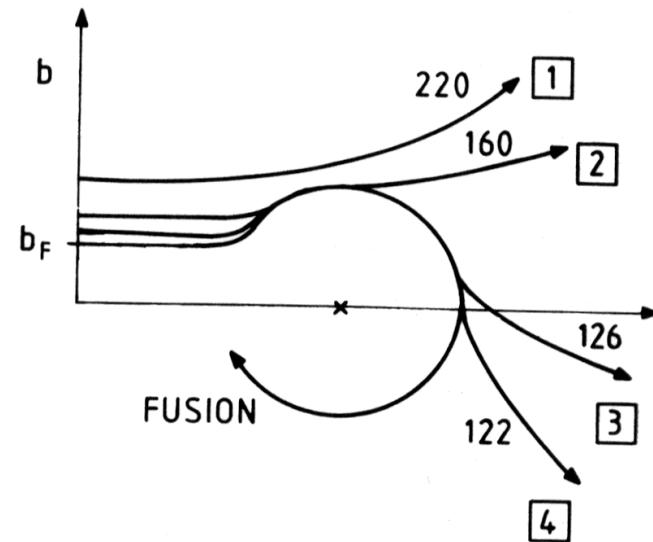
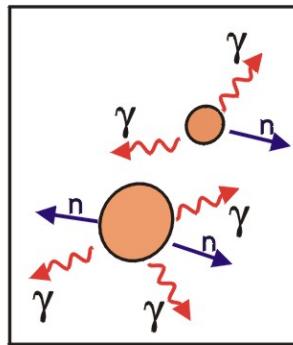
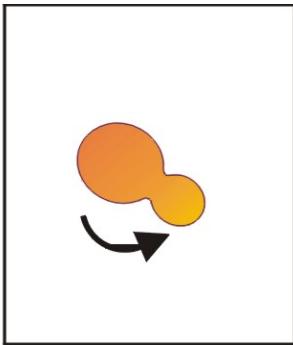
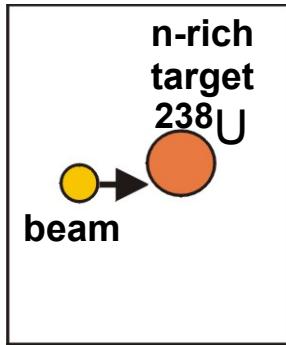
- Coulomb excitation and Inelastic scattering.
- Transfer and quasi-elastic processes (p,n capture...).
- Multi-nucleon transfer.
- Deep Inelastic Collisions.
- Quasi-fusion reactions.
- Fusion with light particles evaporation .
- Fusion with evaporation of Massive Fragments (IMF)
- Fusion-fission

Cross sections up to few barns typically from tens of mb to  $\mu$ b

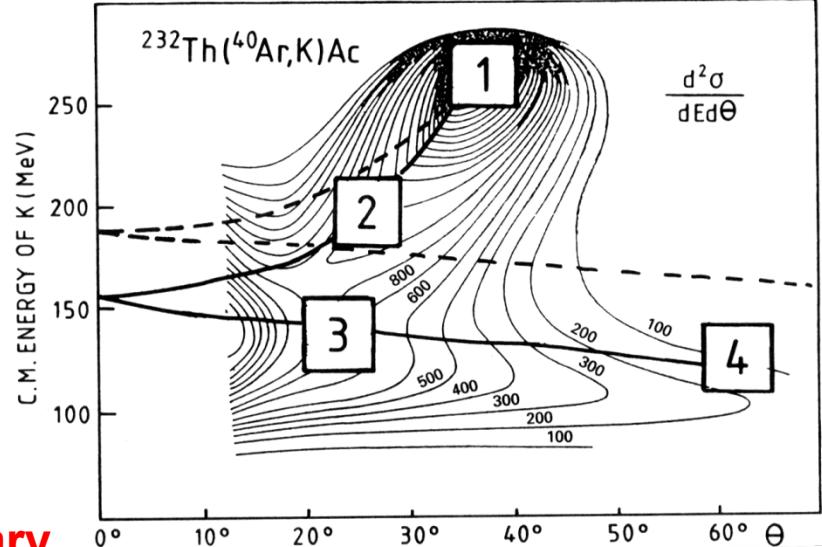
# Example: FUSION-EVAPORATION REACTIONS



# Example: GRAZING REACTIONS

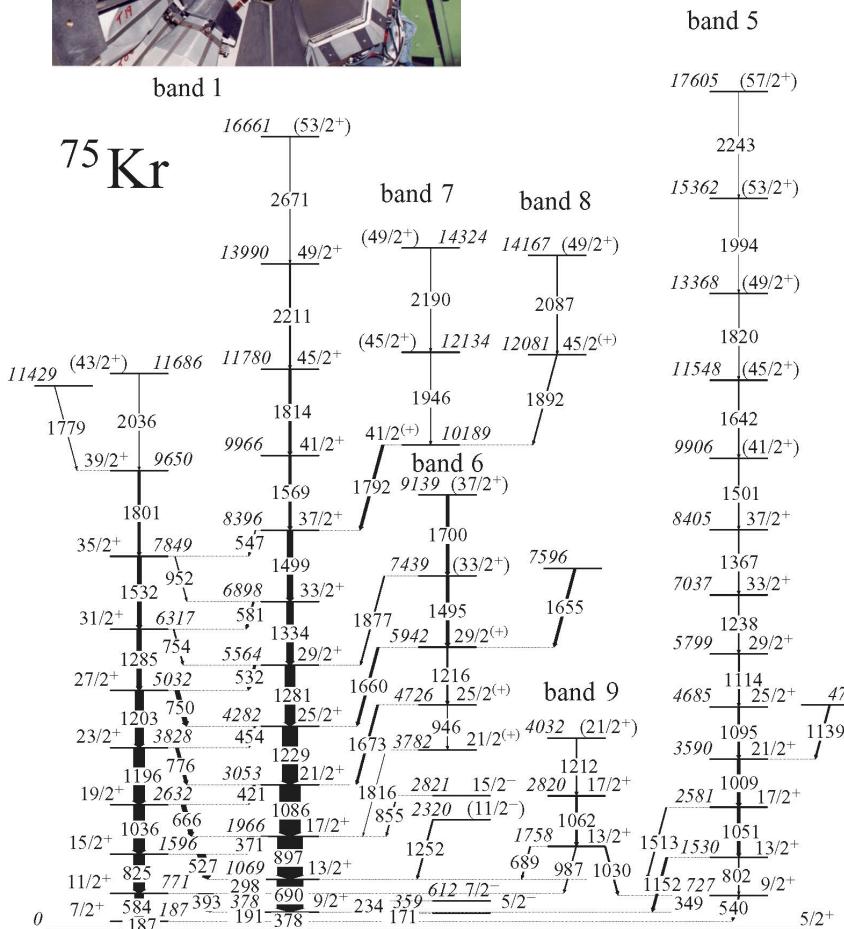
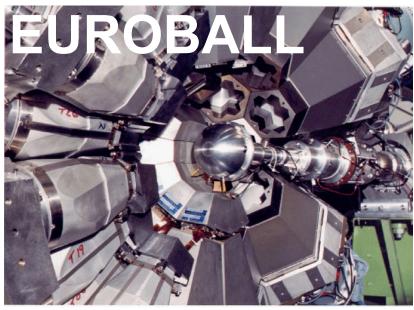


J. Wilczynski, Phys. Lett. 47B(1973) 484



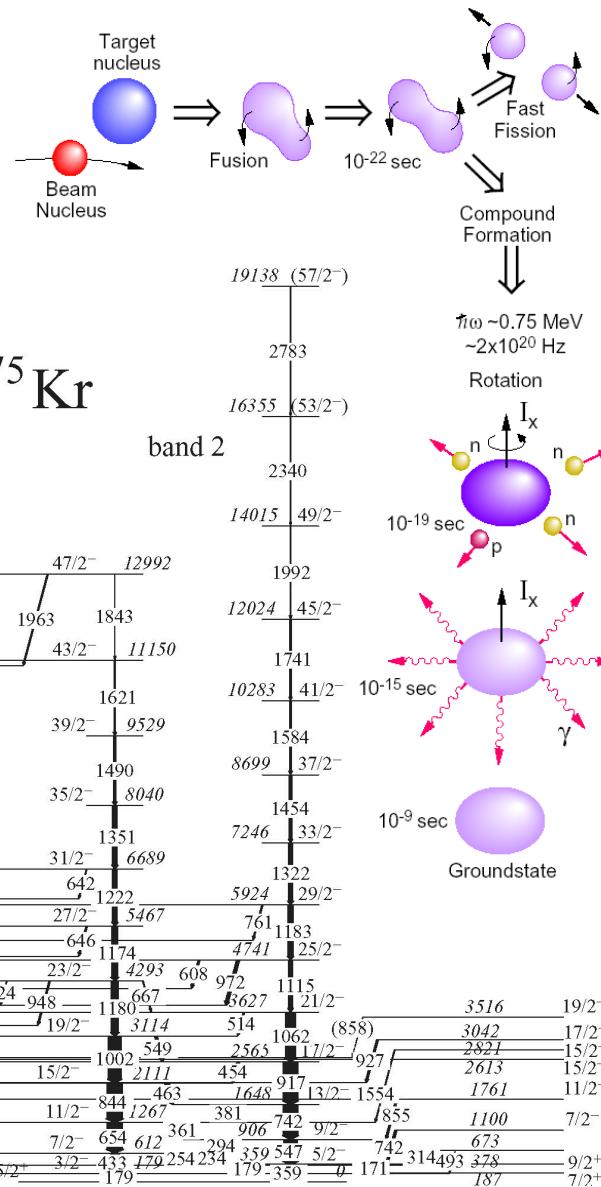
Identification of products with complementary detectors or by  $\gamma$ -spectroscopy of the partners is required

## Example: Spectroscopy with Fusion-Evaporation Reactions



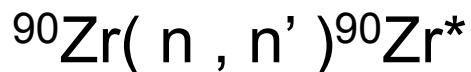
# $^{40}\text{Ca}(^{40}\text{Ca},4\text{pn})^{75}\text{Kr}^*$

States identified up to  $J=57/2$   
and 19 MeV excitation energy



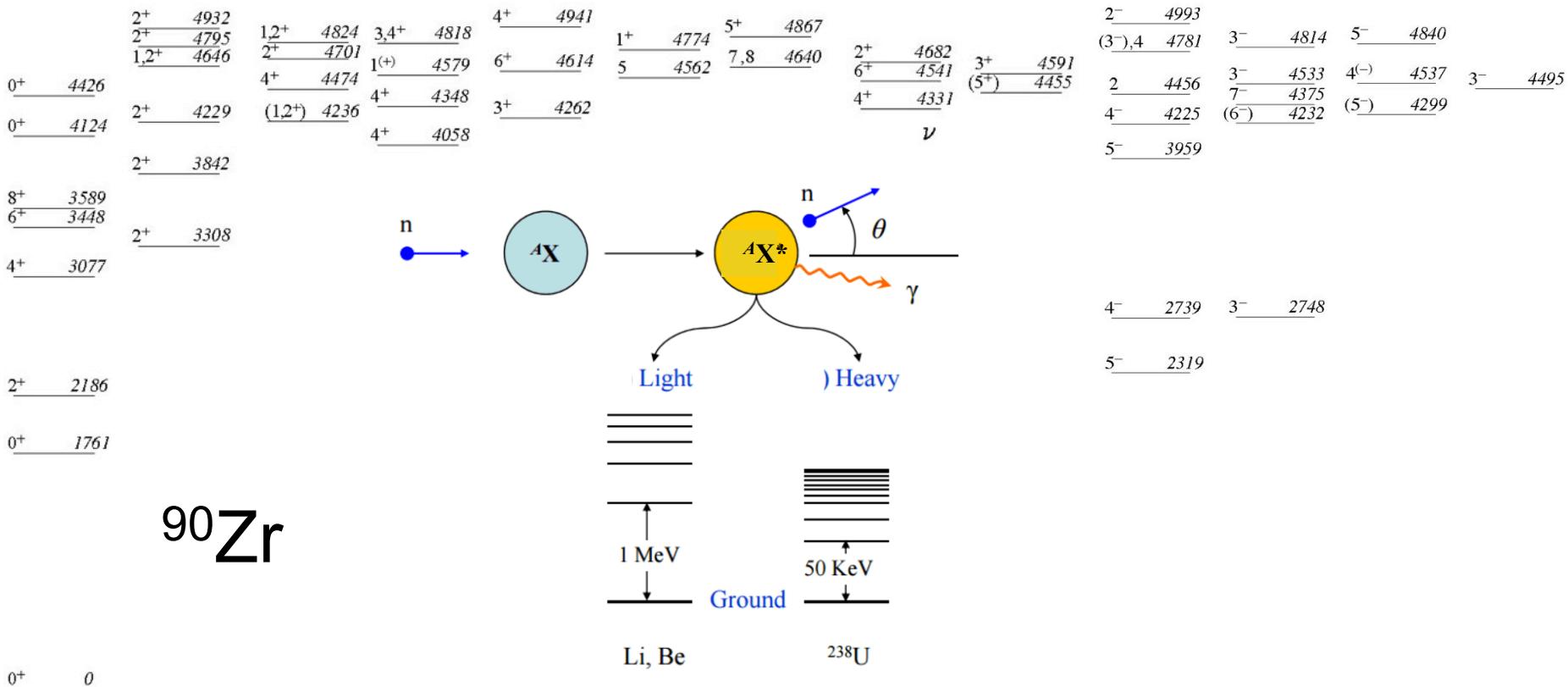
# Example: Spectroscopy with neutron Inelastic Scattering

LANSCE/WNR facility



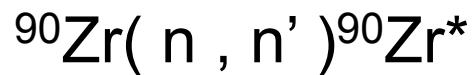
Neutron energy:  
2 to 12 MeV

States identified up to  $J \sim 6$   
and  $\sim 6$  MeV excitation energy



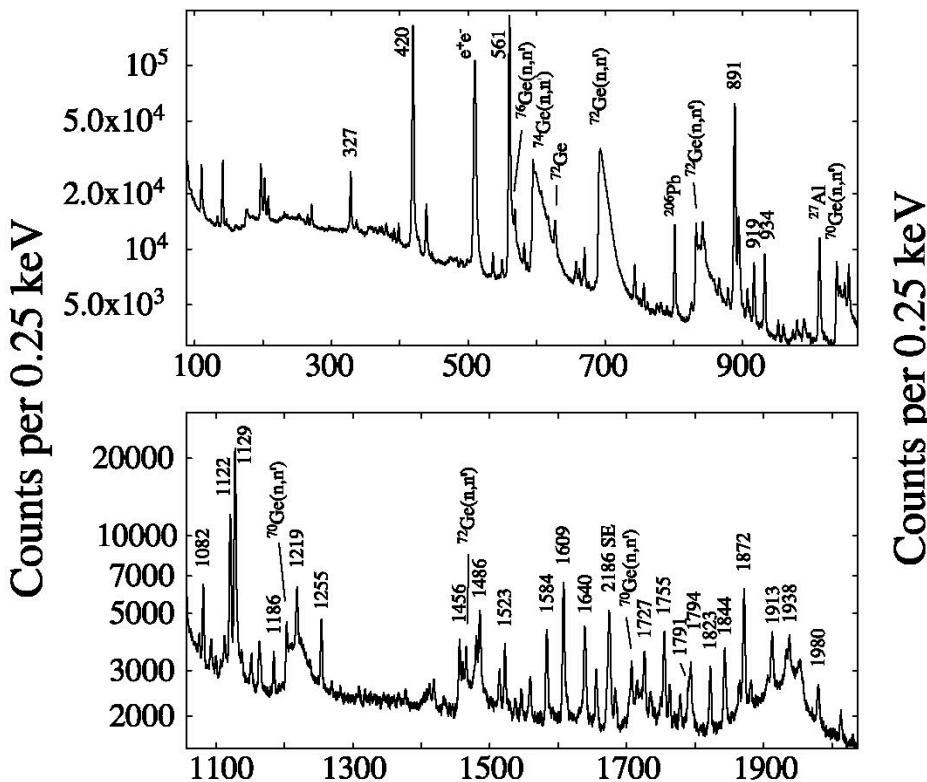
# Example: Spectroscopy with neutron Inelastic Scattering

LANSCE/WNR facility

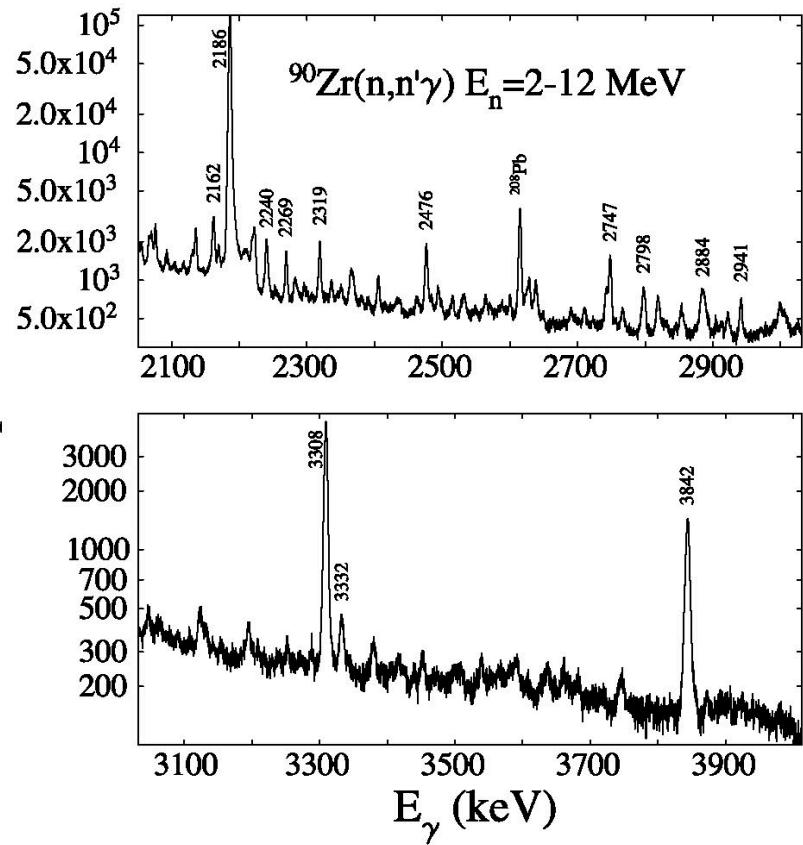


Neutron energy:  
2 to 12 MeV

States identified up to  $J \sim 6$   
and  $\sim 6$  MeV excitation energy



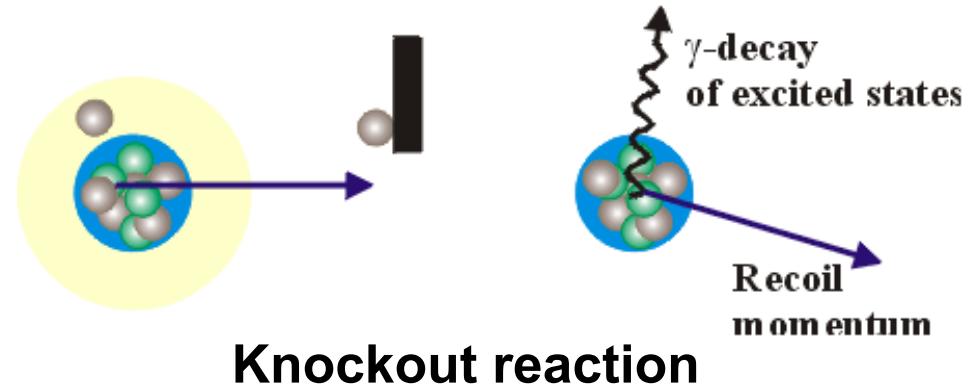
Counts per 0.25 keV



# High energy reaction mechanisms used for $\gamma$ -Spectroscopy (above $\sim 40$ MeV.A)

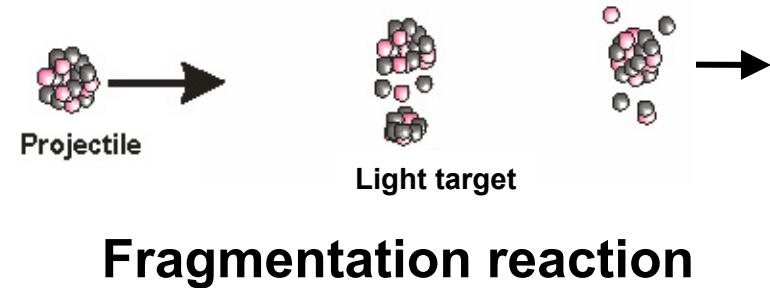
Generally used with exotic ion beams produced by fragmentation or fission at relativistic energies

- Relativistic (single step) Coulomb excitation
- Inverse proton scattering
- Knockout reactions
- Fragmentation reactions



Cross sections :

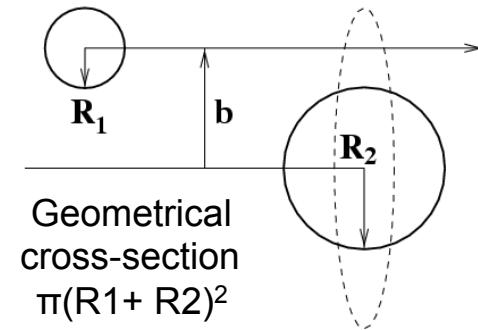
- up to 1 barn for Coulomb (large Z nuclei)
- tens of mbarn for proton scattering and 1 nucleon knockout,
- down to few mb for 2 nucleons knockout.
- smaller cross sections for fragmentation



Fragmentation reaction

# Yields from Cross-Section Estimates

- The Cross-Section estimate  $\sigma$  is given in barn i.e.  $10^{-28} \text{ m}^2 = 100 \text{ fm}$
- The yield of a reaction is proportional to the Cross-section, the number of atoms in the target and the atoms per second in the beam:
  - Cross-section are given in barn's ( $10^{-24} \text{ cm}^2$ )
  - Target thicknesses are usually given in  $\text{mg/cm}^2$
  - The beam intensity is given in particles per second (pps) or in particle nA (pnA).



