

Phenomenology of weak meson production

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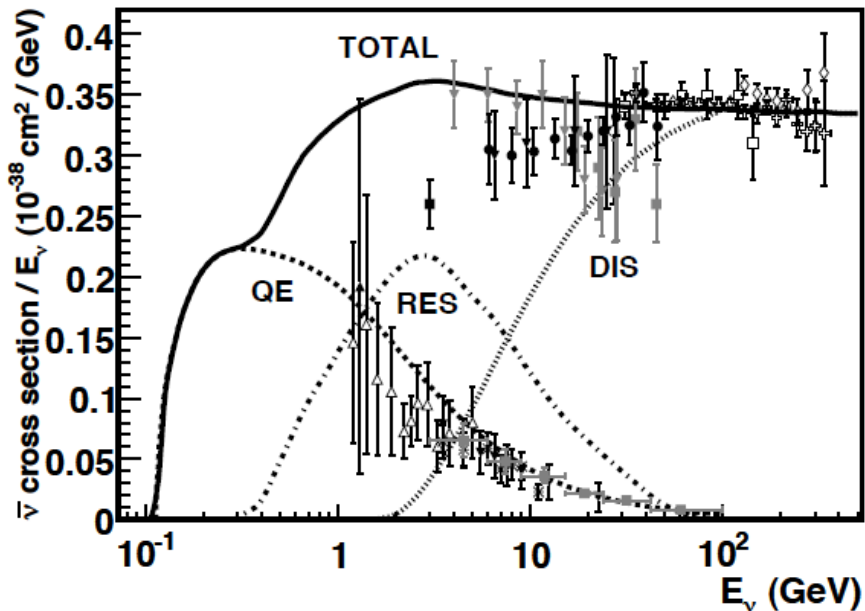
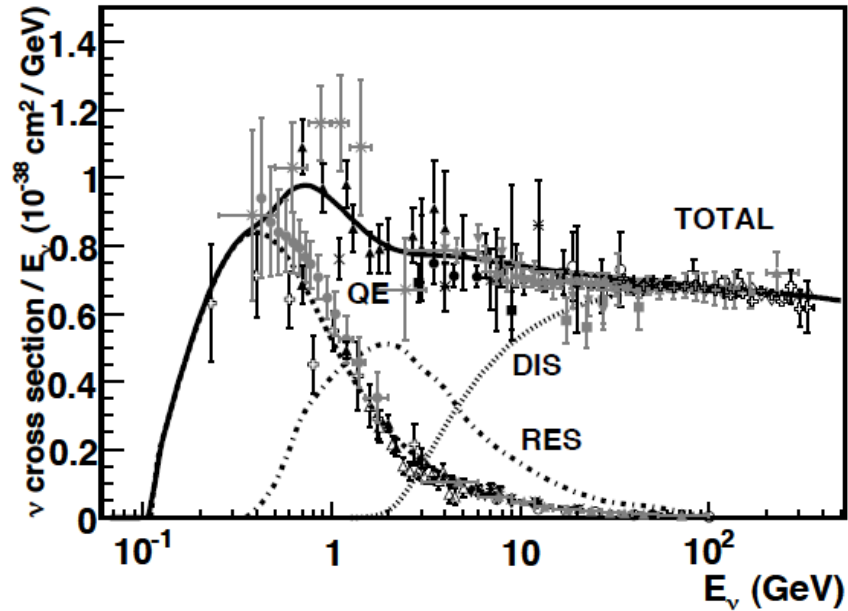
Introduction

- Neutrino interactions with matter are at the heart all experiments seeking to unravel its nature.
- Oscillation experiments (with accelerator ν in the few-GeV region):
T2K, NOvA, MicroBooNE, Hyper-K, DUNE/LBNF
 - Good understanding of neutrino interactions are important for:
 - ν detection, E_ν reconstruction, ν flux calibration
 - determination of (irreducible) backgrounds
 - reduction of systematic errors
 - needed in the quest for CP violation and ν mass hierarchy
 - Precision of 1-5% in ν cross sections are required

Introduction

- Neutrino interactions with matter are at the heart of many interesting and relevant physical processes
 - Astrophysics
 - Dynamics of the core-collapse in supernovae
 - r-process nucleosynthesis
 - Physics Beyond the Standard Model
 - Non-standard ν interactions
 - Hadronic physics
 - Nucleon and Nucleon-Resonance (N- Δ , N-N*) axial form factors
 - Strangeness content of the nucleon spin
 - Nuclear physics
 - Information about: nuclear correlations, MEC, spectral functions
 - Complement electron scattering studies

Introduction



CC cross sections:
world data and **NUANCE** generator
Formaggio, Zeller, Rev. Mod. Phys. (2012)

Weak meson production

$$\nu_l N \rightarrow l \pi N'$$

■ CC: $\nu_\mu p \rightarrow \mu^- p \pi^+, \quad \bar{\nu}_\mu p \rightarrow \mu^+ p \pi^-$
 $\nu_\mu n \rightarrow \mu^- p \pi^0, \quad \bar{\nu}_\mu p \rightarrow \mu^+ n \pi^0$
 $\nu_\mu n \rightarrow \mu^- n \pi^+, \quad \bar{\nu}_\mu n \rightarrow \mu^+ n \pi^-$

■ source of CCQE-like events (in nuclei)

■ needs to be subtracted for a good E_ν reconstruction

■ NC: $\nu_\mu p \rightarrow \nu_\mu p \pi^0, \quad \bar{\nu}_\mu p \rightarrow \bar{\nu}_\mu p \pi^0$
 $\nu_\mu p \rightarrow \nu_\mu n \pi^+, \quad \bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu n \pi^0$
 $\nu_\mu n \rightarrow \nu_\mu n \pi^0, \quad \bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu n \pi^0$
 $\nu_\mu n \rightarrow \nu_\mu p \pi^-, \quad \bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu p \pi^-$

■ e-like background to $\nu_\mu \rightarrow \nu_e$ (T2K)

Weak meson production

- $\Delta S = 0$ e.g. $\nu_l p(n) \rightarrow l^- K^+ \Sigma^+ (\Lambda)$ Nakamura et al., arXiv:1506.03403
- $\Delta S = 1$:
 - Cabibbo suppressed but with lower thresholds than $\Delta S = 0$
 - Kaon: $\nu_l p \rightarrow l^- K^+ p$
 $\nu_l n \rightarrow l^- K^0 p$
 $\nu_l n \rightarrow l^- K^+ n$
- Background for proton decay $p \rightarrow \nu K^+$

Weak meson production

- $\Delta S = -1$:

