

# Charming Baryons

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# Outline

- One heavy **h** and three light **u**, **d**, **s** flavors are considered.
- Heavy Flavor Spin Symmetry (**HQSS**) is important.
- **P** and **V mesons** and **Baryons** with  $J = 1/2^+$  and  $3/2^+$  are considered as constituent hadrons.
- For hidden charm sector ( $N_c = N_{\bar{c}} = 1$ ), **meson**-**Baryon** Lagrangian with Heavy Flavor Spin Symmetry is constructed.
- Minimal extension of the  $SU(3)$  **WT** Lagrangian to fulfill **HQSS**
- No free parameter...



# Outline

- This interaction is presented in different ways:
  - ▶ Field Lagrangian
  - ▶ Hadron creation-annihilation operators
  - ▶  $SU(6) \times \text{HQSS}$  projectors
  - ▶ Multichannel Matrices
- Multichannel Bethe-Salpeter equation is solved  $T = V + VGT$
- Use of our **WT** extended model is done for
  - ▶ Hidden Charm  $N$  and  $\Delta$
  - ▶ Beauty Baryons ( $\Lambda_b$ )
- Study of Compositeness  $X = 1 - Z$  of  $\Lambda$ ,  $\Lambda_c$ ,  $\Lambda_b$  with  $J^P = 1/2^-, 3/2^-$



# $N$ and $\Delta$ with hidden charm $N_h = N_{\bar{h}} = 1$

- Quarks:  $q \in \{u, d, s\}$ ,  $h \in \{c, b\}$ .
- Heavy flavor  $\Rightarrow$  Heavy Quark Spin Symmetry ( $O(1/m_h)$ )  
 $HQSS = SU_h(2) \times SU_{\bar{h}}(2) \times U_h(1) \times U_{\bar{h}}(1)$ 
  - ▶ Hadrons: HQSS multiplets.
  - ▶  $(D^0, D^{*0})$  is a HQSS doublet. mesons : P and V.
  - ▶  $(\Xi'_c, \Xi_c^*)$  is a HQSS doublet. Baryons :  $B(1/2^+)$  and  $B(3/2^+)$
  - ▶ Lagrangian with HQSS .
- The resonances are generated by solving the Bethe- Salpeter equation  $T = V + VGT$  with the appropriate  $V$  interaction and meson -Baryon channels.
- Masses, widths and couplings of  $N$  and  $\Delta$  resonances are calculated.

[CGR, Nieves, Romanets, Salcedo, Tolos PRD87 (13) 074034]



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**mesons** :  $N_{\mathbf{h}} = 1, N_{\bar{\mathbf{h}}} = 0, (\mathbf{h}_{1/2}\bar{q}_{1/2})_{J=0, 1}$ ,

HQSS implies  $J^P = 0^-, 1^-$  are degenerated.

- Pseudoscalar  $D^+, D^0, D_s^+$  ( $3_1^*$ -plet) are HQSS partners of
- Vector  $D^{*+}, D^{*0}, D_s^{*+}$  ( $3_3^*$ -plet) mesons.
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SU<sub>SF</sub>(6) of spin-flavor for light quarks is also fulfilled.
- (P) + (V) with  $N_{\mathbf{h}} = 1$  are made of a light SU(6)  $6^*$ -plet coupled to the spin  $j_{\mathbf{h}} = 1/2$  of the  $\mathbf{h}$ -quark.

P  $3_1^*$ -plet      V  $3_3^*$ -plet  
 HQSS – doublet  
 $D_s^+ \quad D^+ \quad D^{*+}$   
 $D^0 \quad D^{*0}$



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# Constituent Heavy Baryons ( $\mathbf{h}qq$ )

- Baryons:**  $(\mathbf{h}_{j_h=1/2}(q_1 q_2)_{j_l})$ , considering that  $q_1 q_2$  are in a symmetric state in spin-flavor, they belong to a  $SU_{SF}(6)$  21-plet which can be reduced in  $SU_F(3) \times SU_S(2)$  as  $21 = 3_0^* \oplus 6_1$ 
  - HQSS Singlet**  $3_{j_l=0}^* \times \mathbf{h}_{j_h=1/2} = 3_{J=1/2}^*$ :  $\Lambda_{\mathbf{h}}, \Xi_{\mathbf{h}}$
  - HQSS Doublet**  $6_{j_l=1} \times \mathbf{h}_{j_h=1/2} = 6_{J=1/2, 3/2}$ :  
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$3_2^*$ -plet  
HQSS -singlet

$\Lambda_c^+$   
 $\Xi_c^0 \quad \Xi_c^+$

$6_2$ -plet

$\Sigma_c^0 \quad \Sigma_c^+ \quad \Sigma_c^{++}$   
 $\Xi_c'^0 \quad \Xi_c'^+$   
 $\Omega_c^{*0}$

HQSS -doublet

$6_4$ -plet

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$\Sigma_c^0 \quad \Sigma_c^+ \quad \Sigma_c^{++}$   
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- **Baryons:** ( $\mathbf{h}_{j_h=1/2}(q_1 q_2)_{j_l}$ ), considering that  $q_1 q_2$  are in a symmetric state in spin-flavor, they belong to a  $SU_{SF}(6)$  21-plet which can be reduced in  $SU_F(3) \times SU_S(2)$  as  $21 = 3_0^* \oplus 6_1$ 
  - ▶ **HQSS** Singlet  $3_{j_l=0}^* \times \mathbf{h}_{j_h=1/2} = 3_{J=1/2}^*$ :  $\Lambda_{\mathbf{h}}, \Xi_{\mathbf{h}}$
  - ▶ **HQSS** Doublet  $6_{j_l=1} \times \mathbf{h}_{j_h=1/2} = 6_{J=1/2, 3/2}$ :  
 $\Sigma_{\mathbf{h}}, \Xi'_{\mathbf{h}}, \Omega_{\mathbf{h}}$  with  $J = 1/2$  are **HQSS** partners of  
 $\Sigma_{\mathbf{h}}^*, \Xi_{\mathbf{h}}^*, \Omega_{\mathbf{h}}^*$  with  $J = 3/2$ .

