

1st Hadron Spanish Network Days and Spanish-Japanese JSPS Workshop
Valencia, SPAIN, June 15-17, 2015

$\eta'(958)$ -nucleon interaction and Possible bound state of $\eta'(958)$ - N system



Hideko NAGAHIRO (Nara Women's University)



H. Nagahiro, D.Jido, H. Fujioka, K.Itahashi, S. Hirenzaki, PRC87(13)045201 [(p,d) theo.]

Itahashi, Fujioka, Geissel, Hayano, Hirenzaki, Itoh, Jido, Metag, Nagahiro, Nanova, Nishi,
Okochi, Outa, Suzuki, Tanaka, Weick, PTP128(12)601, [(p,d) exp. @GSI]



H. Nagahiro, S. Hirenzaki, E. Oset, A. Ramos, PLB709(12)87, [chiral unitary, (π ,N)]

D. Jido, H. Nagahiro, S. Hirenzaki, PRC85(12)032201(R) [χ sym vs. $m_{\eta'}$, (π ,N)]

H.Nagahiro, M.Takizawa, S. Hirenzaki, PRC74(06)045203 [NJL, (γ ,p)]

H. Nagahiro, S. Hirenzaki, PRL94(05)232503 [$(\gamma$,p)]

heavy $\eta'(958)$ mass

■ $\eta'(958)$ meson ... close connection to the $U_A(1)$ anomaly

» many theoretical works

» in vacuum / at finite temperature / at finite density

- » R. D. Pisarski, R. Wilczek, PRD29(84)338
- » T. Kunihiro, T. Hatsuda, PLB206(88)385 / T. Kunihiro, T. Hatsuda, PLB206(88)385
- » V. Bernard, R.L.Jaffe and U.-G.Meissner, NPB308(1993)753
- » Y. Kohyama, K.Kubodera and M.Takizawa, PLB208(1988)435
- » K. Fukushima, K.Onishi, K.Ohta, PRC63(01)045203
- » P. Costa *et al.*, PLB560(03)171, PRC70(04)025204, e

» poor experimental information at finite density

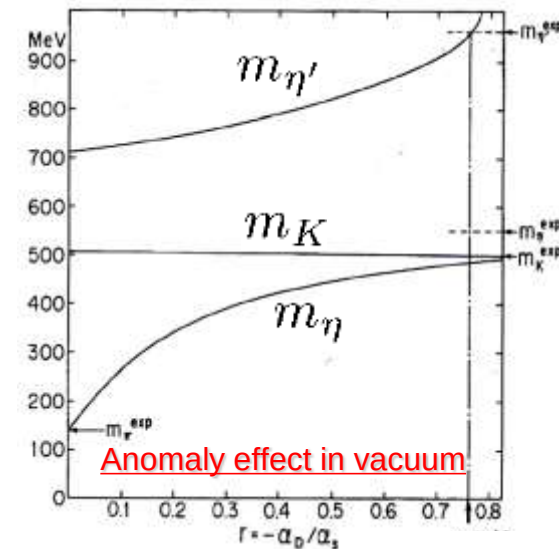
■ $U_A(1)$ anomaly in medium from the viewpoint of “mesons”

» the η' properties, especially **mass shift**, at finite density

■ **Nambu-Jona-Lasinio model** with the **KMT interaction**

$$\mathcal{L} = \bar{q}(i \not{\partial} - m)q + \frac{g_s}{2} \sum_a [(\bar{q}\lambda_a q)^2 + (i\bar{q}\lambda_a \gamma_5 q)^2] \\ + \underbrace{(g_D)}_{\text{explicit breaking the } U_A(1) \text{ sym.}} [\det \bar{q}_i (1 - \gamma_5) q_j + h.c.]$$

Kunihiro, Hatsuda, PLB206(88)385



✓ in-medium η' mass reduction with NJL model

Kobayashi-Maskawa, PTP44(70)1422

G. 't Hooft, PRD14(76)3432

Kunihiro, Hatsuda, PLB206(88)385

Costa et al., PLB560(03)171

⋮

$\langle \bar{q}q \rangle \rightarrow$ small

partial restoration of chiral sym.

$U_A(1)$ breaking [KMT interaction]
(giving heavier mass for η')



$U_A(1)$ anomaly **effect** $\rightarrow$ small in medium

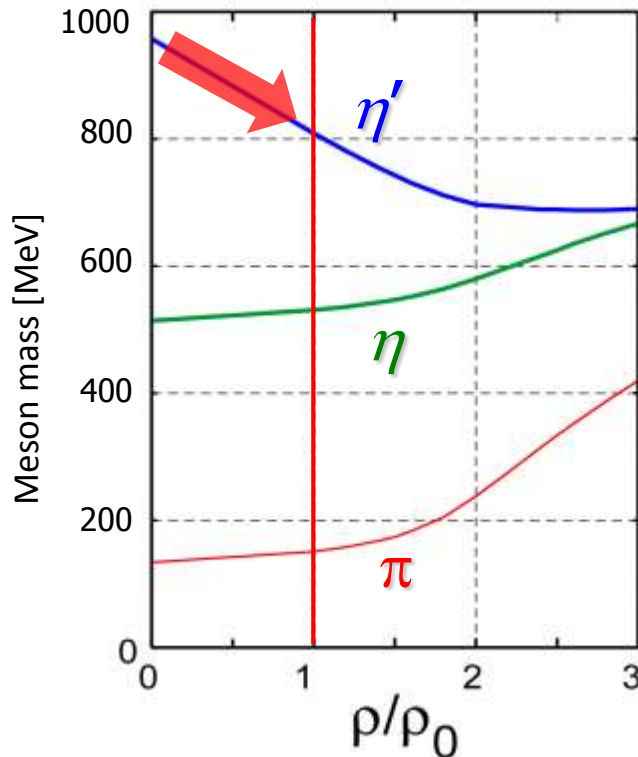
$$\Delta m_{\eta'} \sim -150 \text{ MeV} @ \rho_0$$

cf.) $\Delta m_{\eta'} \sim -40 - -80 \text{ MeV} @ \rho_0$

Quark-meson-coupling model,
S.Bass, A.Thomas, PLB634(06)368

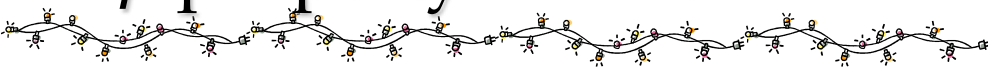
cf.) $\Delta m_{\eta'} \sim -80 \text{ MeV} @ \rho_0$

linear sigma model
S.Sakai, D.Jido, PRC88(13)064906



Costa et al., PLB560(03)171,
Nagahiro-Takizawa-Hirenzaki,
PRC74(06)045203

η' property in medium



→ Phenomenologically poorly understood

✓ small scattering length ?

$$\text{Re}(a_{\eta'p}) = 0 \pm 0.43 \text{ fm}, \text{Im}(a_{\eta'p}) = 0.37^{+0.40}_{-0.16} \text{ fm} \quad \text{in free space}$$

[E. Czerwinski *et al.*, (COSY-11) PRL113(14)062004]

[estimated from FSI on $pp \rightarrow pp\eta'$ observed at COSY]

✓ smaller absorption width in medium ?

$$\Gamma_{\eta'}(\rho_0; \langle |\vec{p}_{\eta'}| \rangle \sim 1 \text{ GeV}/c) \sim 15 - 25 \text{ MeV} @ \rho_0,$$

CBELSA/TAPS [M.Nanova *et al.*, PLB710(12)600]

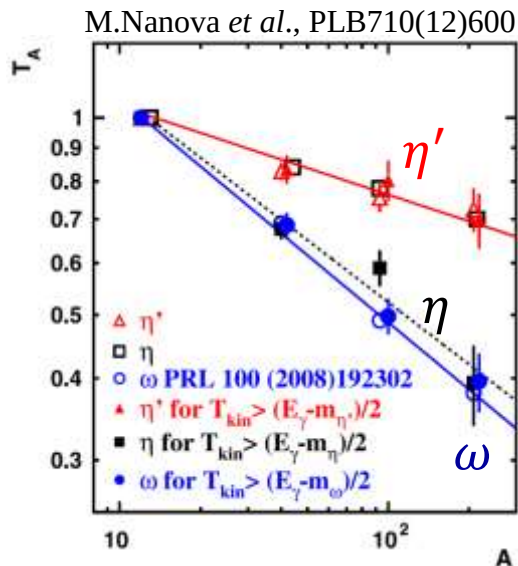
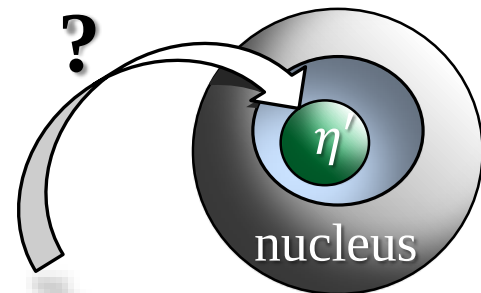
[estimated transparency ratio $\gamma A \rightarrow \eta' X$]

✓ real part of V_{opt} (not bound state observation)

$$\text{Re } V(\rho_0) \sim -(37 \pm 10(\text{stat}) \pm 10(\text{syst})) \text{ MeV}$$

CBELSA/TAPS [M. Nanova *et al.*, PLB727(2013)417-423]

[photroduction of η' off ^{12}C]



Our strategy for studying the η' properties



■ Possible η' bound states and their formation

- » with missing mass spectroscopy : (γ, p) , (π, N) , (p, d) , ...
 - › H.N., S.Hirenzaki, PRL94 (05) 232503
 - › H.N., M.Takizawa, S.Hirenzaki, PRC74 (06)045203
 - › ... and references in title page !

→ $\Gamma_{\eta'}$ in-medium strongly affects its observation possibilities

Experimental information [CBELSA/TAPS [M.Nanova *et al.*, PLB710(12)600]

$$\Gamma_{\eta'}(\rho_0; \langle |\vec{p}_{\eta'}| \rangle \sim 1 \text{ GeV}/c) \sim 15 - 25 \text{ MeV} @ \rho_0$$

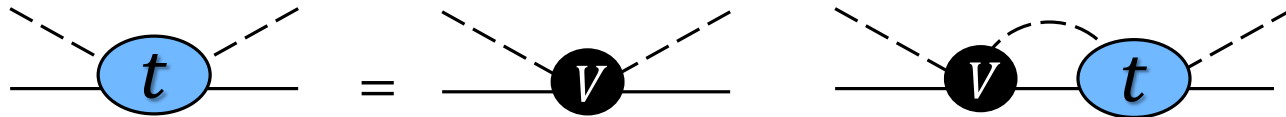
[estimated transparency ratio $\gamma A \rightarrow \eta' X$]

phenomenological approach [H.N., S. Hirenzaki, E. Oset, A. Ramos, PLB]

Based on : Coupled-channel calculation [Oset-Ramos, PLB704(11)334]

$$PB (\pi N, \eta N, K\Lambda, K\Sigma) + VB (K^* \Lambda, K^* \Sigma) + \eta_0 B$$

Unitarized scattering amplitude by coupled-channel BS eq.



