

## Study of $b$ -hadron to $J/\psi h^+ h^-$ decays

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### Abstract

Using data collected by the LHCb detector corresponding to an integrated luminosity of  $3 \text{ fb}^{-1}$ , several types of  $b$ -hadron to  $J/\psi h^+ h^-$  decays are studied. Reported are the most recent results including amplitude analyses of  $\bar{B}_s^0$  and  $\bar{B}^0 \rightarrow J/\psi \pi^+ \pi^-$  decays, precision measurement of lifetime ratio of  $\Lambda_b^0$  to  $\bar{B}^0$  using  $\Lambda_b^0 \rightarrow J/\psi p K^-$ , and first observation of a Cabibbo-suppressed decay  $\Lambda_b^0 \rightarrow J/\psi p \pi^-$ . Studies of  $f_0(980)$  and  $f_0(500)$  substructure are also discussed in  $\pi^+ \pi^-$  final states.

**Keywords:** Standard Model, Amplitude analysis, HEQ,  $B$  Lifetime, Cabibbo-suppressed decay, LHCb, Scalar mesons

### 1. Introduction

Decays  $\bar{B}_s^0$  and  $\bar{B}^0 \rightarrow J/\psi h^+ h^-$ , where  $h$  is either a pion or kaon, are useful for  $CP$  violation measurements [1, 2] and  $\bar{B}_s^0$ , in particular, is used for New Physics searches [3]. (Charged conjugated modes are also used when appropriate.) In order to best exploit these decays, a better understanding of the final state composition is necessary. The study of  $b$ -baryon charmonium decays is of considerable interest both to probe the dynamics of heavy flavour decay processes and to search for the effects of physics beyond the Standard Model.

Here, we report the recent studies performed using the run I data collected by the LHCb detector [4], corresponding to an integrated luminosity of  $3 \text{ fb}^{-1}$ . There are also other decays I didn't cover, especially  $\bar{B}_s^0$  [5] and  $\bar{B}^0 \rightarrow J/\psi K^+ K^-$  [6] that have been studied with the  $1 \text{ fb}^{-1}$  LHCb data. Thanks to the  $J/\psi \rightarrow \mu^+ \mu^-$  decays, for same number of final particles charmonium modes generally have higher reconstruction and trigger efficiencies than hadronic modes at LHCb.

### 2. Amplitude analyses of $\bar{B}_{(s)}^0 \rightarrow J/\psi \pi^+ \pi^-$ decays

The decay also provides an excellent environment for study of the light scalar states which decay to a  $\pi^+ \pi^-$  pair, e.g.  $f_0(980)$  and  $f_0(500)$  also called  $\sigma$ . Figure 1 shows the leading order diagrams for the two decays, where only  $s\bar{s}$  content is involved in the  $\bar{B}_s^0$  decays and  $d\bar{d}$  in the  $\bar{B}^0$  decays. We have used time-integrated amplitude analysis on both channels to understand the resonant structure and  $CP$  components of the decays using data of an integrated luminosity of  $3 \text{ fb}^{-1}$ .

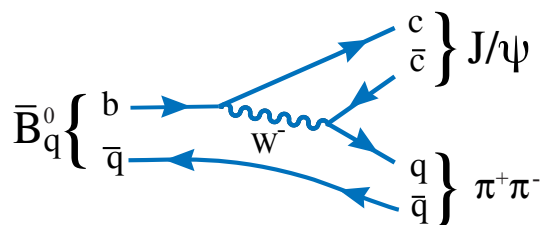


Figure 1: Leading order diagram for  $\bar{B}_q^0$  decays into  $J/\psi \pi^+ \pi^-$ , where  $q = s$  or  $d$ .

The decay  $\bar{B}_s^0$  or  $\bar{B}^0 \rightarrow J/\psi \pi^+ \pi^-$  with  $J/\psi \rightarrow \mu^+ \mu^-$  is described by 4 variables, chosen to be the  $\pi^+ \pi^-$  mass and three helicity angles. Zhang and Stone developed

35 a new theoretical approach which includes all four vari-  
 36 ables and enables the measurement of the fractions of  
 37  $CP$ -even and -odd transversity states [7]<sup>1</sup>. Since one of  
 38 the particles in the final state, the  $J/\psi$ , has spin 1, its  
 39 three decay amplitudes must be considered, while the  
 40  $\pi^+\pi^-$  system is described as the coherent sum of reso-  
 41 nant and possibly nonresonant amplitudes.