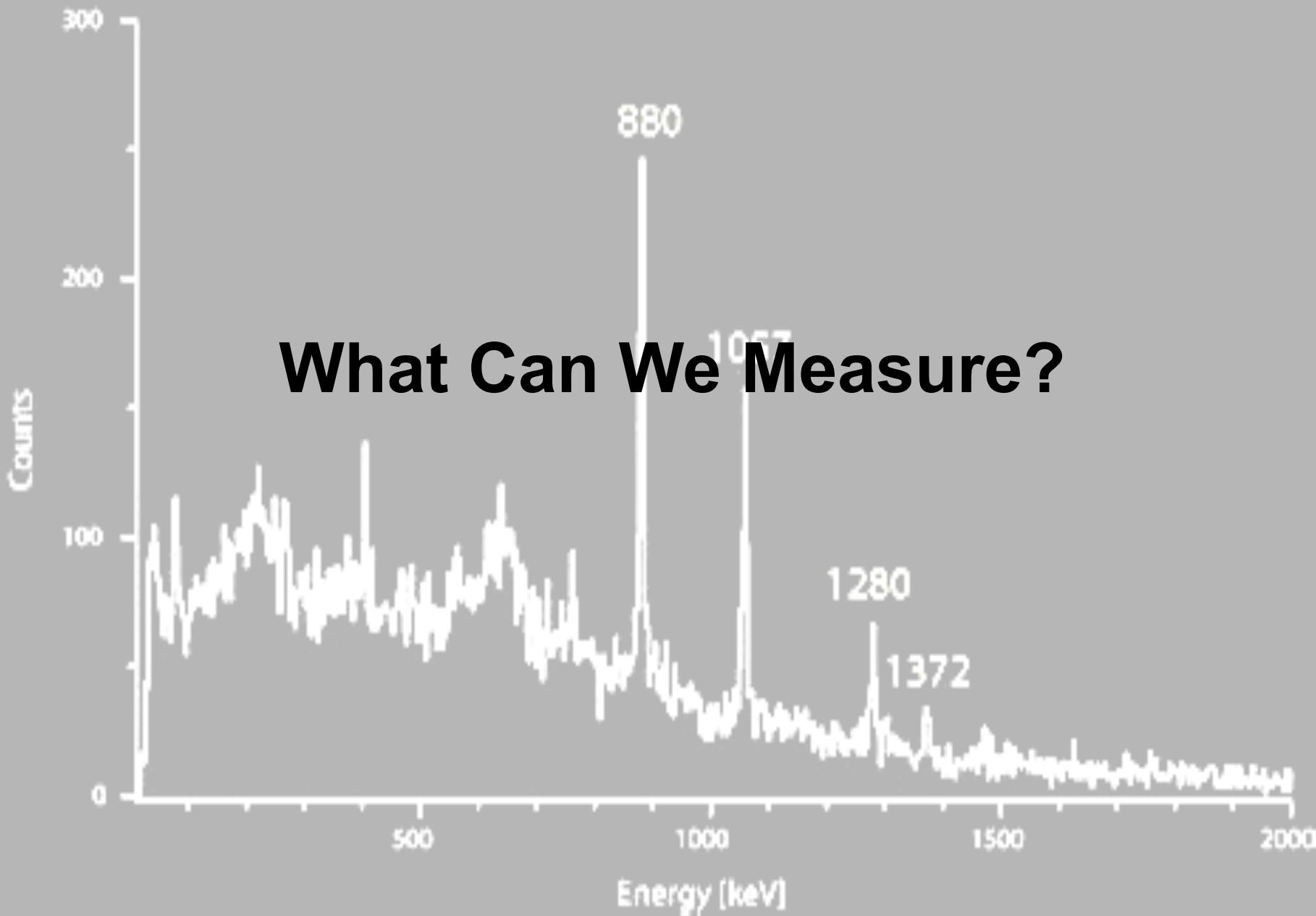
$$yield = \sigma (barn) \cdot 10^{-24} \left( \frac{cm^2}{barn} \right) \cdot \frac{Target \left( \frac{g}{cm^2} \right)}{Mol\ weight \ (g)} \cdot N_A \cdot Beam \left( \frac{Atoms}{s} \right)$$

The production cross-section does not imply that a transition or particular phenomena will be observed with such intensity, e.g. superdeformed bands 1/100 yield

# Further Information on Reactions

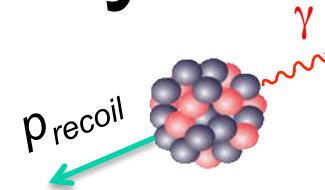
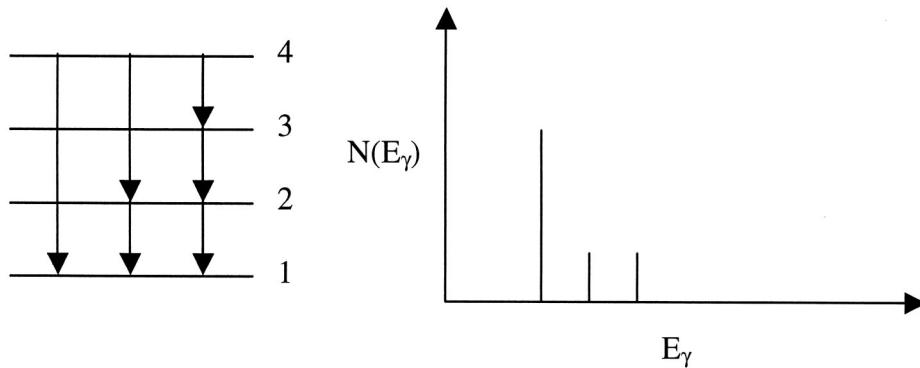
## Cross-Section Determination:

- Inelastic, Transfer Reactions, Grazing etc...
  - <http://nrv.jinr.ru/nrv/>
- GOSIA (Coulomb excitation)
  - <http://www.pas.rochester.edu/~cline/Gosia/>
- Fusion-Evaporation Reactions
  - PACE in LISE++: <http://lise.nscl.msu.edu/lise.html>
  - HIVAP: W. Reisdorf, Z. Phys. A **300**, 227 (1981)
- Relativistic Coulomb Excitation
  - DWEIKO: C.Bertulani et al. Comput. Phys. Commun. 152 (2003) 317.
- Fragmentation, Knock-out etc..
  - LISE++: <http://lise.nscl.msu.edu/lise.html>



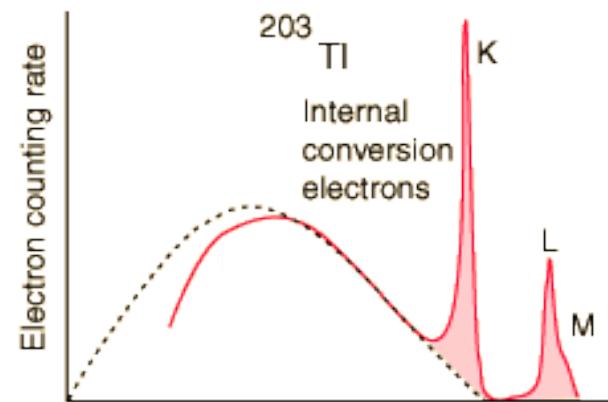
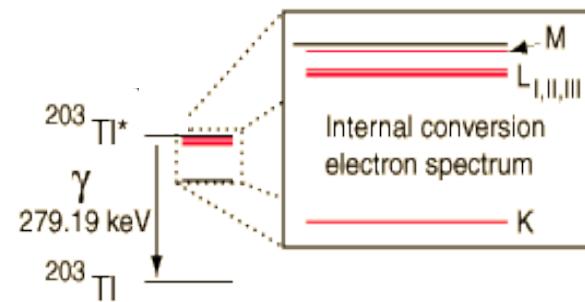
# Electromagnetic decay

- There are three types of electromagnetic decay,  $\gamma$ -ray emission, internal conversion (IC) and pair production ( $E>1.02\text{MeV}$ ).
- In electromagnetic decays  $\Delta N=\Delta Z=\Delta A=0$ , with just a lowering of the excitation energy of the nucleus.
- In  $\gamma$ -ray emission, the emitted photons are mono-energetic and have an energy corresponding to almost all of the energy difference between the final and initial state of the system.



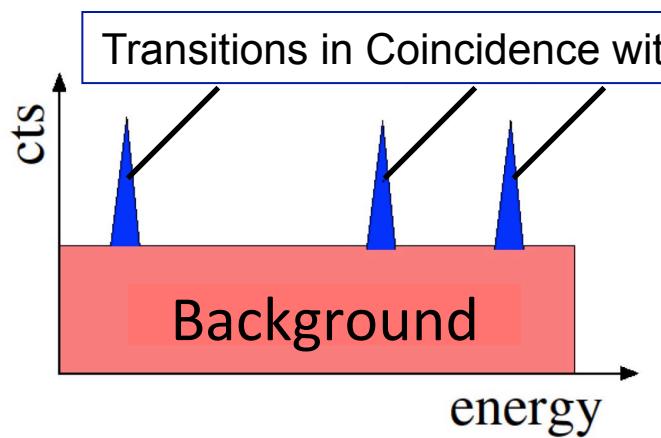
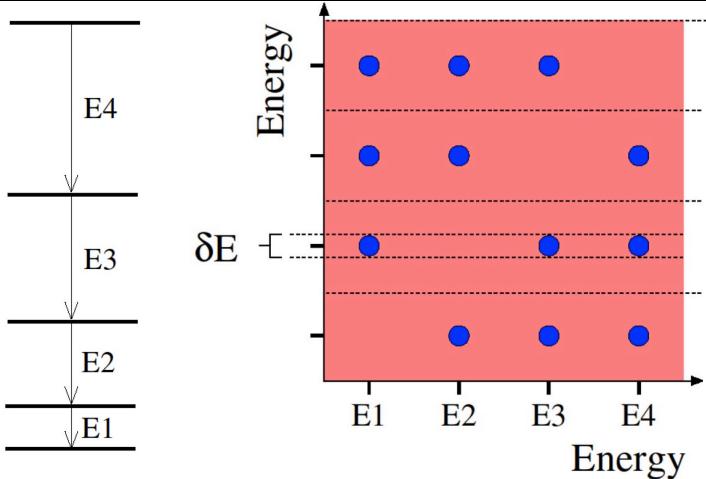
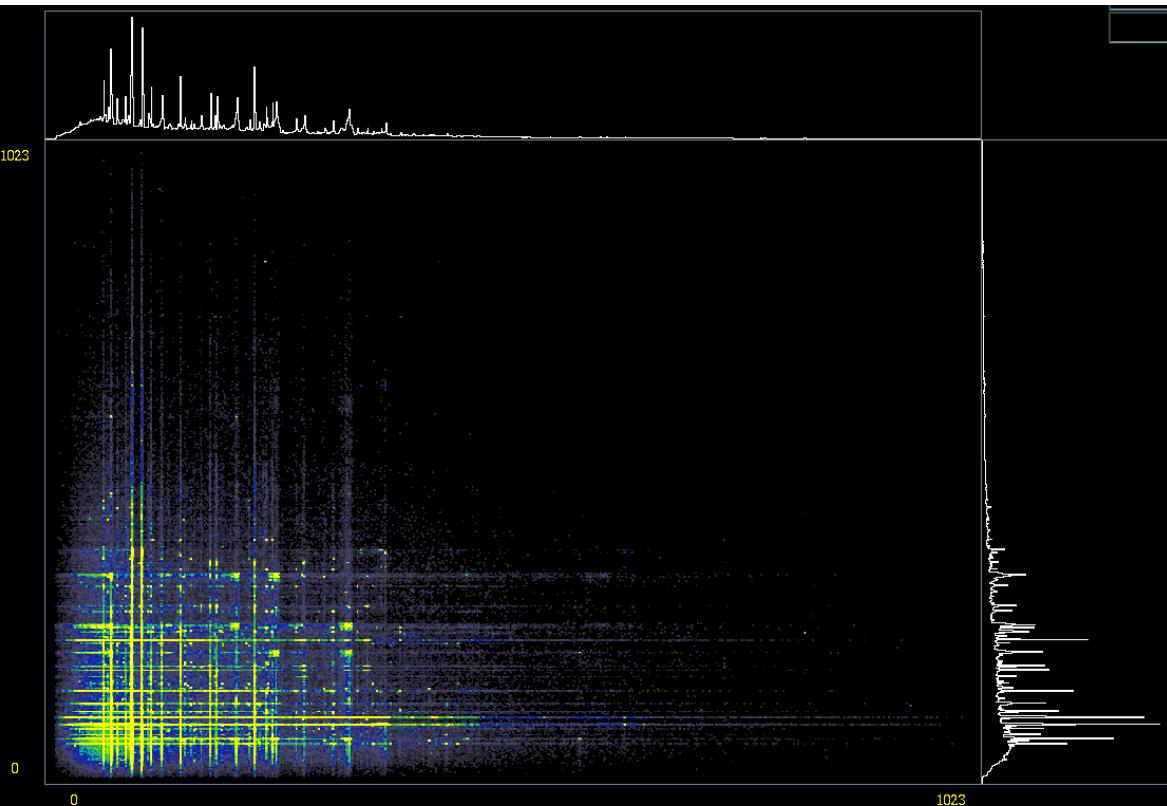
$$p_\gamma = p_{\text{recoil}}$$

$$T_{\text{recoil}} = \frac{p_{\text{recoil}}^2}{2m_{\text{recoil}}} = \frac{p_\gamma^2}{2m_{\text{recoil}}} = \frac{E_\gamma^2}{2m_{\text{recoil}}c^2}$$



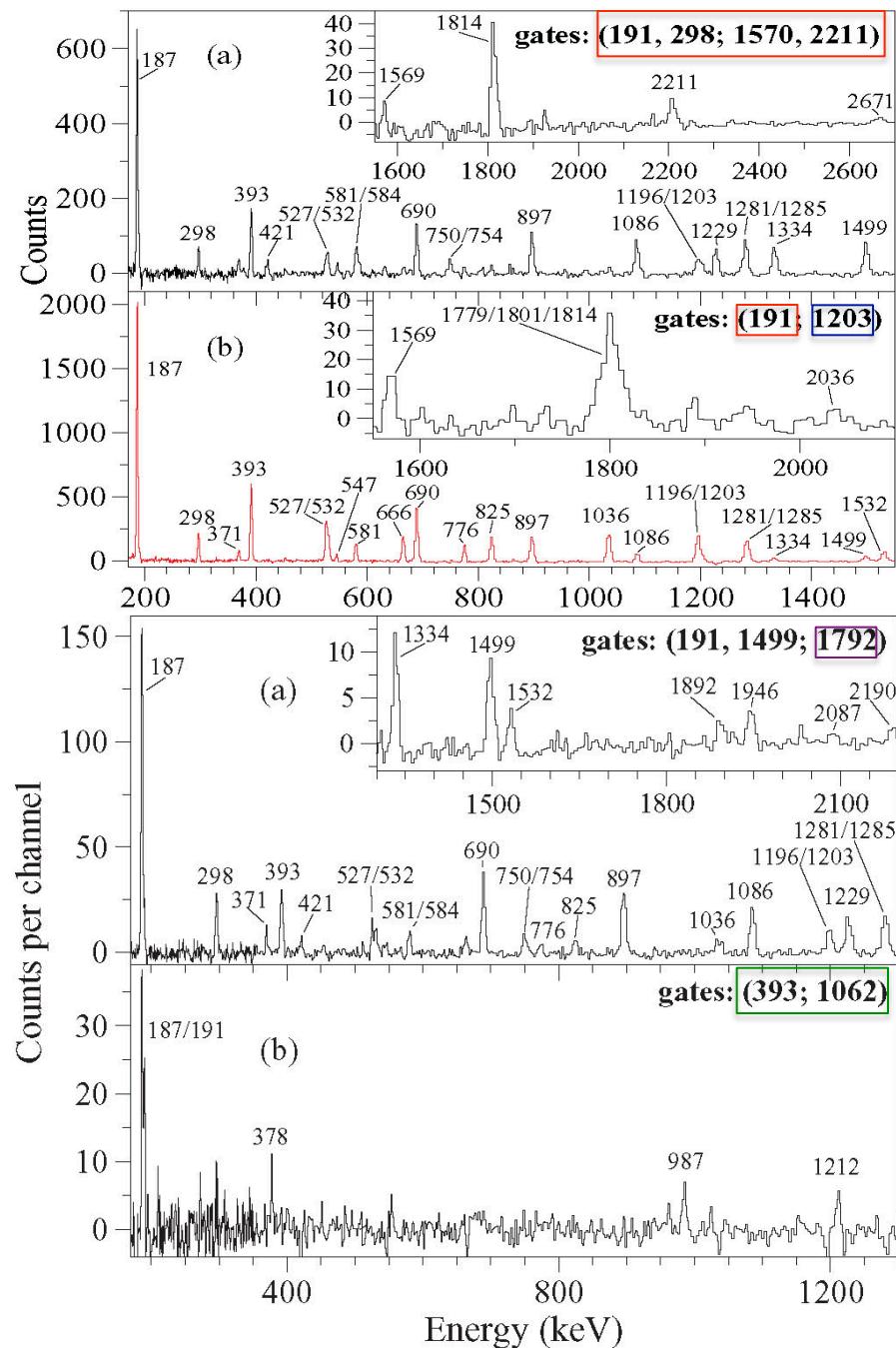
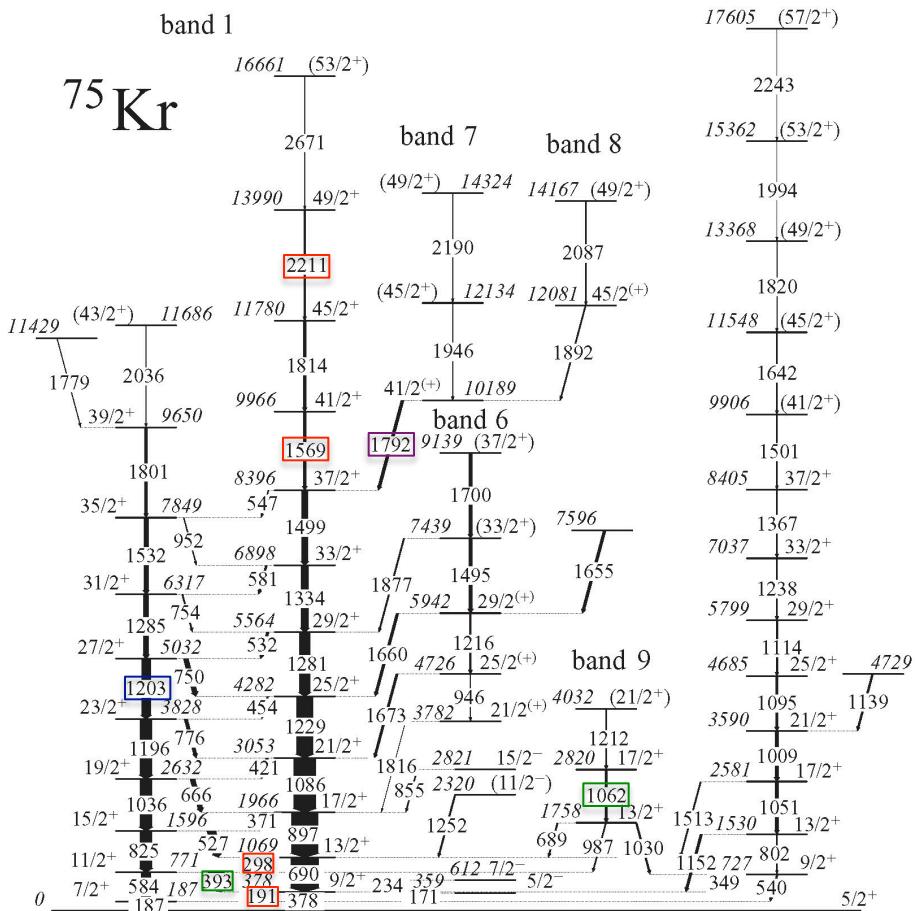
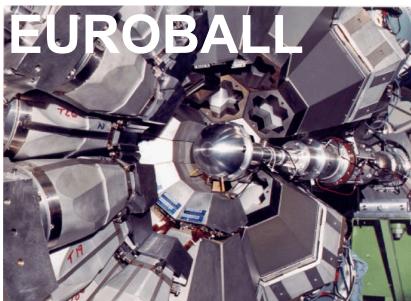
# $\gamma$ -ray Coincidence Analysis

- With two or more detectors it is possible to create two or higher dimension histograms.
- The 1D projection with a condition in one of the axis provides the spectrum of  $\gamma$ -rays “in coincidence”.
- The “coincidence” relationships allow to create the energy level scheme of the nucleus for a particular reaction.



The Compton background is as well in coincidence with the transition

# Example: Coincidence Analysis in Fusion-Evaporation Reactions



# Electromagnetic Decay

- The initial and final states have a definite angular momentum and parity. The photon carries away a definite amount of angular momentum. Angular momentum and parity must be conserved.
- Multipolarity is a measure of the angular momentum carried away by the photon.
- Transitions are classified as electric or magnetic based on whether the radiation is due to a shift in the charge distribution or a shift in the current distribution.
- Based upon the type of operator involved in the transition, there are restrictions on the parity change in the transition.

$$|(I_i - I_f)| \leq \ell \leq (I_i + I_f)\hbar$$

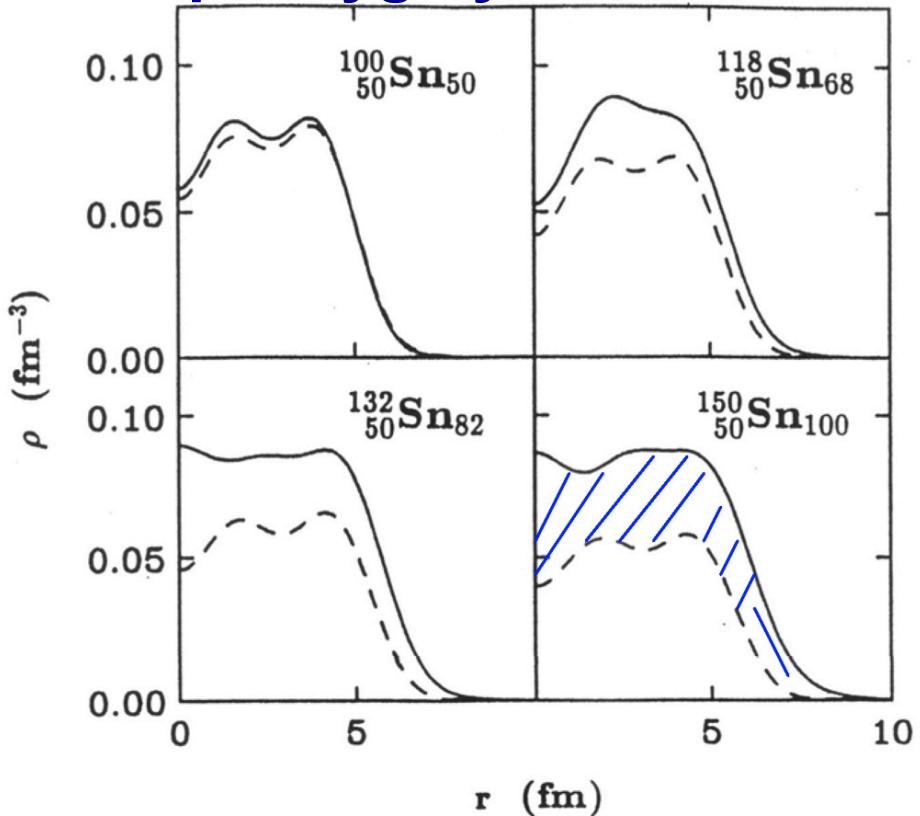
A photon with  $\ell$  units of angular momentum is called a  $2^\ell$ -pole photon.  
 $\ell = 1 \Rightarrow$  dipole  
 $\ell = 2 \Rightarrow$  quadrupole  
 $\ell = 3 \Rightarrow$  octupole

TABLE 9.1  $\gamma$ -Ray Selection Rules and Multipolarities

Radiation Type	Name	$\ell = \Delta I$	$\Delta\pi$
E1	Electric dipole	1	Yes
M1	Magnetic dipole	1	No
E2	Electric quadrupole	2	No
M2	Magnetic quadrupole	2	Yes
E3	Electric octupole	3	Yes
M3	Magnetic octupole	3	No
E4	Electric hexadecapole	4	No
M4	Magnetic hexadecapole	4	Yes

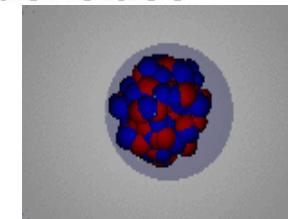
# Example Pygmy Resonances

Dobaczewski, Hamamoto, Nazarewicz and Sheikh,  
Acta.Phys.Pol. **B25** (1994) 541



Calculated one-nucleon densities

— neutrons  
- - - protons



Static distributions of charges and currents give static electric and magnetic fields.