Interaction kernel V

(1) Weinberg-Tomozawa interaction : pseudoscalar-baryon (PB) channel

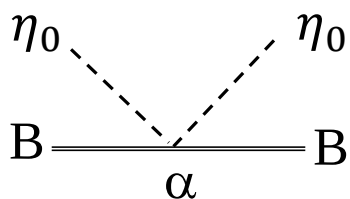
$\pi N, \eta N, K\Lambda, K\Sigma + \eta' N$ by the $\eta - \eta'$ mixing

their result : $|a_{\eta' N}| = 0.01 \text{ fm} \Leftrightarrow |a_{\eta' N}| \sim 0.1 - 0.8 \text{ fm}$ [PLB'00]

(2) Vector meson-baryon (VB) channel ($K^* \Lambda, K^* \Sigma$)

their result : $|a_{\eta' N}| = 0.03 \text{ fm}$

(3) **coupling of the singlet component of pseudoscalar to baryons**



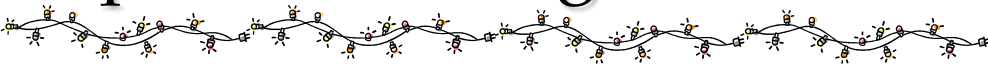
$$\mathcal{L}_{\eta_0 B} \propto \eta_0^2 \langle \partial_\mu \bar{B} \gamma^\mu B - \bar{B} \gamma^\mu \partial_\mu B \rangle$$

Borasoy, PRD61(00)014011
Kawarabayashi-Ohta, PTP66(81)1789

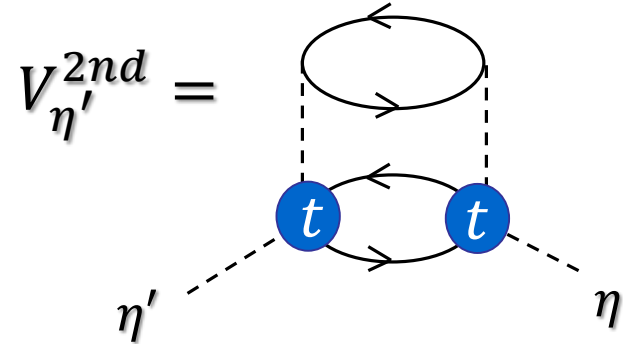
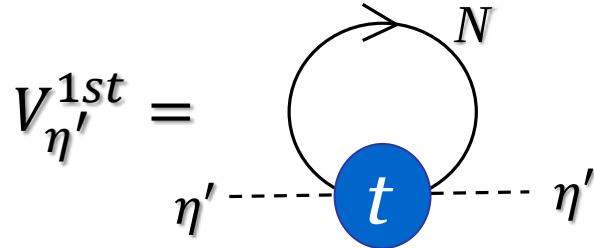
$\propto \dots$ free parameter $\rightarrow |a_{\eta' N}| = 0.1 \text{ fm}$

$\sim$ the det-int ($U_A(1)$ anomaly) in linear σ model [Sakai-Jido, PRC88(13)064906]

phenomenological estimation for $V_{\eta'}^{opt}$



Optical potential $V_{\eta'}$ [H.N., S. Hirenzaki, E. Oset, A. Ramos, PLB709(12)87]



We consider only the **attractive** case & **energy-independent** potential.

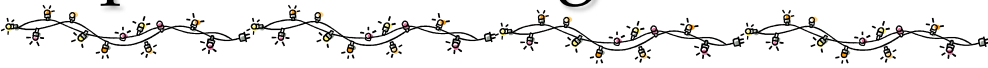
Re $V_{\eta'}$ and Im $V_{\eta'}$ with various α values

in unit of MeV

α	$ a_{\eta'N} $ fm	$V_{\eta'}^{1st}(\rho_0)$	$V_{\eta'}^{2nd}(\rho_0)$	$V_{\eta'}^{total}(\rho_0)$
-0.193	0.1	$-8.6 - 1.7i$	$-0.1 - 0.1i$	$-8.7 - 1.8i$
-0.834	0.3	$-26.3 - 2.1i$	$-0.6 - 0.9i$	$-26.8 - 3.0i$
-1.79	0.5	$-43.8 - 3.0i$	$-1.3 - 2.5i$	$-44.1 - 5.5i$
-9.67	1.0	$-87.7 - 6.9i$	$-4.1 - 10.4i$	$-91.8 - 17.2i$

Re $V \gg$ Im V

phenomenological estimation for $V_{\eta'}^{opt}$

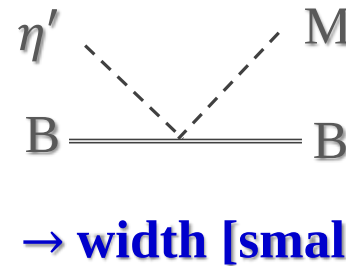
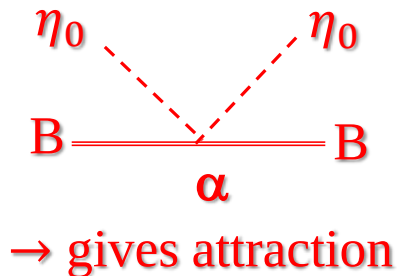


The reason why $\text{Re } V \gg \text{Im } V$ in coupled channel calculation

Kawarabayashi-Ohta, PTP66(81)1789, Borasoy, PRD61(00)014011

Sakai-Jido PRD88(13)064906, ...

WT interaction for η'



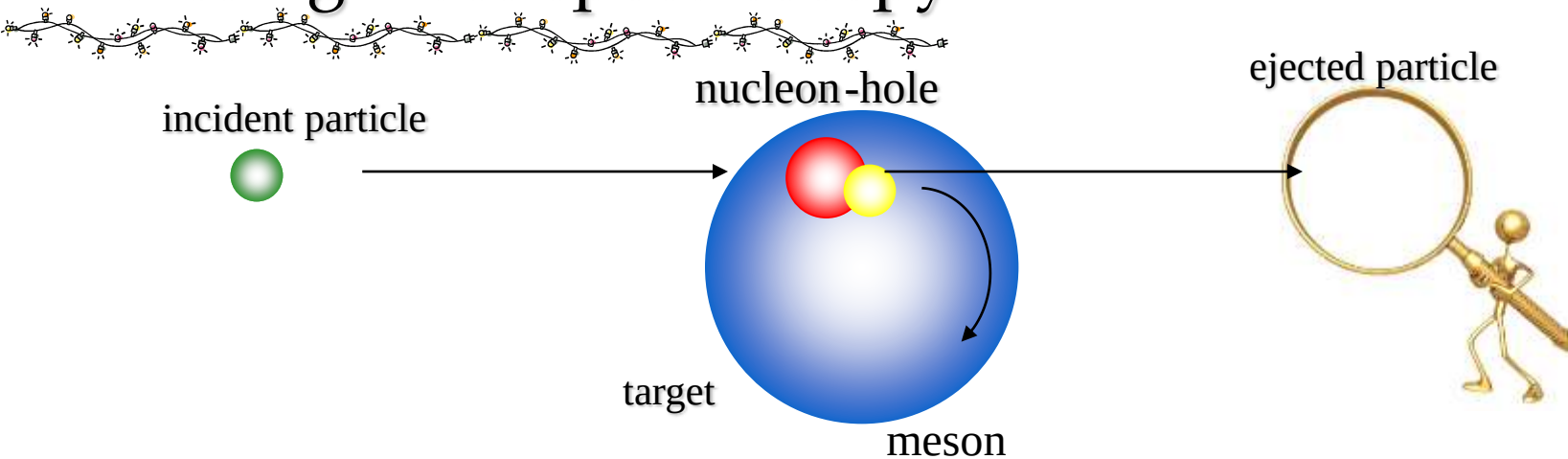
This interaction ...

- ✓ represents the anomaly effect [S.Sakai, D.Jido, PRD88(13)064906]
- ✓ **dominate** the $\eta' N$ interaction
- ✓ contributes mostly to the **η' elastic channel** & barely to the **inelastic channel**

ongoing work [$\rightarrow$ Later]

- ✓ **energy-dependence of $V_{\eta'}$** :
we discuss over a wide energy range (deep bound state $\leftrightarrow a_{\eta' N}$ at threshold)
- ✓ possible **α** value evaluated from, ex.) $\pi N \rightarrow \eta' N$ cross section

Missing mass spectroscopy



one-nucleon picking-up

» **(p,d) reaction @ GSI, August 2014**

Itahashi, Fujioka, Geissel, Hayano, Hirenzaki, Itoh, Jido, Metag, Nagahiro, Nanova, Nishi, Okochi, Outa, Suzuki, Tanaka, Weick, PTP128(12)601.

Nagahiro, Jido, Fujioka, Itahashi, Hirenzaki, PRC87(13)045201.

» **(γ ,p) reaction @ SPring-8, TAPS, ...**

Nagahiro-Hirenzaki, PRL94(05)232503, ...

» **(π ,N) reaction @ J-PARC**

Nagahiro, Hirenzaki, Oset, Ramos, PLB

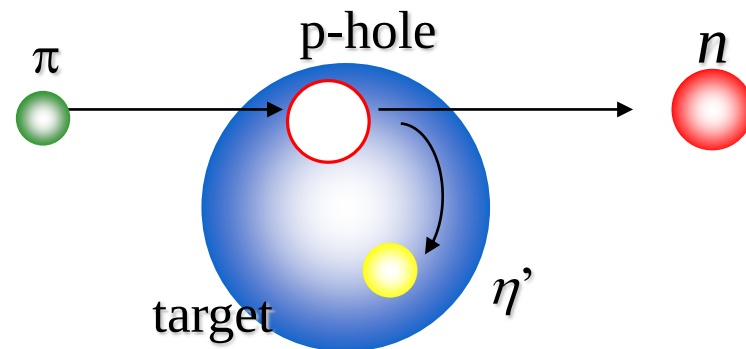
$\eta'(958)$ mesic nuclei by (π^-, n) reaction

