

Semi-microscopic description of core excitations in halo nuclei within breakup reactions

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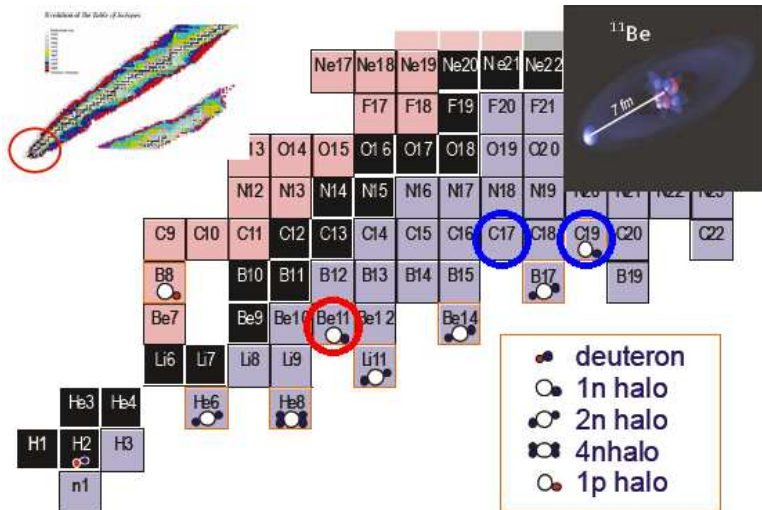
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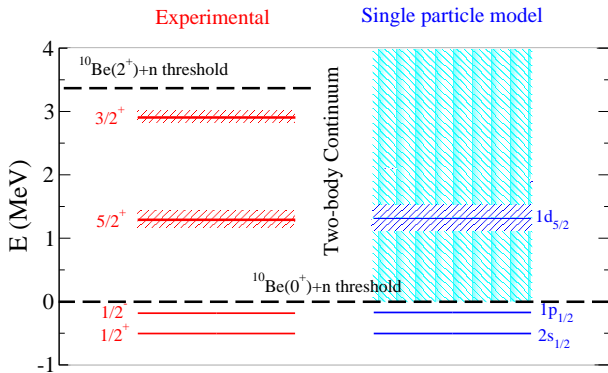
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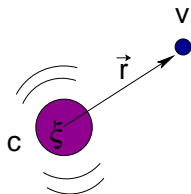
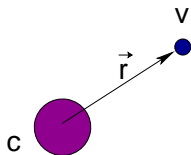
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Trento, 20th October 2014





^{11}Be in a single particle model



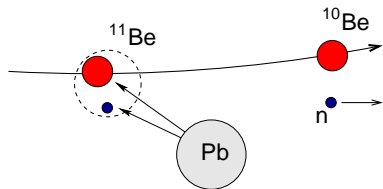
✗ No core excitations

$$|^{11}\text{Be}(1/2^+)\rangle = |^{10}\text{Be}(0^+ \text{ g.s.}) \otimes \nu s_{1/2}\rangle$$

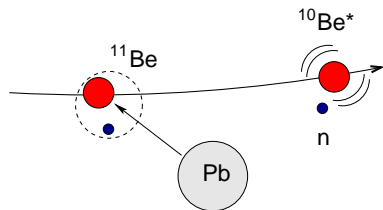
✓ Core excitations

$$|^{11}\text{Be}(1/2^+)\rangle = \alpha |^{10}\text{Be}(0^+ \text{ g.s.}) \otimes \nu s_{1/2}\rangle + \beta |^{10}\text{Be}(2^+) \otimes \nu d_{5/2}\rangle + \dots$$

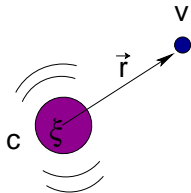
$|\alpha|^2, |\beta|^2 = \text{spectroscopic factors}$



✗ Pure valence excitation



✓ Core-excitation mechanism



Hamiltonian with core excitation

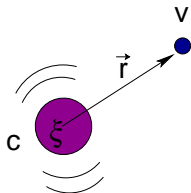
$$\mathcal{H}_p = T(\vec{r}) + h_{core}(\xi) + V_{NC}(\vec{r}, \vec{\xi})$$

Model for the core $h_{core}(\xi)$

- Selecting the model space \Rightarrow which states are included
- The model for core excitations will determine $V_{NC}(\vec{r}, \vec{\xi})$

Same formalism for different interaction models:

- Particle-Rotor model (deformed core)
- Particle-Vibration
- From microscopic transition densities
- ...