These fields can be analyzed in terms of the multipole moments of the charge distribution (dipole moment, quadrupole moment, and so on).

See Krane Section 3.5

e.g. -charge oscillating along one axis: produces an electric dipole radiation field  
-variation of the current (circular current loop): a magnetic dipole radiation field

**Weisskopf estimates:** The transition is due to a single proton that changes from one shell-model state to another: EL/ML electric/Magnetic transition probability.

$$\lambda(EL) \cong \frac{8\pi(L+1)}{L[(2L+1)!!]^2} \frac{e^2}{4\pi\epsilon_0\hbar c} \left(\frac{E}{\hbar c}\right)^{2L+1} \left[\frac{3}{L+3}\right]^2 c R^{2L}$$

$$\lambda(ML) \cong \frac{8\pi(L+1)}{L[(2L+1)!!]^2} \left(\mu_p - \frac{1}{L+1}\right)^2 \left(\frac{\hbar}{m_p c}\right) \left(\frac{e^2}{4\pi\epsilon_0\hbar c}\right) \left(\frac{E}{\hbar c}\right)^{2L+1} \left[\frac{3}{L+2}\right]^2 c R^{2L-2}$$

$$\lambda(E1) = 1.0 \times 10^{14} A^{2/3} E^3$$

$$\lambda(E2) = 7.3 \times 10^7 A^{4/3} E^5$$

$$\lambda(E3) = 34 A^2 E^7$$

$$\lambda(E4) = 1.1 \times 10^{-5} A^{8/3} E^9$$

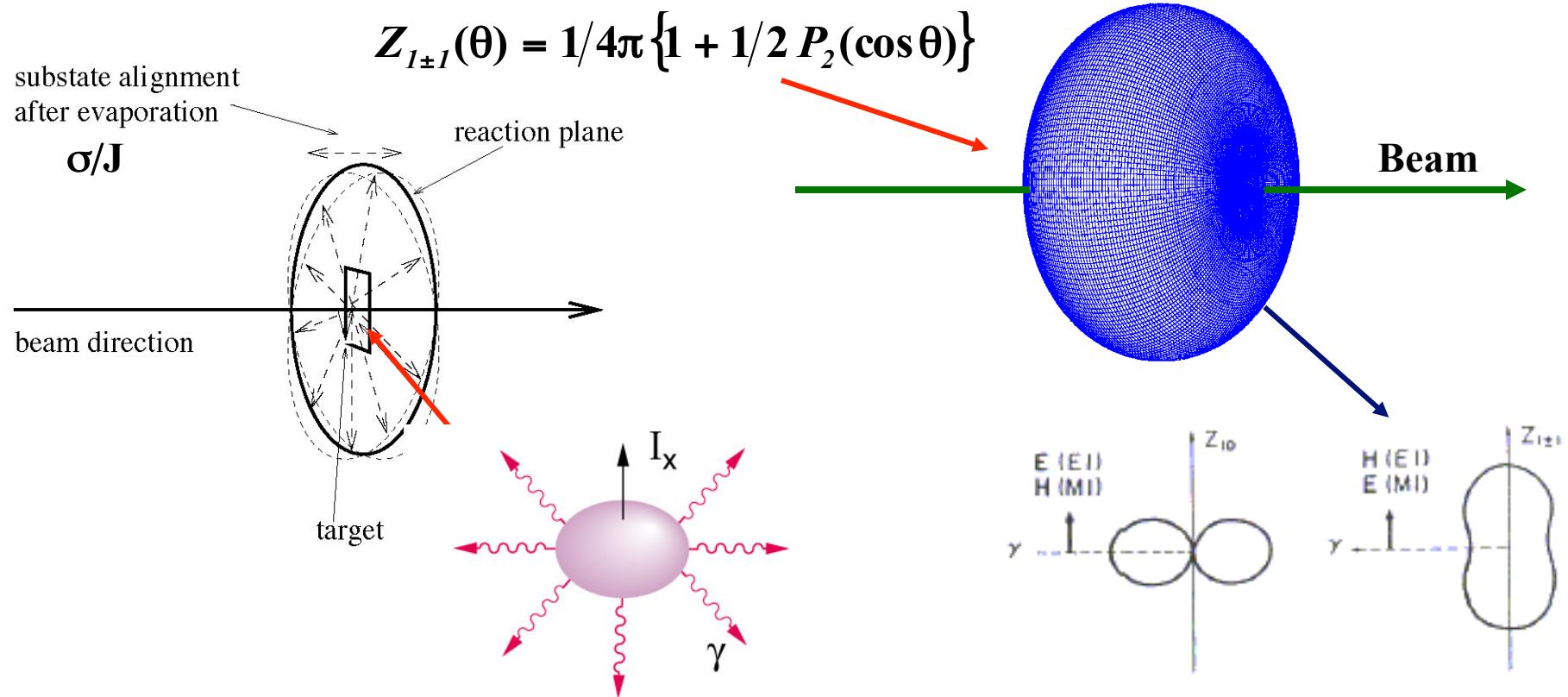
$$\lambda(M1) = 5.6 \times 10^{13} E^3$$

$$\lambda(M2) = 3.5 \times 10^7 A^{2/3} E^5$$

$$\lambda(M3) = 16 A^{4/3} E^7$$

$$\lambda(M4) = 4.5 \times 10^{-6} A^2 E^9$$

# Electromagnetic emission from Oriented Nuclei: Angular distributions



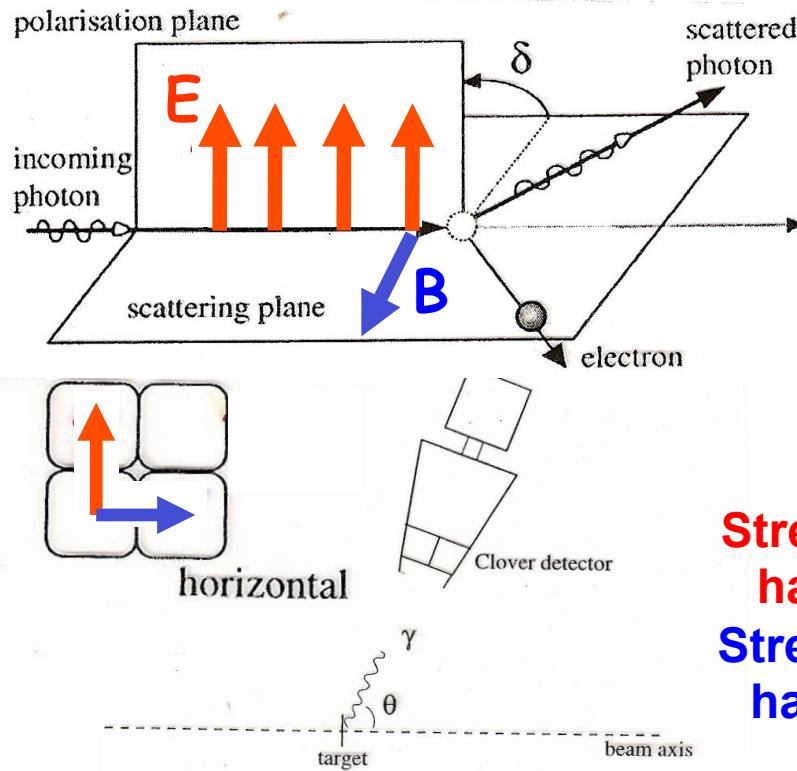
Angular distributions and correlations are only sensitive to the multipolarity L  
Polarization measurements are more sensitive to Character

# Measurement of the linear polarization

- $\gamma$ -rays emitted by oriented nuclei are partially polarized. The polarization vector is different for E and M transitions (character)
- Compton scattering can be used to measure the degree of polarization through the dependency with the polarization vector

$$\frac{d\sigma_{KN}}{d\Omega} = \frac{r_0^2}{4} \left( \frac{E'}{E} \right)^2 \left[ \frac{E'}{E} + \frac{E}{E'} - 2 \sin^2 \theta \cos^2 \varphi \right]$$

$\varphi$  :angle between the scattering plane and the initial polarization plane



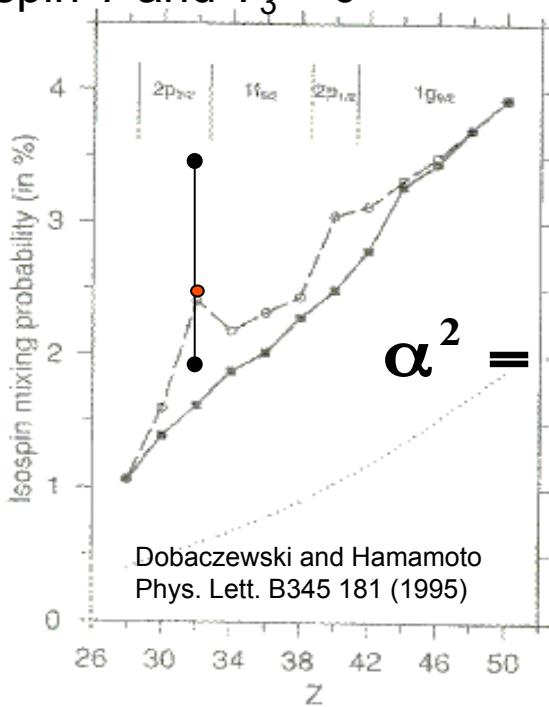
$$P_E(\theta) = \frac{1}{Q} \cdot \frac{N_{\perp} - N_{\parallel}}{N_{\perp} + N_{\parallel}}$$

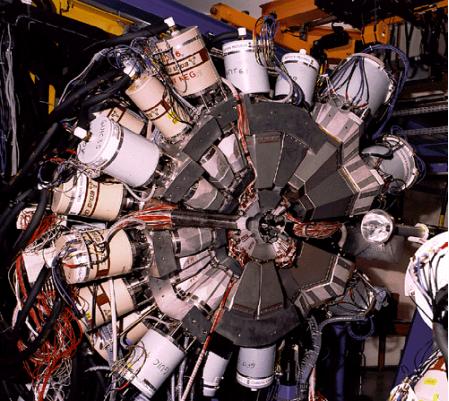
Experiments measure the asymmetry.  
 $Q$  is the sensibility of the polarimeter

**Stretched E $\lambda$  transitions will have positive asymmetry**  
**Stretched M $\lambda$  transitions will have negative asymmetry**

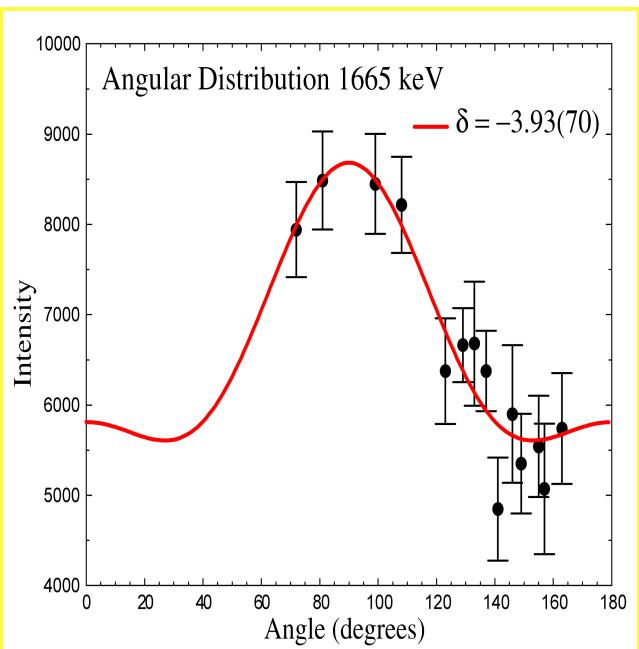
# Forbidden E1 transitions in $^{64}\text{Ge}$ between states with $T=0$

Studying the violation of isospin symmetry induced by the Coulomb interaction is the observation of E1 transitions in even–even  $N = Z$  nuclei. In the long-wavelength limit, the matrix elements of the nuclear E1 operator vanish when both the initial and final states have equal isospin  $T$  and  $T_3 = 0$

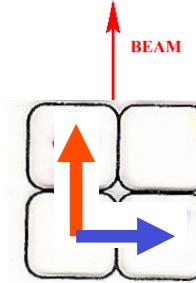




## Angular distribution



$\delta = -3.93(70)$   
 $B(M2) = 6.1(1.6) \text{ W.u.}$   
 $B(E1) = 2.3 (1.3) 10^{-7} \text{ W.u.}$

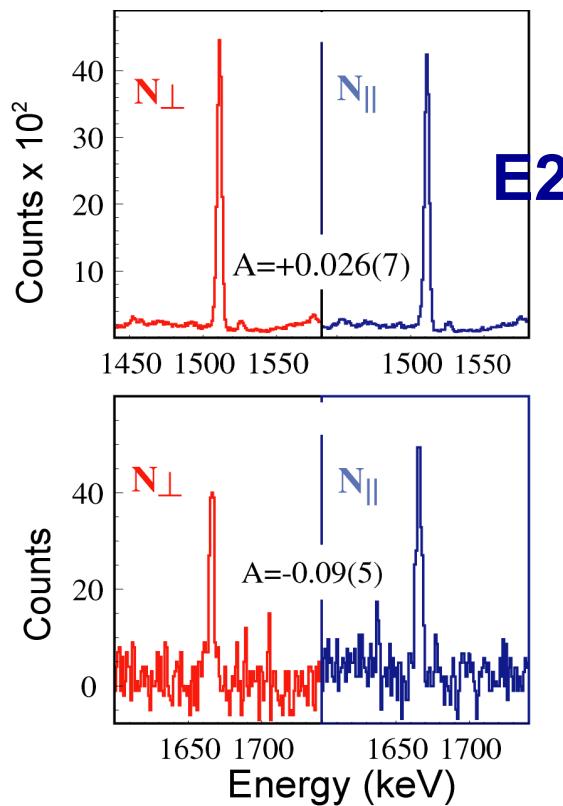
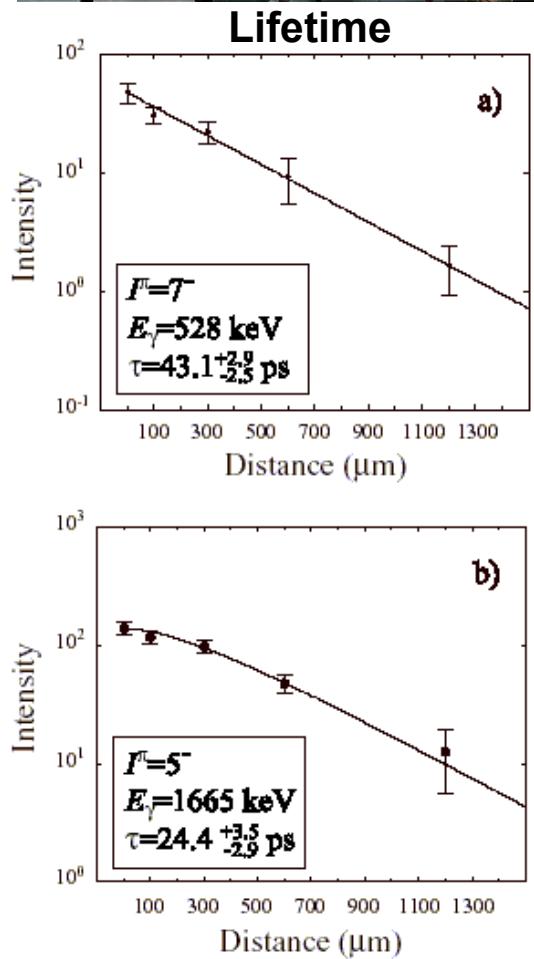


$$A = \frac{N_{\perp} - N_{\parallel}}{N_{\perp} + N_{\parallel}}$$

## Lifetime

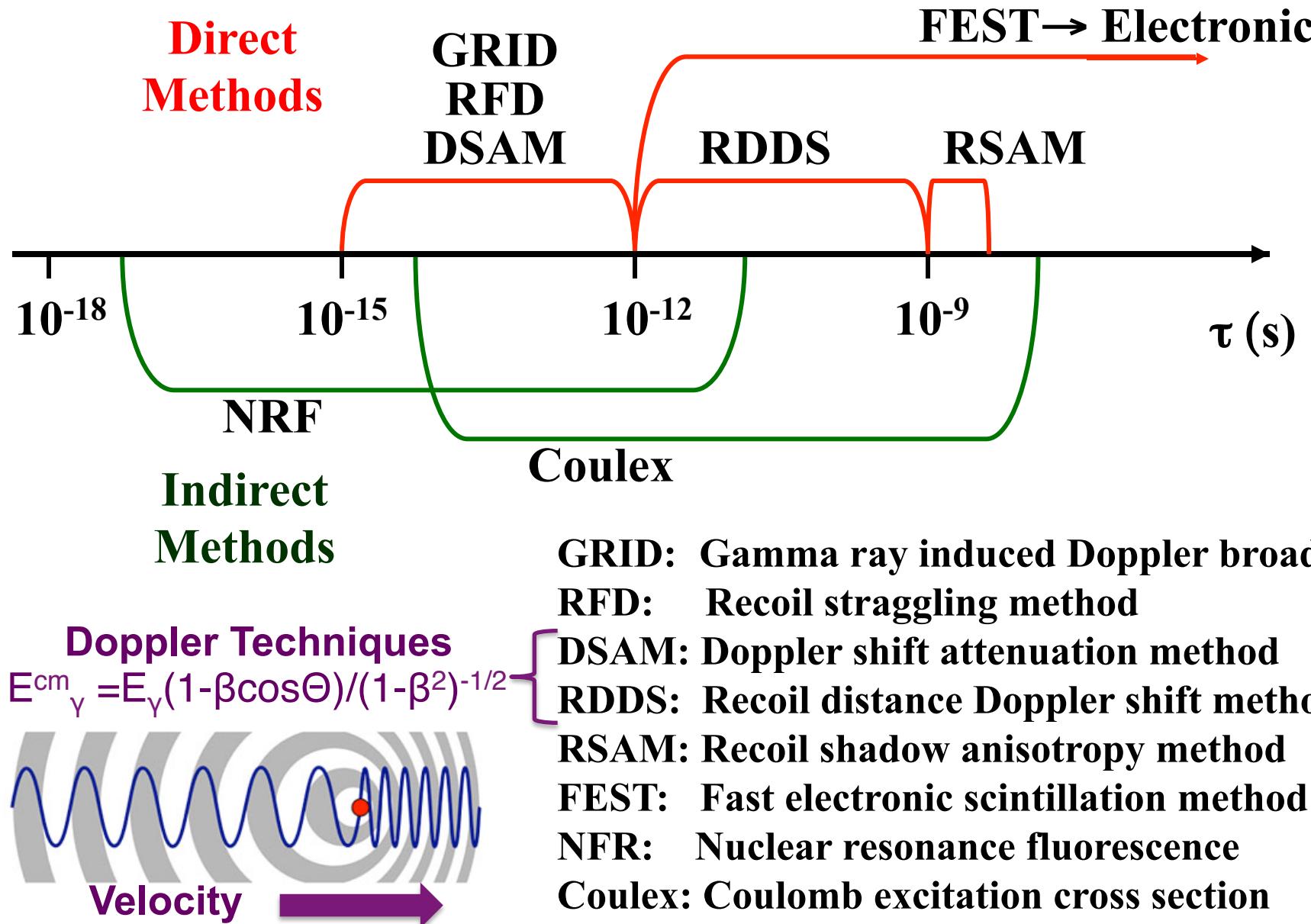
## Asymmetry and polarization

$$A = N_{\perp} - N_{\parallel} / (N_{\perp} + N_{\parallel})$$



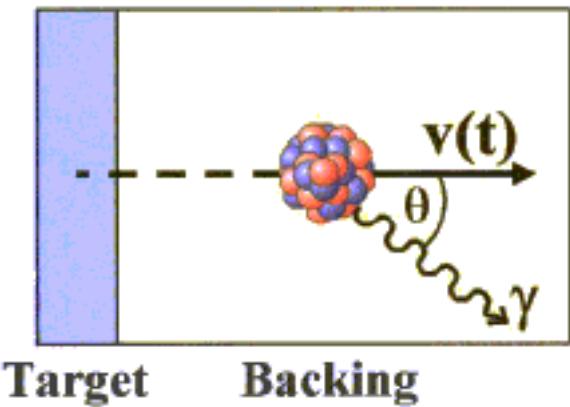
The 1665 keV transition mixed E1/M2 character ~93% quadrupole contents