42 The invariant mass of the selected  $J/\psi\pi^+\pi^-$  combi-  
 43 nations is shown in Fig. 2, where the dimuon is con-  
 44 strained to the  $J/\psi$  mass [8]. There are 27 400  $\bar{B}_s^0$  and  
 45 18 800  $\bar{B}^0$  signal events within  $\pm 20$  MeV of the respec-  
 46 tive peaks. The invariant masses of  $\pi^+\pi^-$  are shown in  
 47 Fig. 3 and 4 for the  $\bar{B}_s^0$  and  $\bar{B}^0$  candidates, respectively,  
 48 superimposed with fit function and each resonance con-  
 49 tribution. The two decays show very distinct spectra.

50 The  $\bar{B}_s^0$  decays can be described by 5 resonances:  
 51  $f_0(980)$ ,  $f_0(1500)$ ,  $f_0(1790)$ ,  $f_2(1270)$  and  $f_2'(1525)$  [9].  
 52 Another solution with a significant nonresonance compo-  
 53 nent along with these five resonances also describe the  
 54 data equally well. Even though the two solutions have  
 55 quite different fit fractions for the  $f_0(980)$ , the largest  
 56 final state component. Similar fractions are found for  
 57 the two spin-2 states in both solutions, and the total D-  
 58 wave fraction is 2.3%. As only perpendicular transversity  
 59 components of the two spin-2 states are  $CP$ -even,  
 60 we set the upper limit of  $CP$ -even fraction  $< 2.3\%$  at  
 61 95% confidence level (CL).

62 The  $\bar{B}^0$  decays can be described by 6 reso-  
 63 nances:  $\rho(770)$ ,  $f_0(500)$ ,  $f_2(1270)$ ,  $\omega(782)$ ,  $\rho(1450)$  and  
 64  $\rho(1700)$  [10]. The largest two contributions with fit  
 65 fractions are  $\rho(770)$  of  $(63.1 \pm 2.2^{+3.4}_{-2.2})\%$  and  $f_0(500)$   
 66 of  $(22.2 \pm 1.2^{+2.6}_{-3.5})\%$ . Whenever two uncertainties are  
 67 quoted, the first is statistical and the second is system-  
 68 atic. The  $CP$ -even fraction is 56%.

### 69 3. Substructure of the $f_0(980)$ and $f_0(500)$ mesons

70 Scalar mesons, especially the  $f_0(980)$ , are not well  
 71 understood. Their masses do not follow the expectation  
 72 in the naïve quark model that the state containing two  
 73 strange quarks is heavier than the state containing only  
 74 one, in stark contrast to the vector mesons [8]. Stone  
 75 and Zhang [11] suggested the use of  $B \rightarrow J/\psi f_0$  decays  
 76 to discern the  $q\bar{q}$  or tetraquark [12], i.e.  $[qq][\bar{q}\bar{q}]$ , nature  
 77 of scalar mesons. In the  $q\bar{q}$  model, the  $f_0(980)$ , denoted  
 78 as  $f_0$ , and the  $f_0(500)$ , denoted as  $\sigma$ , are considered as a  
 79 mixture of light and strange quarks governed by a single

<sup>1</sup>The approach is applied here after integrating over the decay time.