$3_2^*$ -plet  
HQSS -singlet

$\Lambda_c^+$   
 $\Xi_c^0 \quad \Xi_c^+$

$6_2$ -plet

$\Sigma_c^0 \quad \Sigma_c^+ \quad \Sigma_c^{++}$   
 $\Xi_c'^0 \quad \Xi_c'^+$   
 $\Omega_c^{*0}$

$6_4$ -plet

HQSS -doublet

$\Sigma_c^{*0} \quad \Sigma_c^{*+} \quad \Sigma_c^{*++}$   
 $\Xi_c^{*0} \quad \Xi_c^{*+}$   
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# Constituent light hadrons, $(q\bar{q})$ and $(qqq)$

- For consistency: P and V mesons and  $1/2^+$  and  $3/2^+$  Baryons .
- The light mesons are those of the  $35\text{-SU}(6)\text{-plet} = 8_1 \oplus (8_3 \oplus 1_3)$ , which includes the pseudoscalar meson octet of the pions,  $(\pi, \eta, K, \bar{K}) \in 8_1$  and the vector nonet of the rho-mesons,  $(\rho, \omega, \phi, K^*, \bar{K}^*) \in 8_3 \oplus 1_3$ .
- The Baryons are those of the  $56\text{-SU}(6)\text{-plet} = 8_2 \oplus 10_4$ , made of the  $1/2^+$  octet of the N ( $N, \Lambda, \Sigma, \Xi$ ) and the  $3/2^+$  decuplet of the  $\Delta$  ( $\Delta, \Sigma^*, \Xi^*, \Omega$ ).



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# Hadronic Building Blocks

$$\bar{\mathbf{D}} = (\{\bar{D}, \bar{D}^*\}, \{\bar{D}_s, \bar{D}_s^*\}),$$

$$\psi = \{\eta_c, \psi\},$$

$$\mathbf{N} = (N, \Sigma, \Xi, \Lambda),$$

$$\Delta = (\Delta, \Sigma^*, \Xi^*, \Omega),$$

$$\Xi_c = (\Xi_c, \Lambda_c),$$

$$\Sigma_c = (\{\Sigma_c, \Sigma_c^*\}, \{\Xi'_c, \Xi_c^*\}, \{\Omega_c, \Omega_c^*\}).$$





- Focus on the sector with hidden charm and  $C = 0$ .
- Write down the most general (modulo kinematical factors)  $S$ -wave Lagrangian consistent with  $SU(3) \times \text{HQSS}$  for the baryon-meson coupled-channels space.
- For this purpose it is convenient to organize the hadrons forming multiplets of  $\text{HQSS}$  into building blocks with well defined HQSS transformation properties. *[Falk, Grinstein, Jenkins, Manohar, Wise].*

Specifically, consider a HQSS doublet composed of pseudoscalar meson and vector meson with one heavy quark (e.g.  $D$  and  $D^*$ ).

HQSS field doublets:

$$\begin{aligned} \mathbf{D} &= Q_+ (D^*_{\mu}^{(+)} \gamma^{\mu} + D^{(+)} \gamma_5), \\ \psi &= Q_+ (\psi_{\mu}^{(+)} \gamma^{\mu} + \eta_c^{(+)} \gamma_5). \end{aligned}$$

As usual  $(+)$  represents the positive frequency part of the fields, corresponding to purely annihilation field.

$$Q_+ = \frac{1 + \not{v}}{2} \quad (-1)$$

where  $v^{\mu}$  is the heavy hadron velocity ( $v^2 = 1$ )

[ A.V. Manohar and M.B. Wise, *Heavy Quark Physics*, Cambridge Monographs on Particle Physics, Nuclear Physics and Cosmology, vol. 10 (2000).]



## HQSS $N_h = 1$ Baryon doublets:

$$\Sigma_c^\mu = \Sigma_c^{*\mu(+)} + \frac{1}{\sqrt{3}}(\gamma^\mu + v^\mu)\gamma_5 \Sigma_c^{(+)}.$$

- $\Sigma_c$  is the Dirac spinor of the  $1/2^+$  baryon in the doublet
- $\Sigma_c^{*\mu}$  is the Rarita-Schwinger field for the  $3/2^+$  baryon  
 $v_\mu \Sigma_c^{*\mu} = \gamma_\mu \Sigma_c^{*\mu} = 0.$

Finally, for a HQSS singlet baryon with exactly one  $h$  quark (e.g.,  $\Lambda_c$ )

## HQSS $N_h = 1$ Baryon singlets:

$$\Lambda_c = \Lambda_c^{(+)}, \quad \overline{\Lambda}_c = \Lambda_c^\dagger \gamma_0 = \overline{\Lambda}_c^{(-)}$$