missing mass spectroscopy

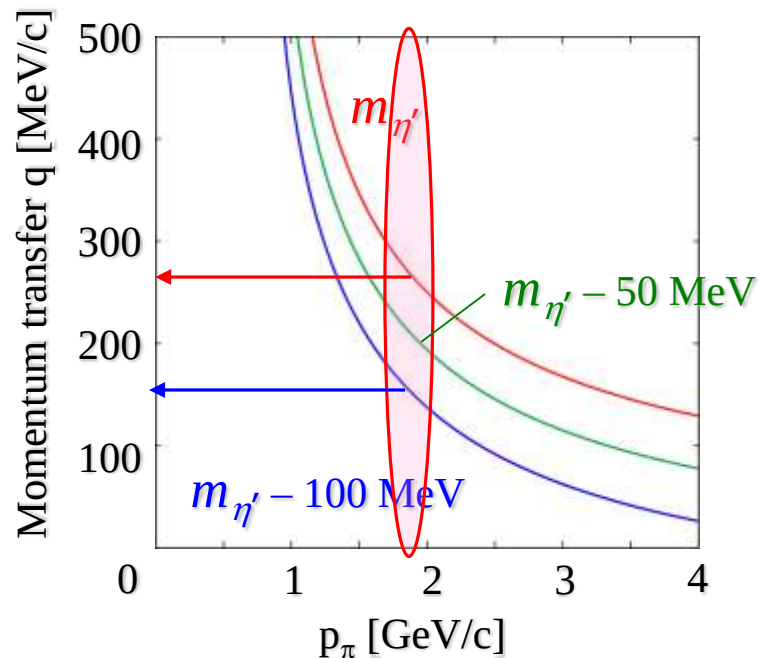
π beam momentum $p_\pi = 1.8 \text{ GeV}/c$

target : ^{12}C , ^{40}Ca

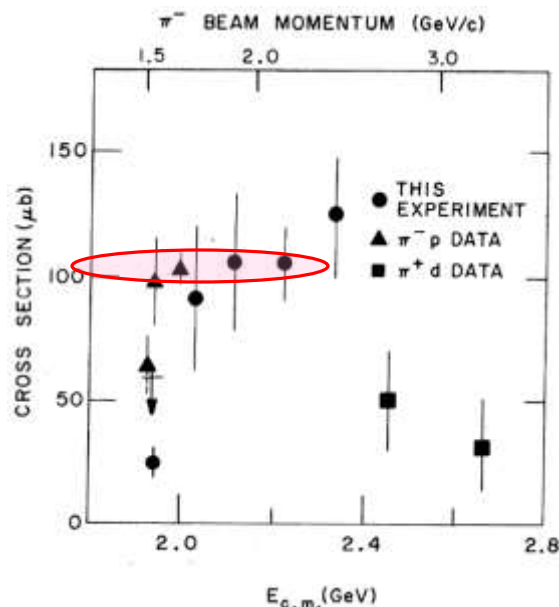
forward reaction : $\theta_n = 0 \text{ deg.}$



momentum transfer



elementary cross section $\pi^- p \rightarrow \eta' n$



$\sigma(\pi^+ n \rightarrow \eta' p) \sim 100 \mu\text{b}$

$\left(\frac{d\sigma}{d\Omega}\right)^{\text{Lab.}} \sim 100 \mu\text{b/sr}$

R.K.Rader *et al.*, PRD6(72)3059

Numerical results $^{12}\text{C}(\pi^-, n)^{11}\text{C}_\eta$,

(BE, Γ)

$$|a_{\eta'N}| = 1.0 \text{ fm}$$

$$V@ \rho_0 = (-91.8 - 17.2i) \text{ MeV}$$

0s

(-46.10, 23.34)

1s

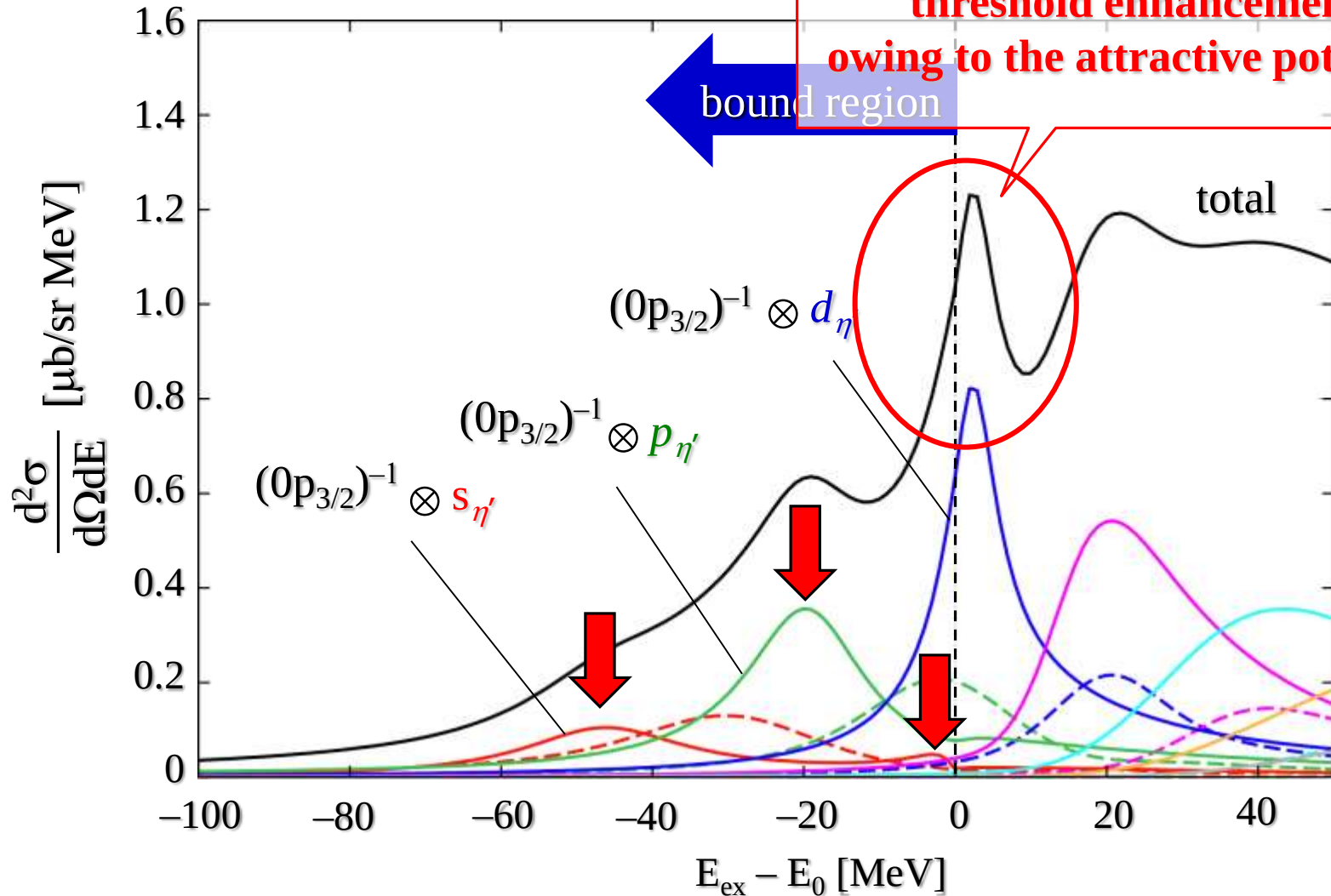
(-0.29, 4.99)

0p

(-18.73, 15.78)

threshold enhancement

owing to the attractive potential



Numerical results $^{12}\text{C}(\pi^-, n)^{11}\text{C}_\eta$,

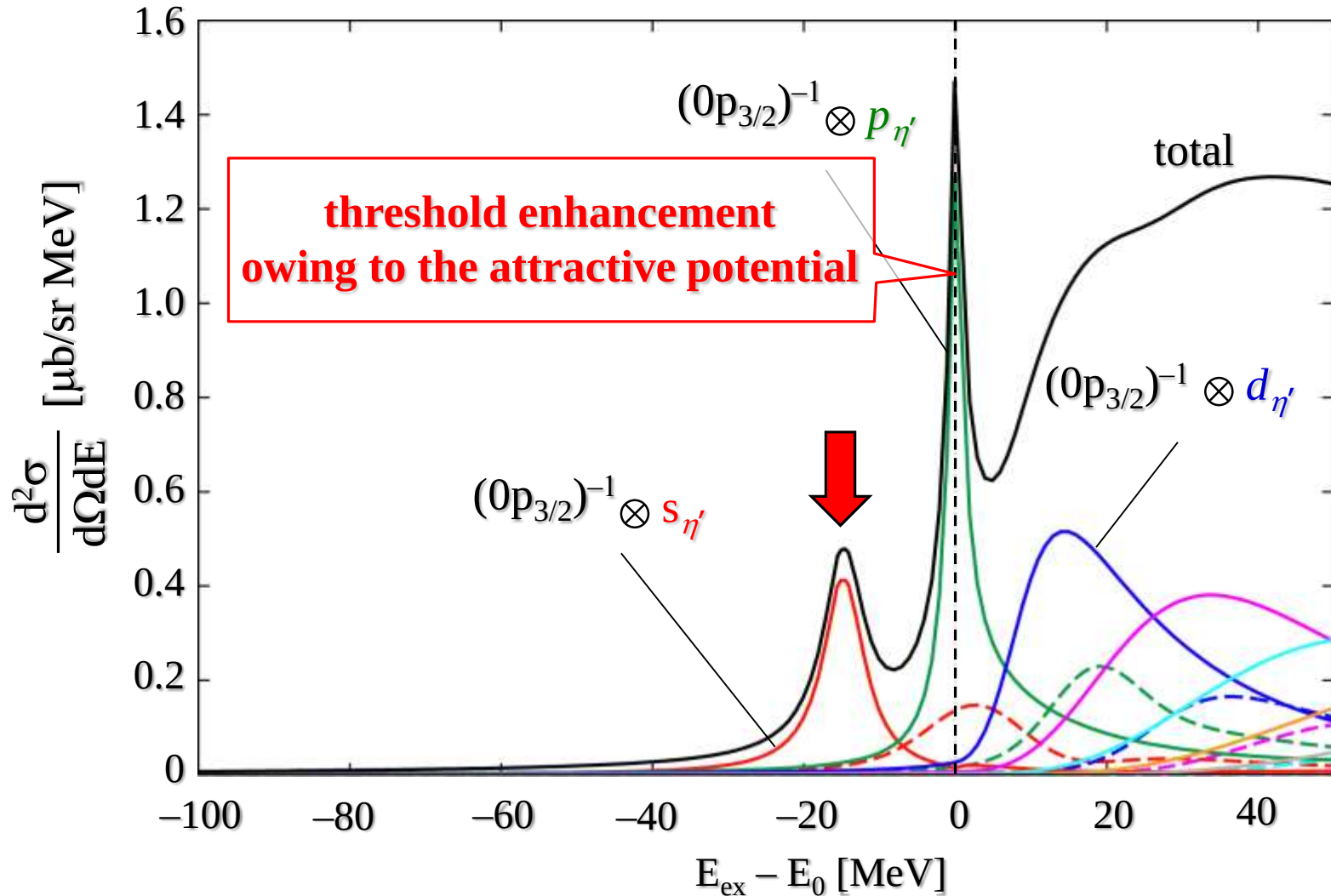
(BE, Γ)

$$|a_{\eta'N}| = 0.5 \text{ fm}$$

$$V@_{\rho_0} = (-44.1 - 5.5i) \text{ MeV}$$

0s

(-14.50, 5.95)