# Techniques for lifetime measurements



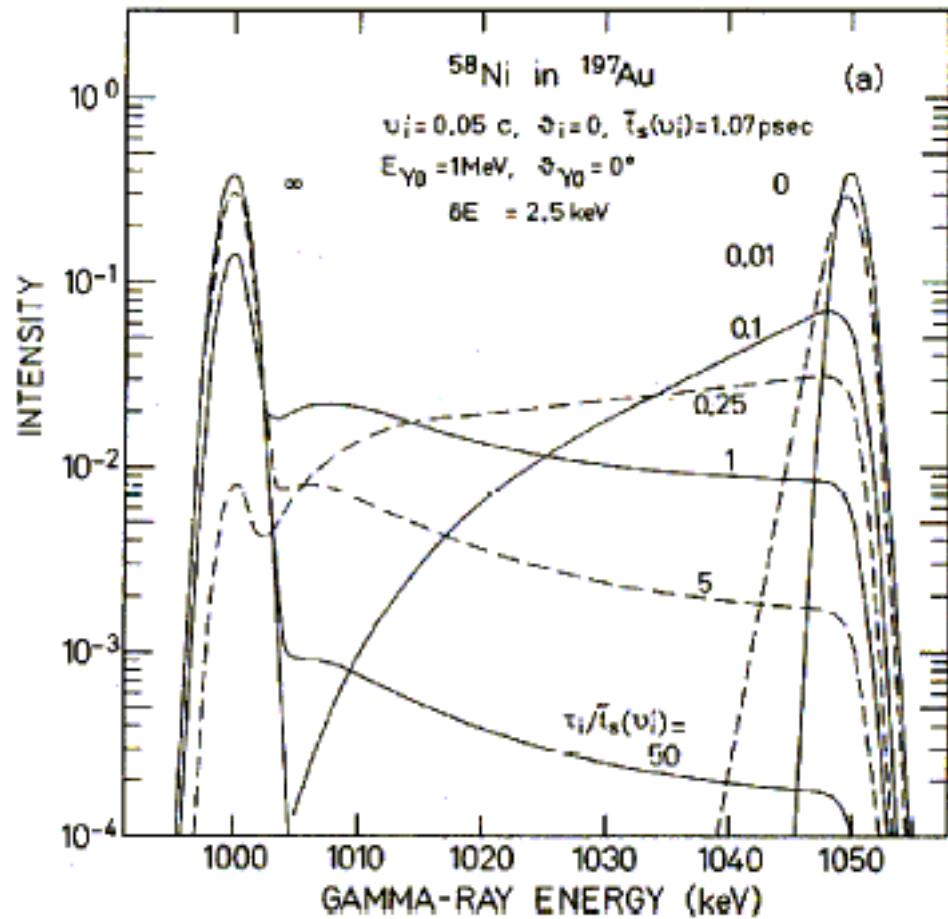
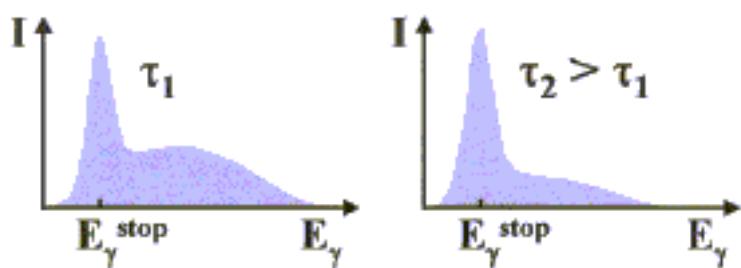
# Doppler Shift Attenuation Method

$$\tau = 0.1 - 1.5 \text{ ps}$$



$v(t)$  from Monte Carlo simulation with stopping power

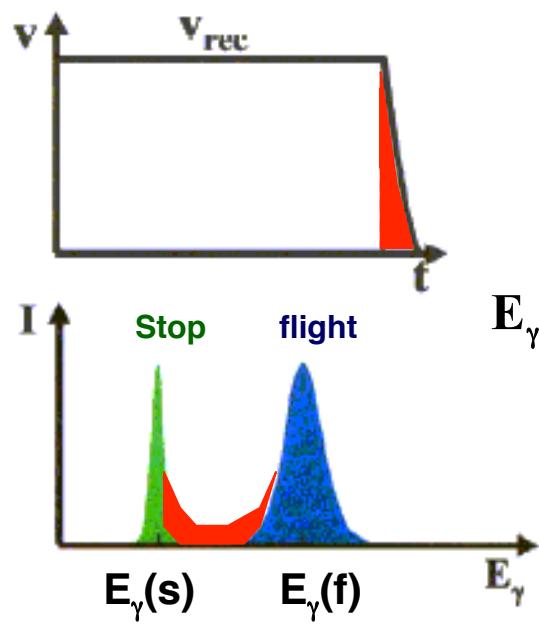
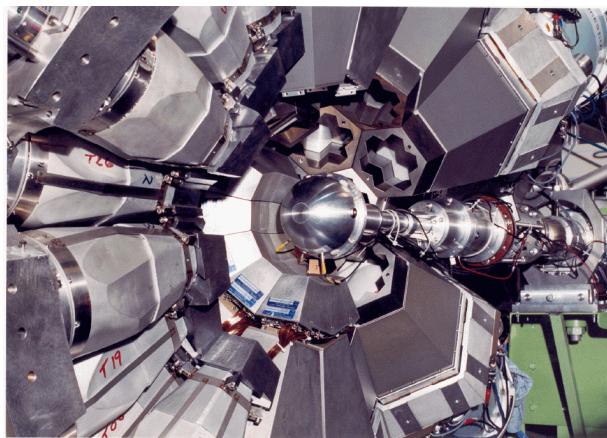
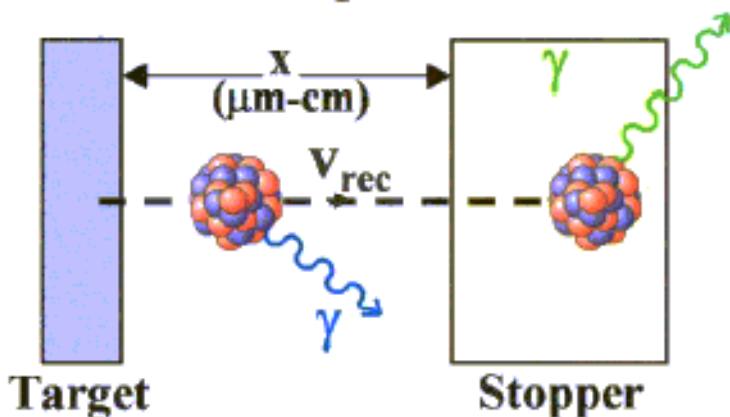
$$\frac{-dE}{dx} = \frac{(4\pi e^2 N Z)}{m_0 V^2 A} \ln\left(\frac{2m_0 V^2}{I}\right)$$



Line shapes for  $^{58}\text{Ni}$  stopped in  $^{197}\text{Au}$  with a beam velocity of  $v/c=0.05$  and measured at  $\theta=0^\circ$

# Recoil Distance Doppler Shift Method

$$\tau = 1\text{ps} - 3\text{ns}$$

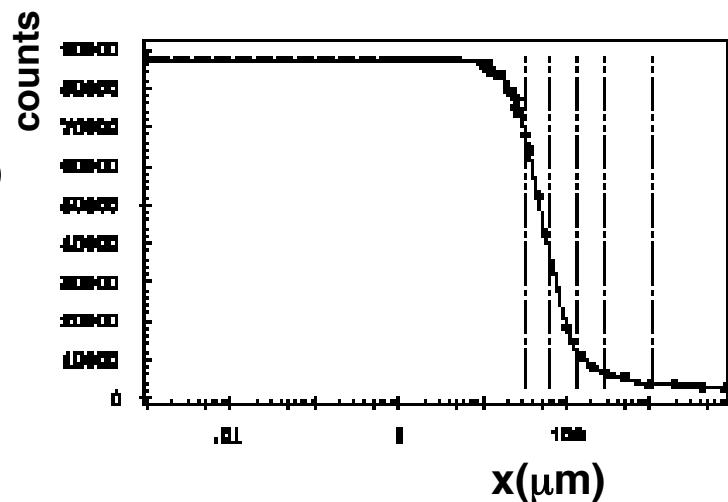


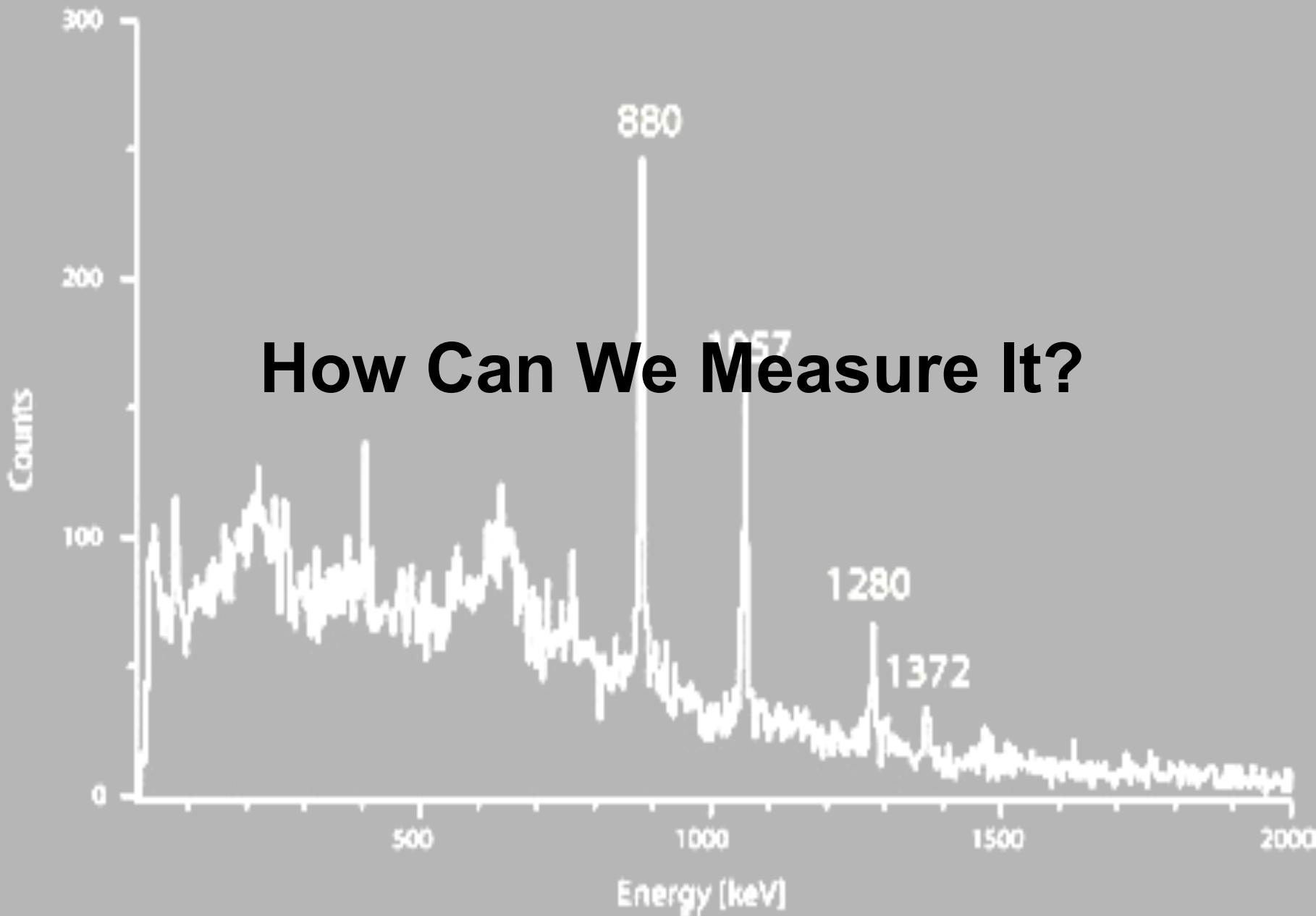
$$E_\gamma(f) \approx E_\gamma(s)(1 + \frac{v_{rec}}{c} \cos \theta)$$

$$I(f) = N_0(1 - e^{-(x/v_{res} \tau)})$$

# Koeln University plunger

## Decay Curve





# Interaction of the $\gamma$ -rays with matter

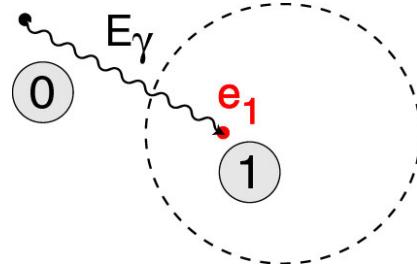
$\sim 100$  keV

$\sim 1$  MeV

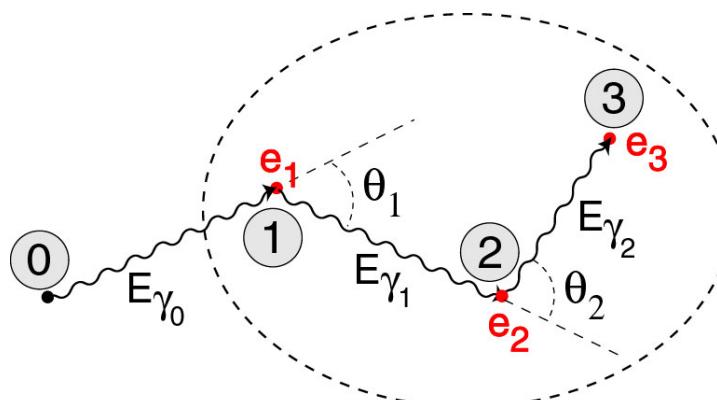
$\sim 10$  MeV

$\gamma$ -ray energy

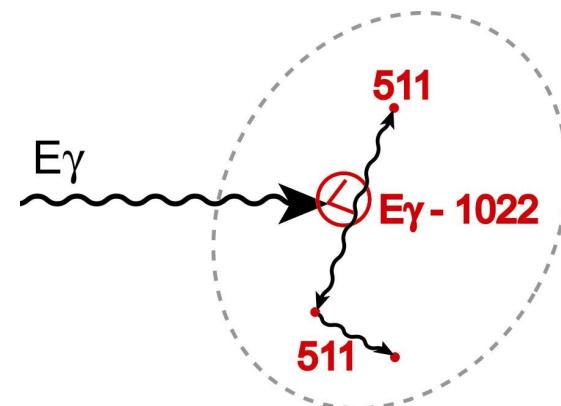
## Photoelectric



## Compton Scattering



## Pair Production



$$E_{\gamma'} = \frac{E_{\gamma}}{1 + \frac{E_{\gamma}}{m_0 c^2} (1 - \cos\theta)}$$

# Instrumentation for HR $\gamma$ -ray spectroscopy

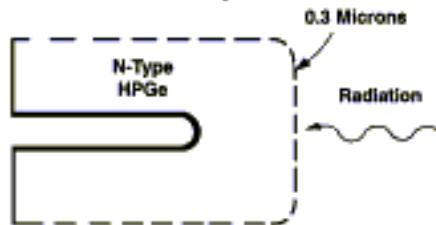
High resolution  $\gamma$ -ray spectroscopy  $\rightarrow$  large volume semiconductor detectors  
in particular detectors based on HP-Ge (impurities  $\sim 10^{-12}$ )

Present Ge

$>2$  kg/crystal

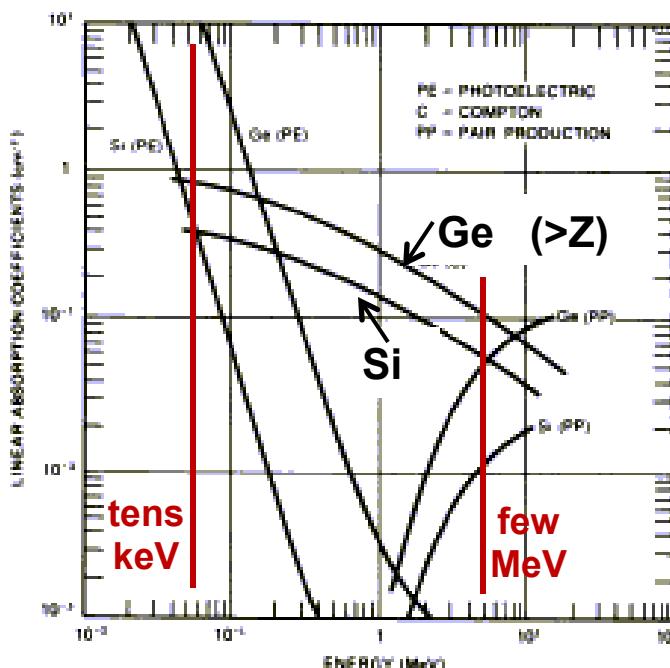


GEM HPGe Crystal



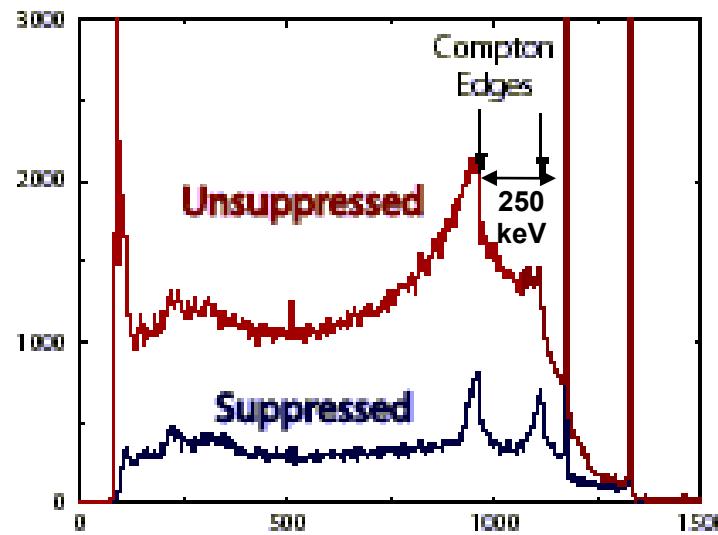
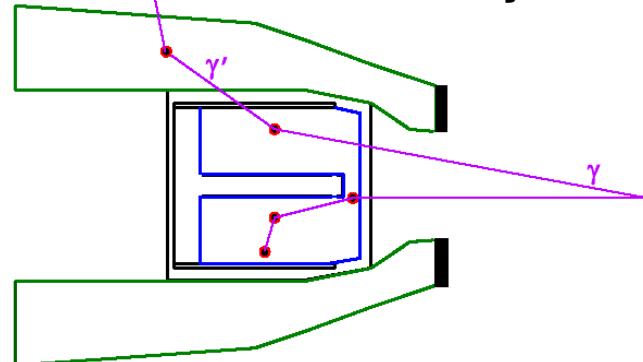
GAMMA-X Crystal

— Very Thick Contact ~600 Mic  
- - - Very Thin Contact ~0.3 Mic



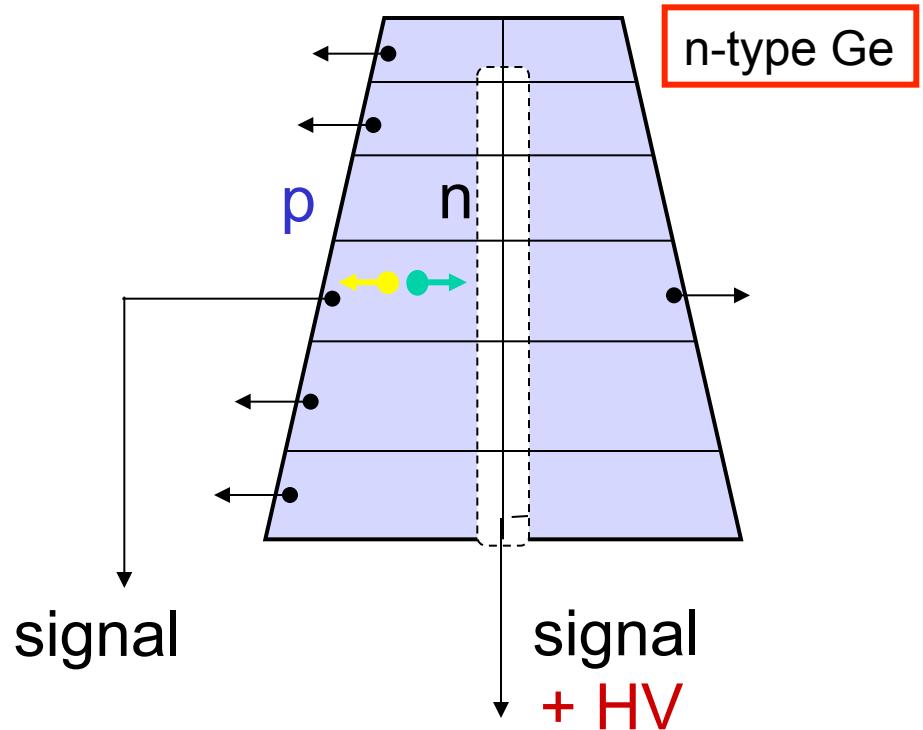
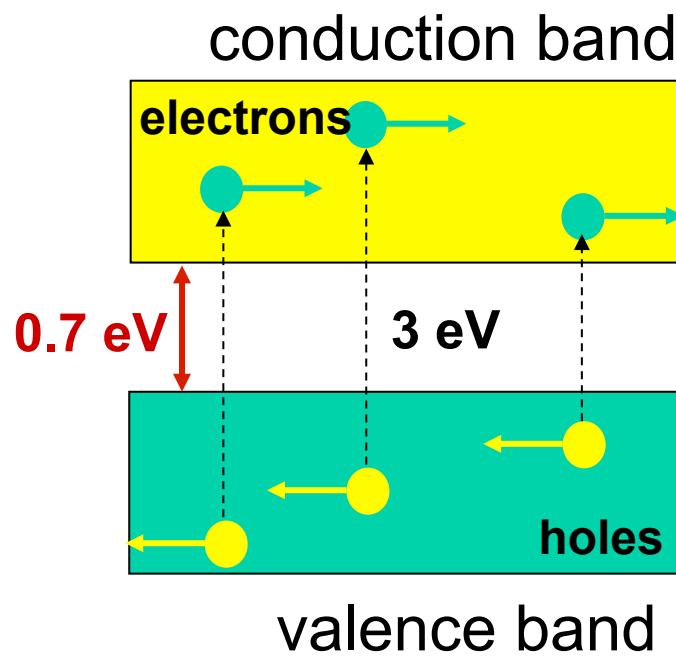
Composite  
detectors