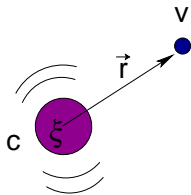
Hamiltonian with core excitation

$$\mathcal{H}_p = T(\vec{r}) + h_{\text{core}}(\xi) + V_{NC}(\vec{r}, \vec{\xi})$$

We look for a basis including core degrees of freedom

Coupling core $\varphi_I(\vec{\xi})$ and single particle $\mathcal{Y}_{lsj}(\hat{r})$ to the total J_p

⇒ n_α different possible combinations or channels $\alpha = \{l, s, j, I\}$



Hamiltonian with core excitation

$$\mathcal{H}_p = T(\vec{r}) + h_{core}(\xi) + V_{NC}(\vec{r}, \vec{\xi})$$

Set of \mathcal{L}^2 functions in this scheme:

$$|\phi_{i,J_p}(\vec{r}, \vec{\xi})\rangle = \sum_{\alpha} R_{i,\alpha}^{THO}(r) \left[\mathcal{Y}_{\ell s j}(\hat{r}) \otimes \varphi_I(\vec{\xi}) \right]_{J_p} \quad i = 1, \dots, N$$

⇒ Total number of functions: N times the number of channels

$$N \cdot n_{\alpha}$$

Pseudo-states (PS) discretization method

- Discrete set of \mathcal{L}^2 functions: $|\phi_n\rangle$

Completeness condition:

$$\sum^N |\phi_i\rangle\langle\phi_i| \approx \mathbf{I}$$

- To diagonalize the internal Hamiltonian of a projectile \mathcal{H}_p

Matrix elements:

$$\mathcal{H}_p \mapsto \sum_{n,n'} |\phi_n\rangle\langle\phi_n|\mathcal{H}_p|\phi_{n'}\rangle\langle\phi_{n'}|$$

Pseudo-states (PS) discretization method

Eigenstates of the matrix $N \times N$:

$$|\varphi_n^{(N)}\rangle = \sum^N C_i^n |\phi_i\rangle$$

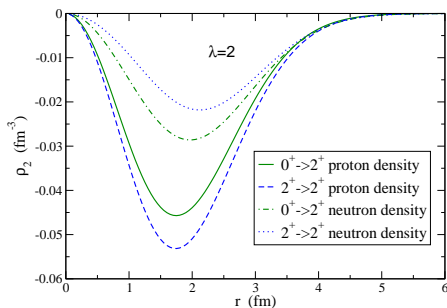
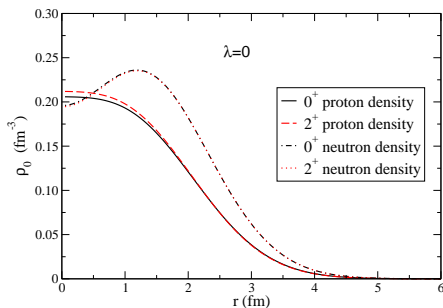
- n_b states with $\varepsilon_n < 0$ representing the bound states.
- $N - n_b, \varepsilon_n > 0 \Rightarrow$ discrete representation of the Continuum
- Orthogonal and normalizable.

What is the most suitable basis? Lagrange, Sturmian, Harmonic Oscillator?