Numerical results $^{12}\text{C}(\pi^-, n)^{11}\text{C}_\eta$,

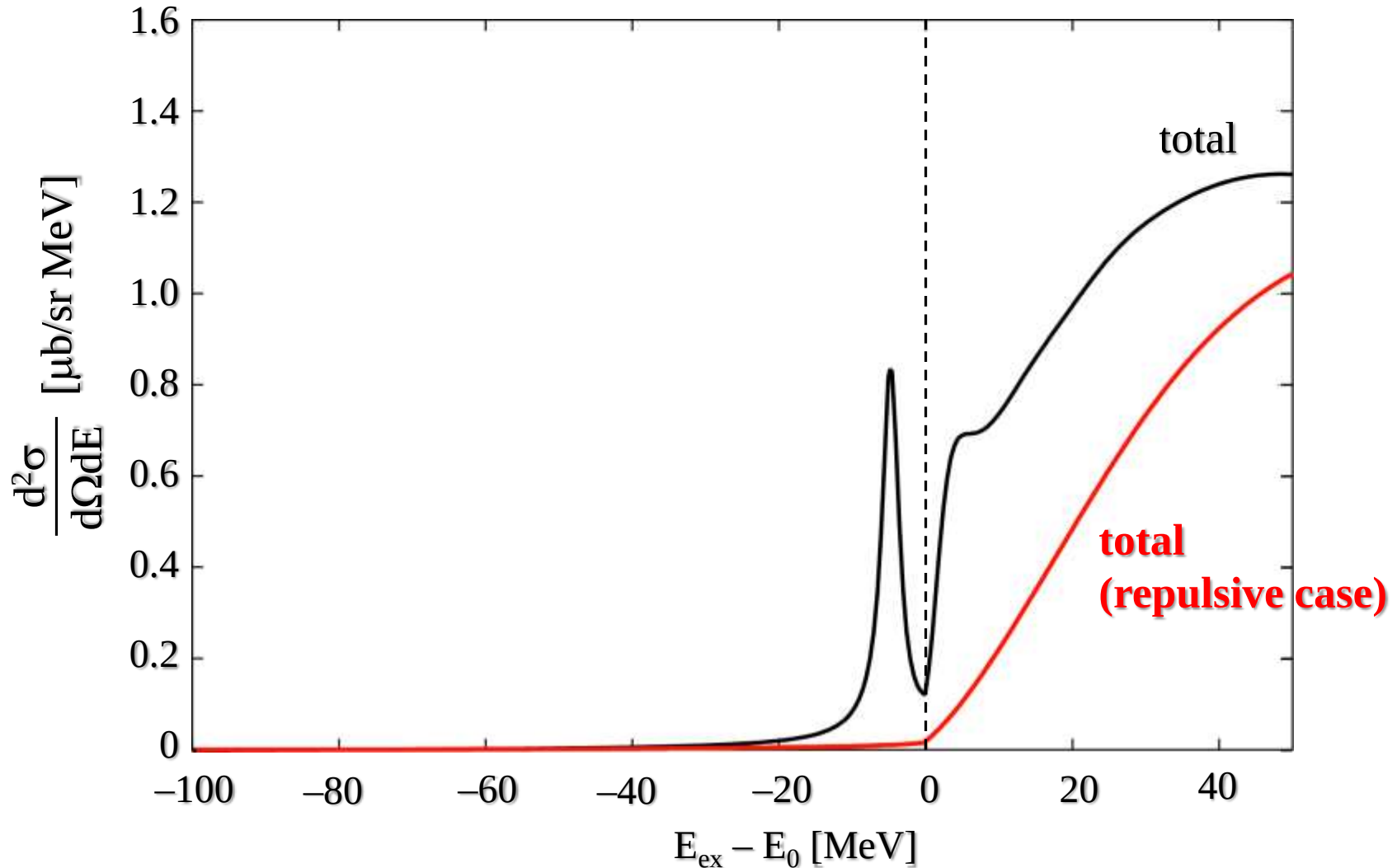
(BE. Γ)

$$|a_{\eta N}| = 0.3 \text{ fm}$$

$$V@ \rho_0 = (-26.8 - 3.0i) \text{ MeV}$$

$0s$

$(-4.65, 2.55)$



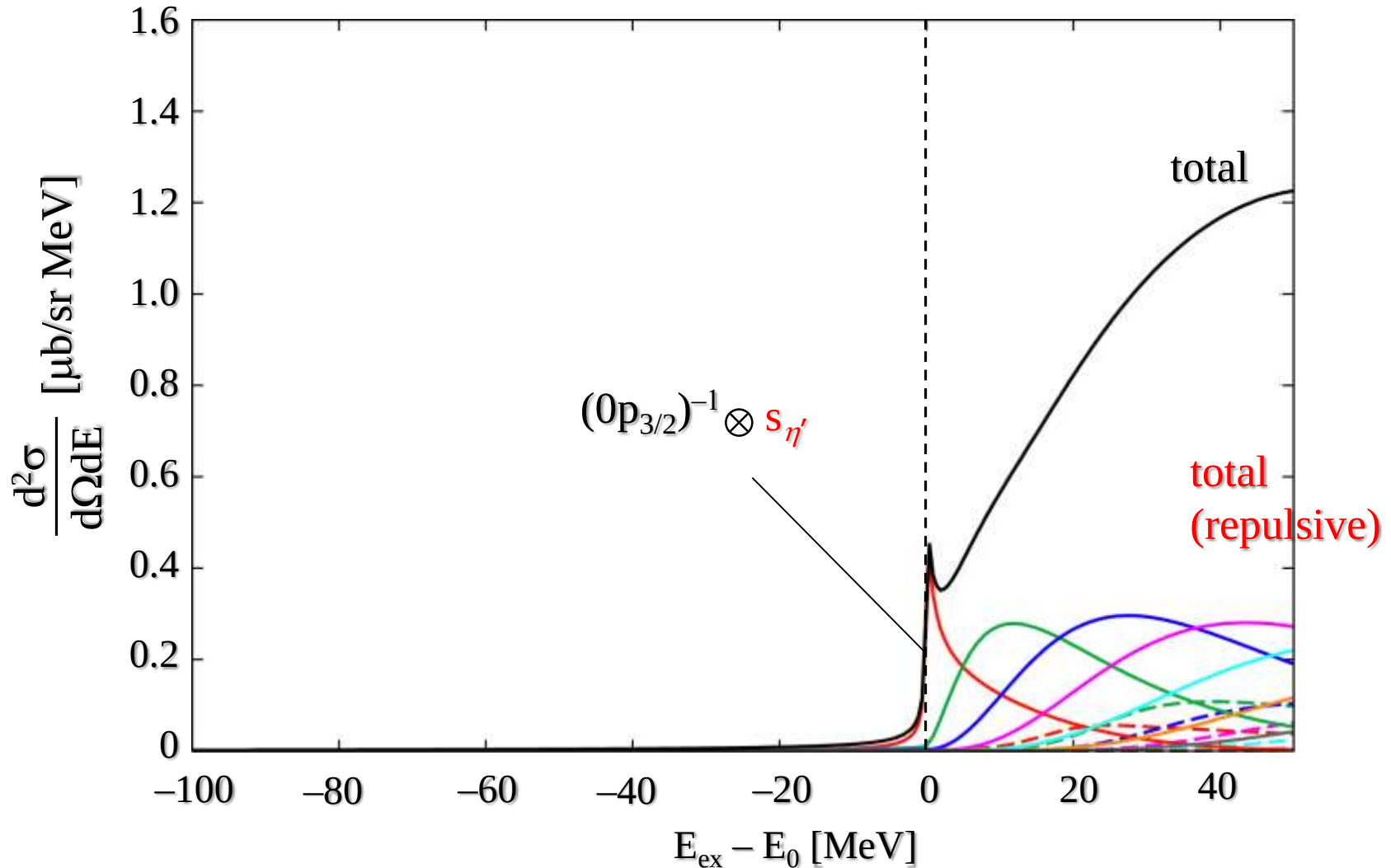
Numerical results $^{12}\text{C}(\pi^-, n)^{11}\text{C}_\eta$,

(BE, Γ)