[ A.V. Manohar and M.B. Wise, *Heavy Quark Physics*, Cambridge Monographs on Particle Physics, Nuclear Physics and Cosmology, vol. 10 (2000). ]

# Lagrangian with SU(3)– and HQSS symmetries

[CGR, Nieves, Romanets, Salcedo, Tolos PRD87 (13) 074034]

Hidden Heavy Flavor:  $N_h = 1$ ,  $N_{\bar{h}} = 1$

- Next, we write down the 12 most general operators allowed by  $SU(3) \times \text{HQSS}$  in the baryon-meson coupled-channels space, in  $S$ -wave and preserving parity.
- The operator  $\overset{\leftrightarrow}{\partial}_\nu = v^\mu (\overset{\rightarrow}{\partial}_\mu - \overset{\leftarrow}{\partial}_\mu)$  acts on the mesons only
- and it is introduced in order to produce the correct kinematical dependence in the amplitudes.

$$\begin{aligned}\mathcal{L}_1(x) &= g_1 \bar{N}^a_b N^b_a \text{tr}(\bar{\psi} i \overset{\leftrightarrow}{\partial}_\nu \psi), \\ \mathcal{L}_2(x) &= g_2 \frac{1}{3!} \bar{\Delta}^\mu_{abc} \Delta^{abc}_\mu \text{tr}(\bar{\psi} i \overset{\leftrightarrow}{\partial}_\nu \psi),\end{aligned}$$

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\mathcal{L}_3(x) &= g_3 \bar{\Xi}^a_c \psi (-i \overleftrightarrow{\partial}_\nu) \bar{D}_b N^b_a + \text{h.c.}, \\
\mathcal{L}_4(x) &= g_4 \epsilon^{bcd} \bar{\Sigma}^\mu_{ab} \psi (-i \overleftrightarrow{\partial}_\nu) \bar{D}_c \gamma_\mu \gamma_5 N^a_d + \text{h.c.}, \\
\mathcal{L}_5(x) &= g_5 \frac{1}{2} \bar{\Sigma}^\mu_{ab} \psi (-i \overleftrightarrow{\partial}_\nu) \bar{D}_c \Delta^\mu_{abc} + \text{h.c.}, \\
\mathcal{L}_6(x) &= g_6 \bar{\Xi}^a_c \Xi_{ca} \text{tr}(\bar{D}_b i \overleftrightarrow{\partial}_\nu \bar{D}^b), \\
\mathcal{L}_7(x) &= g_7 \bar{\Xi}^a_c \Xi_{cb} \text{tr}(\bar{D}_a i \overleftrightarrow{\partial}_\nu \bar{D}^b), \\
\mathcal{L}_8(x) &= g_8 \epsilon^{bcd} \bar{\Sigma}^\mu_{ab} \Xi_{cd} \text{tr}(\bar{D}_c \gamma_\mu \gamma_5 i \overleftrightarrow{\partial}_\nu \bar{D}^a) + \text{h.c.}, \\
\mathcal{L}_9(x) + \mathcal{L}_{10}(x) &= \frac{1}{2} \bar{\Sigma}^\mu_{ab} \Sigma_c^{\nu ab} \text{tr}(\bar{D}_c (g_9 g_{\mu\nu} + g_{10} i \sigma_{\mu\nu}) i \overleftrightarrow{\partial}_\nu \bar{D}^c), \\
\mathcal{L}_{11}(x) + \mathcal{L}_{12}(x) &= \bar{\Sigma}^\mu_{ac} \Sigma_c^{\nu bc} \text{tr}(\bar{D}_b (g_{11} g_{\mu\nu} + g_{12} i \sigma_{\mu\nu}) i \overleftrightarrow{\partial}_\nu \bar{D}^a).
\end{aligned}$$

The traces refer to Dirac space.

- It has **12** independent terms.
- We want to use symmetries or appropriate assumptions to reduce them
- Enforcing also  $SU(6)$  **light spin-flavor** and **Chiral** symmetries
- plus *minimal* extension of **WT** interaction, only **one** independent combination remains.

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# Justifying SU(6) light SF symmetry

- Theoretical reasons:

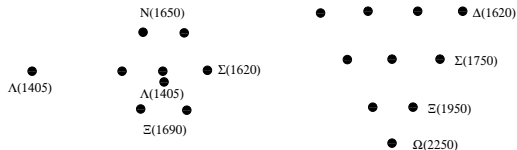
- ▶ Experimental spectroscopy
- ▶ Large  $N_C$  limit
- ▶ LQCD results

- Previous Calculations:

- ▶  $\Lambda_c \dots$ , “Charmed baryon resonances”,  
PRD 79, 054004 (2009), CGR, Magas, Mizutani, Nieves, Ramos, Salcedo, Tolos
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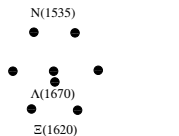
# Odd-parity light excited baryon resonances

SU(6): 70

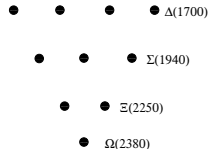
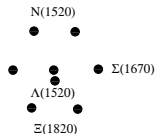


$$J^P = \frac{1}{2}^-$$

SU(6): 56



$$J^P = \frac{3}{2}^-$$



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- Practical reasons:

- ▶ P and V mesons has to be included together (HQSS).
- ▶  $1/2^+$  and  $3/2^+$  Baryons also.
- ▶ Importance of P and V mesons interferences.
- ▶ Reduce number of parameters.