- Cabibbo suppressed but with lower thresholds than $\Delta S = 0$

- antiKaon: $\bar{\nu}_l p \rightarrow l^+ K^- p$

$$\bar{\nu}_l p \rightarrow l^+ \bar{K}^0 n$$

$$\bar{\nu}_l n \rightarrow l^+ K^- n$$

- $\Sigma \pi$: $\bar{\nu}_l p \rightarrow l^+ \Sigma^0 \pi^0$

$$\bar{\nu}_l p \rightarrow l^+ \Sigma^+ \pi^-$$

$$\bar{\nu}_l p \rightarrow l^+ \Sigma^- \pi^+$$

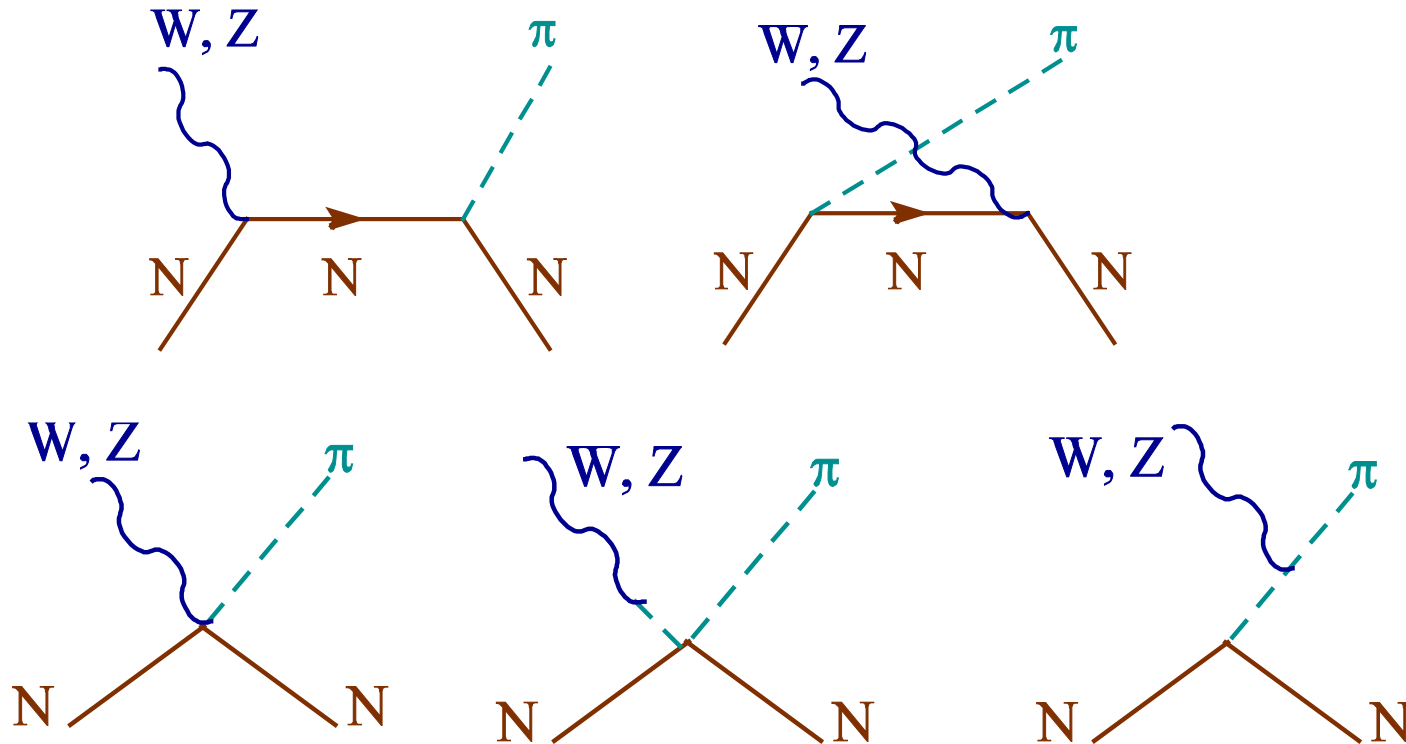
- can proceed through the excitation of Λ or Σ resonances

- in particular: $\Lambda(1405)$

1π production on the nucleon

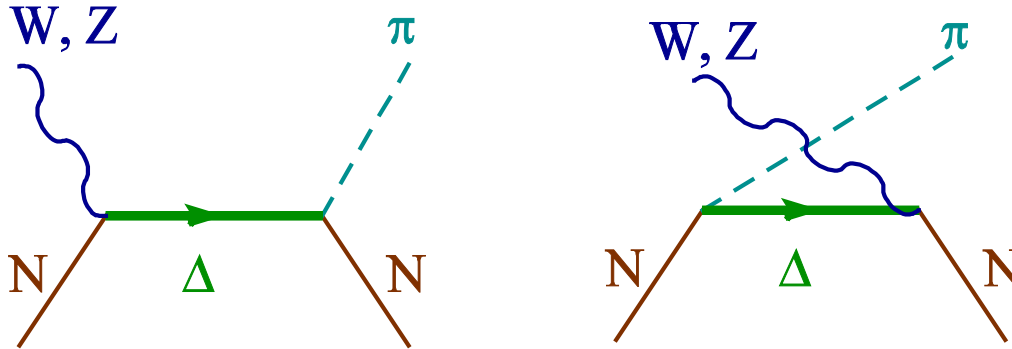
$$\nu_l N \rightarrow l \pi N'$$

■ From Chiral symmetry:



1 π production on the nucleon

- $\Delta(1232)$ excitation:



- N- Δ transition current:

$$J^\mu = \bar{\psi}_\mu \left[\left(\frac{C_3^V}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + \frac{C_5^V}{M^2} (g^{\beta\mu} q \cdot p - q^\beta p^\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + C_5^A g^{\beta\mu} + \frac{C_6^A}{M^2} q^\beta q^\mu \right] u$$

- Vector form factors $\Leftrightarrow$ Helicity amplitudes

1 π production on the nucleon

■ N- Δ transition current

$$J^\mu = \bar{\psi}_\mu \left[\left(\frac{C_3^V}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + \frac{C_5^V}{M^2} (g^{\beta\mu} q \cdot p - q^\beta p^\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + C_5^A g^{\beta\mu} + \frac{C_6^A}{M^2} q^\beta q^\mu \right] u$$

■ Helicity amplitudes can be extracted from data on π photo- and electro-production

$$A_{1/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 1/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = -1/2 \rangle \zeta$$

$$A_{3/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 3/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

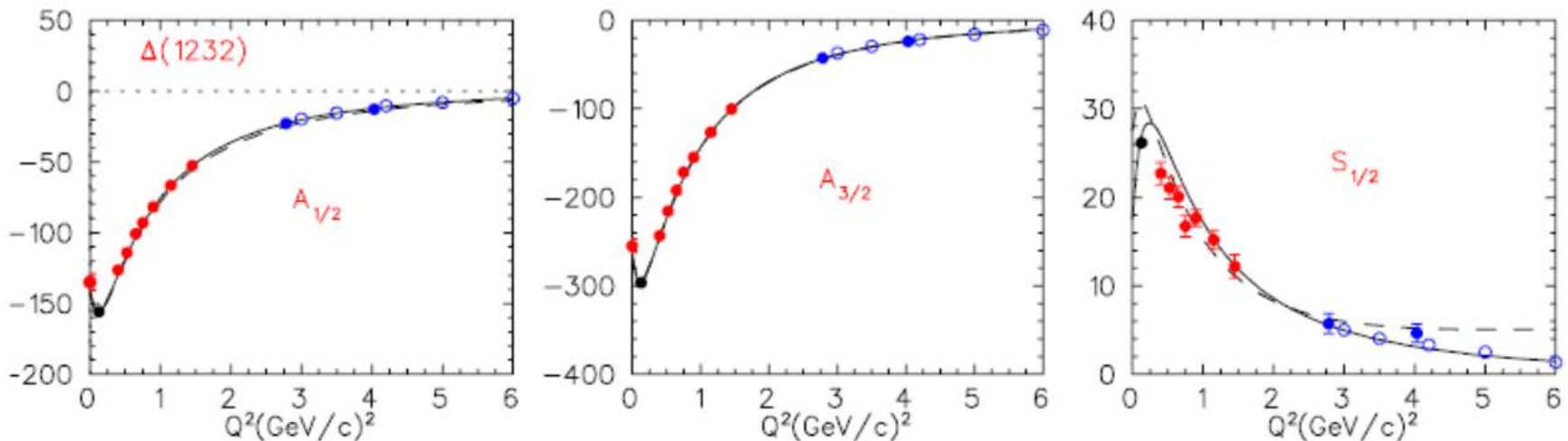
$$S_{1/2} = -\sqrt{\frac{2\pi\alpha}{k_R}} \frac{|\mathbf{q}|}{\sqrt{Q^2}} \langle R, J_z = 1/2 | \epsilon_\mu^0 J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

1 π production on the nucleon

■ N- Δ transition current

$$J^\mu = \bar{\psi}_\mu \left[\left(\frac{C_3^V}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + \frac{C_5^V}{M^2} (g^{\beta\mu} q \cdot p - q^\beta p^\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + C_5^A g^{\beta\mu} + \frac{C_6^A}{M^2} q^\beta q^\mu \right] u$$

■ **Helicity amplitudes** can be extracted from data on π photo- and electro-production Tiator et al., EPJ Special Topics 198 (2011)



1π production on the nucleon

■ N- Δ transition current

$$J^\mu = \bar{\psi}_\mu \left[\left(\frac{C_3^V}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + \frac{C_5^V}{M^2} (g^{\beta\mu} q \cdot p - q^\beta p^\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M} (g^{\beta\mu} \not{q} - q^\beta \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + C_5^A g^{\beta\mu} + \frac{C_6^A}{M^2} q^\beta q^\mu \right] u$$

■ Axial form factors

$$C_6^A = C_5^A \frac{M^2}{m_\pi^2 + Q^2} \leftarrow \text{PCAC}$$

$$C_5^A = C_5^A(0) \left(1 + \frac{Q^2}{M_{A\Delta}^2} \right)^{-2}$$

■ Constraints from ANL and BNL data on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$

■ with large normalization (flux) uncertainties

■ ANL and BNL data **do not** constrain $C_{3,4}^A$: consistent with **zero**
Hernandez et al., PRD81(2010)

1π production on the nucleon

- N- Δ axial form factors: determination of $C_5^A(0)$ and $M_{A\Delta}$
- $C_5^A = C_5^A(0) \left(1 + \frac{Q^2}{M_{A\Delta}^2}\right)^{-2}$
- From ANL and BNL data on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$
- Graczyk et al., PRD 80 (2009)
 - Deuteron effects
 - Non-resonant background **absent**
 - $C_5^A(0) = 1.19 \pm 0.08$, $M_{A\Delta} = 0.94 \pm 0.03$ GeV
- Hernandez et al., PRD 81 (2010)
 - Deuteron effects
 - $C_5^A(0) = 1.00 \pm 0.11$, $M_{A\Delta} = 0.93 \pm 0.07$ GeV
 - 20% reduction of the GT relation $C_5^A(0) = \frac{g_{\Delta N \pi} f_\pi}{\sqrt{6} M} \approx 1.2 \leftarrow$ off diagonal GT relation