$$|a_{\eta'N}| = 0.1 \text{ fm}$$

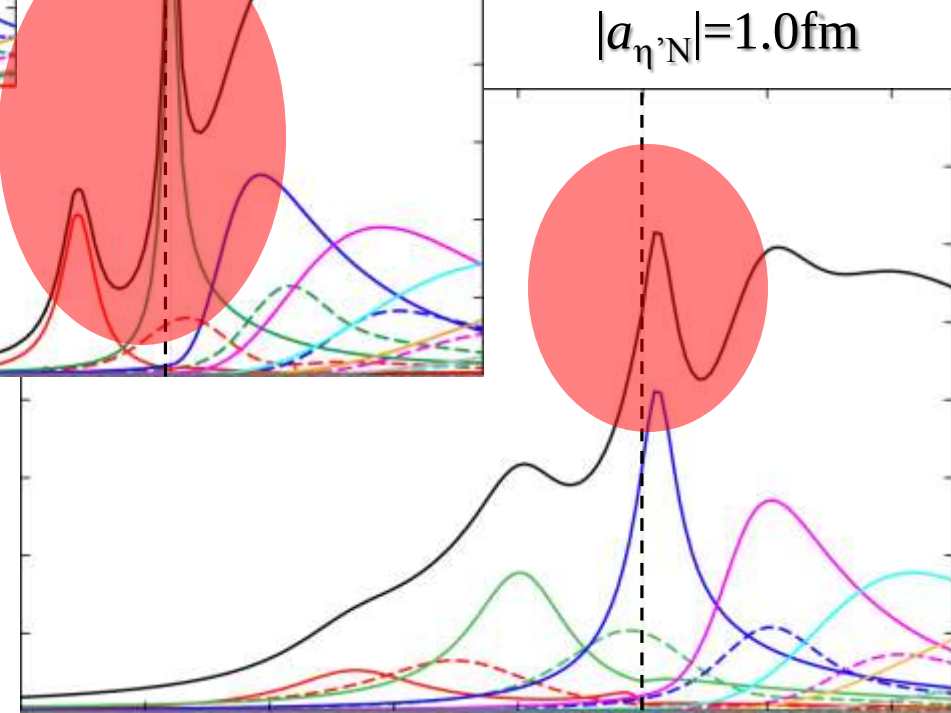
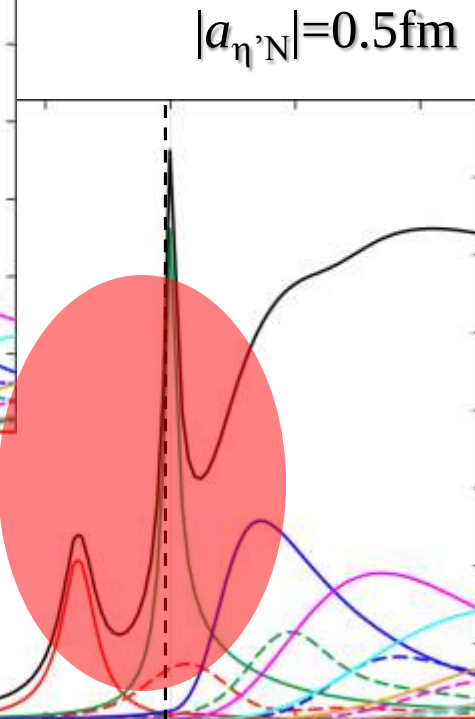
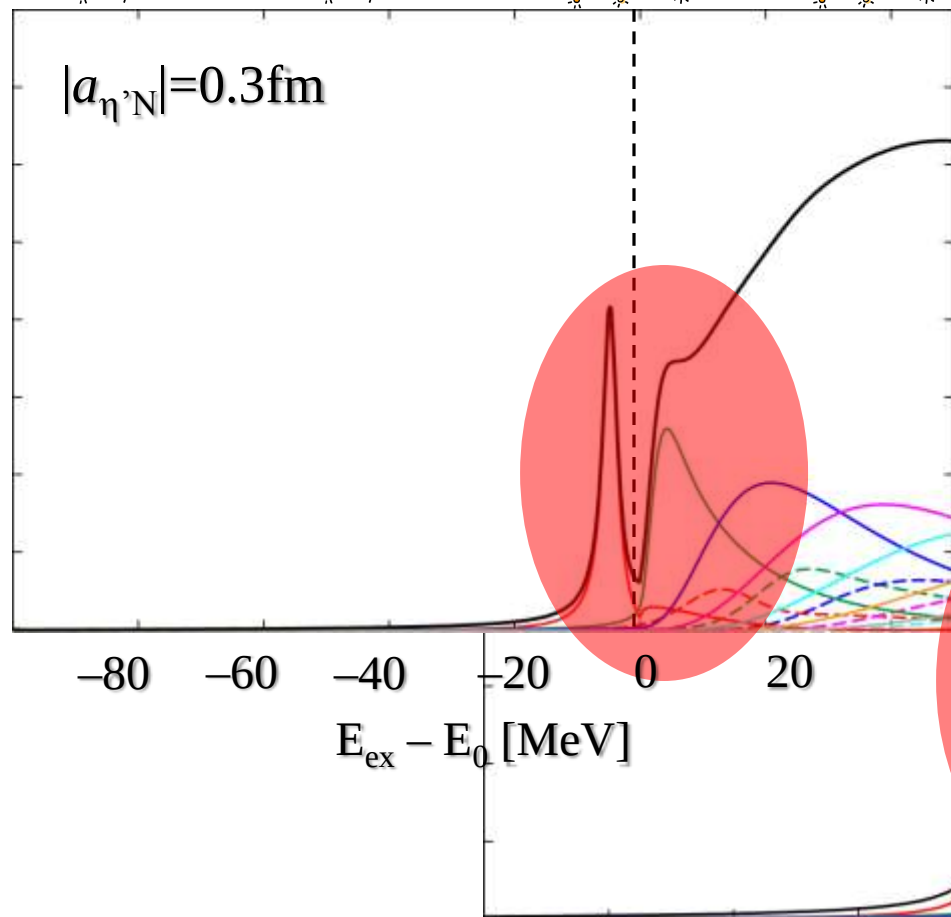
$$V@_{\rho_0} = (-6.4 - 1.8i) \text{ MeV}$$

no bound state



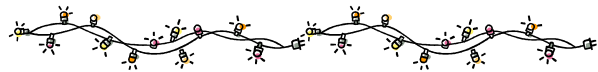
Structure around the η' threshold

**similar spectra are
expected in (p,d) @ GSI
... will be coming soon (?)**

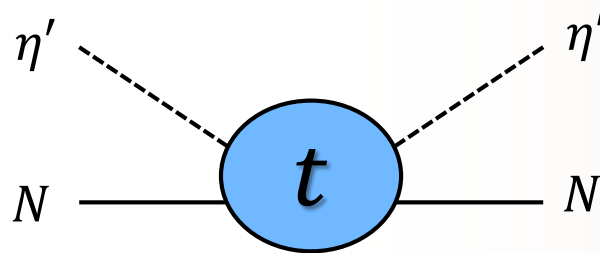


Momentum transfer $\sim 200\text{-}300 \text{ MeV}/c$
is not so small for heavy η'
 $\rightarrow$ See the Next Miyatani's talk

Revisiting $\eta' N$ scattering amplitude considering a **possible $\eta' N$ bound state**



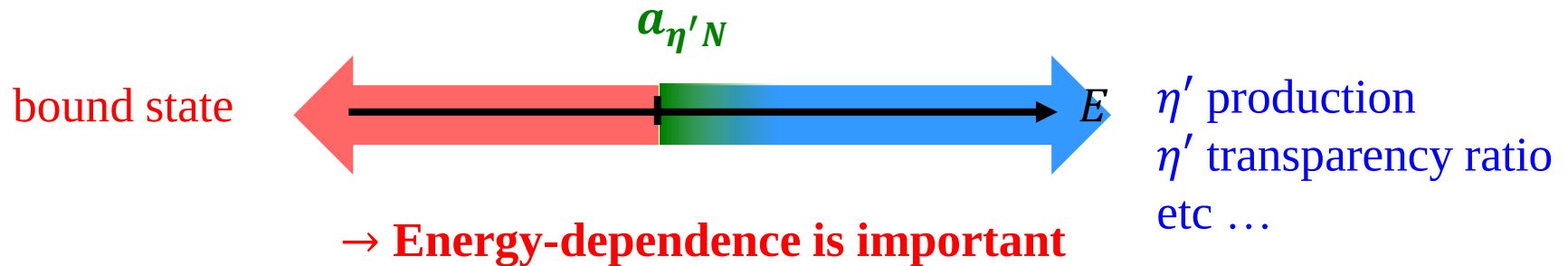
A. Hinata, A. Kiyomura, M. Sakamoto, H.N., S. Hirenzaki, in progress
(Nara Women's Univ.)



on-going theoretical works

We are now revisiting the $\eta' N$ scattering and η' -nucleus optical potential $V_{\eta'}$

- ✓ We have estimated $\text{Re}(V_{\eta'})$ and $\text{Im}(V_{\eta'})$ by using $T_{\eta' N \rightarrow \eta' N}$ [Oset-Ramos(2011)]
at $\eta' N$ threshold value



- ✓ different model for **vector-meson-baryon** channel

[K. P. Khemchandani, A. Martinez Torres H. N. and A. Hosaka, PRD88(13)114016]

- ✓ considering “possibility to have **$\eta' N$ bound state**”

→ subtraction const. positive → negative value ($\Lambda \sim 1\text{GeV}$)

(Oset-Ramos, PLB)

(Hinata *et al.*)

- ✓ trying to extract **possible α value**

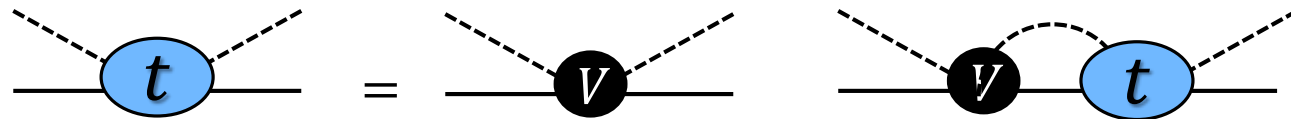
→ $\eta' N$ scattering length, $\pi N \rightarrow \eta' N$ production, η' transparency ratio, ...
& also η' -mesic nuclei formation, ...

- ✓ different model for **vector-meson-baryon** channel

✓ **different model for vector-meson-baryon channel**

K. P. Khemchandani, A. Martinez Torres, H. N. and A. Hosaka, PRD88(13)114016

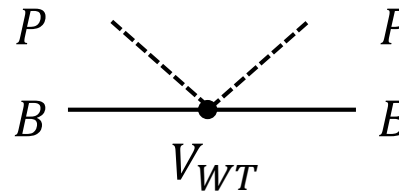
Unitarized scattering amplitude by coupled-channel BS eq.



Interaction kernel V

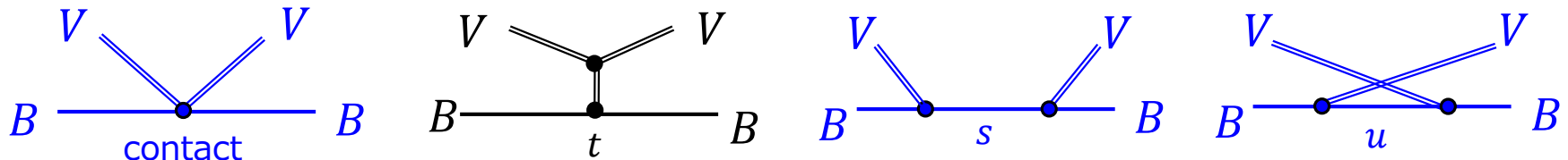
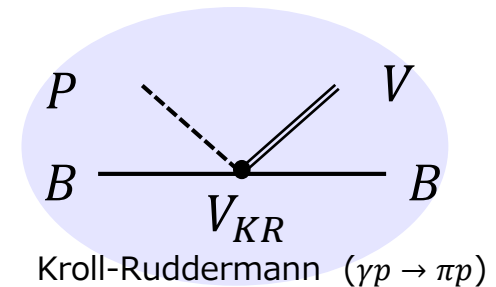
(1) Weinberg-Tomozawa interaction : pseudoscalar-baryon (PB) channel

