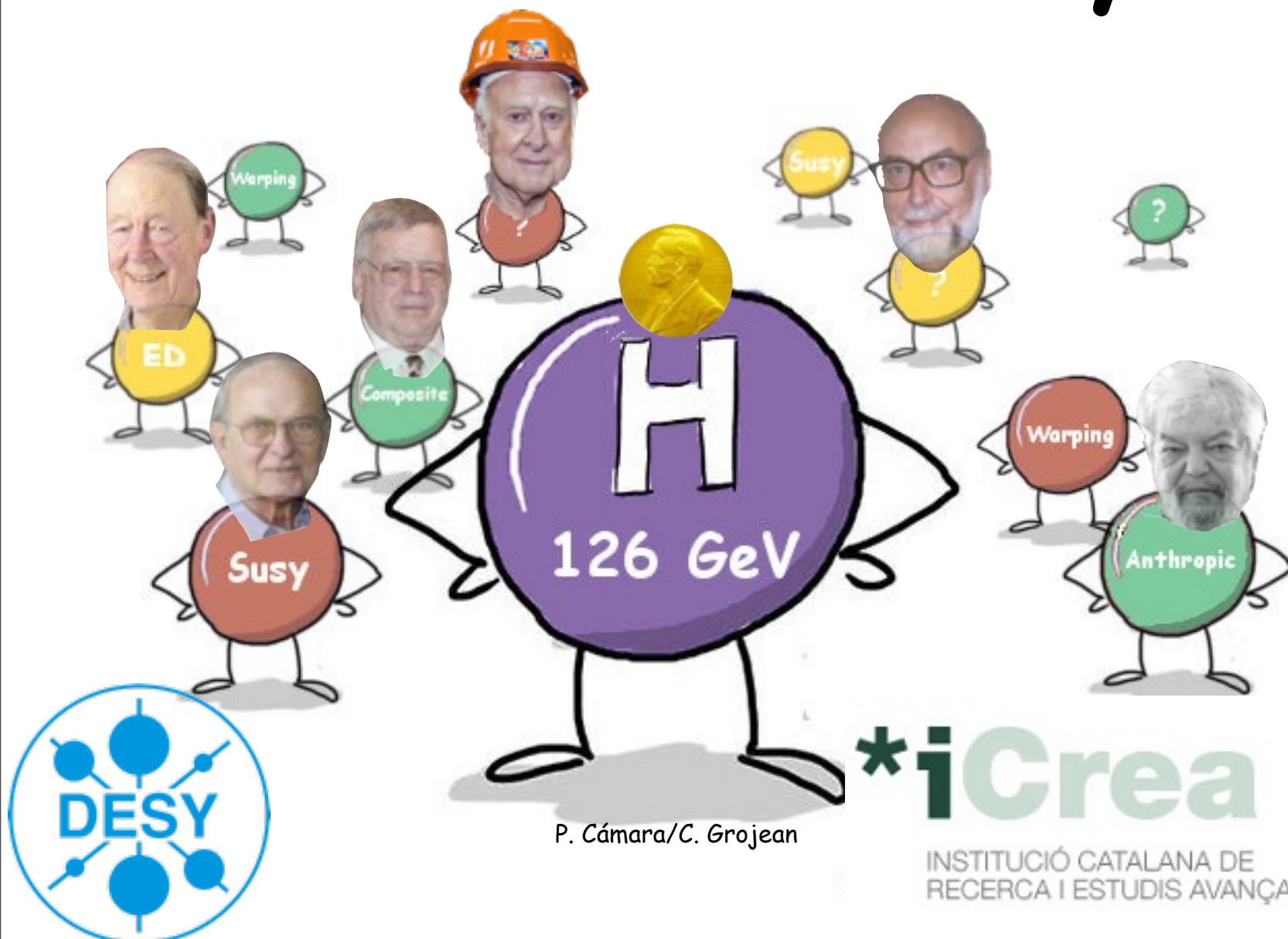


# Higgs Physics within and beyond the SM

*IFIC, Valencia, May 2015*



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# Disclaimer

These are slides that I've prepared for some lectures at the CERN-Latin American School of High Energy Physics last March in Ecuador.

There is partial overlap with what I covered during my blackboard lectures at IFIC even though some parts are missing in these notes.

Do not hesitate to contact me by email if you have any comments or questions.  
And please, report any typo/mistake that you might find in these notes.



# To help you reading these notes...

## Some exercises



do them by yourself!

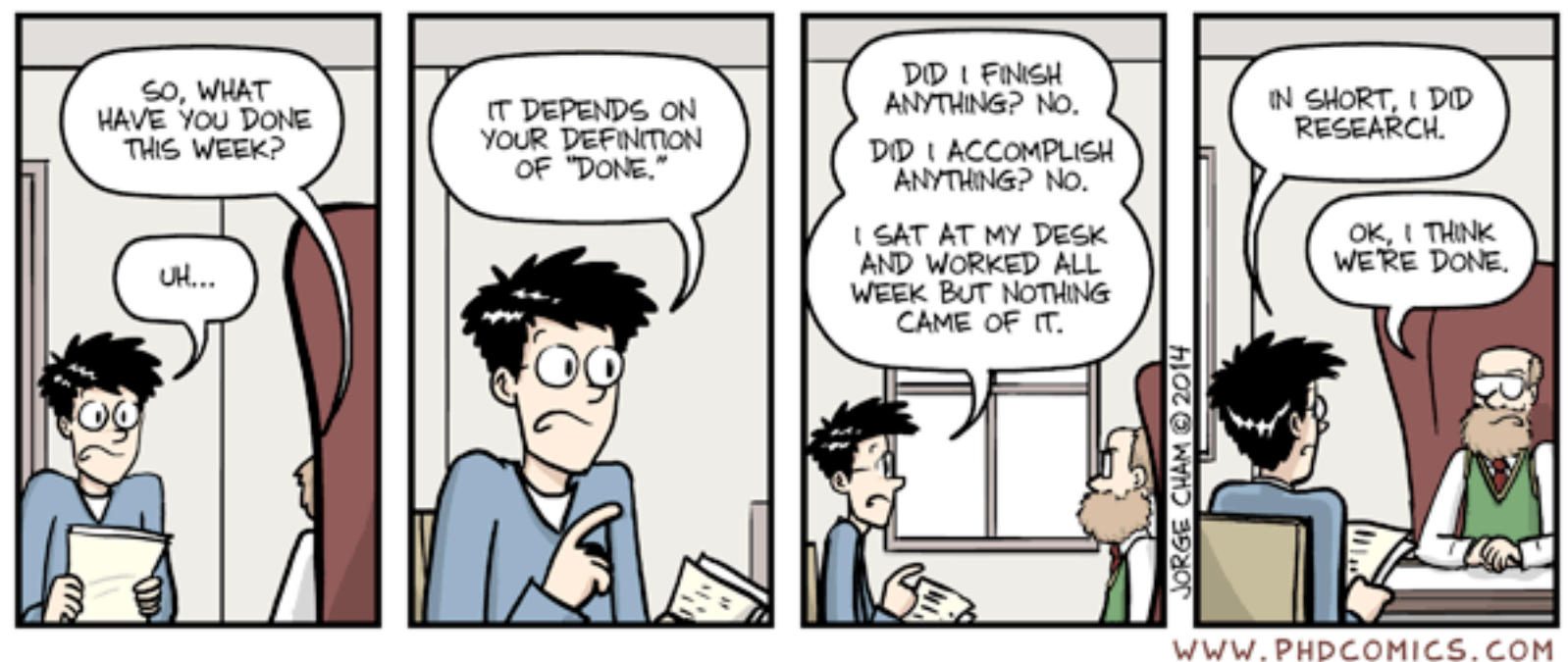
... or ask the discussion leaders to help you

## Some hyperlinks

➡ and ↺ ↻ ➡ to navigate through the pdf

text written in "red" (in particular all the references)

Your work, as PhD students, is to question all what you are listening during the lectures...



# Lecture Outline

1

## First Lecture $\supset$

- Standard Model and EW symmetry breaking  $\supset$
- Higgs mechanism - custodial symmetry  $\supset$
- Goldstone equivalence theorem  $\supset$
- What is the Higgs boson the name of?  $\supset$
- SM Higgs @ colliders  $\supset$
- UV behavior of the Higgs boson (triviality, stability, naturality)  $\supset$
- Symmetries for a natural EWSB  $\supset$

2

## Second Lecture $\supset$

- Implications for SUSY  $\supset$
- Composite Higgs models  $\supset$
- Precision Higgs couplings  $\supset$
- Future Higgs channels:
  - Boosted and off-shell channels  $\supset$
  - Multi-Higgs  $\supset$

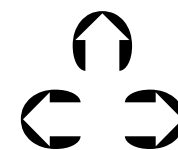
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[pictures: courtesy of NYT]

1

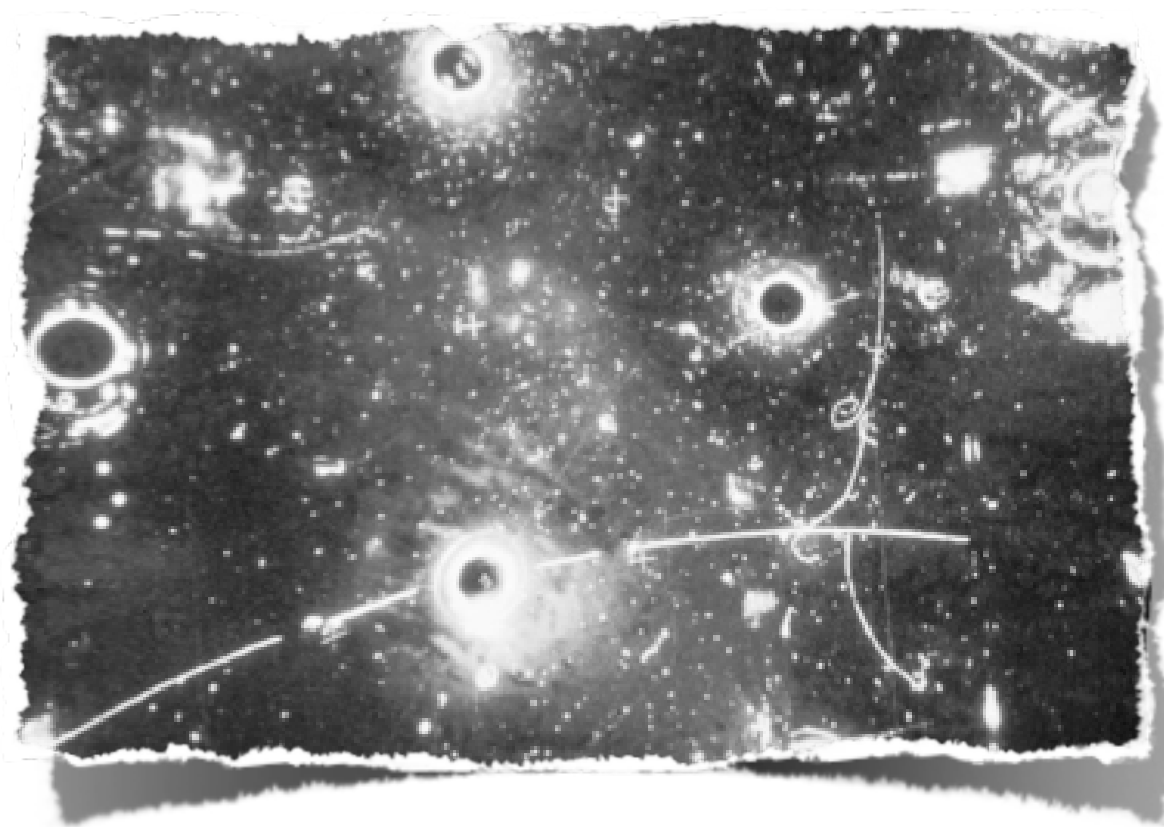
# Standard Model @ EW Symm. Breaking



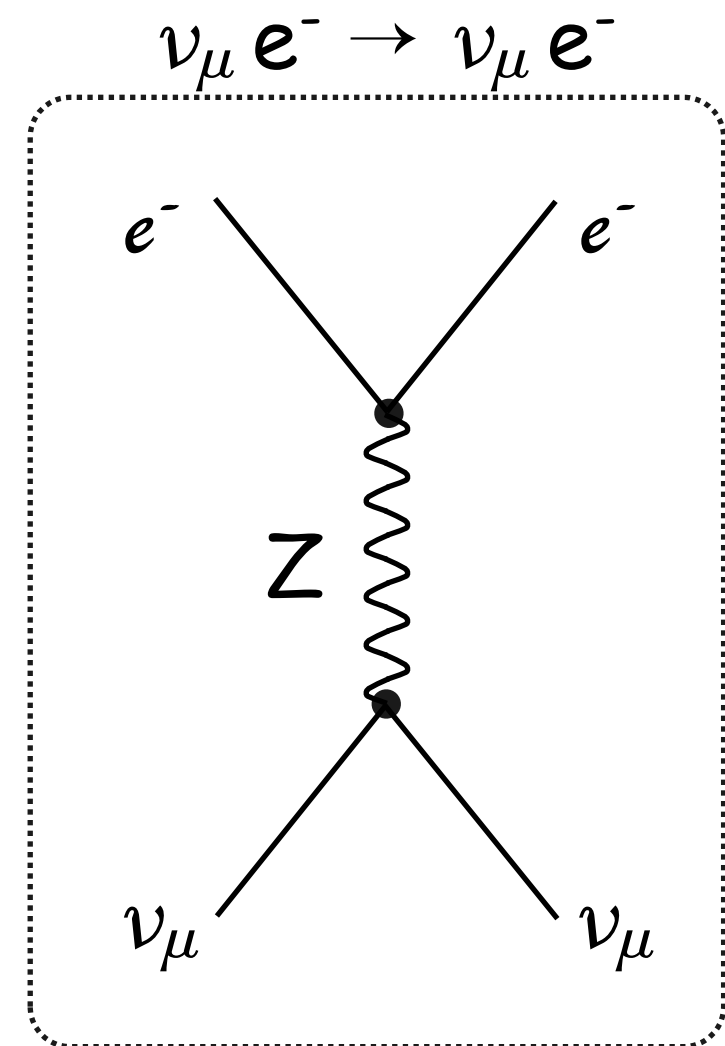
# The Standard Model

the strong, weak and electromagnetic interactions of the elementary particles are described by gauge interactions

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$



Gargamelle collaboration, '73

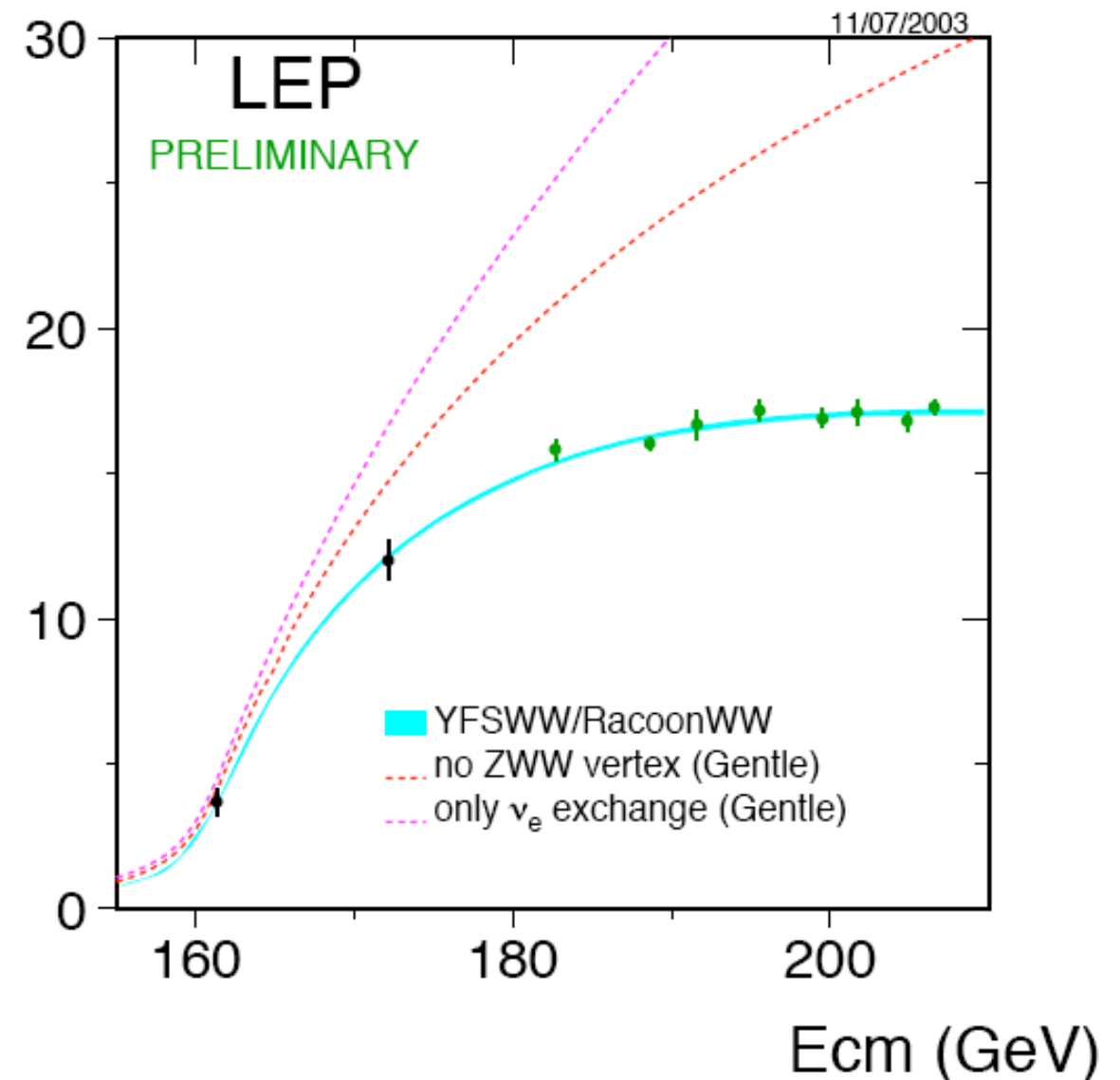
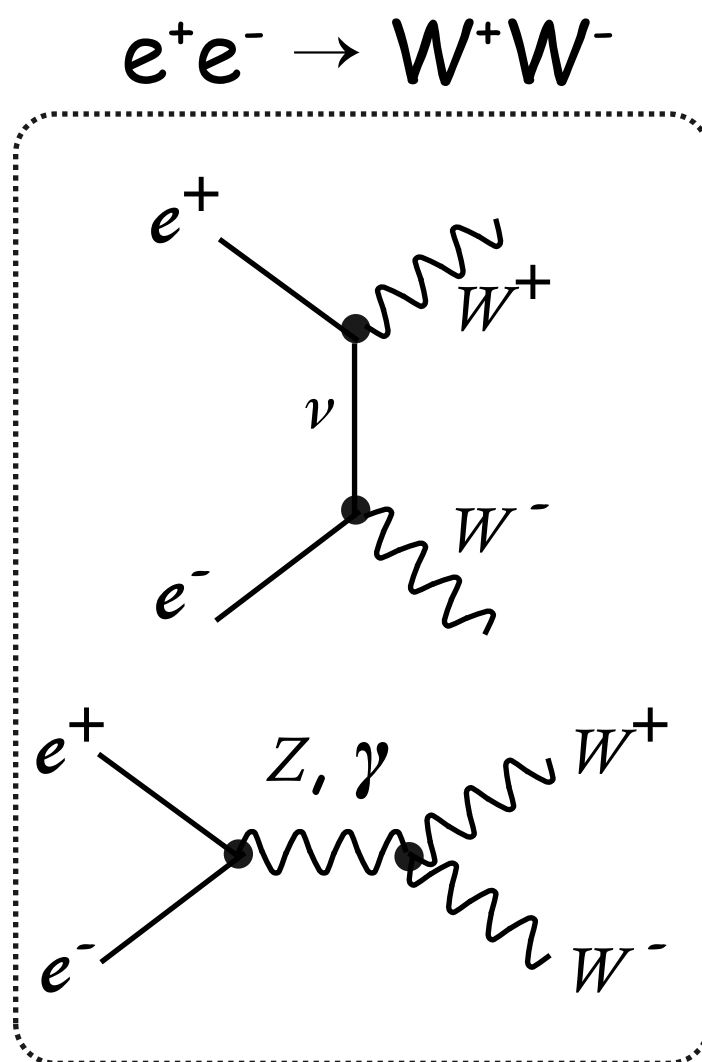




# The Standard Model

the strong, weak and electromagnetic interactions of the elementary particles are described by gauge interactions

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$





# The Standard Model and the Mass Problem

the strong, weak and electromagnetic interactions of the elementary particles are described by gauge interactions

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

the masses of the quarks, leptons and gauge bosons don't obey the full gauge invariance

✱  $\begin{pmatrix} \nu_e \\ e \end{pmatrix}$  is a doublet of  $SU(2)_L$  but  $m_{\nu_e} \ll m_e$

✱ a mass term for the gauge field isn't invariant under gauge transformation  $\delta A_\mu^a = \partial_\mu \epsilon^a + g f^{abc} A_\mu^b \epsilon^c$



spontaneous breaking of gauge symmetry



# The longitudinal polarization of massive W, Z



a massless particle is never at rest: always possible to distinguish (and eliminate!) the longitudinal polarization



the longitudinal polarization is physical for a massive spin-1 particle

(pictures: courtesy of G. Giudice)

symmetry breaking: new phase with more degrees of freedom

$$\epsilon_{\parallel} = \left( \frac{|\vec{p}|}{M}, \frac{E}{M} \frac{\vec{p}}{|\vec{p}|} \right) \text{ polarization vector grows with the energy}$$

# The longitudinal polarization of massive W, Z



a massless particle is never at rest: it is impossible to distinguish  
(and eliminate) the longitudinal polarization

$$3 = 2 + 1$$

Guralnik et al '64



the longitudinal polarization is physical for a massive spin-1 particle

(pictures: courtesy of G. Giudice)

symmetry breaking: new phase with more degrees of freedom

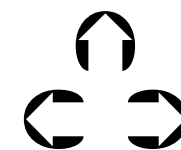
$$\epsilon_{\parallel} = \left( \frac{|\vec{p}|}{M}, \frac{E}{M} \frac{\vec{p}}{|\vec{p}|} \right) \text{ polarization vector grows with the energy}$$



[pictures: courtesy of NYT]

2

# *Higgs Mechanism. Custodial symmetry*



# Higgs Mechanism

Symmetry of the Lagrangian

$$SU(2)_L \times U(1)_Y$$

Higgs Doublet

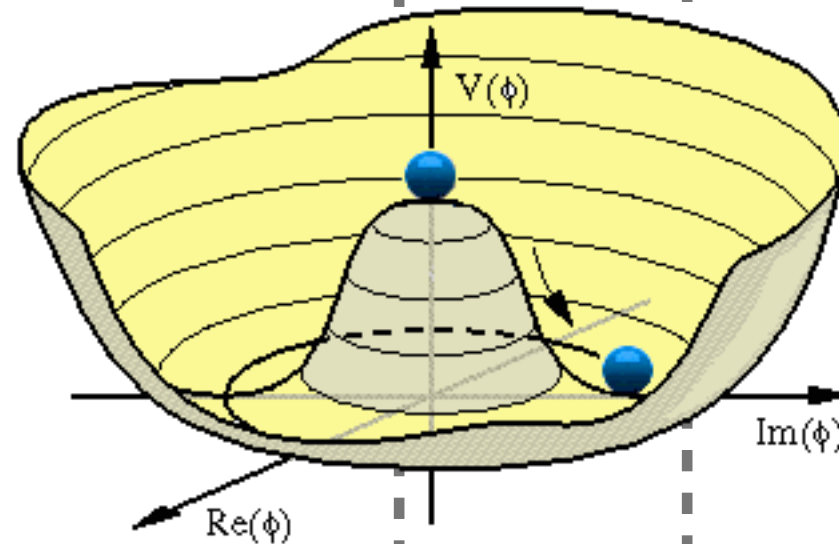
$$H = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix}$$

Symmetry of the Vacuum

$$U(1)_{e.m.}$$

Vacuum Expectation Value

$$\langle H \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix} \text{ with } v \approx 246 \text{ GeV}$$



$$D_\mu H = \partial_\mu H - \frac{i}{2} \begin{pmatrix} gW_\mu^3 + g'B_\mu & \sqrt{2}gW_\mu^+ \\ \sqrt{2}gW_\mu^- & -gW_\mu^3 + g'B_\mu \end{pmatrix} H \quad \text{with } W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \mp W_\mu^2)$$

$$|D_\mu H|^2 = \frac{1}{4} g^2 v^2 W_\mu^+ W^{-\mu} + \frac{1}{8} (W_\mu^3 B_\mu) \begin{pmatrix} g^2 v^2 & -gg'v^2 \\ -gg'v^2 & g'^2 v^2 \end{pmatrix} \begin{pmatrix} W^{3\mu} \\ B^\mu \end{pmatrix}$$

## ☛ Gauge boson spectrum

☛ electrically charged bosons

$$M_W^2 = \frac{1}{4} g^2 v^2$$

☛ electrically neutral bosons

$$Z_\mu = cW_\mu^3 - sB_\mu$$

$$\gamma_\mu = sW_\mu^3 + cB_\mu$$

Weak mixing angle

$$c = \frac{g}{\sqrt{g^2 + g'^2}}$$

$$s = \frac{g'}{\sqrt{g^2 + g'^2}}$$

$$M_Z^2 = \frac{1}{4} (g^2 + g'^2) v^2$$

$$M_\gamma = 0$$



# Custodial Symmetry

Sikivie et al, '80

## ❖ Rho parameter

$$\rho \equiv \frac{M_W^2}{M_Z^2 \cos^2 \theta_w} = \frac{\frac{1}{4} g^2 v^2}{\frac{1}{4} (g^2 + g'^2) v^2 \frac{g^2}{g^2 + g'^2}} = 1$$

## ❖ Consequence of an approximate global symmetry of the Higgs sector

$$H = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix} \quad \text{Higgs doublet} = 4 \text{ real scalar fields}$$

$$V(H) = \lambda \left( H^\dagger H - \frac{v^2}{2} \right)^2 \quad \text{is invariant under the rotation of the four real components}$$

$$SO(4) \sim SU(2)_L \times SU(2)_R$$

$$SU(2)_R$$



$$SU(2)_L \rightarrow (i\sigma^2 H^* \quad H) = \Phi$$

2x2 matrix

$$\Phi^\dagger \Phi = H^\dagger H \begin{pmatrix} 1 & \\ & 1 \end{pmatrix}$$

$$V(H) = \frac{\lambda}{4} (\text{tr} \Phi^\dagger \Phi - v^2)^2$$

explicitly invariant under  $SU(2)_L \times SU(2)_R$

# Custodial Symmetry

Sikivie et al, '80

Higgs vev

$$\langle H \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix} \quad \langle \Phi \rangle = \frac{v}{\sqrt{2}} \begin{pmatrix} 1 & \\ & 1 \end{pmatrix}$$

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

unbroken symmetry in the broken phase

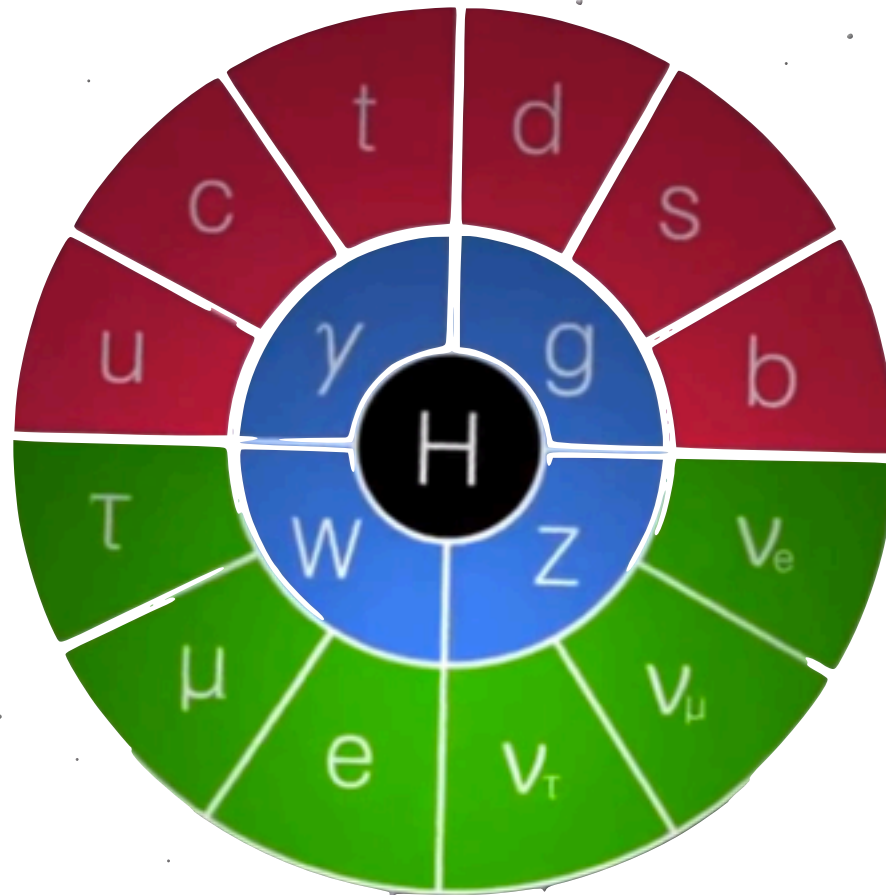
$(W_\mu^1, W_\mu^2, W_\mu^3)$  transforms as a triplet

$$(Z_\mu \gamma_\mu) \begin{pmatrix} M_Z^2 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} Z^\mu \\ \gamma^\mu \end{pmatrix} = (W_\mu^3 B_\mu) \begin{pmatrix} c^2 M_Z^2 & -cs M_Z^2 \\ -cs M_Z^2 & s^2 M_Z^2 \end{pmatrix} \begin{pmatrix} W^{3\mu} \\ B^\mu \end{pmatrix}$$

The  $SU(2)_V$  symmetry imposes the same mass term for all  $W^i$  thus  $c^2 M_Z^2 = M_W^2$

$$\rho = 1$$

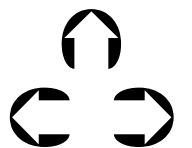
The hypercharge gauge coupling and the Yukawa couplings break the custodial  $SU(2)_V$ , which will generate a (small) deviation to  $\rho = 1$  at the quantum level.



3

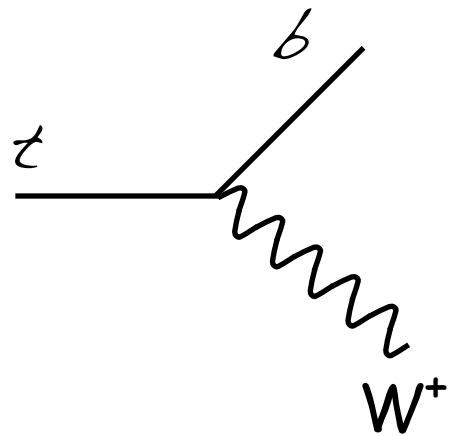
# Goldstone equivalence theorem

[pictures: courtesy of D.E. Kaplan  
@ particle fever]



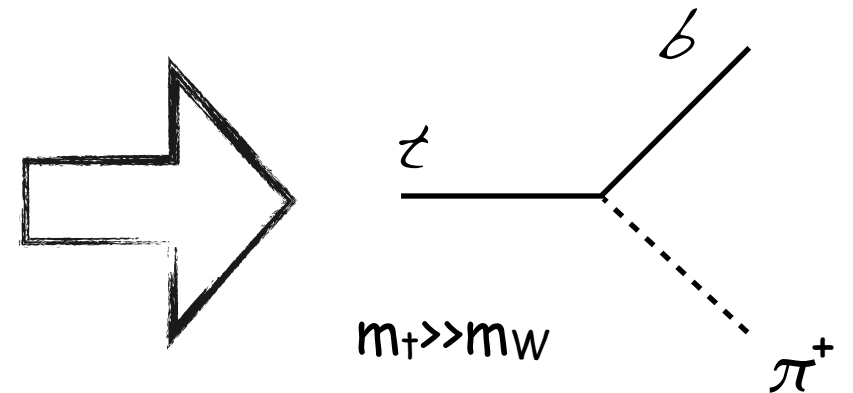
# The BEH mechanism: "V<sub>L</sub>=Goldstone bosons"

At high energy, the physics of the gauge boson becomes simple



$$\Gamma(t \rightarrow b W_L) = \frac{g^2}{64\pi} \frac{m_t^2}{m_W^2} \frac{(m_t^2 - m_W^2)^2}{m_t^3}$$

$$\Gamma(t \rightarrow b W_T) = \frac{g^2}{64\pi} \frac{2(m_t^2 - m_W^2)^2}{m_t^3}$$



democratic decay at threshold

at high energy ( $m_t \gg m_W$ ),  $W_L$  dominates the decay

Goldstone equivalence theorem  
 $W_L^\pm, Z_L \approx SO(4)/SO(3)$

LEP already established the BEH mechanism

The pending question was: how it is realized?

Via a fundamental EW doublet? A la technicolor?

Is there a Higgs boson in addition to the 3 Goldstone bosons?

In other words, LEP established a simple description of EWSB in the energy range

$$m_W \ll E \ll 4\pi v = \frac{8\pi m_W}{g}$$

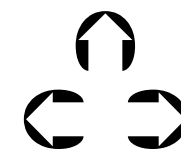
The goal of the LHC was/is to understand what comes next



[pictures: courtesy of I. Low]



*What is the SM Higgs boson?*





# The UV behavior of the weak Goldstone

symmetry breaking: new phase with more degrees of freedom

massive  $W^\pm, Z$ : 3 physical polarizations=eaten Goldstone bosons  $\frac{SU(2)_L \times SU(2)_R}{SU(2)_V}$

$\Rightarrow$  UV behavior of these Goldstone's?  $\Leftarrow$

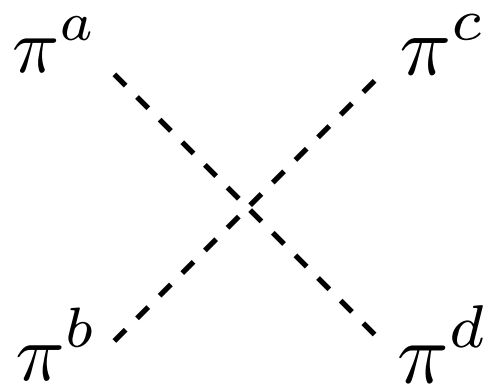
$$\mathcal{L}_{\text{mass}} = m_W^2 W_\mu^+ W^{\mu-} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma)$$

$\Sigma = e^{i\sigma^a \pi^a / v}$   
Goldstone of  
 $SU(2)_L \times SU(2)_R / SU(2)_V$

$$\mathcal{L}_{\text{mass}} = \frac{1}{2} (\partial_\mu \pi^a)^2 - \frac{1}{6v^2} ((\pi^a \partial_\mu \pi^a)^2 - (\pi^a)^2 (\partial_\mu \pi^a)^2) + \dots$$

contact interaction growing with energy

$$\mathcal{A}(\pi^a \pi^b \rightarrow \pi^c \pi^d) = \mathcal{A}(s, t, u) \delta^{ab} \delta^{cd} + \mathcal{A}(t, s, u) \delta^{ac} \delta^{bd} + \mathcal{A}(u, t, s) \delta^{ad} \delta^{bc}$$



$$\mathcal{A}(s, t, u) = \frac{s}{v^2} \quad \text{Weinberg's LET}$$

the behavior of this amplitude is not consistent above  $4\pi v$  ( $\approx 1\div 3 \text{ TeV}$ )

Lee, Quigg & Thacker '77

# A QCD antecedent

QCD pions are Goldstone bosons associated to  $SU(2)_L \times SU(2)_R / SU(2)_V$

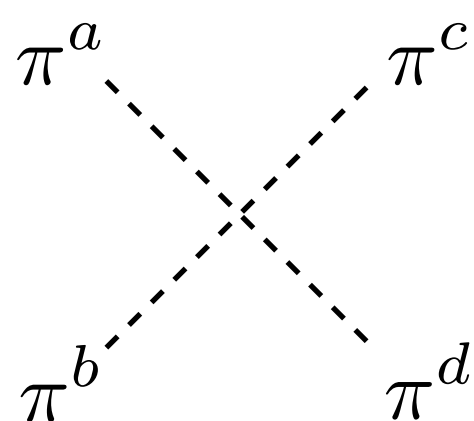


$$U = e^{i\pi^a \sigma^a / f_\pi} \begin{pmatrix} 0 \\ \frac{f_\pi}{\sqrt{2}} \end{pmatrix}$$

kinetic terms for  $U \Leftrightarrow$  interaction terms for  $\pi^a$

$$\mathcal{L} = |\partial_\mu U|^2 = \frac{1}{2}(\partial_\mu \pi^a)^2 - \frac{1}{6f_\pi^2} \left( (\pi^a \partial_\mu \pi^a)^2 - (\pi^a)^2 (\partial_\mu \pi^a)^2 \right) + \dots$$

contact interaction growing with energy



$$\mathcal{A}(\pi^a \pi^b \rightarrow \pi^c \pi^d) = \mathcal{A}(s, t, u) \delta^{ab} \delta^{cd} + \mathcal{A}(t, s, u) \delta^{ac} \delta^{bd} + \mathcal{A}(u, t, s) \delta^{ad} \delta^{bc}$$

$$\mathcal{A}(s, t, u) = \frac{s}{f_\pi^2}$$

$$f_\pi = 93 \text{ MeV}$$



unitarity bound

$$\sqrt{s} \sim 4\sqrt{\pi} f_\pi = 660 \text{ MeV}$$

rho meson ( $m=770 \text{ MeV}$ ) is restoring unitarity

# Longitudinal polarization of a massive spin 1



a massive  
spin 1 particle has  
3 physical polarizations:

$$A_\mu = \epsilon_\mu e^{ik_\mu x^\mu}$$

$$\epsilon^\mu \epsilon_\mu = -1 \quad k^\mu \epsilon_\mu = 0$$

$$k^\mu = (E, 0, 0, k)$$

$$\text{with } k_\mu k^\mu = E^2 - k^2 = M^2$$

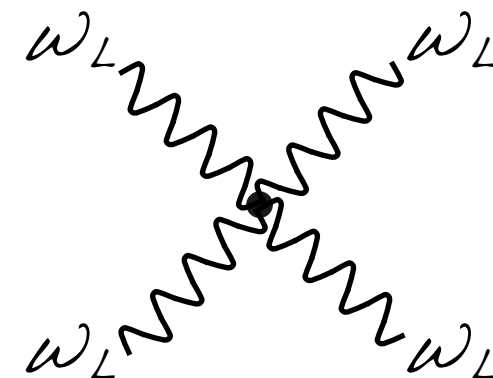
✖ 2 transverse:

$$\begin{cases} \epsilon_1^\mu = (0, 1, 0, 0) \\ \epsilon_2^\mu = (0, 0, 1, 0) \end{cases}$$

✖ 1 longitudinal:  $\epsilon_\parallel^\mu = (\frac{k}{M}, 0, 0, \frac{E}{M}) \approx \frac{k^\mu}{M} + \mathcal{O}(\frac{E}{M})$

( in the R- $\xi$  gauge, the time-like polarization ( $\epsilon^\mu \epsilon_\mu = 1 \quad k^\mu \epsilon_\mu = M$ ) is arbitrarily massive and decouple )

Bad UV behavior for  
the scattering of the longitudinal  
polarizations

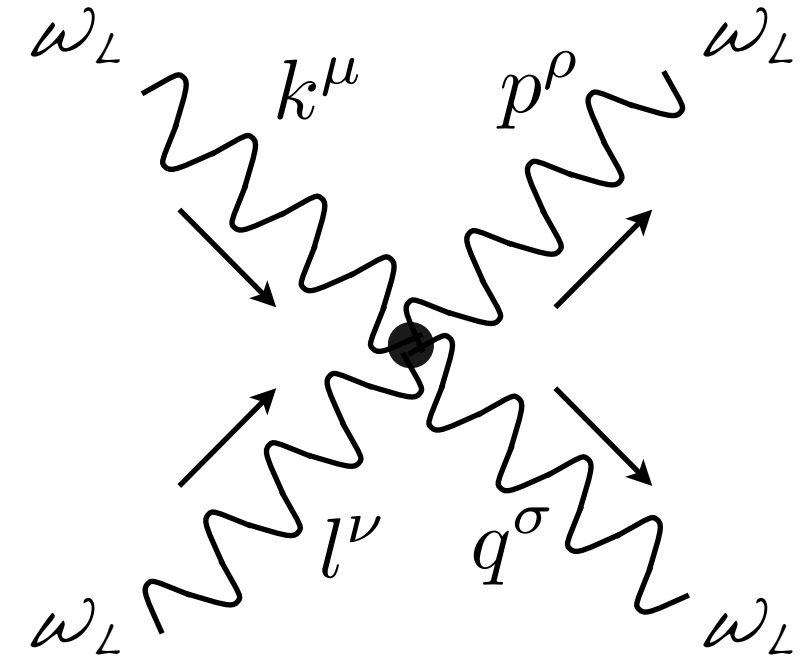


# Why do we need a Higgs ?

## NO LOSE THEOREM

The W and Z masses are inconsistent with the known particle content! Need more particles to soften the UV behavior of massive gauge bosons.

Bad UV behavior for the scattering of the longitudinal polarizations

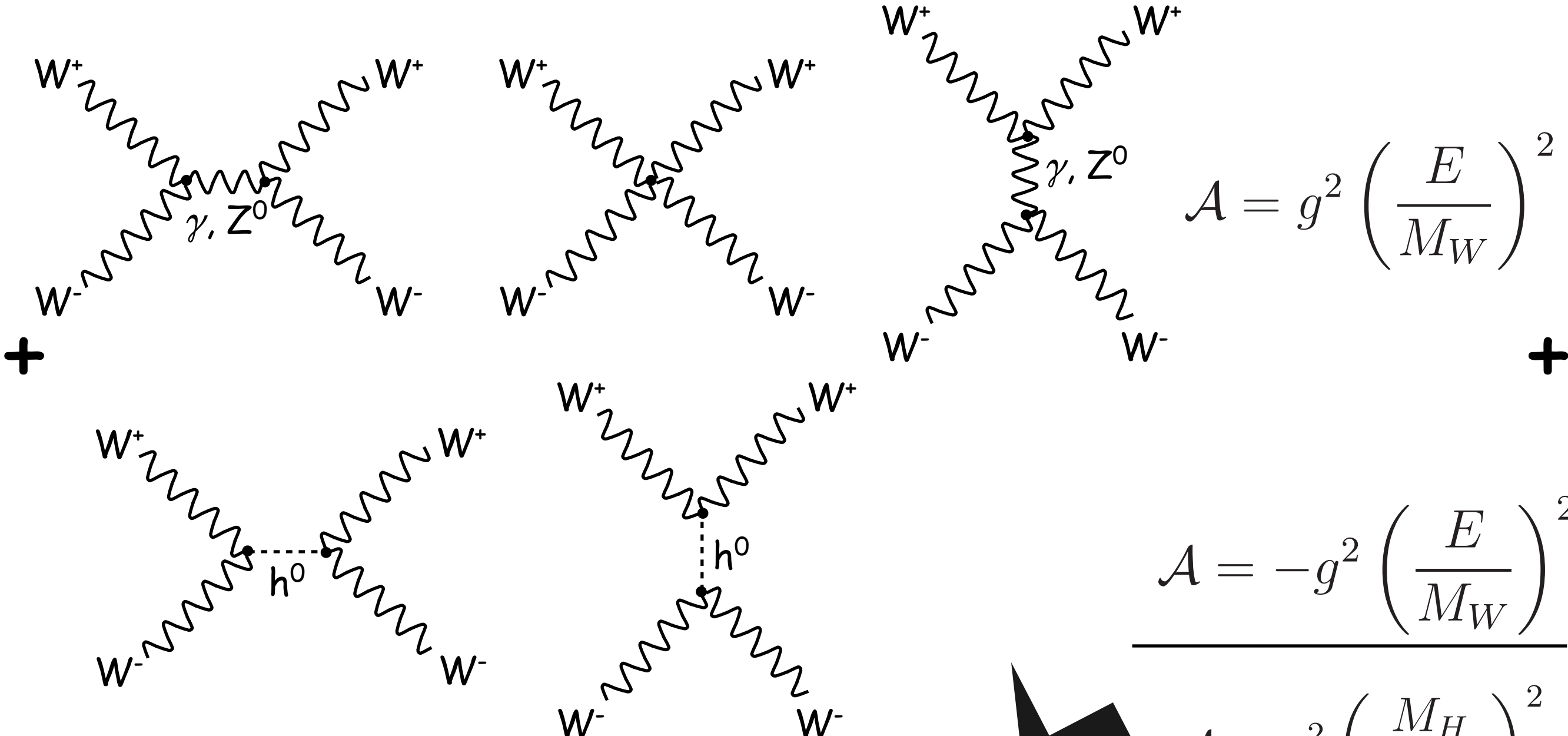


$$\mathcal{A} = \epsilon_{||}^{\mu}(k) \epsilon_{||}^{\nu}(l) i g^2 (2 \eta_{\mu\rho} \eta_{\nu\sigma} - \eta_{\mu\nu} \eta_{\rho\sigma} - \eta_{\mu\sigma} \eta_{\nu\rho}) \epsilon_{||}^{\rho}(p) \epsilon_{||}^{\sigma}(q)$$

$$\mathcal{A} = g^2 \frac{E^4}{4M_W^4}$$

violations of perturbative unitarity around  $E \sim M$

# Why do we need a Higgs ?



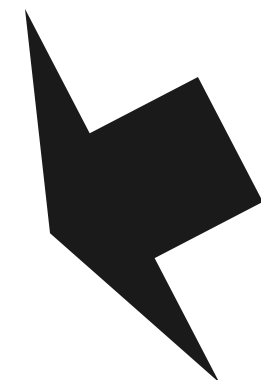
$$\mathcal{A} = g^2 \left( \frac{E}{M_W} \right)^2$$

$$\mathcal{A} = -g^2 \left( \frac{E}{M_W} \right)^2$$

$$\mathcal{A} = g^2 \left( \frac{M_H}{2M_W} \right)^2$$

The Higgs boson unitarize the W scattering  
(if its mass is below  $\sim 1$  TeV)

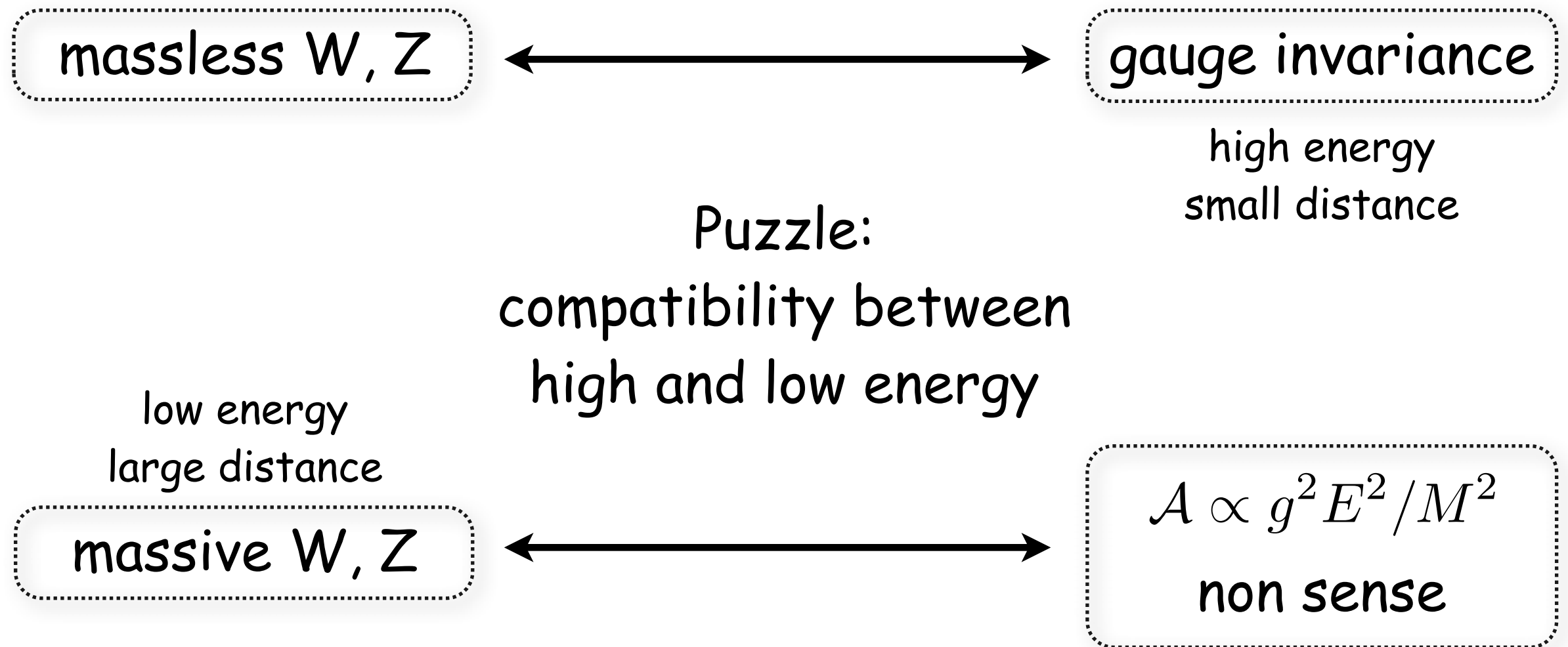
$W_L$  scattering = pion scattering  
Goldstone equivalence theorem



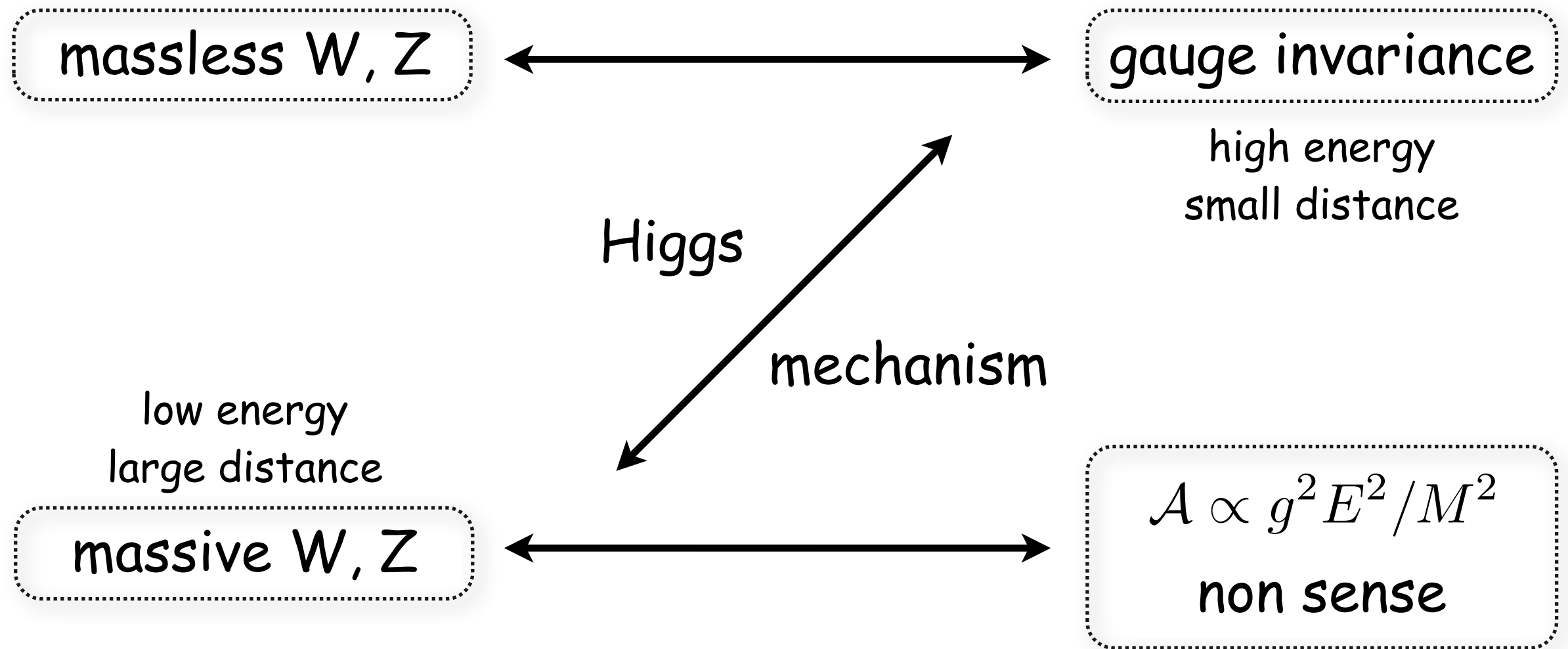
Lewellyn Smith '73  
Dicus, Mathur '73  
Cornwall, Levin, Tiktopoulos '73  
Lee, Quigg, Thacker '77