# Extended WT model with $SU(6)$ and HQSS

- Unique  $SU(2N_F)$  extension of  $SU(3)$  **WT** interaction:

$$H_{WT} = H_{ex} + H_{ac},$$

- Including **heavy** flavors:

**$h\bar{h}$**  annihilation in  $H_{ac}$  breaks HQSS

$H_{WT}$  is not **HQSS**

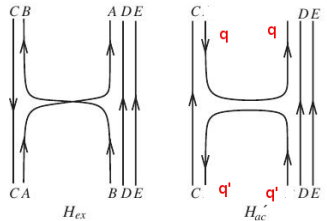
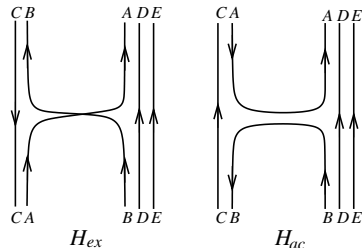
- Minimal modification to impose **HQSS**

▶ **Omit  $h\bar{h}$**  annihilation in  $H$

▶  $A, B \notin \mathbf{h}$  for  $H_{ac}'$ ,

$H_{WT}' = H_{ex} + H_{ac}'$  is **HQSS**

- $H_{WT}'$  keeps light spin-flavor  $SU(6)$ , **HQSS** and Chiral symmetries.



Our extended **WT** model with **SF** and **HQSS** gives the following values for the parameters:

$$\hat{g}_i = 4f^2 g_i,$$

$$N\psi \rightarrow N\psi, \quad \hat{g}_1 = 0, \quad \text{OZI rule}$$

$$\Delta\psi \rightarrow \Delta\psi, \quad \hat{g}_2 = 0, \quad \text{OZI rule}$$

$$N\psi \leftrightarrow \Xi_c \bar{D}, \quad \hat{g}_3 = \sqrt{3/2},$$

$$N\psi \leftrightarrow \Sigma_c \bar{D}, \quad \hat{g}_4 = \sqrt{1/6},$$

$$\Delta\psi \leftrightarrow \Sigma_c \bar{D}, \quad \hat{g}_5 = -1,$$

$$\Xi_c \bar{D} \rightarrow \Xi_c \bar{D}, \quad \hat{g}_6 = 1/2, \quad \hat{g}_7 = -1/2,$$

$$\Xi_c \bar{D} \leftrightarrow \Sigma_c \bar{D}, \quad \hat{g}_8 = 1/2,$$

$$\Sigma_c \bar{D} \rightarrow \Sigma_c \bar{D}, \quad \hat{g}_9 = \hat{g}_{10} = 0, \hat{g}_{11} = \hat{g}_{12} = -1/2.$$

Our model fulfills OZI rule (the vanishing of  $g_1$  and  $g_2$ ).

# Hidden Gauge Model

- **Hidden gauge model** also fulfills **HQSS** and reduces to **SU(3) WT** potential for the hidden charm  $N$ ,  $\Delta$ ,  $\Lambda$  sector.
- It gives a different set of  $g_i$  parameters.
- The **HQSS** extension of **WT** model is not unique.
- The model has been recently used for studying hidden beauty baryon states.

CW Xiao, J Nieves, E Oset - PRD 88 (2013) 056012 “Combining heavy quark spin and local hidden gauge symmetries in the dynamical generation of hidden charm baryons”

CW Xiao, E Oset - Eur.Phys.J. A49 (2013) 139, “Hidden beauty baryon states in the local hidden gauge approach with heavy quark spin symmetry “



- We should note that we actually compute the matrix elements of our interaction using directly the expressions
  - ▶ either in terms of hadron creation and annihilation operators in spin-flavor space, by taking Wick contractions.

$$\begin{aligned}
 H_{\text{WT}}' &= H_{\text{ex}} + H_{\text{ac}}', \\
 H_{\text{ex}} &= : M^A_C M^{\dagger C}_B B^{BDE} B_{ADE}^{\dagger} :, \quad A, \dots, E = 1, \dots, 2N_F, \\
 H_{\text{ac}}' &= - : M^{\dagger a}_C M^C_b B^{bDE} B_{aDE}^{\dagger} :, \quad a, b = 1, \dots, 2(N_F - 1).
 \end{aligned}$$

- ▶ Or given in terms of projectors using Clebsch-Gordan coefficients

$$\mathcal{H}_{C=0} = \mathbf{56}_{2,0} \oplus \mathbf{56}_{2,0} \oplus \mathbf{70}_{2,0}, \quad (\text{SU}(6) \times \text{HQSS}) \quad R_{2j_c+1, C}.$$

The eigenvalues turn out to be  $\lambda_{\mathbf{56}_{2,0}} = \lambda_{\mathbf{70}_{2,0}} = -2$ ,  $\lambda'_{\mathbf{56}_{2,0}} = 6$ .

- Nevertheless, writing the interaction in field-theoretical Lagrangian form is highly interesting in order to make contact with alternative approaches in the literature.



# Multichannel form of interaction

The final expression for the potential to be used throughout this work is

$$V_{ij}^{CSIJ} = D_{ij}^{CSIJ} \frac{1}{4f_i f_j} (k_i^0 + k_j'^0) ,$$

where  $k_i^0$  and  $k_j'^0$  are the CM energies of the incoming and outgoing mesons, respectively, and  $f_i$  and  $f_j$  are the decay constants of the meson in the  $i$ -channel and  $j$ -channel.