1π production on the nucleon

- Watson's theorem

- Unitarity
- Time reversal invariance

$$\sum_M \langle M|T|F\rangle^* \langle M|T|I\rangle = -2\text{Im}\langle F|T|I\rangle \in \mathbb{R}$$

- For $W N \rightarrow \pi N$

- assuming that $|M\rangle = |F\rangle = |\pi N\rangle$
- schematically:

$$\langle \pi N|T|\pi N\rangle^* \langle \pi N|T|W N\rangle = -2\text{Im}\langle \pi N|T|W N\rangle \in \mathbb{R}$$

$$\langle \pi N|T|\pi N\rangle \approx \langle \pi N|T_{\text{strong}}|\pi N\rangle$$

1π production on the nucleon

- Watson's theorem

- Unitarity
- Time reversal invariance

- For $W N \rightarrow \pi N$

$$\sum_{\rho} \sum_L \frac{2L+1}{2J+1} (L, 1/2, J; 0, -\lambda') (L, 1/2, J; 0, -\rho) \langle J, M; L, 1/2 | T_{\text{str}} | J, M; L, 1/2 \rangle^* \langle J, M; 0, \rho | T | 0, 0; r, \lambda \rangle \in \mathbb{R}.$$

- For the dominant $J=3/2, I=3/2, L=1 \Leftrightarrow P_{33}$ partial wave

$$\left[\sum_{\rho} (1, 1/2, 3/2; 0, -\rho) (1, 1/2, 3/2; 0, -\rho) \langle 3/2, M; 0, \rho | T | 0, 0; r, \lambda \rangle \right] e^{-i\delta_{P_{33}}} \in \mathbb{R}$$

writing $T = T_{\Delta} + T_B e^{-i\delta(W, q^2)}$ we impose Watson's theorem.

- This approach has been applied for π photo and electroproduction

Olsson, NPB78 (1974)

Carrasco, Oset, NPA536 (1992)

Gil, Nieves, Oset, NPA627 (1997)

1π production on the nucleon

- Watson's theorem

- Unitarity
- Time reversal invariance

- For $W N \rightarrow \pi N$

$$\sum_{\rho} \sum_L \frac{2L+1}{2J+1} (L, 1/2, J; 0, -\lambda') (L, 1/2, J; 0, -\rho) \langle J, M; L, 1/2 | T_{\text{str}} | J, M; L, 1/2 \rangle^* \langle J, M; 0, \rho | T | 0, 0; r, \lambda \rangle \in \mathbb{R}$$

- For the dominant $J=3/2, I=3/2, L=1 \Leftrightarrow P_{33}$ partial wave

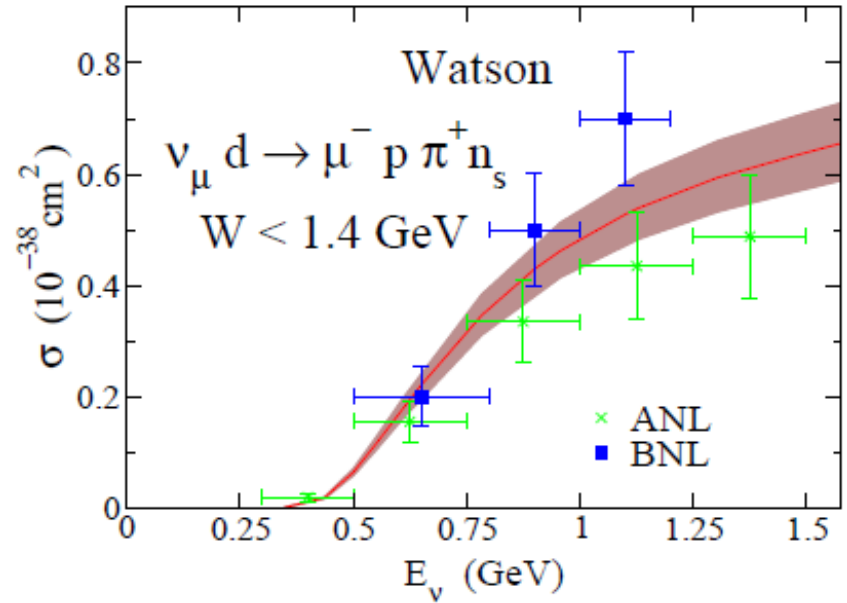
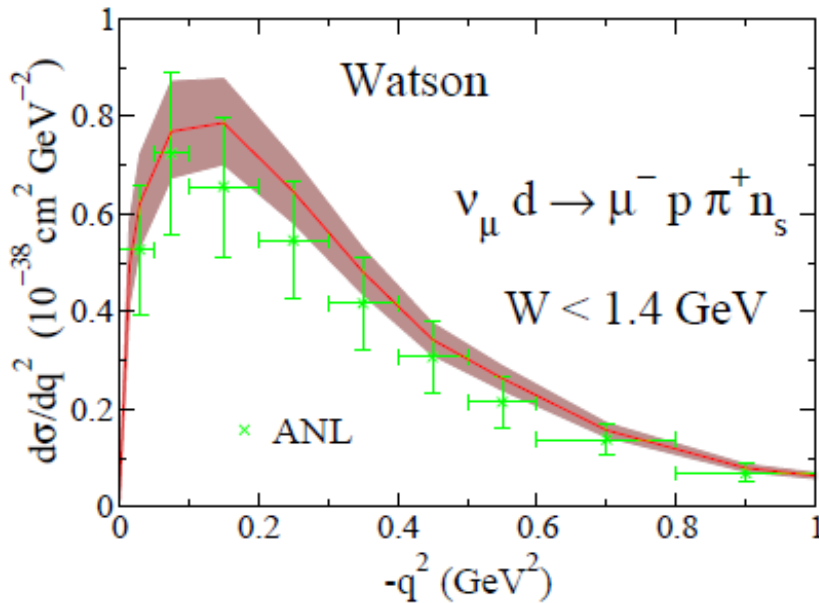
$$\left[\sum_{\rho} (1, 1/2, 3/2; 0, -\rho) (1, 1/2, 3/2; 0, -\rho) \langle 3/2, M; 0, \rho | T | 0, 0; r, \lambda \rangle \right] e^{-i\delta_{P_{33}}} \in \mathbb{R}$$

writing $T = T_{\Delta} + T_B e^{-i\delta(W, q^2)}$ we impose Watson's theorem.

- This approach has been applied for π photo and electroproduction
- In weak production two phases δ_V and δ_A are needed

1π production on the nucleon

- Fit to ANL and BNL data with $W < 1.4$ GeV

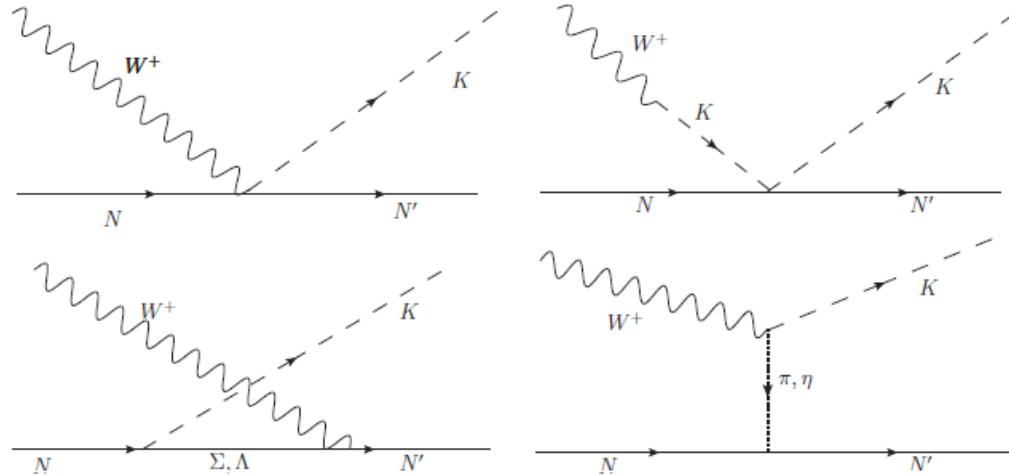


- $C_5^A(0) = 1.12 \pm 0.11$, $M_{A\Delta} = 0.95 \pm 0.06 \text{ GeV}$

- Consistent with the off-diagonal GT relation $C_5^A(0) = \frac{g_{\Delta N\pi} f_\pi}{\sqrt{6}M} \approx 1.2$

Strangeness production

- $\Delta S = 1$: $\nu_l p \rightarrow l^- K^+ p$
 $\nu_l n \rightarrow l^- K^0 p$
 $\nu_l n \rightarrow l^- K^+ n$