Compton suppressed  
Ge-detectors  $\rightarrow$  arrays



# Germanium detector

Sensitivity factors: Energy Resolution, Peak to Total Ratio



Number of e-h pairs for 1 MeV,  $N = 10^6 / 3 = 3 \times 10^5$

Energy resolution  
(Fano Factor)

$$\sqrt{N}/N = 0.0018 \rightarrow 1.8 \text{ keV} (E_\gamma = 1 \text{ MeV})$$

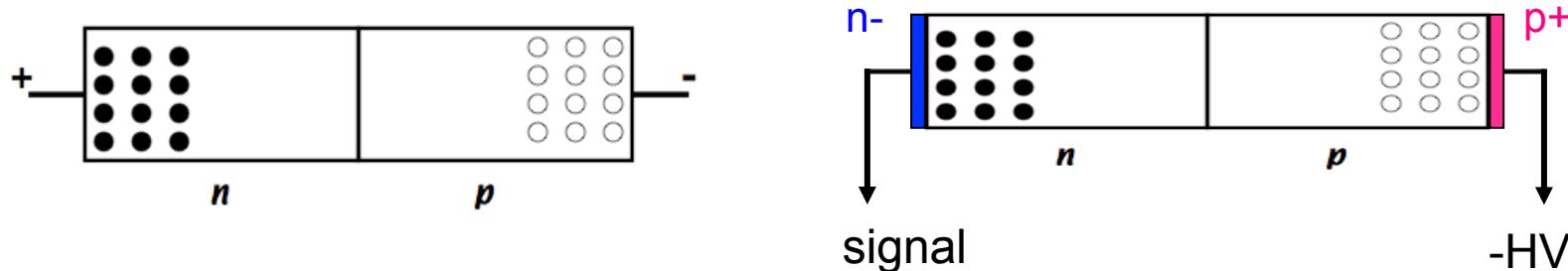
Thermally activated charge carriers in the conduction band density at room temperature  $\sim 2.5 \cdot 10^{13} \text{ cm}^{-3}$  for Ge ( $\sim 1.5 \cdot 10^{10} \text{ cm}^{-3}$  for Si)

To reduce the number of free charge carriers :

=> deplete material: np junction

=> increase depletion by applying a reverse bias

=> for Ge, cool detector with  $\text{LN}_2$  - 77K



$$\text{FWHM}^2 = W_D^2 + W_X^2 + W_E^2 + W_{\text{Doppler}}^2$$

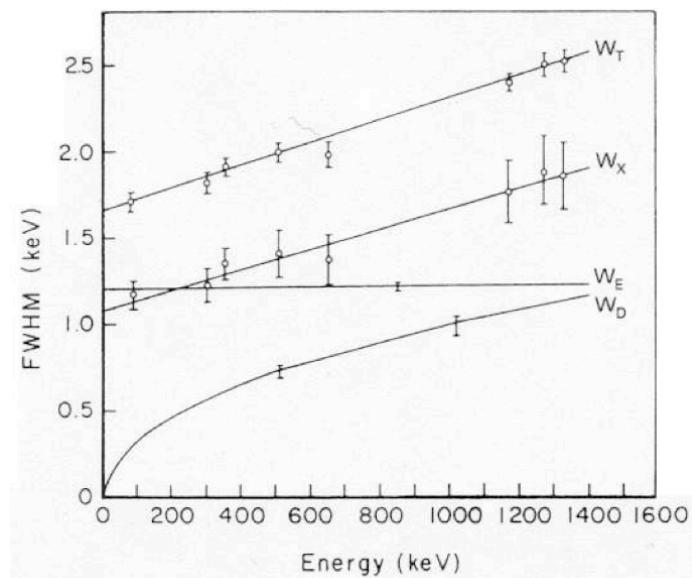
$$W_D = 2.35 \sqrt{F \epsilon E_\gamma} \text{ Statistical fluctuations of carriers}$$

$\epsilon = 2.96 \text{ eV}$  @ 77 K Fano factor  $F \sim 0.1$   
(not all the deposited energy goes to create e-h pairs)

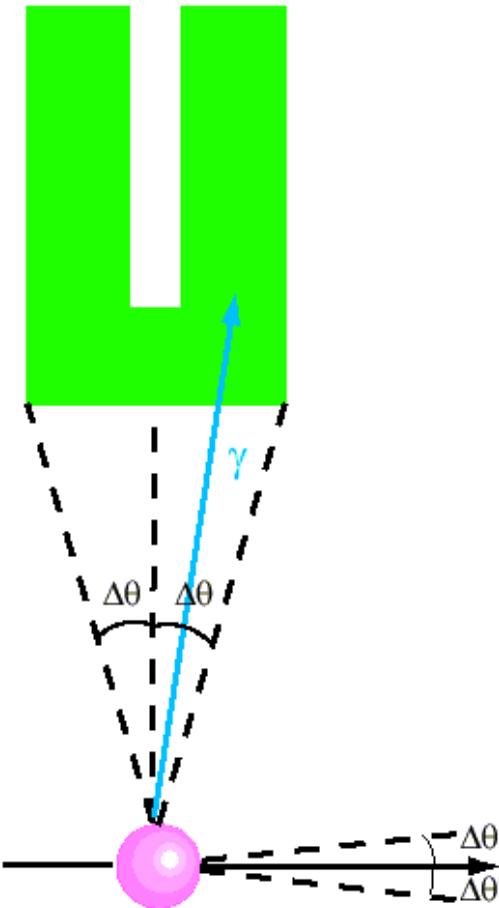
$W_X$  incomplete charge collection

$W_E$  electronic noise

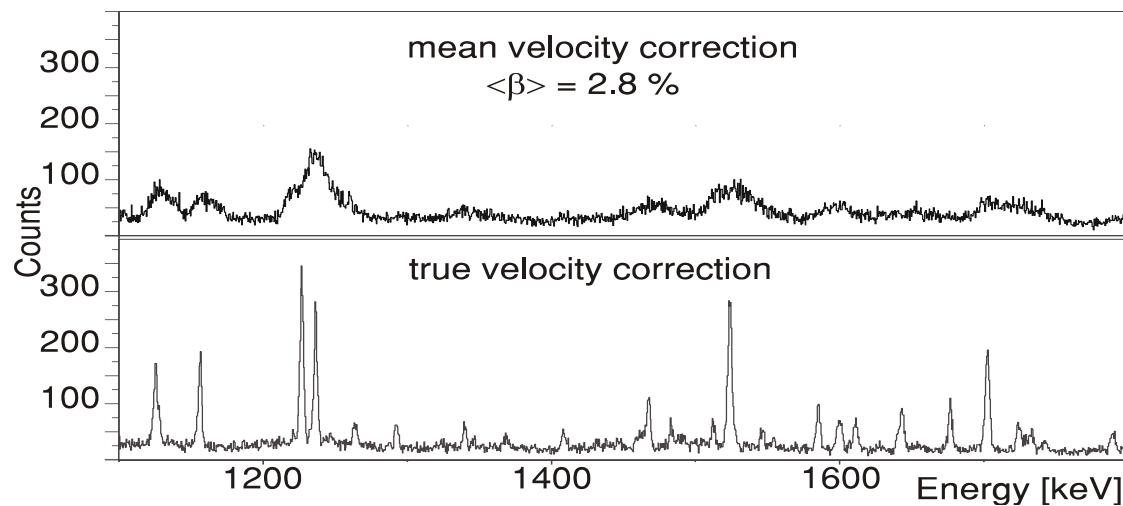
$W_{\text{doppler}}$  Doppler broadening



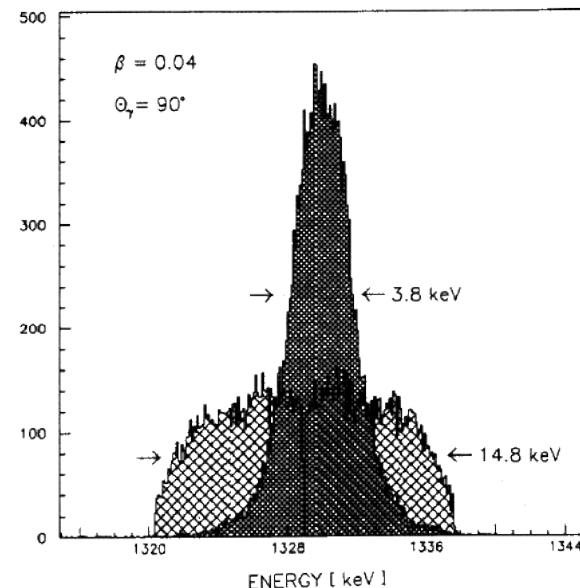
# Doppler Broadening



$$E_s = E_0 (1 + v/c \cos \theta)$$
$$\Delta E_s = E_0 v/c \sin \theta \Delta \theta$$



Dedicated ancillary detectors for the determination of the recoil trajectory



Development of  
segmented Ge  
detectors and  
Pulse Shape  
Analysis  
techniques for  
position  
determination

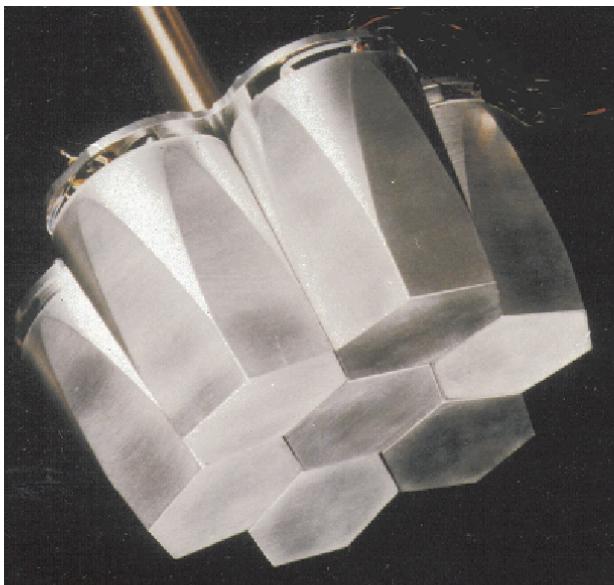
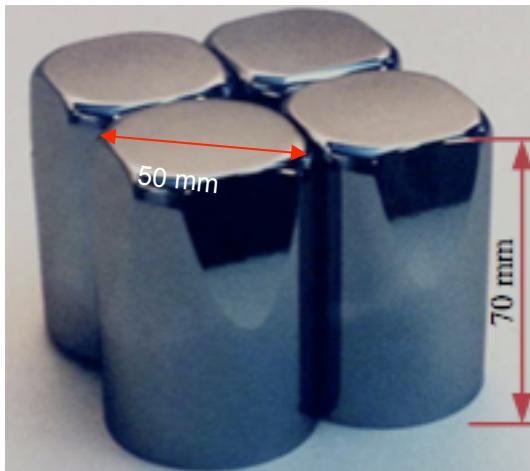
# Composite detectors

=> Reduction of  $\Delta\theta_D$

- Eurogam II

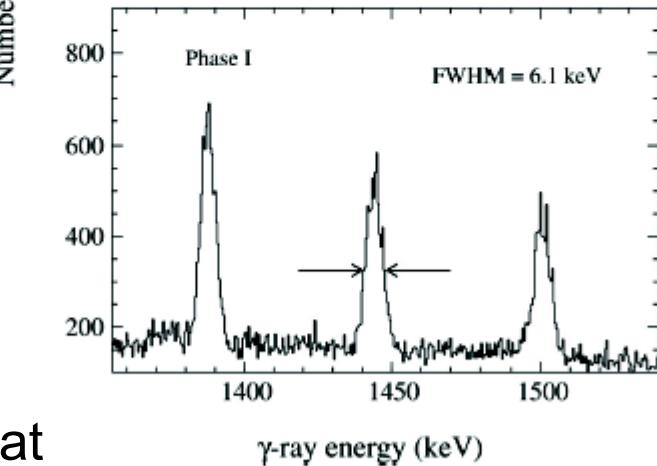
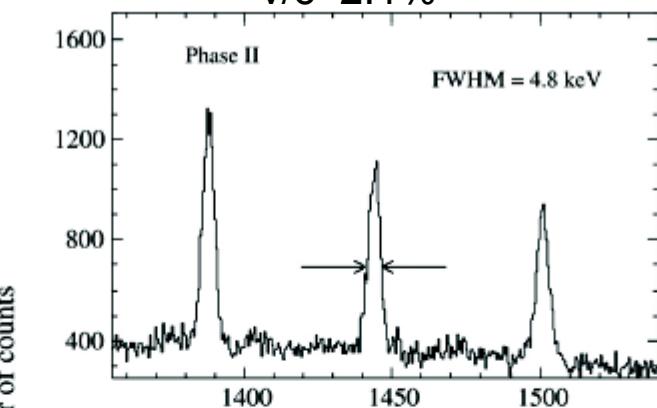
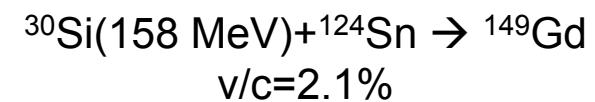
- Clovers:

- 4 crystals in 1 cryostat



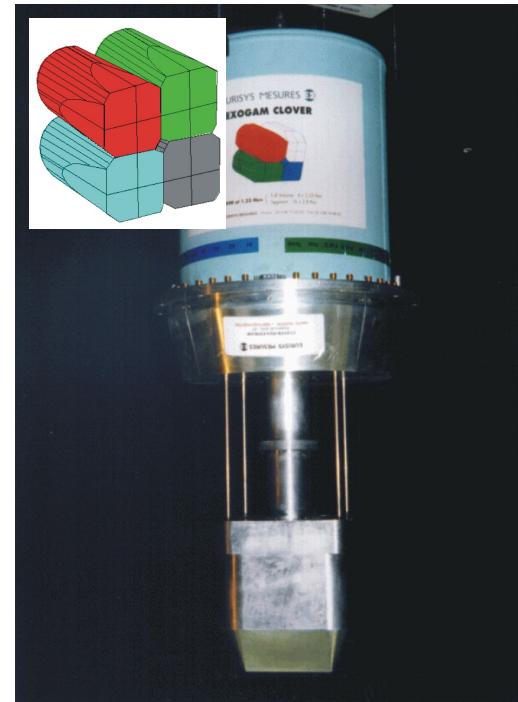
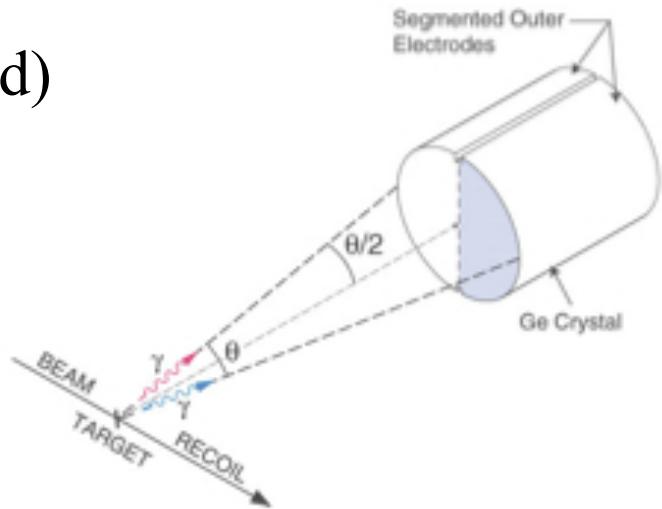
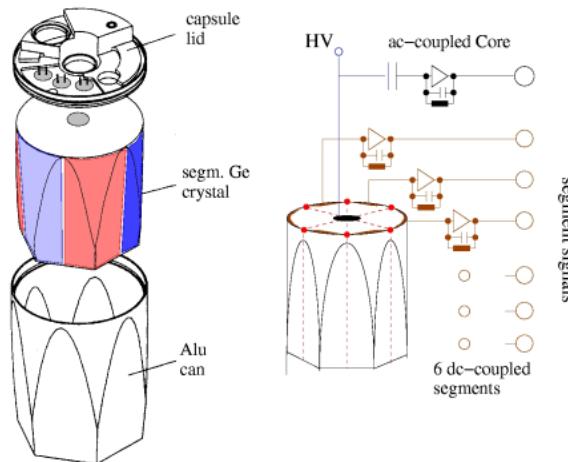
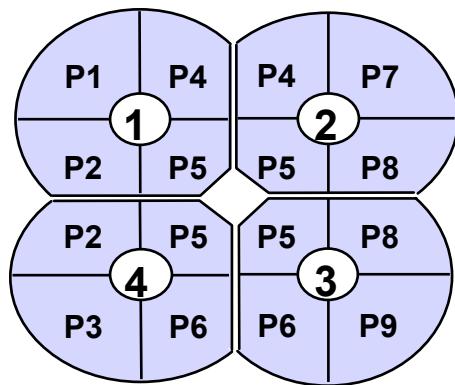
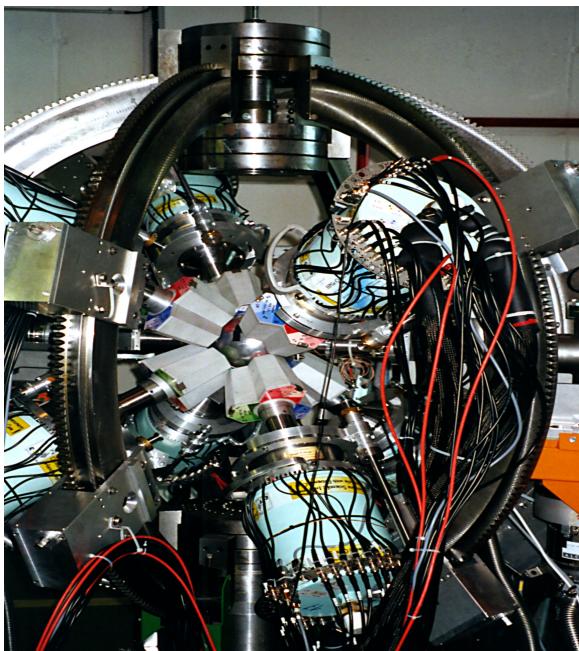
- Euroball
- Clusters:

- 7 crystals in 1 cryostat

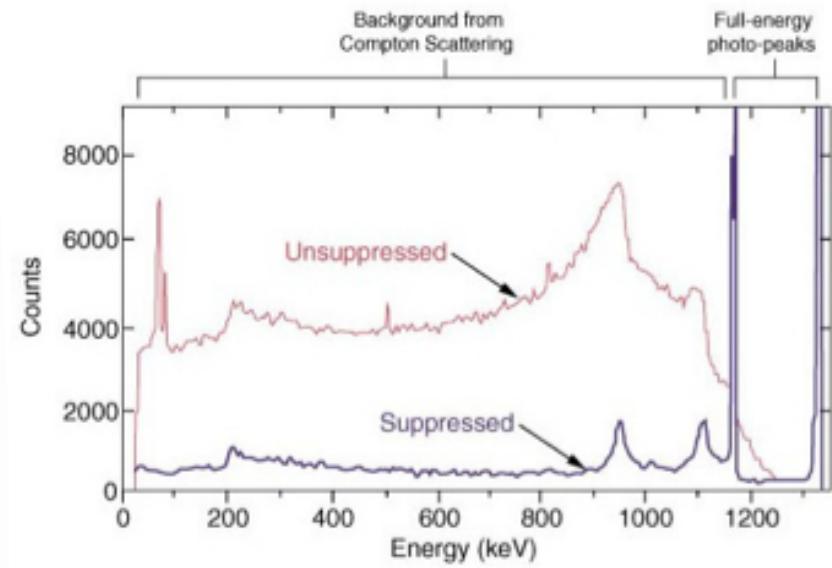
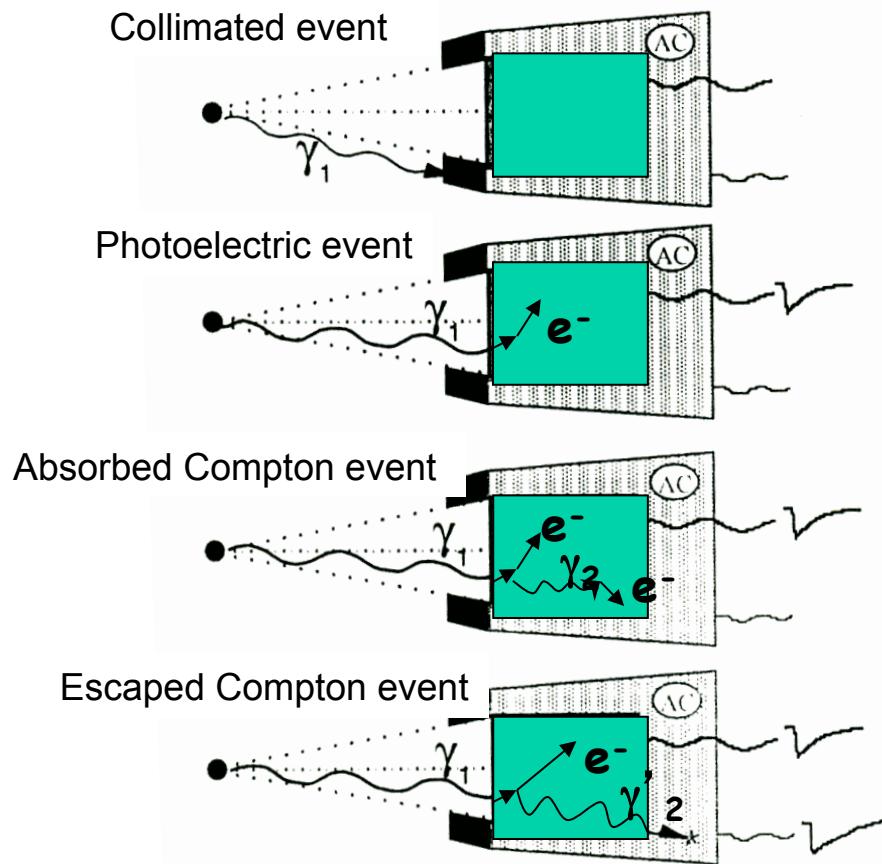


# Electrical Segmentation of detectors

- Gammasphere segmented detector (2 Fold)
- Exogam at GANIL (Segmented Clover)
- Miniball at ISOLDE (Segmented)