# Higgs as UV moderator



# Higgs as UV moderator





# Unitarity Bound

Lee, Quigg, Thacker '77  
Chanowitz, Gaillard '85

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 s} |\mathcal{A}|^2$$

Partial wave amplitude decomposition:

$$\mathcal{A} = 16\pi \sum_{l=0}^{\infty} (2l+1) P_l(\cos \theta) a_l$$

$$a_l = \frac{1}{32\pi} \int_{-1}^{+1} d(\cos \theta) P_l(\cos \theta) \mathcal{A}$$

$$\sigma = \frac{16\pi}{s} \sum_{l=0}^{\infty} (2l+1) |a_l|^2$$

$$P_0(x) = 1, P_1(x) = x, P_2(x) = 3x^2/2 - 1/2 \dots$$

$$\int_{-1}^1 dx P_l(x) P_{l'}(x) = \frac{2}{2l+1} \delta_{ll'}$$

Optical theorem:

$$\sigma = \text{Im} (\mathcal{A}|_{\theta=0}) / s \quad \Rightarrow \quad \text{Im} (a_l) = |a_l|^2 \quad \Rightarrow \quad (\text{Im} (a_l) - 1/2)^2 + (\text{Re} (a_l))^2 = 1/4$$

$$|\text{Re} (a_l)| \leq 1/2$$

$$W^+ W^- \rightarrow W^+ W^-$$

$$\mathcal{A} = \mathcal{A}(s) + \mathcal{A}(t)$$

SM without a Higgs

$$\mathcal{A}(s) = s/v^2$$

$$a_0 = \frac{s}{8\pi v^2}$$



$$\sqrt{s} = 2E \leq 4\sqrt{\pi}v \approx 1.7 \text{ TeV}$$

SM with a Higgs

$$\mathcal{A}(s) = (s - s^2/(s - m_h^2))/v^2$$

$$a_0 = \frac{m_h^2}{16\pi v^2}$$



$$m_h \leq 2\sqrt{2}\pi v \approx 1.2 \text{ TeV}$$

**Stronger Bound**

$2W^+W^- + ZZ$  scattering

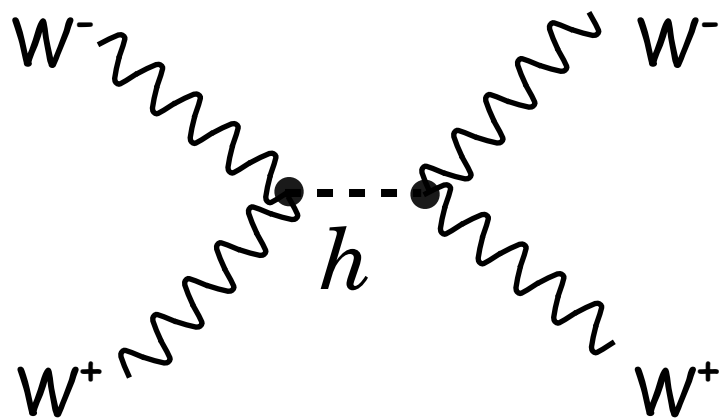
$$m_h \leq 4\sqrt{\pi/3}v \approx 1.0 \text{ TeV}$$

# What is the Higgs the name of?

A single scalar degree of freedom neutral under  $SU(2)_L \times SU(2)_R / SU(2)_V$

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

'a', 'b' and 'c' are arbitrary free couplings



$$\mathcal{A} = \frac{1}{v^2} \left( s - \frac{a^2 s^2}{s - m_h^2} \right)$$

growth cancelled for  
 $a = 1$   
restoration of  
perturbative unitarity

Cornwall, Levin, Tiktopoulos '73

Contino, Grojean, Moretti, Piccinini, Rattazzi '10

$$\Sigma = e^{i\sigma^a \pi^a / v}$$

Goldstone of  $SU(2)_L \times SU(2)_R / SU(2)_V$

$$D_\mu \Sigma \approx W_\mu$$

# What is the Higgs the name of?

A single scalar degree of freedom neutral under  $SU(2)_L \times SU(2)_R / SU(2)_V$

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

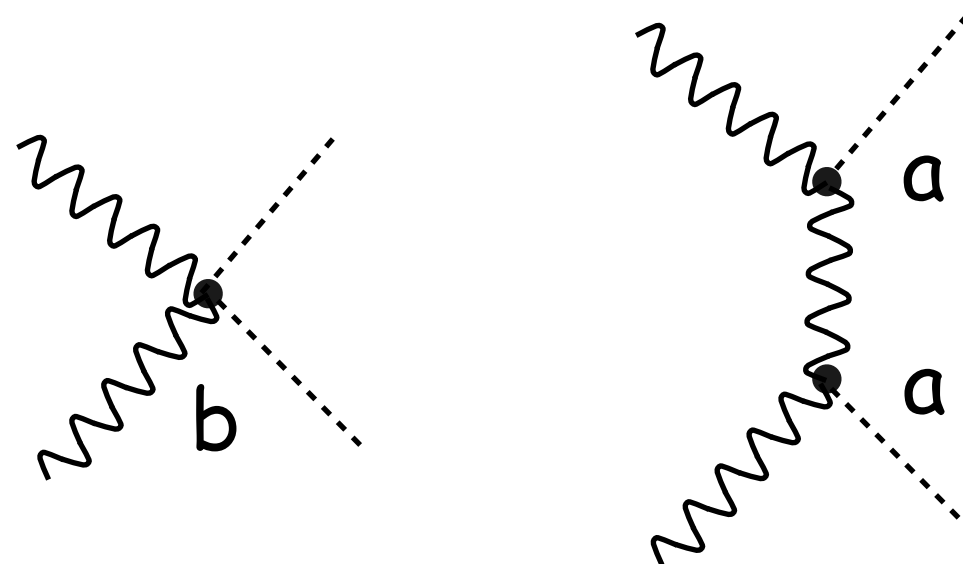
'a', 'b' and 'c' are arbitrary free couplings

For  $a=1$ : perturbative unitarity in elastic channels  $WW \rightarrow WW$

For  $b = a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

Cornwall, Levin, Tiktopoulos '73

Contino, Grojean, Moretti, Piccinini, Rattazzi '10





# What is the Higgs the name of?

A single scalar degree of freedom neutral under  $SU(2)_L \times SU(2)_R / SU(2)_V$

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

'a', 'b' and 'c' are arbitrary free couplings

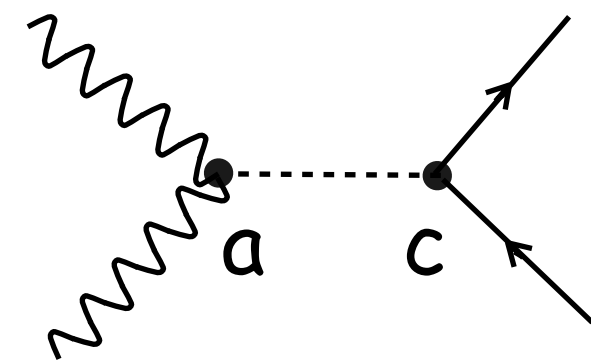
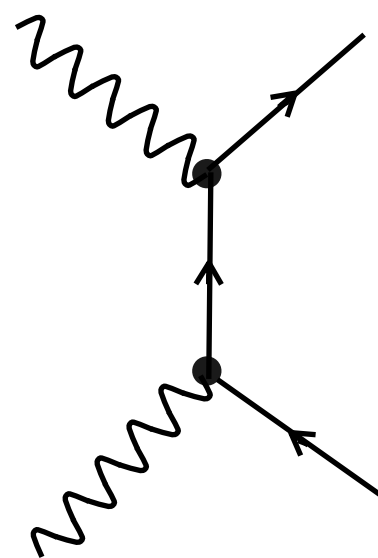
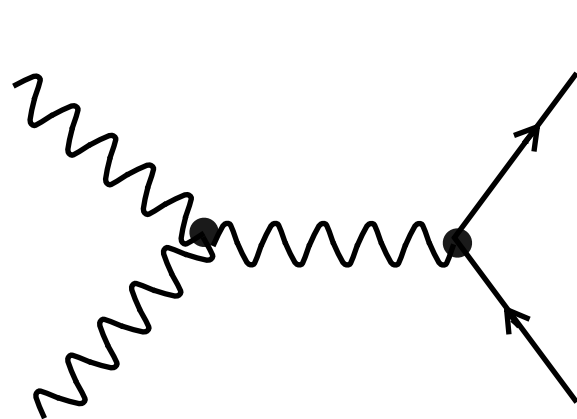
For  $a=1$ : perturbative unitarity in elastic channels  $WW \rightarrow WW$

For  $b = a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

For  $ac=1$ : perturbative unitarity in inelastic  $WW \rightarrow \psi \psi$

Cornwall, Levin, Tiktopoulos '73

Contino, Grojean, Moretti, Piccinini, Rattazzi '10



# What is the Higgs the name of?

A single scalar degree of freedom neutral under  $SU(2)_L \times SU(2)_R / SU(2)_V$

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

'a', 'b' and 'c' are arbitrary free couplings

For  $a=1$ : perturbative unitarity in elastic channels  $WW \rightarrow WW$

For  $b = a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

For  $ac=1$ : perturbative unitarity in inelastic  $WW \rightarrow \psi \psi$

'a=1', 'b=1' & 'c=1' define the SM Higgs

Higgs properties are fixed once all masses are known (including  $m_H$ ):

$$\mathcal{L}_{\text{EWSB}} \text{ can be rewritten as } D_\mu H^\dagger D_\mu H$$

$$H = \frac{1}{\sqrt{2}} e^{i\sigma^a \pi^a / v} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

$h$  and  $\pi^a$  (ie  $W_L$  and  $Z_L$ ) combine to form a linear representation of  $SU(2)_L \times U(1)_Y$

# What is the Higgs the name of?

The SM Higgs couplings are fixed to restore unitarity with mass

$$\Sigma = e^{i\sigma^a \pi^a / v} \quad \text{Goldstone of } SU(2)_L \times SU(2)_R / SU(2)_V \quad D_\mu \Sigma = g V_\mu$$

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

'a', 'b' and 'c' are arbitrary free couplings

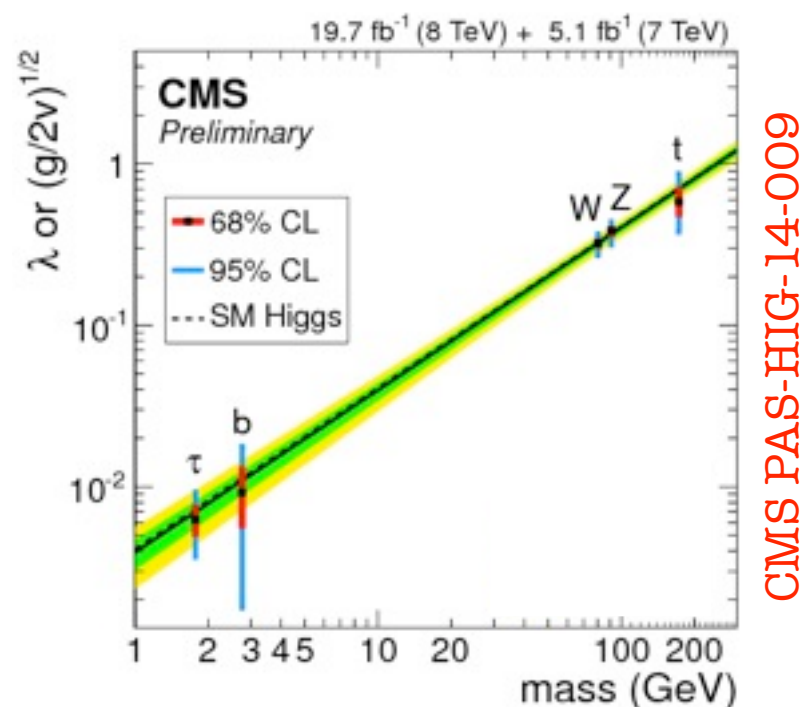
For  $a=1$ : perturbative unitarity in elastic channels  $WW \rightarrow WW$

For  $b=a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

For  $ac=1$ : perturbative unitarity in inelastic  $WW \rightarrow \psi \psi$

Cornwall, Levin, Tiktopoulos '73

Contino, Grojean, Moretti, Piccinini, Rattazzi '10

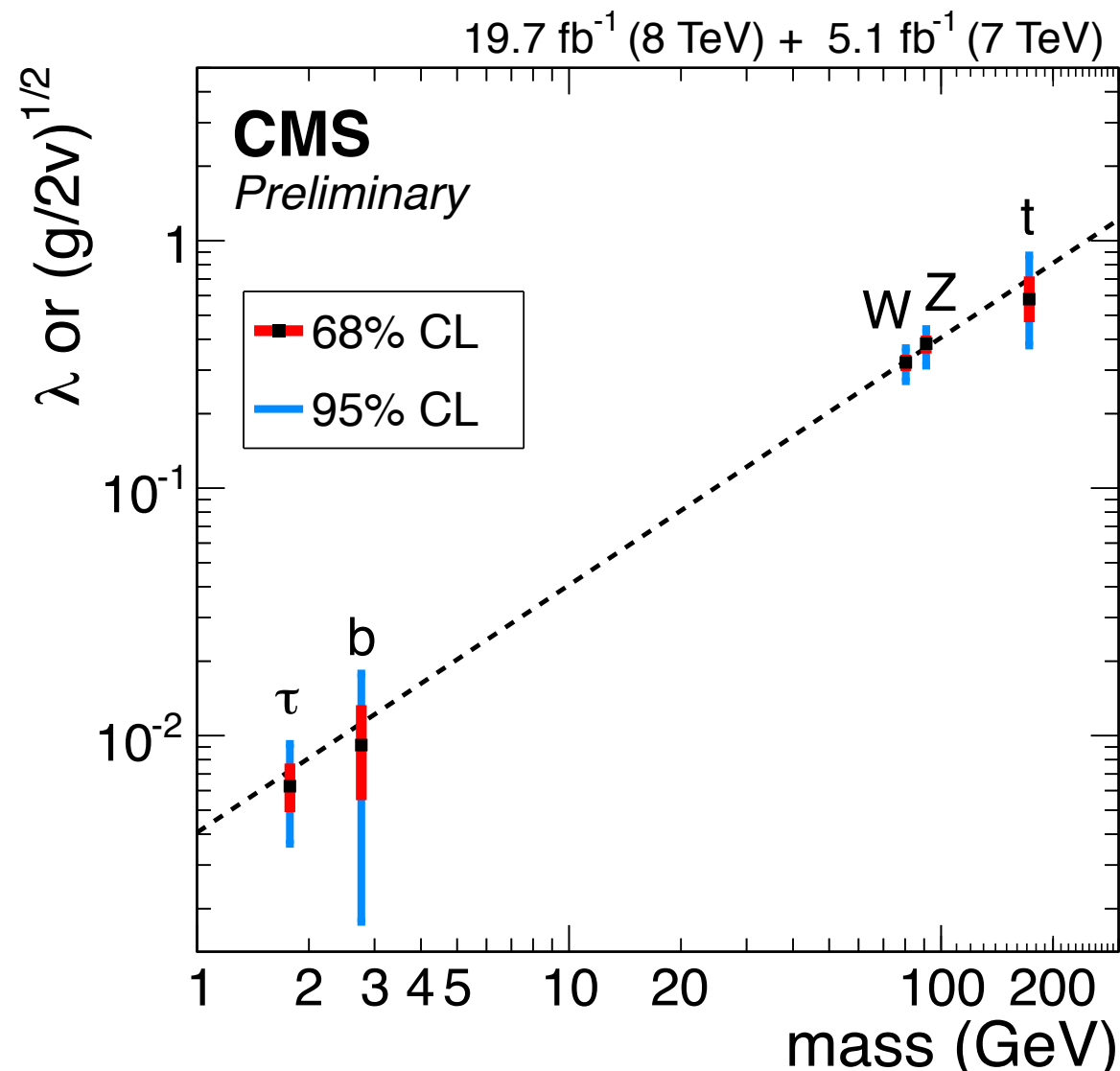


Higgs couplings  
are proportional  
to the masses of the particles

$$\lambda_\psi \propto \frac{m_\psi}{v}, \quad \lambda_V^2 \equiv \frac{g_{VVh}}{2v} \propto \frac{m_V^2}{v^2}$$

# What is the Higgs the name of?

The SM Higgs couplings are fixed to restore unitarity with mass



Higgs group @ Snowmass '13

Facility	LHC	HL-LHC
$\sqrt{s}$ (GeV)	14,000	14,000
$\int \mathcal{L} dt$ (fb <sup>-1</sup> )	300/expt	3000/expt
$\kappa_\gamma$	5 – 7%	2 – 5%
$\kappa_g$	6 – 8%	3 – 5%
$\kappa_W$	4 – 6%	2 – 5%
$\kappa_Z$	4 – 6%	2 – 4%
$\kappa_\ell$	6 – 8%	2 – 5%
$\kappa_d = \kappa_b$	10 – 13%	4 – 7%
$\kappa_u = \kappa_t$	14 – 15%	7 – 10%

~ Is this fit theoretically consistent? ~

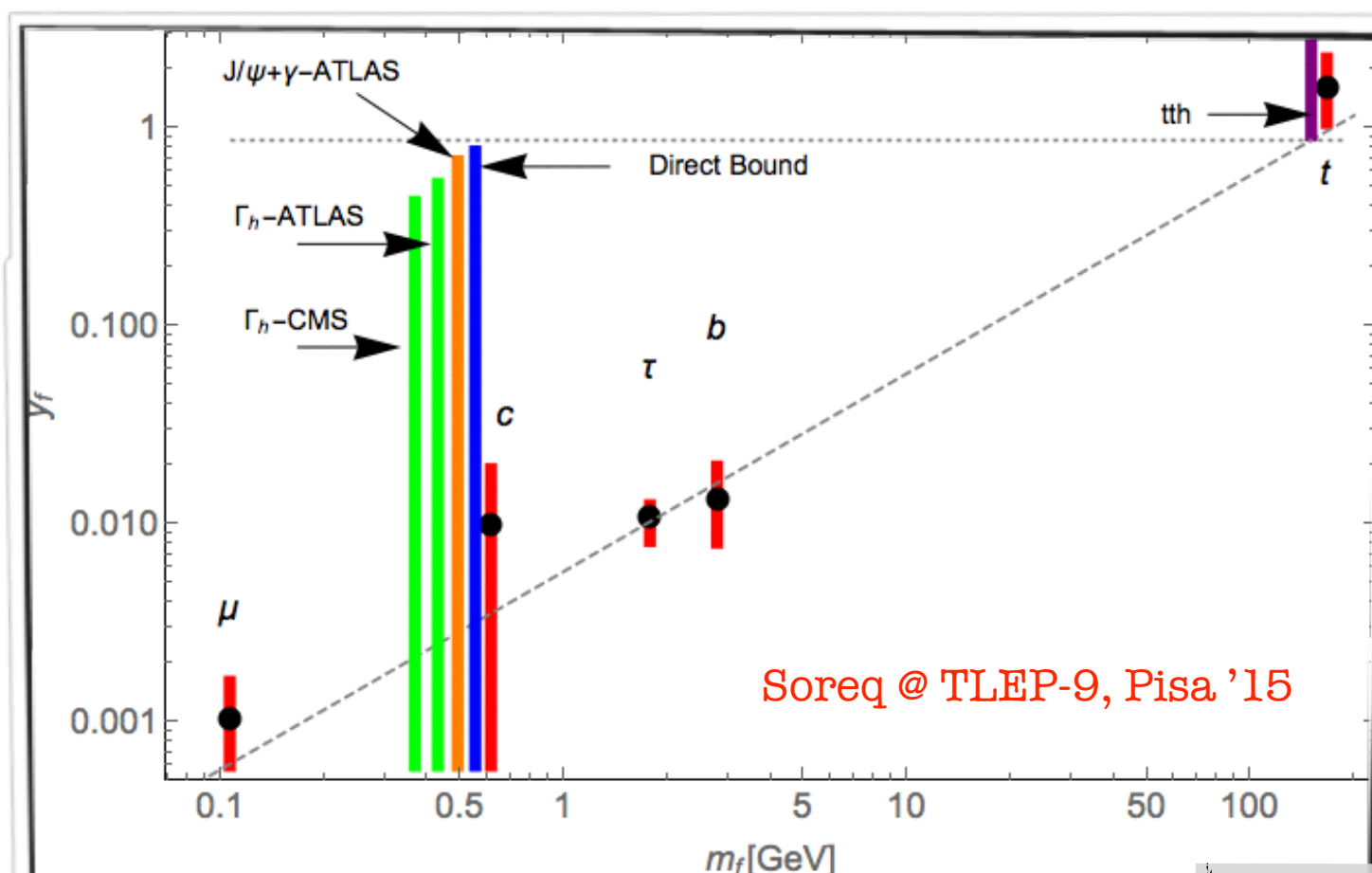
can you generate a 500% deviations

in the bottom coupling without generating other coupling

structures not taken into account in the fit?

# What is the Higgs the name of?

The SM Higgs couplings are fixed to restore unitarity with mass



Higgs group @ Snowmass '13

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$\kappa_d = \kappa_b$	10 – 13%	4 – 7%
$\kappa_u = \kappa_t$	14 – 15%	7 – 10%

missing information to complete the picture

◦ width measurement?

◦ couplings to light particles?

inclusive (e.g. c-tagging) or exclusive ( $h \rightarrow J/\Psi + \gamma$ )

◦ coupling to top?

known indirectly ( $gg \rightarrow h$ ) or via difficult  $tth$  channel

~ Is this fit theoretically consistent? ~

can you generate a 500% deviations

in the bottom coupling without generating other coupling structures not taken into account in the fit?



# Higgs and Flavor

In SM, the Yukawa interactions are the only source of the fermion masses

$$y_{ij} \bar{f}_{L_i} H f_{R_j} = \frac{y_{ij} v}{\sqrt{2}} \bar{f}_{L_i} f_{R_j} + \frac{y_{ij}}{\sqrt{2}} h \bar{f}_{L_i} f_{R_j}$$

mass

higgs-fermion interactions

both matrices are simultaneously diagonalizable

no tree-level Flavor Changing Current induced by the Higgs

Not true anymore if the SM fermions mix with vector-like partners<sup>(\*)</sup> or for non-SM Yukawa

$$y_{ij} \left( 1 + c_{ij} \frac{|H|^2}{f^2} \right) \bar{f}_{L_i} H f_{R_j} = \frac{y_{ij} v}{\sqrt{2}} \left( 1 + c_{ij} \frac{v^2}{2f^2} \right) \bar{f}_{L_i} f_{R_j} + \left( 1 + 3c_{ij} \frac{v^2}{2f^2} \right) \frac{y_{ij}}{\sqrt{2}} h \bar{f}_{L_i} f_{R_j}$$

Look for SM forbidden Flavor Violating decays  $h \rightarrow \mu\tau$  and  $t \rightarrow hc$

- weak indirect constrained by flavor data (e.g.  $\mu \rightarrow e\gamma$ ): BR < 10% Blankenburg, Ellis, Isidori '12
  - ATLAS and CMS have the sensitivity to set bounds O(1%) Harnik et al '12
  - ILC/CLIC/FCC-ee can certainly do much better Davidson, Verdier '12
- CMS-PAS-HIG-2014-005

(\*) e.g. Buras, Grojean, Pokorski, Ziegler '11

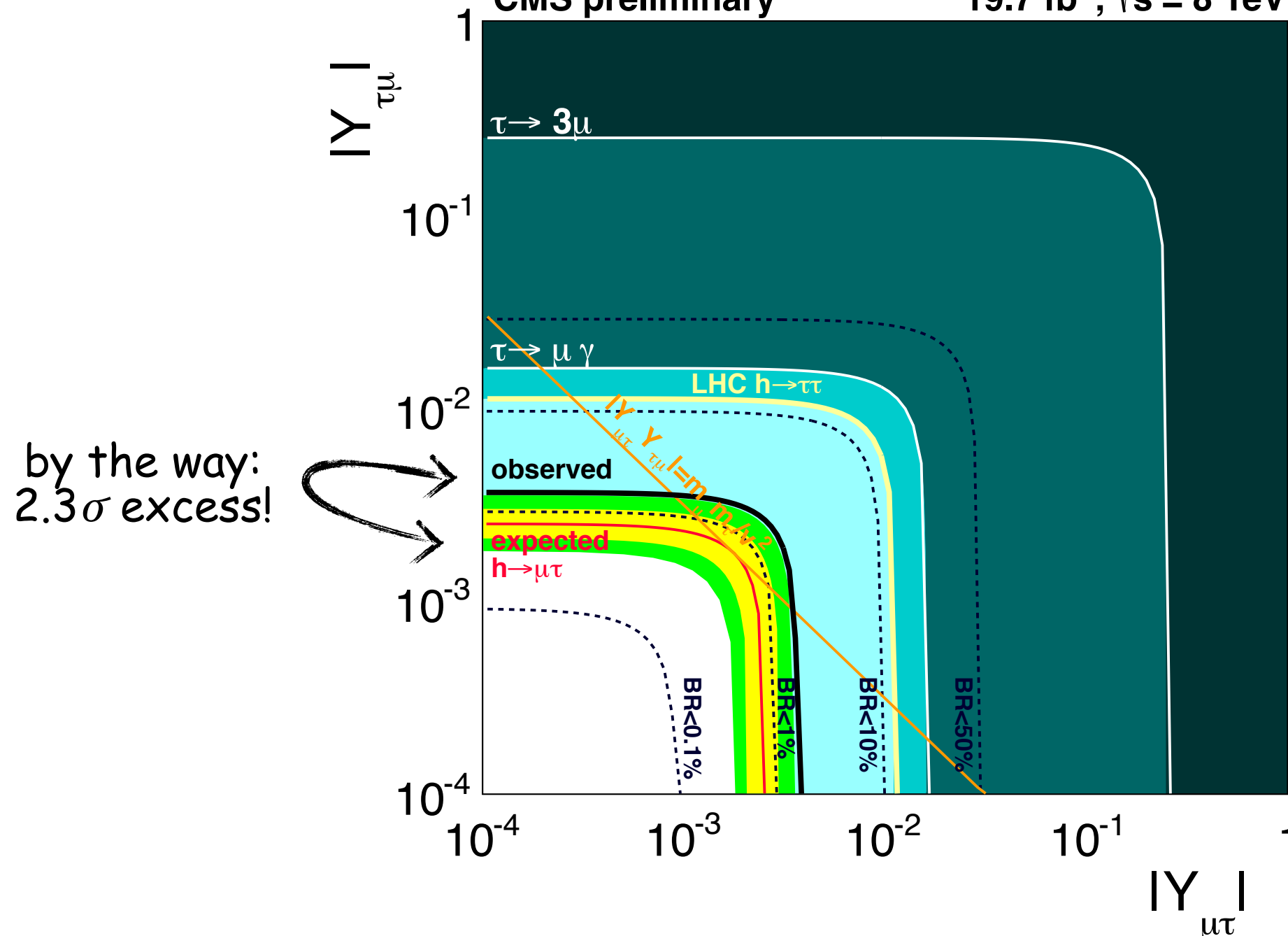
# Higgs and Flavor

In SM, the Yukawa interactions are the only source of the fermion masses

CMS-PAS-HIG-2014-005

CMS preliminary

19.7 fb<sup>-1</sup>,  $\sqrt{s} = 8$  TeV



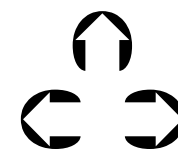
Off-diagonal Higgs couplings can reveal the origin of flavor

The interesting models of flavor ( $Y_{ij} \approx \sqrt{m_i m_j}/v^2$ ) start being probed by the experimental data



5

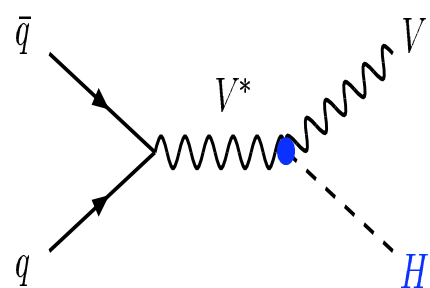
# *SM Higgs @ colliders*



# (SM) Higgs Production

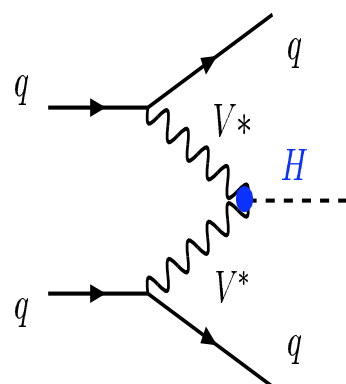
(see for instance A. Djouadi, hep-ph/0503172)

## Higgs-strahlung



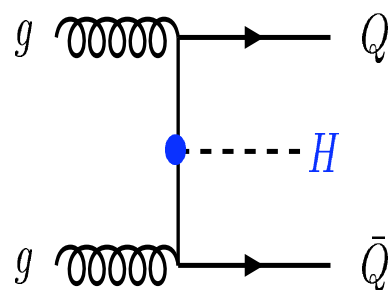
$\propto 1/s$ : Tevatron, ~~LHC~~

## Vector boson fusion

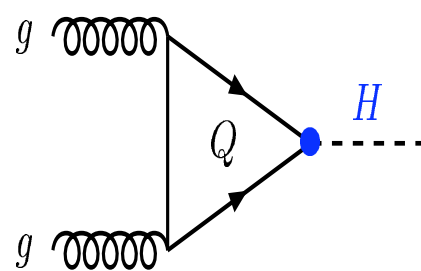


forward jet tagging  
central jet veto  
small hadronic activity

## QQ associated production

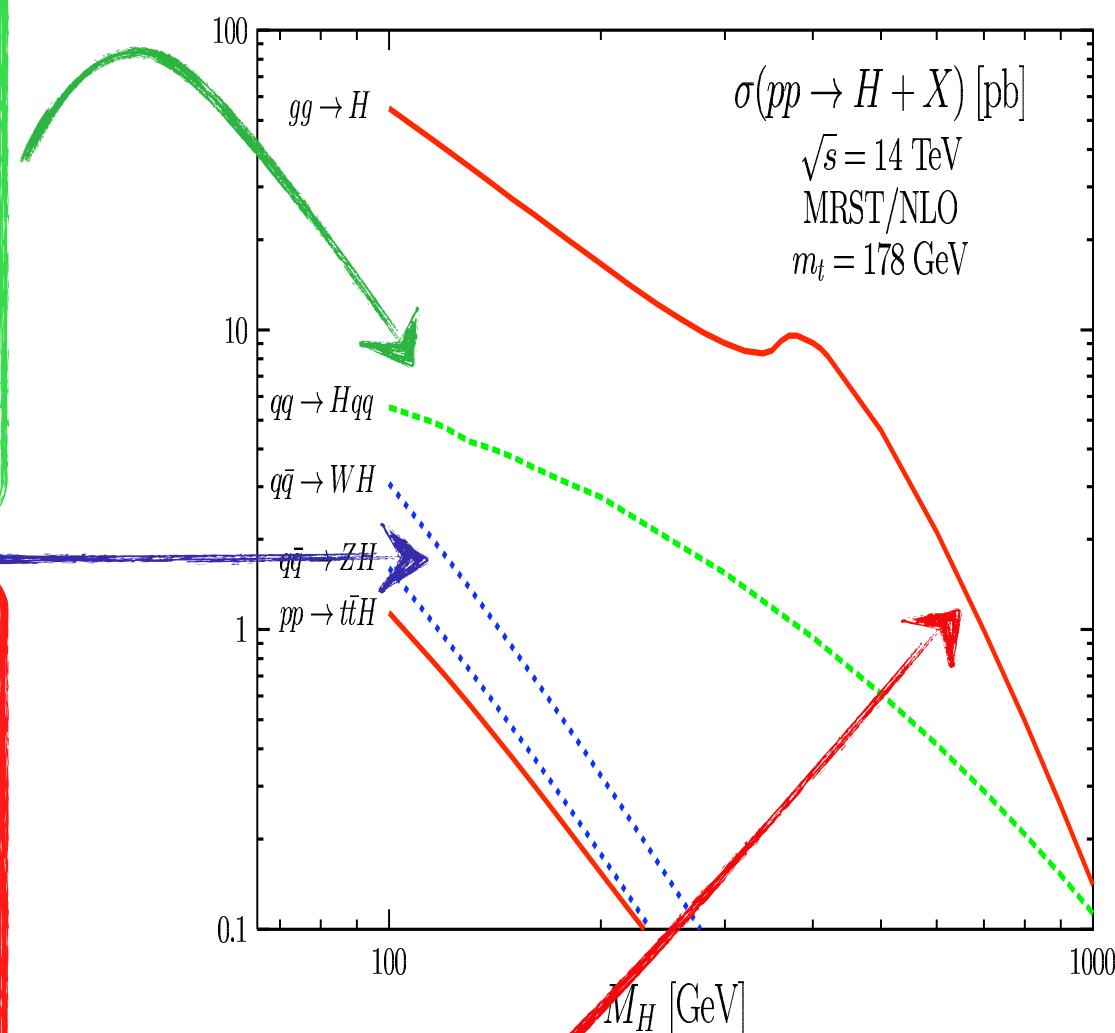


## Gluon fusion



single final state  
large NLO enhancement

## Higgs production @ LHC

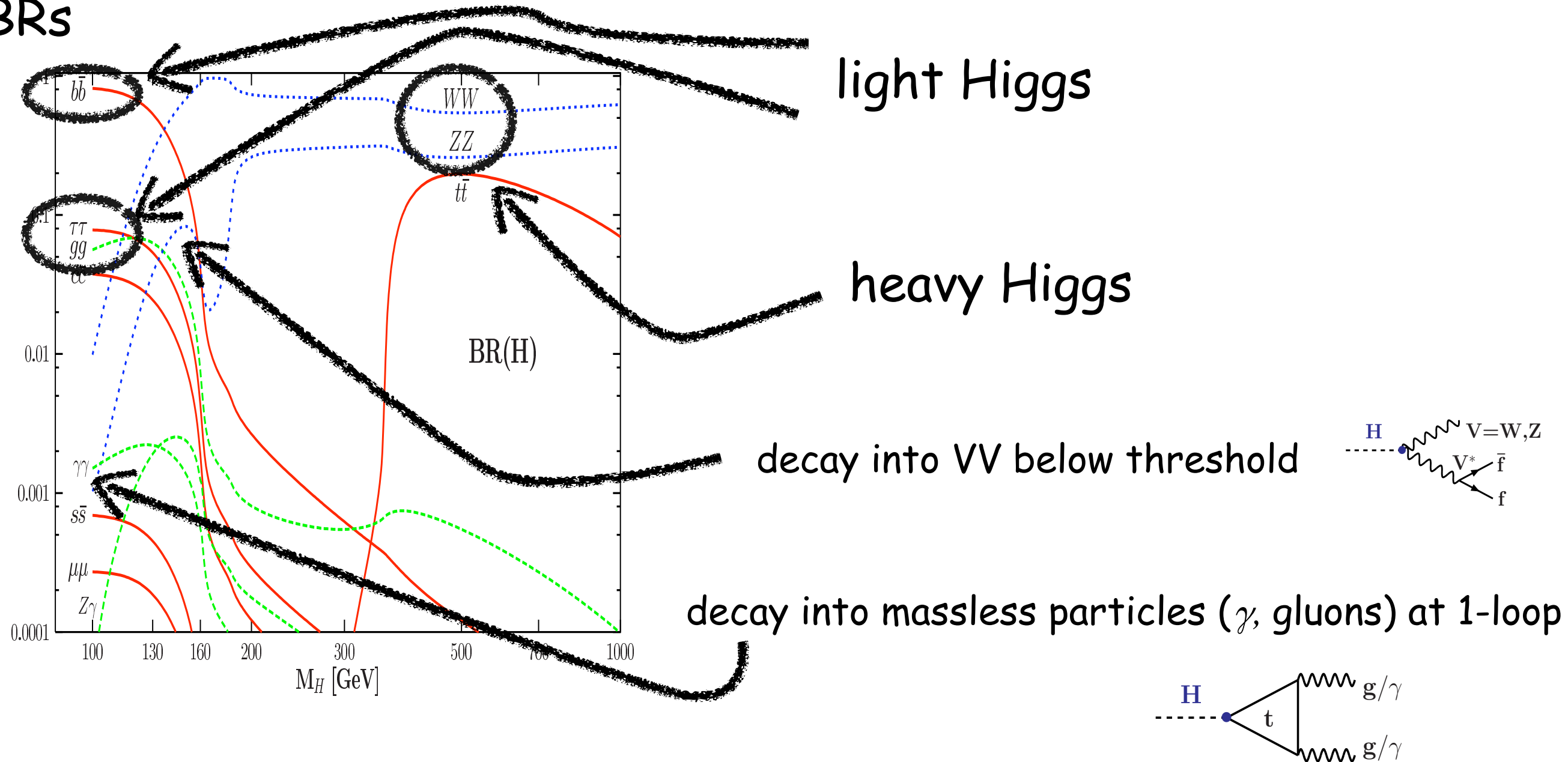


# (SM) Higgs Decays

Higgs couples proportionally to masses:

it decays into the heaviest particle available by phase space

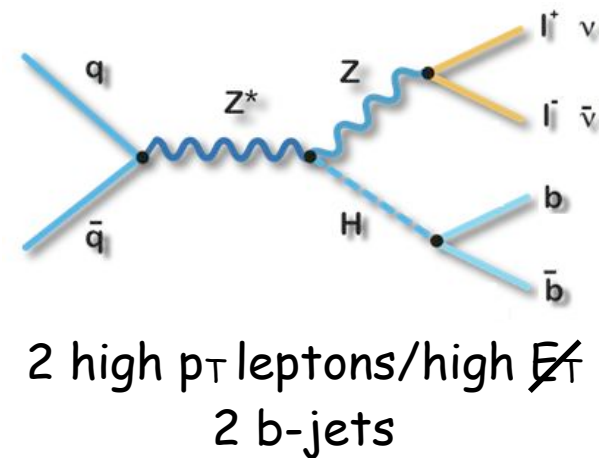
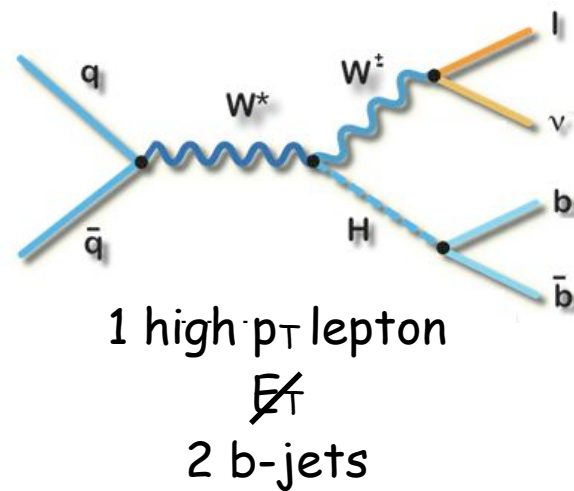
BRs





# (SM) Higgs Searches @ Tevatron

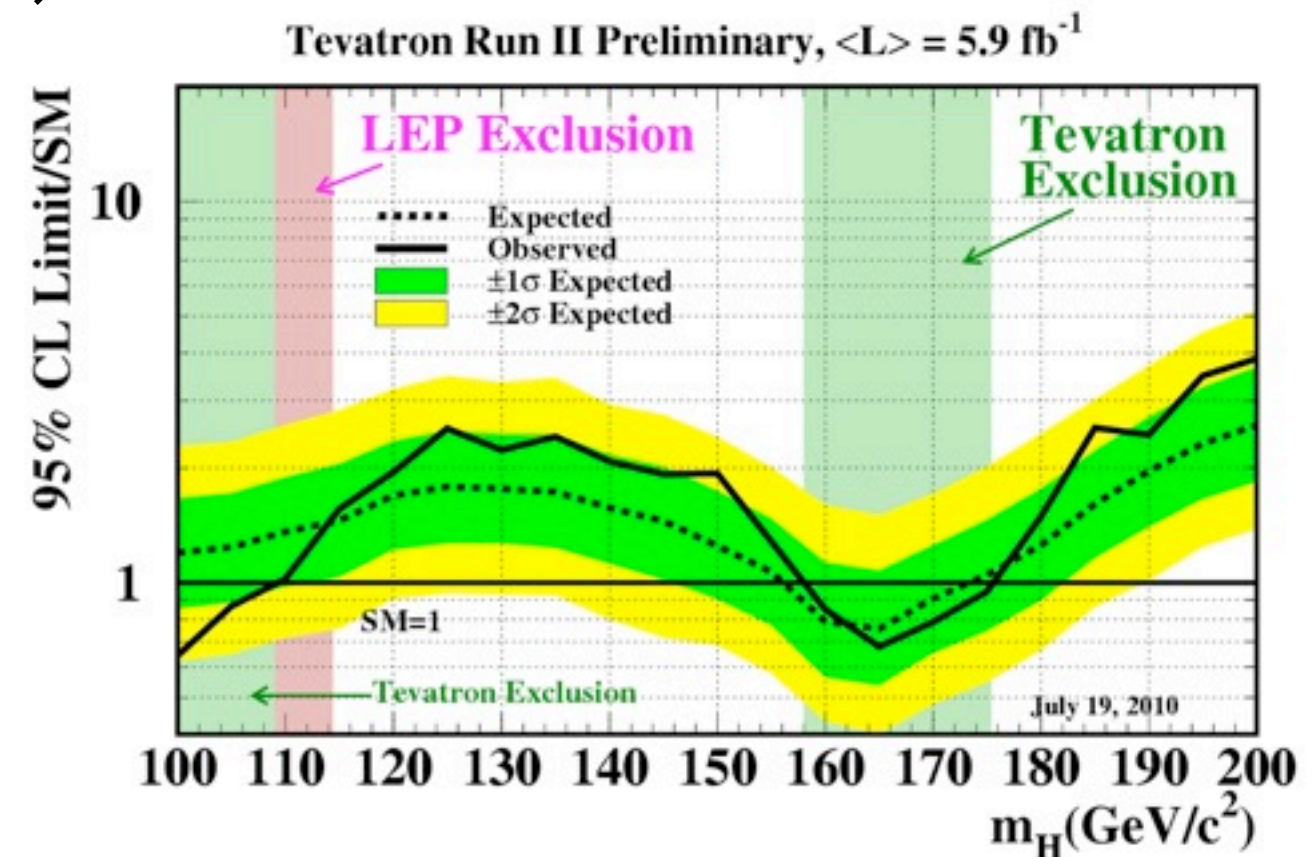
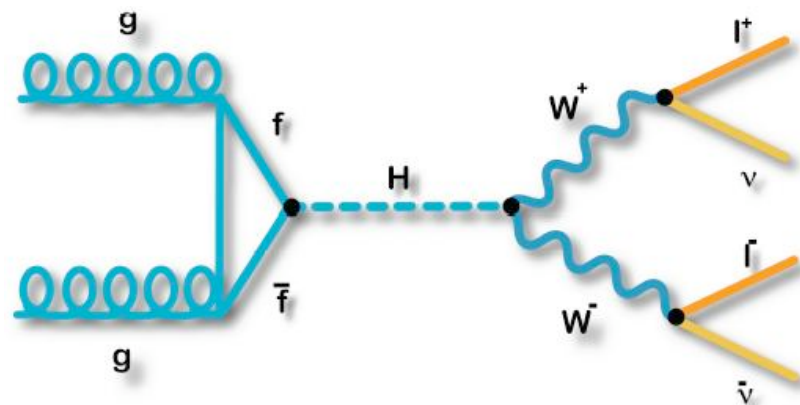
## Low Mass Higgs



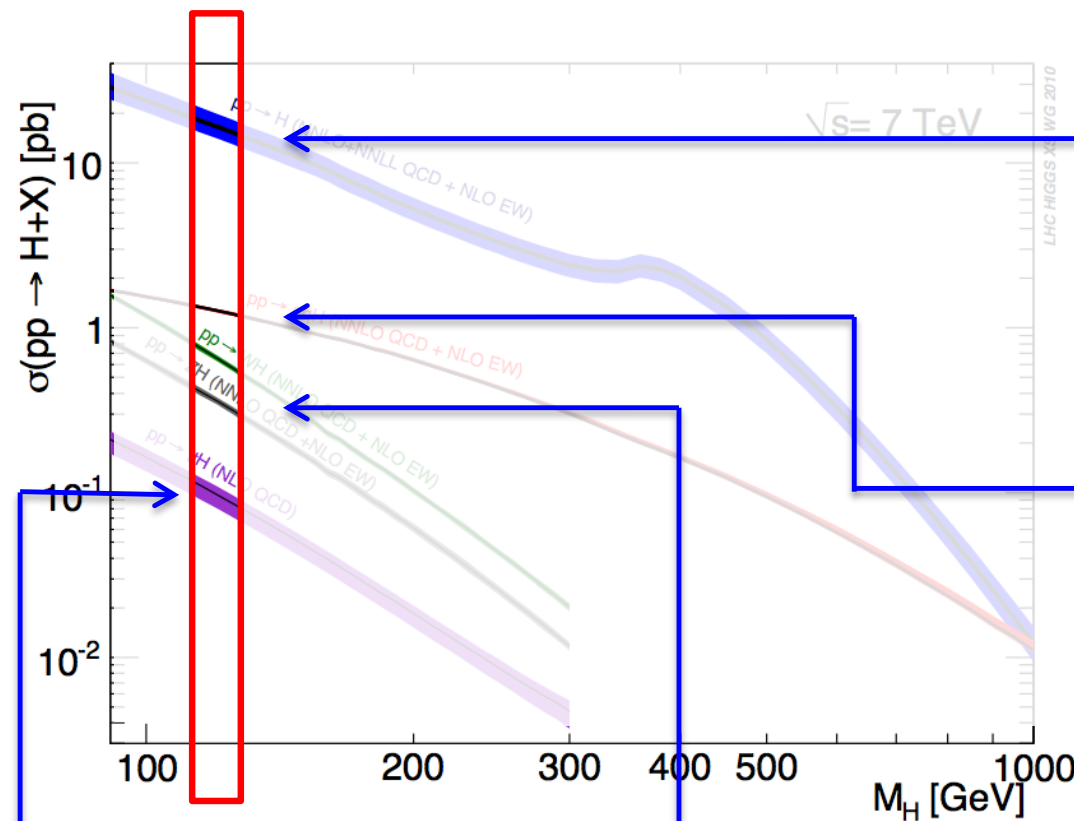
## Issues:

- lepton identification
- b-tagging performance
- dijet mass resolution

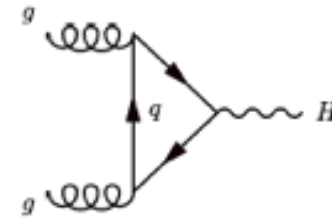
## Higg Mass Higgs



# (SM) Higgs Searches @ the LHC



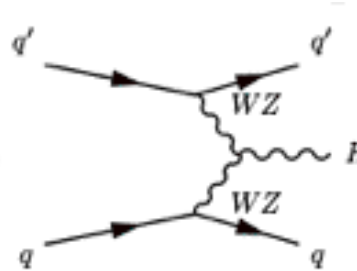
~3 k events produced!



## - Gluon fusion process :

Dominant process known at NNnLO TH uncertainty ~O(10%)

~0.5 M events produced!



## - Vector Boson Fusion :

known at NLO TH uncertainty ~O(5%)

Distinctive features with two forward jets and a large rapidity gap

~40 k events produced!

## - W and Z Associated Production :

known at NNLO TH uncertainty ~O(5%)

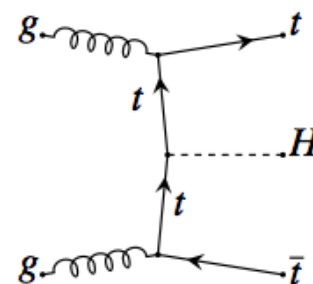
Very distinctive feature with a Z or W decaying leptonically

~20 k events produced!

## - Top Associated Production :

known at NLO TH uncertainty ~O(15%)

Quite distinctive but also quite crowded



# (SM) Higgs Searches @ the LHC

- Dominant decay mode b (57%)

Very large backgrounds, associated production W,Z H and Boost!