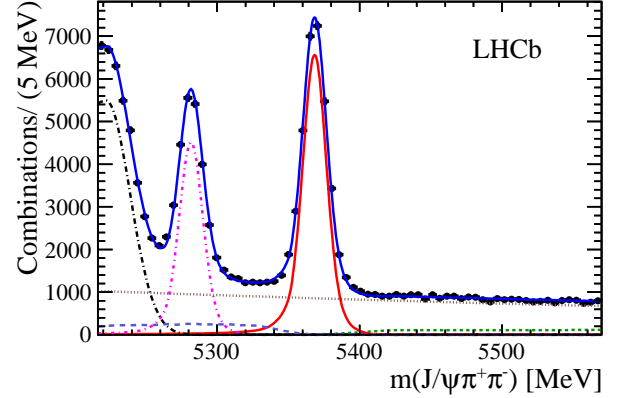


Figure 2: Invariant mass of  $J/\psi\pi^+\pi^-$  combinations. The data have been fitted with double Crystal Ball signals and several background functions. The (red) solid curve shows the  $\bar{B}_s^0$  signal, the (purple) dot-dashed curve is  $\bar{B}^0$  signal, the (brown) dotted line shows the combinatorial background, the (green) short-dashed line shows the  $B^-$  background, the (light blue) long-dashed line is the sum of  $\bar{B}_s^0 \rightarrow J/\psi\eta'$ ,  $\bar{B}_s^0 \rightarrow J/\psi\phi$  with  $\phi \rightarrow \pi^+\pi^-\pi^0$  backgrounds and the  $\Lambda_b^0 \rightarrow J/\psi K^- \pi$  reflection, the (black) dot-long dashed curve is the  $\bar{B}^0 \rightarrow J/\psi K^- \pi^+$  reflection and the (blue) solid curve is the total.

80 mixing angle  $\phi$ , so that their wave functions are

$$\begin{aligned} |f_0\rangle &= \cos\phi|s\bar{s}\rangle + \sin\phi|n\bar{n}\rangle \\ |\sigma\rangle &= -\sin\phi|s\bar{s}\rangle + \cos\phi|n\bar{n}\rangle, \end{aligned}$$

where  $|n\bar{n}\rangle \equiv \frac{1}{\sqrt{2}}(|u\bar{u}\rangle + |d\bar{d}\rangle)$ . (1)

When these states are viewed as  $q\bar{q}q\bar{q}$  states the wave functions becomes

$$|f_0\rangle = \frac{1}{\sqrt{2}}([su][\bar{s}\bar{u}] + [sd][\bar{s}\bar{d}]), \quad |\sigma\rangle = [ud][\bar{u}\bar{d}]. \quad (2)$$

81 Here the tetraquark states are considered to be unmixed,  
 82 for which there is some justification with a mixing angle  
 83 estimate of  $< 5^\circ$  [12]<sup>2</sup>.

Two ratios of decay widths suggested by Stone and Zhang [11] as discriminates between the two and four quark models are tested by the LHCb data. Table 1 shows the predictions of the two ratios compared between the  $q\bar{q}$  and the tetraquark models. LHCb measures both ratios of branching fraction are consistent with zero, as

$$\frac{\mathcal{B}(\bar{B}_s^0 \rightarrow J/\psi f_0(500), f_0(500) \rightarrow \pi^+\pi^-)}{\mathcal{B}(\bar{B}_s^0 \rightarrow J/\psi f_0(980), f_0(980) \rightarrow \pi^+\pi^-)} < 3.4\% \quad (3)$$

<sup>2</sup>The LHCb result using  $\bar{B}_s^0 \rightarrow J/\psi\pi^+\pi^-$  decays shown in Table 2 gives tetraquark mixing angle  $< 7.7^\circ$  at 90% CL.

Table 1: Ratios of decay widths and predictions of the value for  $r_{\bar{B}^0}$  in either the  $q\bar{q}$  model, or the tetraquark model. The form-factors are notated as  $F_i^j$ , and the phase space factor  $\Phi_j^i$ , where  $i$  indicates either  $\sigma$  or  $f_0$  and  $j$  indicates either  $\bar{B}^0$  or  $\bar{B}_s^0$ .