# Signal-to-noise ratio and Compton suppression



$$P/T \sim 0.2-0.3 \Rightarrow 0.5-0.6$$

# HR $\gamma$ -Spectroscopy Instrumentation for Nuclear Structure

Late 90's  
Large  $\gamma$ -Arrays



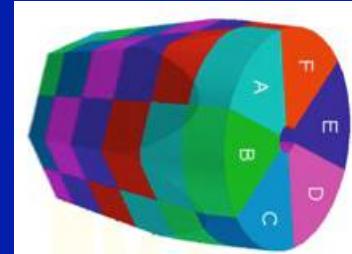
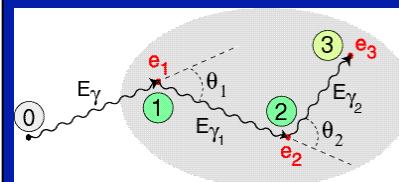
$\epsilon \sim 10 - 5 \%$   
( $M_\gamma = 1 - M_\gamma = 30$ )

Compact  $\gamma$ -Arrays optimized  
Doppler correction, low  $M_\gamma$



$\epsilon \sim 20 \%$   $M_\gamma = 1$

Tracking Arrays based on  
Position Sensitive Ge Detectors



AGATA

Two Tracking Arrays projects:  
GRETA (USA) & AGATA (EU)



>15y R&D



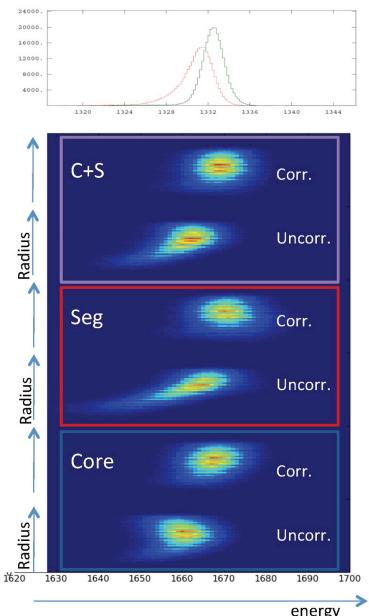
$\epsilon \sim 40 - 20 \%$   
( $M_\gamma = 1 - M_\gamma = 30$ )

# Tracking Array Benefits

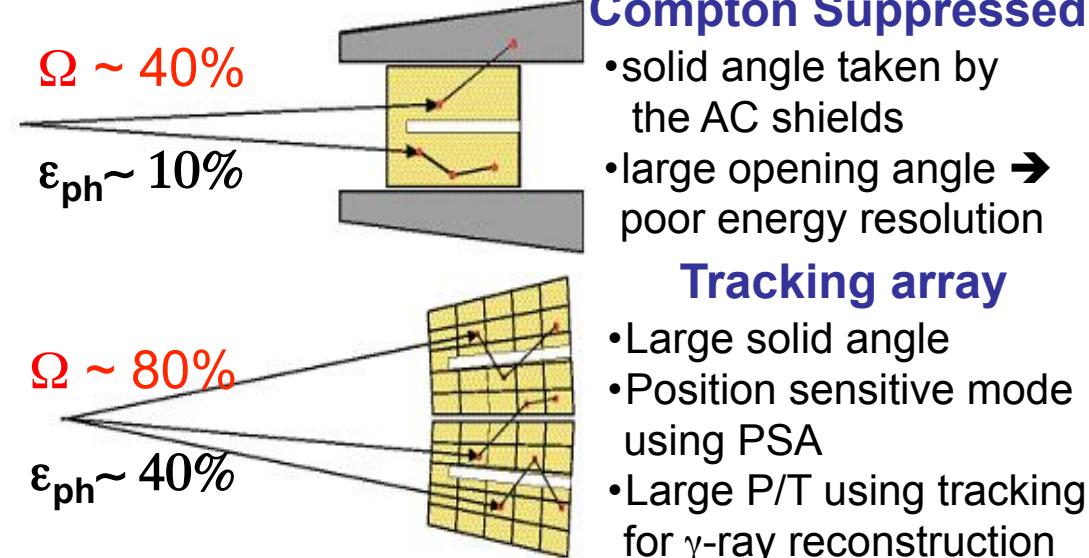
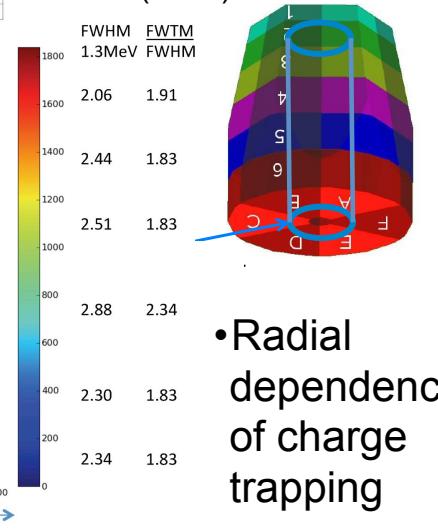
## Conditions:

- Low intensity for the nuclei of interest / require high sensitivity
- High background levels
- Large Doppler broadening (specially in in-flight facilities)
- High counting rates (digital FEE)
- High  $\gamma$ -ray multiplicities (Tracking)

### Correction of neutron damage

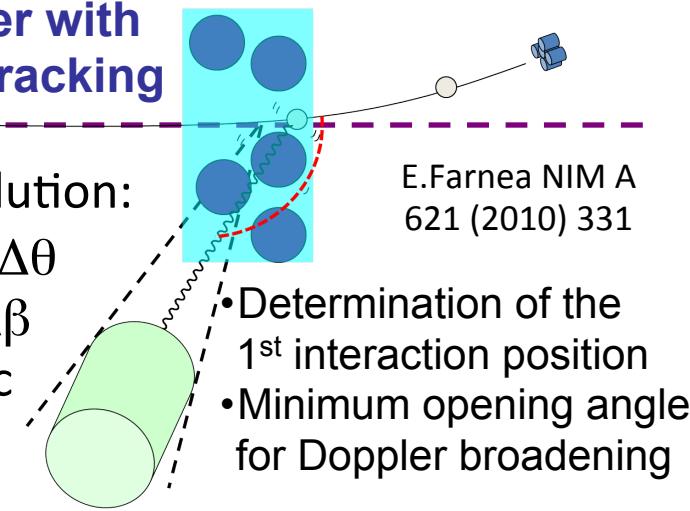


B.Bruyneel EPJ A  
49 (2013) 61

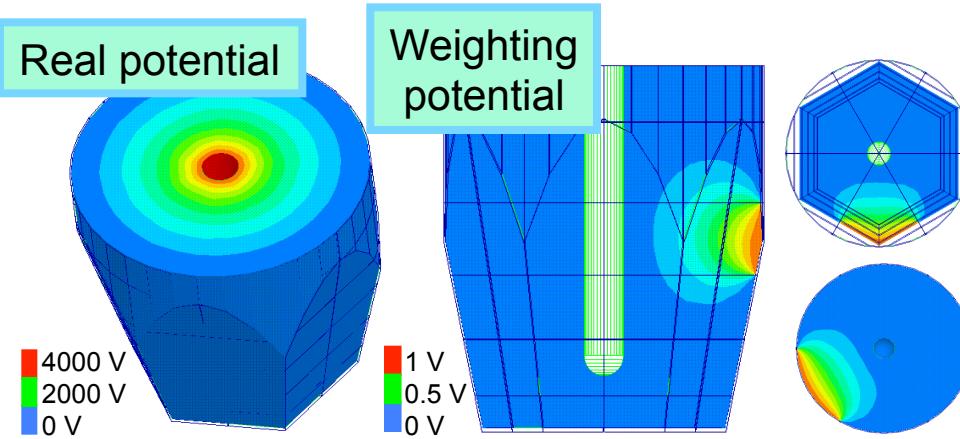


## Doppler with PSA + Tracking

Total Resolution:  
Opening  $\Delta\theta$   
Recoil  $\Delta\beta$   
Intrinsic

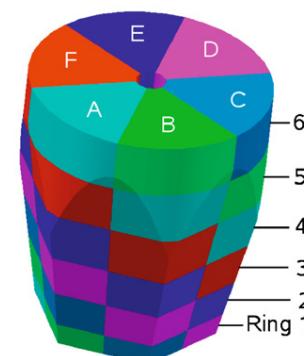
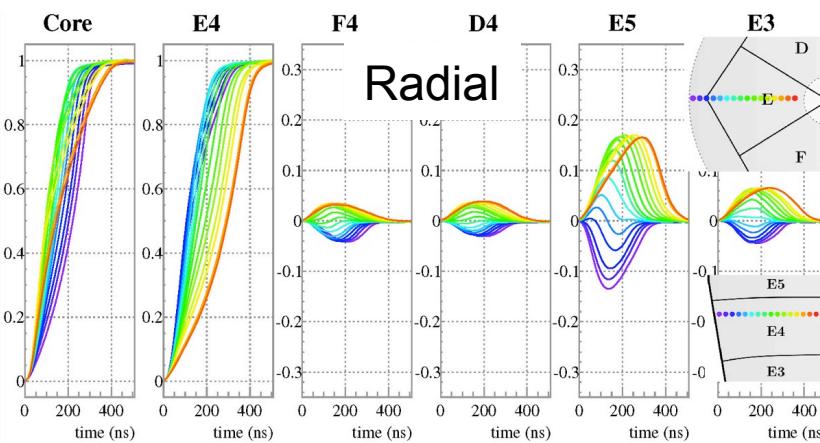
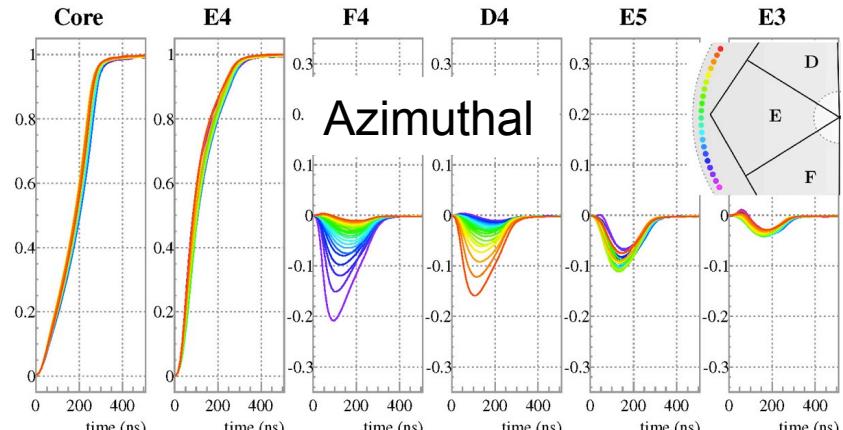
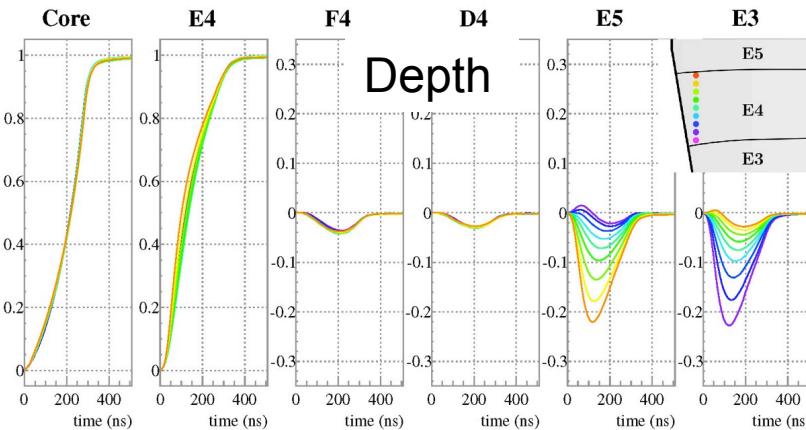


# Position Sensitive Detector for $\gamma$ -rays



Induced current by the moving charge in the sensing contact → weighting potential Ramo's Theorem.  $i_k = -q\vec{v} \cdot \vec{\nabla} \phi_k(r_q)$

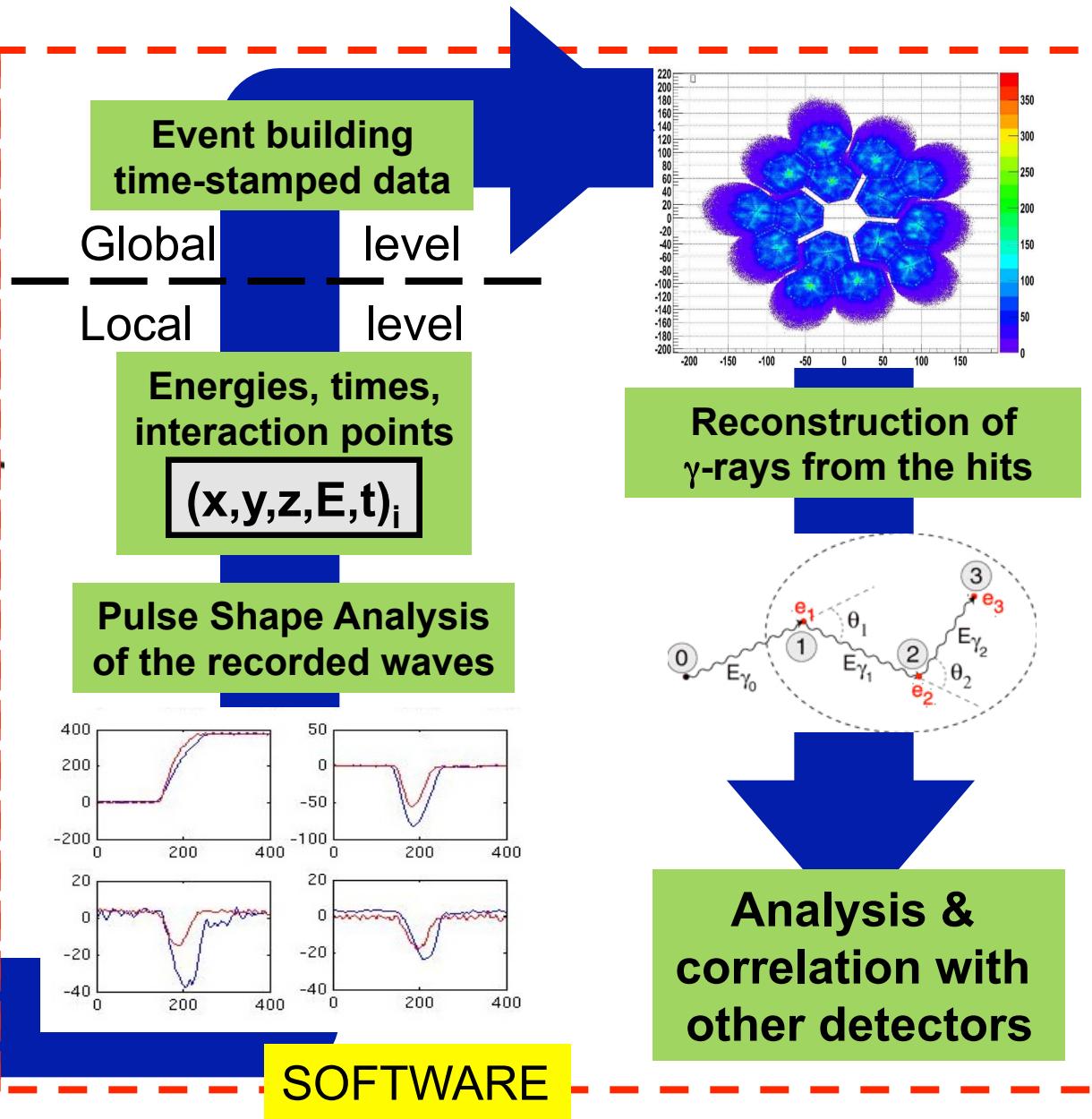
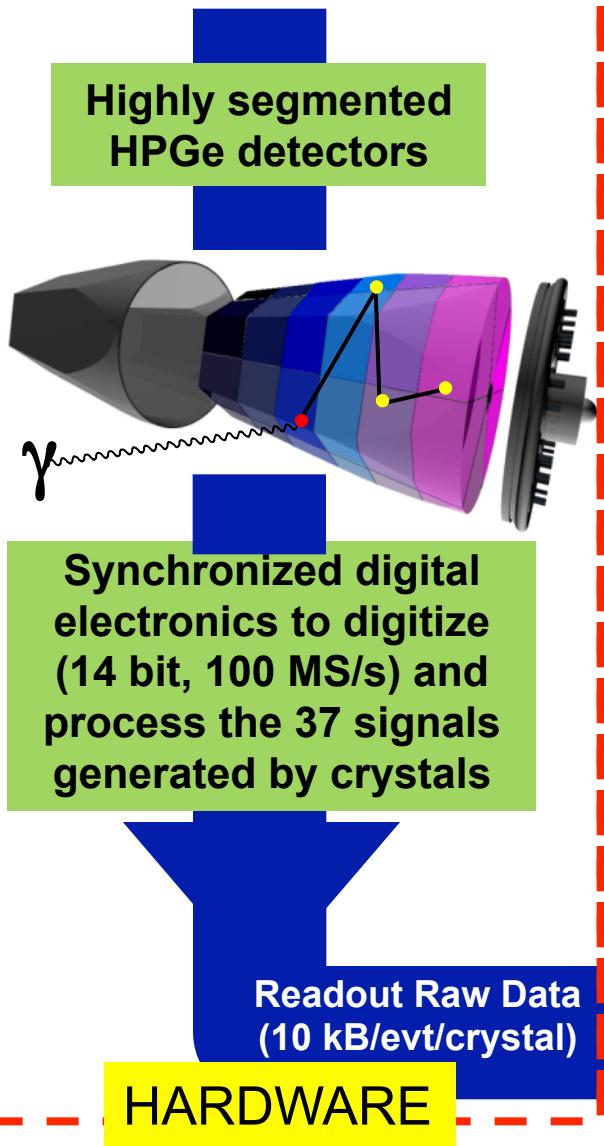
E. Gatti, et al. NIM 193 (82) 651



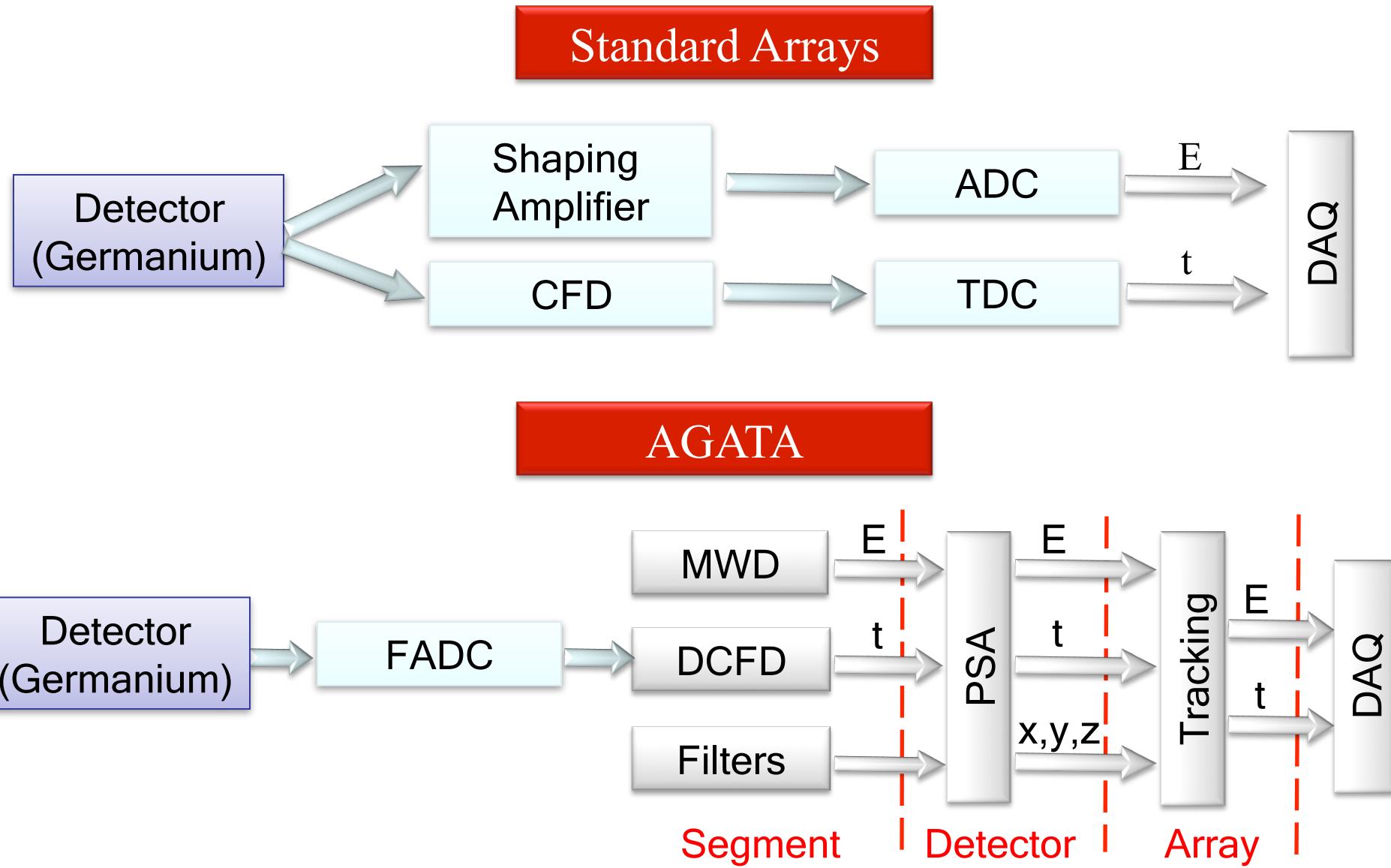
Figures courtesy of  
M.Ginsz, et al.,  
IPHC Strasbourg



