

**Anomalous Higgs couplings in angular asymmetries
of $H \rightarrow Z\ell^+\ell^-$ and $e^+e^- \rightarrow HZ$**

Diogo Boito

Technische Universität München (TUM)

-- M Beneke, DB, Y.-M. Wang, [arXiv:1406.1361](https://arxiv.org/abs/1406.1361)

- **Introduction**
- **Operators and couplings**
- **Form factor and angular structures**
- **Main results**

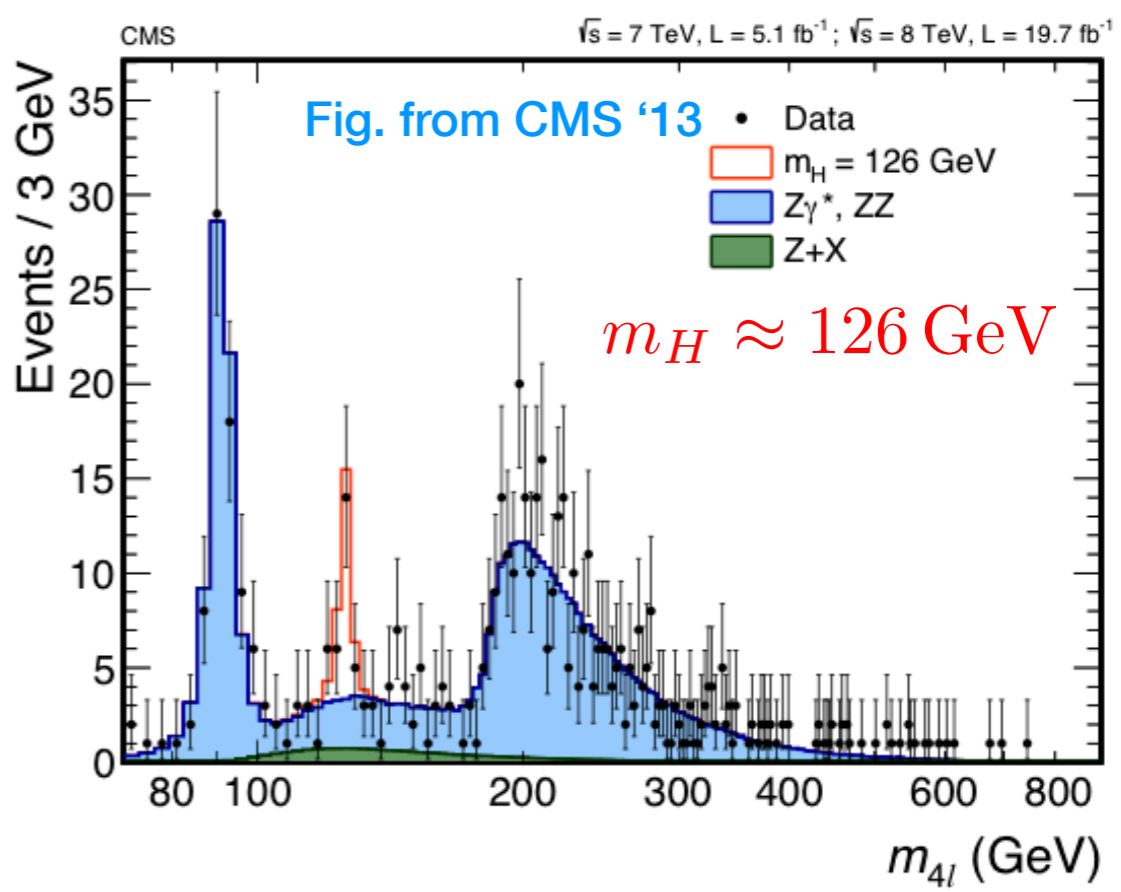
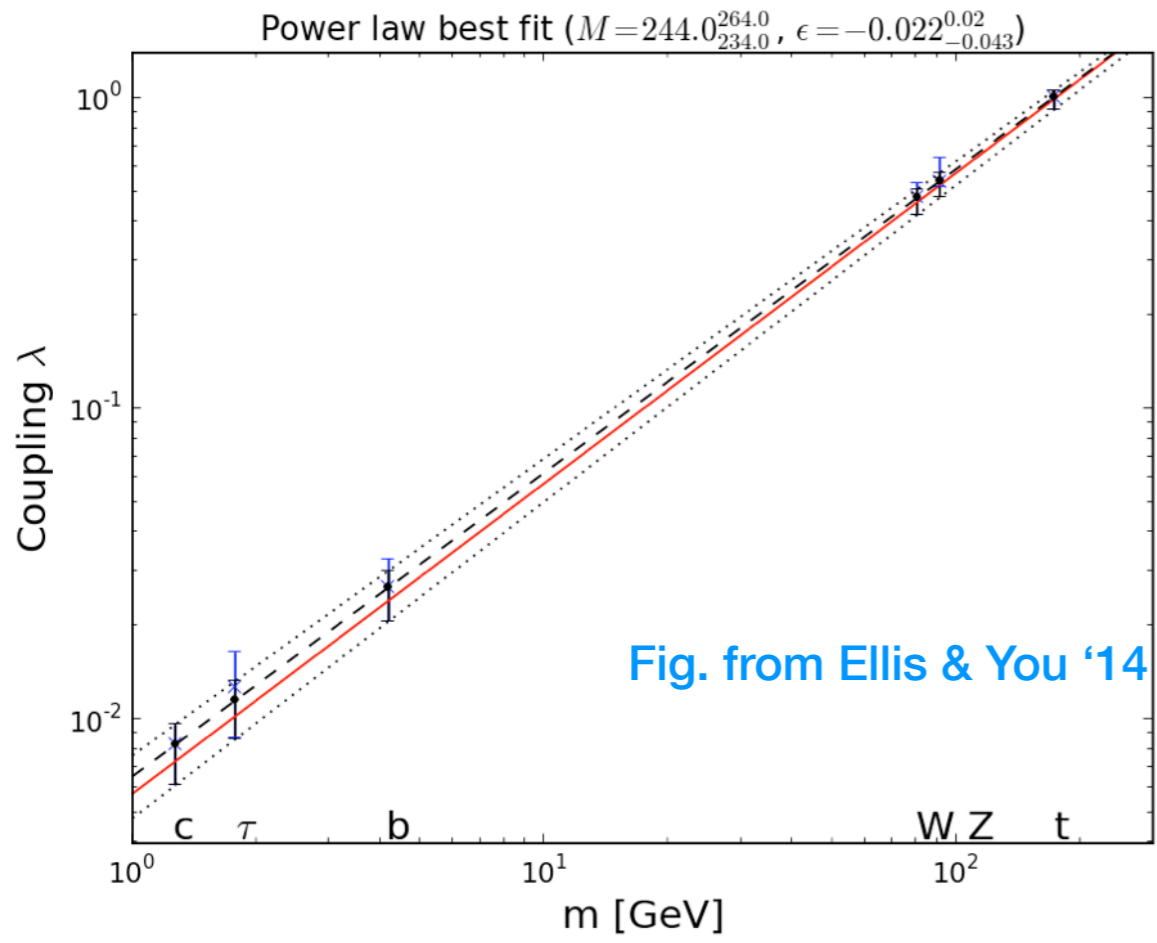
Beyond Standard Model physics is elusive