Table :  $N(1/2^-)$ ,  $C = 0$ ,  $S = 0$ ,  $I = 1/2$ ,  $J = 1/2$ .

$D^{CSIJ}$	$N\eta_c$	$N\psi$	$\Lambda_c \bar{D}$	$\Lambda_c \bar{D}^*$	$\Sigma_c \bar{D}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$
$N\eta_c$	0	0	$\sqrt{\frac{3}{2}}$	$-\sqrt{\frac{9}{2}}$	$\sqrt{\frac{3}{2}}$	$\sqrt{\frac{1}{2}}$	2
$N\psi$	0	0	$-\sqrt{\frac{9}{2}}$	$-\sqrt{\frac{3}{2}}$	$\sqrt{\frac{1}{2}}$	$\sqrt{\frac{25}{6}}$	$-\sqrt{\frac{4}{3}}$
$\Lambda_c \bar{D}$	$\sqrt{\frac{3}{2}}$	$-\sqrt{\frac{9}{2}}$	1	0	0	$-\sqrt{3}$	$\sqrt{6}$
$\Lambda_c \bar{D}^*$	$-\sqrt{\frac{9}{2}}$	$-\sqrt{\frac{3}{2}}$	0	1	$-\sqrt{3}$	-2	$-\sqrt{2}$
$\Sigma_c \bar{D}$	$\sqrt{\frac{3}{2}}$	$\sqrt{\frac{1}{2}}$	0	$-\sqrt{3}$	-1	$\sqrt{\frac{4}{3}}$	$\sqrt{\frac{2}{3}}$
$\Sigma_c \bar{D}^*$	$\sqrt{\frac{1}{2}}$	$\sqrt{\frac{25}{6}}$	$-\sqrt{3}$	-2	$\sqrt{\frac{4}{3}}$	$\frac{1}{3}$	$-\sqrt{\frac{2}{9}}$
$\Sigma_c^* \bar{D}^*$	2	$-\sqrt{\frac{4}{3}}$	$\sqrt{6}$	$-\sqrt{2}$	$\sqrt{\frac{2}{3}}$	$-\sqrt{\frac{2}{9}}$	$\frac{2}{3}$



Table :  $N(3/2^-)$ ,  $C = 0$ ,  $S = 0$ ,  $I = 1/2$ ,  $J = 3/2$ .

$D^{CSIJ}$	$N\psi$	$\Lambda_c \bar{D}^*$	$\Sigma_c^* \bar{D}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$
$N\psi$	0	$\sqrt{6}$	$-\sqrt{2}$	$\sqrt{\frac{2}{3}}$	$-\sqrt{\frac{10}{3}}$
$\Lambda_c \bar{D}^*$	$\sqrt{6}$	1	$-\sqrt{3}$	1	$-\sqrt{5}$
$\Sigma_c^* \bar{D}$	$-\sqrt{2}$	$-\sqrt{3}$	-1	$-\sqrt{\frac{1}{3}}$	$\sqrt{\frac{5}{3}}$
$\Sigma_c \bar{D}^*$	$\sqrt{\frac{2}{3}}$	1	$-\sqrt{\frac{1}{3}}$	$-\frac{5}{3}$	$-\sqrt{\frac{5}{9}}$
$\Sigma_c^* \bar{D}^*$	$-\sqrt{\frac{10}{3}}$	$-\sqrt{5}$	$\sqrt{\frac{5}{3}}$	$-\sqrt{\frac{5}{9}}$	$-\frac{1}{3}$



# Previous hidden charm investigations

- Hidden gauge formalism
  - ▶ J.-J. Wu, R. Molina, E. Oset, and B. S. Zou, Phys. Rev. C 84, 015202 (2011),
  - ▶ J.-J. Wu, T.-S. H. Lee, and B. S. Zou, Phys. Rev. C 85, 044002 (2012).
- Zero range vector exchange model
  - ▶ J. Hofmann and M. F. M. Lutz, Nucl. Phys. A763, 90 (2005),
  - ▶ J. Hofmann and M. F. M. Lutz, Nucl. Phys. A776, 17 (2006).
- Constituent quark model
  - ▶ S. G. Yuan, K.W. Wei, J. He, H. S. Xu, and B. S. Zou, Eur. Phys. J. A 48, 61 (2012).



# Hidden charm resonances

[*CGR, Nieves, Romanets, Salcedo, Tolos PRD87 (13) 074034*]