	Mode ratio	$q\bar{q}$	tetraquark
$\frac{\Gamma(\bar{B}_s^0 \rightarrow J/\psi \sigma)}{\Gamma(\bar{B}_s^0 \rightarrow J/\psi f_0)}$	$\frac{ F_{B_s^0}^\sigma(m_{J/\psi}^2) ^2 \Phi_{B_s^0}^\sigma}{ F_{B_s^0}^{f_0}(m_{J/\psi}^2) ^2 \Phi_{B_s^0}^{f_0}} \times r_{\bar{B}_s^0}$	$r_{\bar{B}_s^0} = \tan^2 \phi$	$r_{\bar{B}_s^0} = 0$
$\frac{\Gamma(\bar{B}^0 \rightarrow J/\psi f_0)}{\Gamma(\bar{B}^0 \rightarrow J/\psi \sigma)}$	$\frac{ F_{B^0}^{f_0}(m_{J/\psi}^2) ^2 \Phi_{B^0}^{f_0}}{ F_{B^0}^\sigma(m_{J/\psi}^2) ^2 \Phi_{B^0}^\sigma} \times r_{\bar{B}^0}$	$r_{\bar{B}^0} = \tan^2 \phi$	$r_{\bar{B}^0} = \frac{1}{2}$

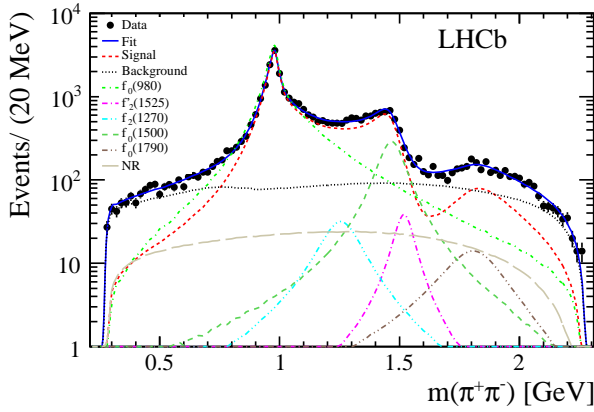


Figure 3: Invariant mass of  $\pi^+\pi^-$  from  $\bar{B}_s^0$  candidates.

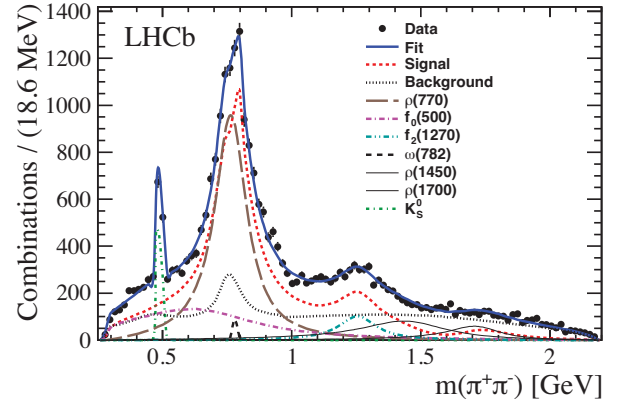


Figure 4: Invariant mass of  $\pi^+\pi^-$  from  $\bar{B}^0$  candidates.

at 90% CL, and

$$\frac{\mathcal{B}(\bar{B}^0 \rightarrow J/\psi f_0(980), f_0(980) \rightarrow \pi^+\pi^-)}{\mathcal{B}(\bar{B}^0 \rightarrow J/\psi f_0(500), f_0(500) \rightarrow \pi^+\pi^-)} = (0.6_{-0.4-2.6}^{+0.7+3.3})\% \quad (4)$$

To interpret the results, we use  $\mathcal{B}(f_0(980) \rightarrow \pi^+\pi^-) = (0.46 \pm 0.06)$  and  $\mathcal{B}(f_0(980) \rightarrow \pi^+\pi^-) = \frac{2}{3}$ , and phase space ratio  $\frac{\Phi_{f_0}^\sigma}{\Phi_{f_0}^{f_0}} = 1.25$ . The interpretation of the results is listed in Table 2. With current data, the pure  $q\bar{q}$  gives a consistent picture where both channels give upper limit on the mixing phase. Using the pure tetraquark model, the measured  $r_{\bar{B}^0}$  is inconsistent with the prediction of 50% at the 8 standard deviation level. Thus we have ruled out  $f_0(980)$  and  $f_0(500)$  being pure tetraquark state. The mixing of  $q\bar{q}$  and tetraquark for the scalar mesons is also possible [12]. In the calculations, we use the form factor ratios equal to 1. Both two and four quark models give the same prediction for the decay width ratio of  $\bar{B}_s^0 \rightarrow J/\psi f_0$  to  $\bar{B}^0 \rightarrow J/\psi \sigma$ . Using LHCb measured values, Ref. [11] verified that  $|F_{B_s^0}^{f_0}(m_{J/\psi}^2)/F_{B^0}^\sigma(m_{J/\psi}^2)| = 0.99_{-0.04}^{+0.13}$  consistent with 1.