# Gamma Tracking Array Concept

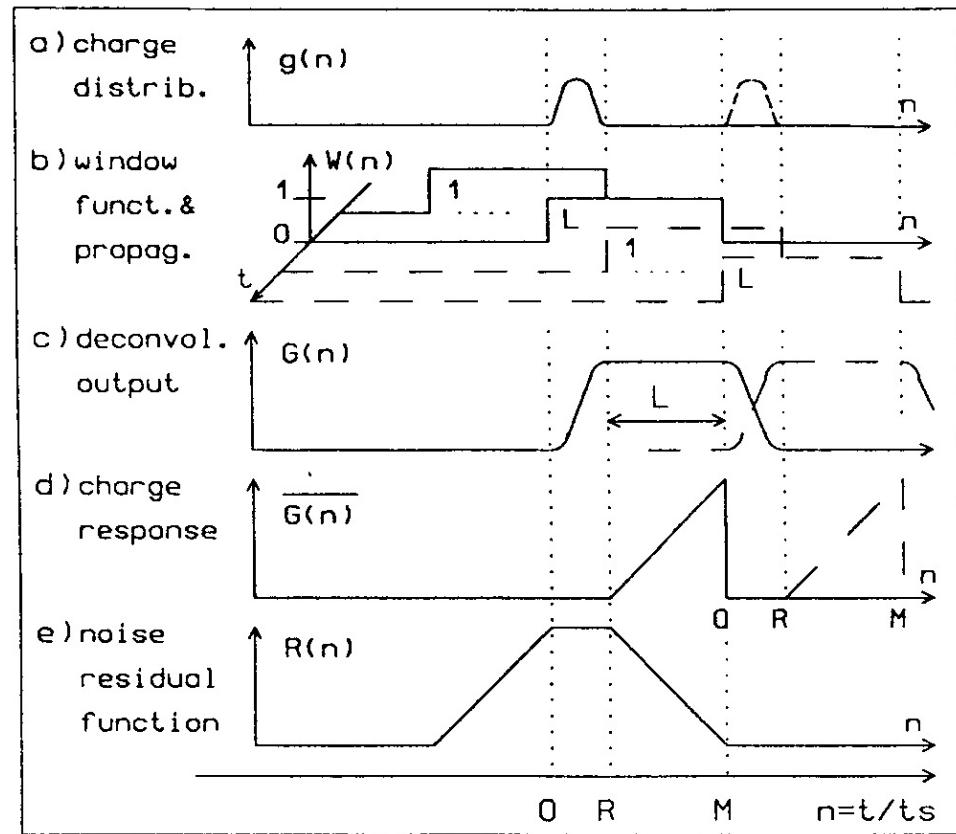


# Analogue vs Digital Electronics



# Energy with Digital signals: Moving Window Deconvolution

- removes shaping-effect of preamplifier  
⇒ current signal recovered
- calculates real collected charge by integrating current signal integration carried out within a moving window to avoid summation of events
- noise-suppression by averaging charge signal
- recursive algorithm

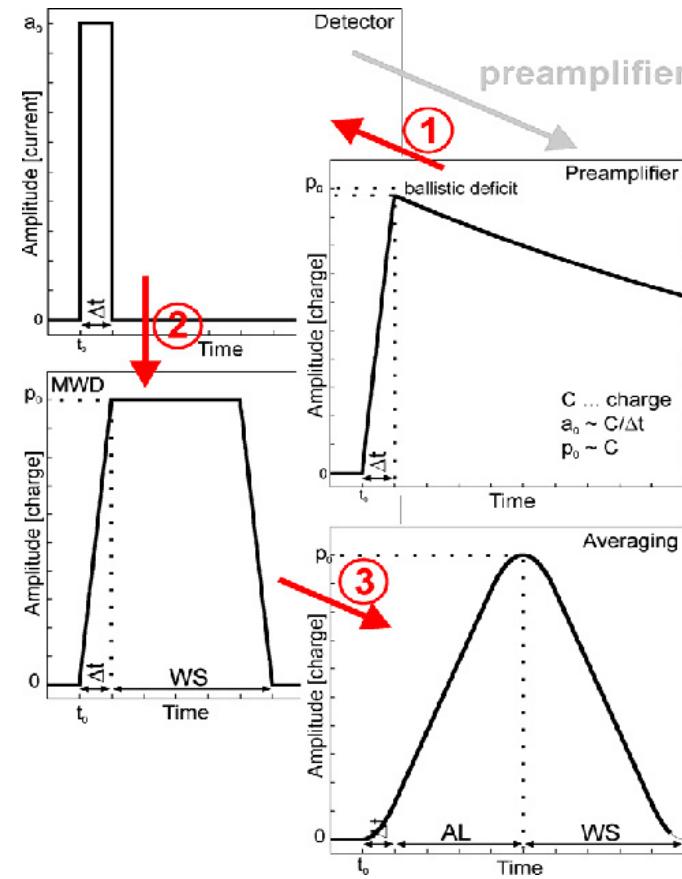


$$G[n] = G[n - 1] + \text{FADC}[n] - k \times \text{FADC}[n - 1] - \text{FADC}[n - L] + k \times \text{FADC}[n - L - 1]$$

$$K = \text{pre-amplifier response (e}^{-\alpha})$$

# Energy with Digital signals: Moving Window Deconvolution

- removes shaping-effect of preamplifier  
⇒ current signal recovered
- calculates real collected charge by integrating current signal integration carried out within a moving window to avoid summation of events
- noise-suppression by averaging charge signal
- recursive algorithm



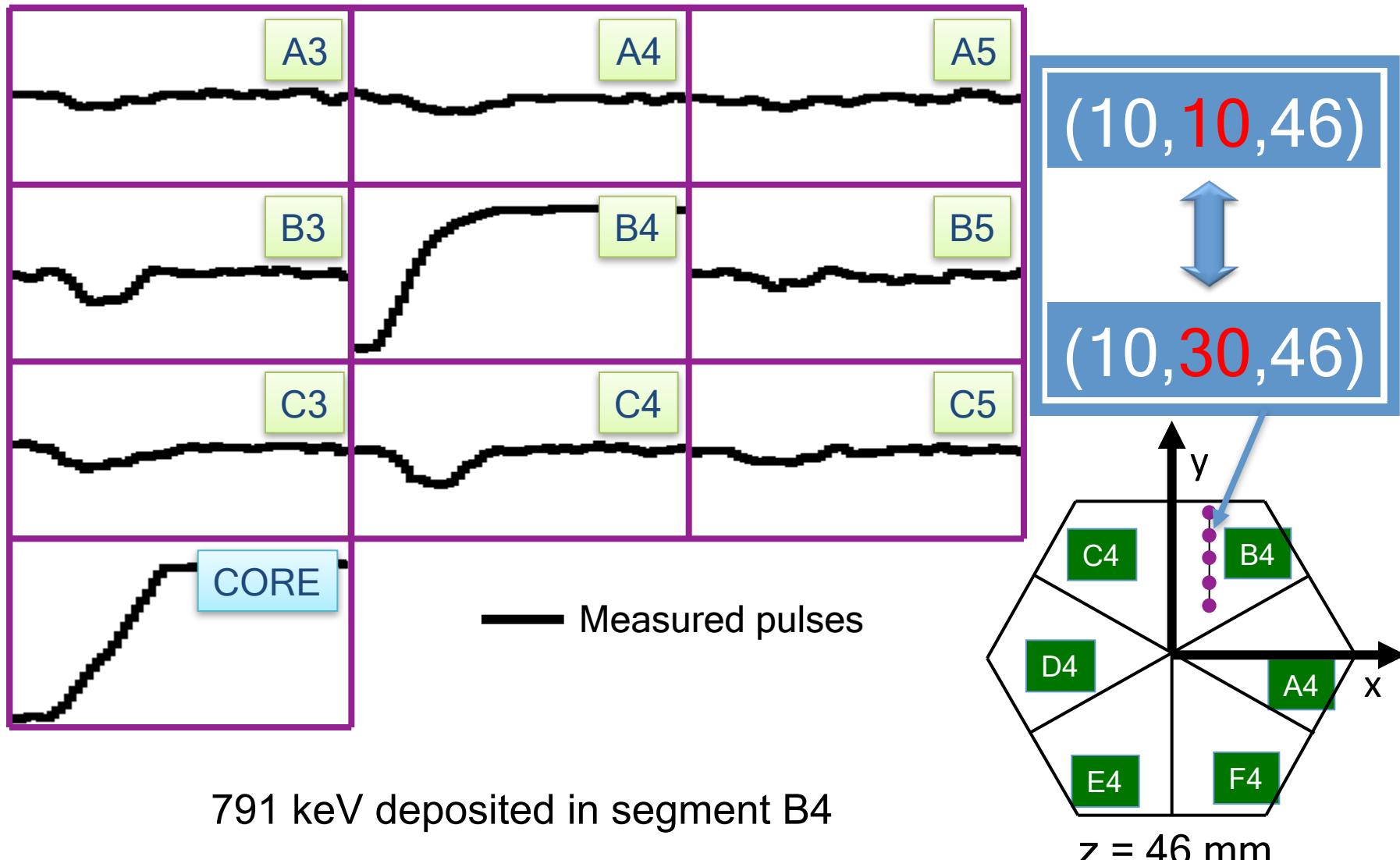
$$G[n] = G[n - 1] + FADC[n] - k \times FADC[n - 1] - FADC[n - L] + k \times FADC[n - L - 1]$$

$$k = \text{pre-amplifier response } (e^{-\alpha})$$

# Digital Pulse Processing for typical functions

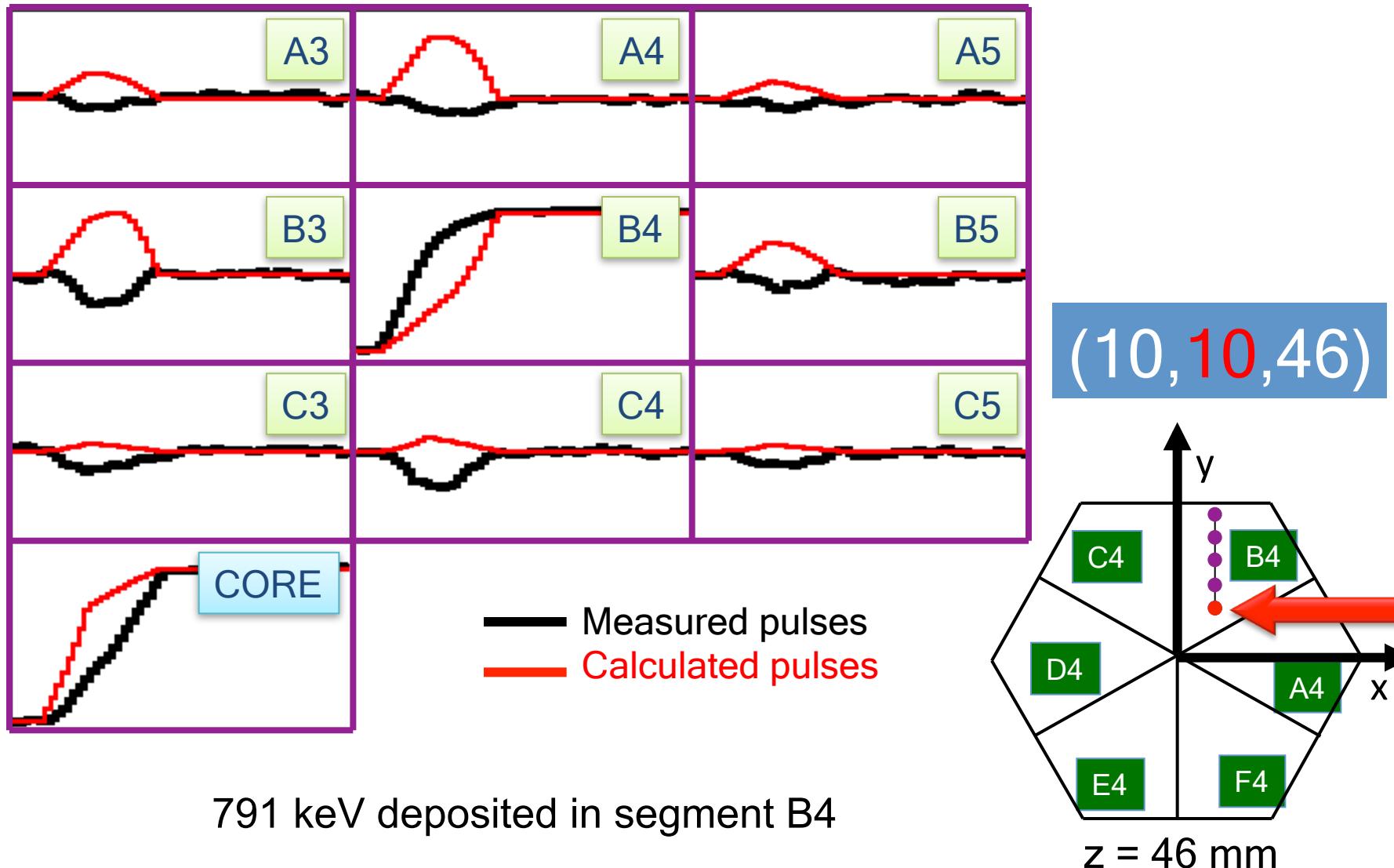
- *Leading Edge Discrimination:*
  - $y[n] = x[n] - x[n-k]$  (*differentiation*)
  - $y[n] = (x[n] + x[n-2]) + x[n-1] \ll 1$  (*Gaussian filtering*)
  - Threshold comparison  $\rightarrow$  LED time
- *Constant Fraction Discrimination:*
  - $y[n] = x[n] - x[n-k]$  (*differentiation*)
  - $y[n] = (x[n] + x[n-2]) + x[n-1] \ll 1$  (*Gaussian filtering*)
  - $y[n] = x[n-k] \ll a - x[n]$  (*constant fraction*)
  - Zero crossing comparison  $\rightarrow$  CFD time