- The Higgs seems to be the one from the SM.
- Quantum numbers compatible with SM predictions

ATLAS arXiv:1307.1432; CMS arXiv:1312.5353

- Couplings proportional to the mass

- Higgs in 4l



- Parametrization of BSM physics assuming SM symmetry $SU(3) \times SU(2) \times U(1)$ (linearly realized)

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}}^{(4)} + \frac{1}{\Lambda^2} \sum_{k=1}^{59} \alpha_k \mathcal{O}_k,$$

Buchmüller & Wyler '86
Grzadkowski et al '10

We also employ $\hat{\alpha}_k = \frac{v^2}{\Lambda^2} \alpha_k$

- Many different operator basis allowed and in use.
- Several operators affect Higgs physics. Many are constrained by data.

Operators and couplings

- We employ the “Polish” basis (with MFV). Relevant operators:

Grzadkowski et al ‘10

$\Phi^4 D^2$	$X^2 \Phi^2$	$\psi^2 \Phi^2 D$
$\mathcal{O}_{\Phi\Box} = (\Phi^\dagger\Phi)\Box(\Phi^\dagger\Phi)$	$\mathcal{O}_{\Phi W} = (\Phi^\dagger\Phi)W_{\mu\nu}^I W^{I\mu\nu}$	$\mathcal{O}_{\Phi\ell}^{(1)} = (\Phi^\dagger i\overleftrightarrow{D}_\mu\Phi)(\bar{\ell}\gamma^\mu\ell)$
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	$\mathcal{O}_{\Phi WB} = (\Phi^\dagger\tau^I\Phi)W_{\mu\nu}^I B^{\mu\nu}$	$\mathcal{O}_{\Phi e} = (\Phi^\dagger i\overleftrightarrow{D}_\mu\Phi)(\bar{e}\gamma^\mu e)$
	$\mathcal{O}_{\Phi\tilde{W}} = (\Phi^\dagger\Phi)\tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	←
	$\mathcal{O}_{\Phi\tilde{B}} = (\Phi^\dagger\Phi)\tilde{B}_{\mu\nu}B^{\mu\nu}$	← CP odd
	$\mathcal{O}_{\Phi\tilde{W}B} = (\Phi^\dagger\tau^I\Phi)\tilde{W}_{\mu\nu}^I B^{\mu\nu}$	←

- Additionally, a four-fermion operator contributes to the redefinition of G_F

$$\mathcal{O}_{4L}^{prst} = (\bar{\ell}_p\gamma_\mu\ell_r)(\bar{\ell}_s\gamma^\mu\ell_t)$$

$$m_Z = m_{Z_0}(1 + \delta_Z), \quad G_F = G_{F_0}(1 + \delta_{G_F}), \quad \alpha_{em} = \alpha_{em_0}(1 + \delta_A),$$

$$\delta_Z = \hat{\alpha}_{ZZ} + \frac{1}{4}\hat{\alpha}_{\Phi D}, \quad \delta_{G_F} = -\hat{\alpha}_{4L} + 2\hat{\alpha}_{\Phi\ell}^{(3)}, \quad \delta_A = 2\hat{\alpha}_{AA}$$

$$\alpha_{ZZ} = c_W^2\alpha_{\Phi W} + s_W^2\alpha_{\Phi B} + s_W c_W\alpha_{\Phi WB}$$

$$\alpha_{AA} = s_W^2\alpha_{\Phi W} + c_W^2\alpha_{\Phi B} - s_W c_W\alpha_{\Phi WB}$$