$\pi N, \eta N, K\Lambda, K\Sigma$



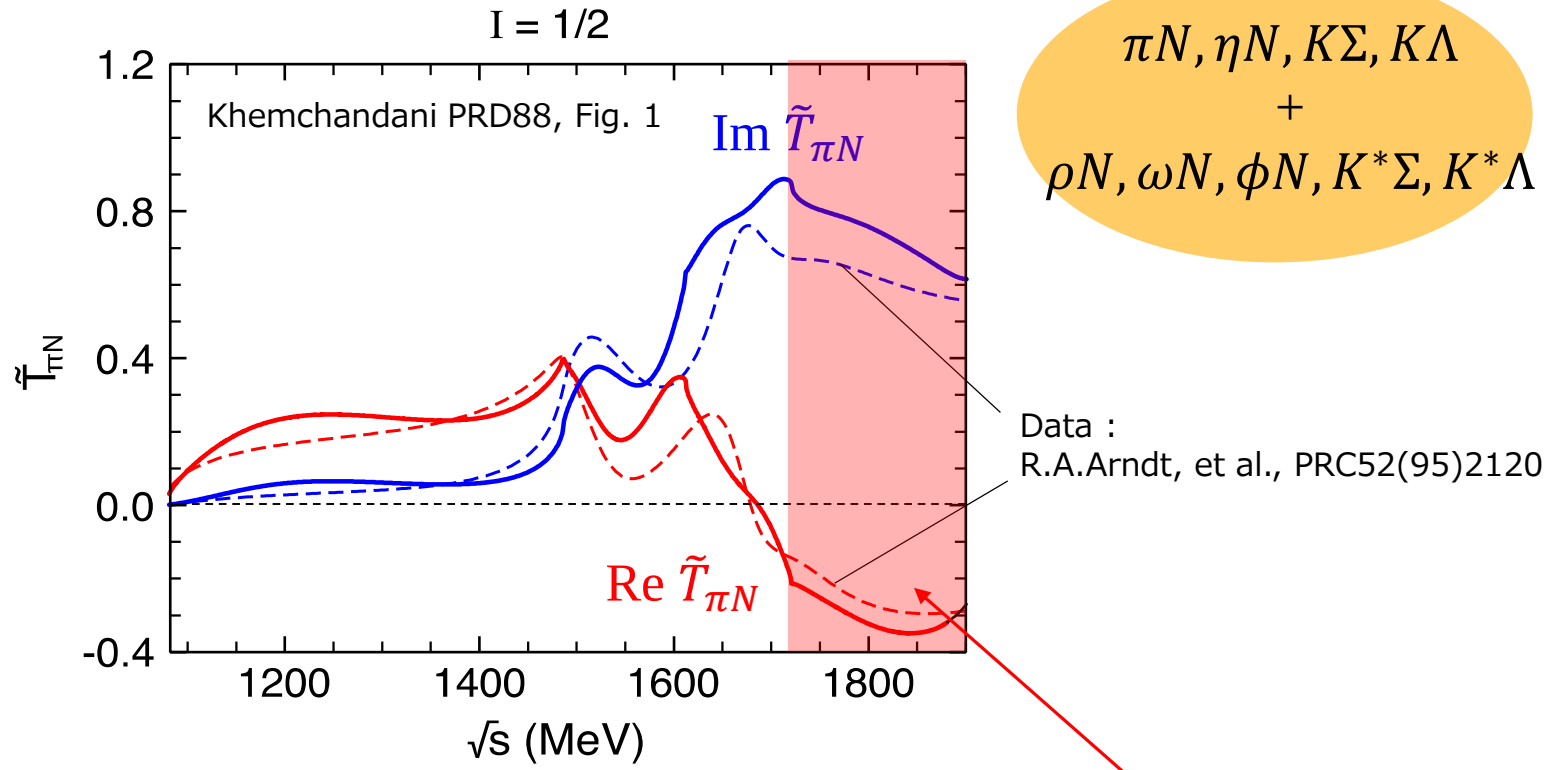
(2) Vector meson-baryon (VB) channel

$\rho N, \omega N, \phi N, K^*\Sigma, K^*\Lambda$



✓ **different model for vector-meson-baryon channel**

K. P. Khemchandani, A. Martinez Torres, H. N. and A. Hosaka, PRD88(13)114016

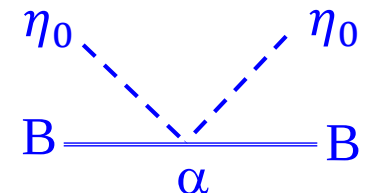


$\pi N, \eta N, K\Sigma, K\Lambda$
 $+$
 $\rho N, \omega N, \phi N, K^*\Sigma, K^*\Lambda$

$\pi N \rightarrow \pi N$ scattering amplitude ... good agreement at $\sqrt{s} \sim 1.9$ GeV

Hinata, Kiyomura, Sakamoto (Nara WU.)

→ we add $\eta' N$ channel in V_{WT} through η - η' mixing and $V_{\eta_0 B}$ (singlet- η Baryon interaction) as well



✓ considering “possibility to have $\eta' N$ bound state”

→ subtraction const. positive → negative value ($\Lambda \sim 1 \text{ GeV}$)

subtraction constants for the loop function

[Oset-Ramos-PLB, and our previous work]

$a_{\pi N}, a_{\eta N}, a_{K\Sigma}, a_{K\Lambda}$

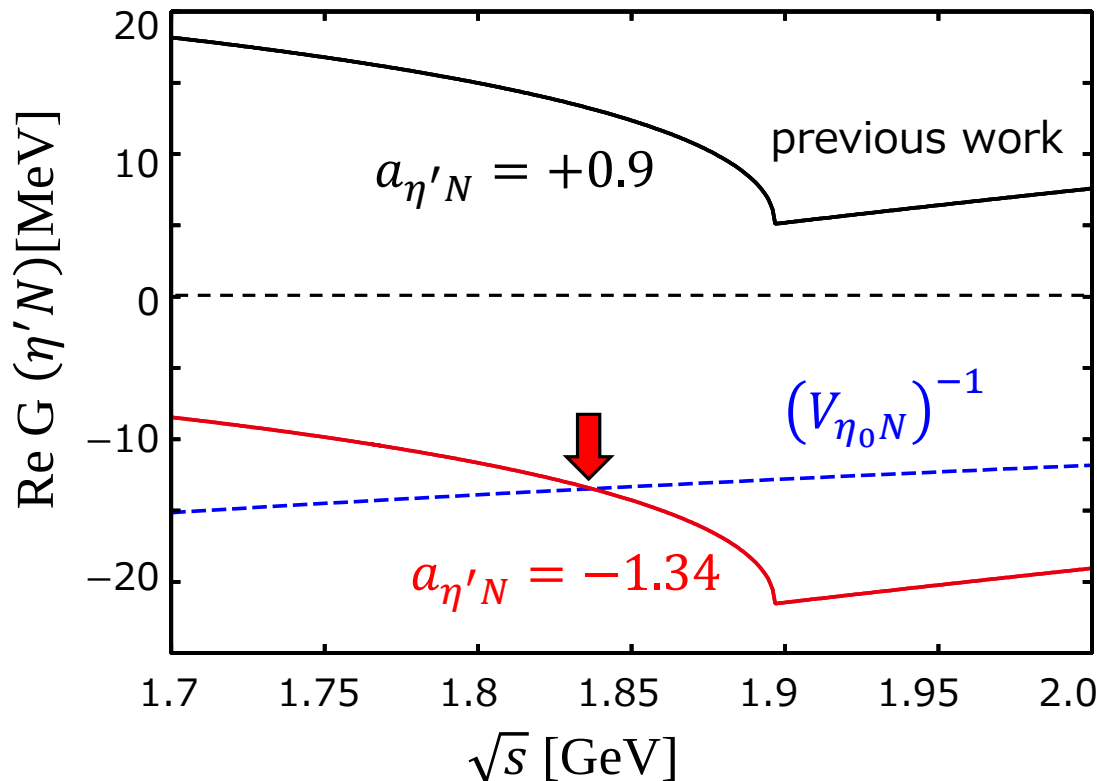
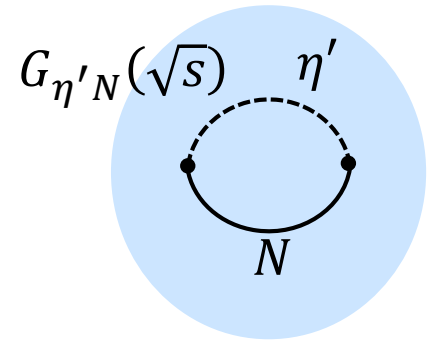
$a_{\eta' N} = a_{\eta N} = 0.9$



$a_{\eta' N} = -1.34$

→ to reproduce $N^*(1535)$ (Inoue et al., PRC65)

$\Lambda \sim 1 \text{ GeV/c}$



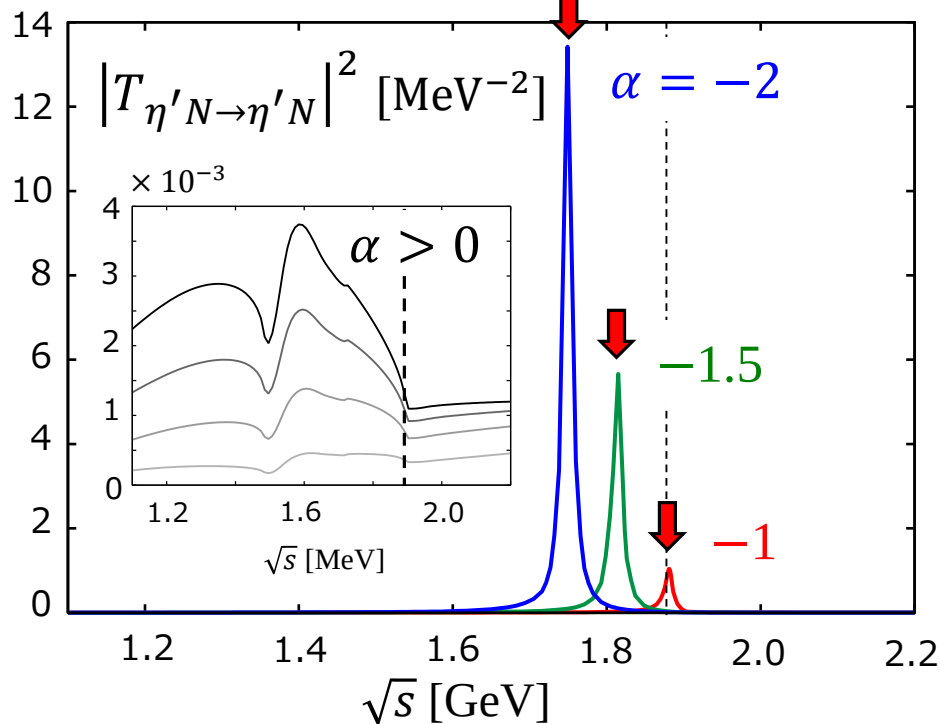
$$(V_{\eta_0 N})^{-1} - G(\sqrt{s}) = 0$$

→ $\eta' N$ bound state
due to $\eta_0 B$ coupling ?