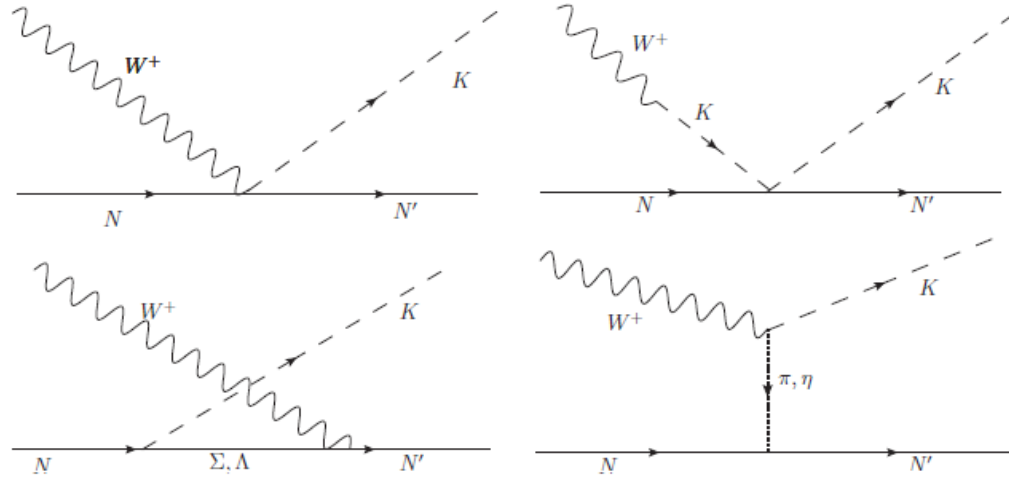
- Rafi Alam et al., PRD 82 (2010)

- SU(3) symmetric chiral Lagrangian
- Physical hadron masses
- s-channel baryon pole diagrams absent
- Couplings depend on V_{us} , D , F , f_π
 - fixed by nucleon and hyperon semileptonic decay and pion decay
- Global dipole form factor

$$F(q^2) = \left(1 - \frac{q^2}{M_F^2}\right)^{-2} \quad M_F = 1 \pm 0.1 \text{ GeV}$$

Strangeness production

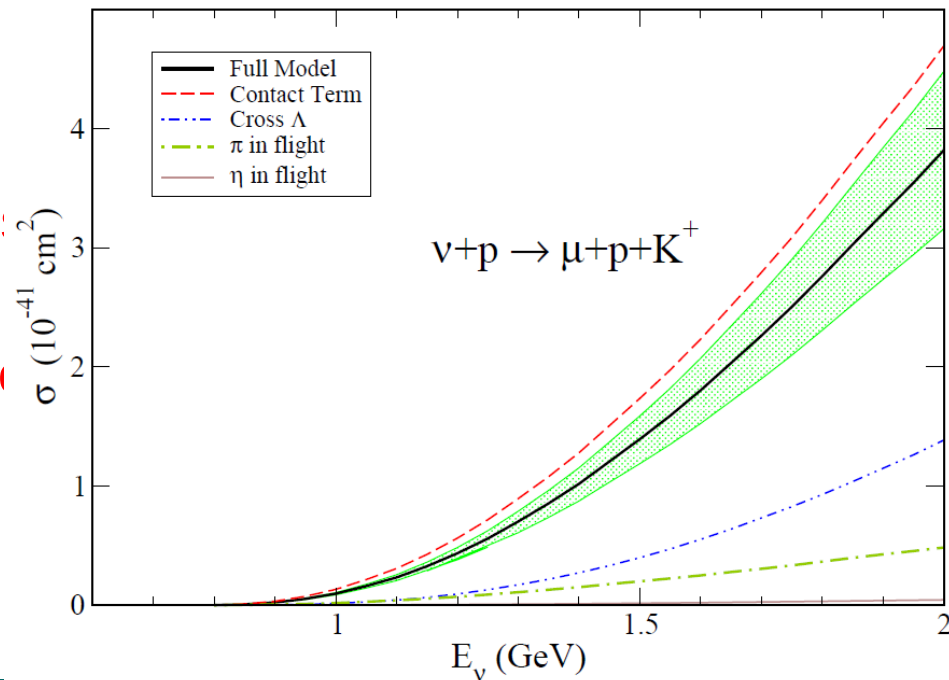
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- Rafi Alam et al., PRD 82 (2010)

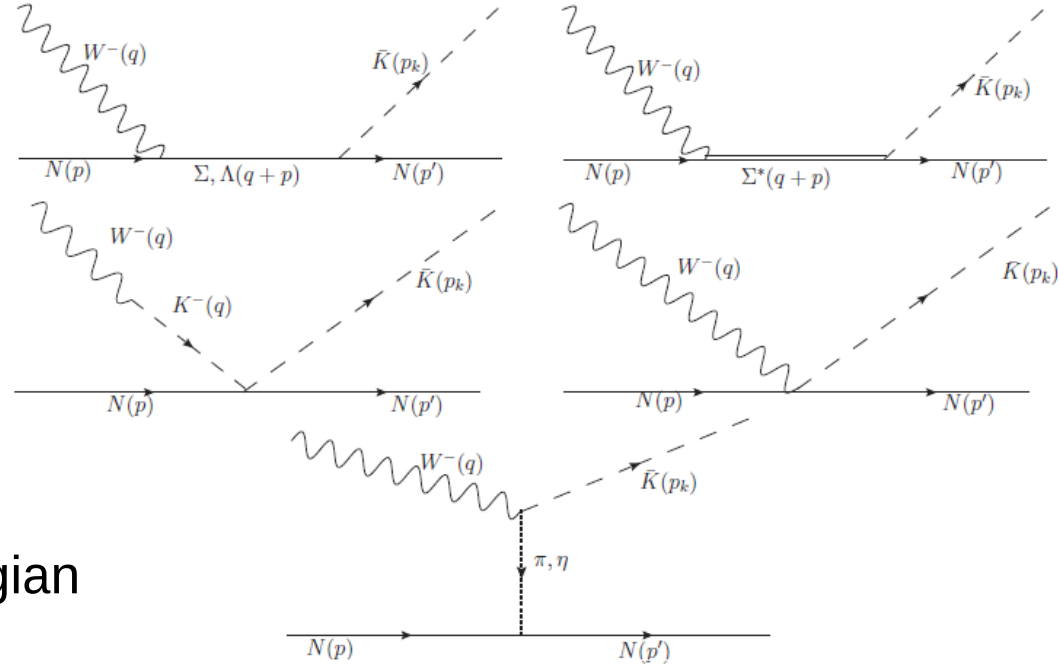
- SU(3) symmetric chiral Lagrangian
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$$F(q^2) = \left(1 - \frac{q^2}{M_F^2}\right)^{-2} \quad M_F = 1 \pm 0.1 \text{ GeV}$$



Strangeness production

- $\Delta S = -1$: $\bar{\nu}_l p \rightarrow l^+ K^- p$
 $\bar{\nu}_l p \rightarrow l^+ \bar{K}^0 n$
 $\bar{\nu}_l n \rightarrow l^+ K^- n$

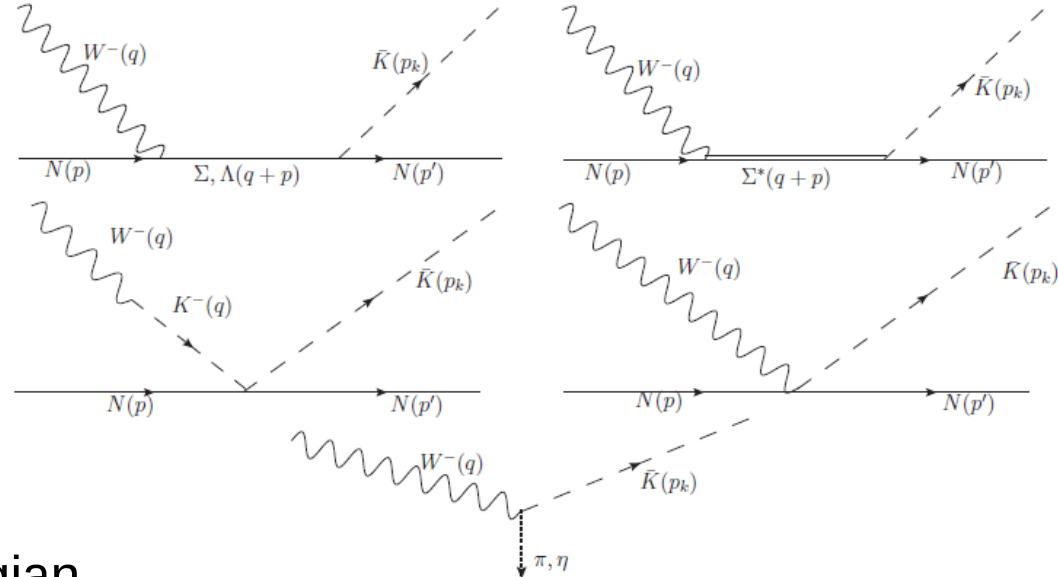


- Rafi Alam et al., PRD 85 (2012)
- SU(3) symmetric chiral Lagrangian
- Physical hadron masses
- s-channel baryon pole diagrams present
 - spin 3/2 $\Sigma(1385)$
- Couplings depend on V_{us} and D, F, f_π ← fixed by semileptonic decays
- Global dipole form factor

$$F(q^2) = \left(1 - \frac{q^2}{M_F^2}\right)^{-2} \quad M_F = 1 \pm 0.1 \text{ GeV}$$