- The  $\tau\tau$  channel (6.3%)

VBF, VH, but also ggF with new mass reconstruction techniques

- The  $\gamma\gamma$  channel (0.2%)

Discovery channel, high mass resolution (High stat, and backgrounds)

- The ZZ Channel (3%)

- Subsequent all leptons decays (low statistics): golden channel

- llqq and llvv sensitive mostly at high mass

- The WW Channel (22%)

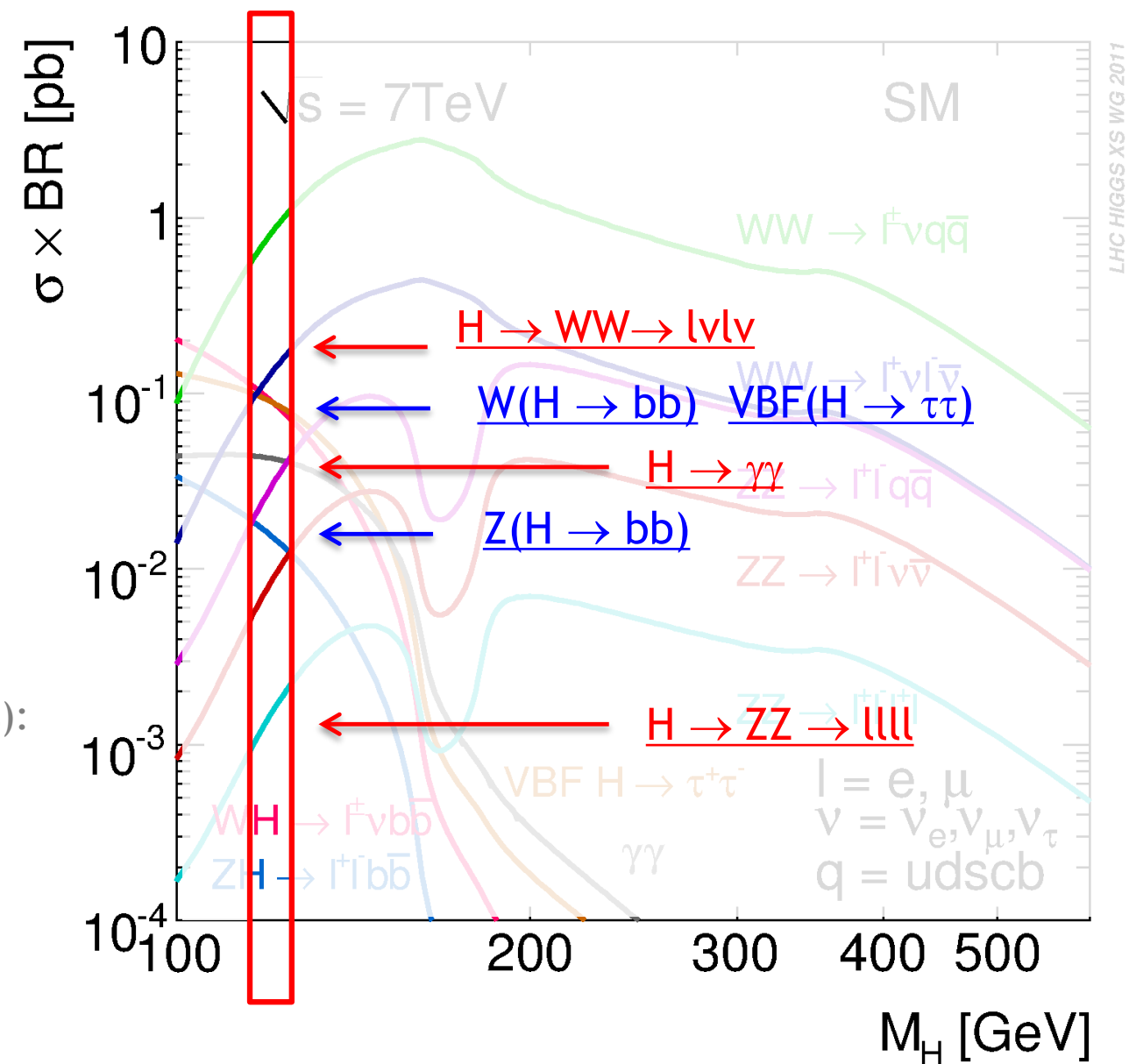
- Subsequent l $\nu$ l $\nu$  very sensitive channel

- lvqq sensitive mostly at high mass

- The  $\mu\mu$  channel (0.02%) and  $Z\gamma$  (0.2%)

Low statistics from the low branching in  $\mu\mu$  or both the low branching and subsequent decay in leptons ( $Z\gamma$ )

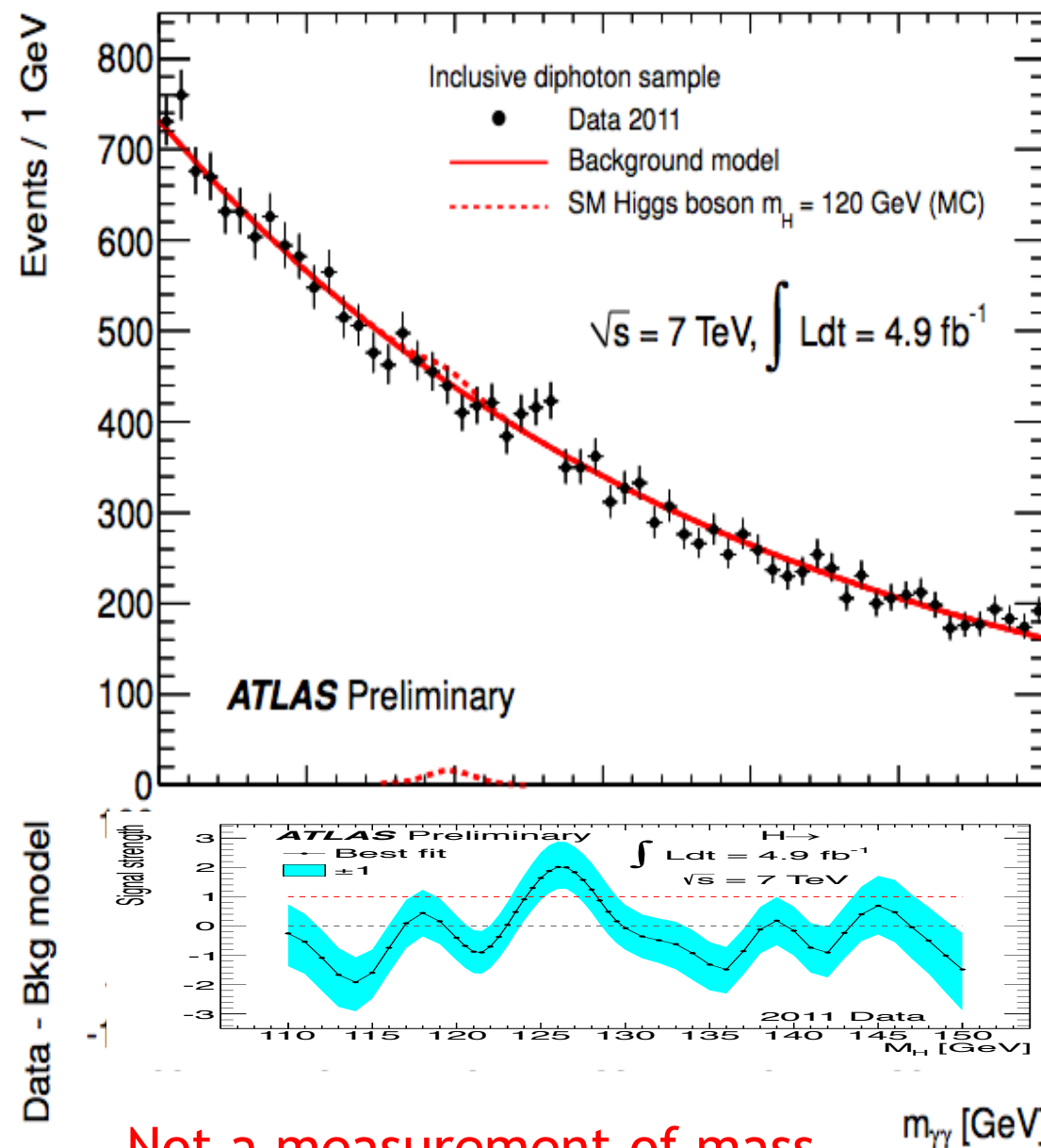
- The cc channel (3%) Very difficult



slide courtesy of M. Kado, CERN ATC '14

# The Higgs discovery @ the LHC

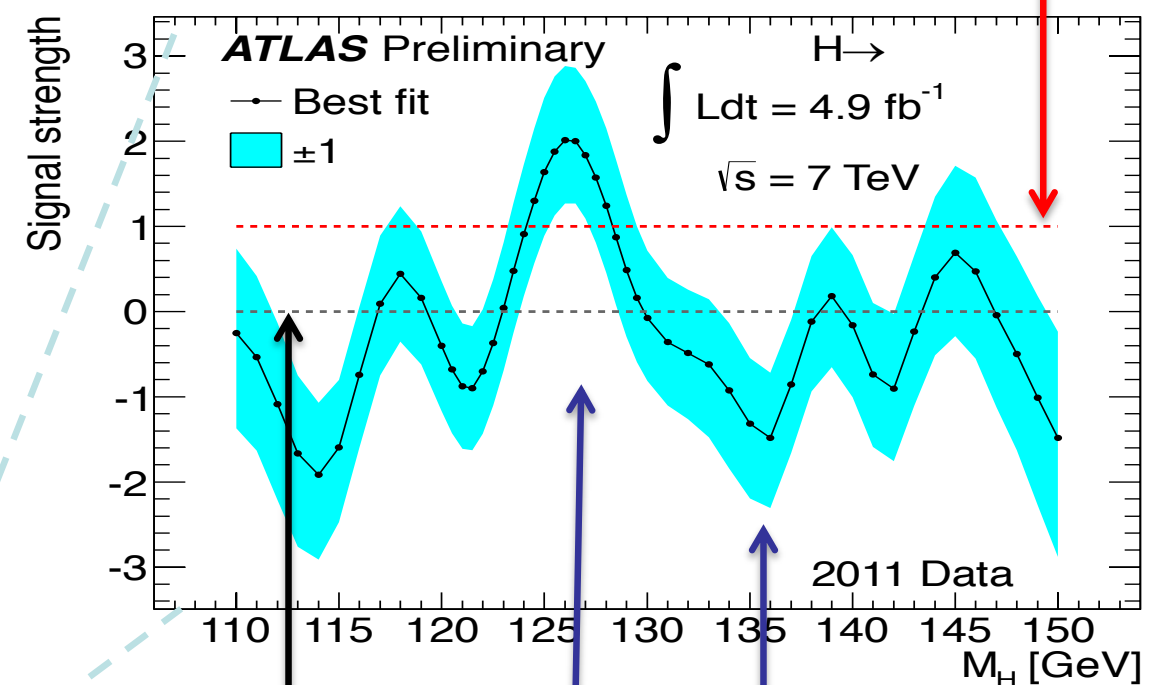
$$gg \rightarrow H \rightarrow \gamma\gamma$$



Not a measurement of mass

Not a measurement of cross section

Relate to Higgs mass hypothesis



Expected Background

Excess

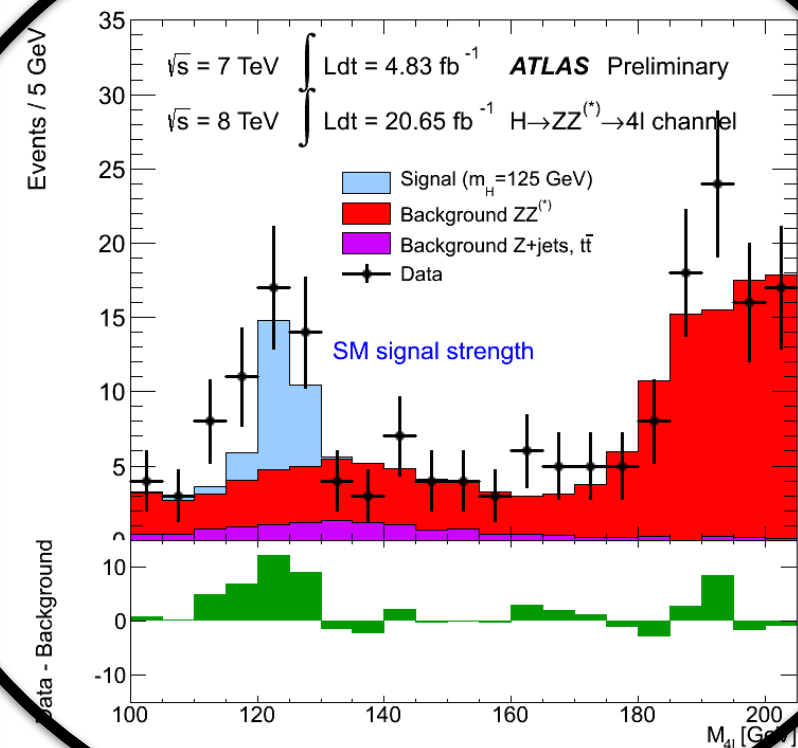
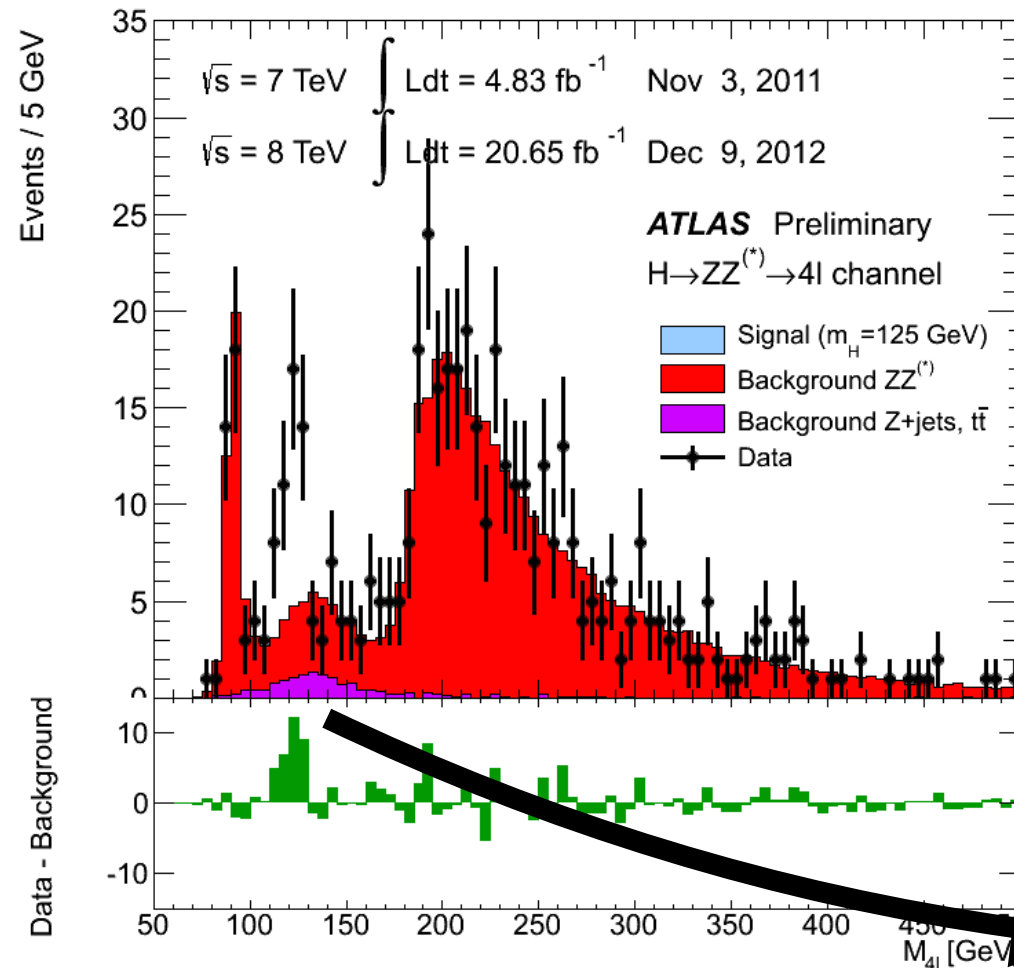
Deficit

Expected Signal

slide courtesy of M. Kado, CERN ATC '14

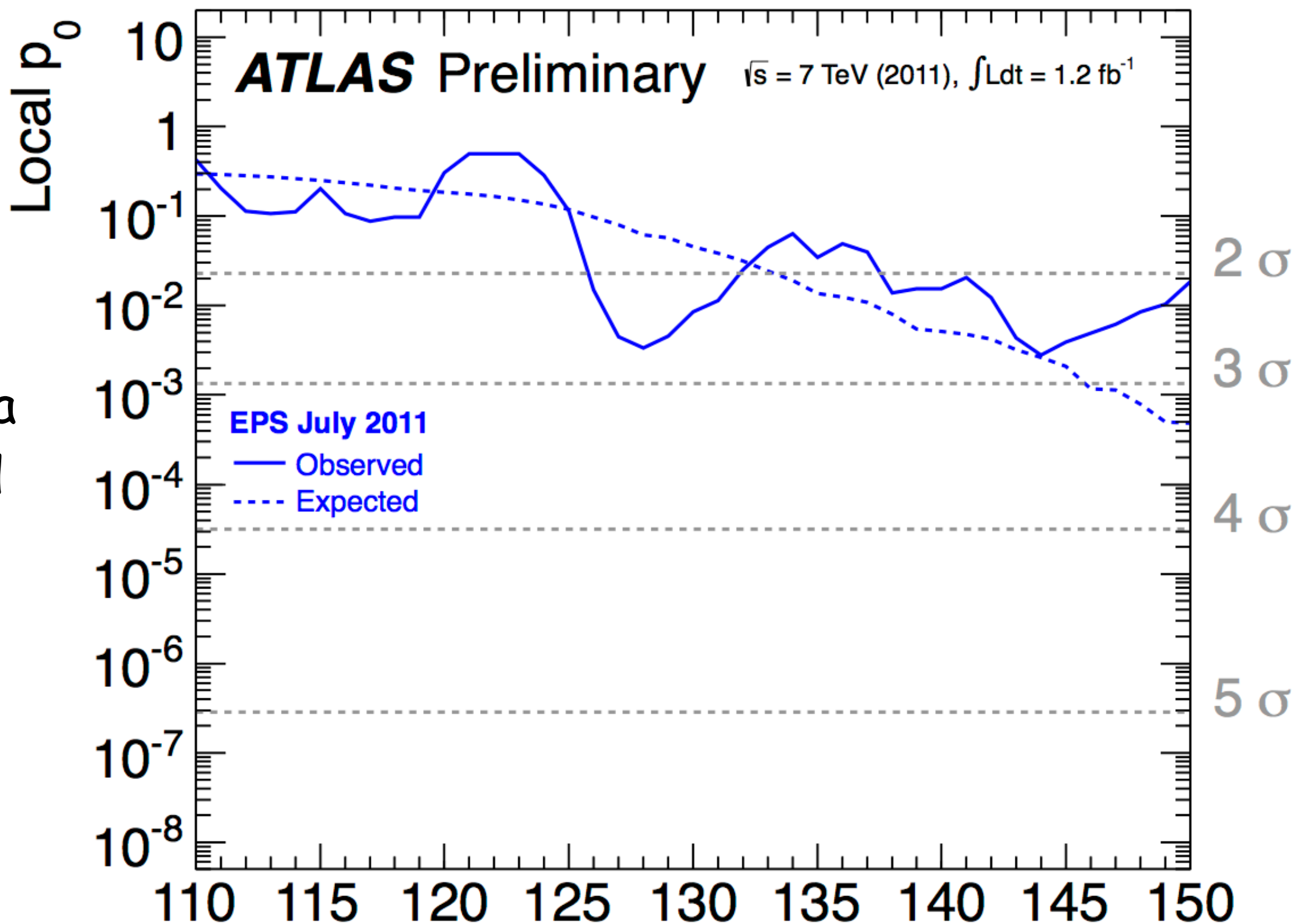
# The Higgs discovery @ the LHC

$$gg \rightarrow H \rightarrow ZZ^* \rightarrow 4l$$

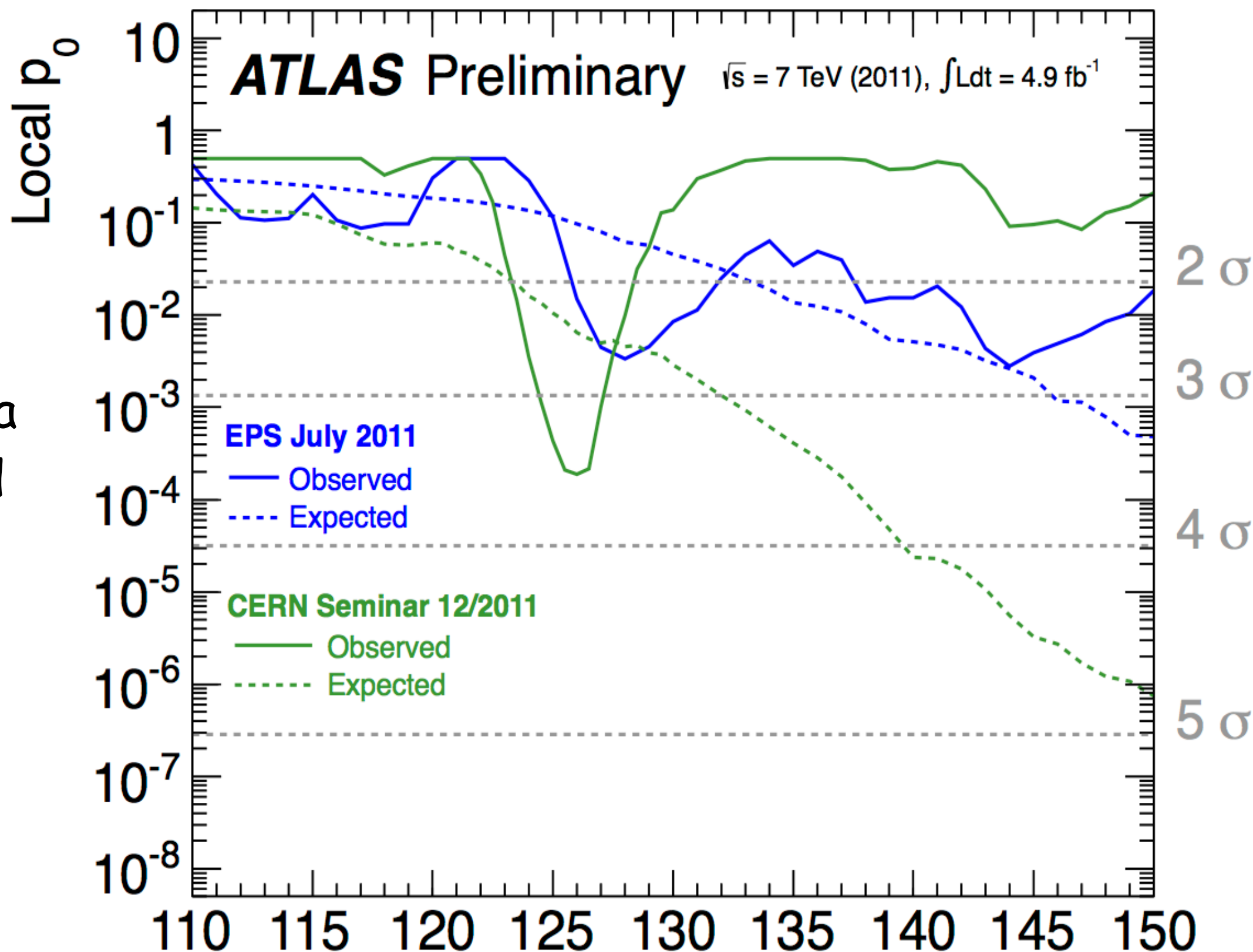




# Higgs Discovery Reloaded

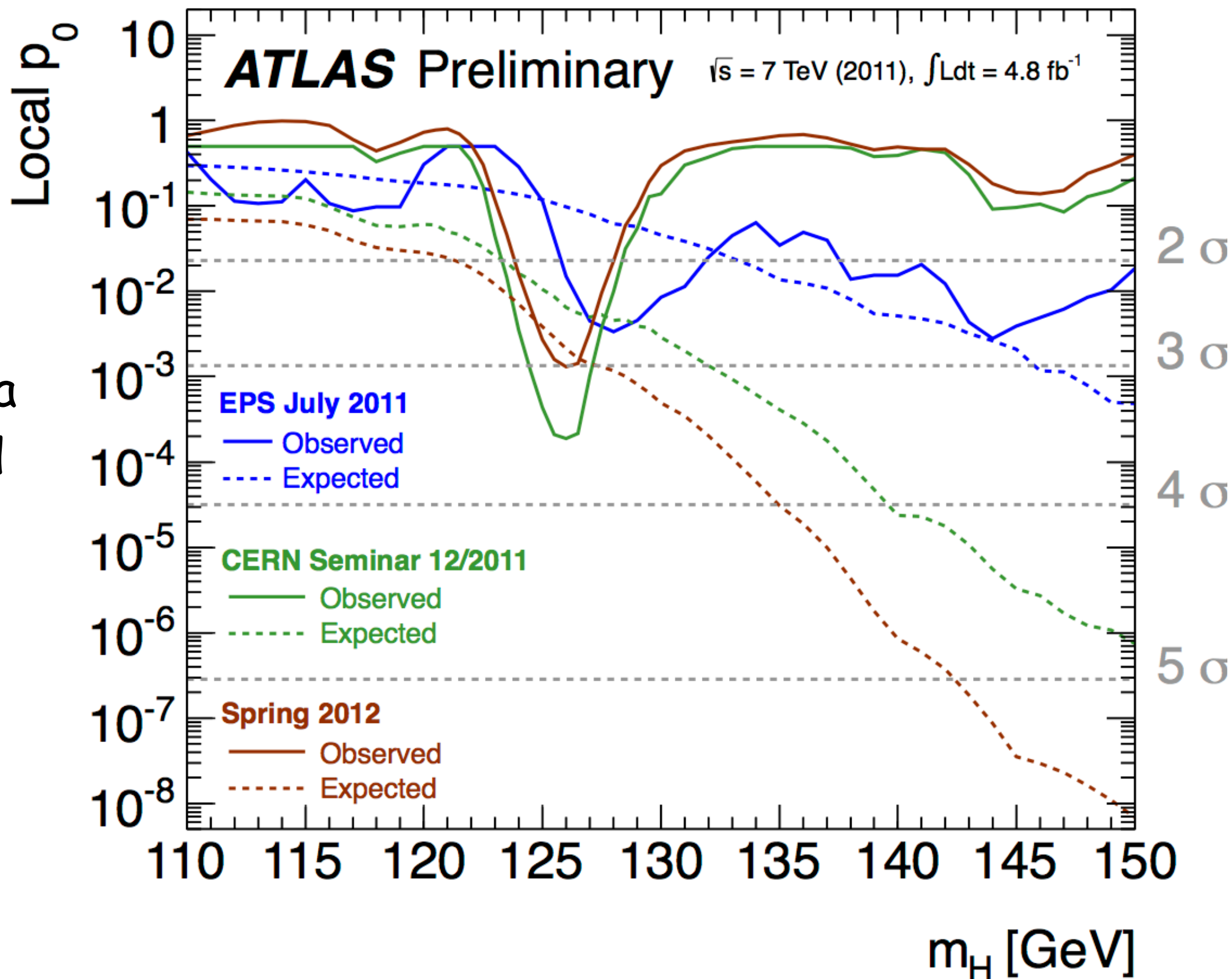


# Higgs Discovery Reloaded

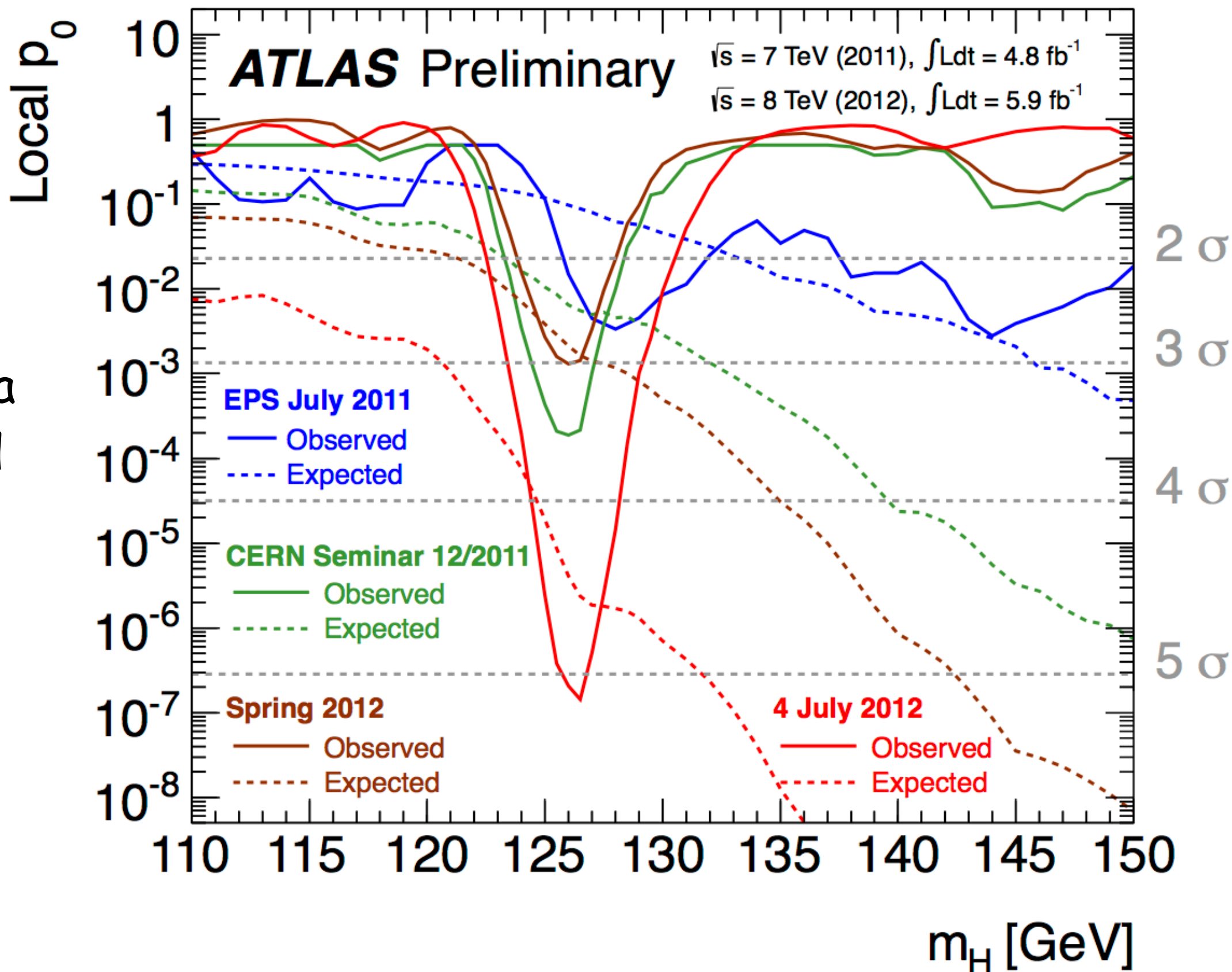


# Higgs Discovery Reloaded

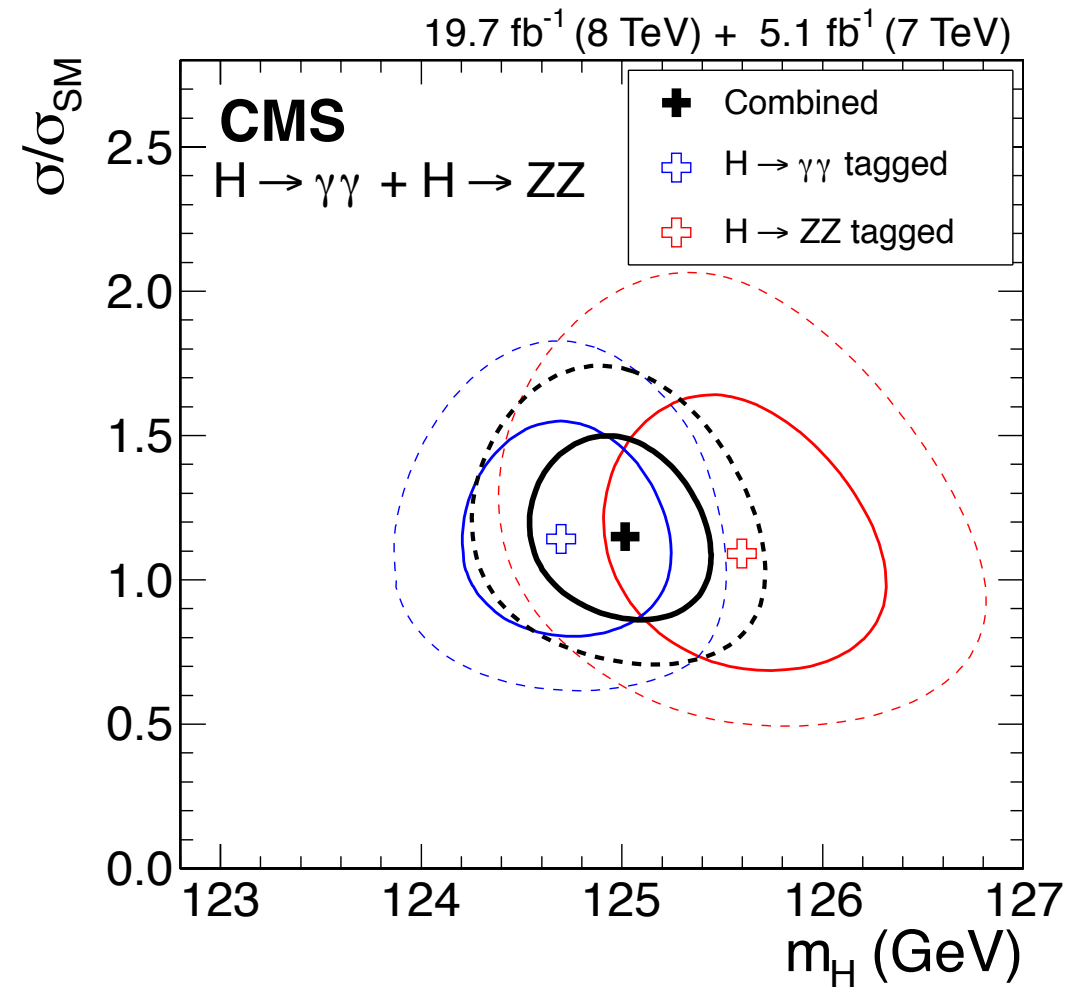
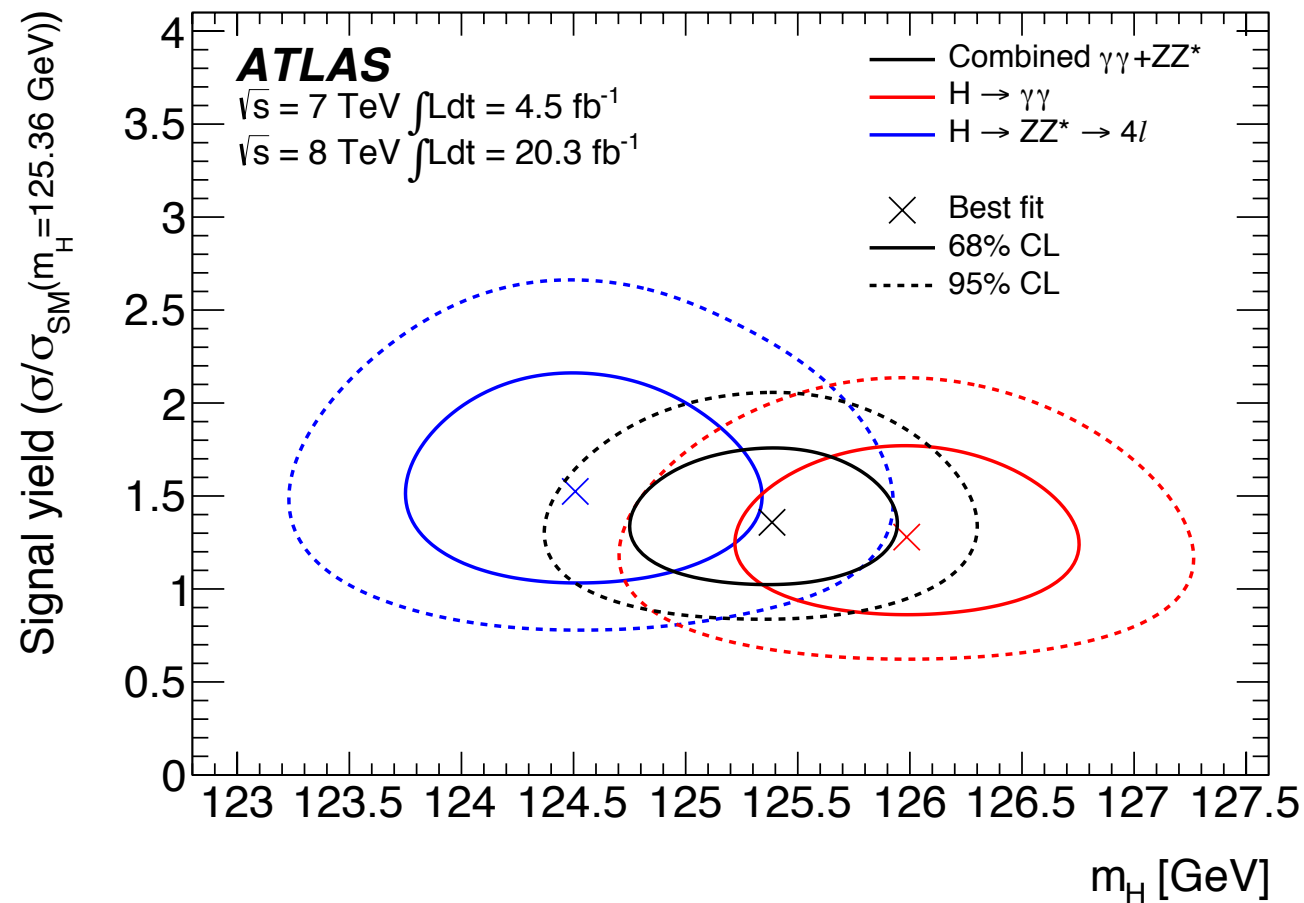
probability  
to observe a  
background  
fluctuation  
instead of  
the signal



# Higgs Discovery Reloaded



# Towards Higgs measurements



Experiment	$H \rightarrow \gamma\gamma$	$H \rightarrow ZZ^* \rightarrow 4\ell$	combined
ATLAS	$125.98 \pm 0.42(\text{stat.}) \pm 0.28(\text{syst.})$	$124.51 \pm 0.52(\text{stat.}) \pm 0.06(\text{syst.})$	$125.36 \pm 0.37(\text{stat.}) \pm 0.18(\text{syst.})$
CMS	$124.70 \pm 0.31(\text{stat.}) \pm 0.15(\text{syst.})$	$125.59 \pm 0.42(\text{stat.}) \pm 0.17(\text{syst.})$	$125.02 \pm 0.27(\text{stat.}) \pm 0.15(\text{syst.})$



# The Higgs program

*"With great power comes great responsibility"*

which, in particle physics, really means

Voltaire & Spider-Man

*"With great discoveries come great measurements"*

BSMers desperately looking for anomalies  
(true credit: F. Maltoni)

The Higgs has access to EW coupled New Physics  
which is less constrained by direct searches than strongly coupled NP

1

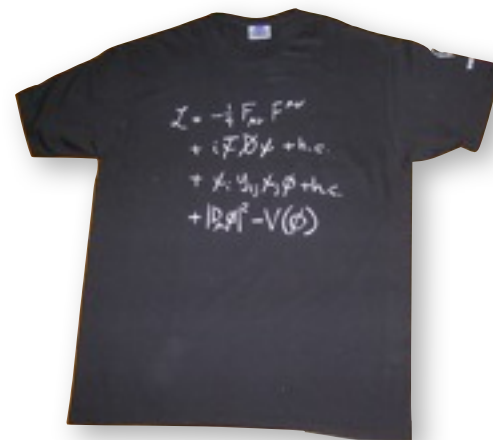
Higgs properties

JPC

Important & nice to see progresses but  
"this question carries a similar potential  
for surprise as a football game between  
Brazil and Tonga" **Resonaances**

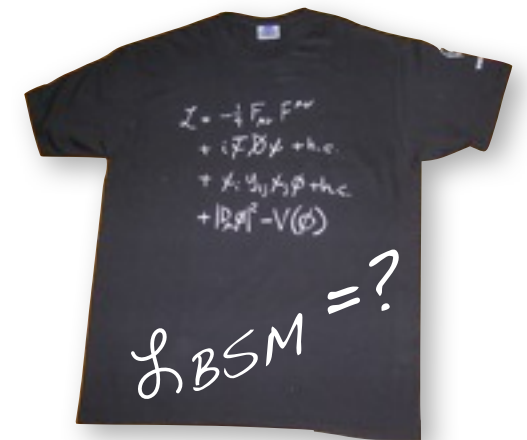
2

Higgs couplings



3

BSM implications





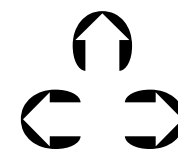


[pictures: courtesy of G. Giudice]

6

# *UV behaviour of the Higgs boson*

*(triviality, stability, hierarchy)*

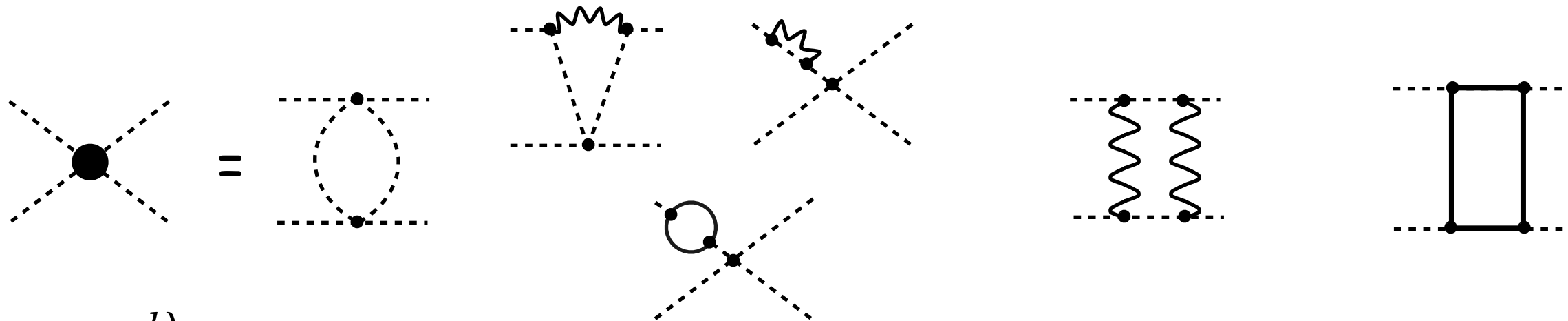


# Quantum Behavior of the Higgs<sup>4</sup> Coupling (I)

$$V(h) = -\frac{1}{2}\mu^2 h^2 + \frac{1}{4}\lambda h^4$$

vev:  $v^2 = \mu^2 / \lambda$

mass:  $m_H^2 = 2\lambda v^2$



$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2 g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{Higher loops} + \text{Small Yukawa}$$

Large mass ( $\lambda$  dominated RGE)

$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2$$

$\lambda$  increases with  $Q$ : IR-free coupling

$$\lambda(Q) = \frac{m_H^2}{2v^2 - \frac{3}{2\pi^2} m_H^2 \ln(Q/v)}$$

# Quantum Behavior of the Higgs<sup>4</sup> Coupling (I)

$$V(h) = -\frac{1}{2}\mu^2 h^2 + \frac{1}{4}\lambda h^4$$

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Large mass ( $\lambda$  dominated RGE)

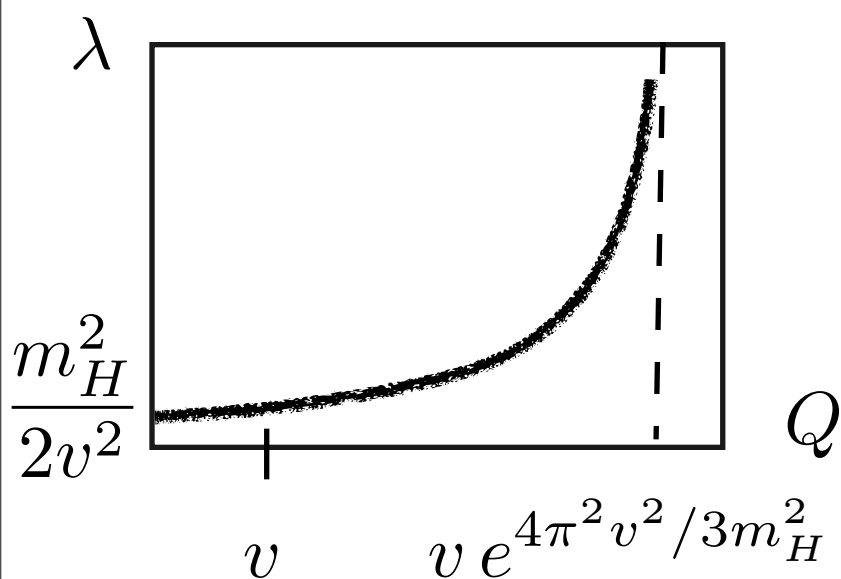
$$\lambda(Q) = \frac{m_H^2}{2v^2 - \frac{3}{2\pi^2} m_H^2 \ln(Q/v)}$$

Wilson '71  
Wilson, Kogut '74

Landau pole

Triviality bound

$$\Lambda \leq v e^{4\pi^2 v^2 / 3m_H^2}$$



New physics should appear before that point to restore stability

for  $m_H$  fixed, upper bound on  $\Lambda$   
for  $\Lambda$  fixed, upper bound on  $m_H$

No microscopic description: for  $\Lambda \rightarrow \infty$ , trivial theory ( $\lambda=0$ )


# Quantum Behavior of the Higgs<sup>4</sup> Coupling (II)

$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{Higher loops} + \text{Small Yukawa}$$

Small mass ( $y_t$  dominated RGE)

$$16\pi^2 \frac{d\lambda}{d \ln Q} = -6y_t^4$$

$\lambda$  decreases with  $Q$ .



$$\left( 16\pi^2 \frac{dy_t}{d \ln Q} = \frac{9}{2} y_t^3 + \text{Higher loops} + \text{Small Yukawa} \quad y^2(Q) = \frac{y^2(Q_0)}{1 - \frac{9}{16\pi^2} y^2(Q_0) \ln \frac{Q}{Q_0}} \right)$$

$$\lambda(Q) = \lambda_0 - \frac{\frac{3}{8\pi^2} y_0^4 \ln \frac{Q}{Q_0}}{1 - \frac{9}{16\pi^2} y_0^2 \ln \frac{Q}{Q_0}}$$

# Quantum Behavior of the Higgs<sup>4</sup> Coupling (II)

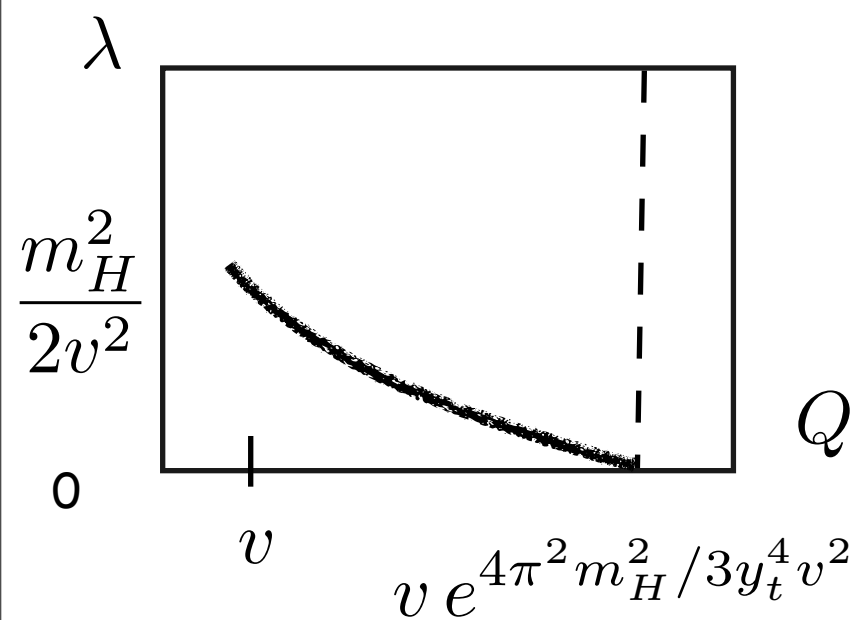
$$16\pi^2 \frac{d\lambda}{d \ln Q} = 24\lambda^2 - (3g'^2 + 9g^2 - 12y_t^2)\lambda + \frac{3}{8}g'^4 + \frac{3}{4}g'^2g^2 + \frac{9}{8}g^4 - 6y_t^4 + \text{Higher loops} + \text{Small Yukawa}$$

Small mass ( $y_t$  dominated RGE)

$$\lambda(Q) = \lambda_0 - \frac{\frac{3}{8\pi^2} y_0^4 \ln \frac{Q}{Q_0}}{1 - \frac{9}{16\pi^2} y_0^2 \ln \frac{Q}{Q_0}}$$

$\lambda < 0 \Rightarrow$  potential unbounded from below

$$\lambda(Q) = 0 \quad \text{for} \quad \lambda_0 \approx \frac{3}{8\pi^2} y_0^4 \log \frac{Q}{Q_0}$$



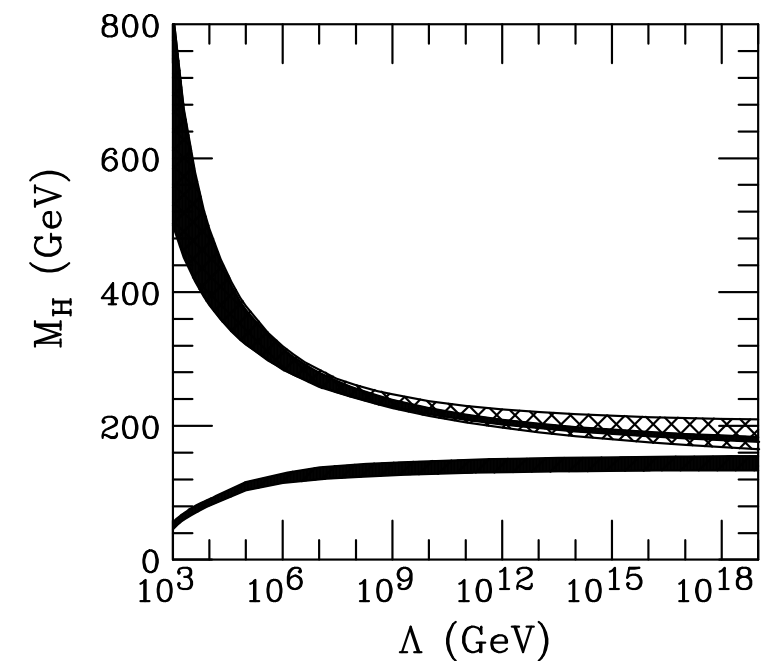
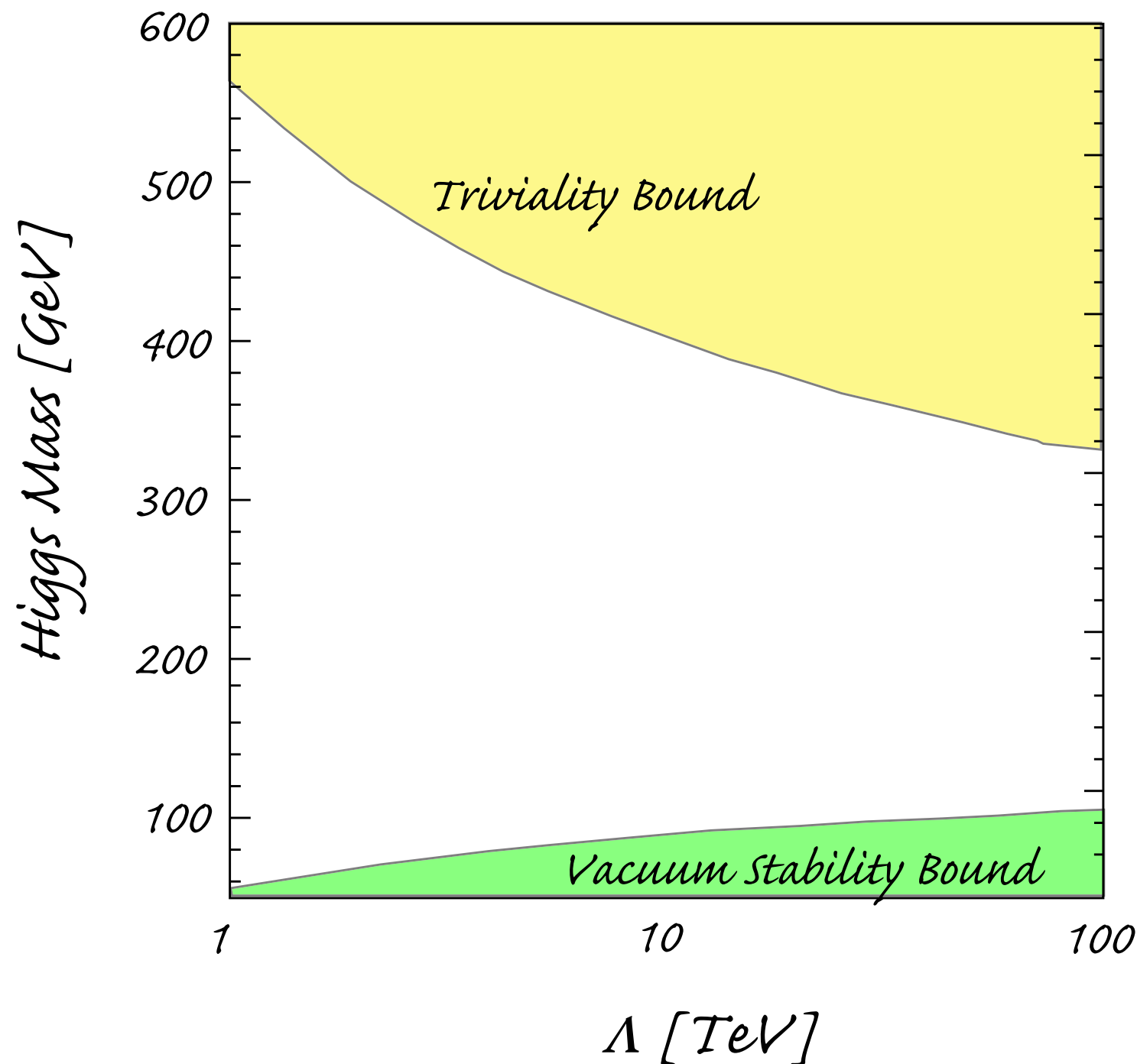
New physics should appear before that point to restore stability

$$\Lambda \leq v e^{4\pi^2 m_H^2 / (3y_t^4 v^2)} \quad \text{Stability bound}$$

for  $\Lambda$  fixed, lower bound on  $m_H$

Linde '76, '80  
Weinberg '76  
Maini et al '78, '79  
Politzer, Wolfram '79  
Lindner '86  
+...