HO vs THO:

$$\phi(s) \mapsto e^{-\left(\frac{s}{b}\right)^2} \quad \Longrightarrow \quad \phi[s(r)] \mapsto e^{-\frac{\gamma^2}{2b^2}r}$$

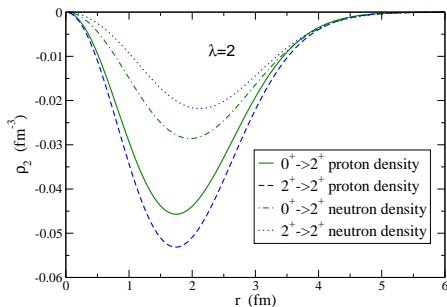
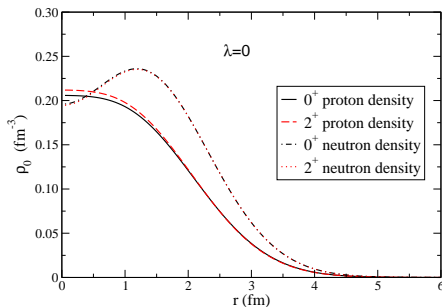
P-AMD



Densities from Antisymmetrized Molecular Dynamics (AMD)

Y. Kanada-En'yo *et al.* Phys. Rev. C 60, 064304 (1999)

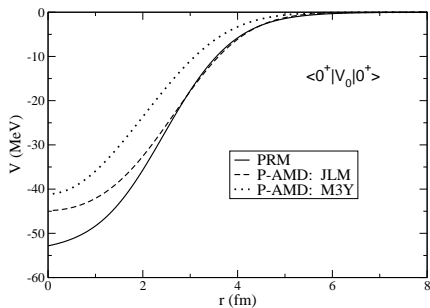
P-AMD



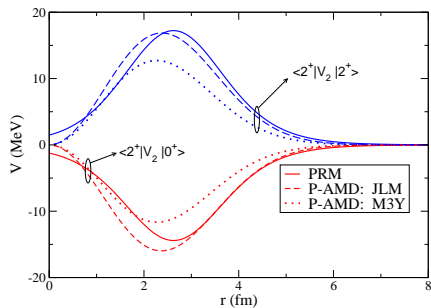
$$\langle I || V_{NC}^\lambda(r, \vec{\xi}) || I' \rangle = \int dr' \left[\langle I || \rho_\lambda(r', \xi) || I' \rangle v_{nn}(|\vec{r} - \vec{r}'|) \right]$$

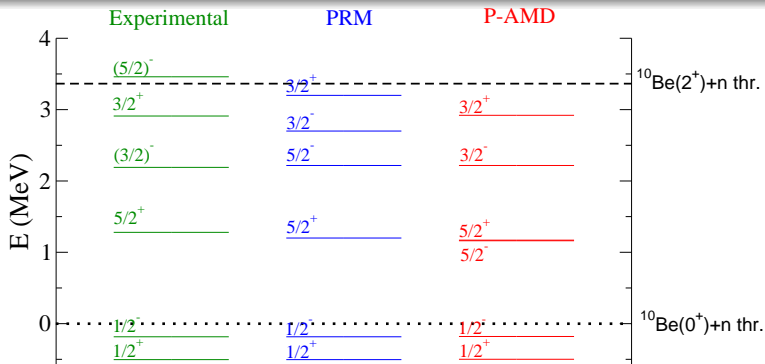
JLM interaction Phys. Rev. C 16, 80 (1977).

P-AMD



PRC89, 014333 (2014)