Strangeness production

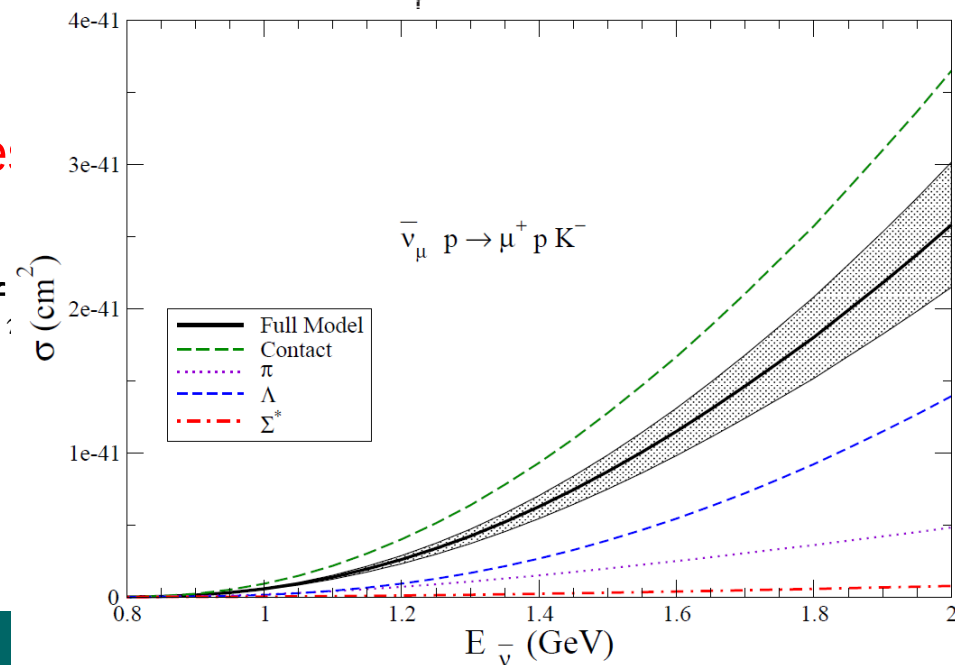
- $\Delta S = -1$: $\bar{\nu}_l p \rightarrow l^+ K^- p$
 $\bar{\nu}_l p \rightarrow l^+ \bar{K}^0 n$
 $\bar{\nu}_l n \rightarrow l^+ K^- n$



- Rafi Alam et al., PRD 85 (2012)

- SU(3) symmetric chiral Lagrangian
- Physical hadron masses
- s-channel baryon pole diagrams pre:
 - spin 3/2 $\Sigma(1385)$
- Couplings depend on V_{us} and D, F, f_1^2
- Global dipole form factor

$$F(q^2) = \left(1 - \frac{q^2}{M_F^2}\right)^{-2} \quad M_F = 1 \pm 0.1 \text{ GeV}$$



Strangeness production

- $\bar{\nu}_l p \rightarrow l^+ \phi B$ Ren et al., PRC91 (2015)

$$\phi B = K^- p, \bar{K}^0 n, \pi^0 \Lambda, \pi^0 \Sigma^0, \eta \Lambda, \eta \Sigma^0, \pi^+ \Sigma^-, \pi^- \Sigma^+, K^+ \Xi^-, K^0 \Xi^0$$

- **SU(3)** symmetric chiral Lagrangian
- **Physical** hadron masses
- Couplings depend on V_{us} and D, F, f_π $\leftarrow$ fixed by **semileptonic decays**
- Global dipole form factor

$$F(q^2) = \left(1 - \frac{q^2}{M_F^2}\right)^{-2} \quad M_F = 1 \pm 0.1 \text{ GeV}$$

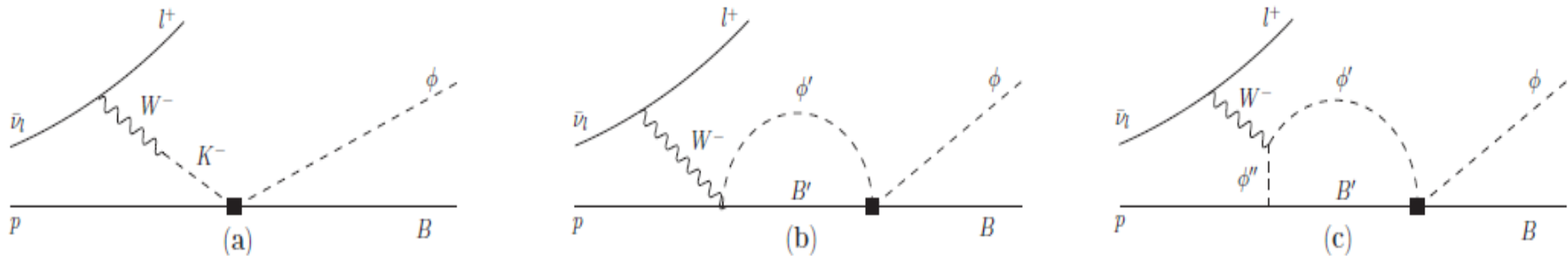
- s-wave projection
- **Unitarization in coupled channels**

Strangeness production

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- Unitarization in coupled channels



- T: Solution of the Bethe-Salpeter eq. in coupled channels

$$T = V + VGT = [1 - VG]^{-1}V$$

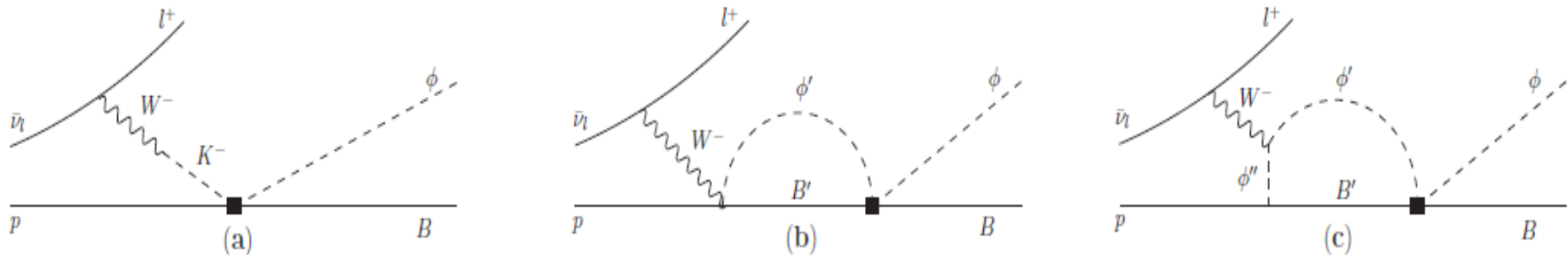
- V: from leading order chiral Lagrangian
- Cut-off regularization of the loop functions with $q_{\text{max}} = 630$ MeV
- Oset, Ramos, NPA635 (1998)

Strangeness production

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$$\phi B = K^- p, \bar{K}^0 n, \pi^0 \Lambda, \pi^0 \Sigma^0, \eta \Lambda, \eta \Sigma^0, \pi^+ \Sigma^-, \pi^- \Sigma^+, K^+ \Xi^-, K^0 \Xi^0$$

- Unitarization in coupled channels



- $\Lambda(1405)$ dynamically generated
- Two poles: $M \approx 1385 \text{ MeV}, \Gamma \approx 150 \text{ MeV}$
 $M \approx 1420 \text{ MeV}, \Gamma \approx 40 \text{ MeV}$
- Suggested by Dalitz et al.(60ies) and obtained in many theoretical studies

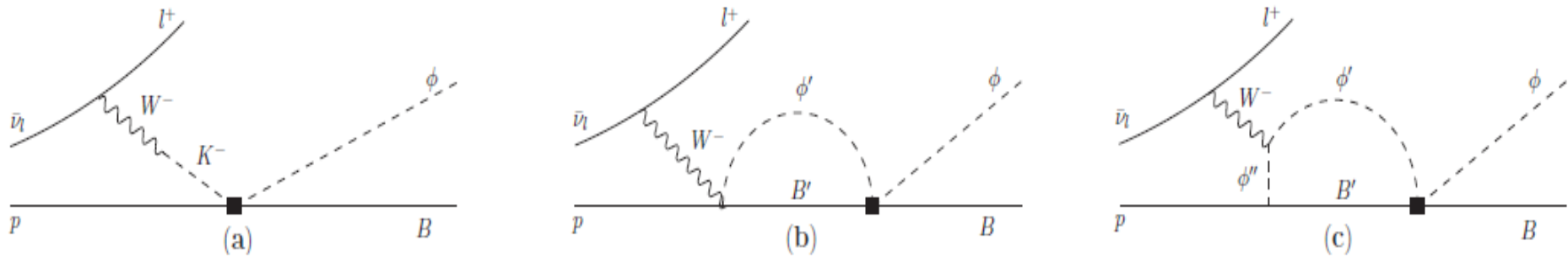
Oller, Meissner, PLB500(2001); Jido et al. NPA725(2003); Borasoy et al. PRC74(2006);
 Geng, Oset, EPJA34(2007); Hyodo, Jido, Prog.Part.Nucl.Phys.67(2012);
 Guo, Oller PRC87(2013); Roca, Oset PRC87(2013); Mai, Meissner, EPJA51(2015); ...