Solving exactly the RG equation, we obtain the maximum domain of validity of the SM

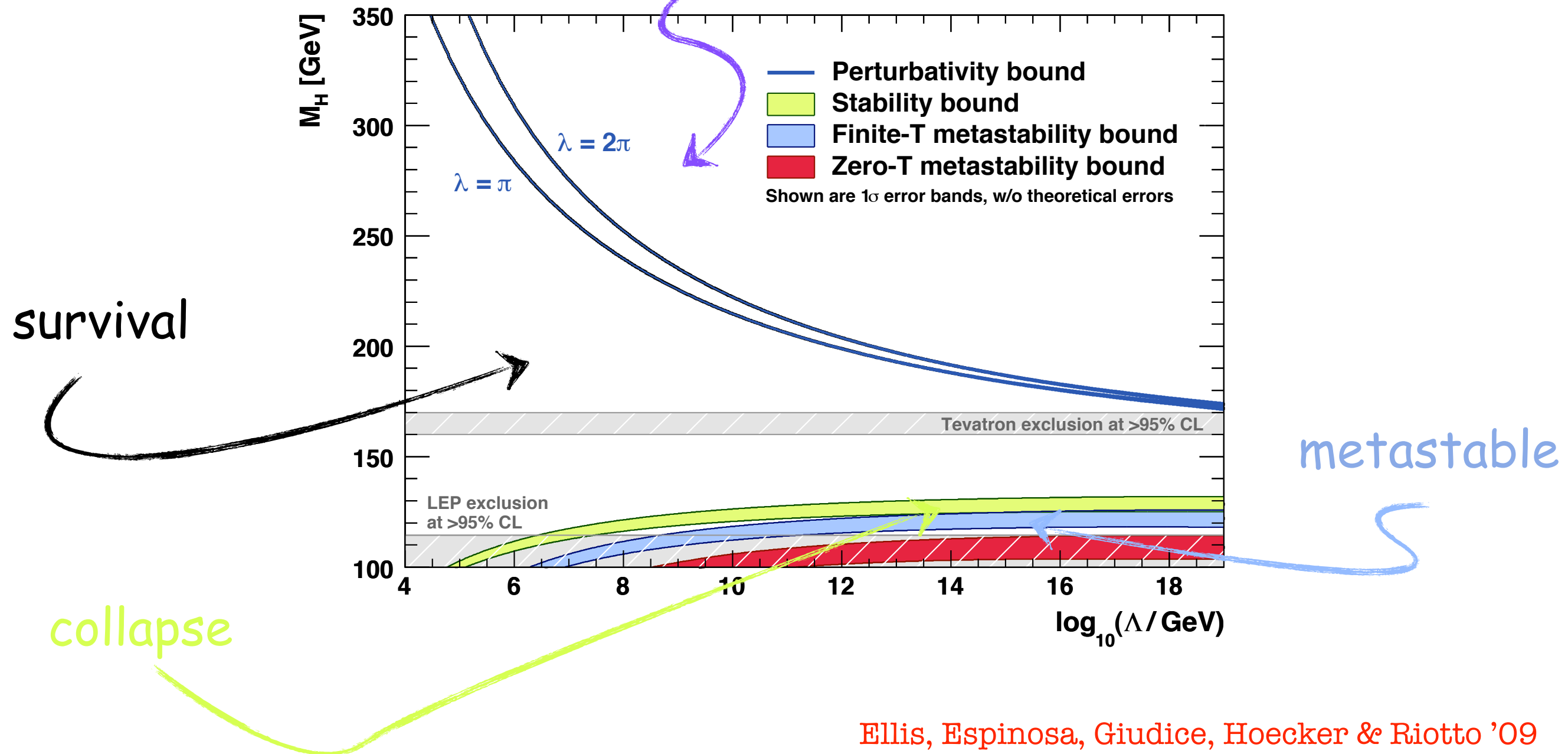


Hambye, Riesselmann '97

Only a light Higgs ( $130 \text{ GeV} < m_H < 170 \text{ GeV}$ ) allows for the absence of New Physics at low energy



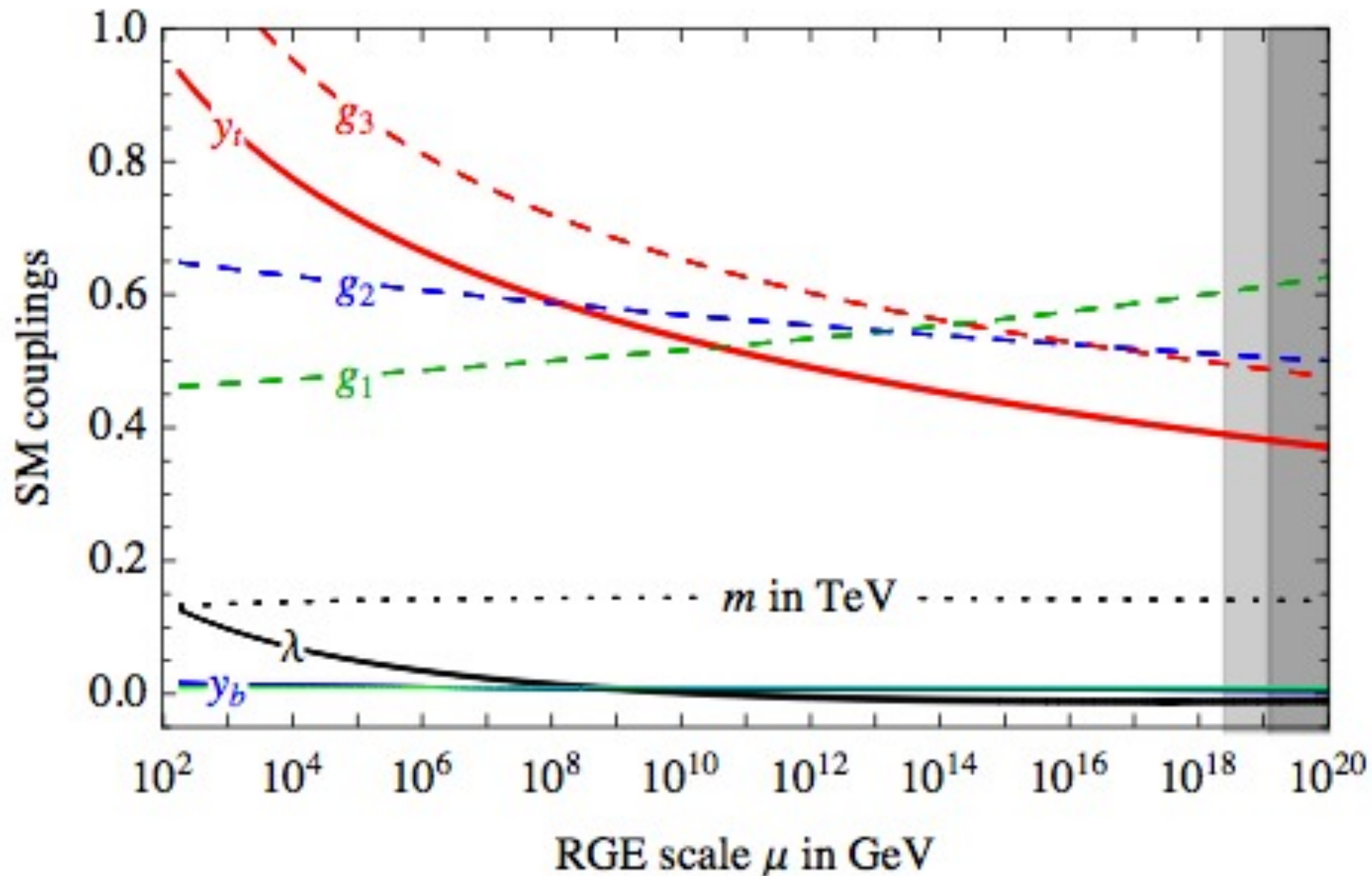
Solving exactly the RG equation, we obtain the maximum domain of validity of the SM  
 blow-up



Only a light Higgs ( $130 \text{ GeV} < m_H < 170 \text{ GeV}$ ) allows for the absence of New Physics at low energy

... and for  $m_H=125\text{GeV}$

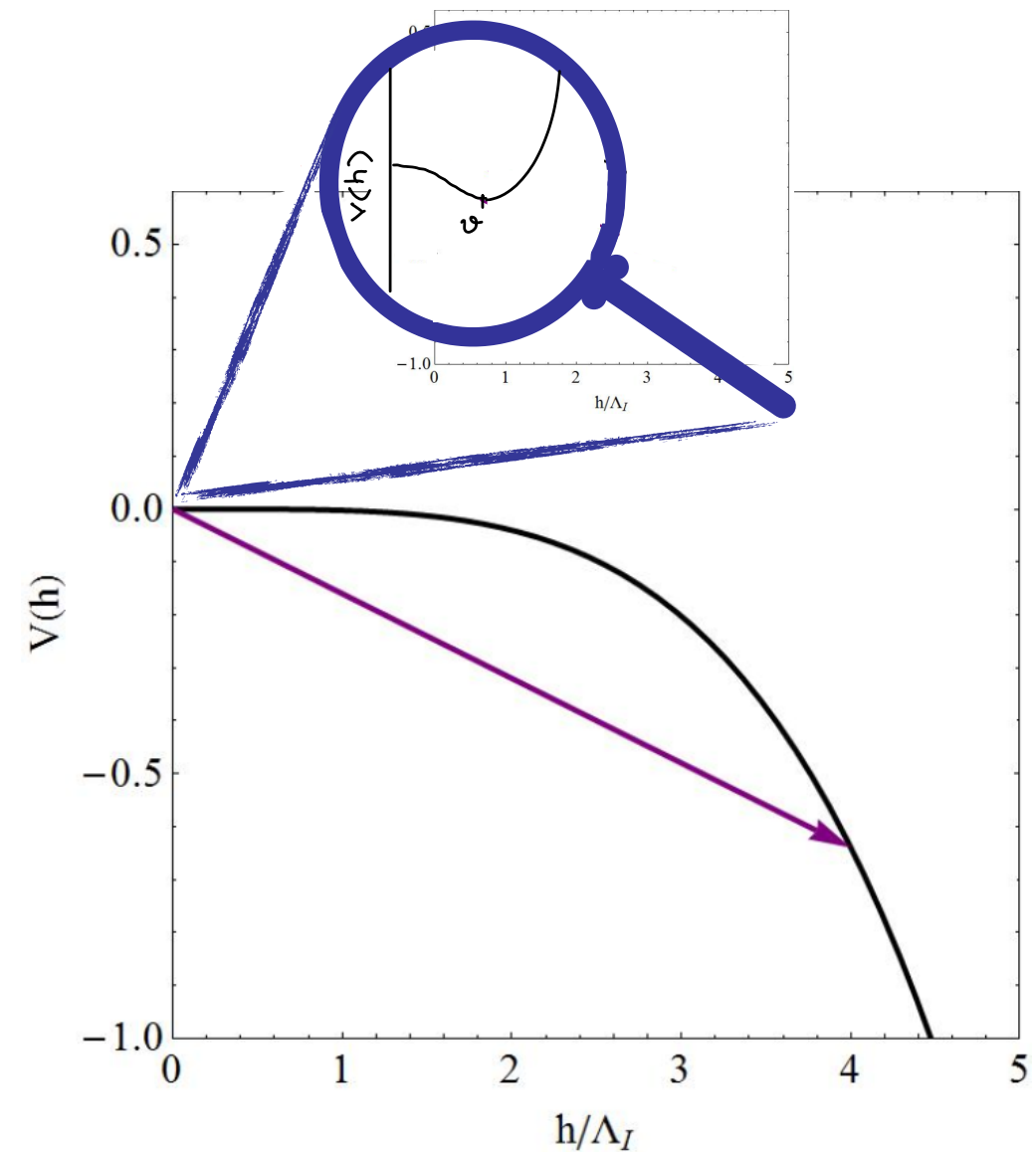
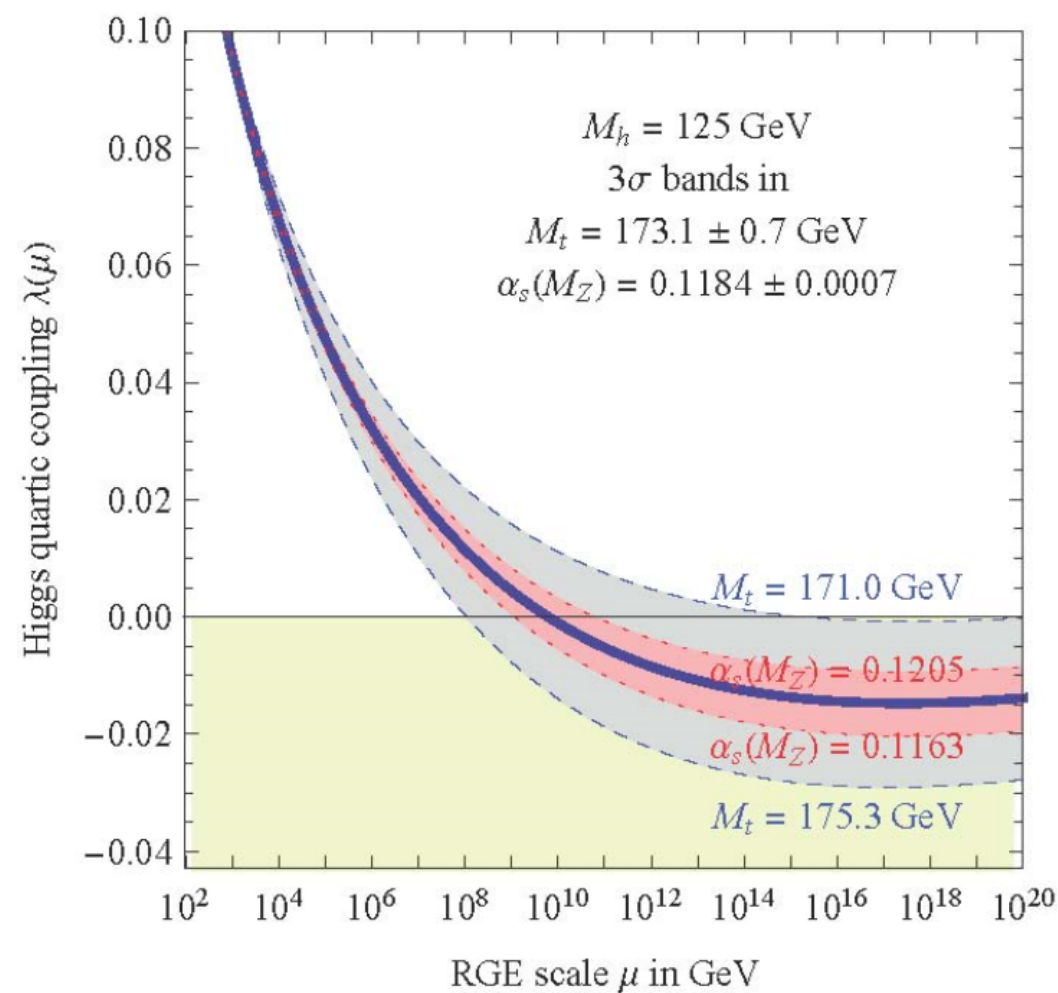
Buttazzo et al '13



Can the SM (without new physics)  
be valid up to  $M_{\text{Pl}}$  and remain weakly coupled?

# Stability vs Metastability

Degrassi et al '12



Life time of the EW vacuum?

delicate computation!

exp(-bounce action)

prefactors also matter

needs to control all cosmological history of the Universe  
 thermal fluctuations?

# Stability vs Metastability: a question of precision!

## NNLO STABILITY BOUND

Lower bound on  $M_h$  for stability up to  $M_{Pl}$ :

State-of-the-art NNLO calculation:

- 2-loop  $V_{eff}$  (Ford, Jack, Jones [ph/0111190])
- 3-loop RGES (... , Chetyrkin, Zoller [ph/1205.2892],  
Bednyakov, Pikelner, Velizhanin [ph/1212.6829])
- 2-loop matching in  $\lambda \leftrightarrow M_h^2$ ;  $h_t \leftrightarrow M_t$   
(... , Shaposhnikov et al [ph/1205.2893],  
, Degrandi et al [ph/1205.6497],  
, Bottazzo et al [ph/1307.3536])

For stability up to  $M_{Pl}$ :

$$M_h [\text{GeV}] > 129.4 + 1.4 \left( \frac{M_t (\text{GeV}) - 173.1}{0.7} \right) - 0.5 \left( \frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0_{th}$$

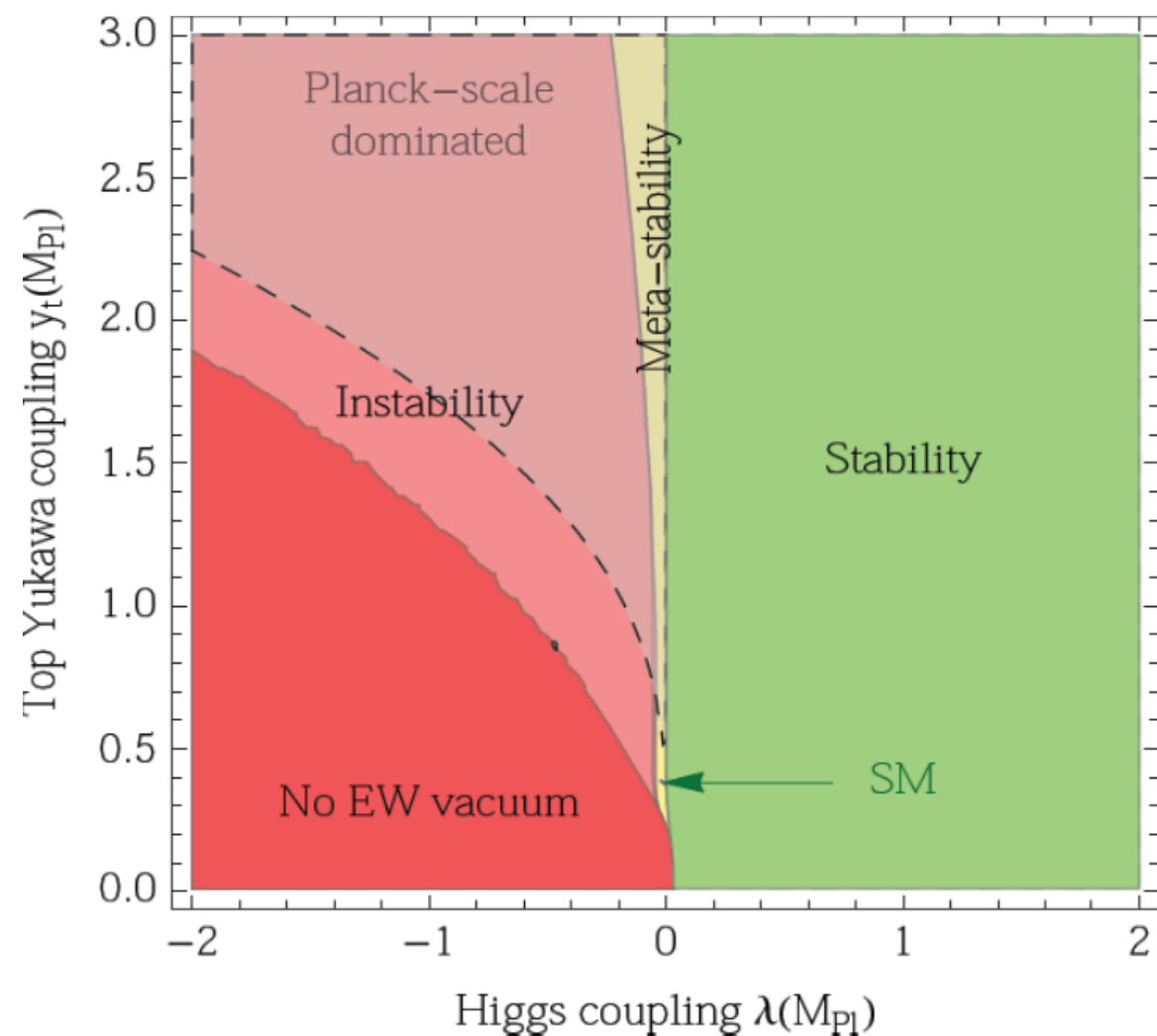
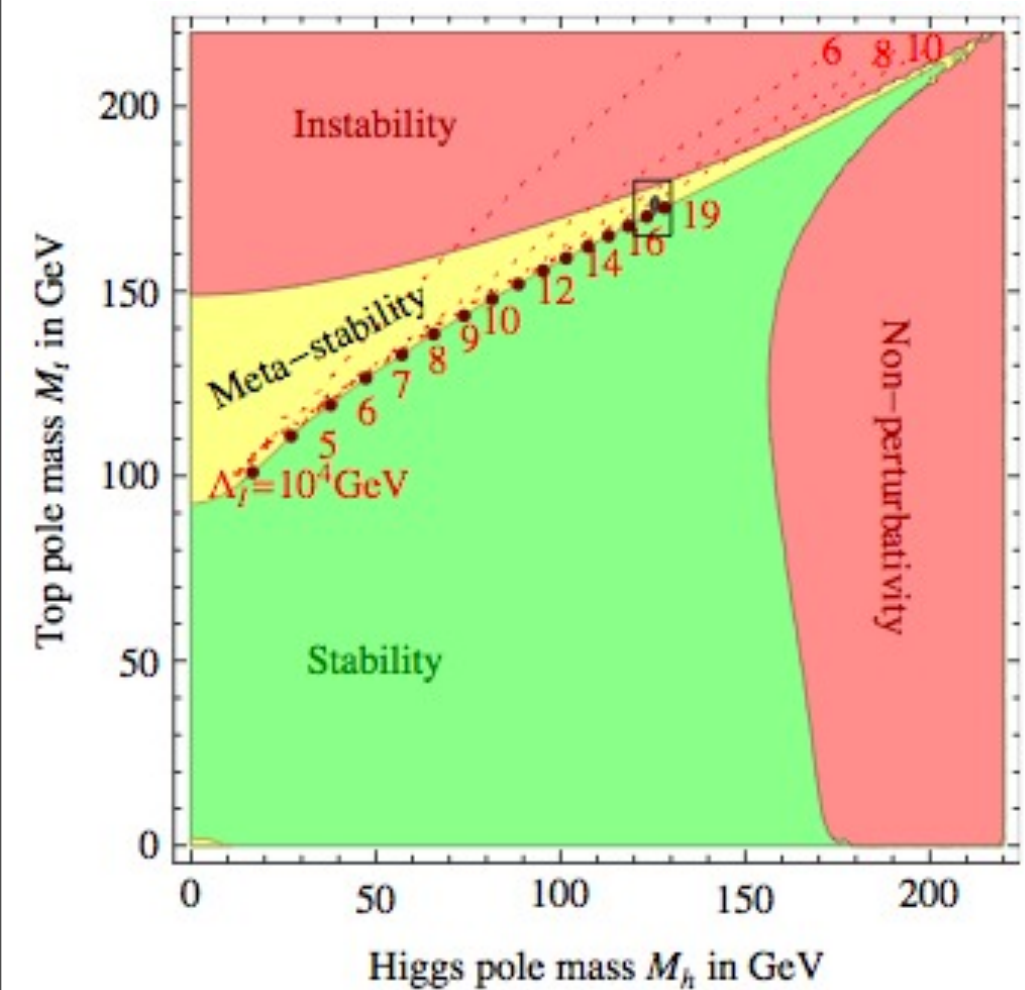
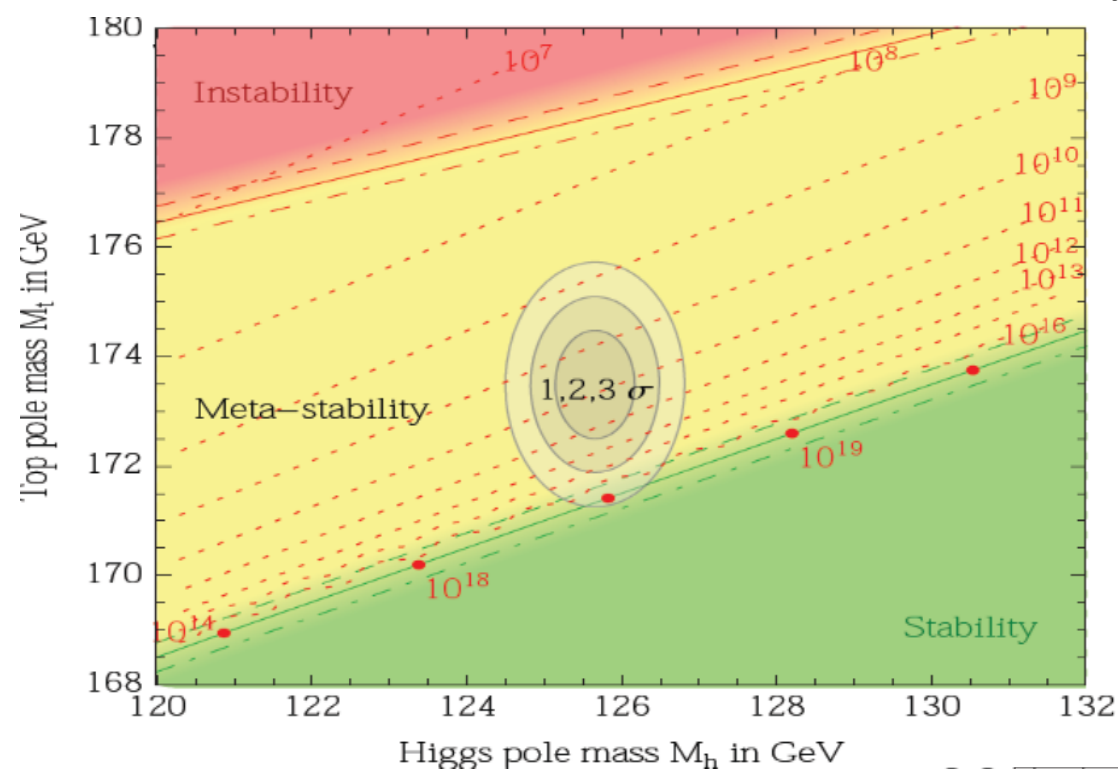
Degrandi et al '12

$$M_h [\text{GeV}] > 129.6 + 2 \left( \frac{M_t (\text{GeV}) - 173.35}{1} \right) - 0.5 \left( \frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 0.3_{th}$$

Bottazzo et al '13

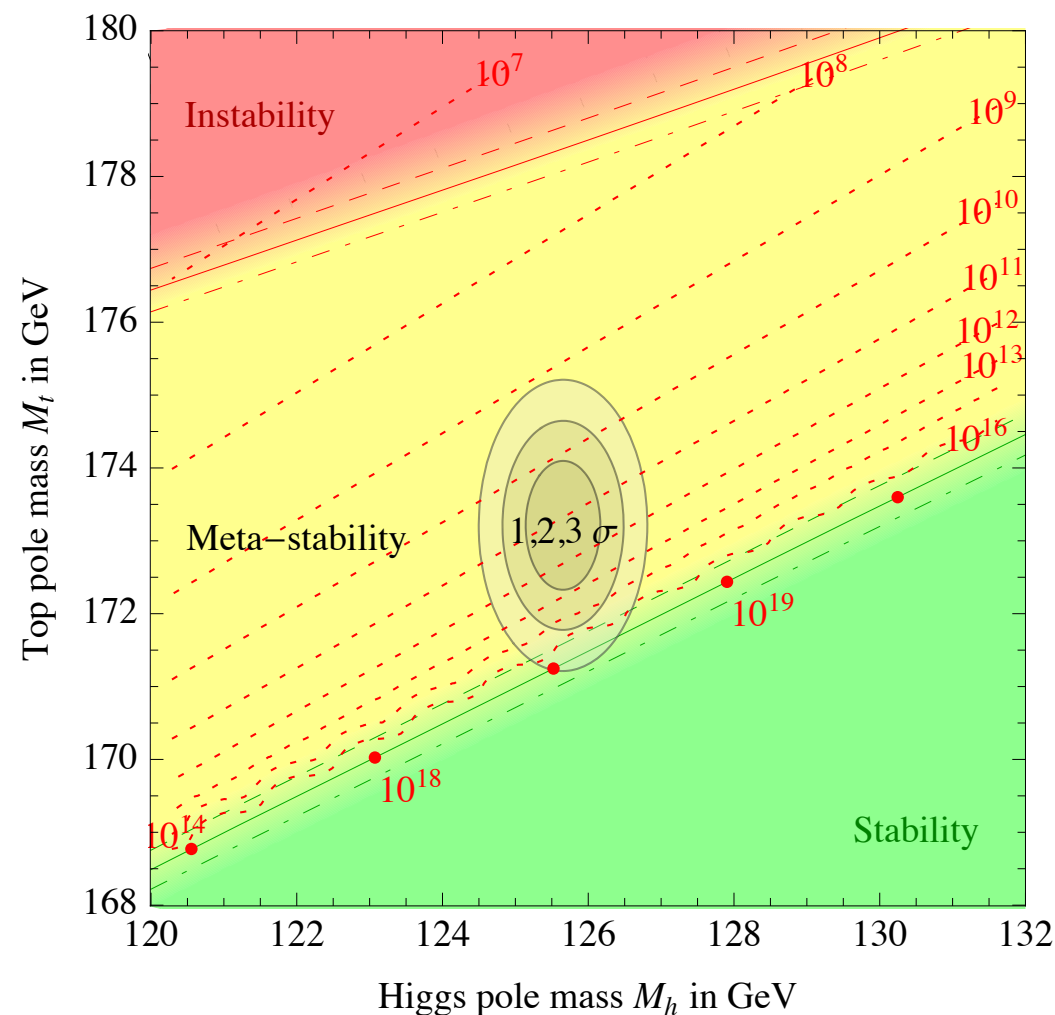
# Are we living at a edge of the phase diagram?

Bezrukov et al '12  
Degrassi et al '12  
Buttazzo et al '13





# The fate of the EW vacuum



Buttazzo et al '13

It is almost certain ( $>4\sigma$ ) that  $m_H > M_{\text{mestability}}$  and totally certain that  $m_H < M_{\text{Landau}}^{h^3}$  (even though this certainty might be questioned by threshold effects at the Planck scale [Holthausen, Lim and Lindner '12](#))

Not totally clear yet if  $m_H$  is above  $M_{\text{stability}}$ , but rather important question since

- ☑ if  $m_H > M_{\text{stability}}$ , the Higgs could serve as an inflaton
- ☑ if  $m_H = M_{\text{stability}}$  the SM is asymptotically safe, ie consistent up to arbitrary high energy [Bezrukov et al '12](#)

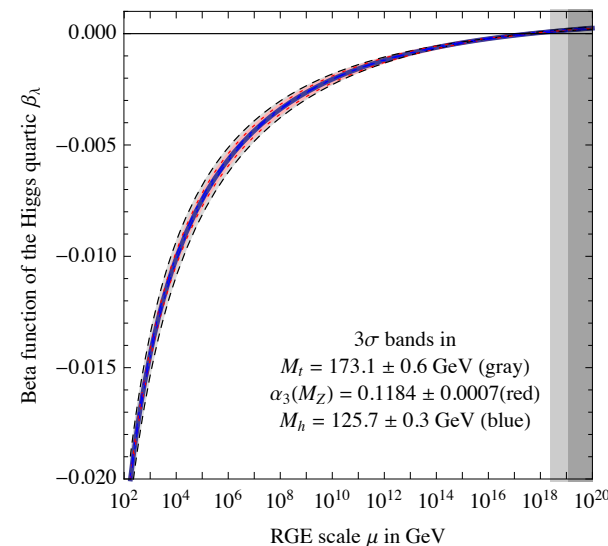
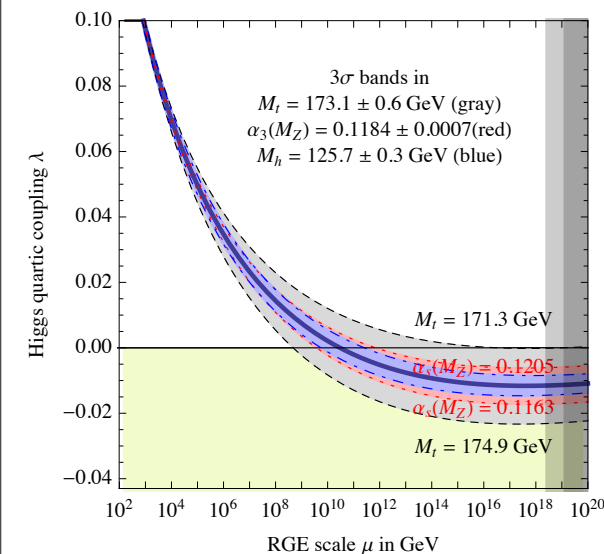
need precise Higgs&top mass/couplings (and  $\alpha_s$ ) measurements (ILC,  $\mu$  coll.)

and better understanding of pole vs MS top mass [Alekhin, Djouadi, Moch '12](#)



# From the EW scale to $M_{Pl}$ ... and return

Many of my theory colleagues started wild speculations/extrapolations



$$\lambda(M_{Pl}) = -0.0113 - 0.0065 \left( \frac{M_t}{\text{GeV}} - 173.10 \right) + \\ + 0.0018 \frac{\alpha_3(M_Z) - 0.1184}{0.0007} + 0.0029 \left( \frac{M_h}{\text{GeV}} - 125.66 \right)$$

Buttazzo et al '13

*Is the Higgs potential vanishing potential at  $M_{Pl}$ ?*

Froggatt, Nielsen, Takanishi '01

Arkani-Hamed et al '08

Shaposhnikov, Wetterich '09

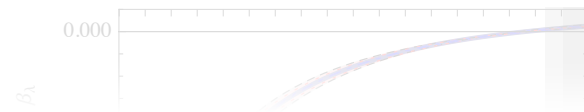
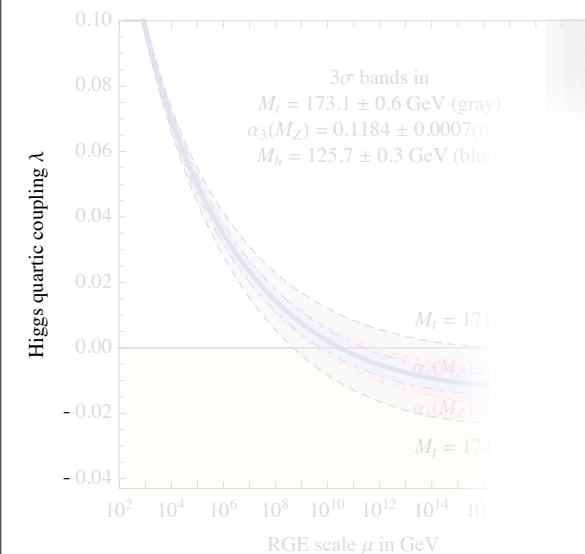
EWSB determined by Planck physics?  $M_{Pl}$  calculable from weak scale non-gravitational quantities?  
absence of new energy scale between the Fermi and the Planck scale?  
Anthropic vs. natural EWSB...

But these implications are based on the assumptions

- (1) that the 126 GeV particle observed is *\*exactly\** the SM Higgs
- (2) that the Dark Matter sector is decoupled from the weak sector

# From the EW scale to $M_{Pl}$ ... and return

Many of my theory colleagues started wild speculations/extrapolations



$$\lambda(M_{Pl}) = -0.0113 - 0.0065 \left( \frac{M_t}{\text{GeV}} - 173.10 \right) +$$

$$\frac{0.1184}{7} + 0.0029 \left( \frac{M_h}{\text{GeV}} - 125.66 \right)$$

Buttazzo et al '13

## SM/DM Couplings

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{DM}} + \epsilon \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{DM}}$$

ing potential at  $M_{Pl}$ ?

Jielsen, Takanishi '01

i-Hamed et al '08

nikov, Wetterich '09

*Expected*

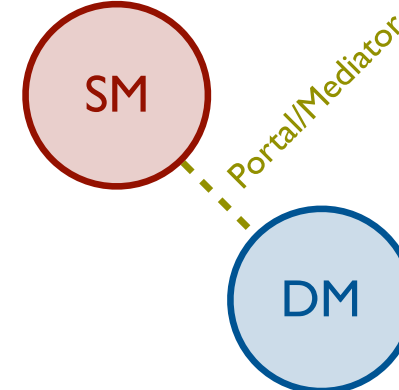
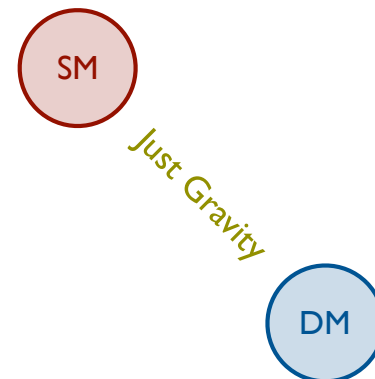
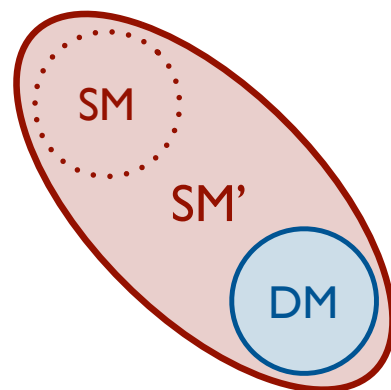
*Most exotic*

*Exotic*

Canonical WIMP

Nightmare Scenario

"Hidden Sectors"



$SM @ M_{Pl}$

Thaler HCP'10

gravitational quantities?  
 dark scale?

ions  
 e SM Higgs  
 weak sector

(1) that  
 (2) that

# How robust is the conclusion?

## BSM & STABILITY

Even without naturalness, BSM must exist...

Its impact on the Higgs instability can be

Example

IRRELEVANT

See-saw neutrinos

$$M_R \lesssim 10^{13} \text{ GeV}$$

MAKE IT WORSE

See-saw neutrinos

$$M_R \gtrsim 10^{13} \text{ GeV}$$

CURE IT

See-saw neutrinos

$$M_R \sim \langle S \rangle \quad \& \quad \lambda_{HS} |H|^2 |S|^2$$

Lebedev '12, Elias-Miro et al. '12

# Solution to the Higgs<sup>4</sup> Coupling Instabilities

find a symmetry such that

$$\lambda \equiv g^2$$

the Higgs quartic will inherit the good UV asymptotically free behavior of the gauge coupling

---

---

Examples of such symmetry:

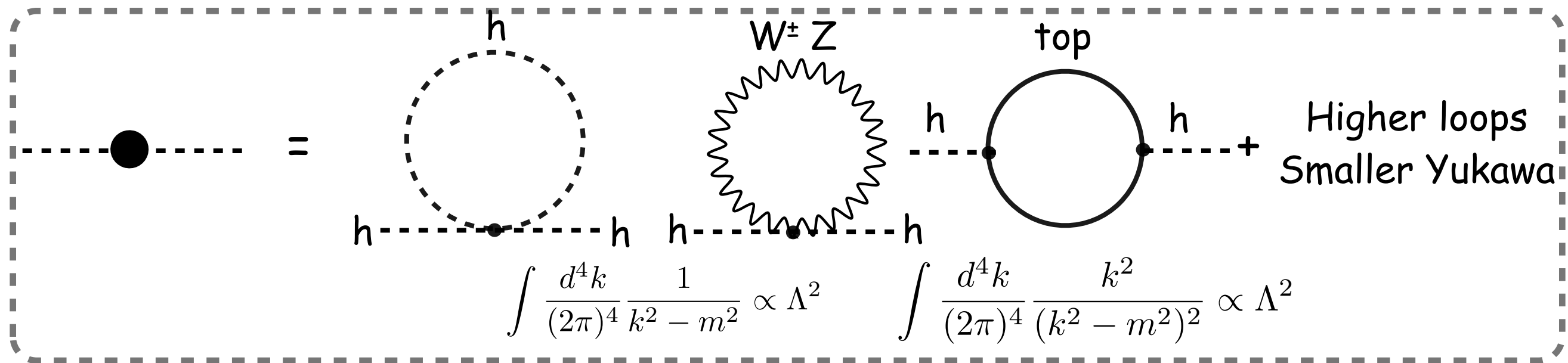
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- ✠ supersymmetry
- ✠ gauge-Higgs unification: the Higgs is identified as a component of the gauge field along some extra-dimensions.

# Quantum Instability of the Higgs Mass

so far we looked only at the RG evolution of the Higgs quartic coupling (dimensionless parameter). The Higgs mass has a totally different behavior: it is highly dependent on the UV physics, which leads to the so called hierarchy problem



Weisskopf '39  
't hooft '79

$$\delta m_H^2 = (2m_W^2 + m_Z^2 + m_H^2 - 4m_t^2) \frac{3G_F \Lambda^2}{8\sqrt{2}\pi^2}$$

$$m_H^2 \sim m_0^2 - (115 \text{ GeV})^2 \left( \frac{\Lambda}{700 \text{ GeV}} \right)^2$$

# $\Lambda^2$ from the Coleman-Weinberg Potential



exercise

$$V(h) = \int \frac{d^4 k_E}{2(2\pi)^4} \text{STr} \ln (k_E^2 + M^2(h))$$



$$V(h) = -\frac{\Lambda^4}{128\pi^2} \text{STr} 1 + \frac{\Lambda^2}{32\pi^2} \text{STr} M^2(h) + \frac{1}{64\pi^2} \text{STr} M^4(h) \ln \frac{M^2(h)}{\Lambda^2}$$

$$M_W^2 = \frac{1}{4} g^2 h^2$$

$2 \times 3$

$$M_Z^2 = \frac{1}{4} (g^2 + g'^2) h^2$$

$3$

$$M_t^2 = \frac{1}{2} y_t^2 h^2$$

$4 \times 3$

$$M_H^2 = \lambda (3h^2 - v^2)$$

$1$

$$M_G^2 = \lambda (h^2 - v^2)$$

$3$

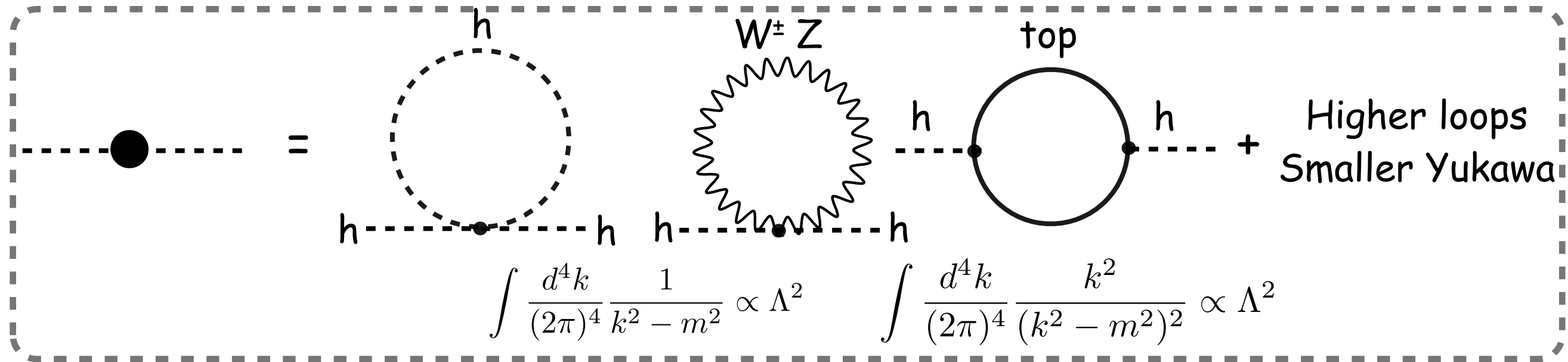
$h$  dependent masses away from the true vacuum  
(for  $h=v$ , we recover the usual expression  
for the Higgs mass  
and the Goldstone are massless)

$$V(h) = (2m_W^2 + m_Z^2 + m_H^2 - 4m_t^2) \frac{3G_F \Lambda^2}{32\sqrt{2}\pi^2} h^2$$

in agreement with the loop computation

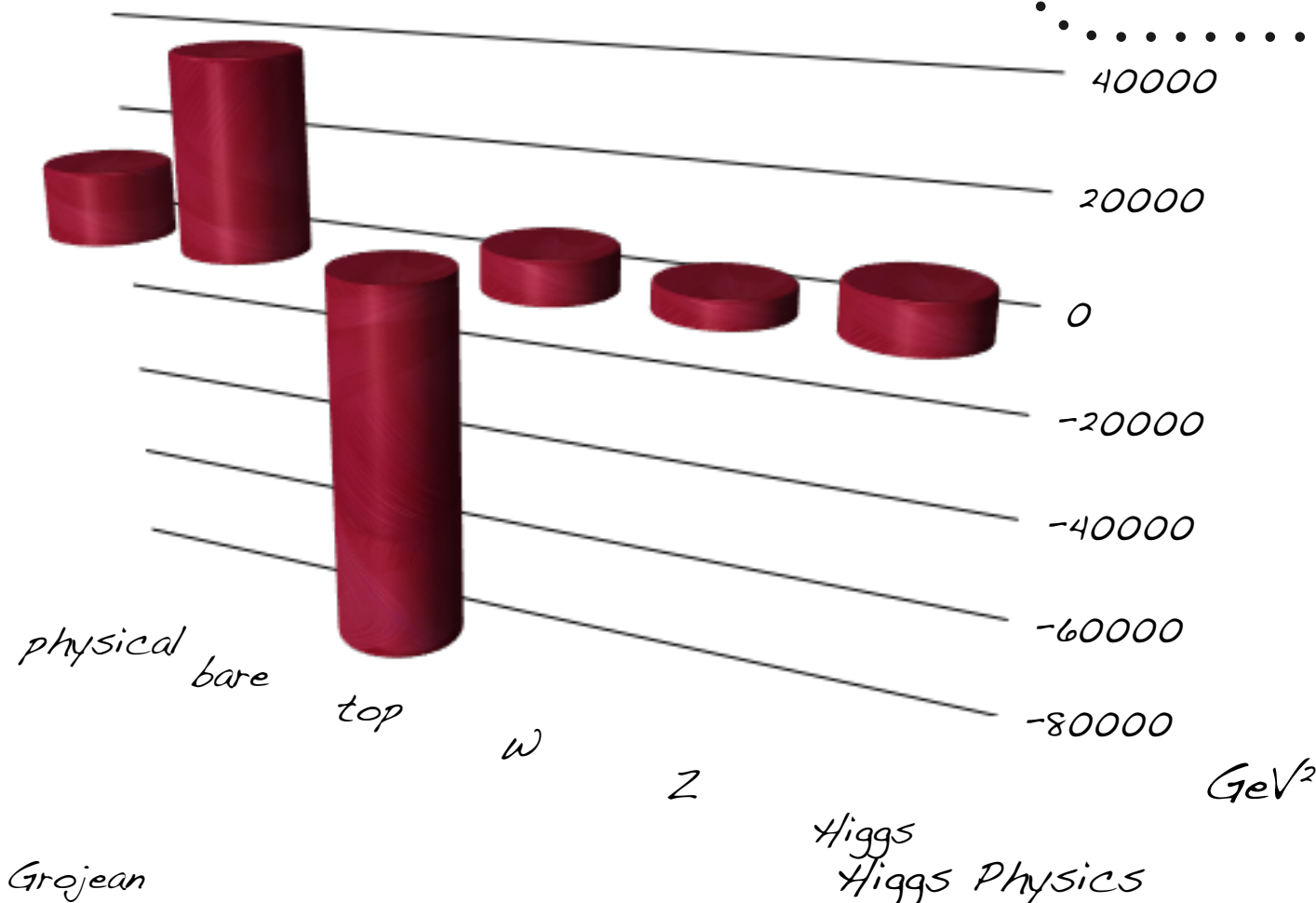


# Quantum Instability of the Higgs Mass

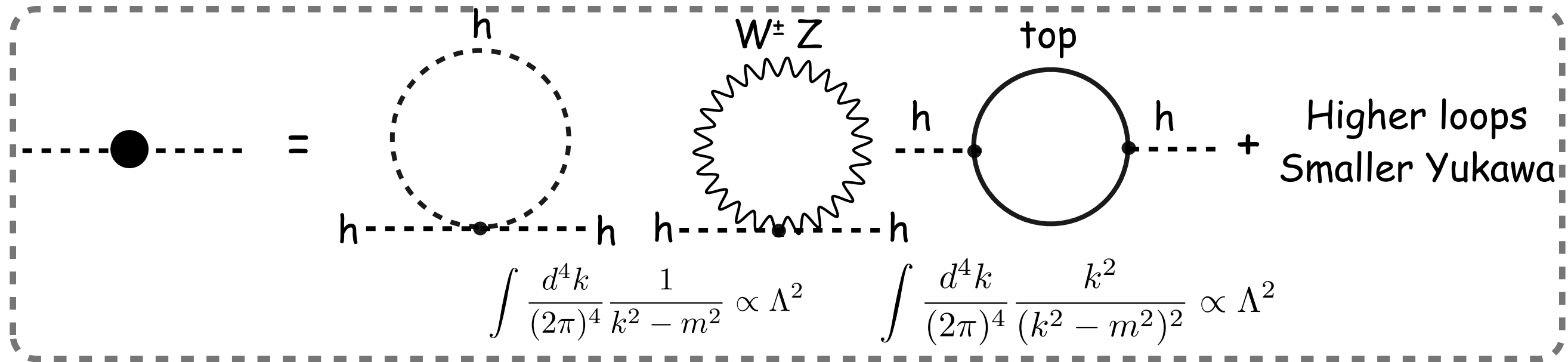


$$\Lambda = 1 \text{ TeV}$$

$$m_H^2 \sim m_0^2 - (115 \text{ GeV})^2 \left( \frac{\Lambda}{700 \text{ GeV}} \right)^2$$