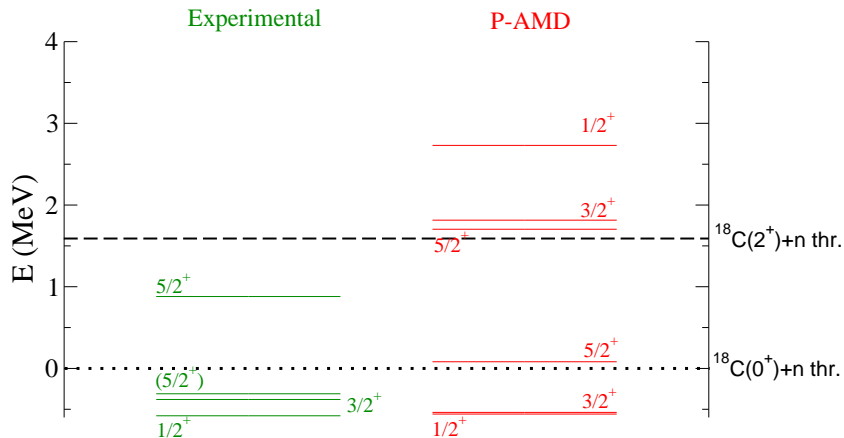


^{11}Be Spectrum

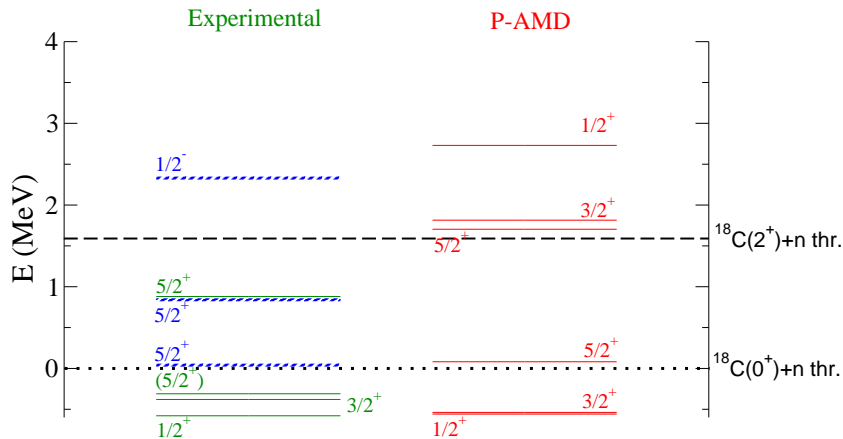
Renormalization factors

$$\lambda_+ = 1.058 \text{ and } \lambda_- = 0.995$$

PRC 70, 054606 (2004); PRC 81, 034321 (2010); PL B 611, 239 (2005).

^{19}C Spectrum

PL B 660, 320 (2008); PL B 614, 174 (2005) SAMURAI

^{19}C Spectrum

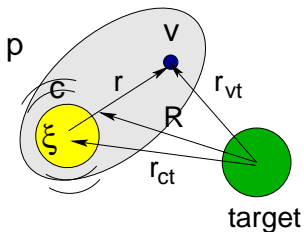
PL B 660, 320 (2008); PL B 614, 174 (2005) **SAMURAI**

Reactions

DWBAx

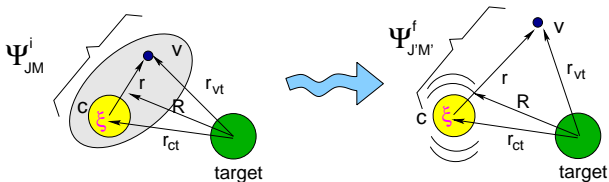
$^{19}\text{C}+p$ @ 67 MeV/u

DWBAx calculations



No-recoil approach

- ⇒ Only first order excitation.
 - ⇒ Same results for these energies than XCDCC.
- A. M. Moro *et al.* AIP Conf. Proc. 1491, 335 (2012)



$$T_{if}^{JM, J'M'} \approx T_{val}^{JM, J'M'} + T_{core}^{JM, J'M'}$$

Only first order plus no-recoil:

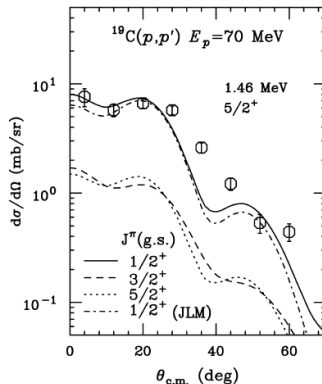
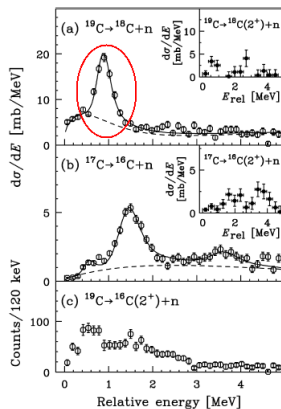
- ① $T_{val}^{JM, J'M'} \Rightarrow$ Valence excitations
- ② $T_{core}^{JM, J'M'} \Rightarrow$ Core excitations