Strangeness production

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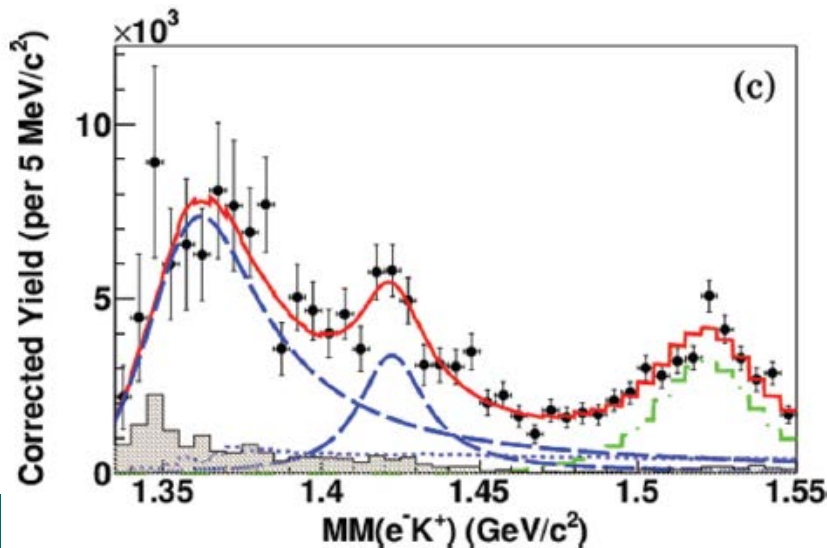
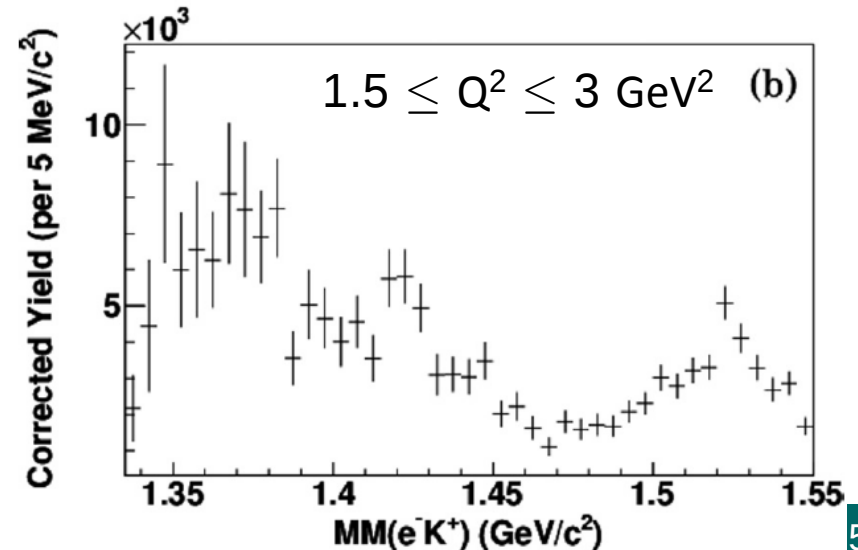
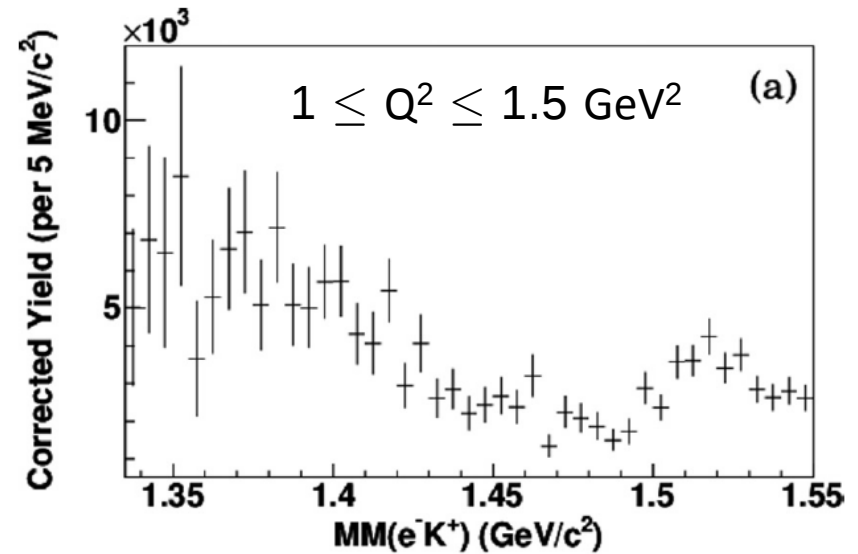
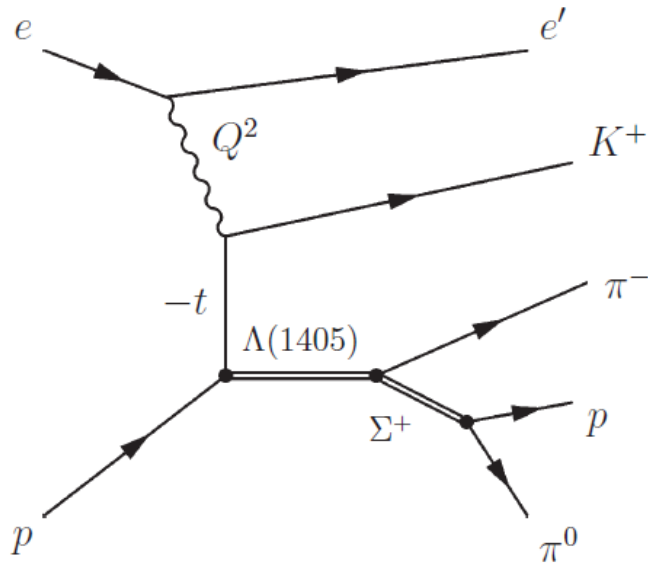
- Unitarization in coupled channels



- $\Lambda(1405)$ dynamically generated
- Two poles: $M \approx 1385 \text{ MeV}, \Gamma \approx 150 \text{ MeV}$
 $M \approx 1420 \text{ MeV}, \Gamma \approx 40 \text{ MeV}$
- Suggested by Dalitz et al.(60ies) and obtained in many theoretical studies
- Consistent with data:
 $K^- p \rightarrow \phi B, K^- p \rightarrow \pi^0 \pi^0 \Sigma^0, p p \rightarrow p K^- \Lambda(1405), \gamma p \rightarrow K^+ \pi \Sigma,$
 $e p \rightarrow e' K^+ \Lambda(1405)$

Strangeness production

■ $ep \rightarrow e' K^+ \Lambda(1405)$ Lu et al. (CLAS), PRC88(2013)