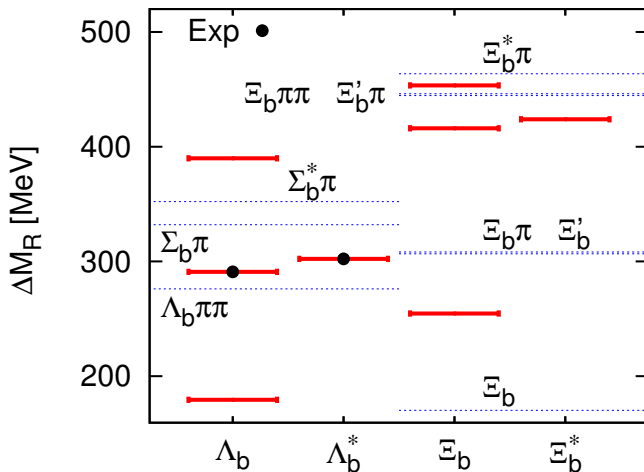
Ref.	Model	$M_R$ [MeV]	$N(1/2^-)$ $g$ to main channels					$N(3/2^-)$ $g$ to main channels					$N(5/2^-)$ $g$	
			$\Lambda_c \bar{D}$	$\Lambda_c \bar{D}^*$	$\Sigma_c \bar{D}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$	$M_R$ [MeV]	$\Lambda_c \bar{D}^*$	$\Sigma_c \bar{D}^*$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$	$M_R$ [MeV]	$\Sigma_c^* \bar{D}^*$
This work:	$(8_2)_{2,0} \subset 70_{2,0}$	3918	3.1	0.5	0.2	2.6	2.6							
		3926	0.4	3.0	4.2	0.2	0.7	3946	3.4	3.6	1.1	1.5		
	$(8_4)_{2,0} \subset 70_{2,0}$	3974	0.4	2.2	2.1	3.4	3.1	3987	1.0	2.7	4.3	1.8		
								4006	1.0	1.6	3.2	4.2	4027	5.6
[65,66]	zero range vector exchange	3520				5.3		3430				5.6		
[75]	hidden gauge	4265	0.1		3.0									
		4415		0.1		2.8		4415	0.1		2.8			
[76]	hidden gauge	4315	$\times$		$\times$									
		4454		$\times$		$\times$		4454	$\times$		$\times$			
[119]	quark model $uudc\bar{c}$	FS-CM						FS-CM					FS-CM	
		3933–4267												
		4013–4363						4013–4389						
		4119–4377						4119–4445						
		4136–4471						4136–4476						
		4156–4541						4236–4526					4236–4616	



**Exp:**  $1/2^- \Lambda_b(5912)$  and  $3/2^- \Lambda_b(5920)$ .

LHCb, PRL 109, 172003 (2012)

**Extended WTmodel:** CGR, Nieves, Romanets, Salcedo, Tolos, PRD 87,034032 (2013)



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**Aim:** Flavor structure of odd lowest  $\Lambda$  resonances,  $J^P = 1/2^-, 3/2^-$ :  
strange:  $\Lambda$ , charm  $\Lambda_c$ , beauty  $\Lambda_b$  with our hadronic model  
also

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- Heavy Quark Spin Symmetry (HQSS)
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- $\Lambda$  ( $1/2^-$ ) Two  $\Lambda(1405)$ : ( $1^{st}$ ) narrow  $\propto \bar{K}N$ , ( $2^{nd}$ ) wide  $\propto \pi\Sigma$
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Our model with no free parameter provides this structure.

As many other models

Details for charm sector  $I = 0$ ,  $C = 1$ :  $\Lambda_c$ 's

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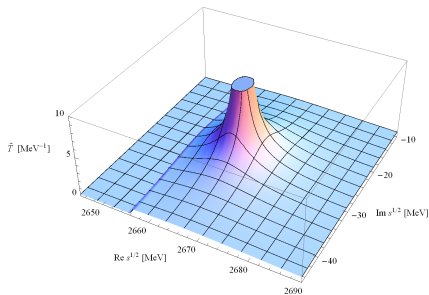
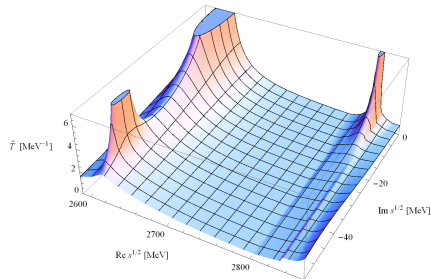
# Low laying $\Lambda_c$

## Results for charm:

$$\boxed{1/2^-} \Lambda_c(2595)$$

O. Romanets PRD 85 114032

$$\boxed{3/2^-} \Lambda_c(2625).$$



$$\tilde{T}^{IJC}(z) \equiv \max_j \sum_i |T_{ij}^{IJC}(z)|$$

# Results for charm

State	$J^P$	$\sqrt{\alpha}$	$M_R$	$\Gamma_R$
$\Lambda_c(2595)$ 1st	$1/2^-$	1	2619.0	1.2
$\Lambda_c(2595)$ 2nd	$1/2^-$	1	2617.0	90.0
$\Lambda_c(2625)$ 3rd	$3/2^-$	1	2667.0	55.0



# Couplings to $\pi\Sigma$ or $\pi\Sigma^*$

State	$J^P$	$\sqrt{\alpha}$	$M_R$	$\Gamma_R$	$ g_i $
$\Lambda_c(2595)$ 1st	$1/2^-$	1	2619.0	1.2	0.30 ( $\pi\Sigma_c$ )
$\Lambda_c(2595)$ 2nd	$1/2^-$	1	2617.0	90.0	2.4 ( $\pi\Sigma_c$ )
$\Lambda_c(2625)$ 3rd	$3/2^-$	1	2667.0	55.0	2.2 ( $\pi\Sigma_c^*$ )