Table 2: Interpretation of the results for substructure of the  $f_0(980)$  and  $f_0(500)$  mesons using either the  $q\bar{q}$  model or the tetraquark model, where the upper limits are at 90% CL.

Model	$\bar{B}_s^0 \rightarrow J/\psi \pi^+\pi^-$	$\bar{B}^0 \rightarrow J/\psi \pi^+\pi^-$
$q\bar{q}$	$ \phi  < 7.7^\circ$	$ \phi  < 17^\circ$
Tetraquark	$r_{\bar{B}_s^0} < 1.8\%$	$r_{\bar{B}^0} = (1.1_{-0.7-0.7}^{+1.2+6.0})\%$

#### 4. Precision measurement of $\Lambda_b^0$ to $\bar{B}^0$ lifetime ratio

The heavy quark expansion (HQE) theory, first developed in 1986 [13], is used to extract values of  $|V_{ub}|$  and  $|V_{cb}|$  from inclusive  $B^-$  and  $\bar{B}^0$  semileptonic decays, so its verification is of prime importance. It leads to a theoretical prediction for the decay width, and hence lifetime, for each  $b$ -flavored hadron [14]. One such set of predictions was [15] that  $\tau(\bar{B}_s^0)/\tau(\bar{B}^0) \approx 1.0$ ,  $\tau(B^-)/\tau(\bar{B}^0) \approx 1.1$  and  $\tau(\Lambda_b^0)/\tau(\bar{B}^0) \approx 0.96$ . The theory was improved by further calculations. For example, in the case of the ratio of lifetimes of the  $\Lambda_b^0$  baryon,  $\tau(\Lambda_b^0)$ , to the  $\bar{B}^0$  meson,  $\tau(\bar{B}^0)$ , differences of only a few percent were expected [16, 17], as the corrections of order  $O(1/m_b^2)$  and  $O(1/m_b^3)$  effects are both small.