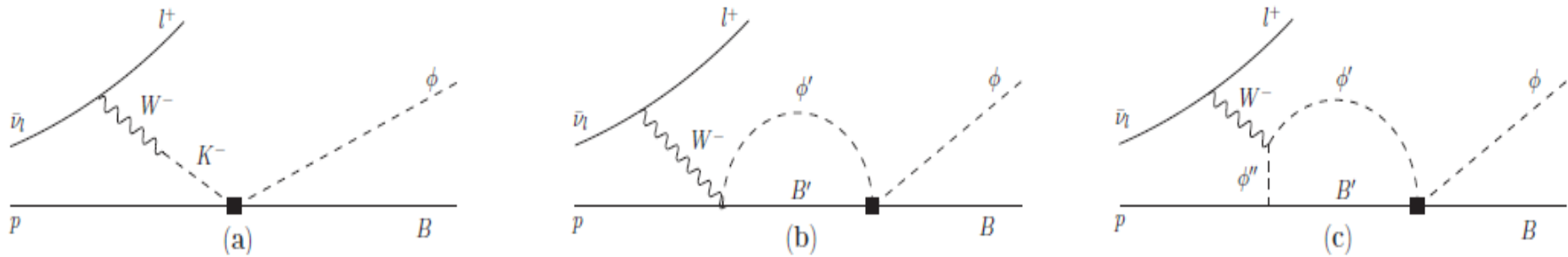


Strangeness production

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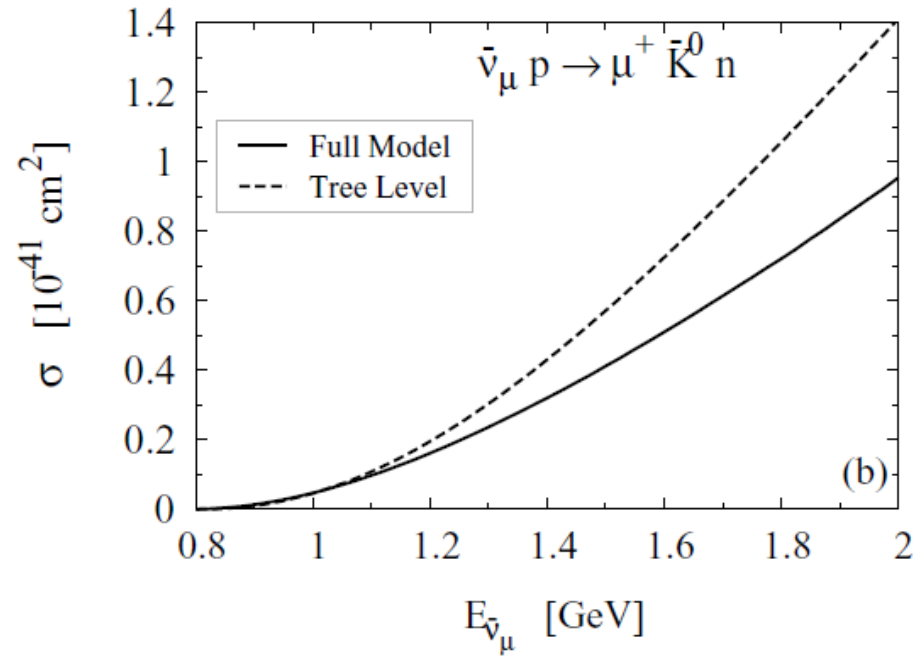
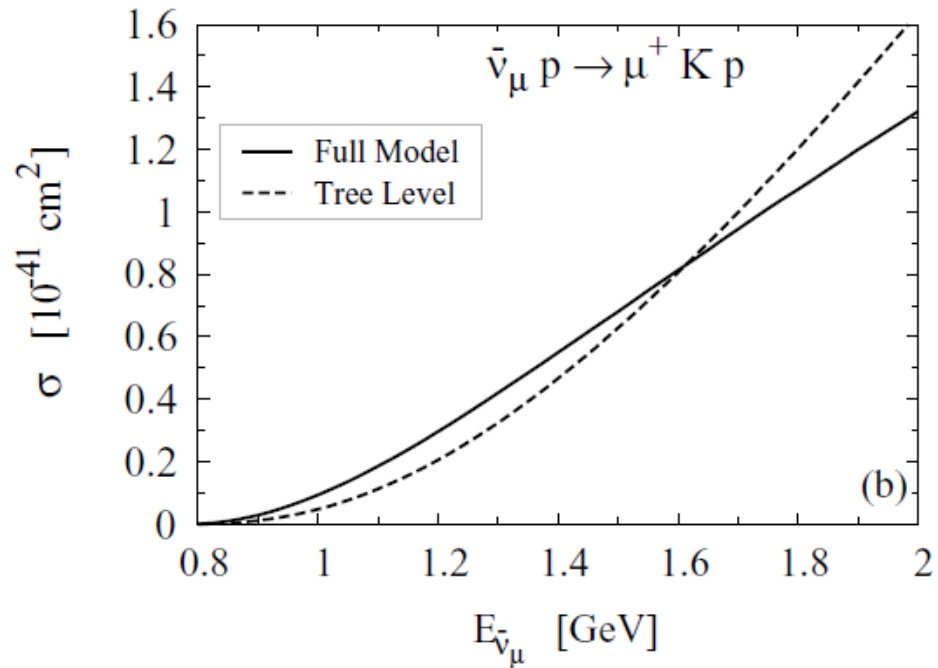
- Unitarization in coupled channels



- $\Lambda(1405)$ dynamically generated
- Two poles: $M \approx 1385 \text{ MeV}, \Gamma \approx 150 \text{ MeV}$
 $M \approx 1420 \text{ MeV}, \Gamma \approx 40 \text{ MeV}$
- $\bar{\nu}_l p \rightarrow l^+ \Lambda(1405)$ vs $\gamma p \rightarrow K^+ \pi \Sigma, e p \rightarrow e' K^+ \Lambda(1405)$
 - no lineshape distortion due to $K^+ \Lambda(1405)$ FSI
 - but Cabibbo suppressed

Strangeness production

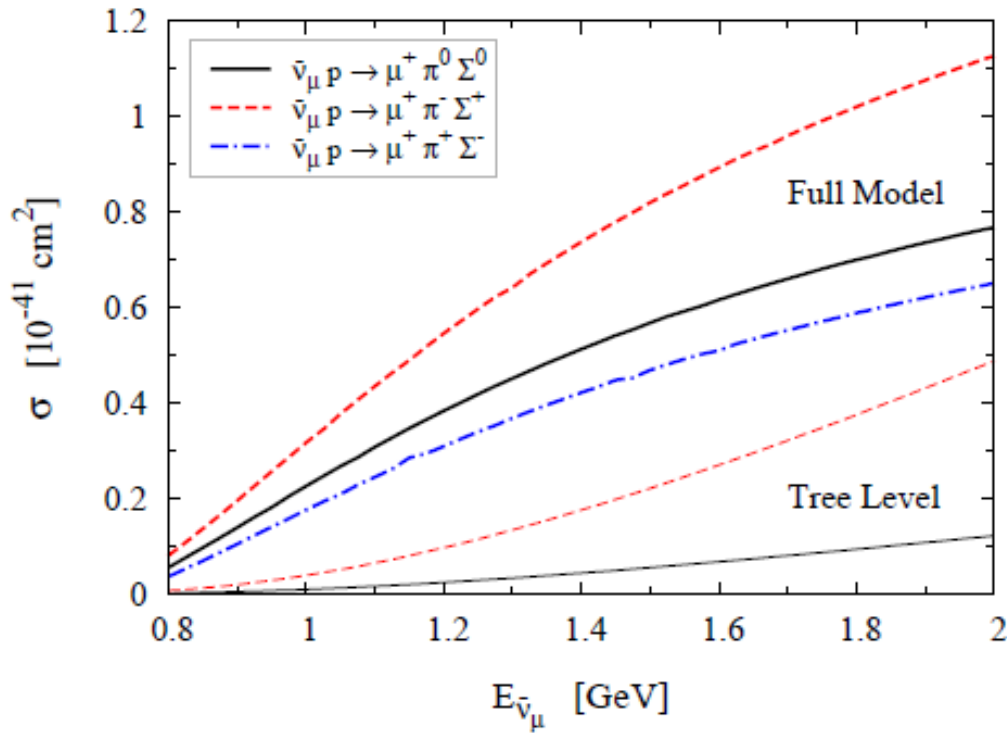
- $\bar{\nu}_l p \rightarrow l^+ \bar{K} N$ Ren et al., PRC91 (2015)



- Unitarization effects are not large: mostly a **reduction** of the cross section