# All flavors

State	$J^P$	$\sqrt{\alpha}$	$M_R$	$\Gamma_R$	$ g_{\pi\Sigma^{(*)}} $
$\Lambda(1405)$	$1/2^-$	1	1430.0	5.5	0.50 ( $\pi\Sigma^-$ )
$\Lambda(1405)$	$1/2^-$	1	1373.0	170.0	2.6 ( $\pi\Sigma^-$ )
$\Lambda(1520)$	$3/2^-$	1	1540.0	74.0	2.3 ( $\pi\Sigma^*$ )
$\Lambda_c(2595)$ 1st	$1/2^-$	1	2619.0	1.2	0.30 ( $\pi\Sigma_c$ )
$\Lambda_c(2595)$ 2nd	$1/2^-$	1	2617.0	90.0	2.4 ( $\pi\Sigma_c$ )
$\Lambda_c(2625)$ 3rd	$3/2^-$	1	2667.0	55.0	2.2 ( $\pi\Sigma_c^*$ )
$\Lambda_b(5912)$	$1/2^-$	1	5878.0	0.0	0.04 ( $\pi\Sigma_b$ )
$\Lambda_b(5912)$	$1/2^-$	1	5949.0	0.0	1.3 ( $\pi\Sigma_b$ )
$\Lambda_b(5920)$	$3/2^-$	1	5963.0	0.0	1.5 ( $\pi\Sigma_b^*$ )



# 1st $\Lambda_c$

State	$J^P$	$\sqrt{\alpha}$	$M_R$	$\Gamma_R$	$1 - Z$
$\Lambda_c(2595)$	$\frac{1}{2}^-$	1	2619.0	1.2	0.878
Channel	$ g_i $	$g_i$	$X_i$	$(X'_i)$	
$\pi\Sigma_c$	0.31	$0.22 + 0.22i$	-0.012	$(-0.023)$	
<b>DN</b>	3.49	$-3.49 - 0.14i$	<b>0.275</b>	<b>(0.292)</b>	
$\eta\Lambda_c$	0.40	$0.40 - 0.00i$	0.007	$(0.009)$	
<b>D*N</b>	5.64	$-5.64 + 0.14i$	<b>0.465</b>	<b>(0.451)</b>	
$K\Xi_c$	0.22	$0.22 - 0.00i$	0.002	$(0.001)$	
$\omega\Lambda_c$	0.18	$0.18 + 0.04i$	0.001	$(0.001)$	
$K\Xi'_c$	0.04	$0.02 + 0.04i$	-0.000	$(0.000)$	
$D_s\Lambda$	1.38	$-1.38 + 0.01i$	0.026	$(0.026)$	
<b>D<sub>s</sub>*<math>\Lambda</math></b>	2.87	$-2.87 + 0.03i$	<b>0.086</b>	<b>(0.057)</b>	
$\rho\Sigma_c$	0.41	$0.39 + 0.12i$	0.003	$(0.005)$	
$\eta'\Lambda_c$	0.92	$0.92 + 0.01i$	0.018	$(0.018)$	
$\rho\Sigma_c^*$	0.58	$0.58 - 0.07i$	0.007	$(0.006)$	
$\phi\Lambda_c$	0.01	$0.01 + 0.00i$	0.000	$(0.000)$	



# Compositeness of the $\Lambda$ states: Weights of Weinberg

- 60's Weinberg: the deuteron is best described as composed of a proton and a neutron, rather than a genuine dibaryon. **Sum-rule = 1**  
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- In the unitarized setting the sum rule follows from the identity:

$$-1 = \sum_{i,j} g_i g_j \left( \delta_{ij} \frac{\partial G_i(\sqrt{s})}{\partial \sqrt{s}} + G_i(\sqrt{s}) \frac{\partial V_{ij}(\sqrt{s})}{\partial \sqrt{s}} G_j(\sqrt{s}) \right) \Big|_{\sqrt{s}=\sqrt{s_R}}.$$

$G_j$  is the meson-baryon loop. It holds for bound states and resonances, as well as energy dependent or energy independent interactions.

- Use of the definitions

$$X_i = -\text{Re} \left( g_i^2 \frac{dG_i}{d\sqrt{s}} \Big|_{\sqrt{s_R}} \right), \quad Z = -\text{Re} \sum_{i,j} g_i g_j \left( G_i \frac{\partial V_{ij}}{\partial \sqrt{s}} G_j \right) \Big|_{\sqrt{s_R}} \quad (-2)$$

provides the sum rule

$$1 = Z + \sum_i X_i.$$



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provides the sum rule

$$1 = Z + \sum_i X_i.$$



- Compositeness introduced yesterday in *A. Ramos's talk*
- Follow *F. Aceti et al. EPJ A 50, 57 (2014)* for the interpretation of the Weinberg's sum rule and its generalization to resonances.
- In the unitarized setting the sum rule follows from the identity:

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# 1st $\Lambda_c$

State	$J^P$	$\sqrt{\alpha}$	$M_R$	$\Gamma_R$	$1 - Z$
$\Lambda_c(2595)$	$\frac{1}{2}^-$	1	2619.0	1.2	0.878 bf (0.844)
Channel	$ g_i $	$g_i$	$X_i$	$(X'_i)$	
$\pi\Sigma_c$	0.31	$0.22 + 0.22i$	-0.012	$(-0.023)$	
<b>DN</b>	3.49	$-3.49 - 0.14i$	<b>0.275</b>	<b>(0.292)</b>	
$\eta\Lambda_c$	0.40	$0.40 - 0.00i$	0.007	$(0.009)$	
<b>D*N</b>	5.64	$-5.64 + 0.14i$	<b>0.465</b>	<b>(0.451)</b>	
$K\Xi_c$	0.22	$0.22 - 0.00i$	0.002	$(0.001)$	
$\omega\Lambda_c$	0.18	$0.18 + 0.04i$	0.001	$(0.001)$	
$K\Xi'_c$	0.04	$0.02 + 0.04i$	-0.000	$(0.000)$	
$D_s\Lambda$	1.38	$-1.38 + 0.01i$	0.026	$(0.026)$	
<b>D<sub>s</sub>*<math>\Lambda</math></b>	2.87	$-2.87 + 0.03i$	<b>0.086</b>	<b>(0.057)</b>	
$\rho\Sigma_c$	0.41	$0.39 + 0.12i$	0.003	$(0.005)$	
$\eta'\Lambda_c$	0.92	$0.92 + 0.01i$	0.018	$(0.018)$	
$\rho\Sigma_c^*$	0.58	$0.58 - 0.07i$	0.007	$(0.006)$	
$\phi\Lambda_c$	0.01	$0.01 + 0.00i$	0.000	$(0.000)$	