Experimental tests of the HQE using lifetime mea-

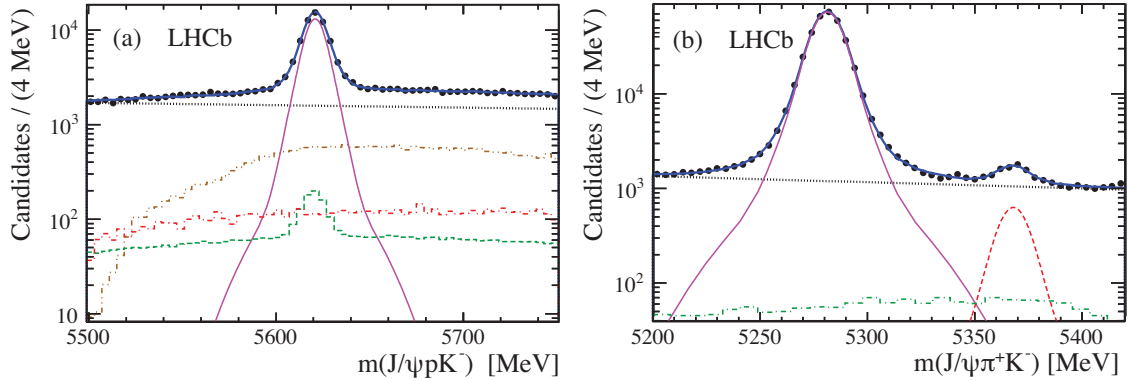


Figure 5: Fits to the invariant mass spectrum of (a)  $J/\psi pK^-$  and (b)  $J/\psi \pi^+K^-$  combinations. The  $\Lambda_b^0$  and  $\bar{B}^0$  signals are shown by the (magenta) solid curves. The (black) dotted lines are the combinatorial backgrounds, and the (blue) solid curves show the totals. In (a) the  $\bar{B}_s^0 \rightarrow J/\psi K^+K^-$  and  $\bar{B}^0 \rightarrow J/\psi \pi^+K^-$  reflections, caused by particle misidentification, are shown with the (brown) dot-dot-dashed and (red) dot-dashed shapes, respectively, and the (green) dashed shape represents the doubly misidentified  $J/\psi K^+\bar{p}$  final state, where the kaon and proton masses are swapped. In (b) the  $B_s^0 \rightarrow J/\psi \pi^+K^-$  mode is shown by the (red) dashed curve and the (green) dot-dashed shape represents the  $\Lambda_b^0 \rightarrow J/\psi pK^-$  reflection.

115 measurements started in the 1990's. Measurements at LEP  
 116 indicated that  $\tau(\Lambda_b^0)/\tau(\bar{B}^0)$  was significantly lower than  
 117 the prediction: in 2003 one widely quoted average of  
 118 all data gave  $0.798 \pm 0.052$  [18], while another gave  
 119  $0.786 \pm 0.034$  [19].

120 More recent measurements showed indications that a  
 121 higher value is possible [20], although the uncertainties  
 122 of these measurements are large. The LHCb collabora-  
 123 tion performed measurements of the lifetime ratio uti-  
 124 lizing the  $\Lambda_b^0 \rightarrow J/\psi pK^-$  decay using  $1 \text{ fb}^{-1}$  of data [21]  
 125 and then updated with  $3 \text{ fb}^{-1}$  sample [22]. This  $\Lambda_b^0$  de-  
 126 cay mode was first seen by LHCb. For similar decay  
 127 width, this decay mode has much better reconstruction  
 128 efficiency than the  $J/\psi \Lambda$  final state [23], as it contains  
 129 four charged tracks from the  $\Lambda_b^0$  decay vertex. Only the  
 130  $3 \text{ fb}^{-1}$  measurement is discussed here.

131 In this measurement the  $\Lambda_b^0$  decay time distribution is  
 132 compared to that of  $\bar{B}^0 \rightarrow J/\psi K^-\pi^+$  decays. The re-  
 133 constructed invariant mass distributions for both modes  
 134 are shown in Fig. 5. For  $\bar{B}^0$  candidates the invariant  
 135  $\pi^+K^-$  mass was required to be within  $\pm 100 \text{ MeV}$  of the  
 136  $\bar{K}^{*0}(892)$  mass. There are approximately 50 000  $\Lambda_b^0$  sig-  
 137 nal events and 340 000  $\bar{B}^0$  signal events.

138 The decay time acceptances obtained from the simu-  
 139 lations are shown in Fig. 6(a). The individual accep-  
 140 tances in both cases exhibit the same behaviour of de-  
 141 creasing below 1 ps. The ratio of the decay time accep-  
 142 tances is shown in Fig. 6(b). The yield of  $b$  hadrons for  
 143 both decay modes is determined by fitting the candidate  
 144 invariant mass distributions in each decay time bin. The  
 145 resulting signal yields as a function of decay time are  
 146 shown in Fig. 7.