Strangeness production

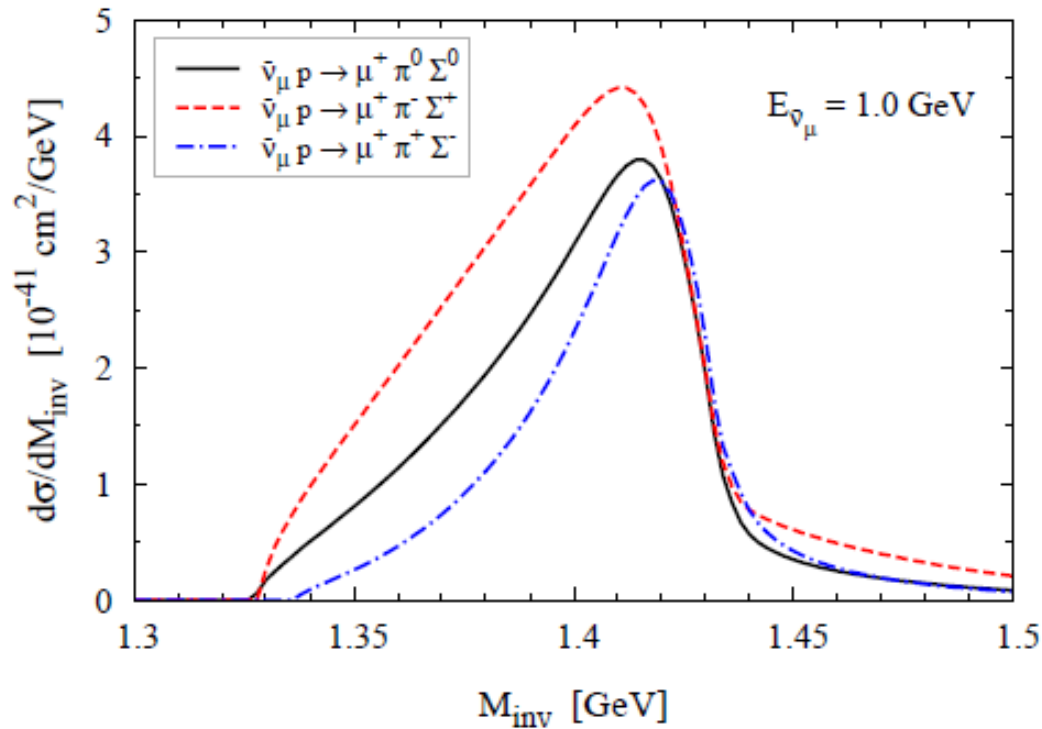
- $\bar{\nu}_l p \rightarrow l^+ \Sigma \pi$ Ren et al., PRC91 (2015)



- Cross sections largely driven by the $\Lambda(1405)$ resonance

Strangeness production

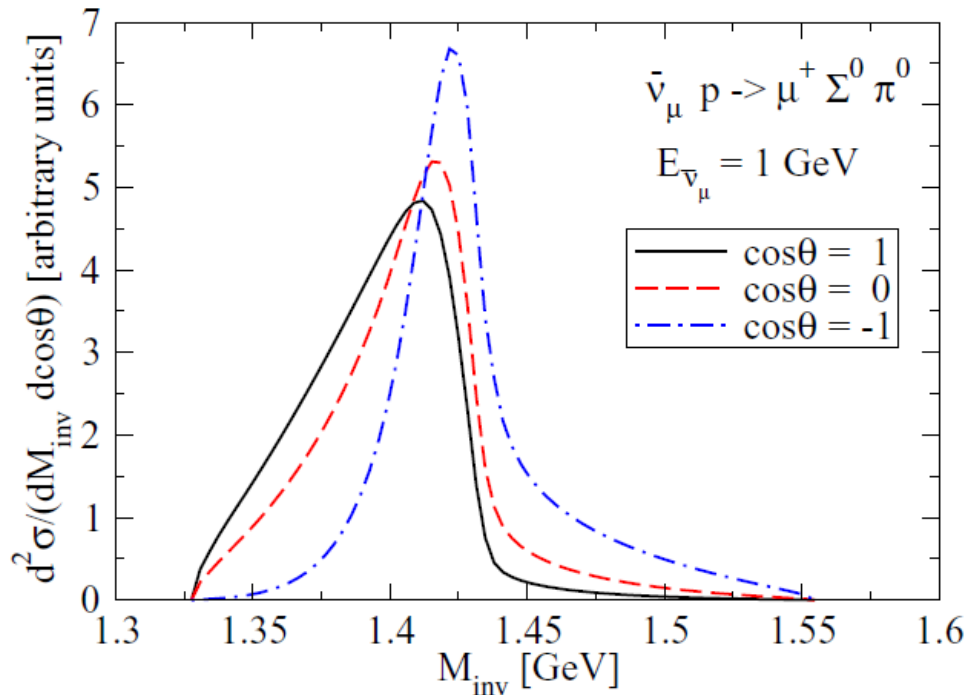
- $\bar{\nu}_l p \rightarrow l^+ \Sigma \pi$ Ren et al., PRC91 (2015)



- Cross sections largely driven by the $\Lambda(1405)$ resonance
- Differences in strength vs the $\pi^0 \Sigma^0$ channel from the $I=1$ amplitude
- Single asymmetric peak with more weight from the 1420 MeV pole

Strangeness production

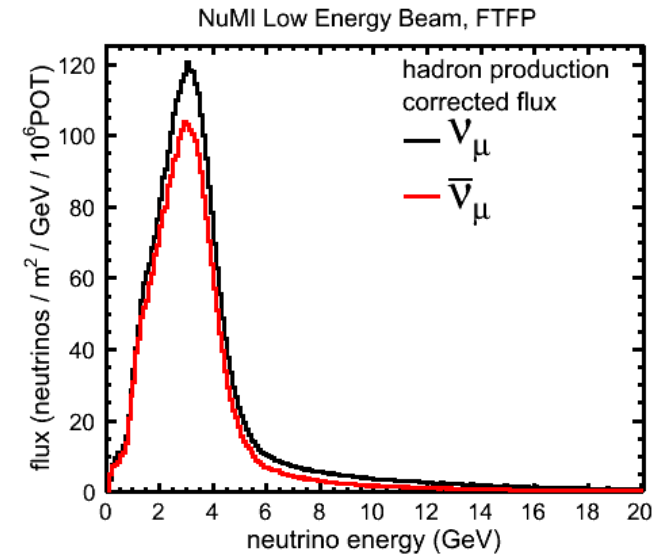
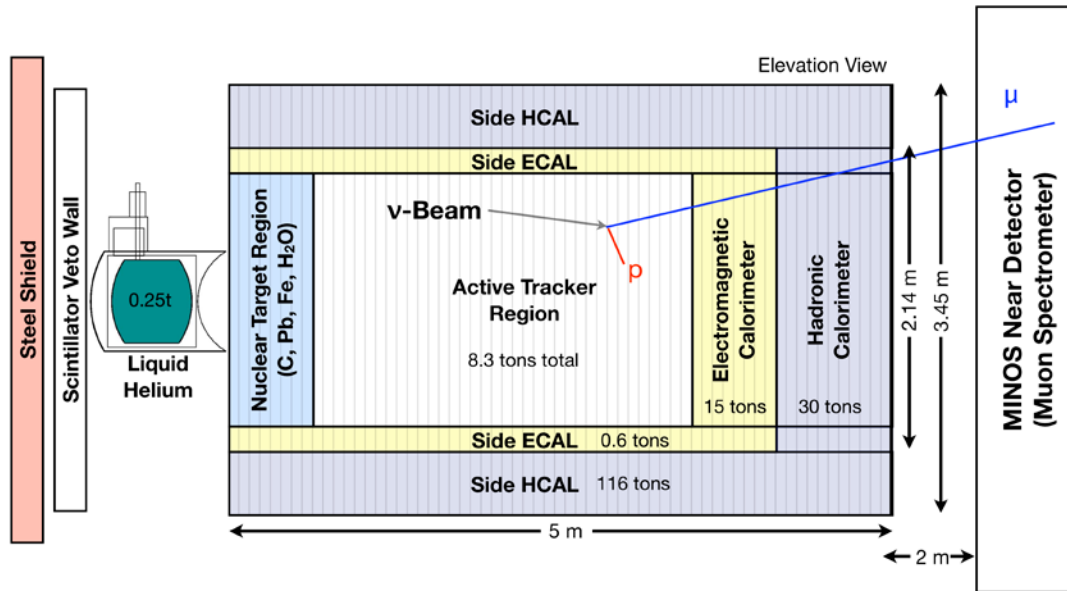
- $\bar{\nu}_l p \rightarrow l^+ \Sigma \pi$ Ren et al., PRC91 (2015)



- Single asymmetric peak with more weight from the 1420 MeV pole
- Backwards: $\sim$ Breit-Wigner resonance with $M \approx 1420 \text{ MeV}$, $\Gamma \approx 40 \text{ MeV}$
- Although $d^2\sigma(\cos\theta = -1) \sim d^2\sigma(\cos\theta = 1)/14$

Strangeness production

■ $\bar{\nu}_l p \rightarrow l^+ \Sigma \pi$ @ MINERvA (FNAL)



■ $\approx 2000 \pi \Sigma$ pairs @ scintillator

Conclusions

- ν scattering on nucleons and nuclei is relevant for oscillation studies
- Interesting for hadron and nuclear physics
- This is the case, in particular, for weak meson production
- Weak pion production and $|\Delta S| = 1$ reactions discussed
- Models are improved by unitarization
- Weak pion production: consistency with the off-diagonal G-T relation for the $N-\Delta$ transition is restored by imposing the Watson's theorem
- Weak production of $\Lambda(1405)$ studied for the first time
- New ν -N measurements are highly desirable