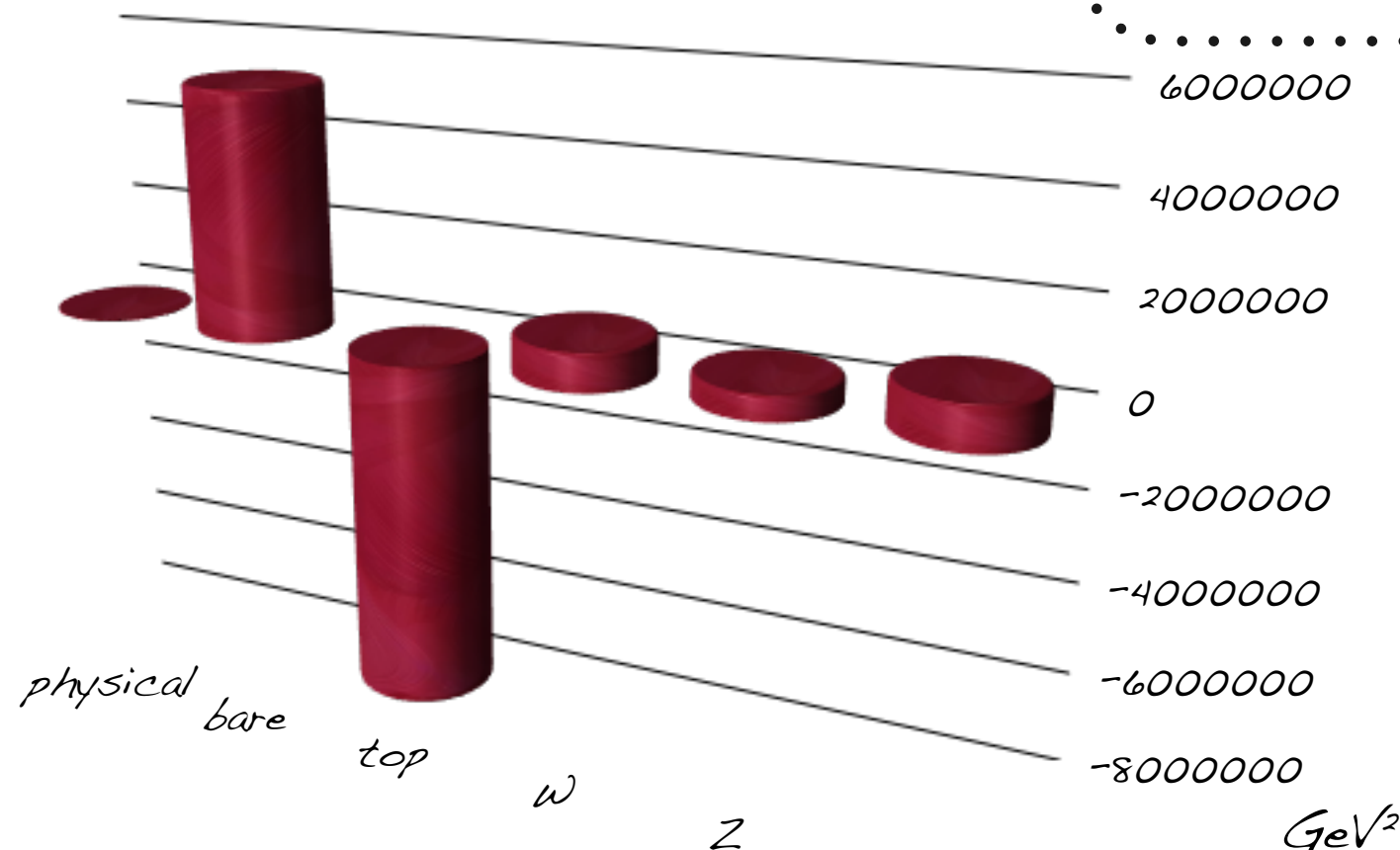


# Quantum Instability of the Higgs Mass



$$\Lambda = 10 \text{ TeV}$$

$$m_H^2 \sim m_0^2 - (115 \text{ GeV})^2 \left( \frac{\Lambda}{700 \text{ GeV}} \right)^2$$



# Playing with $\Lambda^2$ : Veltman throat

$$\delta m_H^2 = (2m_W^2 + m_Z^2 + m_H^2 - 4m_t^2) \frac{3G_F \Lambda^2}{16\sqrt{2}\pi^2}$$

People taking the  $\Lambda^2$  terms literally would say it is possible to cure the hierarchy pb if

$$m_H^2 = 4m_t^2 - 2m_W^2 - m_Z^2 \approx (320 \text{ GeV})^2$$

This is a too naive interpretation

- in the absence of any symmetry, there is no reason to use the same cutoff for all particles
- the throat doesn't survive at higher loop order
- it would anyway require a very particular value of the Higgs mass that it is not dictated by any symmetry

# What the hell is the meaning of $\Lambda^2$ ?

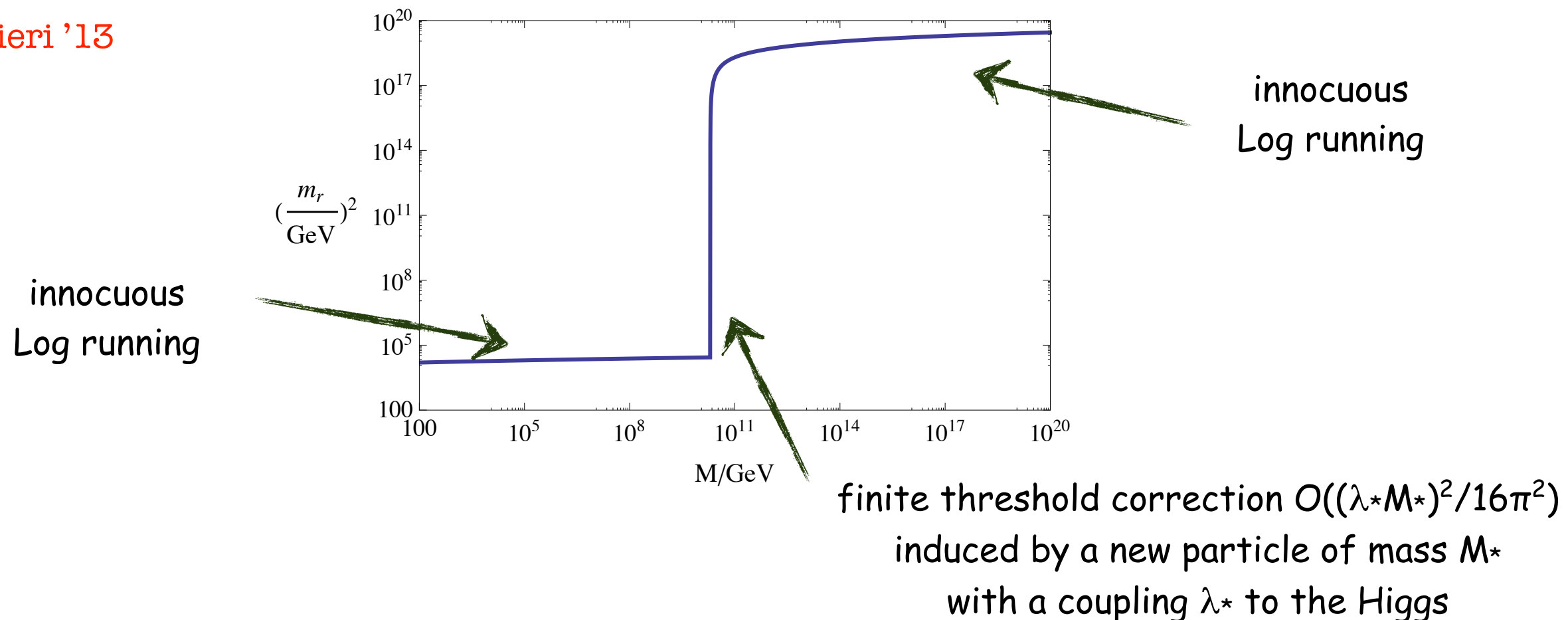
It is often argued that  $\Lambda^2$  terms have no meaning since they are put to 0 in dim. reg.  
hence the believe that there is no hierarchy pb!

THIS IS TRUE IN THE SM

the hierarchy pb exists only when multiple scales are present

The hierarchy pb can be seen when dealing with the renormalized running Higgs mass

e.g. Barbieri '13



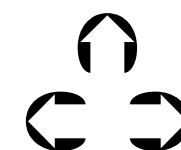
Need to tune  $O((m_h/M^*)^2)$  the value of  $m_H$  at high scale to reproduce  $m_H(\text{EW})$   
UV sensitivity



[picture courtesy of A. Weiler]



# *Symmetries for a natural EWSB*



# How to Stabilize the Higgs Potential

## Goldstone's Theorem

spontaneously broken global symmetry  $\Rightarrow$  massless scalar

... but the Higgs has sizable non-derivative couplings

## The spin trick

$2s+1$  polarization states

a particle of spin  $s$ :

...with the only exception of a particle moving at the speed of light

... fewer polarization states

Spin 1    Gauge invariance  $\longrightarrow$  no longitudinal polarization

Spin 1/2    Chiral symmetry  $\longrightarrow$  only one helicity

$\searrow$   
 $\nearrow$   $m=0$

... but the Higgs is a spin 0 particle



# Naturalness

't Hooft naturality: a number is naturally small when the symmetry of the theory increases as the parameter is set to zero

Spin 1/2  $\begin{pmatrix} \chi \\ \psi \end{pmatrix}$

$$-i\bar{\chi}\bar{\sigma}^\mu\partial_\mu\chi - i\psi\sigma^\mu\partial_\mu\bar{\psi} + m(\chi\psi + \bar{\chi}\bar{\psi})$$

invariant under  $\chi \rightarrow e^{i\alpha}\chi$   
 $\psi \rightarrow e^{-i\alpha}\psi$

if  $m = 0$ ,  
 also invariant under  $\chi \rightarrow e^{i\alpha}\chi$   
 $\psi \rightarrow e^{i\alpha}\psi$

Spin 1

$$-\frac{1}{4}(\partial_\mu A_\nu - \partial_\nu A_\mu)(\partial^\mu A^\nu - \partial^\nu A^\mu) - \frac{1}{2}m^2 A_\mu A^\mu$$

iff  $m = 0$ ,  
 invariant under  $A_\mu \rightarrow A_\mu + \partial_\mu\epsilon$

# Symmetries to Stabilize a Scalar Potential

Supersymmetry

fermion  $\sim$  boson

Higher Dimensional  
Lorentz invariance

$\Leftarrow$  gauge-Higgs  
unification models

[Manton '79, Fairlie '79, Hosotani '83 +...]

$$A_\mu \sim A_5$$

4D spin 1

4D spin 0

These symmetries cannot be exact symmetry of the Nature.  
They have to be broken. We want to look for a soft breaking in  
order to preserve the stabilization of the weak scale.

# Other symmetries?

Ghost symmetry

Grinstein, O'Connell, Wise '07

SM particle  $\sim$  ghost

It was known since Pauli-Villars that ghosts can soften the UV behavior of the propagators. But they are unstable per se.

Lee-Wick in the 60's proposed a trick to stabilize the ghosts (at the price of a violation of causality at the microscopic scale).

# What amount conformal invariance?

SM is nearly scale invariant classically

and scale invariance will forbid any Higgs mass term

SM mass and running couplings break conformal invariance

but maybe conformal symmetry is only “softly” broken and restored at high energy

Bardeen '95

$U(1)_Y$  and gravity grow in the UV  $\Rightarrow$  large conformal breaking

one needs a transition between SM and Conformal Field Theory behavior

w/ particles @ transition scale



usual hierarchy pb



w/o particles @ transition scale



it was shown that the anomalous dimensions of the operators coupled to the Higgs change at the threshold and this reintroduces a fine-tuning unless the threshold is around the weak scale

Marques Tavares, Schmaltz, Skiaba '13

Not totally impossible scenario but requires some unknown dynamics

# EWSB might be unnatural

nothing to say but the usual words:

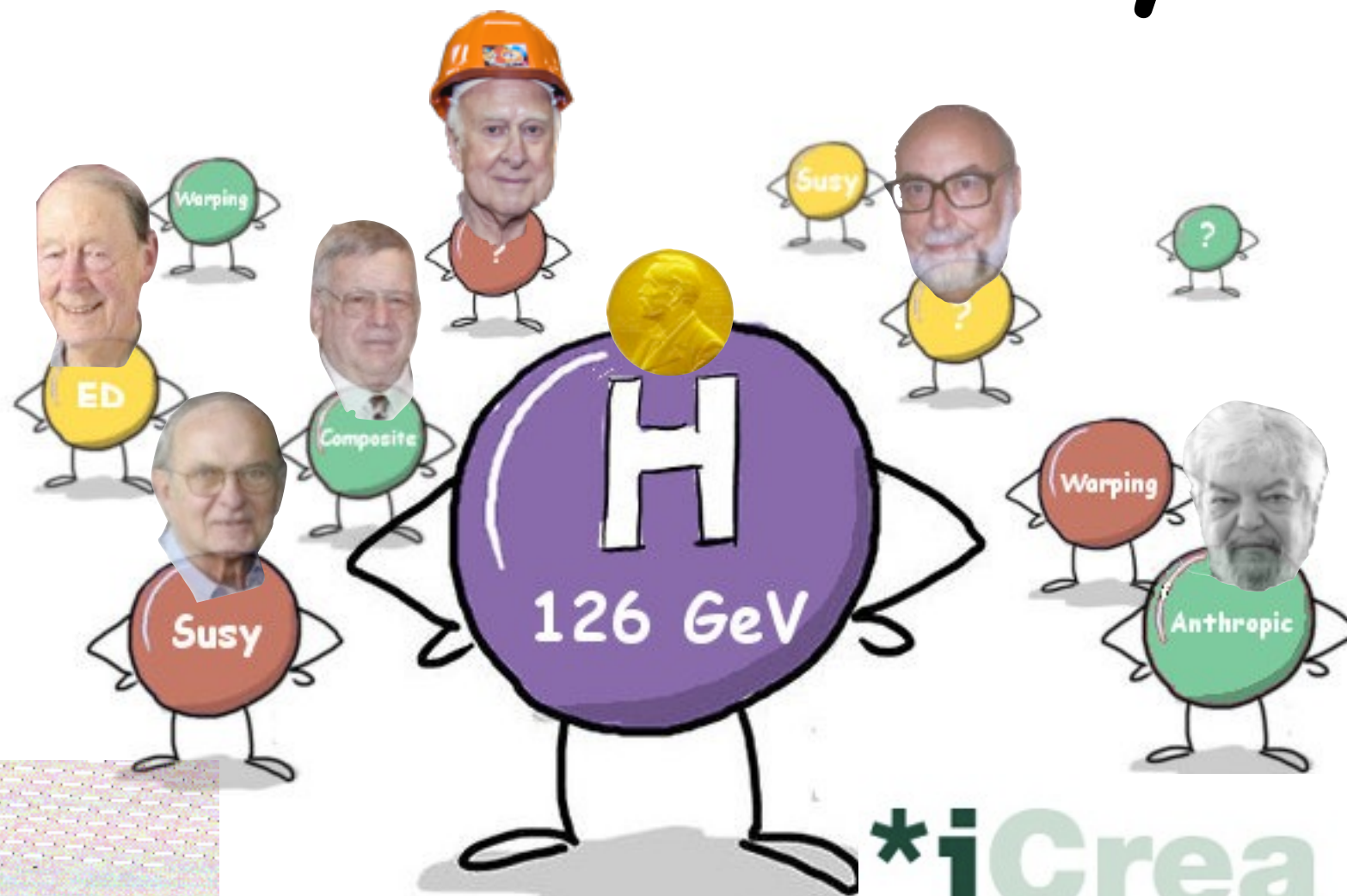
- cosmological constant problem...
- multiverse...
- landscape of vacua...
- laws of physics are environmental...
- anthropic solution...
- end of reductionism...

will be tested to an unprecedented level ( $10^{-4}$ )

if we lose naturalness,  
what should be the guiding principle towards our  
understanding of physics at higher and higher energies?

# Higgs Physics within and beyond the SM

*IFIC, Valencia, May 2015*



P. Cámara/C. Grojean

**\*iCrea**

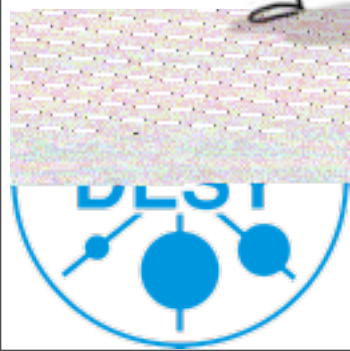
INSTITUCIÓ CATALANA DE  
RECERCA I ESTUDIS AVANÇATS

*Christophe Grojean*

DESY (Hamburg)

ICREA@IFAE (Barcelona)

( [christophe.grojean@cern.ch](mailto:christophe.grojean@cern.ch) )





# Disclaimer

These are slides that I've prepared for some lectures at the CERN-Latin American School of High Energy Physics last March in Ecuador.

There is partial overlap with what I covered during my blackboard lectures at IFIC even though some parts are missing in these notes.

Do not hesitate to contact me by email if you have any comments or questions.  
And please, report any typo/mistake that you might find in these notes.

# Lecture Outline

1

## First Lecture $\supset$

- Standard Model and EW symmetry breaking  $\supset$
- Higgs mechanism - custodial symmetry  $\supset$
- Goldstone equivalence theorem  $\supset$
- What is the Higgs boson the name of?  $\supset$
- SM Higgs @ colliders  $\supset$
- UV behavior of the Higgs boson (triviality, stability, naturality)  $\supset$
- Symmetries for a natural EWSB  $\supset$

2

## Second Lecture $\supset$

- Implications for SUSY  $\supset$
- Composite Higgs models  $\supset$
- Precision Higgs couplings  $\supset$
- Future Higgs channels:
  - Boosted and off-shell channels  $\supset$
  - Multi-Higgs  $\supset$

1 2

# We all have a Post higgs Depression

For the first time in the history of physics,  
we have a \*consistent\* description of the fundamental constituents of matter and their interactions and this description can be extrapolated to very high energy (up  $M_{\text{Planck}}$ ?)

## My key message MLM@Aspen'14

- The days of “guaranteed” discoveries or of no-lose theorems in particle physics are over, at least for the time being ....
- .... but the big questions of our field remain wild open (hierarchy problem, flavour, neutrinos, DM, BAU, .... )
- This simply implies that, more than for the past 30 years, future HEP's progress is to be driven by experimental exploration, possibly renouncing/reviewing deeply rooted theoretical bias

Where and how does the SM break down?  
Which machine(s) will reveal this breakdown?

# HEP with a Higgs boson

*"If you don't have the ball, you cannot score"*



# HEP with a Higgs boson

*"If you don't have the ball, you cannot score"*

Now with the Higgs boson in their hands,  
particle physicists can... play as well as the Barça players

## Higgs as a target

- observe it in as many channels as possible to measure its properties
- check of the coupling structure of the SM and its deformations
- interpret deviations of Higgs couplings as a sign of NP

## Higgs as a tool

- a portal to New Physics
- in initial states: rare decays (BSM Higgs decays)

e.g.,  $h \rightarrow \mu\tau$ ,  $h \rightarrow J/\Psi + \gamma$

- in final states as an object that can be reconstructed and tagged (BSM Higgs productions)

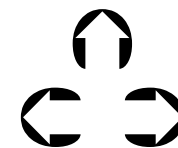
e.g.,  $t \rightarrow h + c$ ,  $H \rightarrow hh$

Profound change in paradigm:

missing SM particle  $\Rightarrow$  tool to explore SM and venture into physics landscape beyond



# Implications for SUSY





# Is SUSY/MSSM Natural?

The Higgs mass is calculable in the MSSM

$$m_h^2 = M_Z^2 \cos^2 2\beta + \delta_t^2$$

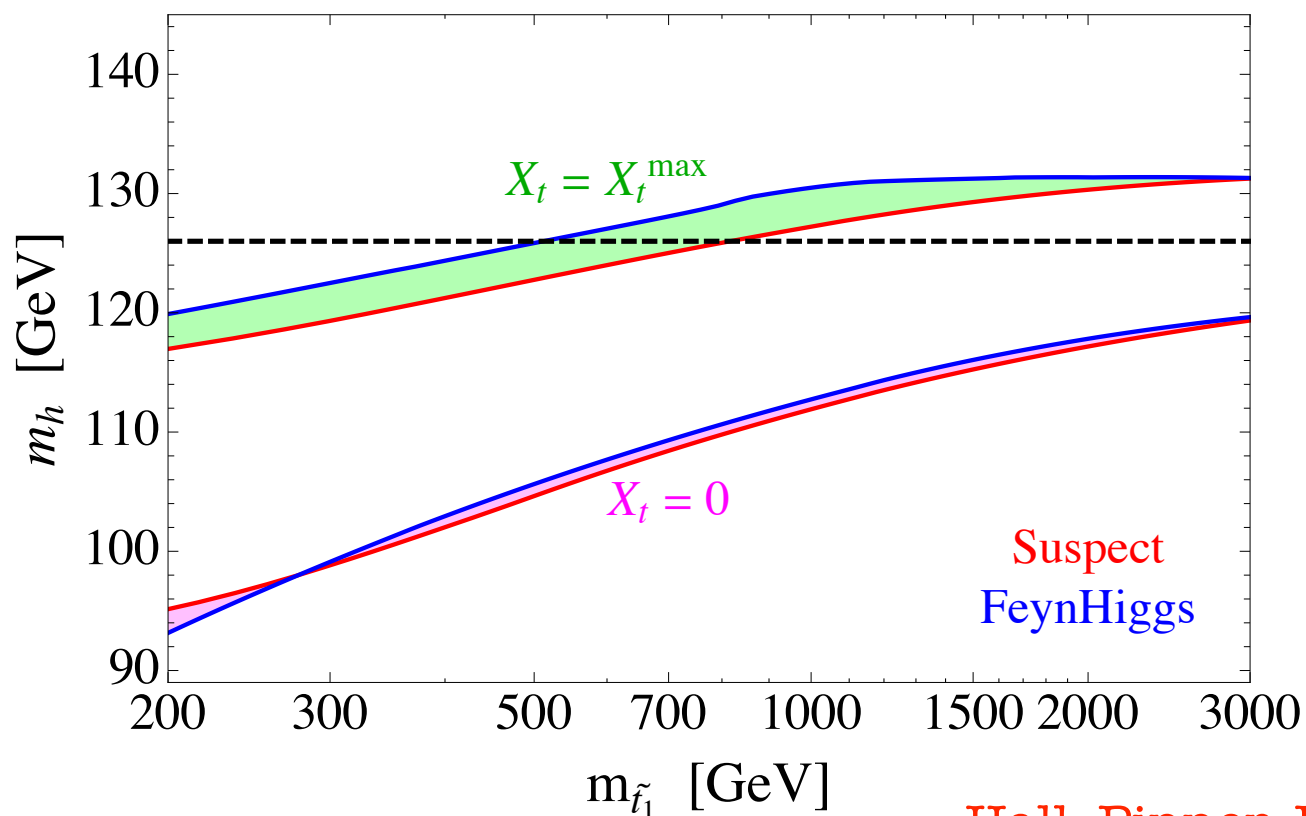
$\swarrow$   $(125 \text{ GeV})^2$ 
 $\swarrow$   $(\geq 87 \text{ GeV})^2$

$$\delta_t^2 \approx \frac{3\sqrt{2}G_F M_t^4}{16\pi^2} \left[ \log \frac{M_t^2}{M_{\tilde{t}}^2} + \frac{X_t^2}{M_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12M_{\tilde{t}}^2} \right) \right]$$

$M_{\tilde{t}}$  stop mass (degenerate)  
 $X_t$  stop mixing

substantial loop contribution from stops

MSSM Higgs Mass



large mixing  
heavy stops

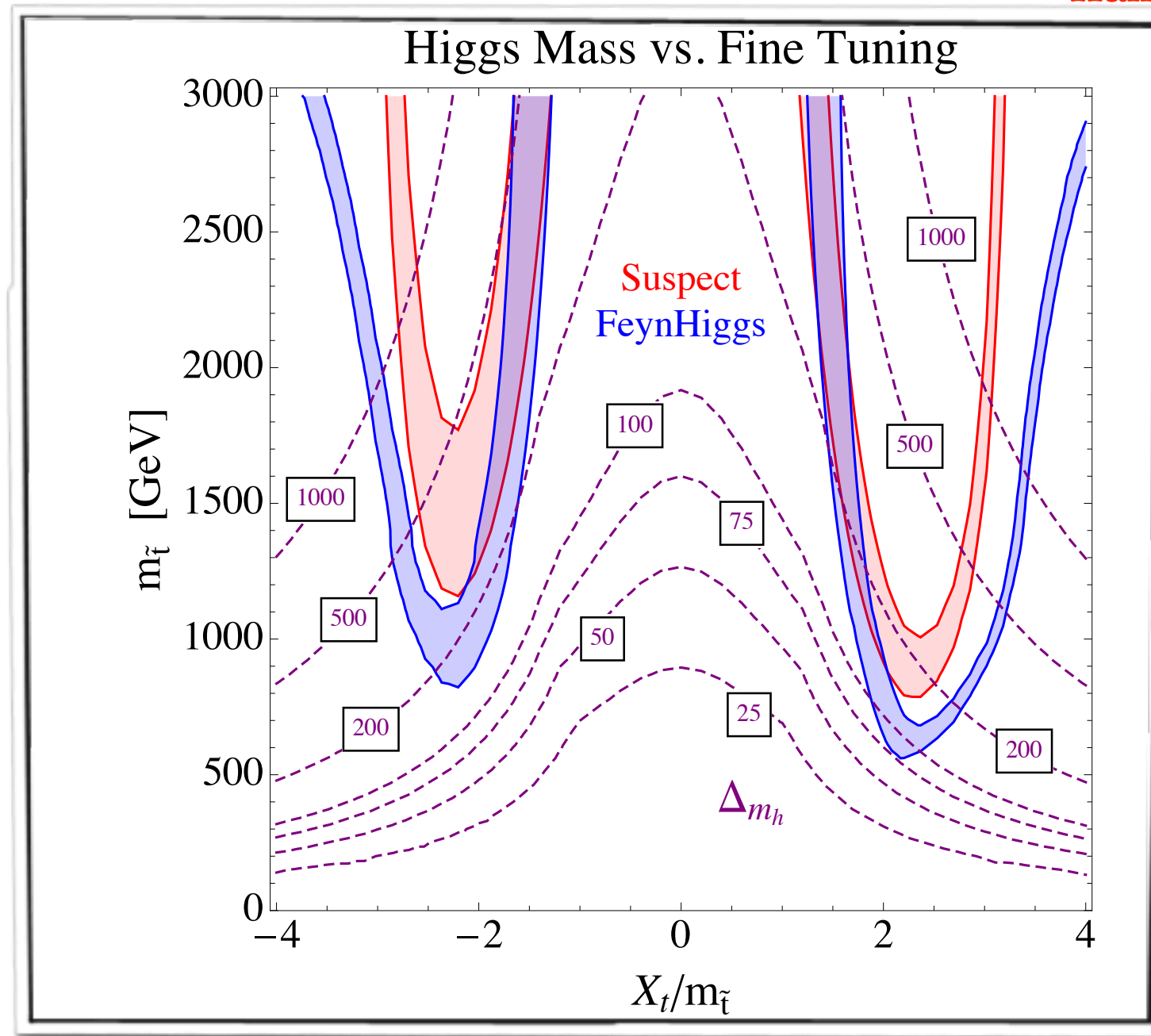
$$\sqrt{m_{Q_3} m_{u_3}} \gtrsim 700 \text{ GeV}$$

$\Downarrow \Downarrow$   
fine-tuning  $\geq 1\%$

Hall, Pinner, Ruderman '11  
+ many similar analyses

# MSSM fine-tuning

Hall, Pinner, Ruderman '11



maximal mixing  
requires  
engineering

$$m_{\tilde{t}}^2(M_Z) \simeq 5.0 M_3^2(M_G) + 0.6 m_{\tilde{t}}^2(M_G)$$

$$A_t(M_Z) \simeq -2.3 M_3(M_G) + 0.2 A_t(M_G)$$

... generically  $|A_t/m_{\tilde{t}}| \leq 1$

Fermisek, Kim '06

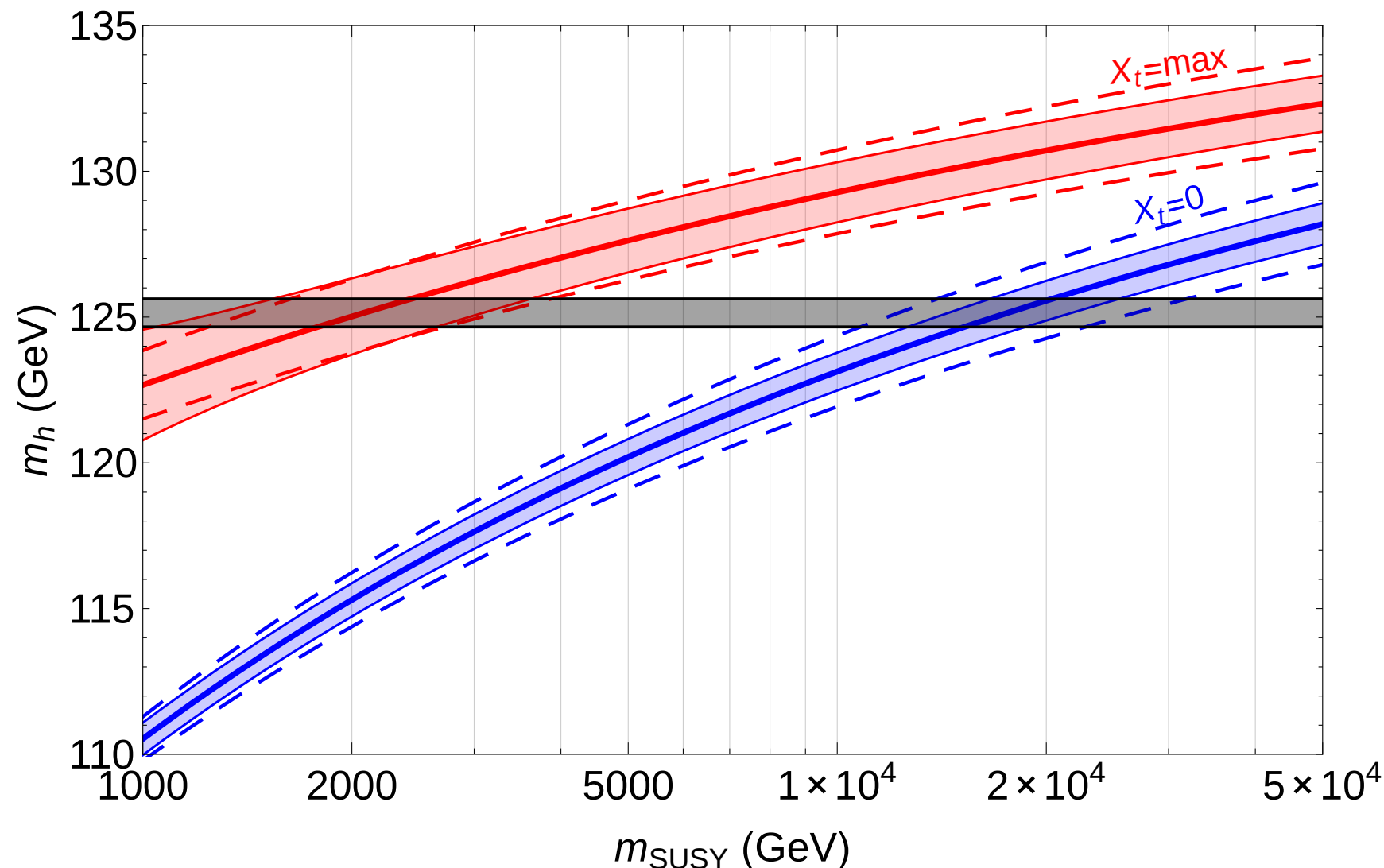
# Towards precise prediction of MSSM Higgs mass

further improved predictions (full 2-loop QCD corrections)

Bagnaschi et al '14

Degrassi et al '14

Pedro Vega, Villadoro 'to appear



requires  
even heavier stops  
to accommodate  
a 125 GeV Higgs

[plot from J. Pedro Vega and G. Villadoro, 'to appear]

# Saving SUSY

SUSY is Natural  
but not plain vanilla

❌ ~~CMSSM~~

❌ pMSSM

❌ NMSSM

❌ Hide SUSY, e.g. smaller phase space

▶ reduce production (eg. split families)

Mahbubani et al

▶ reduce MET (e.g. ~~R-parity~~, compressed spectrum)

Csaki et al

▶ dilute MET (decay to invisible particles with more invisible particles)

▶ soften MET (stealth susy, stop -top degeneracy)

Fan et al

**LHC<sub>100fb-1</sub> will tell!**

Good coverage of  
hidden natural susy

▶ mono-top searches (DM, flavored naturalness - mixing among different squark flavors-, stop-higgsino mixings)

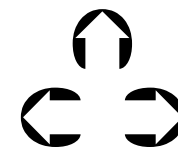
▶ mono-jet searches with ISR recoil (compressed spectra)

▶ precise tt inclusive measurement+ spin correlations (stop → top + very soft neutralino)

▶ multi-hard-jets (RPV, hidden valleys, long decay chains)



# Composite Higgs models



# Why should you care about compositeness?

Higgs compositeness means new fundamental interactions

## Pospelov's 38 years rule...

38 years rule = new forces of nature are discovered every 38 years for the last 150 yrs

1. 1860s – first papers of Maxwell on EM. Light is EM excitation. E & M unification.
2. 1897 – Becquerel discovers radioactivity – first evidence of weak charged currents (in retrospect).
3. 1935 – Chadwick gets NP for his discovery of neutron with subsequent checks that there exists strong n-p interaction. Strong force is established.
4. 1973 – Gargamelle experiment sees the evidence for weak neutral currents in  $\nu$ -N scattering
5. 2011/2012 Discovery of the Higgs, i.e. new Yukawa force.
6. *Prediction: Discovery of a new dark force – 2050?*

(+/- 2 years or so).

M. Pospelov, SHiP collab. meeting, Naples '15



# Why should you care about compositeness?

All SM shortcomings are intimately linked to the Higgs elementary nature

$$\mathcal{L}_{\text{Higgs}} = V_0 - \mu^2 H^\dagger H + \lambda (H^\dagger H)^2 + (y_{ij} \bar{\psi}_{Li} \psi_{Rj} H + h.c.)$$



*vacuum energy*  
*cosmological constant*

$$V_0 \approx (2 \times 10^{-3} \text{ eV})^4 \ll M_{\text{Pl}}^4$$



*hierarchy problem*

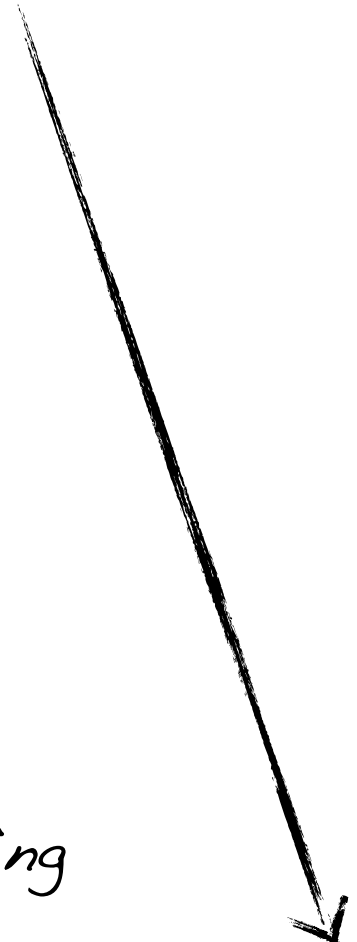
$$m_H \approx 100 \text{ GeV} \ll M_{\text{Pl}}$$



*triviality/stability*  
*of EW vacuum*



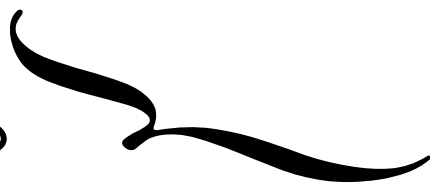
*mass and mixing*  
*hierarchy*



*flavour & CP:*  
*no FCNC, small CP*

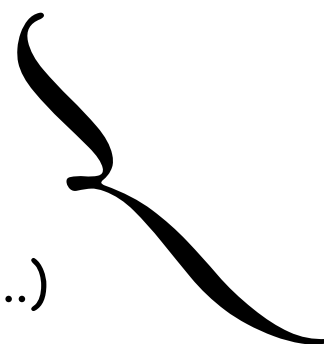
*String?*

*SUSY?*  
*TeV New Physics?*



*well described*  
*experimentally by CKM*

*(up to a few exceptions:  $A_{\text{FB}}^{t\bar{t}}$ ,  $\Delta A_{\text{CP}}^c$ ...)*



# Why should you care about compositeness?

All SM shortcomings are intimately linked to the Higgs elementary nature

$$\mathcal{L}_{\text{Higgs}} = V_0 - \mu^2 H^\dagger H + \lambda (H^\dagger H)^2 + (y_{ij} \bar{\psi}_{Li} \psi_{Rj} H + h.c.)$$



*vacuum energy*  
*cosmological constant*

$$V_0 \approx (2 \times 10^{-3} \text{ eV})^4 \ll M_{\text{Pl}}^4$$



*hierarchy problem*

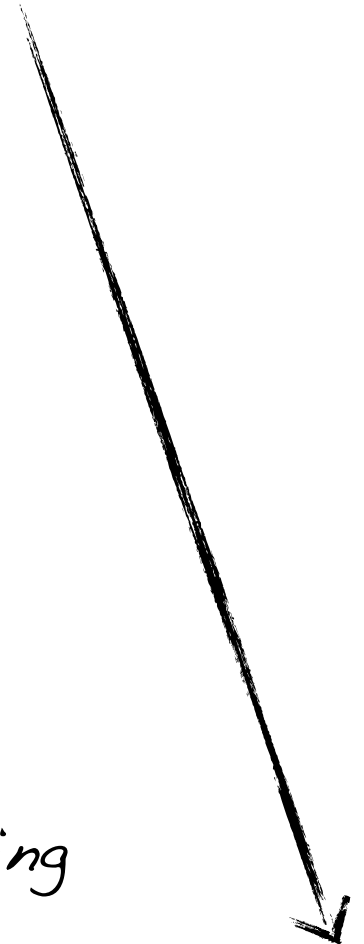
$$m_H \approx 100 \text{ GeV} \ll M_{\text{Pl}}$$



*triviality/stability*  
*of EW vacuum*



*mass and mixing*  
*hierarchy*



*flavour & CP:*  
*no FCNC, small CP*

All these problems because the Higgs boson would be the first elementary particle whose interactions are not endowed with a gauge structure

## Higgs = Elementary or Composite?

# Which composite scenario?

## Minimal Composite Higgs

ex:  $SO(5)/SO(4)$

SILH

$$\xi = \frac{v^2}{f^2} \ll 1$$

*Strong sector*  
( $g^*, f$ )  
PNGB Higgs

$$g_{SM}^2 / g^*$$

*SM*  
( $g, g', y_+$ )

## Partly Composite Higgs

$$\xi = \frac{v^2}{f^2} \ll 1$$

*Strong sector*  
( $g^*, f$ )  
 ~~$\langle EW \rangle \sim 0$~~

$$g_{SM}^2 / g^*$$

*SM*  
( $g, g', y_+$ )

Higgs

## Bosonic Technicolor

Induced EWSB

$$\varepsilon = \frac{f}{v} \ll 1$$

*Strong sector*  
( $g^*, f$ )  
 ~~$\langle EW \rangle \sim f$~~

$$g_{SM}^2 / g^*$$

*SM*  
( $g, g', y_+$ )

Higgs

# Which composite scenario?

## Minimal Composite Higgs

SILH

$$\xi = \frac{v^2}{f^2} \ll 1$$

$$\frac{1}{f^2} (\partial_\mu |H|^2)^2$$

$$\frac{\lambda_4}{f^2} |H|^6$$

$$\kappa_V \equiv \frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = 1 + \xi$$

$$\kappa_3 \equiv \frac{g_{hhh}}{g_{hhh}^{\text{SM}}} = 1 + \xi$$

## Partly Composite Higgs

$$\xi = \frac{v^2}{f^2} \ll 1$$

$$\frac{\varepsilon^4}{f^2} (\partial_\mu |H|^2)^2$$

$$\frac{\varepsilon^6}{f^2} |H|^6$$

$$\kappa_V \equiv \frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = 1 + \varepsilon^4 \xi$$

$$\kappa_3 \equiv \frac{g_{hhh}}{g_{hhh}^{\text{SM}}} = 1 + \varepsilon^2 \frac{g_*^2 v^2}{m_h^2} \varepsilon^4 \xi$$

## Bosonic Technicolor

Induced EWSB

$$\varepsilon = \frac{f}{v} \ll 1$$

$$\frac{\varepsilon^4}{f^2} (\partial_\mu |H|^2)^2$$

$$\frac{\varepsilon^6}{f^2} |H|^6$$

$$\kappa_V \equiv \frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = 1 + \varepsilon^2$$

$$\kappa_3 \equiv \frac{g_{hhh}}{g_{hhh}^{\text{SM}}} = 1 + \mathcal{O}(1)$$

# Patterns of Higgs coupling deviations

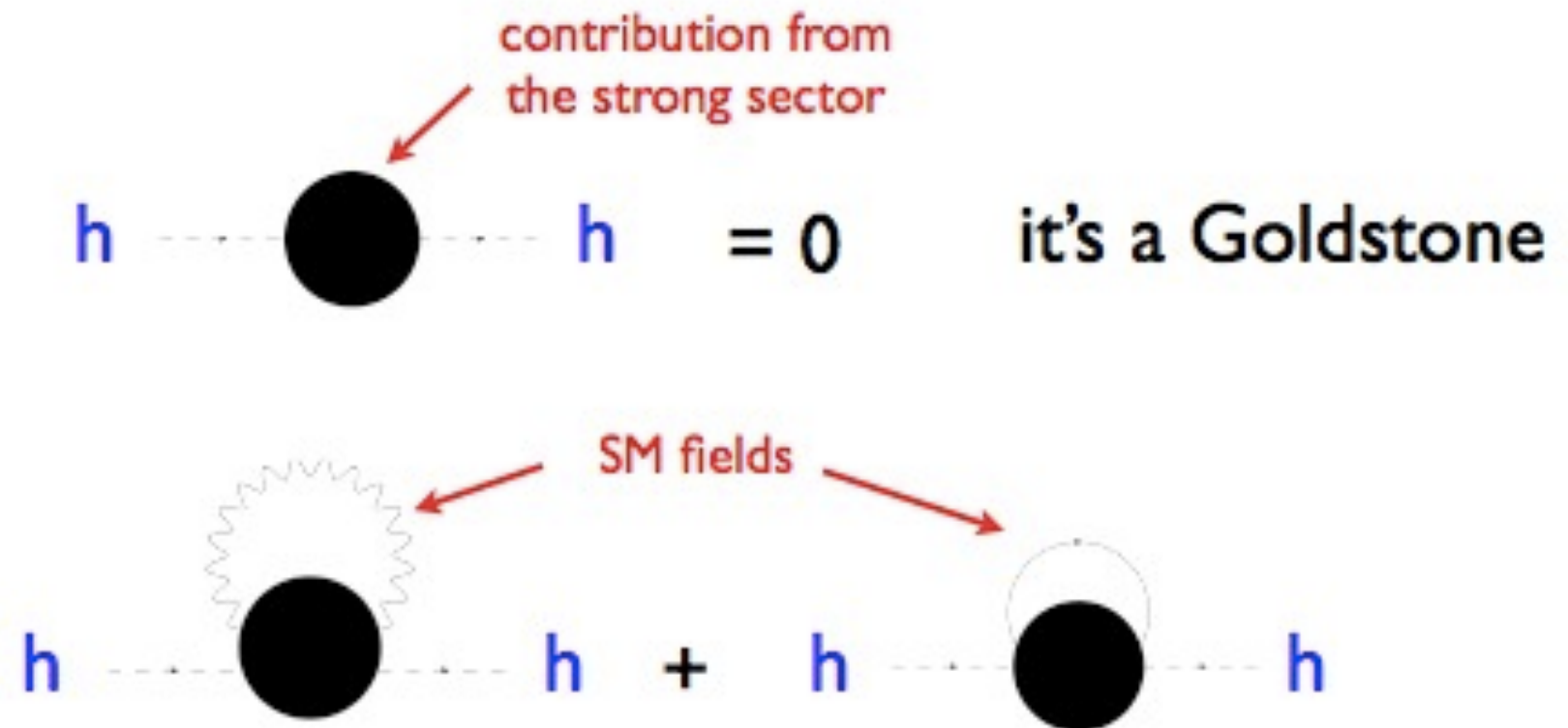
expected largest relative deviations

	hff	hVV	h $\gamma\gamma$	h $\gamma Z$	hGG	h <sup>3</sup>
<b>MSSM</b>	✓		✓	✓	✓	
<b>NMSSM</b>	✓	✓	✓	✓	✓	
<b>PGB Composite</b>	✓	✓		✓		✓
<b>SUSY Composite</b>	✓	✓	✓	✓	✓	✓
<b>SUSY partly-composite</b>			✓	✓	✓	✓
<b>“Bosonic TC”</b>						✓
<b>Higgs as a dilaton</b>			✓	✓	✓	✓

A. Pomarol, Naturalness '15

# Light composite Higgs from "light" resonances

The interactions between the strong sector and the SM generate a potential for the Higgs



Impossible to compute the details of the potential from first principles  
but using general properties on the asymptotic behavior of correlators  
(saturation of Weinberg sum rules with the first few lightest resonances)

it is possible to estimate the Higgs mass

Pomarol, Riva '12

$$m_h^2 \approx \frac{3}{\pi^2} \frac{m_t^2 m_Q^2}{f_{G/H}^2}$$



Marzocca, Serone, Shu '12

$$m_Q \lesssim 700 \text{ GeV} \left( \frac{m_h}{125 \text{ GeV}} \right) \left( \frac{160 \text{ GeV}}{m_t} \right) \left( \frac{f}{500 \text{ GeV}} \right)$$

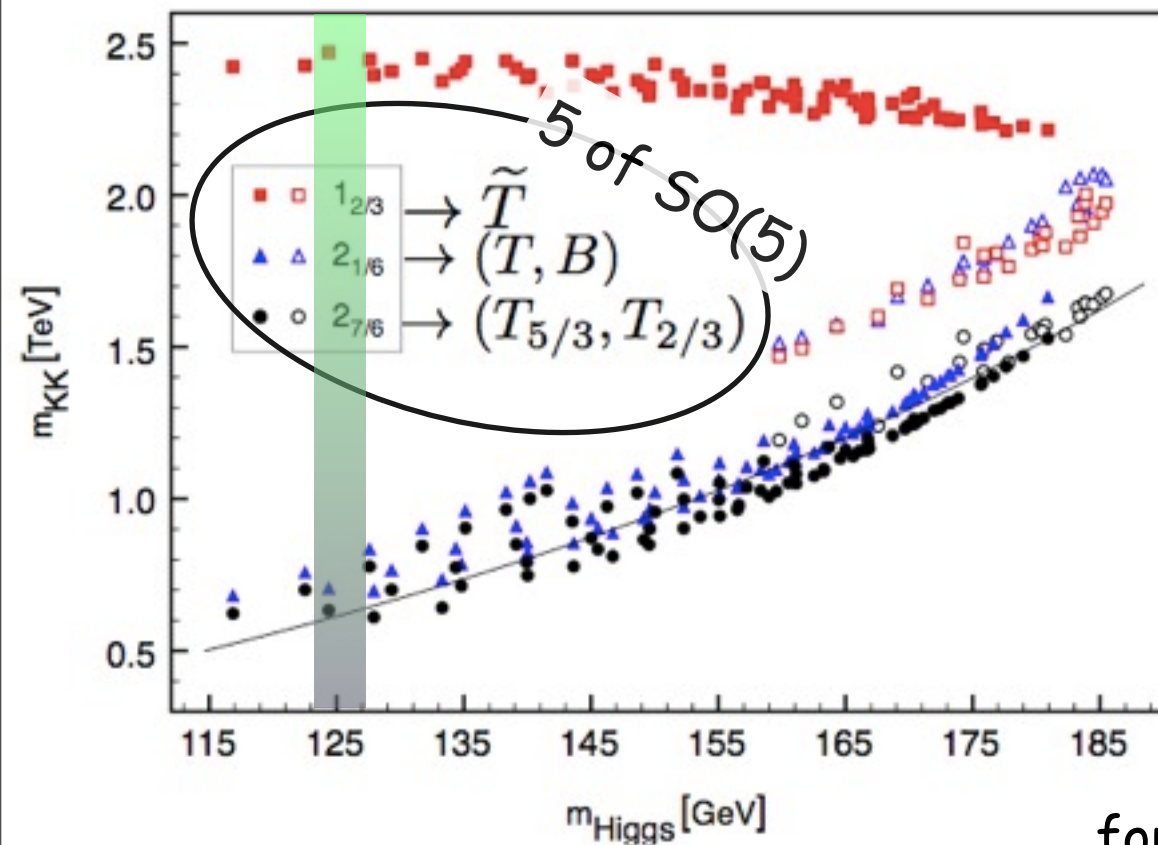
fermionic resonances below  $\sim 1 \text{ TeV}$   
vector resonances  $\sim \text{few TeV}$  (EW precision constraints)  
 $\sim$  for a natural ( $< 20\%$  fine-tuning) set-up  $\sim$



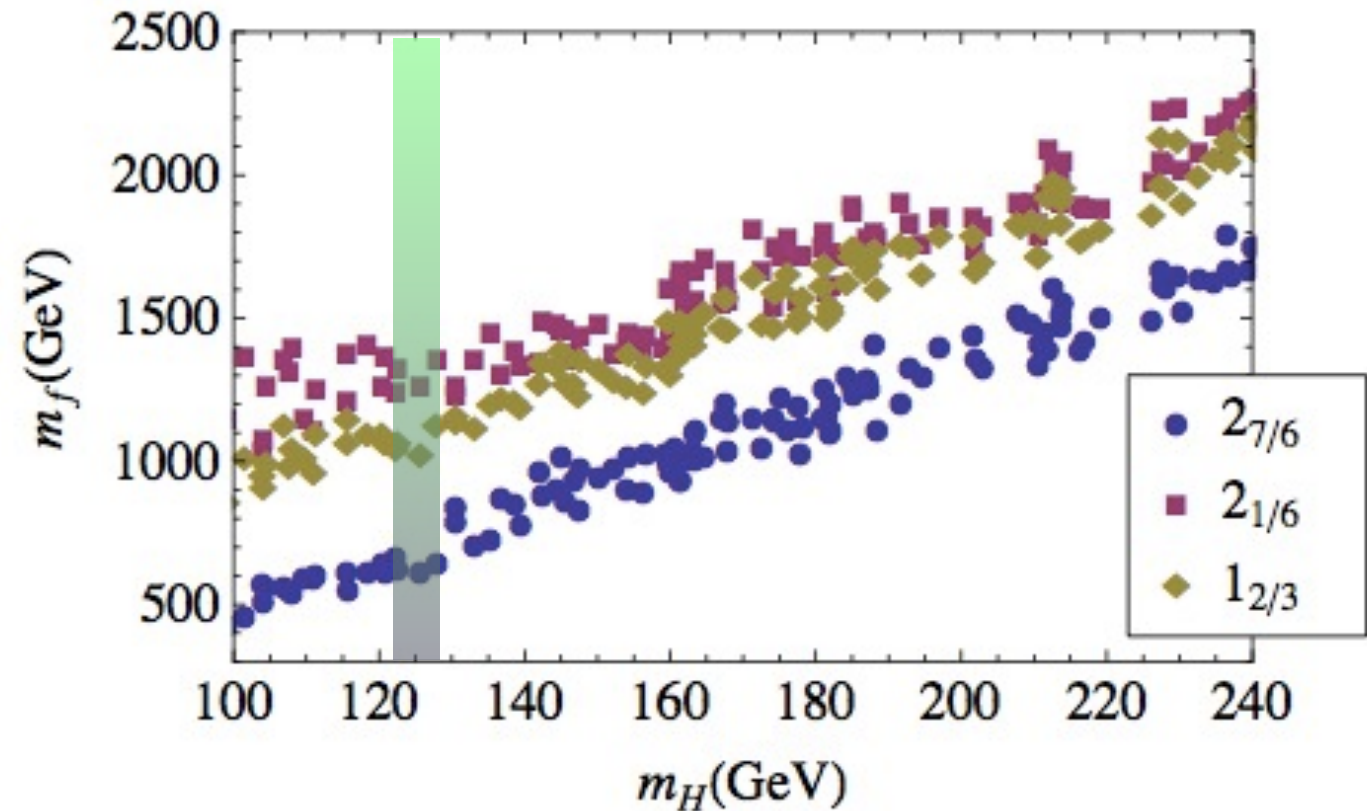
# Light composite Higgs from "light" resonances

true spectrum in explicit realizations

Contino, Da Rold, Pomarol '06



De Curtis, Redi, Tesi '11



for similar results, see also

Matsedonskyi, Panico, Wulzer '12

&

Marzocca, Serone, Shu '12

Nice AdS/CFT interpretation

$$\text{Dim}[\mathcal{O}_\Psi] = \frac{3}{2} + |M_\Psi + \frac{1}{2}|$$

$$M_\Psi = 1/2 \leftrightarrow \text{dim}[\mathcal{O}_\Psi] = 3/2 \leftrightarrow \text{light free field decoupled from CFT}$$