$\eta' N$ bound state and $\sigma_{\pi N \rightarrow \eta' N}$

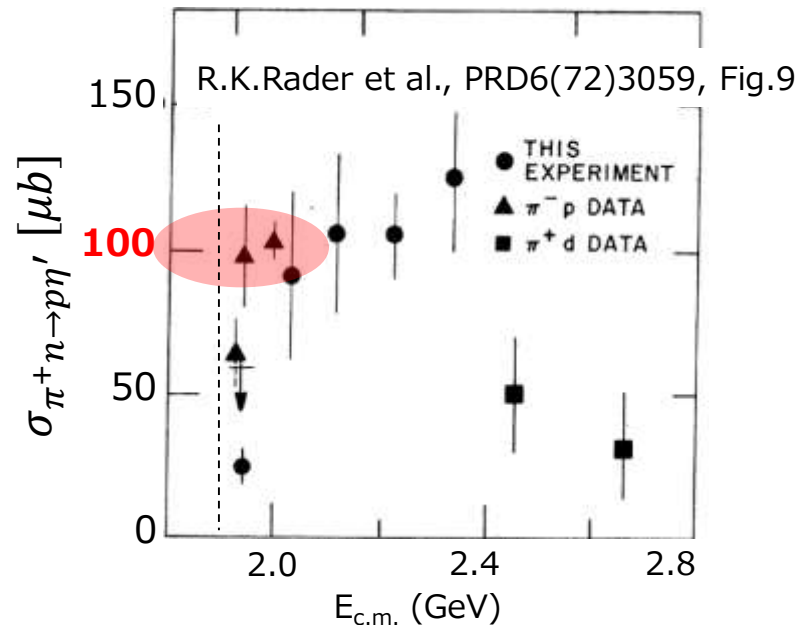
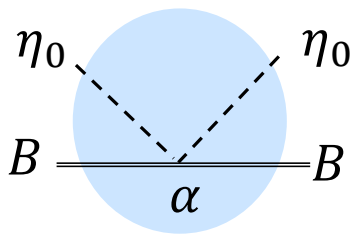
by Hinata, Kiyomura, Sakamoto [Nara WU.]

$\eta' N \rightarrow \eta' N$ scattering amplitude

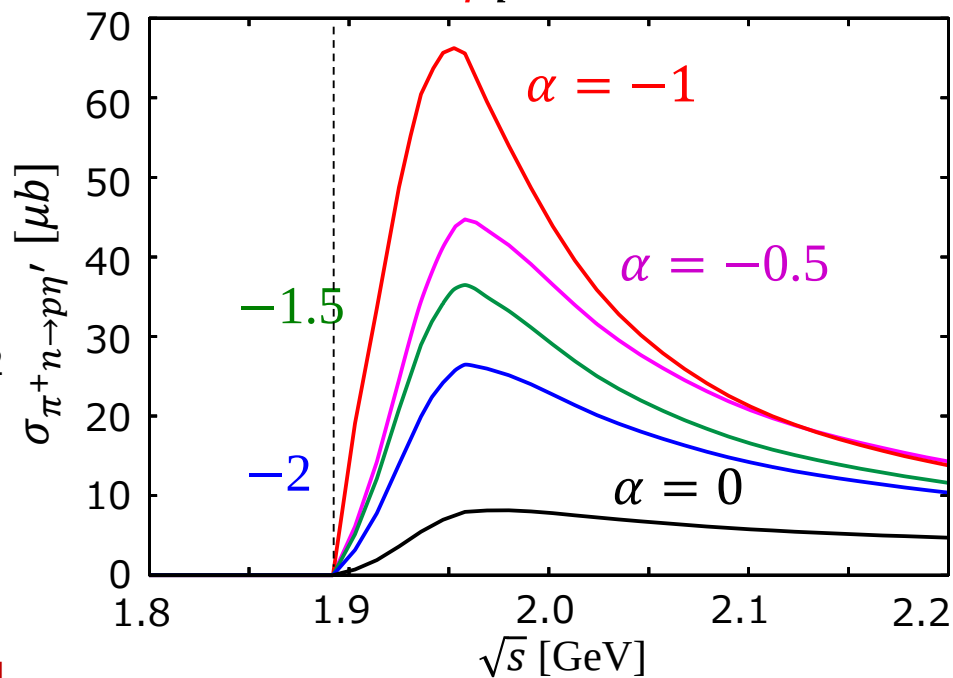


$\eta' N$ bound state

cf.) S. Sakai and D. Jido,
 PRC88(13)064906,
 based on linear σ model



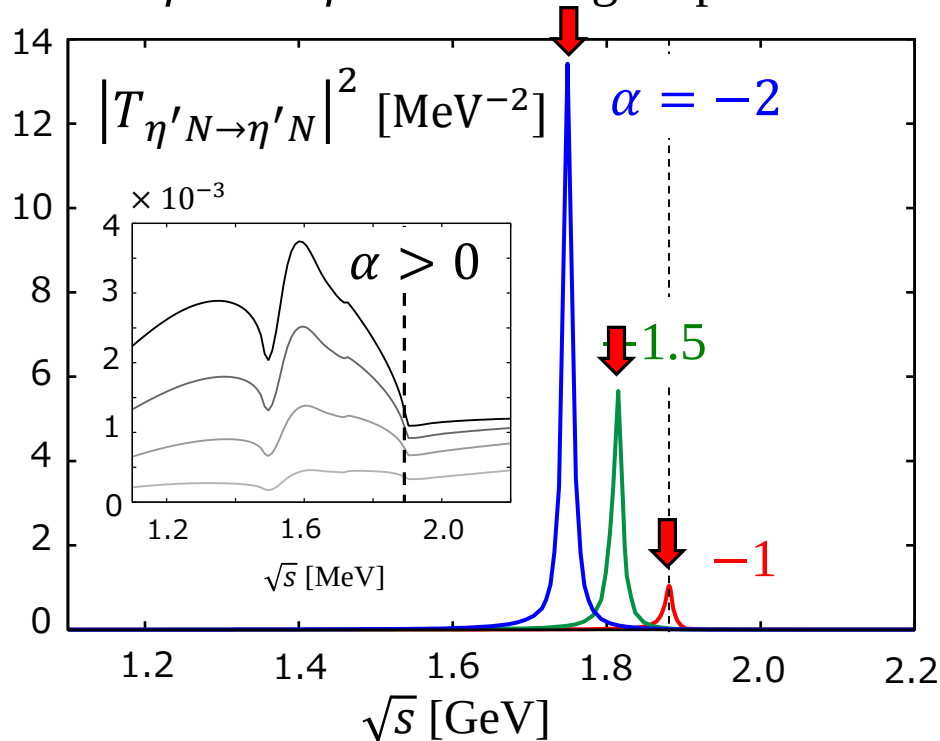
$\pi^+ n \rightarrow \eta' p$ cross section



$\eta' N$ scattering length

✓ **small scattering length**

$\eta' N \rightarrow \eta' N$ scattering amplitude

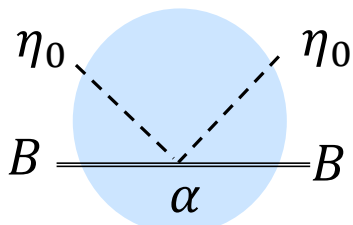
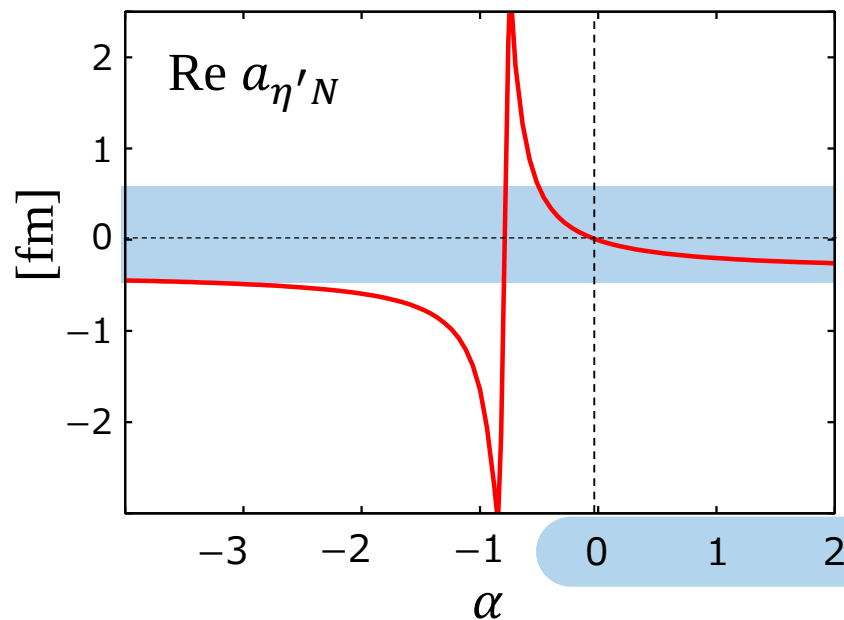


$$\text{Re}(a_{\eta' p}) = 0 \pm 0.43 \text{ fm}$$

$$\text{Im}(a_{\eta' p}) = 0.37^{+0.40}_{-0.16} \text{ fm}$$

[E. Czerwinski *et al.*, (COSY-11),
PRL113(14)062004]

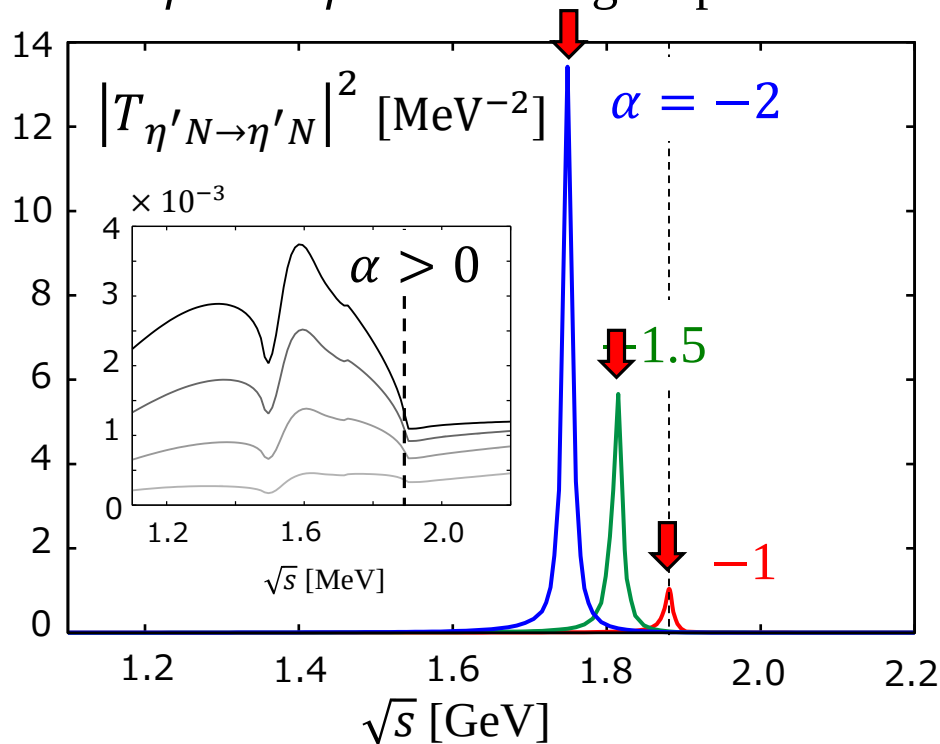
$\eta' N$ scattering length [fm]