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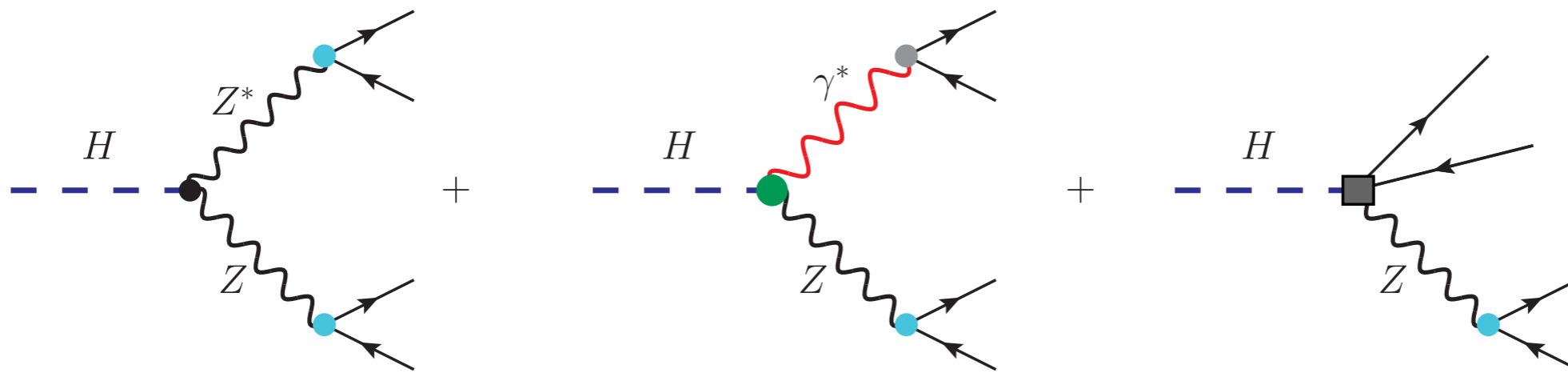
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- New interactions and modifications to SM vertices

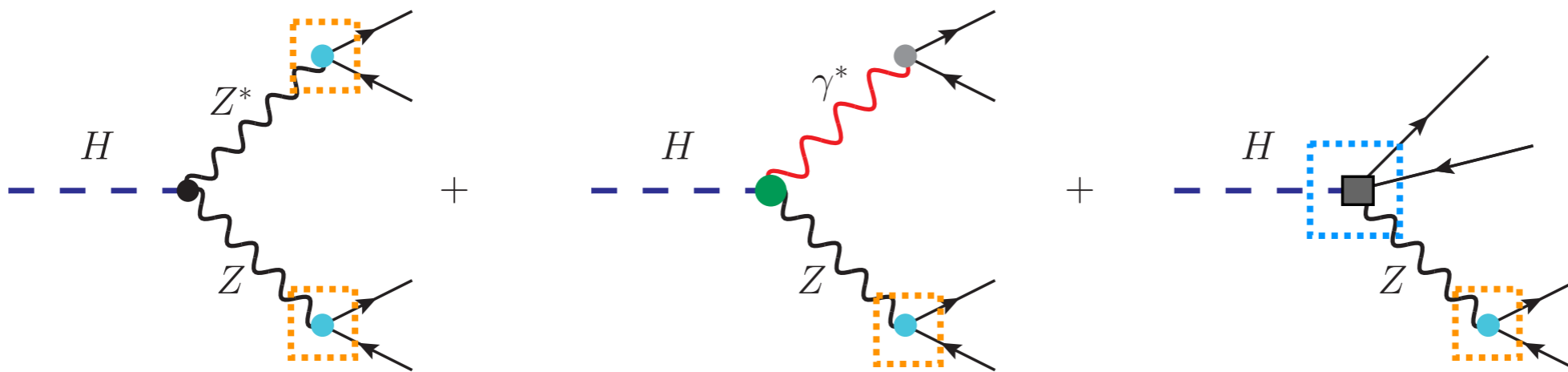
$$\mathcal{L}_{\text{eff}} \supset c_{ZZ}^{(1)} H Z_\mu Z^\mu + c_{ZZ}^{(2)} H Z_{\mu\nu} Z^{\mu\nu} + c_{Z\tilde{Z}} H Z_{\mu\nu} \tilde{Z}^{\mu\nu} + c_{AZ} H Z_{\mu\nu} A^{\mu\nu} + c_{A\tilde{Z}} H Z_{\mu\nu} \tilde{A}^{\mu\nu} \\ + H Z_\mu \bar{\ell} \gamma^\mu (c_V + c_A \gamma_5) \ell + Z_\mu \bar{\ell} \gamma^\mu (g_V - g_A \gamma_5) \ell - g_{\text{em}} Q_\ell A_\mu \bar{\ell} \gamma^\mu \ell,$$