# Rich phenomenology of the top partners

## Search in same-sign di-lepton events

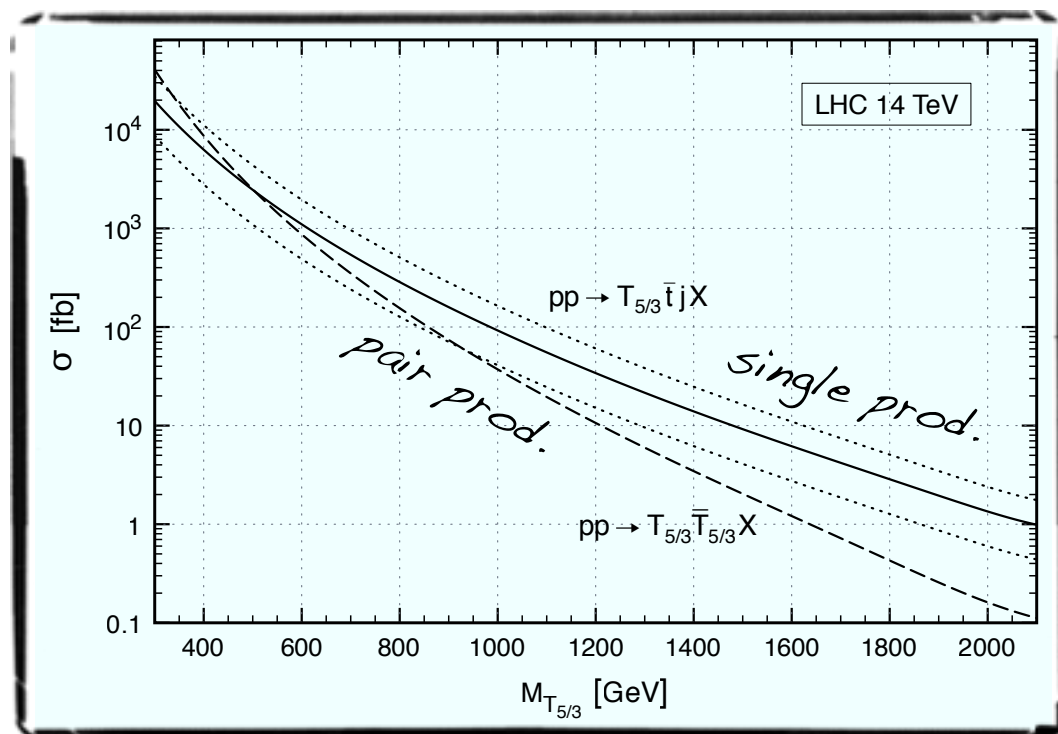
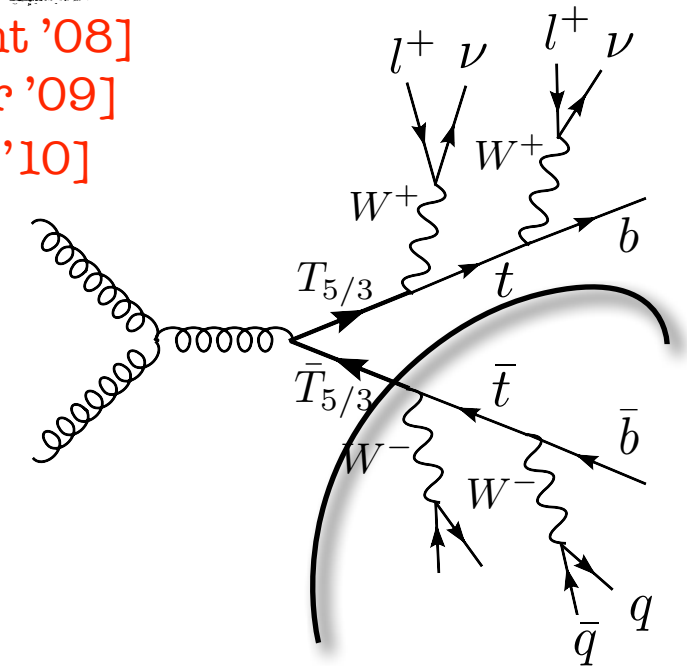
- $t\bar{t} + jets$  is not a background [except for charge mis-ID and fake  $e^-$ ]
- the resonant  $(tW)$  invariant mass can be reconstructed

discovery potential (LHC<sub>14TeV</sub>)

$M_{5/3} = 500 \text{ GeV}$  ( $\sigma \times BR \approx 100/\text{fb}$ )  $\rightarrow 56 \text{ pb}^{-1}$

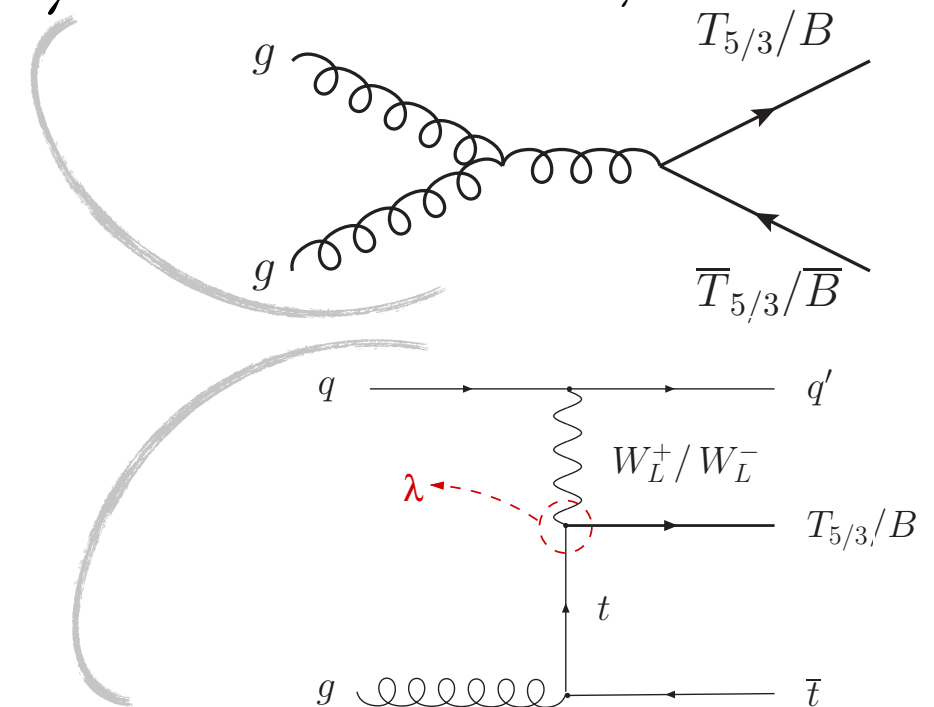
$M_{5/3} = 1 \text{ TeV}$  ( $\sigma \times BR \approx 2/\text{fb}$ )  $\rightarrow 15 \text{ fb}^{-1}$

[Contino, Servant '08]  
[Mrazek, Wulzer '09]  
[Dissertori et al '10]



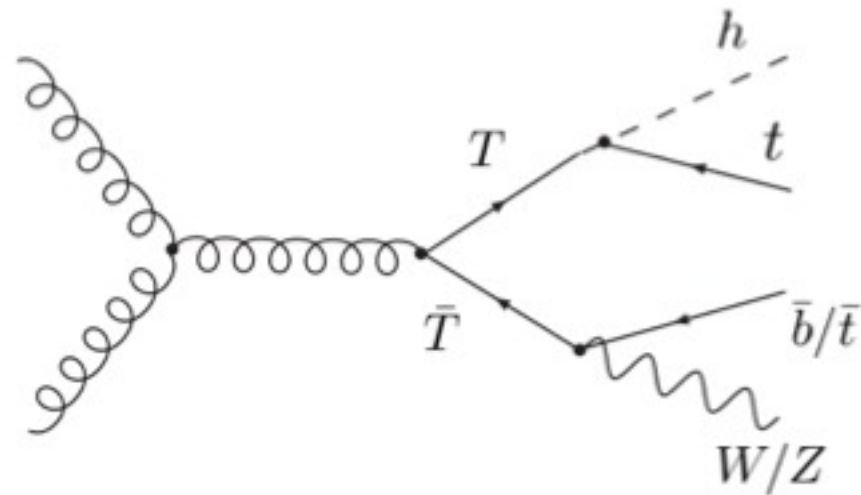
[Contino, Servant '08]

Pair production (model independent)



Single production (model dependent)

# Rich phenomenology of the top partners



## $l^\pm + 4b$ final state

Aguilar-Saavedra '09

$$T\bar{T} \rightarrow HtW^- \bar{b} \rightarrow HW^+ bW^- \bar{b}$$

$$H \rightarrow b\bar{b}, WW \rightarrow \ell\nu q\bar{q}'$$

$$T\bar{T} \rightarrow HtV\bar{t} \rightarrow HW^+ bVW^- \bar{b}$$

$$H \rightarrow b\bar{b}, WW \rightarrow \ell\nu q\bar{q}', V \rightarrow q\bar{q}/\nu\bar{\nu}$$

## $l^\pm + 6b$ final state

Aguilar-Saavedra '09

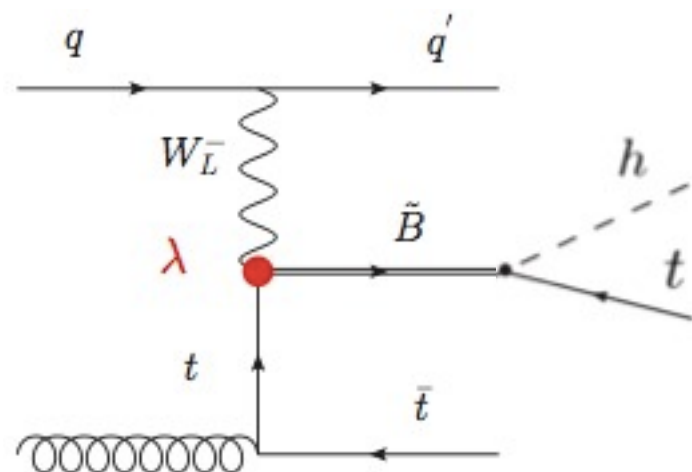
$$T\bar{T} \rightarrow HtH\bar{t} \rightarrow HW^+ bHW^- \bar{b}$$

$$H \rightarrow b\bar{b}, WW \rightarrow \ell\nu q\bar{q}'$$

## $\gamma\gamma$ final state

Azatov et al '12

$$thbW/thtZ/thth, h \rightarrow \gamma\gamma$$



## $l^\pm + 4b$ final state

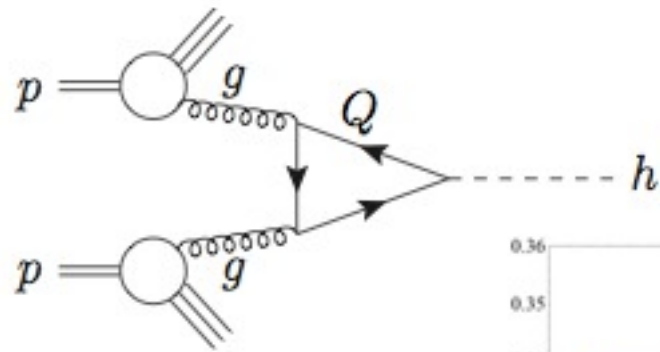
Vignaroli '12

$$pp \rightarrow (\tilde{B} \rightarrow (h \rightarrow b\bar{b})b)t + X$$

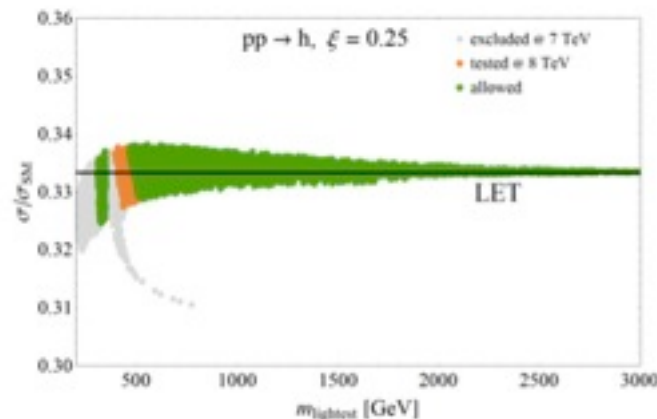


# Top partners & Higgs physics

~ current single higgs processes are insensitive to top partners ~



$$\sigma_{14\text{TeV}}^{\text{SM}} \approx 50 \text{ pb}$$



two competing effects that cancel:

- ☑ T's run in the loops
- ☑ T's modify top Yukawa coupling

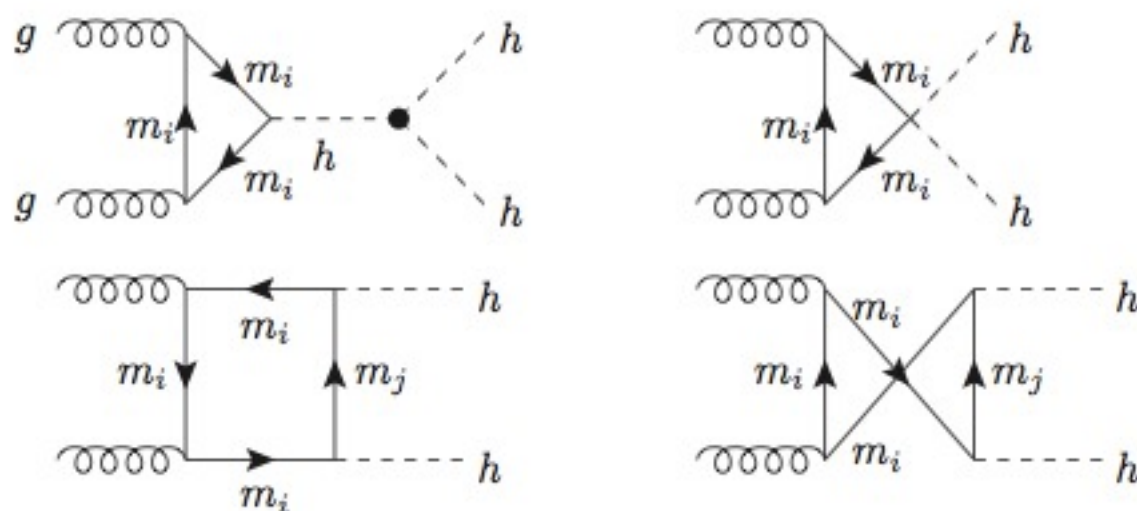
Falkowski '07

Azatov, Galloway '11

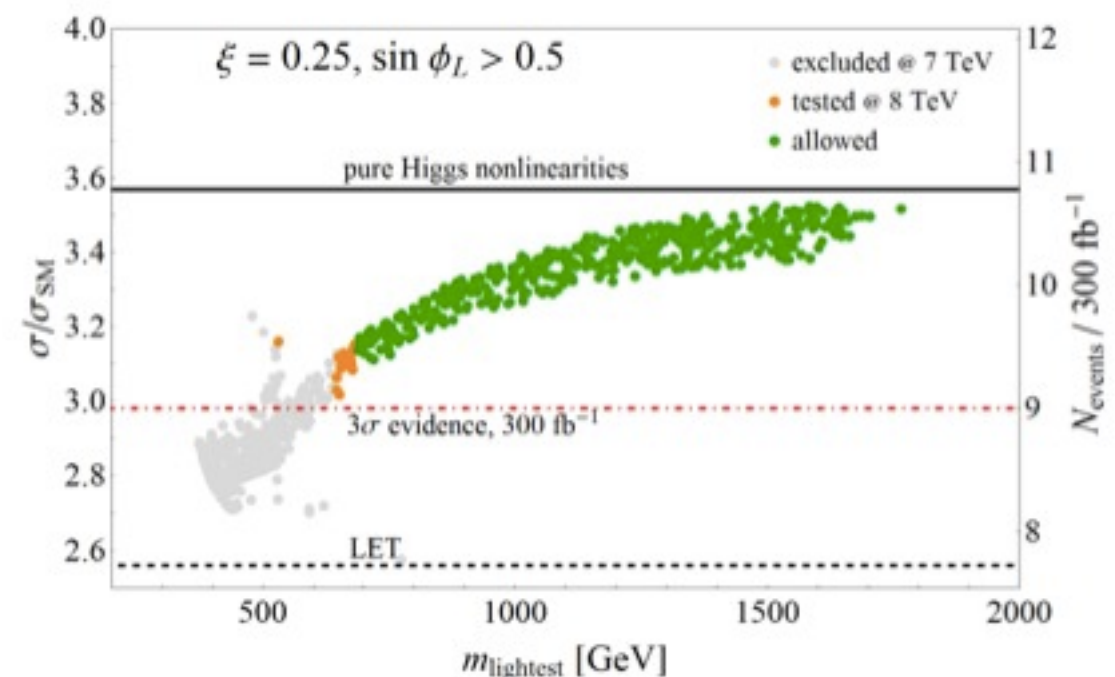
Delaunay, Grojean, Perez, '13

~ sensitivity in double Higgs production ~

Gillioz, Grober, Grojean, Muhlleitner, Salvioni '12



$$\sigma_{14\text{TeV}}^{\text{SM}} = 17.9\text{fb}$$



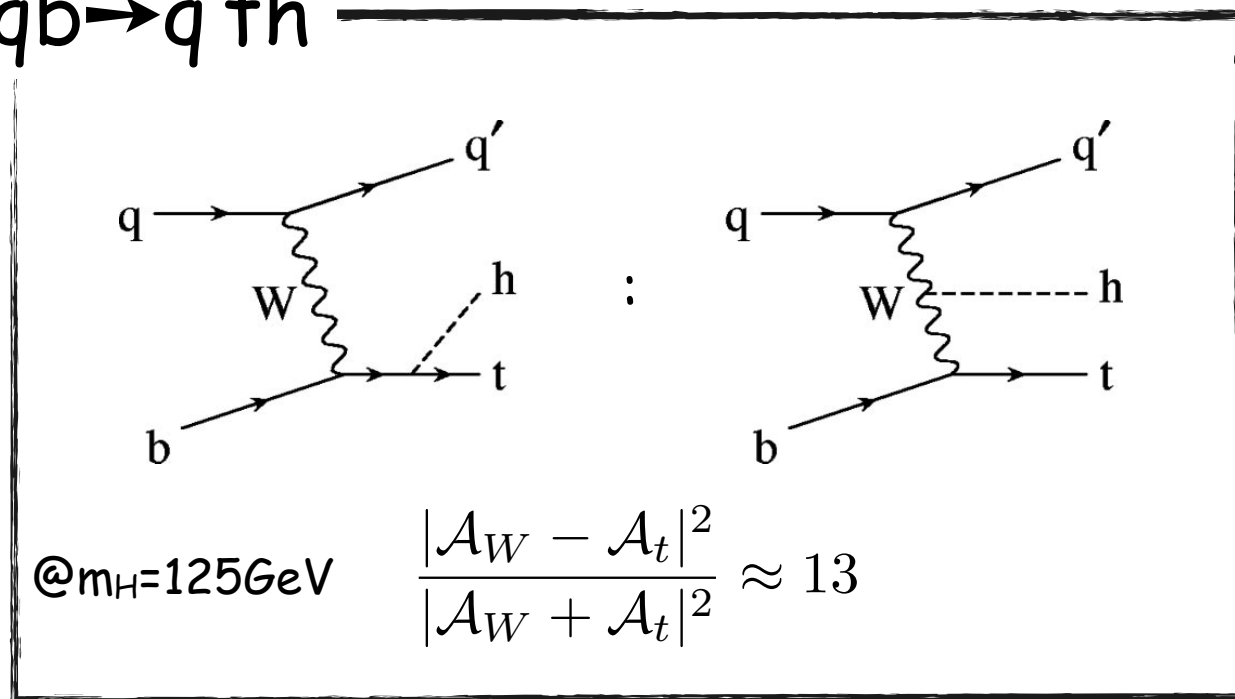
# Top partners & Higgs physics

direct measurement of top-higgs coupling

htt is important but challenging channel

may be easier channel to look at

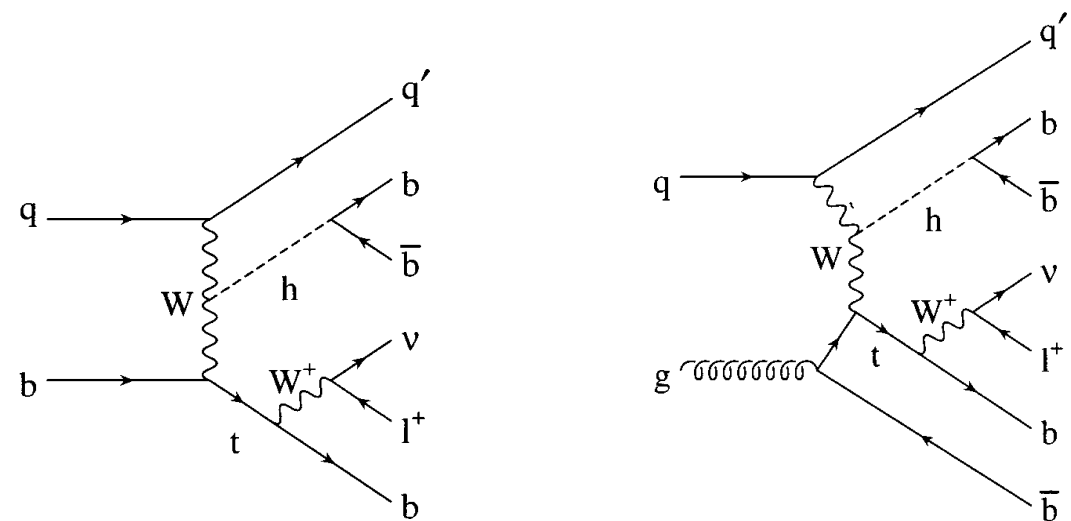
$qb \rightarrow q'th$



Farina, Grojean, Maltoni, Salvioni, Thamm '12

look at final states:

$3b + 1 \text{ fwd jet} + l^\pm + p^T$ .  $4b + 1 \text{ fwd jet} + l^\pm + p^T$ .

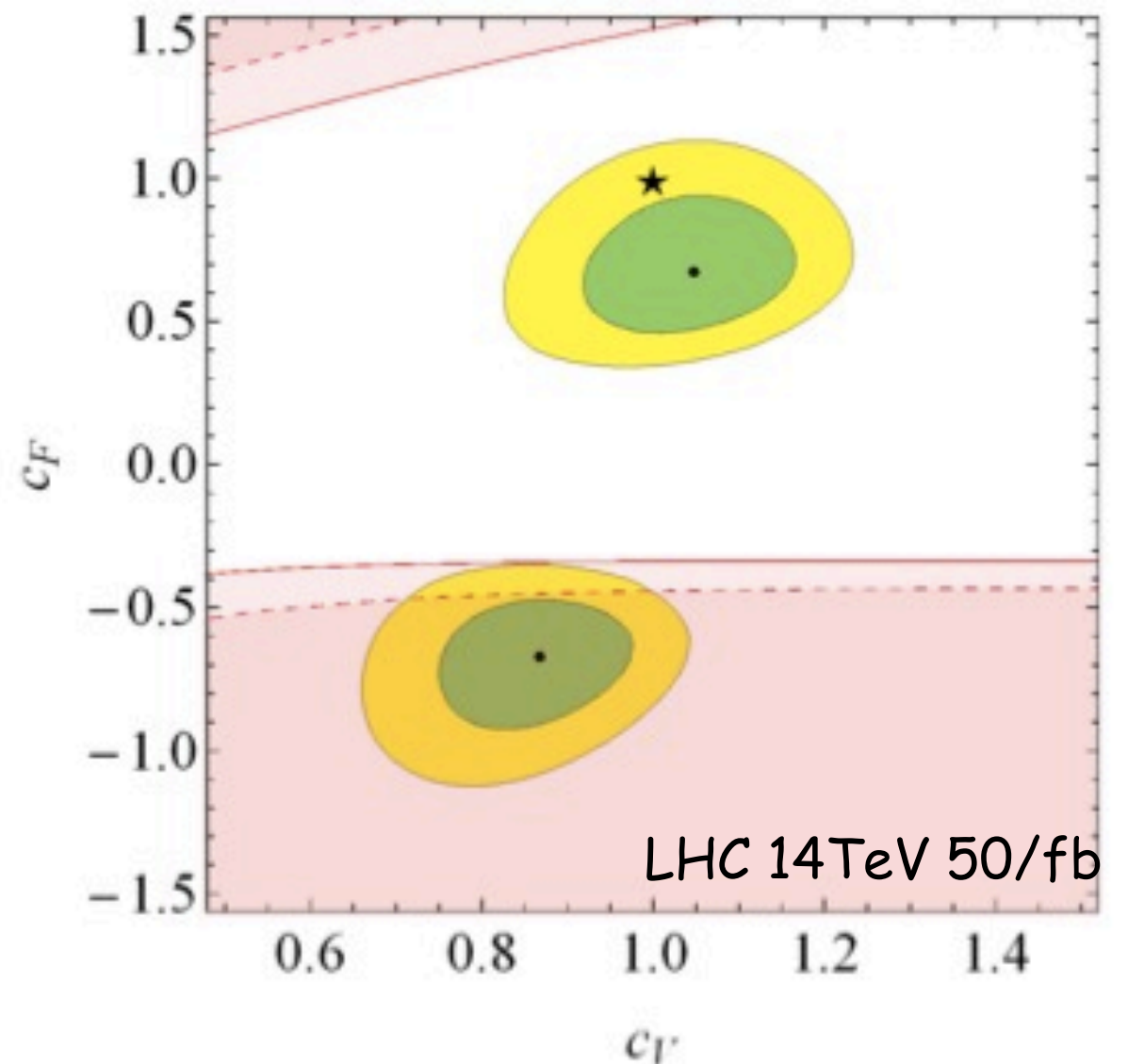
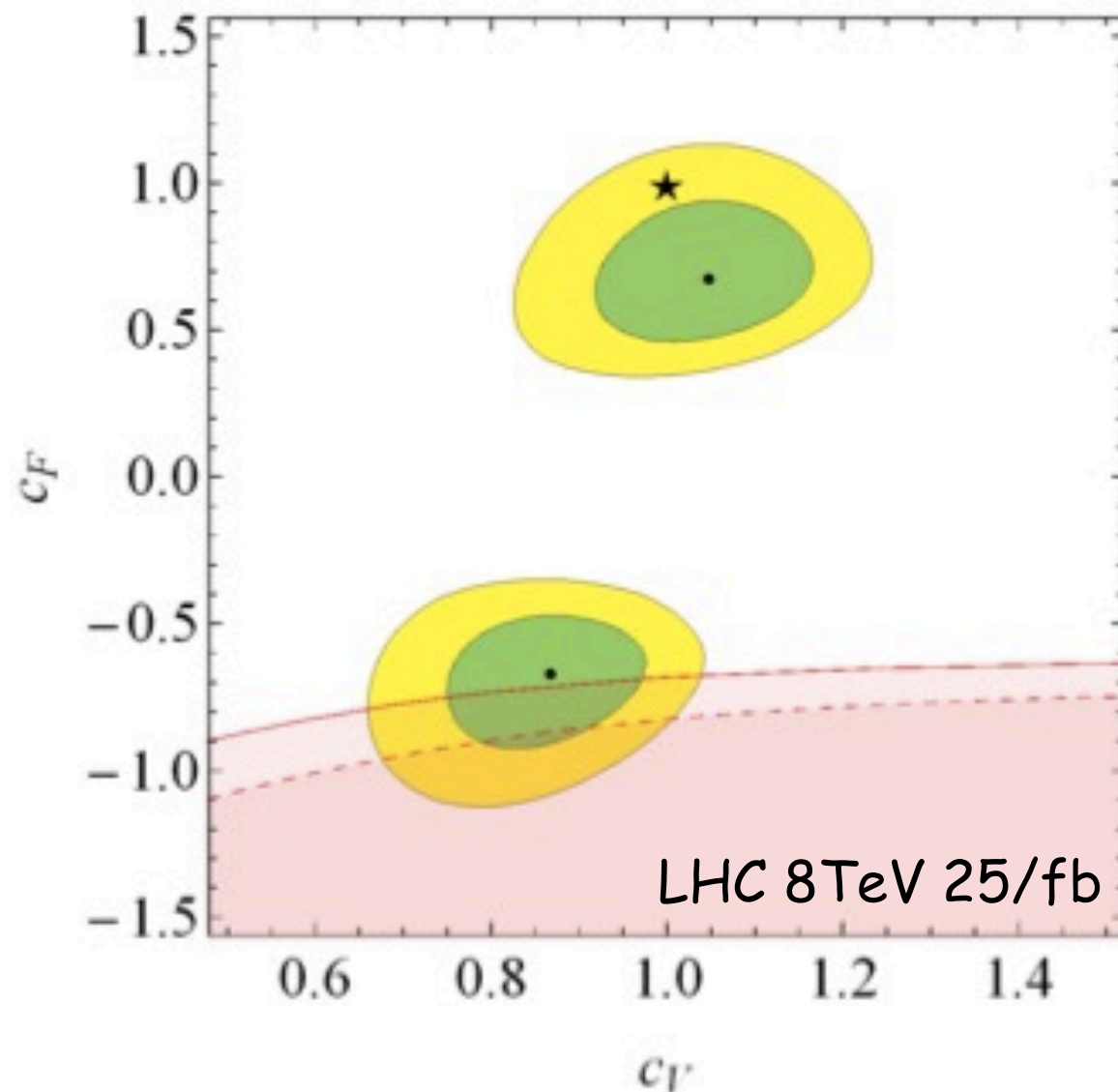


	$\sigma(pp \rightarrow tjh)$ [fb]		$\sigma(pp \rightarrow tjh\bar{b})$ [fb]	
	$c_F = 1$	$c_F = -1$	$c_F = 1$	$c_F = -1$
8 TeV	17.3	252.7	12.14	181.4
14 TeV	80.6	1042	59.6	828.5

# Top partners & Higgs physics

direct measurement of top-higgs coupling

single-top in association with Higgs



*68% and 95% CL exclusion region vs current Higgs coupling fit*

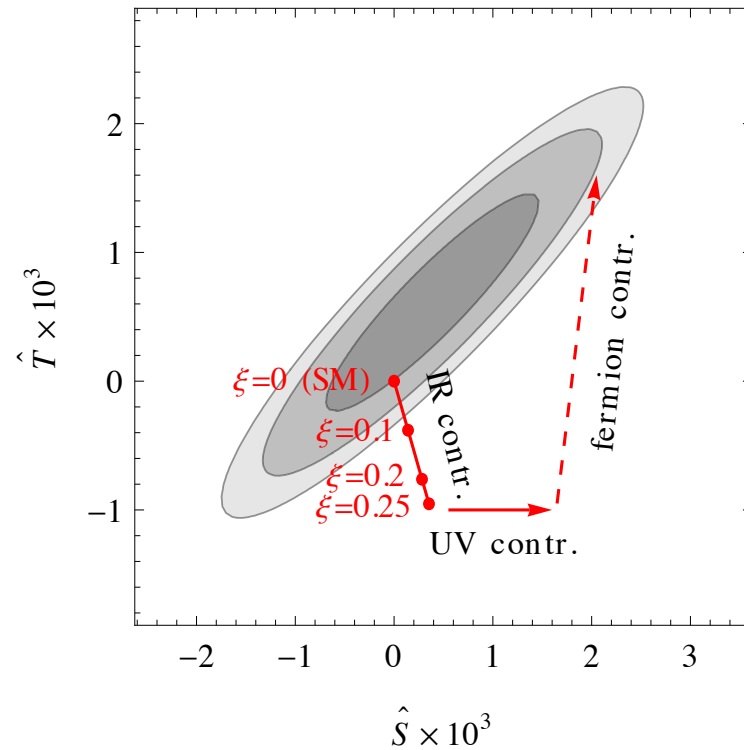
Farina, Grojean, Maltoni, Salvioni, Thamm '12



# Top partners & EWPT

Grojean, Matsedonskyi, Panico '13

## Oblique parameters



### tree-level contribution

$$\Delta \hat{S} \simeq \frac{g^2}{g_*^2} \xi \simeq \frac{m_w^2}{m_*^2}$$

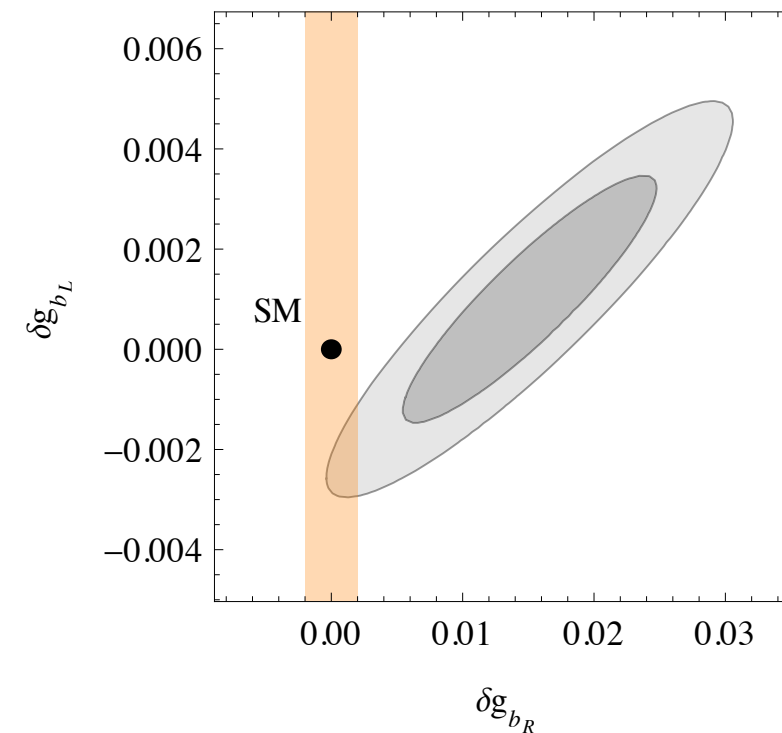
### Higgs loop

$$\Delta \hat{S} = \frac{g^2}{192\pi^2} \xi \log \left( \frac{m_*^2}{m_h^2} \right) \simeq 1.4 \cdot 10^{-3} \xi \quad \Delta \hat{T} = -\frac{3g'^2}{64\pi^2} \xi \log \left( \frac{m_*^2}{m_h^2} \right) \simeq -3.8 \cdot 10^{-3} \xi$$

### fermion loop

$$\Delta \hat{S}_{ferm}^{div} = \frac{g^2}{8\pi^2} (1 - 2c^2) \xi \log \left( \frac{m_*^2}{m_4^2} \right) \quad \Delta \hat{T} \simeq \frac{N_c}{16\pi^2} y_t^2 \xi \simeq 2 \cdot 10^{-2} \xi$$

## $Zb_L b_L$



### tree-level contribution

$$\frac{\delta g_{b_L}}{g_{b_L}^{SM}} \sim \frac{y_L^2 f^2}{m^2} \frac{m_z^2}{m_*^2} \simeq 8 \cdot 10^{-4} \frac{f}{m} \left( \frac{4\pi}{g_*} \right)^2 \xi$$

### fermion loop

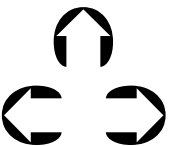
$$\frac{\delta g_{b_L}}{g_{b_L}^{SM}} \simeq \frac{y_t^2}{16\pi^2} \xi \log \left( \frac{m_*^2}{m_4^2} \right) \simeq 2 \cdot 10^{-2} \xi$$

$\xi < 0.1 \Rightarrow$  we might have to wait LHC-HL to see any new physics in Higgs data  
BSM Higgs precision era



# Precision program in single Higgs processes

(assuming a mass gap between weak scale and new physics scale)




# Higgs/BSM Primaries

Several deformations away from the SM are harmless in the vacuum and need a Higgs field to be probed

e.g. 
$$\frac{1}{g_s^2} G_{\mu\nu}^2 + \frac{|H|^2}{\Lambda^2} G_{\mu\nu}^2 \rightarrow \left( \frac{1}{g_s^2} + \frac{v^2}{\Lambda^2} \right) G_{\mu\nu}^2$$

operator is not visible in the vacuum  
(redefinition of input parameter)



But can affect  $h$  physics:



# Higgs/BSM Primaries

How many of these effects can we have?

Pomarol, Riva '13

Elias-Miro et al '13

Gupta, Pomarol, Riva '14

As many as parameters in the SM: **8** for one family  
(assuming CP-conservation)

$g_s$

$$|H|^2 G_{\mu\nu}^A G^{A\mu\nu}$$

→ **GGh coupling**

$g$

$$|H|^2 B_{\mu\nu} B^{\mu\nu}$$

→ **h $\gamma\gamma$  coupling**

yet to be measured  
at the LHC

$g'$

$$|H|^2 W_{\mu\nu}^a W^{a\mu\nu}$$

→ **hZ $\gamma$  coupling**

$m_W$

$$|H|^2 |D_\mu H|^2$$

→ **hVV\* (custodial invariant)**

$m_h$

$$|H|^6$$

→ **h<sup>3</sup> coupling**

$m_f$

$$|H|^2 \bar{f}_L H f_R + h.c.$$

→ **htt, hbb, h $\tau\tau$**

(f=t,b, $\tau$ )

the 6 others have been measured (~15%) up to a flat direction  
between the top/gluon/photon couplings

# Higgs/BSM Primaries

How many of these effects can we have?

Pomarol, Riva '13

Elias-Miro et al '13

Gupta, Pomarol, Riva '14

Almost a 1-to-1 correspondence  
with the 8  $\kappa$ 's in the Higgs fit

Coupling	300 fb <sup>-1</sup> Theory unc.:			3000 fb <sup>-1</sup> Theory unc.:		
	All	Half	None	All	Half	None
$\kappa_Z$	8.1%	7.9%	7.9%	4.4%	4.0%	3.8%
$\kappa_W$	9.0%	8.7%	8.6%	5.1%	4.5%	4.2%
$\kappa_t$	22%	21%	20%	11%	8.5%	7.6%
$\kappa_b$	23%	22%	22%	12%	11%	10%
$\kappa_\tau$	14%	14%	13%	9.7%	9.0%	8.8%
$\kappa_\mu$	21%	21%	21%	7.5%	7.2%	7.1%
$\kappa_g$	14%	12%	11%	9.1%	6.5%	5.3%
$\kappa_\gamma$	9.3%	9.0%	8.9%	4.9%	4.3%	4.1%
$\kappa_{Z\gamma}$	24%	24%	24%	14%	14%	14%

Atlas projection

With some important differences:

- 1) width approximation built-in
- 2)  $\kappa_W/\kappa_Z$  is not a primary  
(constrained by  $\Delta\rho$  and TGC)
- 3)  $\kappa_g, \kappa_\gamma, \kappa_{Z\gamma}$  do not separate UV and IR contributions

8

for one family

(assuming CP-conservation)

GGh coupling

h $\gamma\gamma$  coupling

yet to be measured  
at the LHC

hZ $\gamma$  coupling

hVV\* (custodial invariant)

h<sup>3</sup> coupling

htt, hbb, h $\tau\tau$

# Don't forget LEP!

The parameter 'a' controls the size of the one-loop IR contribution to the LEP precision observables

$$\mathcal{L} \supset \frac{1}{f^2} |H|^2 |D_\mu H|^2$$

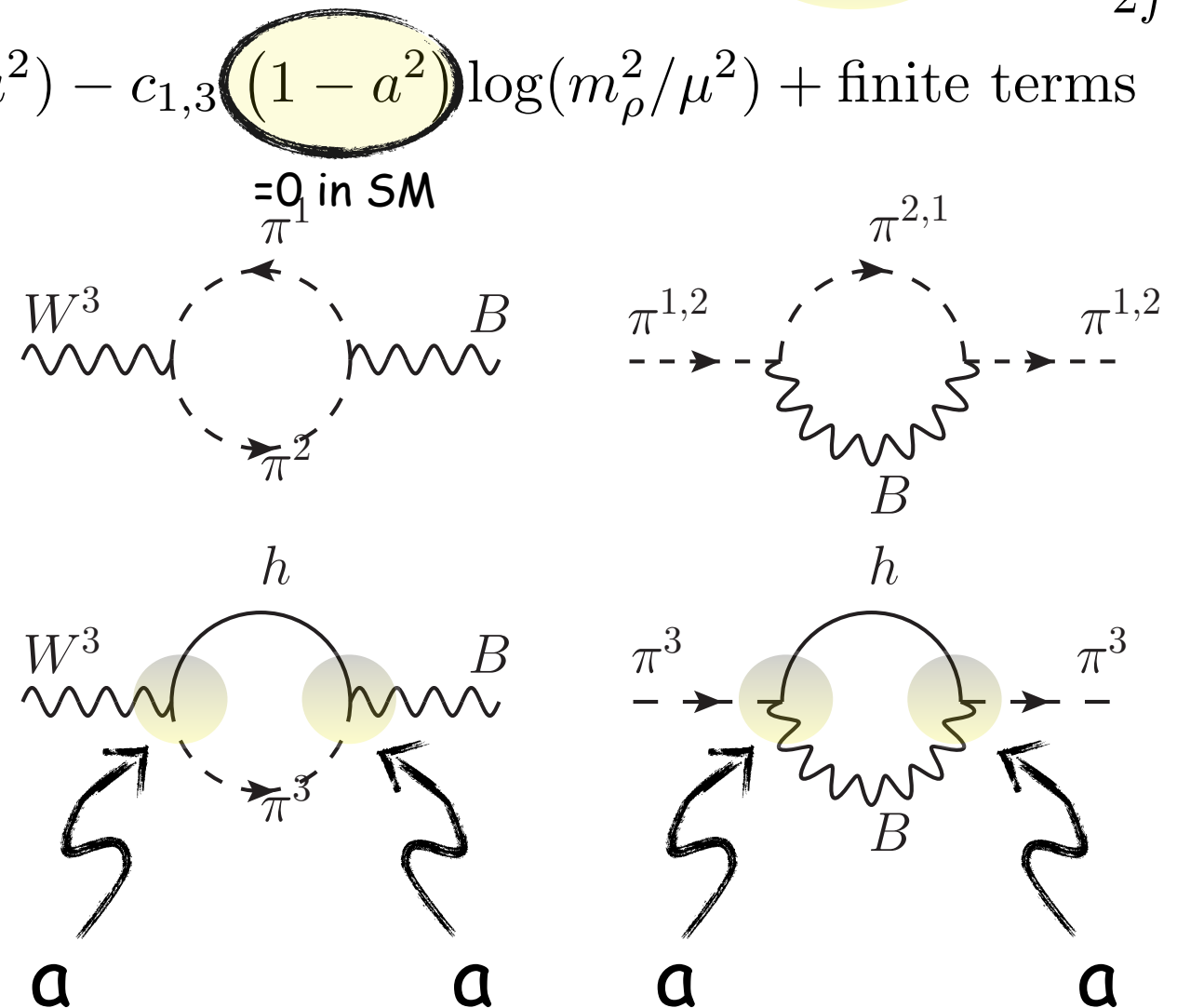
$$\Rightarrow a = \kappa_V = 1 + \frac{v^2}{2f^2}$$

$$\epsilon_{1,3} = c_{1,3} \log(m_Z^2/\mu^2) - c_{1,3} a^2 \log(m_h^2/\mu^2) - c_{1,3} (1 - a^2) \log(m_\rho^2/\mu^2) + \text{finite terms}$$

$$c_1 = + \frac{3}{16\pi^2} \frac{\alpha(m_Z)}{\cos^2 \theta_W} \quad c_3 = - \frac{1}{12\pi} \frac{\alpha(m_Z)}{4 \sin^2 \theta_W}$$

$$\Delta\epsilon_{1,3} = -c_{1,3} (1 - a^2) \log(m_\rho^2/m_h^2)$$

Barbieri, Bellazzini, Rychkov, Varagnolo '07



Log. div. cancel only for  $a=1$  (SM)  
 $a \neq 1$  log. sensitivity on the scale of new physics



# Don't forget LEP!

The parameter 'a' controls the size of the one-loop IR contribution to the LEP precision observables

$$\mathcal{L} \supset \frac{1}{f^2} |H|^2 |D_\mu H|^2$$
$$\Rightarrow a = \kappa_V = 1 + \frac{v^2}{2f^2}$$

$$\Delta\epsilon_{1,3} = -c_{1,3} (1 - a^2) \log(m_\rho^2/m_h^2)$$

Barbieri, Bellazzini, Rychkov, Varagnolo '07

EW fit:

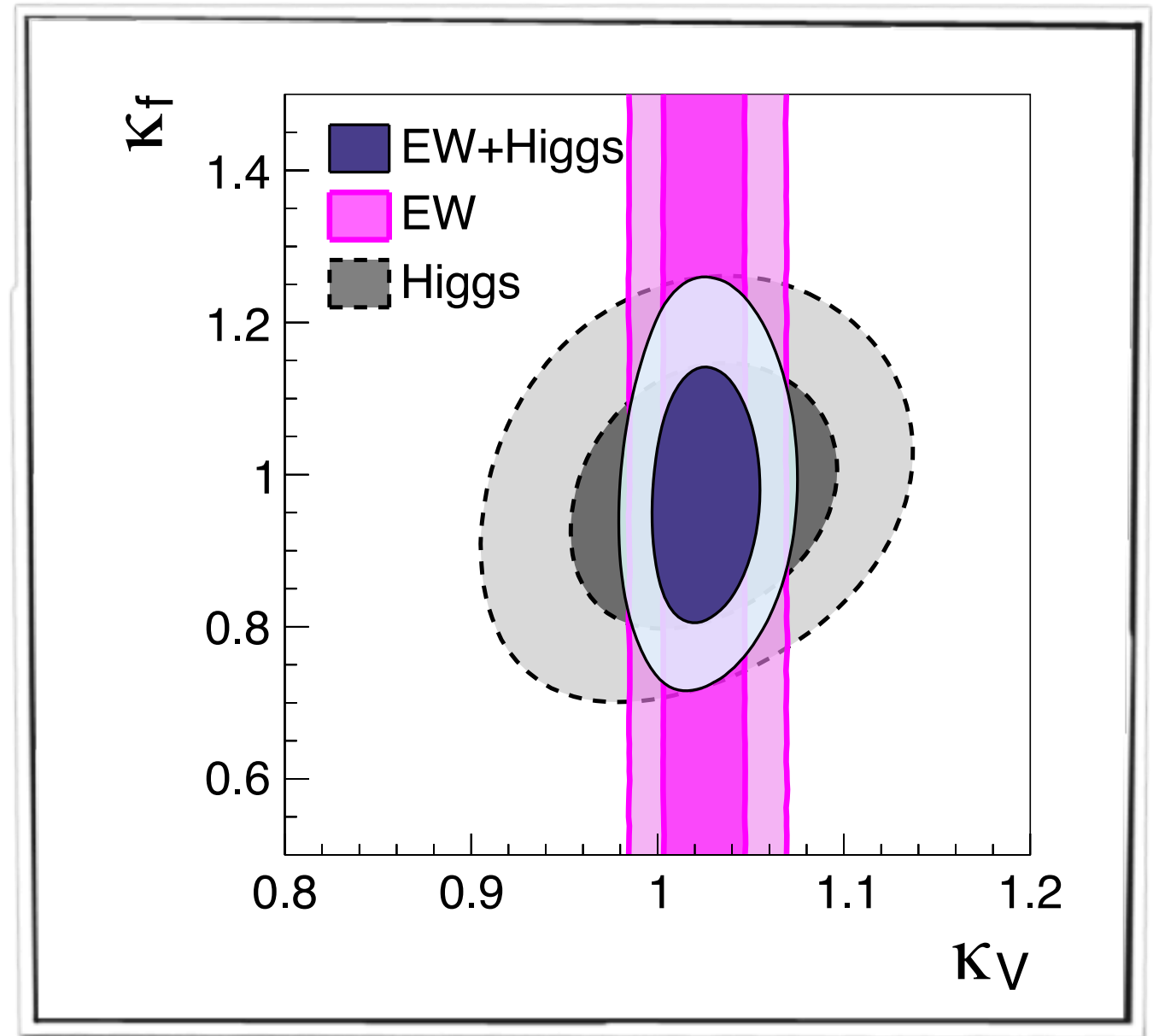
$$0.98 \leq a^2 \leq 1.12$$

Ciuchini et al '13

see also Grojean et al '13

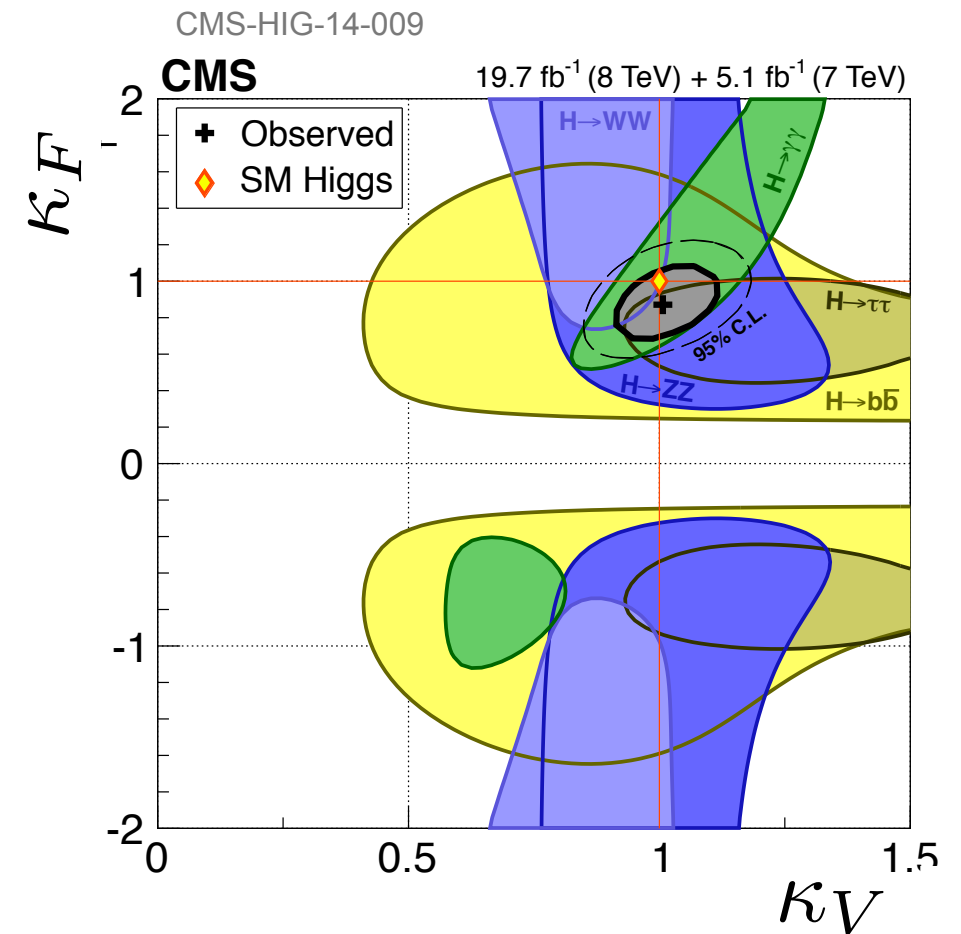
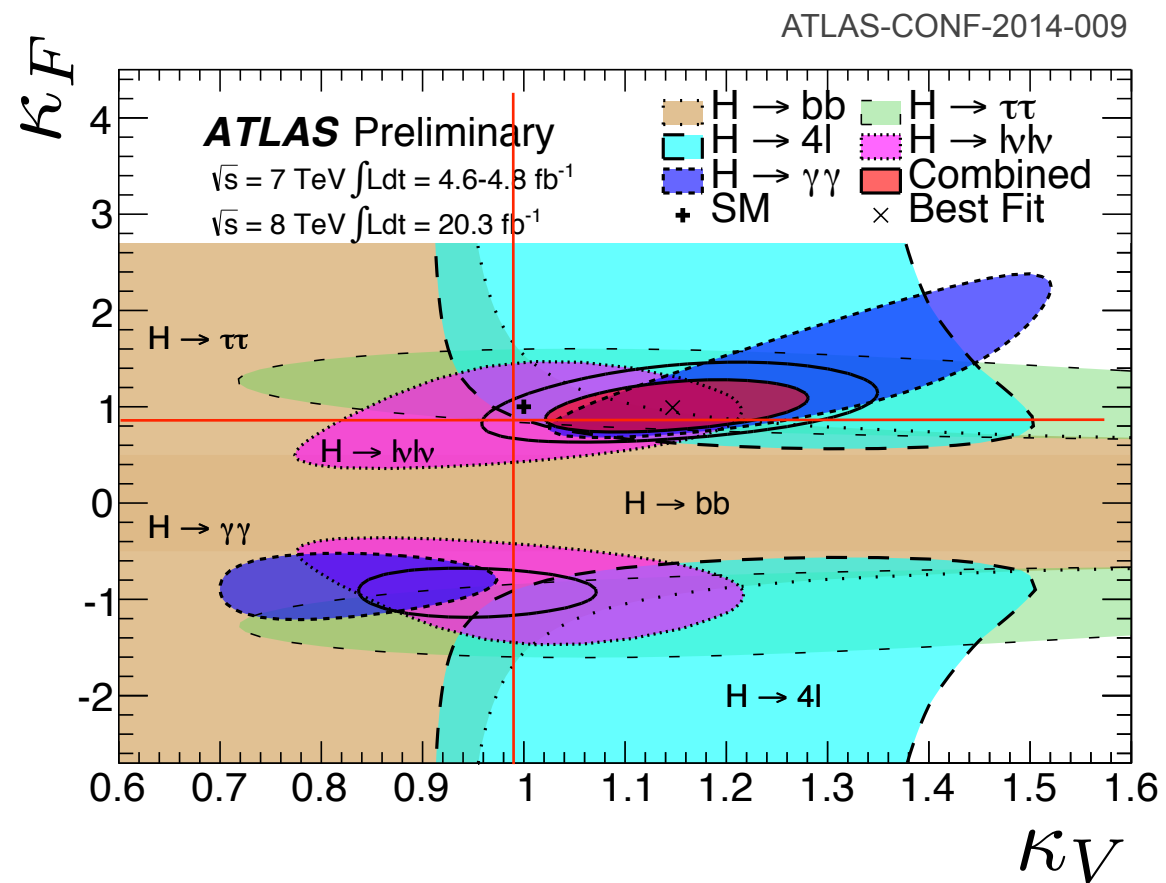
The LEP indirect constraints on the other BSM primaries are not competitive

Elias-Miro et al '13



Ciuchini et al '13

# Experimental results



# CP violation in Higgs physics?

Is CP a good symmetry of Nature? 2 CP-violating couplings in the SM:

$V_{CKM}$  (large,  $O(1)$ ), but screened by small quark masses) and  $\theta_{QCD}$  (small,  $O(10^{-10})$ )

Can the  $0^+$  SM Higgs boson have CP violating couplings?