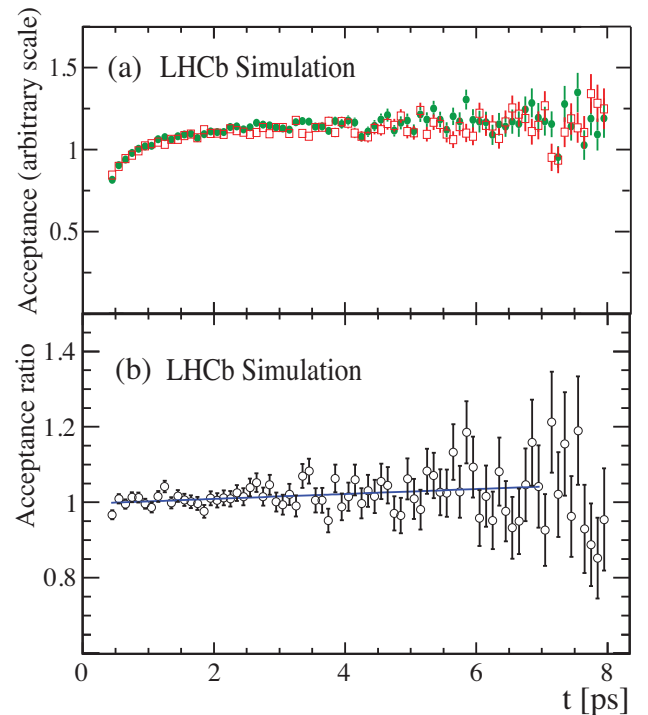


Figure 6: (a) Decay time acceptances (arbitrary scale) from simulation for (green) circles  $\Lambda_b^0 \rightarrow J/\psi pK^-$ , and (red) open-boxes  $\bar{B}^0 \rightarrow J/\psi \bar{K}^{*0}(892)$  decays. (b) Ratio of the decay time acceptances between  $\Lambda_b^0 \rightarrow J/\psi pK^-$  and  $\bar{B}^0 \rightarrow J/\psi \bar{K}^{*0}(892)$  decays obtained from simulation. The (blue) line shows the result of the linear fit.

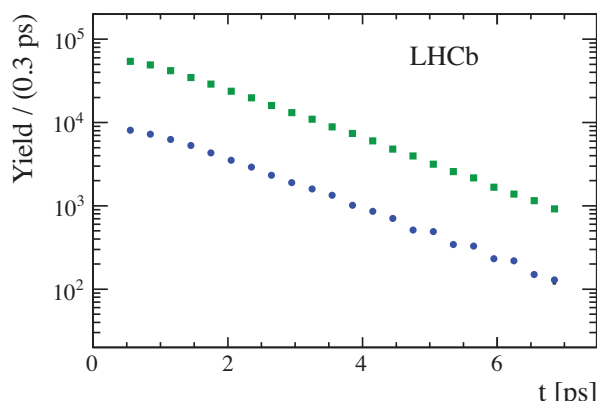


Figure 7: Decay time distributions for  $\Lambda_b^0 \rightarrow J/\psi p K^-$  shown as (blue) circles, and  $\bar{B}^0 \rightarrow J/\psi \bar{K}^{*0}(892)$  shown as (green) squares. For most entries the error bars are smaller than the points.

147 The ratio of lifetimes is determined as  $\frac{\tau(\Lambda_b^0)}{\tau(\bar{B}^0)} = 0.974 \pm$   
 148  $0.006 \pm 0.004$ . Multiplying the lifetime ratio by  $\tau(\bar{B}^0) =$   
 149  $1.519 \pm 0.007$  ps, the  $\Lambda_b^0$  baryon lifetime is  $\tau(\Lambda_b^0) =$   
 150  $1.479 \pm 0.009 \pm 0.010$  ps. A summary of  $\Lambda_b^0$  lifetime measurements done since 1990 is shown in Fig. 8.

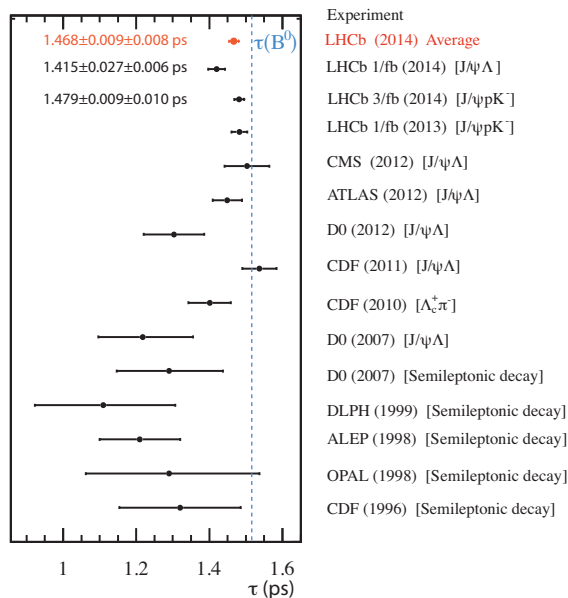


Figure 8: Summary of measured  $\Lambda_b^0$  lifetimes. The vertical dashed line shows the world average  $\bar{B}^0$  lifetime.