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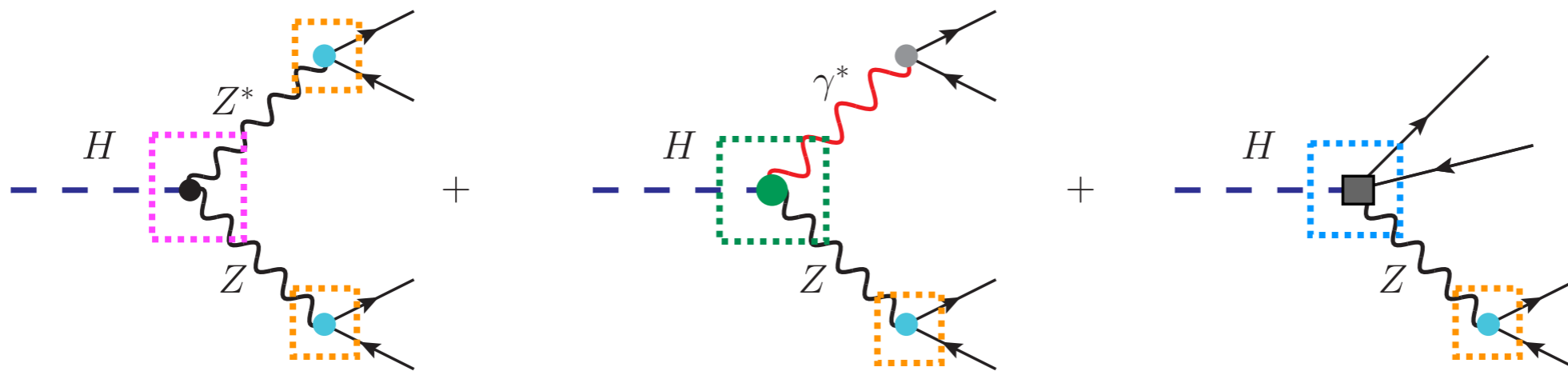
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$$\hat{\alpha}_{AZ} \in [-1.3, 2.6] \times 10^{-2} \quad \hat{\alpha}_{\Phi\ell}^{V,A} \in [-5, 5] \times 10^{-3}$$

Pomarol and Riva '14

estimate using data for

$$\Delta S, \Delta T, m_W, g_{V,A}$$

Beneke, DB, Wang '14

- Contact $HZ\ell\ell$ in the “Polish” basis

Grzadkowski et al '10

$$HZ_\mu \bar{\ell} \gamma^\mu (c_V + c_A \gamma_5) \ell \longrightarrow c_{V,A} = \sqrt{2} G_F m_Z \hat{\alpha}_{\Phi,\ell}^{V,A}$$

$$\hat{\alpha}_{\Phi,\ell}^{V,A} = \hat{\alpha}_{\Phi e} \pm \left(\hat{\alpha}_{\Phi\ell}^{(1)} + \hat{\alpha}_{\Phi\ell}^{(3)} \right)$$

- In the basis used by Pomarol and Riva '14

Elias-Miró, Espinosa, Massó, Pomarol '13

$$\begin{aligned} \cancel{O_{\Phi\ell}^{(1)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi) (\bar{\ell} \gamma^\mu \ell)} \\ \cancel{O_{\Phi\ell}^{(3)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu^I \Phi) (\bar{\ell} \gamma^\mu \tau^I \ell)} \end{aligned} \longrightarrow c_V = c_A$$

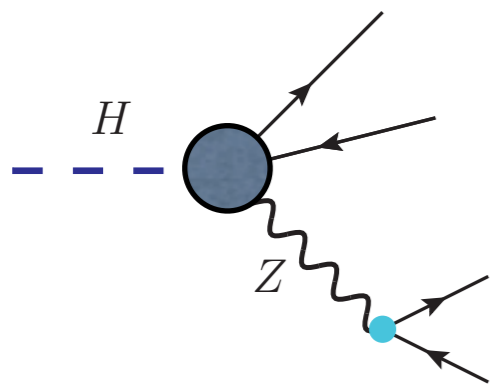
only right-handed couplings are non-vanishing: $c_L = 0$