# Pulse Shape Analysis Concept

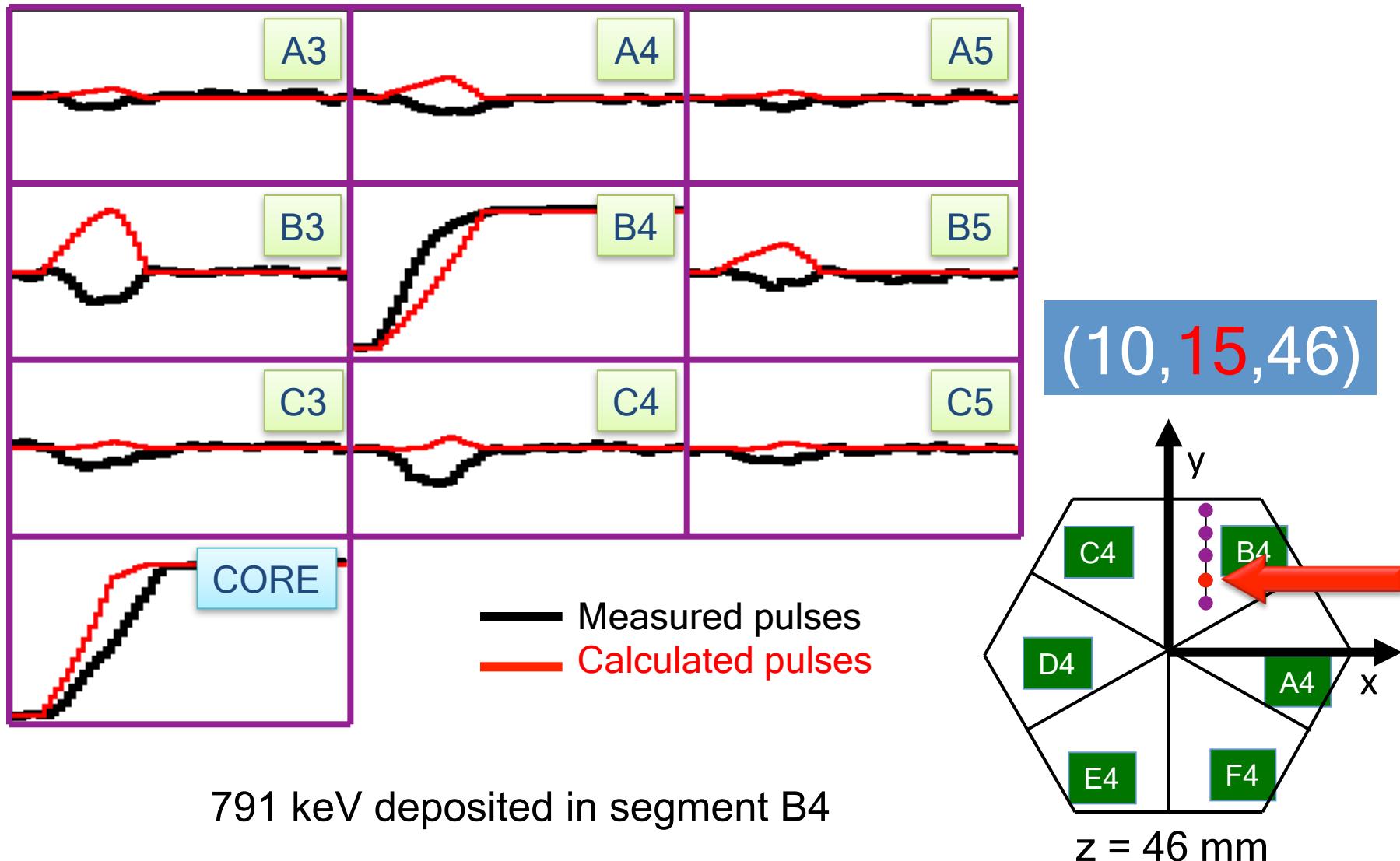


**Very Important: Measured pulses need to be time aligned**

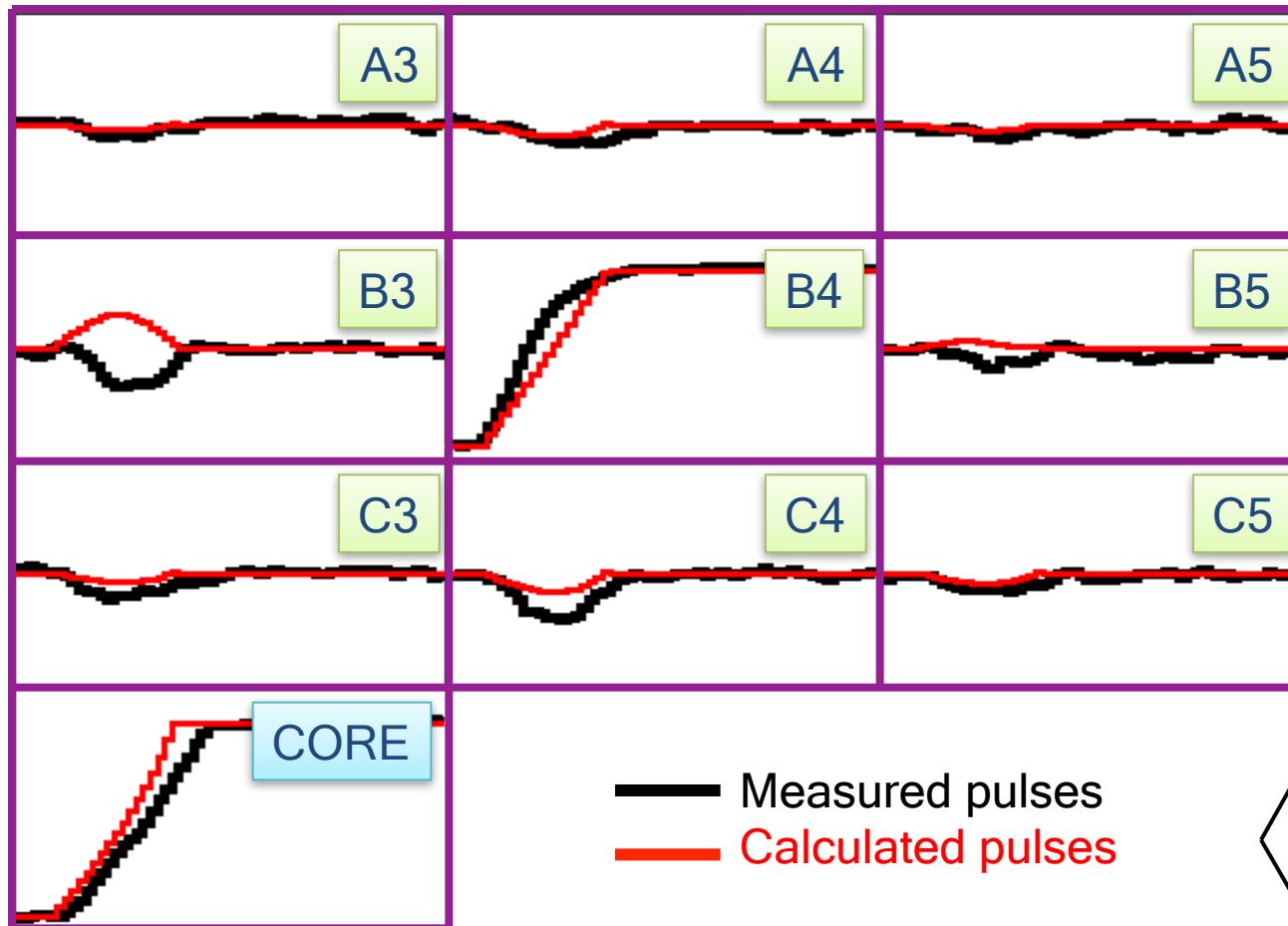
# Pulse Shape Analysis Concept



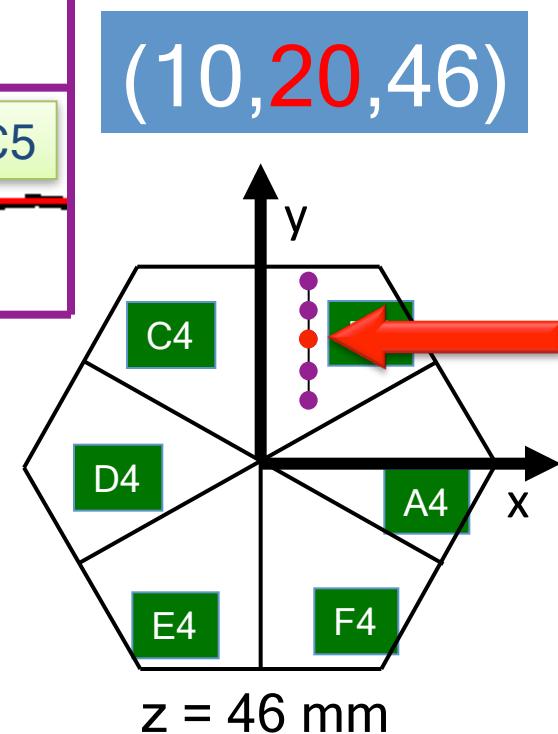
# Pulse Shape Analysis Concept



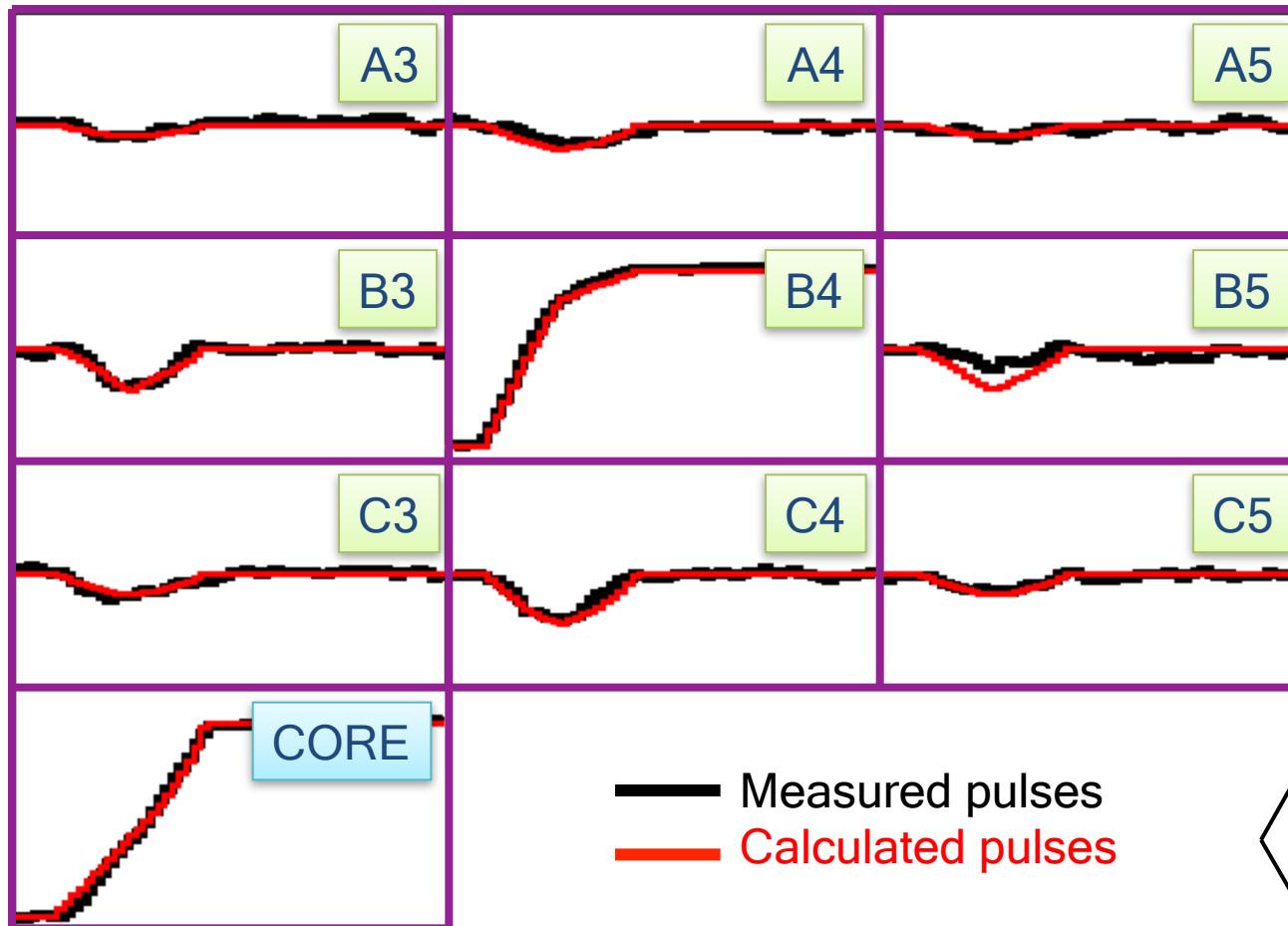
# Pulse Shape Analysis Concept



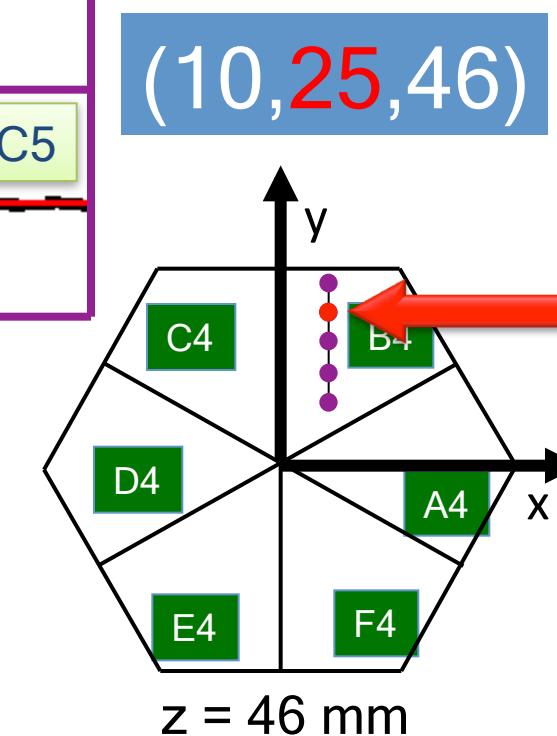
791 keV deposited in segment B4



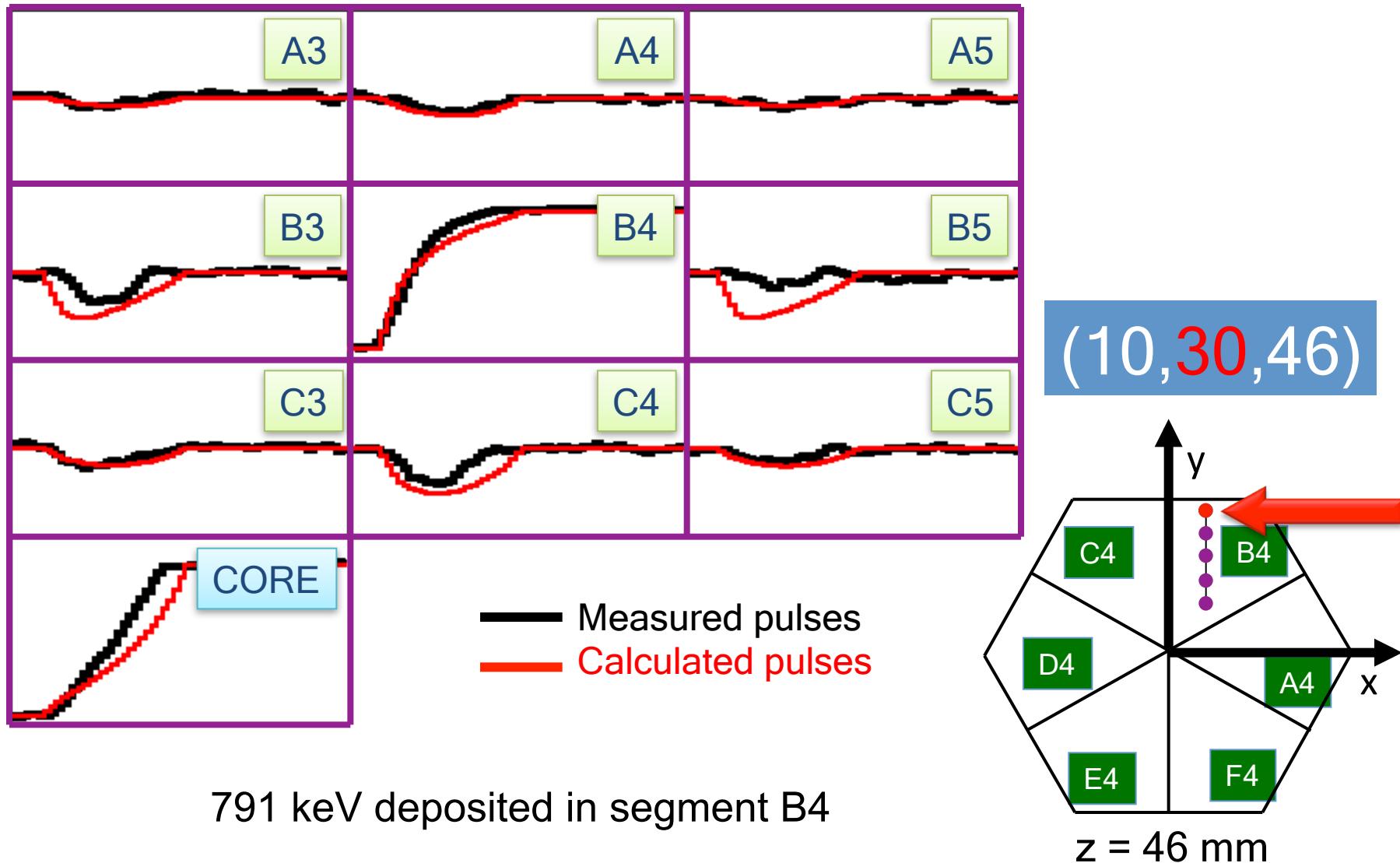
# Pulse Shape Analysis Concept



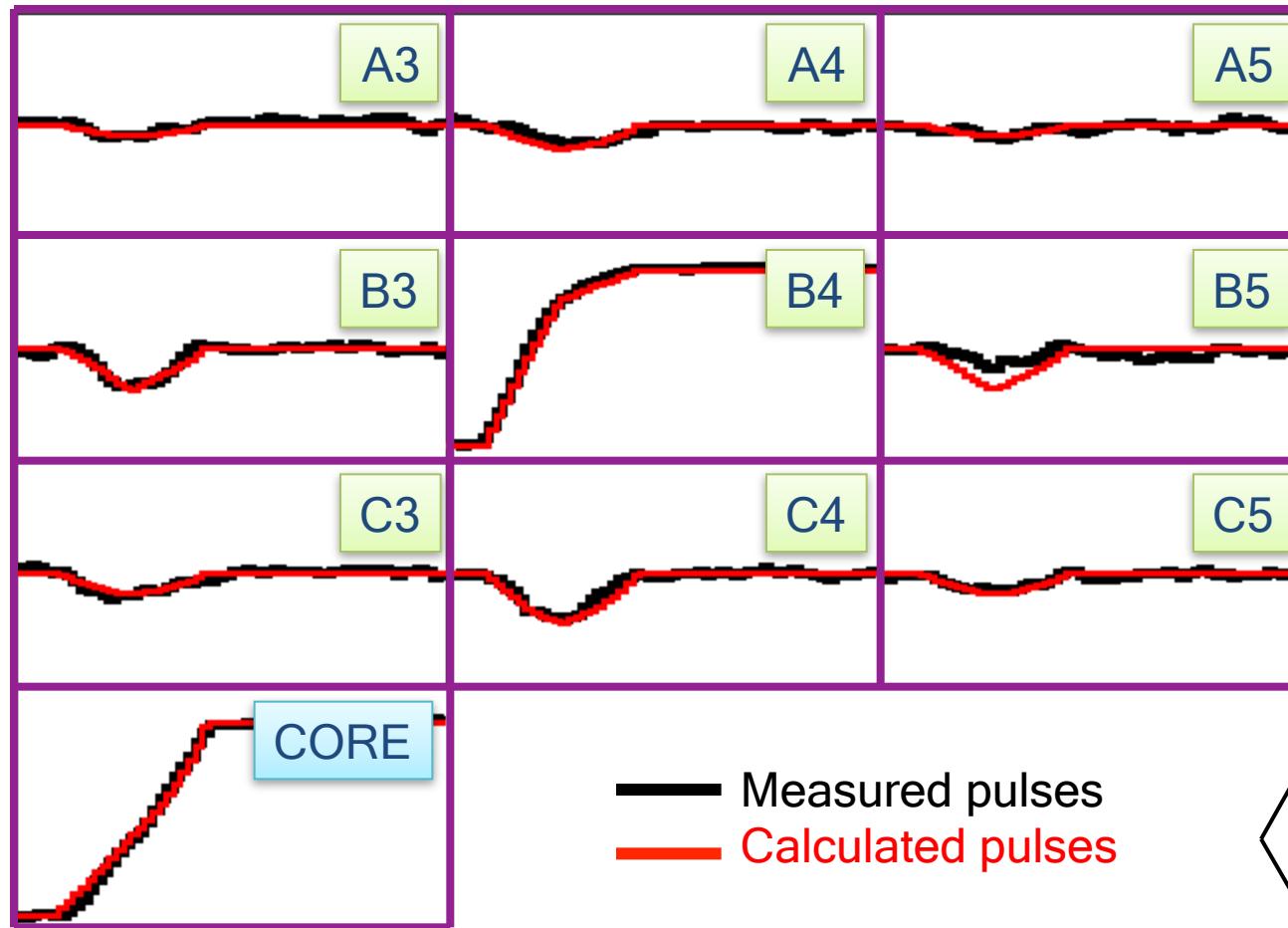
791 keV deposited in segment B4



# Pulse Shape Analysis Concept



# Pulse Shape Analysis Concept

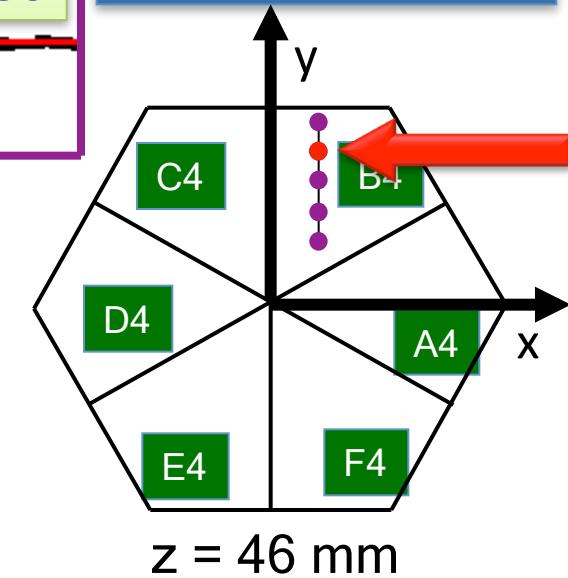


791 keV deposited in segment B4

Set of Energies +  
Interaction Positions  Tracking

Result of  
*Grid Search*  
algorithm  
*R. Venturelli*

(10,25,46)



# Interaction - Reconstruction Mechanisms

			$\sim 100 \text{ keV}$	$\sim 1 \text{ MeV}$	$\sim 10 \text{ MeV}$	$\gamma\text{-ray energy}$
Photoelectric	Compton Scattering	Pair Production				
Isolated hits	Angle/Energy	Pattern of hits				
Probability of interaction depth	$E_{\gamma'} = \frac{E_{\gamma}}{1 + \frac{E_{\gamma}}{m_0 c^2} (1 - \cos\theta)}$	$E_{1\text{st}} = E_{\gamma} - 2 mc^2$				

Reconstruction efficiencies are limited by :  
 Position resolution; Short range scattering; Compton profile.

# The tracking Algorithms in AGATA

Two main classes:

- algorithms based on back-tracking

J. Van der Marel, B. Cederwall, **NIMA 437 (1999) 538.**

J. Van der Marel, B. Cederwall, **NIMA 447 (2002) 391.**

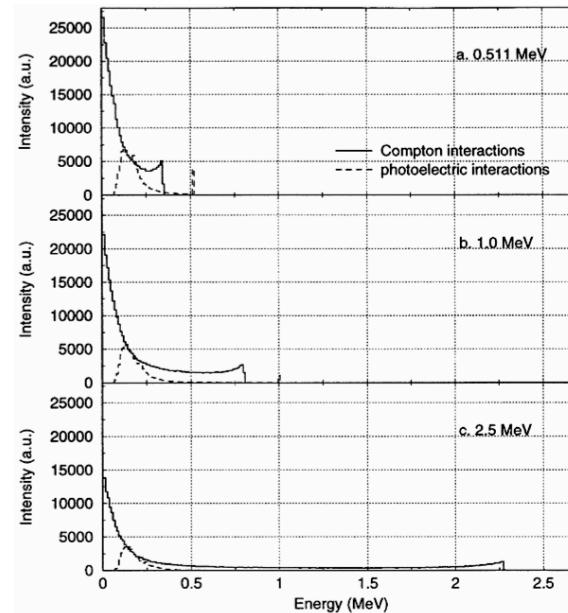
L. Milechina, B. Cederwall, **NIMA 508 (2003) 394.**

- algorithms based on clusterisation and forward-tracking

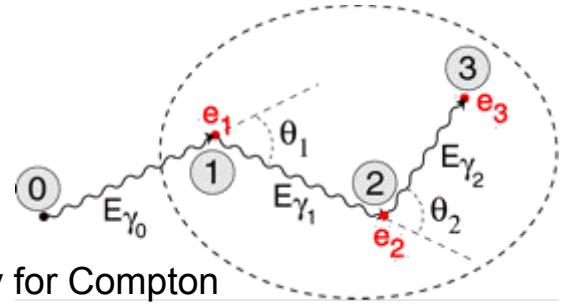
G.J. Schmid, et al., **NIMA 430 (1999) 69.**

D. Bazzacco, MGT code developed within the TMR program 'Gamma-ray tracking detectors'

I. Piqueras, et al. **NIMA 516 (2004) 122**



## Forward-tracking



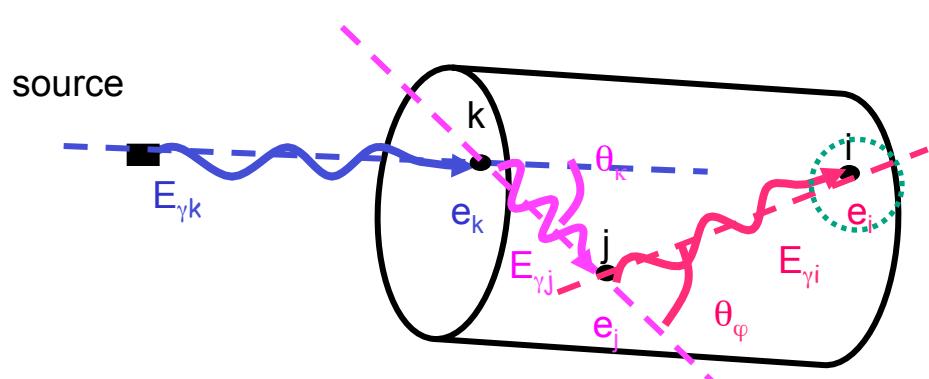
$$E_{s,p} = \frac{E_t}{1 + E_t/m_e c^2 (1 - \cos \theta_p)}$$

Probability for Compton or photoelectric and for the path in Germanium

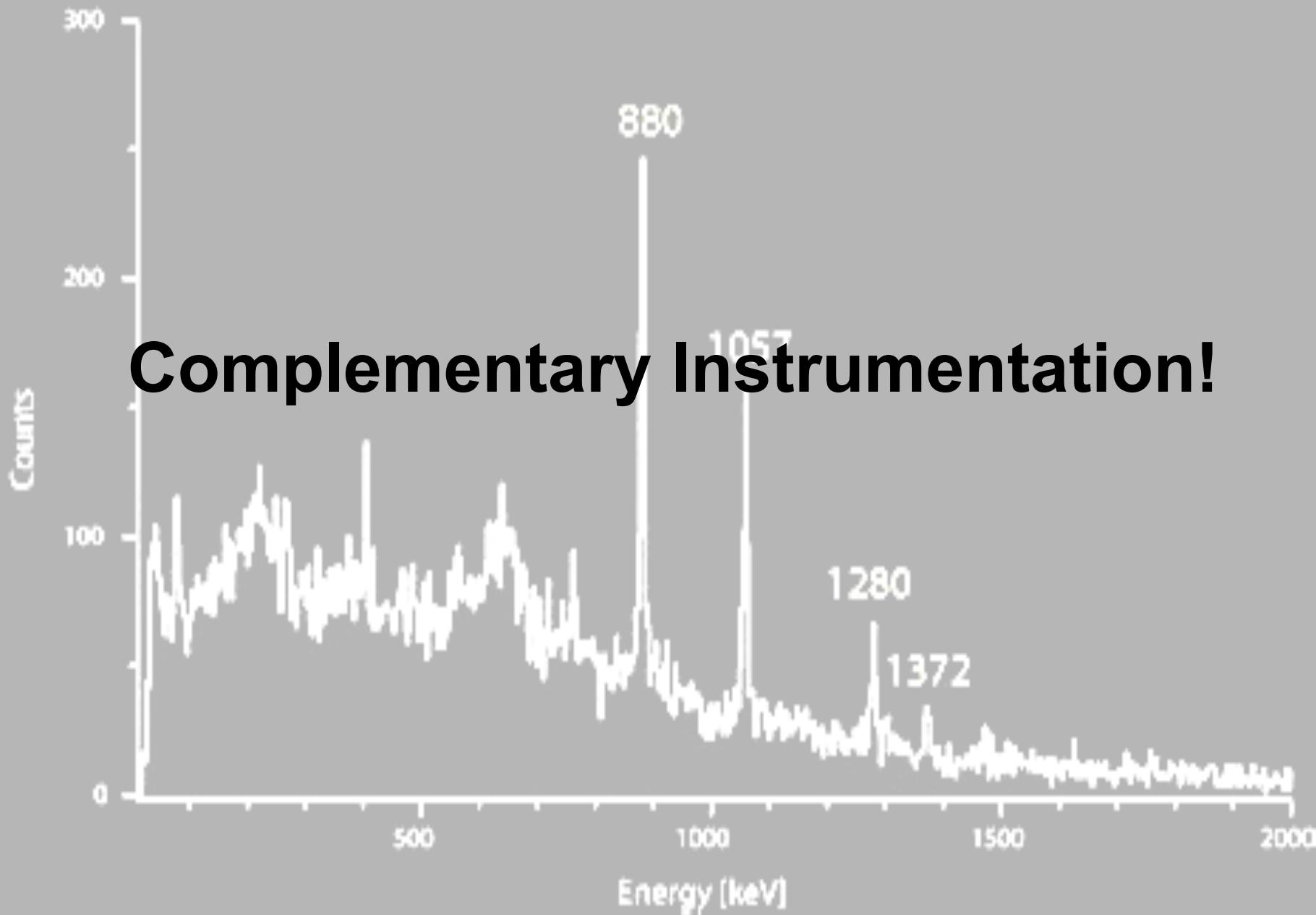
$$L = \prod_{n=1}^N P_n \exp \left[ - \left( \frac{E_{\gamma n} - E_{\gamma n, \text{pos}}}{\sigma_E} \right)^2 \right]$$

Likelihood

## Back-tracking



$$\cos(\theta) = 1 - m_e c^2 (1/E_{\text{sc}} - 1/E_{\text{inc}})$$



# Complementary Instrumentation

- Fundamental to increase the sensitivity of the  $\gamma$ -ray detector. Identifying the reaction channel or reaction products:
  - Particle detectors (Light charged particles or neutrons)
  - Spectrometers (Identification of the reaction products)
  - Beam Trackers (for relativistic experiments)
  - etc...
- Fundamental to perform some measurements
  - Plunger devices for RDDS measurements
  - Fast Scintillators for timing measurements
  - etc...