Among the 59 irrelevant directions, 6 ~~CP~~ Higgs/BSM primaries

$$\begin{aligned}\Delta\mathcal{L}_{BSM} = & i\delta\tilde{g}_{hff} h\bar{f}_L f_R + h.c. & (f=b, \tau, t) \\ & + \tilde{\kappa}_{GG} \frac{h}{v} G^{\mu\nu} \tilde{G}_{\mu\nu} & (\tilde{F}_{\mu\nu} \equiv \epsilon_{\mu\nu\rho\sigma} F^{\rho\sigma}) \\ & + \tilde{\kappa}_{\gamma\gamma} \frac{h}{v} F^{\gamma\mu\nu} \tilde{F}_{\mu\nu} \\ & + \tilde{\kappa}_{\gamma Z} \frac{h}{v} F^{\gamma\mu\nu} \tilde{F}_{\mu\nu}^Z\end{aligned}$$

# CP violation in Higgs physics?

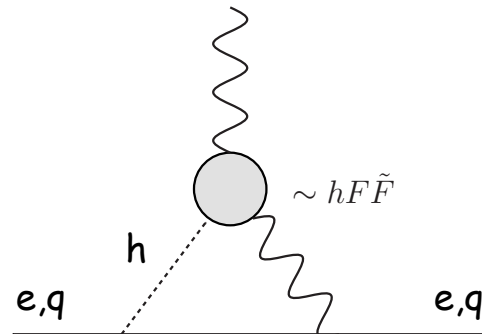
Among the 59 irrelevant directions, 6 ~~CP~~ Higgs/BSM primaries

$$\begin{aligned}\Delta\mathcal{L}_{\text{BSM}} = & i\delta\tilde{g}_{hff} h\bar{f}_L f_R + h.c. & (f=b, \tau, t) \\ & + \tilde{\kappa}_{GG} \frac{h}{v} G^{\mu\nu} \tilde{G}_{\mu\nu} & (\tilde{F}_{\mu\nu} \equiv \epsilon_{\mu\nu\rho\sigma} F^{\rho\sigma}) \\ & + \tilde{\kappa}_{\gamma\gamma} \frac{h}{v} F^{\gamma\mu\nu} \tilde{F}_{\mu\nu} \\ & + \tilde{\kappa}_{\gamma Z} \frac{h}{v} F^{\gamma\mu\nu} \tilde{F}_{\mu\nu}^Z\end{aligned}$$

**operators with  $\gamma$ :**

already severely constrained  
by e and q EDMs

McKeen, Pospelov, Ritz '12



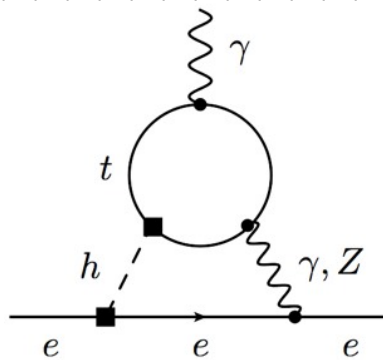
$$\tilde{\kappa}_{\gamma\gamma} \sim \tilde{\kappa}_{\gamma Z} \leq 10^{-4}$$

$$\Lambda_{\text{CP}} > 25 \text{ TeV}$$

**operators with top:**

already severely constrained  
by e and q EDMs

Brod, Haisch, Zupan '13



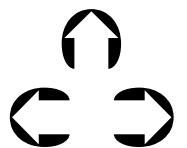
$$\delta\tilde{g}_{htt} \leq 0.01$$

$$\Lambda_{\text{CP}} > 2.5 \text{ TeV}$$

Caveats: h couplings to light particles can be significantly reduced



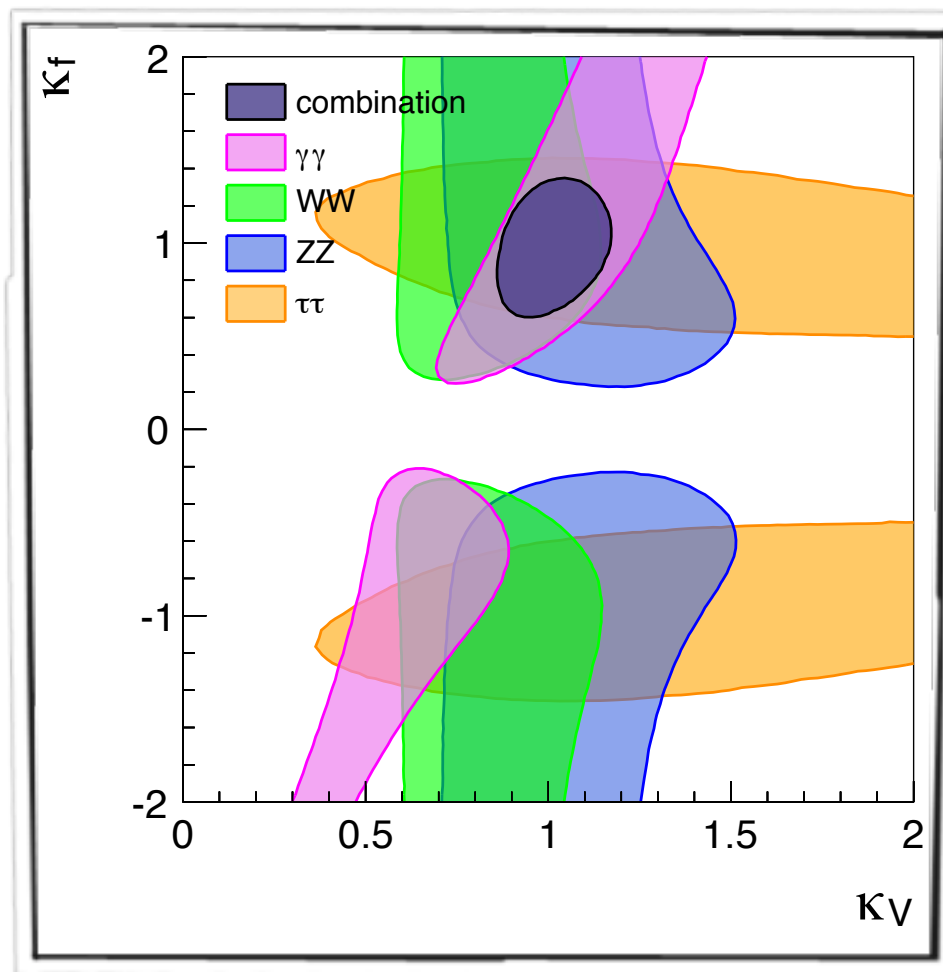
# Boosted and off-shell Higgs channels



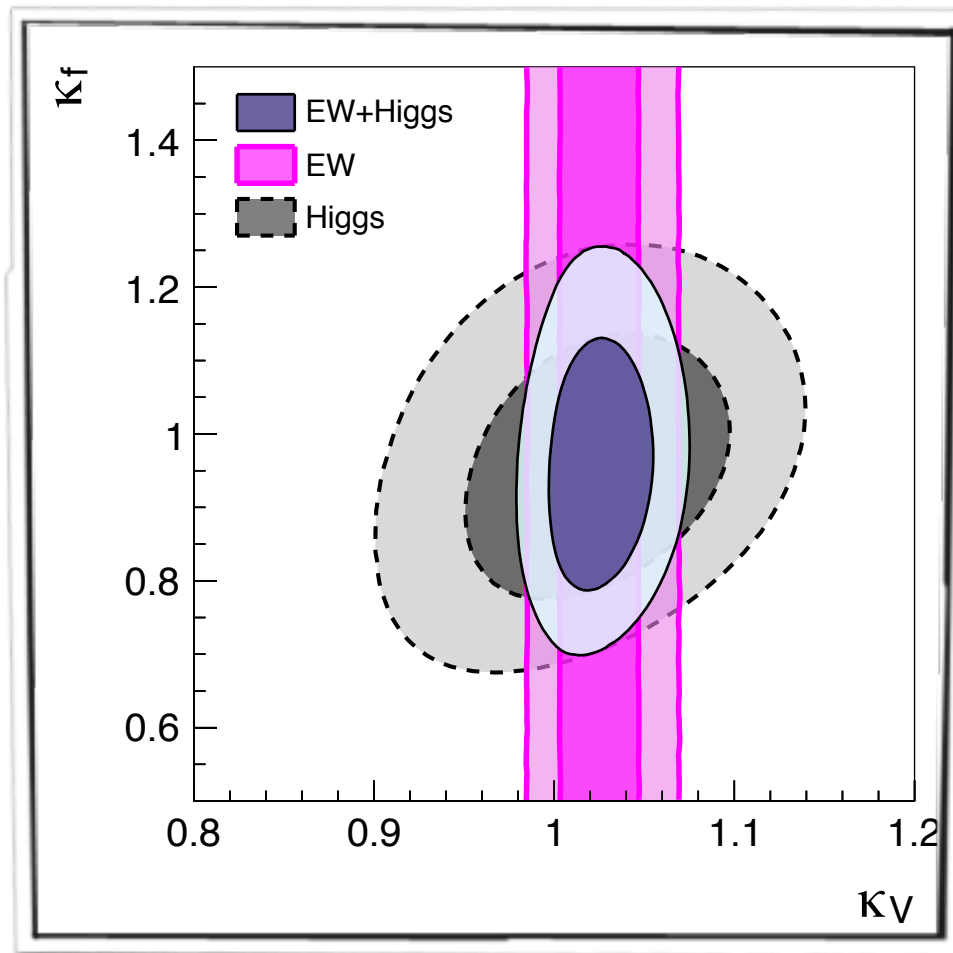
# Why going beyond inclusive Higgs processes?

So far the LHC has mostly produced Higgses on-shell  
in processes with a characteristic scale  $\mu \approx m_H$

↓ ↓  
access to Higgs couplings @  $m_H$



Ciuchini et al '13



Ciuchini et al '13



# Why going beyond inclusive Higgs processes?

So far the LHC has mostly produced Higgses on-shell  
in processes with a characteristic scale  $\mu \approx m_H$



access to Higgs couplings @  $m_H$

Producing a Higgs with boosted additional particle(s)  
probe the Higgs couplings @ large energy  
(important to check that the Higgs boson ensures perturbative unitarity)

## Probing new corrections to the SM Lagrangian?

on-shell Z @ LEP1

constraints on  
S and T oblique corrections

off-shell Z @ LEP2

constraints on  
W and Y oblique corrections  
(same order as S and T but cannot be probed @ LEP1)

But... off-shell Higgs data do not probe new corrections  
that cannot be constrained by on-shell data

# Boosted Higgs

## inability to resolve the top loops

- the bearable lightness of the Higgs: rich spectroscopy w/ multiple decays channels
- the unbearable lightness: loops saturate and don't reveal the physics @ energy physics <sup>(\*)</sup>

$m_H(\text{GeV})$	$\frac{\sigma_{NLO}(m_t)}{\sigma_{NLO}(m_t \rightarrow \infty)}$	$\frac{\sigma_{NLO}(m_t, m_b)}{\sigma_{NLO}(m_t \rightarrow \infty)}$
125	1.061	0.988
150	1.093	1.028
200	1.185	1.134

e.g. Grazzini, Sargsyan '13

<sup>(\*)</sup> unless it doesn't decouple  
(e.g. 4th generation)

the inclusive rate  
doesn't "see" the finite mass of the top

⇒ cannot disentangle ○ long distance physics (modified top coupling)  
○ short distance physics (new particles running in the loop) ⇐

$$\mathcal{L} = \frac{\alpha_s c_g}{12\pi} |H|^2 G_{\mu\nu}^a{}^2 + \frac{\alpha c_\gamma}{2\pi} |H|^2 F_{\mu\nu} + y_t c_t \bar{q}_L \tilde{H} t_R |H|^2$$

$$\frac{\sigma(gg \rightarrow h)}{\text{SM}} = (1 + (c_g - c_t)v^2)^2 \quad \frac{\Gamma(h \rightarrow \gamma\gamma)}{\text{SM}} = (1 + (c_\gamma - 4c_t/9)v^2)^2$$

fermionic top-partners in composite Higgs models exactly lead to  $\Delta c_t = \Delta c_g = \frac{9}{4} \Delta c_\gamma$ .

having access to  $h\bar{t}t$  final state will resolve this degeneracy  
but notoriously difficult channel

14%-4% @ LHC<sup>14</sup><sub>300</sub>-LHC<sup>14</sup><sub>3000</sub> vs 10%-4% @ ILC<sup>500</sup><sub>500</sub>-ILC<sup>1000</sup><sub>1000</sub>

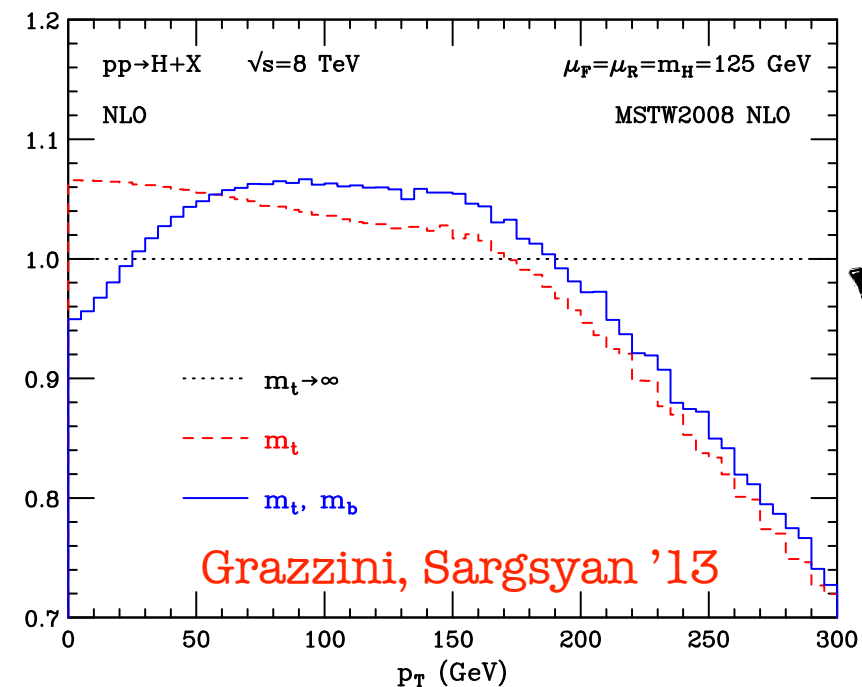
# Resolving top loop: Boosted Higgs

## cut open the top loops

high  $p_T \approx$  Higgs off-shell  
we "see" the details of the particles  
running inside the loops

Baur, Glover '90

Langenegger, Spira, Starodumov, Trueb '06



Note: LO only

$NLO_{m_t}$  is not known

$1/m_t$  corrections known  $O(\alpha_s^4)$

few % up to  $p_T \sim 150$  GeV

Harlander et al '12

the high  $p_T$  tail  
is tens' % sensitive  
to the mass of top

# Resolving top loop: Boosted Higgs

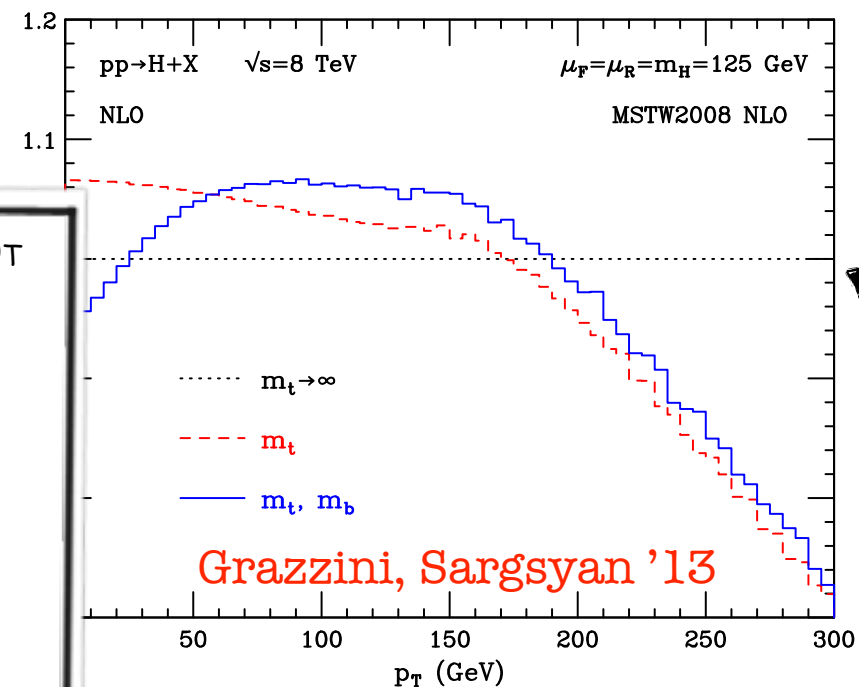
cut open the top loops

Don't think it is easy to produce a Higgs with high  $p_T$

$\sqrt{s}$ [TeV]	$p_T^{\min}$ [GeV]	$\sigma_{p_T^{\min}}^{\text{SM}}$ [fb]	$\delta$	$\epsilon$	$gg, qg$ [%]
14	100	2200	0.016	0.023	67, 31
	150	830	0.069	0.13	66, 32
	200	350	0.20	0.31	65, 34
	250	160	0.39	0.56	63, 36
	300	75	0.61	0.89	61, 38
	350	38	0.86	1.3	58, 41
	400	20	1.1	1.8	56, 43
	450	11	1.4	2.3	54, 45
	500	6.3	1.7	2.9	52, 47
	550	3.7	2.0	3.6	50, 49
	600	2.2	2.3	4.4	48, 51
	650	1.4	2.6	5.2	46, 53
	700	0.87	3.0	6.2	45, 54
	750	0.56	3.3	7.2	43, 56
	800	0.37	3.7	8.4	42, 57

+1000  
reduction

Grojean, Salvioni, Schlaffer, Weiler '13



Grazzini, Sargsyan '13

Note: LO only

$\text{NLO}_{m_t}$  is not known

$1/m_t$  corrections known  $O(\alpha_s^4)$

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Harlander et al '12

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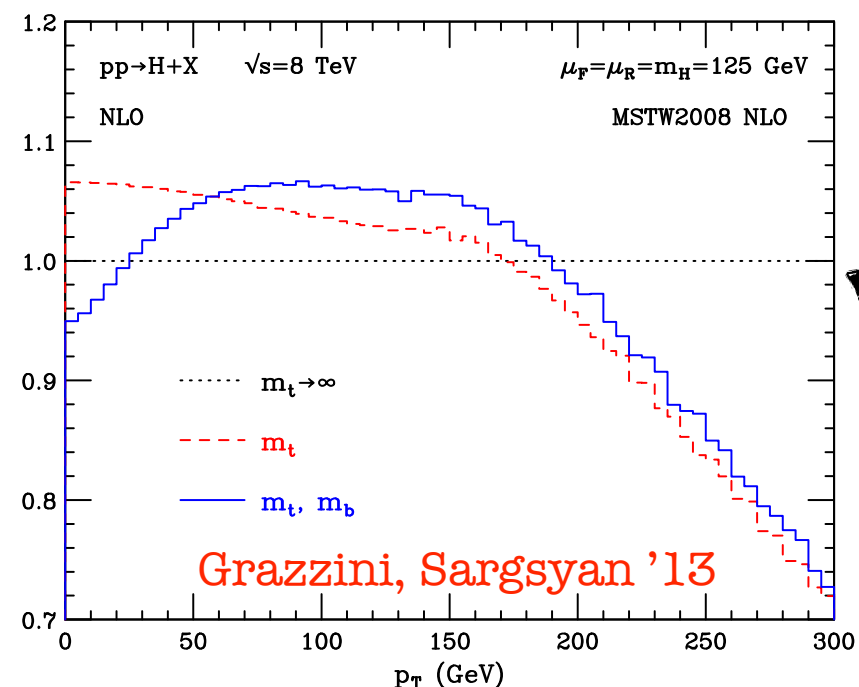
# Resolving top loop: Boosted Higgs

cut open the top loops

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we "see" the details of the particles  
running inside the loops

Baur, Glover '90

Langenegger, Spira, Starodumov, Trueb '06



Note: LO only

NLO<sub>mt</sub> is not known

$1/m_t$  corrections known  $O(\alpha_s^4)$

few % up to  $p_T \sim 150$  GeV

Harlander et al '12

the high  $p_T$  tail  
is tens' % sensitive  
to the mass of top

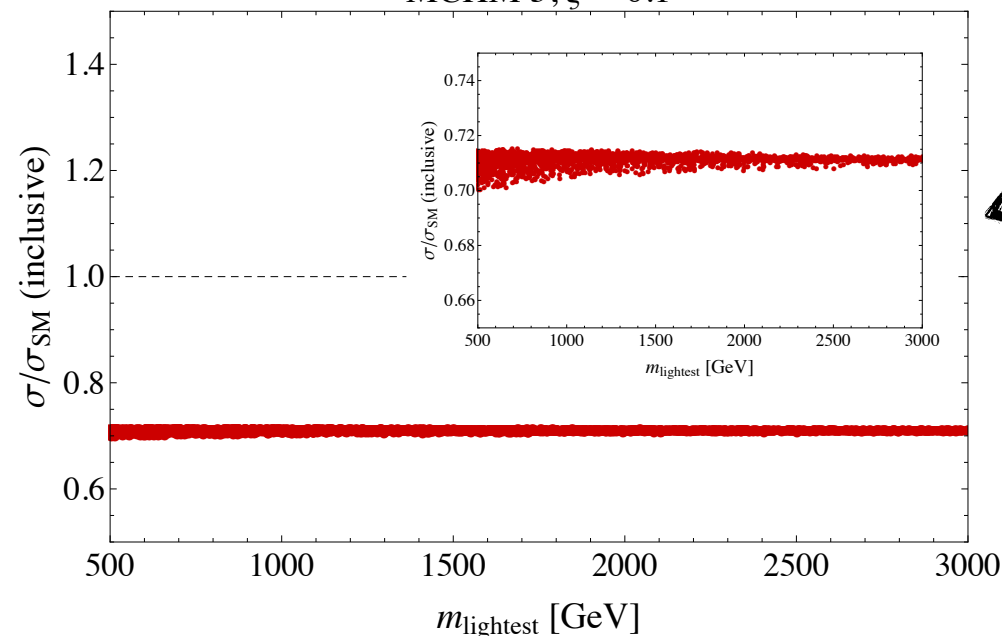
see also Banfi, Martin, Sanz '13

see also Azatov, Paul '13

Composite Higgs Model  
top partners contributions

Grojean, Salvioni, Schlaffer, Weiler '13

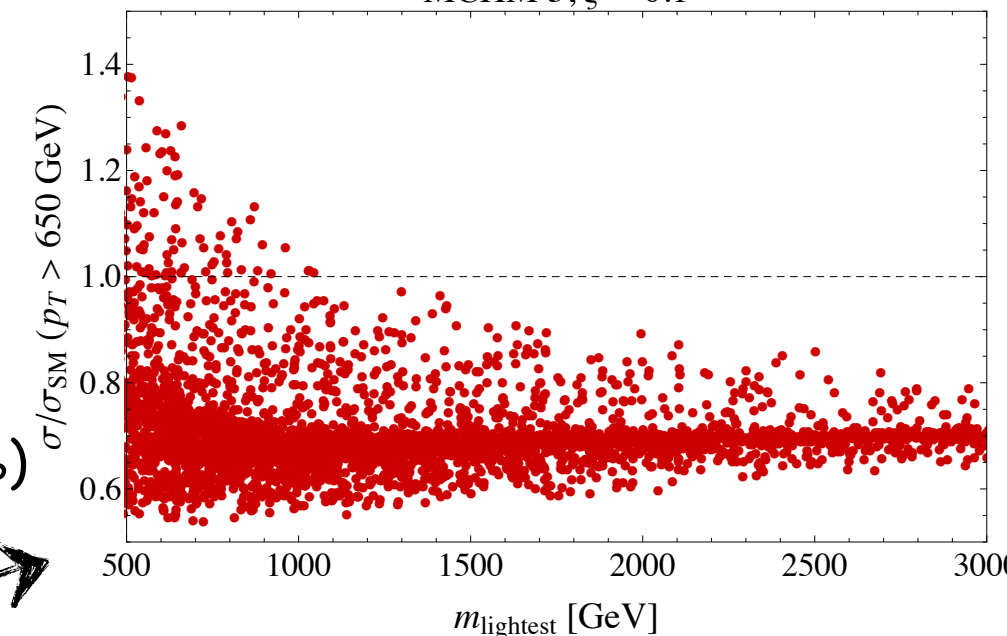
MCHM 5,  $\xi = 0.1$



inclusive rate:  $O(\%)$

with high- $p_T$  cut:  $O(\times 10\%)$

MCHM 5,  $\xi = 0.1$



high- $p_T$  tail "sees" the top partners that are missed by the inclusive rate

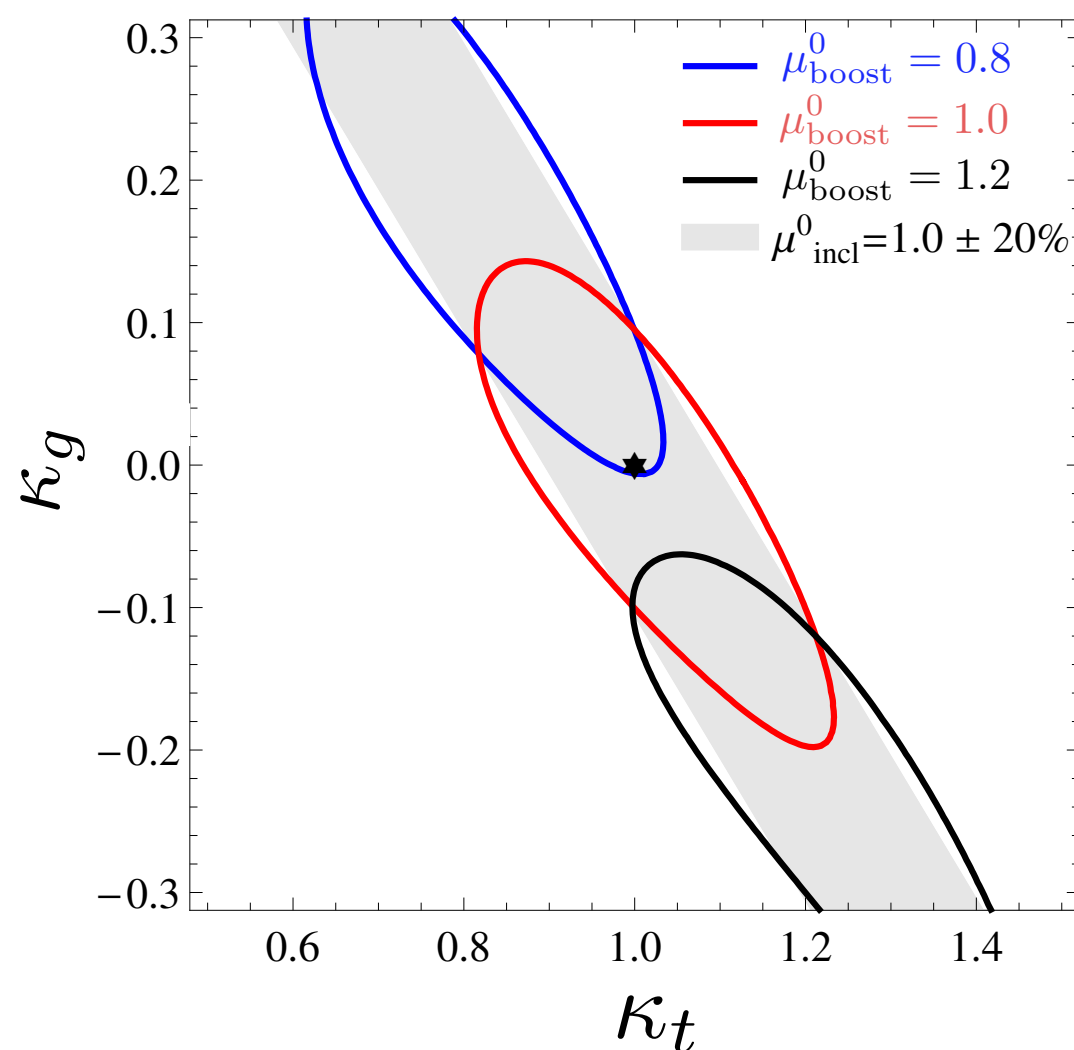
# Boosted Higgs

high  $p_T$  tail discriminates short and long distance physics contribution to  $gg \rightarrow h$

$$\sqrt{s} = 14 \text{ TeV}, \int dt \mathcal{L} = 3 \text{ ab}^{-1}, p_T > 650 \text{ GeV}$$

(partonic analysis in the boosted "ditau-jets" channel)

see Schlaffer et al '14 for a more complete analysis including WW channel



10-20% precision on  $\kappa_t$



competitive/complementary to htt channel  
for the measure the top-Higgs coupling

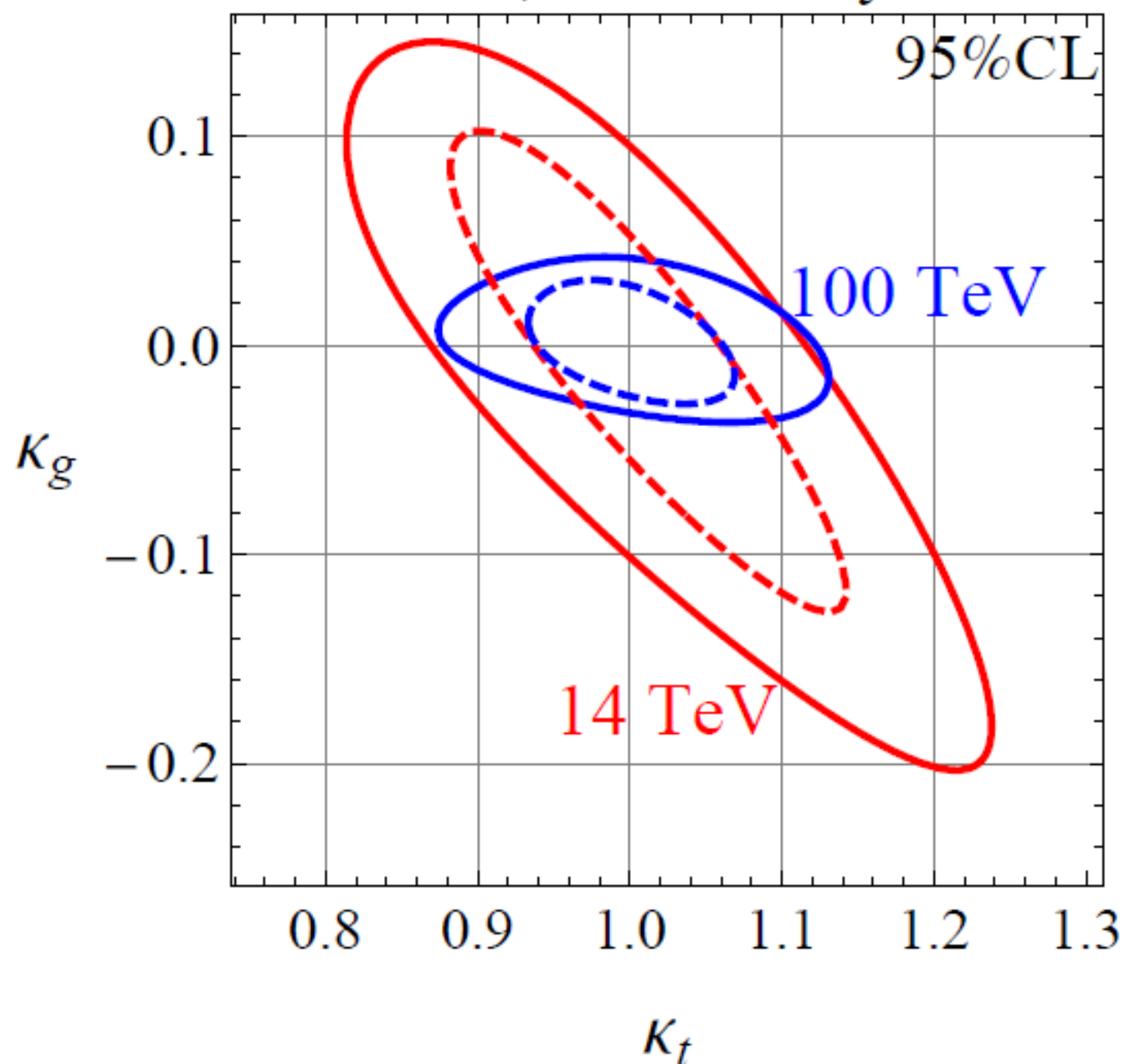
Are the NLO<sub>m</sub> QCD corrections (not known) going to destroy all the sensitivity?  
Frontier priority: N<sup>3</sup>LO<sub>∞</sub> for inclusive xs or NLO<sub>mt</sub> for pT spectrum?



# Boosted Higgs

high  $p_T$  tail discriminates short and long distance physics contribution to  $gg \rightarrow h$

3000  $\text{fb}^{-1}$ , 10 or 5% syst. unc.



A perfect case for a very energetic machine

$t\bar{t}h$  increases by 10 from 14 to 100 TeV

$h+j_{p_T > 600 \text{ GeV}}$  increases by 210

$$\mathcal{R}_{14} = \frac{\sigma(p_T > 650 \text{ GeV})}{\sigma(p_T > 150 \text{ GeV})}$$

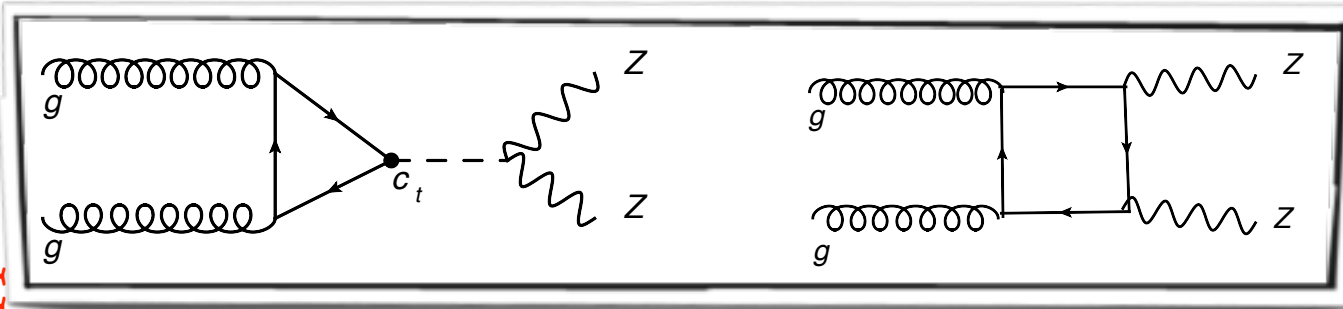
$$\mathcal{R}_{100} = \frac{\sigma(p_T > 2000 \text{ GeV})}{\sigma(p_T > 500 \text{ GeV})}$$

Frontier priority:  $N^3\text{LO}_\infty$  for inclusive xs or  $\text{NLO}_{\text{mt}}$  for  $p_T$  spectrum?

# Off-shell Higgs: $gg \rightarrow h^* \rightarrow ZZ \rightarrow 4l$

off-shell effects enhanced by the particular couplings of H to  $V_L$

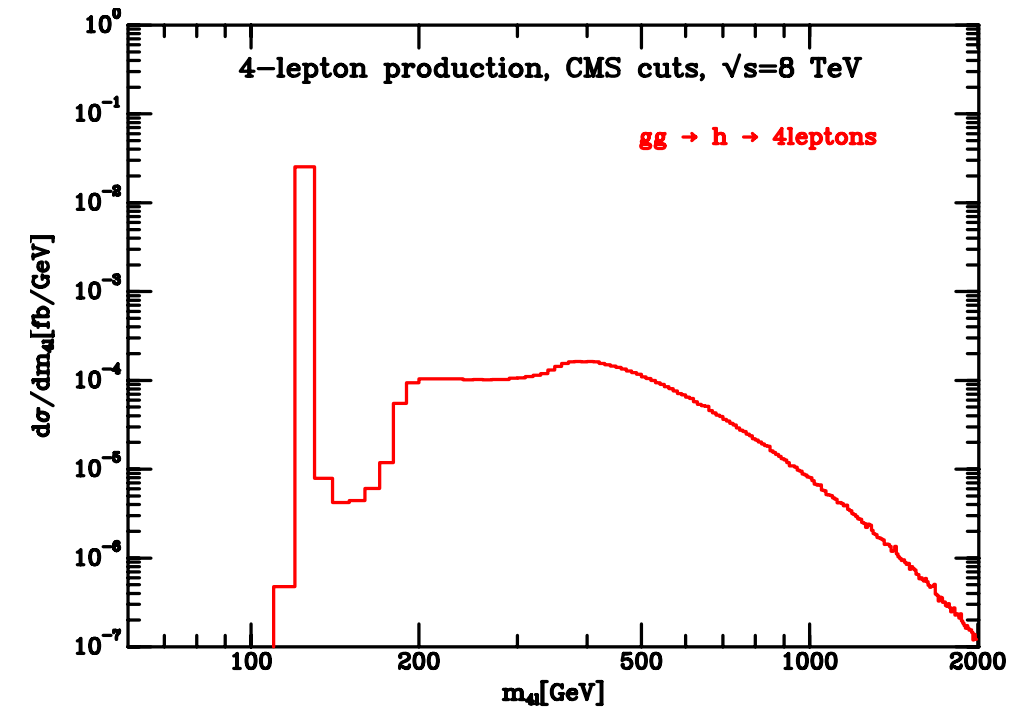
Glover, van der Bij '89



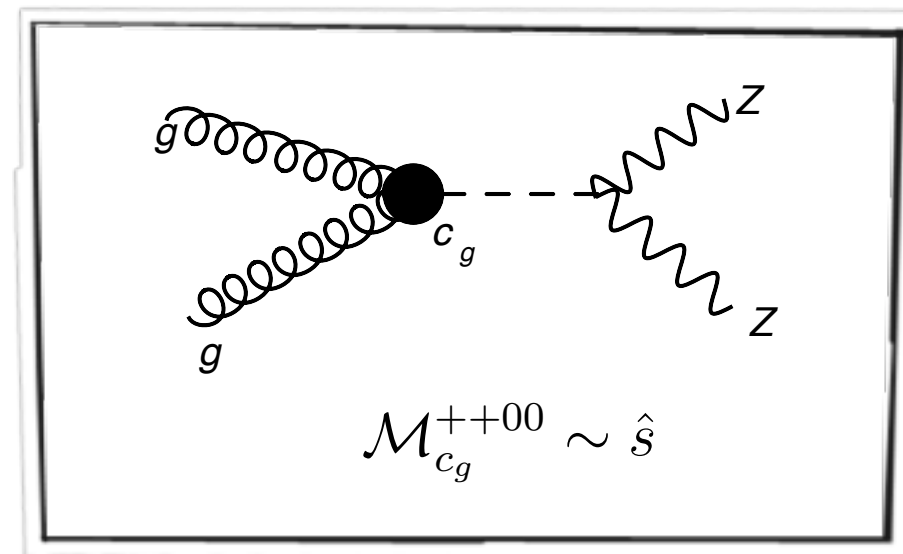
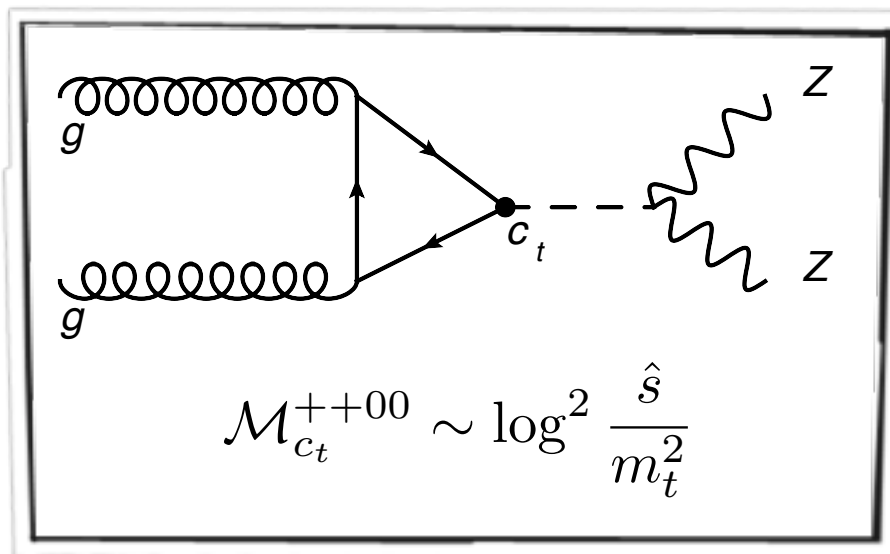
$$\mathcal{M}_{\text{Higgs}}^{++00} \sim \log^2 \frac{\hat{s}}{m_t^2} \quad \mathcal{M}_{\text{box}}^{++00} \sim -\log^2 \frac{\hat{s}}{m_t^2}$$

SM: cancelation forced by unitarity

BSM: deviations of Higgs couplings at large  $s$  will be amplified



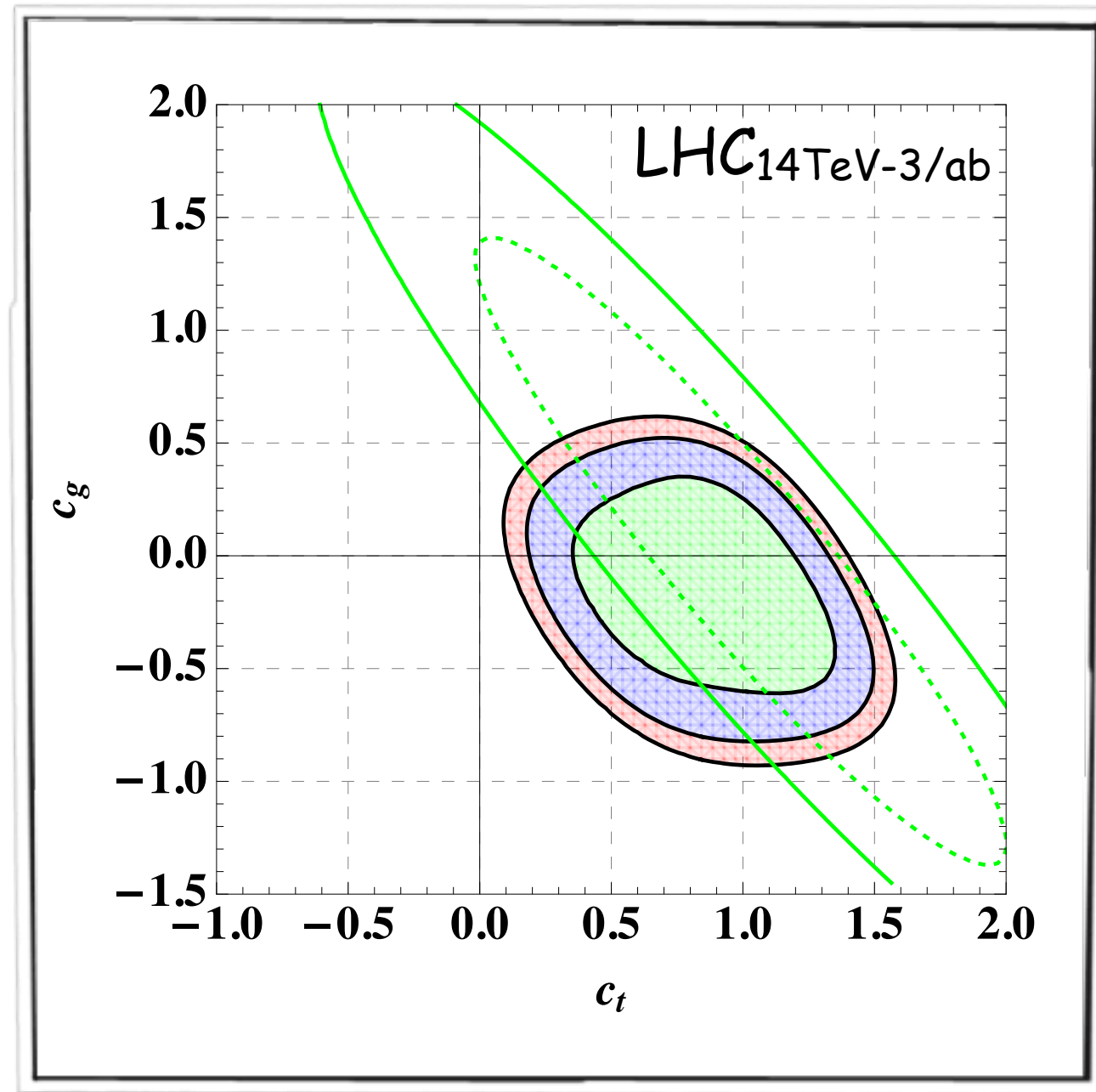
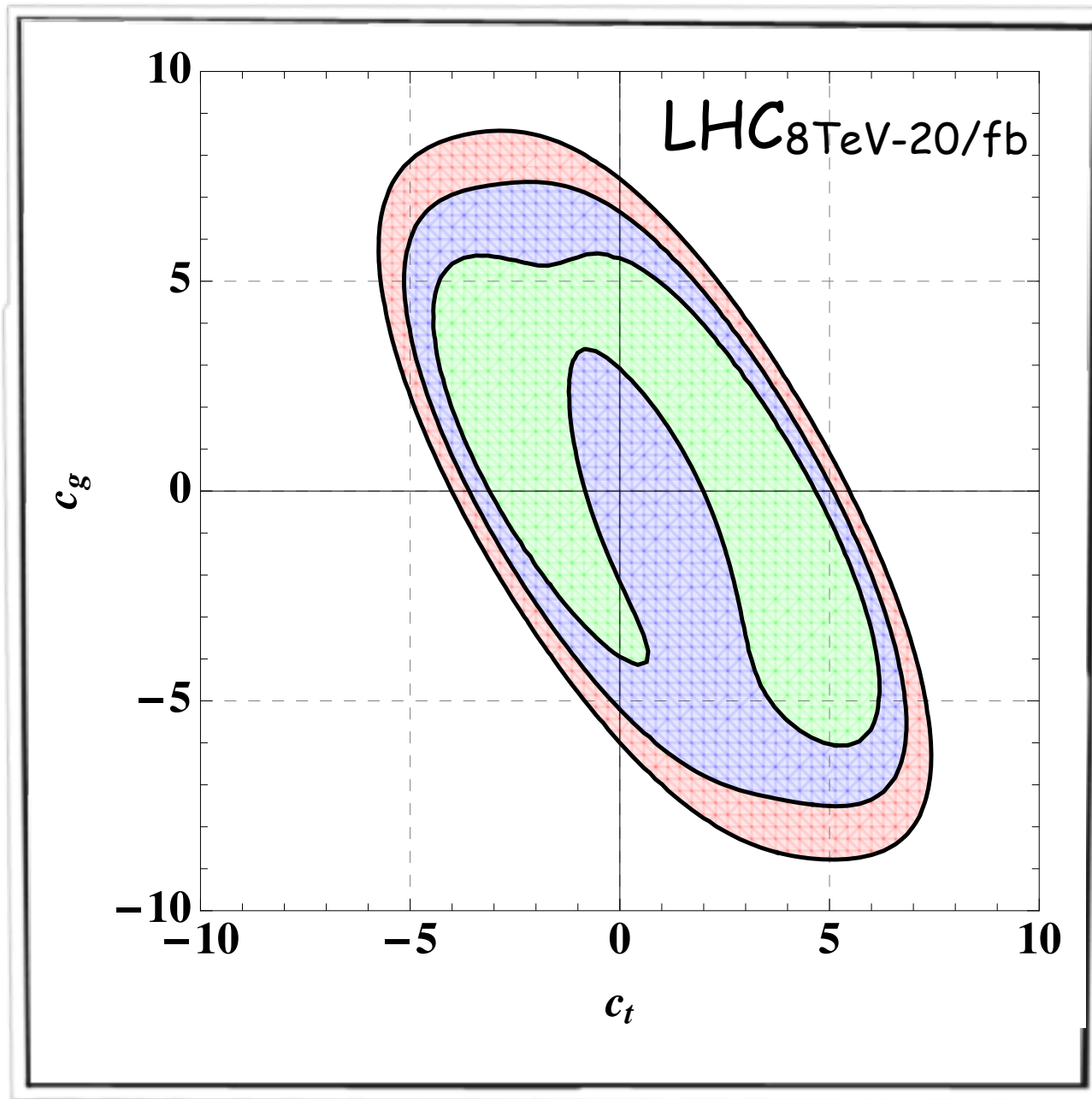
CMS interpretation in terms of bounds of the Higgs width is limited  
data can be better used to measure the structure of the couplings at high  $\sqrt{s}$