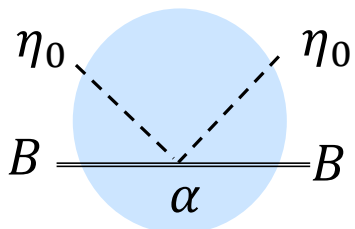
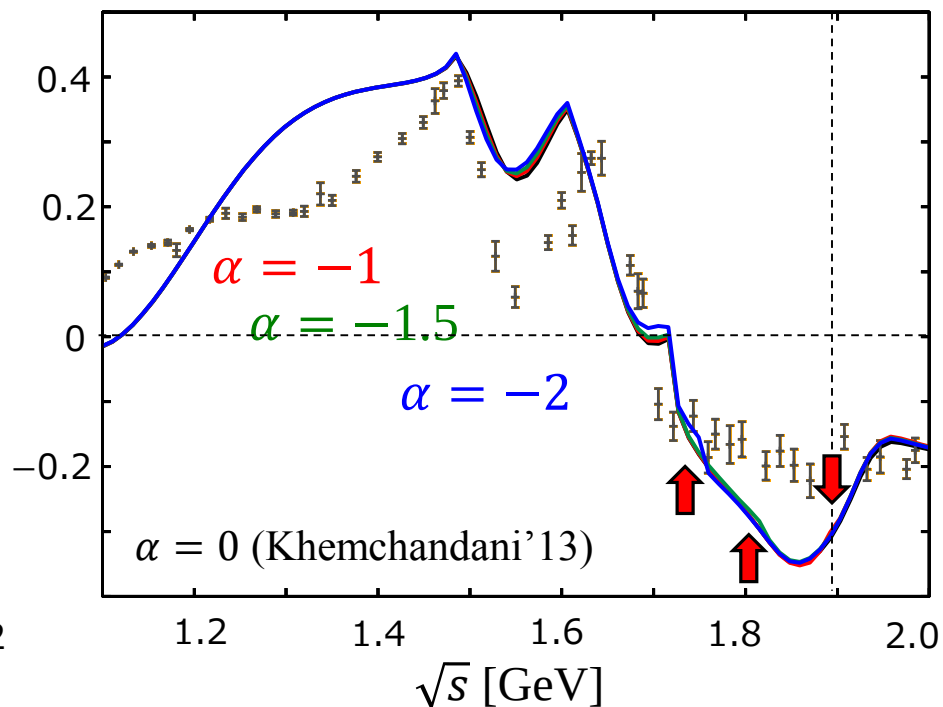
πN scattering amplitudes

by Hinata, Kiyomura, Sakamoto [Nara WU.]

$\eta' N \rightarrow \eta' N$ scattering amplitude



πN amplitude (real part)



such a “narrow N^* ” exists ??

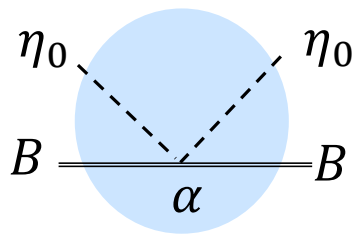
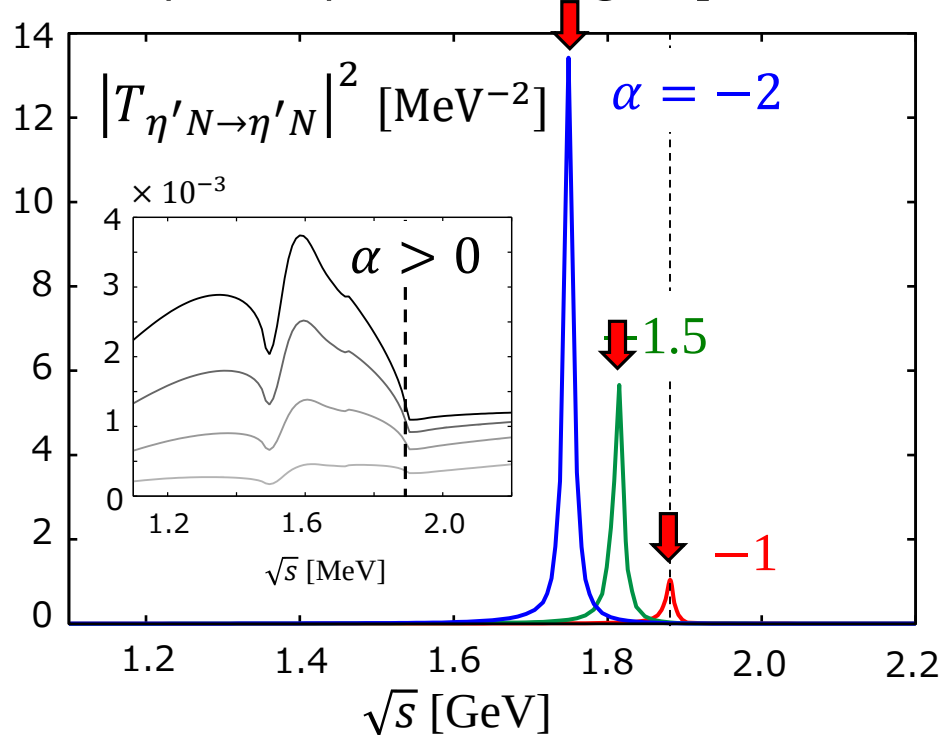
... at least it does not couple to πN due to its singlet char.

data : CNS, <http://gwdac.phys.gwu.edu/>

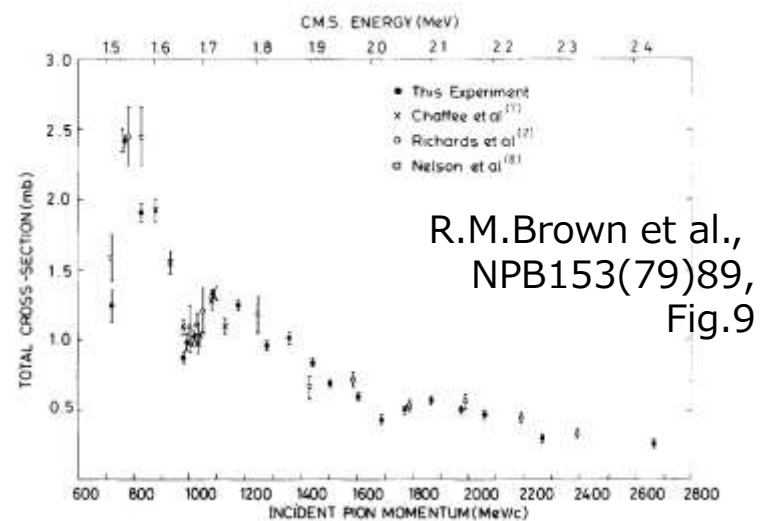
$\sigma_{\pi N \rightarrow \eta N}$ cross section

by Hinata, Kiyomura, Sakamoto [Nara WU.]

$\eta' N \rightarrow \eta' N$ scattering amplitude

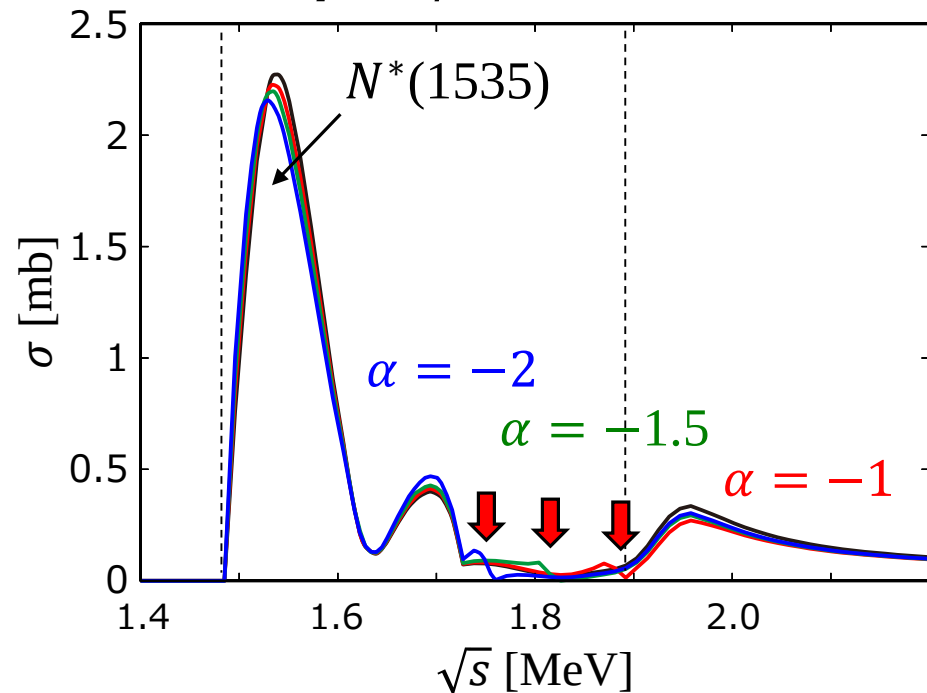


$\eta' N$ b.s. cannot be seen in η production

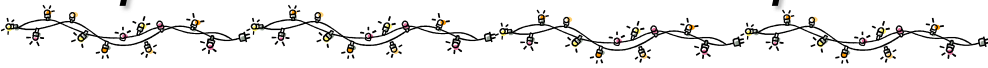


R.M.Brown et al.,
NPB153(79)89,
Fig.9

$\pi^- p \rightarrow \eta n$ cross section



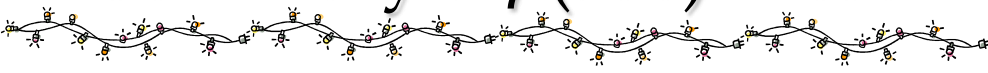
$\eta' N$ bound state $\Leftrightarrow \eta'$ -nucleus bound state ?



- ✓ $\pi N \rightarrow \eta' N$ is **sensitive** to $V_{\eta_0 B}$ interaction (α), where, however, the $\eta' N$ bound state **cannot be reached** (above the threshold)
- ✓ The $\eta' N$ bound state **does not appear** in the π or η production, because it couples to $\eta' N$ channel selectively due to its singlet character.
- ✓ The large $\pi N \rightarrow \eta' N$ production prefers the **attractive** $V_{\eta_0 B}$, while the small scattering length prefers **zero or repulsive** $V_{\eta_0 B}$.
- ✓ $\eta' N$ b.s. must play an **important role in η' -nucleus** optical potentials, which gives **strong energy dependence**.

$\eta' N$ b.s. can be found as (deeply) η' -nucleus bound state ?

Summary : $\eta'(958)$ -meson-nucleus bound system



**Partial restoration of Chiral sym and $U_A(1)$ anomaly effect
in the viewpoint of mesic-nuclei**

(possible) large mass reduction **without** large absorption

$$\text{Re } V \gg \text{Im } V$$

special & unique feature of η'
different from η , ω , ϕ -mesic nuclei

ongoing theoretical works in NaraWU

- ✓ Considering $\eta'N$ bound state
- ✓ estimate possible α (strength of singlet meson-baryon int.)
 - $\leftrightarrow$ transparency ratio of η'
 - $\leftrightarrow \pi N \rightarrow \eta'N$ cross section
 - $\leftrightarrow \eta'N$ scattering length and so on...