- Order of magnitude agreement with the constraints on c_R from Pomarol and Riva '14

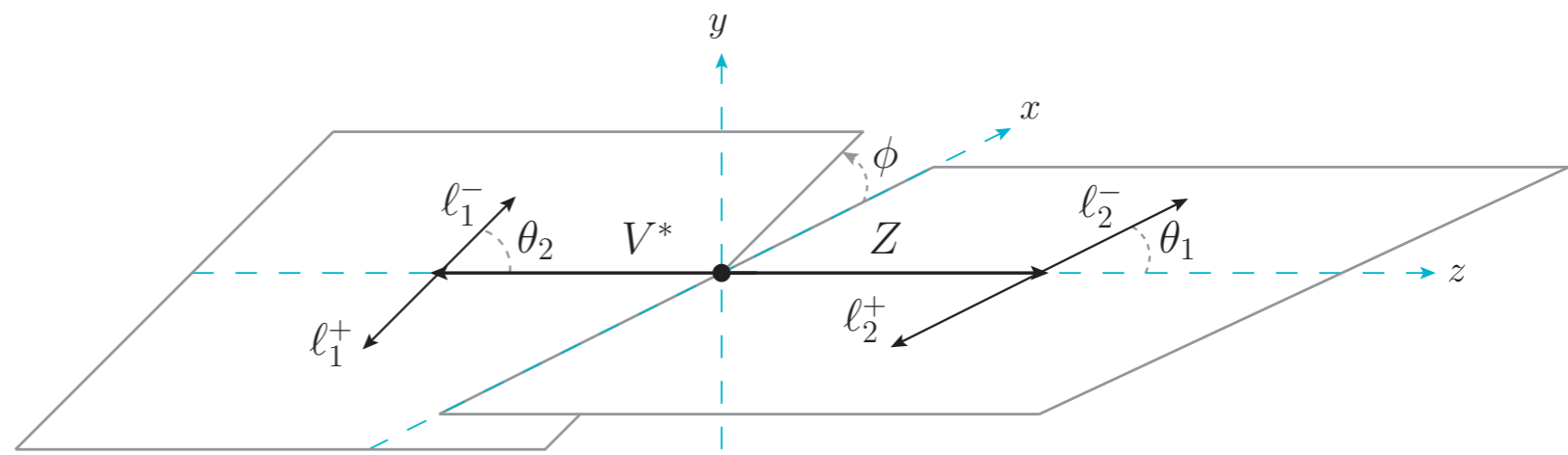
see also Alonso, Jenkins, Manohar and Trott '13