152 **5. First observation of Cabibbo-suppressed decay**  
 153  $\Lambda_b^0 \rightarrow J/\psi p \pi^-$

LHCb has first observed the Cabibbo-suppressed decay  $\Lambda_b^0 \rightarrow J/\psi p \pi^-$  using a data sample corresponding to an integrated luminosity of  $3 \text{ fb}^{-1}$  [24]. A prominent signal is observed and the branching fraction relative to the decay mode  $\Lambda_b^0 \rightarrow J/\psi p K^-$  is determined to be

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p \pi^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p K^-)} = 0.0824 \pm 0.0025(\text{stat}) \pm 0.0042(\text{syst}).$$

154 The measured ratio is consistent with the expectation  
 155 computed using relative CKM matrix elements and  
 156 phase space factors. Figure 9 shows the distribution of  
 157  $\Lambda_b^0 \rightarrow J/\psi p \pi^-$  and  $\Lambda_b^0 \rightarrow J/\psi p K^-$  masses.

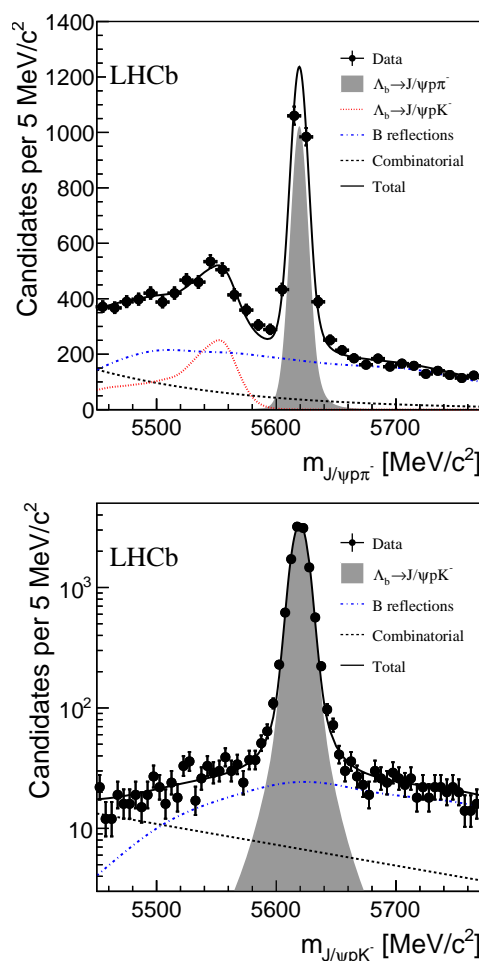


Figure 9: Distribution of (top)  $\Lambda_b^0 \rightarrow J/\psi p \pi^-$  and (bottom)  $\Lambda_b^0 \rightarrow J/\psi p K^-$  masses with fit projections overlaid.

A search for direct  $CP$  violation is performed. The difference in the  $CP$  asymmetries between these two de-

cays is found to be

$$\begin{aligned} & \mathcal{A}_{CP}(\Lambda_b^0 \rightarrow J/\psi p \pi^-) - \mathcal{A}_{CP}(\Lambda_b^0 \rightarrow J/\psi p K^-) \\ & = (+5.7 \pm 2.4 \text{ (stat)} \pm 1.2 \text{ (syst)})\%, \end{aligned}$$

158 which is compatible with  $CP$  symmetry at the  $2.2\sigma$   
159 level.

## 160 6. Conclusion

161 Using the  $3 \text{ fb}^{-1}$  data sample, LHCb has used various  
162  $b$ -hadron to  $J/\psi h^+ h^-$  decays to test the Standard Model  
163 and search for New Physics, as well as understand the  
164 scalar mesons.

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