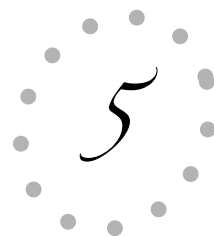


# Off-shell Higgs: $gg \rightarrow h^* \rightarrow ZZ \rightarrow 4l$

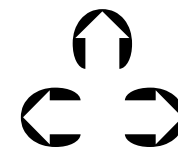
off-shell effects enhanced by the particular couplings of  $H$  to  $V_L$

Azatov, Grojean, Paul, Salvioni '14



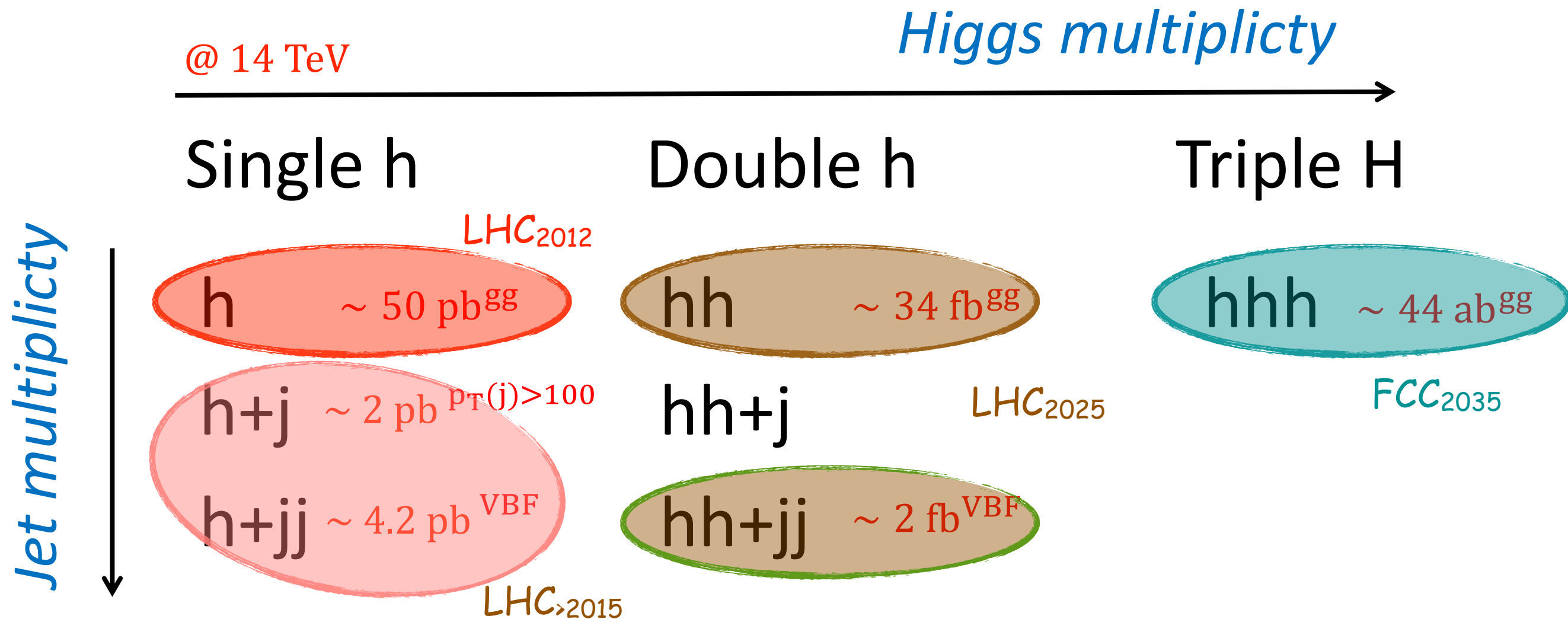


# Multi-Higgs channels



# Beyond single Higgs processes

Producing one Higgs is good. Producing H+X is better



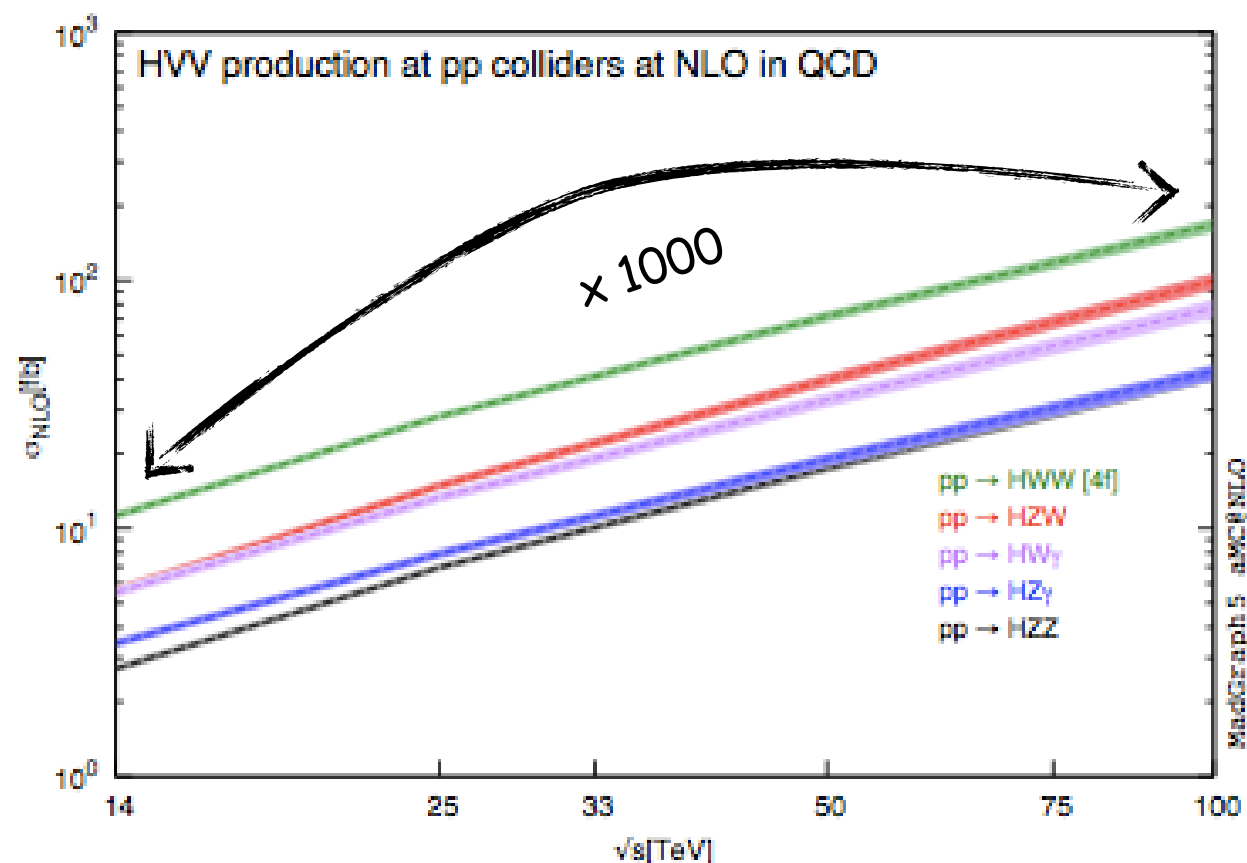
- also roughly indicates possible initial states/related kinematics
- Jet multiplicity might be replaced with V=W,Z, top, etc...

(adapted from M. Son@Planck2014)

# Beyond single Higgs processes

Producing one Higgs is good. Producing H+X is better  
A long term plan?

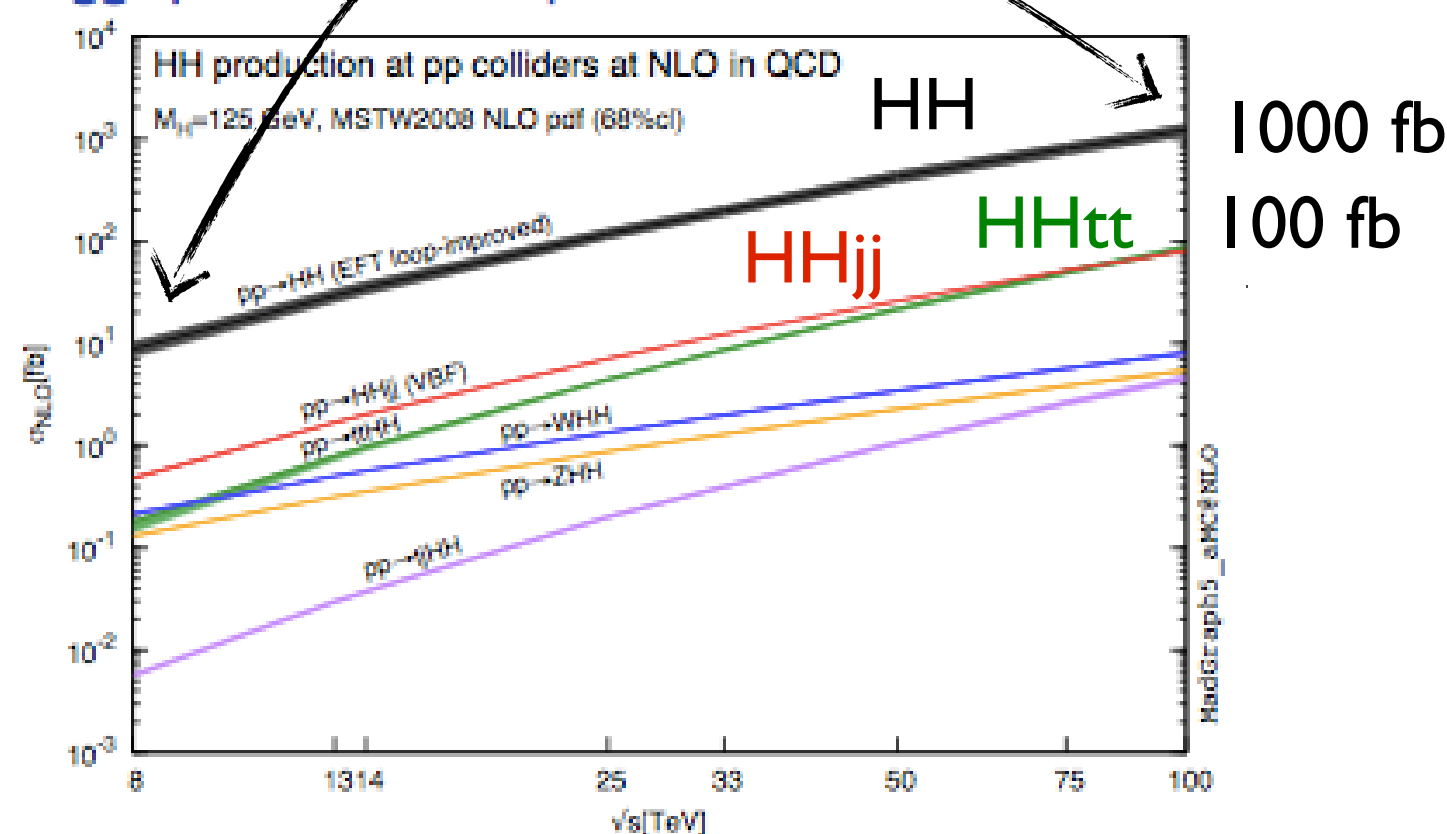
## Higgs-diboson associated production



100 fb

FCC = H+X factory

## Higgs-pair associated production



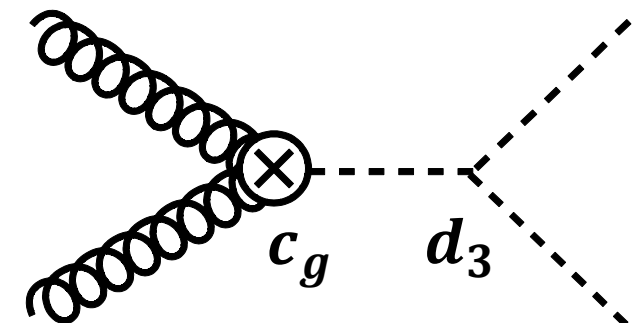
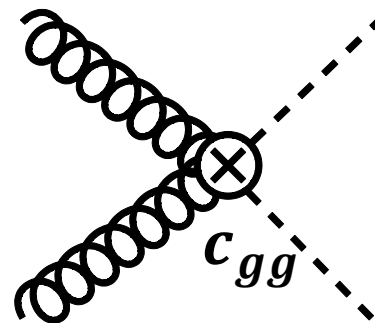
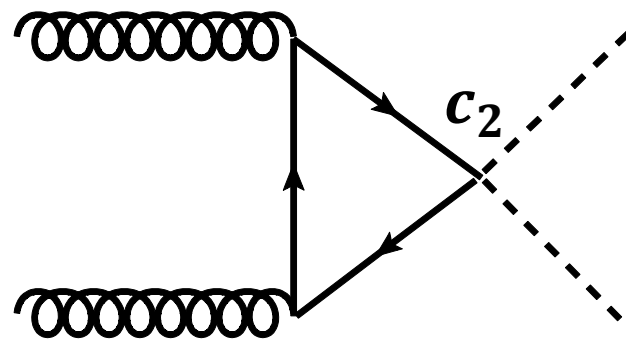
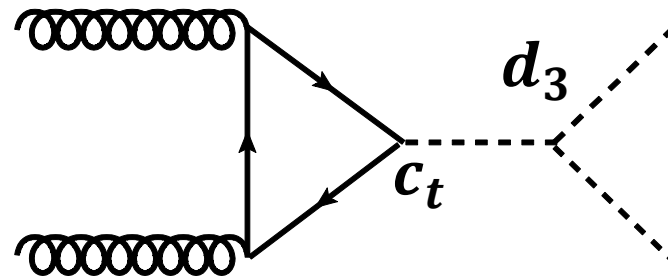
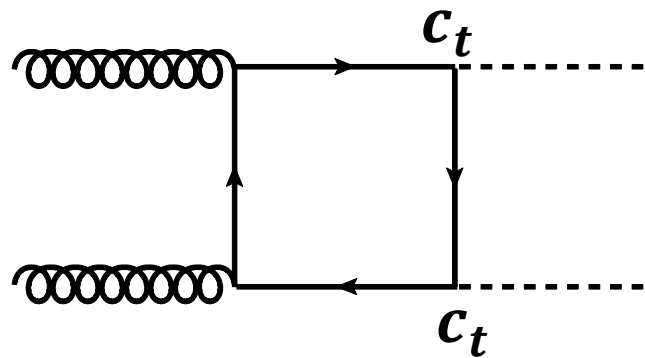
1000 fb  
100 fb

(Plots from P. Torrielli and MLM, CERN'14)



# What do we learn from $gg \rightarrow HH$ ?

in principle  $gg \rightarrow HH$  gives access to many new couplings, including non-linear couplings



In practice, if the Higgs is part of an EW doublet, these new couplings are related to single-Higgs couplings

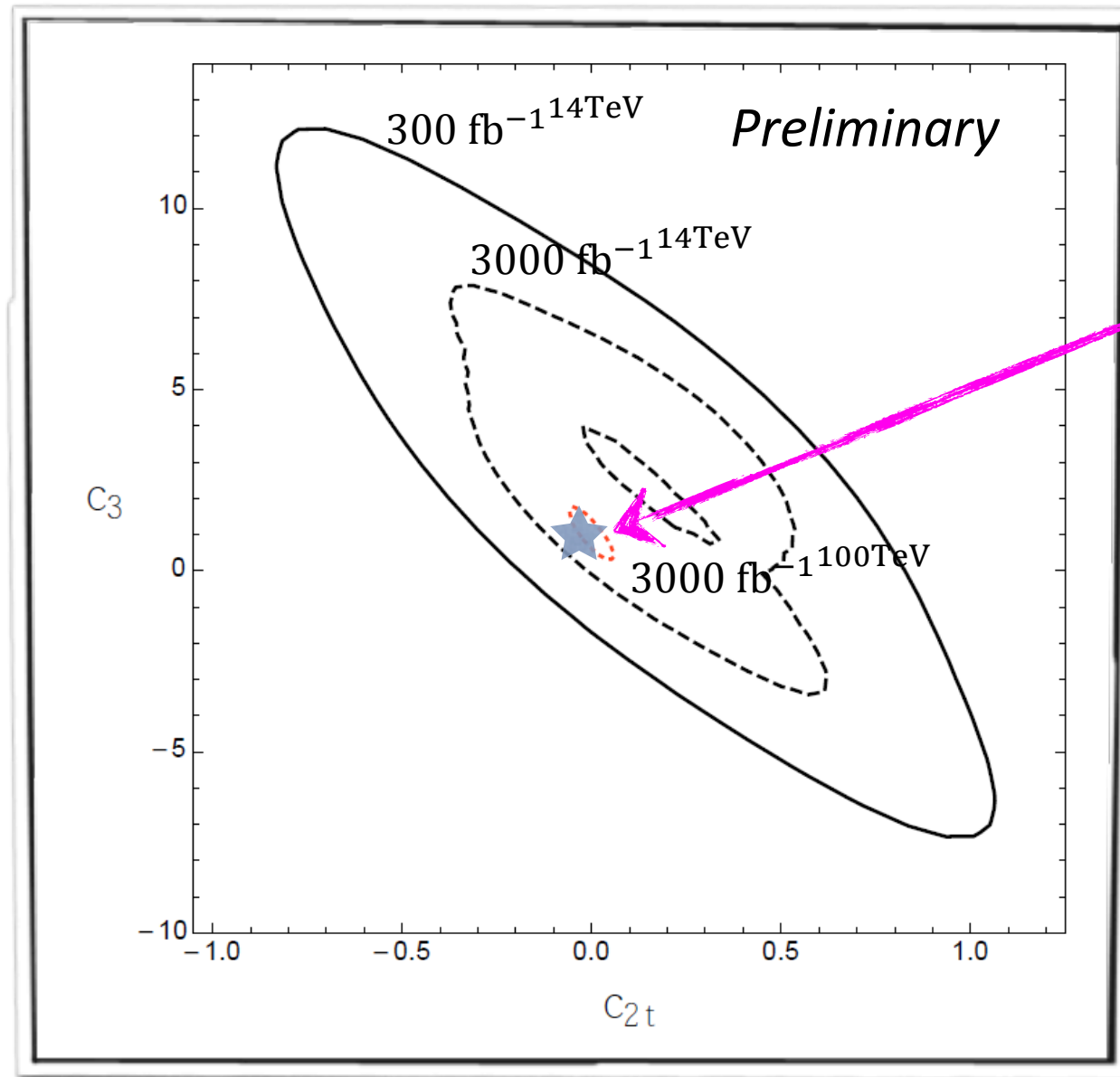
$$c_{2t} = 3(c_t - 1) \quad c_{gg} = c_g$$

Examples of connection between 1-Higgs and 2-Higgs vertices

Important to measure independently these vertices

and check the relations imposed by structure/symmetries/dynamics of the theory

# What do we learn from $gg \rightarrow HH$ ?



SM

Azatov, Contino, Panico, Son '15

see also Goertz, Papaefstathiou, Yang, Zurita '14

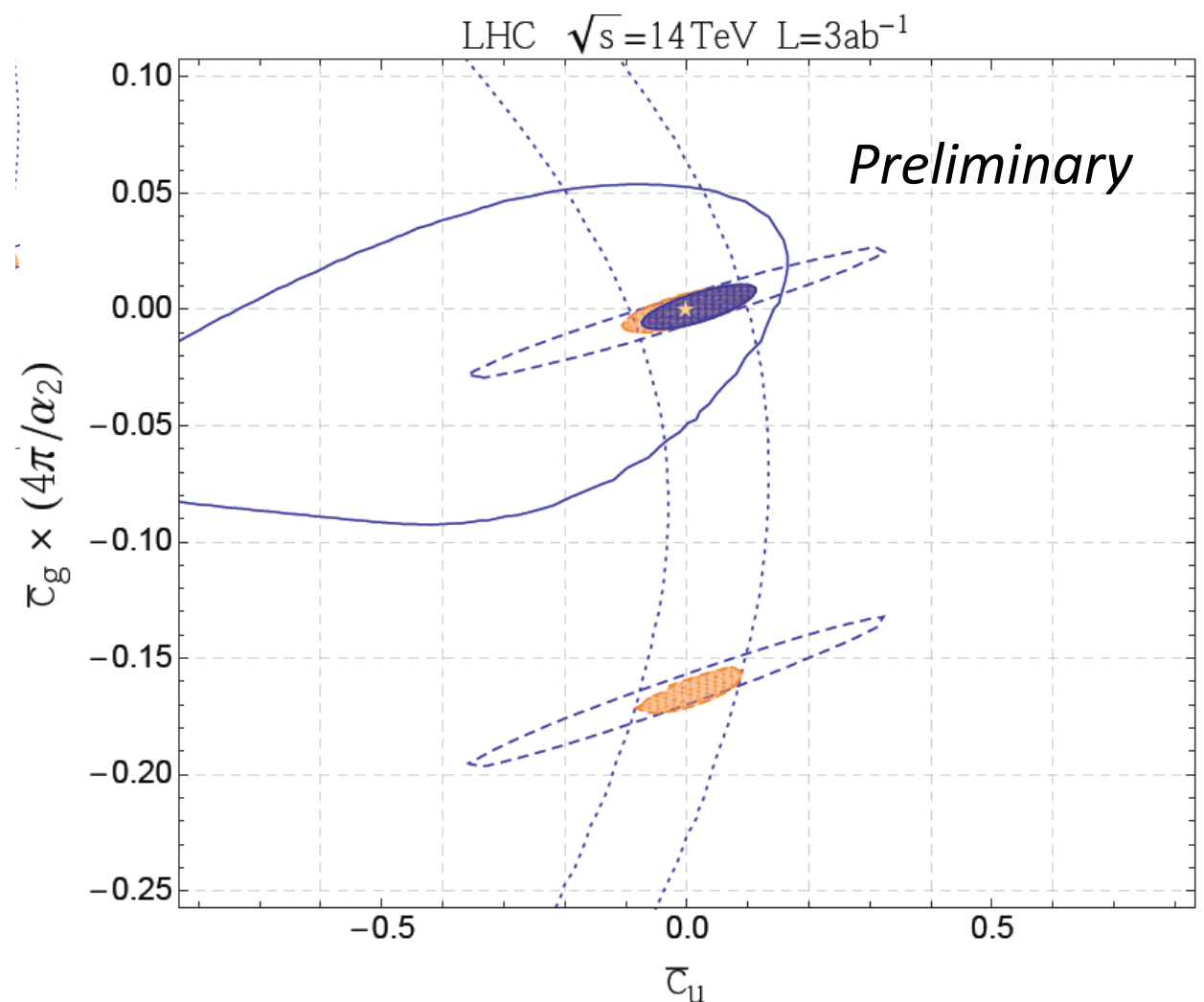
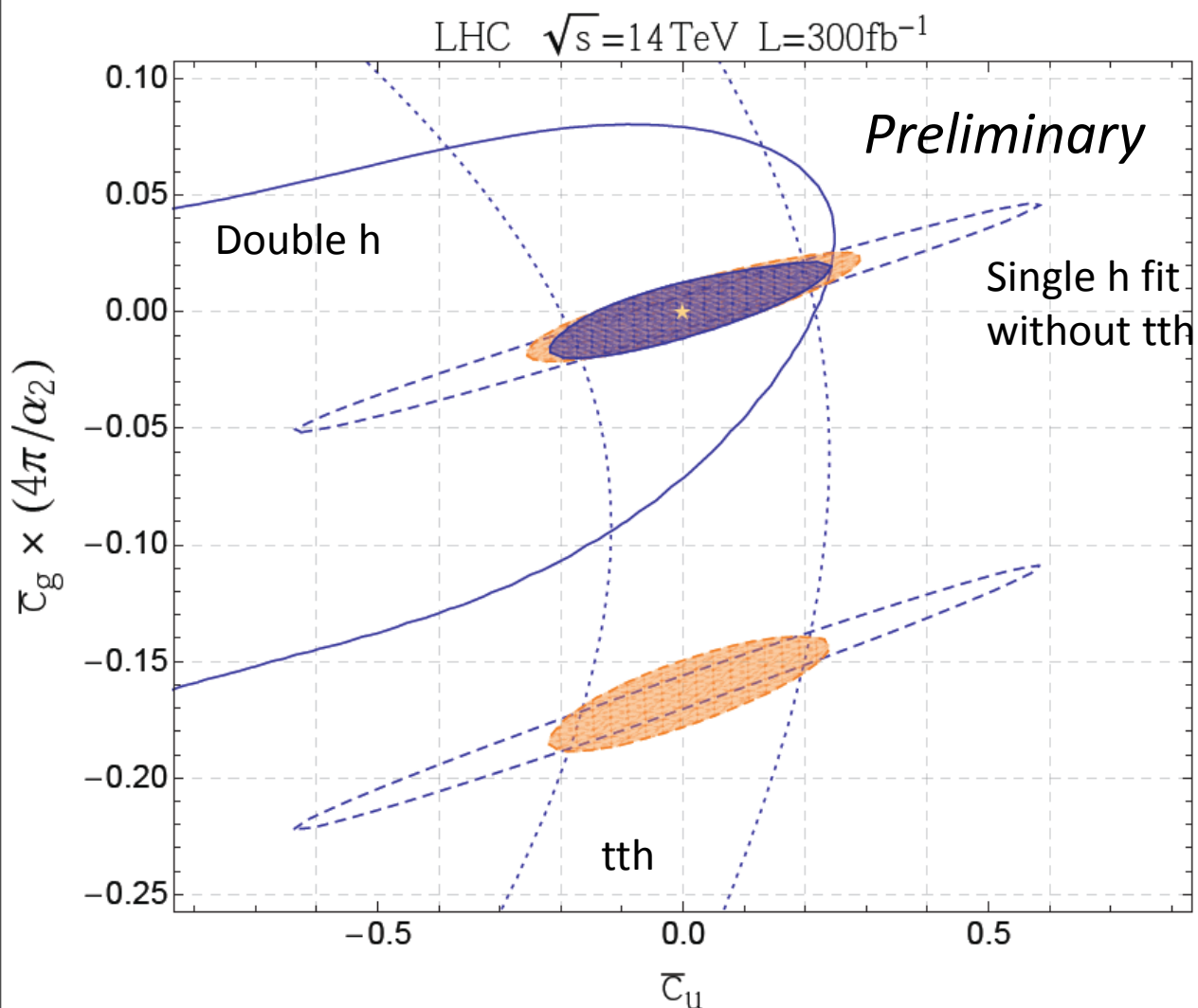
## Remarks:

- unique access to  $c_3$  but sensitivity is limited (within the validity of EFT?).
- statistically limited, with more luminosity
  - ⇒ access to distribution
  - ⇒ discriminating power  $c_3$  vs.  $c_{2t}$  vs  $c_g$

# What do we learn from $gg \rightarrow HH$ ?

in principle  $gg \rightarrow HH$  gives access to many new couplings, including non-linear couplings

after marginalizing over  $c_3$ , HH channel provides additional infos on single Higgs couplings



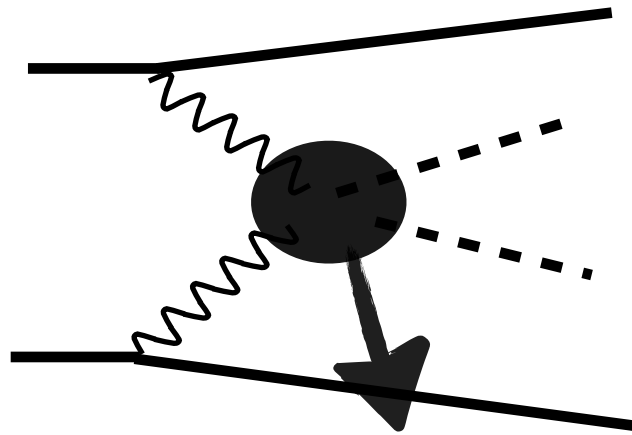
Azatov, Contino, Panico, Son 'to appear

HH channel is useful to break the degeneracy  
between 2 minima in the fit of single Higgs processes

# Multiple Higgs interactions in $WW \rightarrow HH$

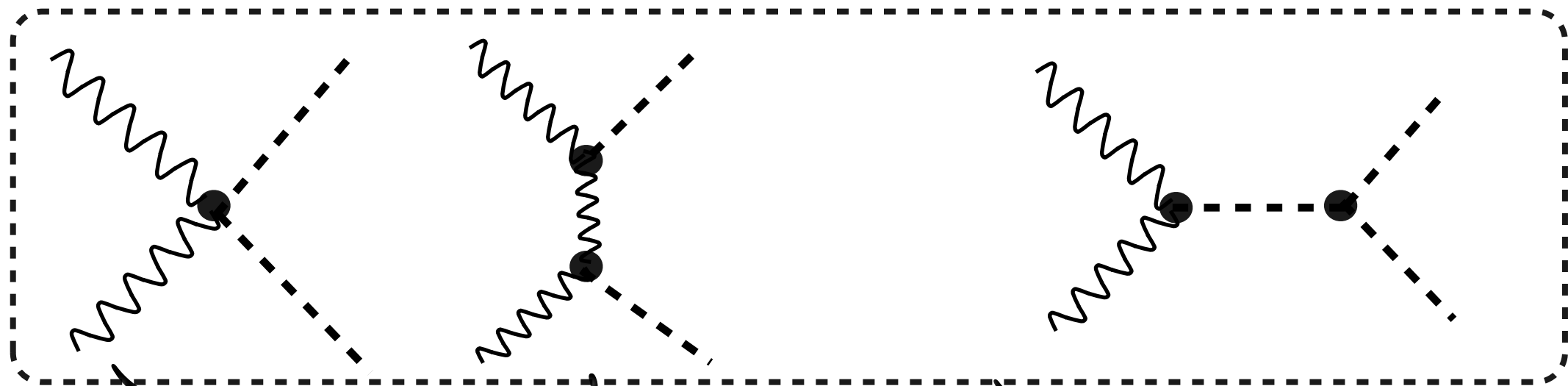
in the SM, the Higgs is essential to prevent strong interactions in EWSB sector

(e.g.  $WW$  scattering) Contino, Grojean, Moretti, Piccini, Rattazzi '10



$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) \quad \text{SM: } a=b=d_3=d_4=1$$

$$V(h) = \frac{1}{2} m_h^2 h^2 + d_3 \frac{1}{6} \left( \frac{3m_h^2}{v} \right) h^3 + d_4 \frac{1}{24} \left( \frac{3m_h^2}{v^2} \right) h^4 + \dots$$



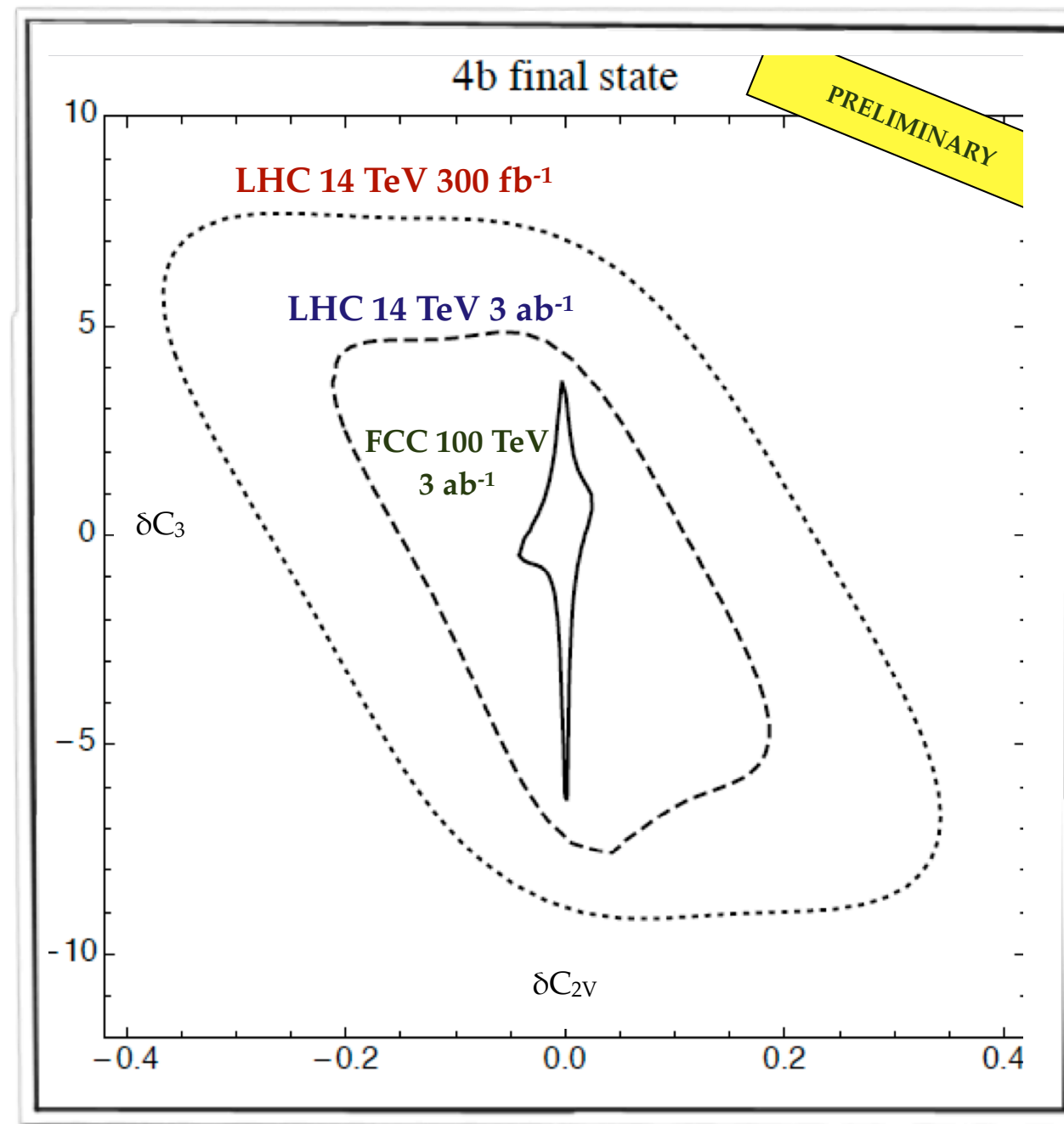
$$A \sim (b - a^2) \frac{4m_{hh}^2}{v^2} \quad m_{hh}^2 \gg m_W^2$$

asymptotic behavior  
sensitive to strong interaction

$$A \sim \text{cst.} + 3ad_3 \frac{m_h^2}{v^2} \quad m_{hh}^2 \sim 4m_h^2$$

threshold effect  
anomalous coupling'

# Multiple Higgs interactions in $WW \rightarrow HH$

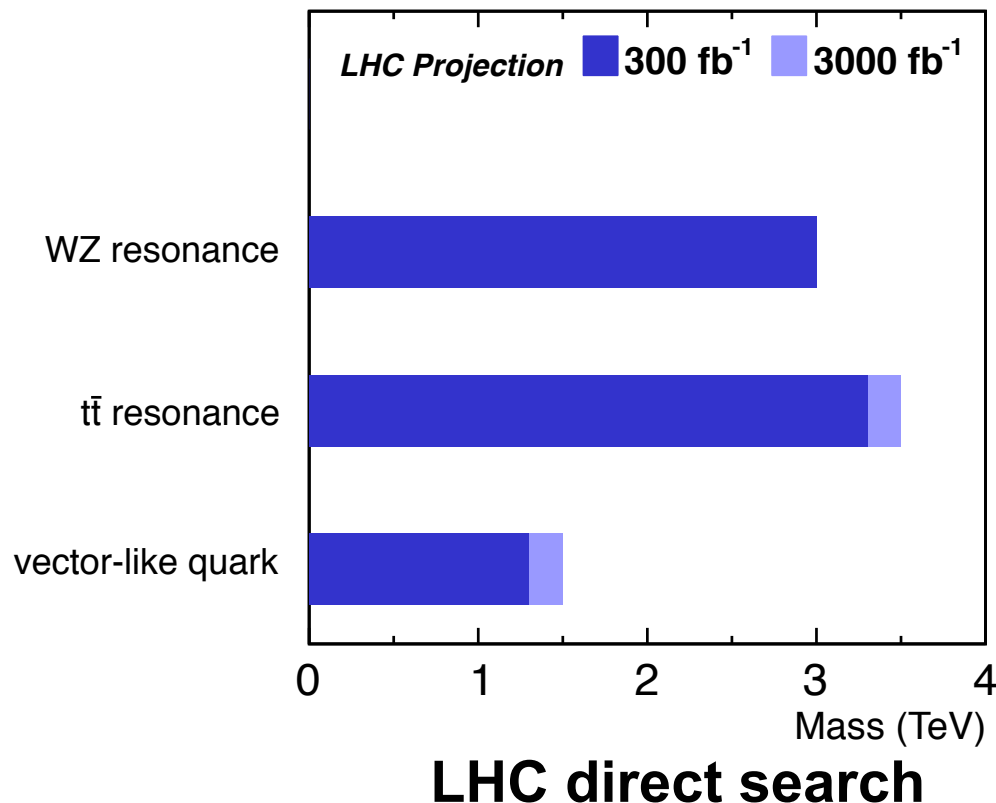
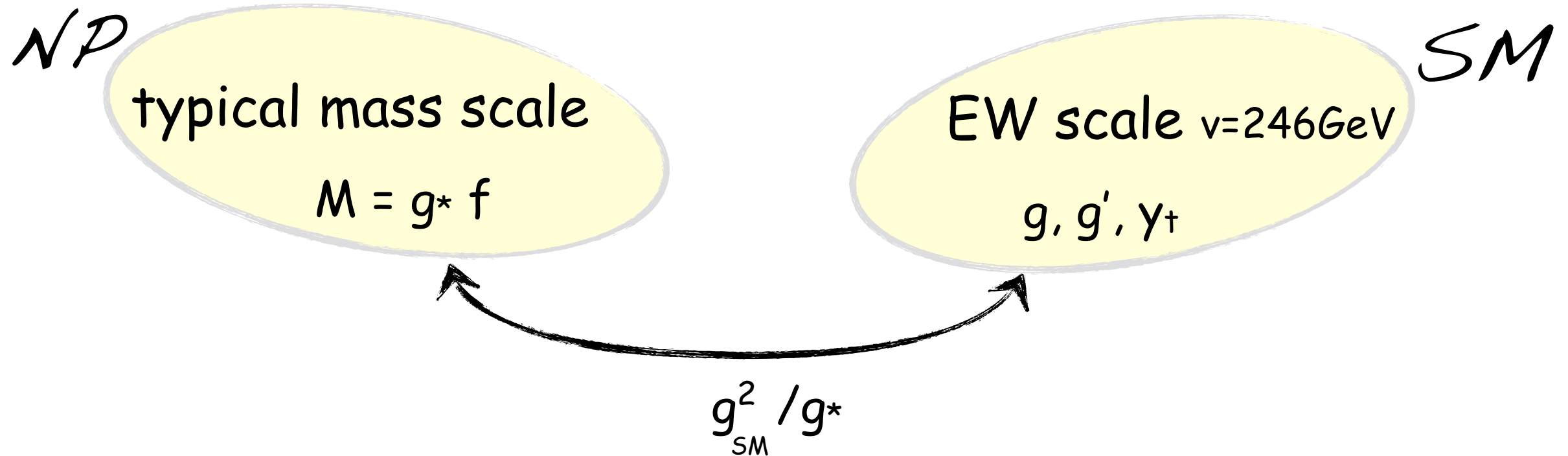


Bondu, Contino, Massironi, Rojo 'to appear

# Conclusions: Higgs & New Physics - a love affair

Precision /indirect searches (high lumi.) vs. direct searches (high energy)

Contino, Grojean, Pappadopulo, Rattazzi, Thamm '13



○ Precision Higgs study:  $\xi \equiv \frac{\delta g}{g} = \frac{v^2}{f^2}$

○ Direct searches for resonances:  $m_\rho \approx g_* f$

Which one is doing best?  
it depends on value of  $g_*$



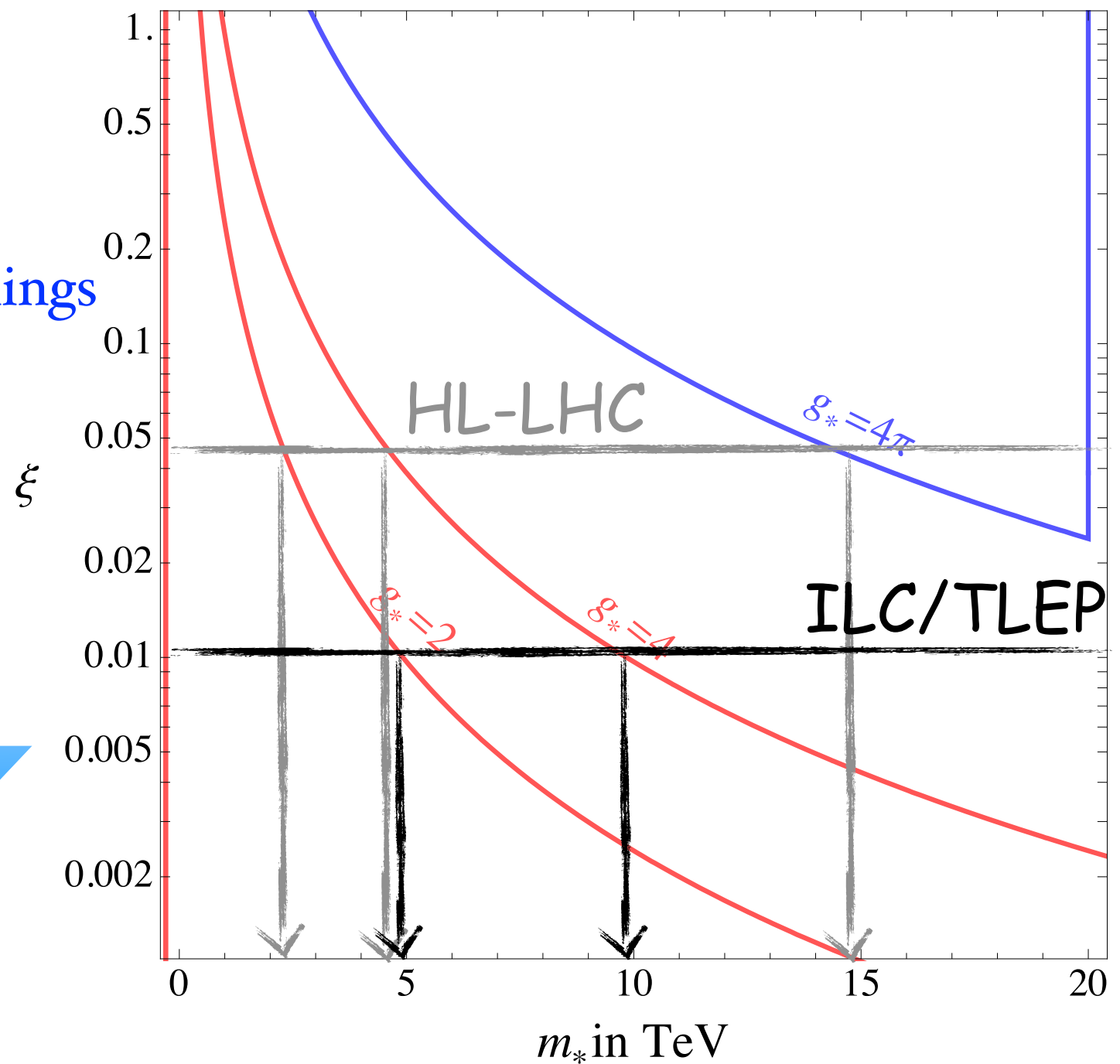
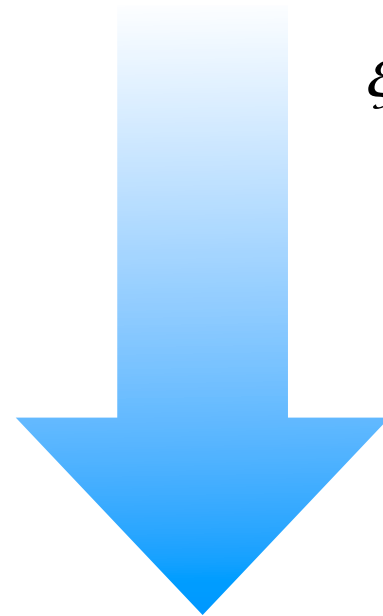
# Conclusions: Higgs & New Physics - a love affair

Precision /indirect searches (high lumi.) vs. direct searches (high energy)

Contino, Grojean, Pappadopulo, Rattazzi, Thamm '13

► nice complementarity between direct searches and precision Higgs physics

Higgs couplings



direct searches



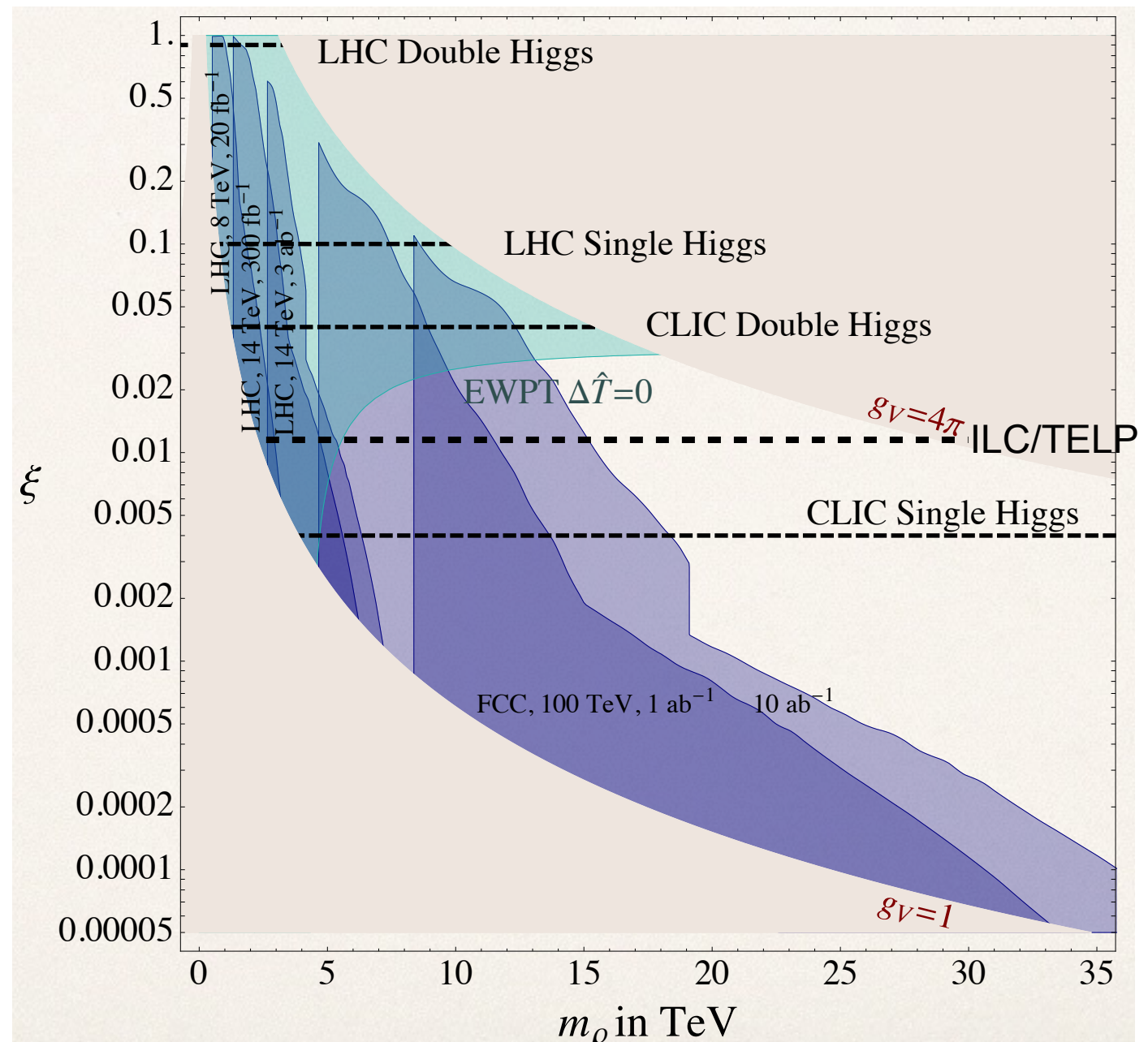
Rattazzi, BSM@100TeV, CERN '14

# Conclusions: Higgs & New Physics - a love affair

Precision /indirect searches (high lumi.) vs. direct searches (high energy)

► large region of parameter space already disfavored by EW precision data

► complementarity between direct searches @ hadron machine and indirect higgs measurements @ lepton machine



Contino, Grojean, Pappadopulo, Rattazzi, Thamm '13

Torre, Thamm, Wulzer '14

a deviation in Higgs couplings also teaches us on the maximum mass scale to search for!  
e.g. 10% deviation  $\Rightarrow m_V < 10\text{TeV}$  i.e. resonance within the reach of FCC-hh

# Conclusions

"Higgs = emergency tire of the SM"

Altarelli @ Blois'10



[picture courtesy to Andreas Weiler]

Soon the LHC run 2 will start exploring a new energy domain...  
while waiting for other big machines (ILC, CLIC, FCC-ee, FCC-hh).  
You have a chance to be part of this exciting adventure.

Good luck!