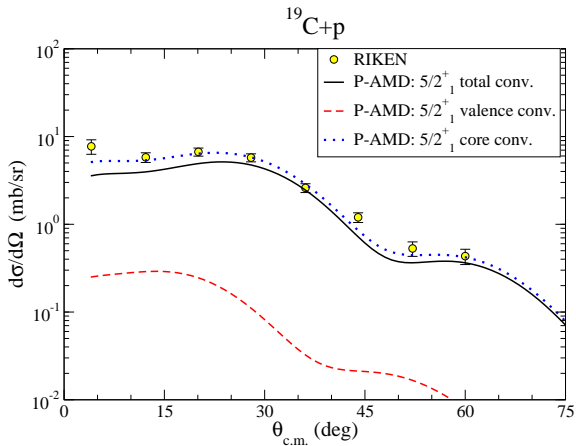
\Rightarrow They explicitly separates in the calculation

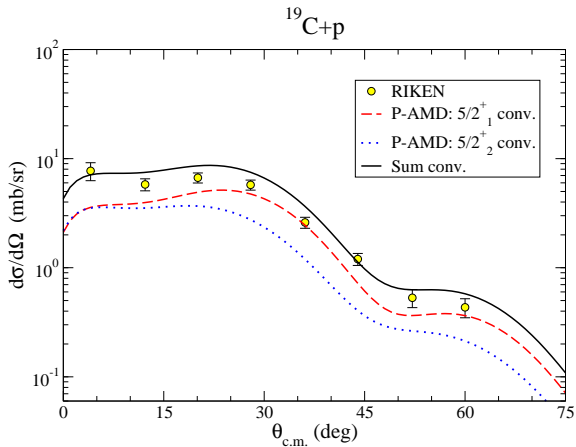
A. M. Moro & R. Crespo, Phys. Rev. C 85, 054613 (2012)

\Rightarrow We can extract spectroscopic factors from their interference

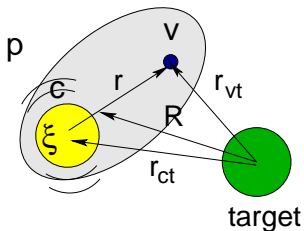
A. M. Moro & J. A. Lay, Phys. Rev. Lett. 109, 232502 (2012)

$^{19}\text{C}+p$ @ 67 MeV/uY. Satou *et al.*, Phys. Lett. B 660, 320 (2008).Microscopic DWBA calculations suggest a $1/2^+ \Rightarrow 5/2^+$ transition

$^{19}\text{C}+p$ @ 67 MeV/u

$^{19}\text{C}+p$ @ 67 MeV/u

XCDCC calculations



Including core excitations in CDCC

- ⇒ We already showed how to discretize the continuum with core excitations
- ⇒ DWBA only valid for intermediate and high energies
- ⇒ CDCC also includes the effect of break up in the elastic cross section

👉 *V. Pseudo's Talk*

P-AMD

- Accurate **semi-microscopic description** of even-odd halo nuclei
- Predictive power for unknown halo nuclei like $^{19,21}\text{C}$
- Could be able to include **core excitations from different sources**

Break up

- The **interplay** between **core and valence contributions** is crucial to understand resonant break up of halo nuclei
- **Break up reactions** are sensitive to **spectroscopic factors** of resonant states difficult to populate in traditional transfer reactions

Next steps

- Apply the P-AMD model with other densities and other halo nuclei
- Perform full PS-XCDCC calculations with the P-AMD model
- Continue for inclusive observables

Thank you!!

And also to:

Theory

- University of Seville : J. Gómez-Camacho
- University of Lisbon : R. Crespo
- University of Surrey : R. C Johnson
- Yukawa Institute, Kyoto University : Y. Kanada-En'yo

Experiment

- IEM-CSIC, Madrid : V. Pesudo, M. J. G. Borge, O. Tengblad
- S1202 Collaboration (formerly E1104)