# Compositeness

The novelty comes from the systematic study of the 2composition of these resonances, as a function of the heavy quark mass, addressing the question of to what extent the structure of the resonances is fully saturated by the

available s-wave meson-baryon channels.

	$s$	$c$	$b$
<b>1st <math>\Lambda</math></b>	<b>0.90</b>	<b>0.85</b>	<b>0.95</b>
<b>2nd <math>\Lambda</math></b>	0.35	0.40	<b>0.85</b>
<b>3rd <math>\Lambda</math></b>	0.25	0.35	<b>0.80</b>

- Regarding the overall compositeness of the nine  $\Lambda$  resonances studied, we find that for a given flavor sector, the closer to threshold (on the complex plane) the better the resonance is described as an s-wave meson-baryon molecule.
- Also, the heavier the flavor the higher the compositeness  $1 - Z$ . More explicitly, we find that  $1 - Z$  is large for the first  $\Lambda(1/2^-)$  of each flavor and the compositeness decreases as we move to the second  $\Lambda(1/2^-)$  states and then to the  $\Lambda(3/2^-)$  ones.
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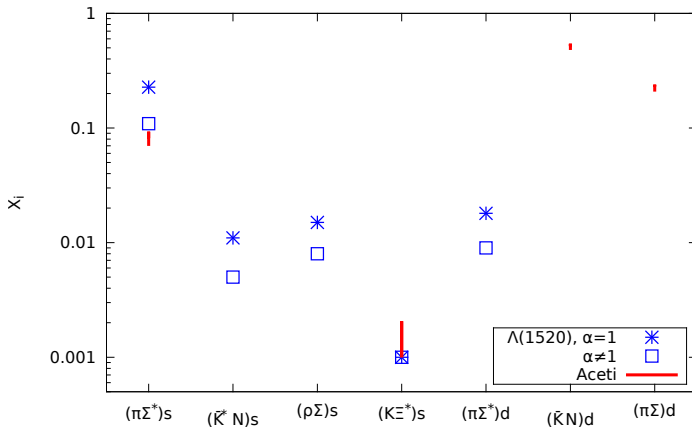
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Weights  $X_i$  of

the main channels contributing to the composition of the  $\Lambda(1520)$ . Our results (in blue) are represented by stars for  $\alpha = 1$ , and by squares when the subtraction point is modified to bring the mass of the resonance to its experimental value.

The vertical lines in red indicate the weights obtained in *Aceti, Oset and Roca, PRC 90 025208 (2014)* for the two  $s$ -wave and two  $d$ -wave channels considered

there using various sets of fitting parameters.



# Summary

- For hidden charm sector ( $N_c = N_{\bar{c}} = 1$ ), using hadronic degrees of freedom, the most general parity, SU(3) and **HQSS** symmetric meson-Baryon Lagrangian is constructed
  - 12** independent operators
- Minimal extension of SU(3) **WT** Lagrangian provides a  $H_{WT}'$  Hamiltonian that preserves **chiral**, **light spin-flavor** and **HQSS** symmetries
- This interaction is presented in different ways:
  - ▶ Field Lagrangian
  - ▶ Hadron creation-annihilation operators
  - ▶ SU(6) projectors
  - ▶ Multichannel Matrices
- Results of our **WT** extended model are presented for
  - ▶ Hidden Charm  $N$  and  $\Delta$
  - ▶ Beauty Baryons ( $\Lambda_b$ )

# Compositeness of the strange, charm and beauty odd $\Lambda$ states

- Appears today in arXiv
- Authors: C. Hidalgo-Duque, J. Nieves, L.L. Salcedo, L. Tolos
- The compositeness of the  $\Lambda$  states in the strange, charm and beauty sectors is studied on a unitarized meson-baryon model.
- In the strange sector we use an  $SU(6)$  extension of the Weinberg-Tomozawa meson-baryon interaction
- We further implement the heavy-quark spin symmetry (HQSS) to construct the meson-baryon interaction when charmed or beauty hadrons are involved.
- We obtain two  $J^P = 1/2^-$   $\Lambda$  states and one  $J^P = 3/2^-$   $\Lambda$  for the strange, charm and beauty sectors.
- We find that the  $\Lambda$  states which are bound states (the three  $\Lambda_b$ ) or narrow resonances (one  $\Lambda(1405)$  and one  $\Lambda_c(2965)$ ) are well described as molecular states composed of s-wave meson-baryon pairs.
- The  $\frac{1}{2}^-$  wide  $\Lambda(1405)$  and  $\Lambda_c(2965)$  as well as the  $\frac{3}{2}^-$   $\Lambda(1520)$  and