Form factors and angular structures

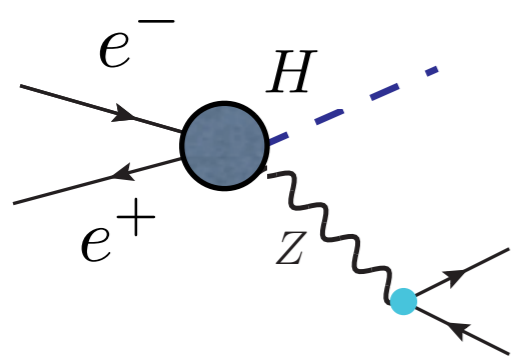
● Two crossing symmetric processes



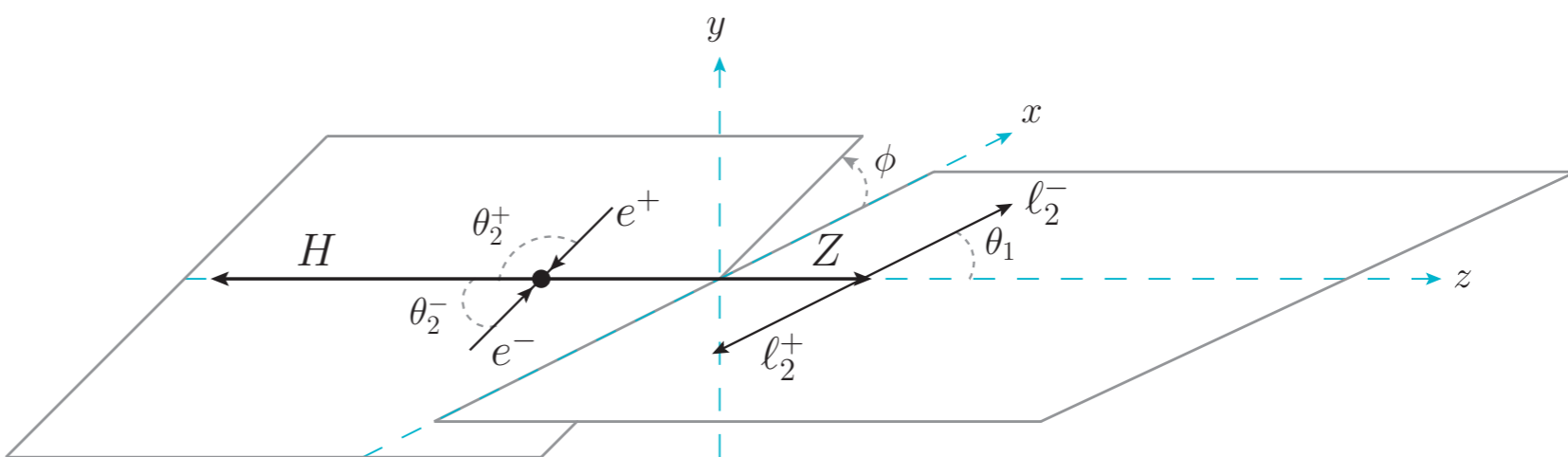
$$H \rightarrow Z l^+ l^- \rightarrow 4l$$



$$\frac{d^4\Gamma}{dq^2 d \cos \theta_1 d \cos \theta_2 d\phi} = \frac{1}{m_H} \mathcal{N}(q^2) \mathcal{J}(q^2, \theta_1, \theta_2, \phi).$$



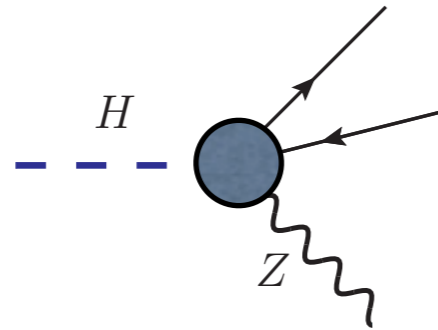
$$e^+ e^- \rightarrow H Z \rightarrow H l l$$



$$\frac{d\sigma}{d \cos \theta_1 d \cos \theta_2 d\phi} = \frac{1}{m_H^2} \mathcal{N}_\sigma(q^2) \mathcal{J}(q^2, \theta_1, \theta_2, \phi),$$

- Higgs on shell.
- Narrow-width approximation for the Z propagator (on-shell Z).
- SM tree level + d=6 terms at tree level.
- We only keep terms up to $\mathcal{O}(1/\Lambda^2)$
- $m_\ell = 0$

- Form factors



$$\mathcal{M}_{HZ\ell\ell}^\mu = \frac{1}{m_H} \bar{u} \left[\gamma^\mu (H_{1,V} + H_{1,A} \gamma_5) + \frac{q^\mu \not{p}}{m_H^2} (H_{2,V} + H_{2,A} \gamma_5) + \frac{\epsilon^{\mu\nu\sigma\rho} p_\nu q_\sigma}{m_H^2} \gamma_\rho (H_{3,V} + H_{3,A} \gamma_5) \right] v$$

↑ SM + d = 6
↑ d = 6 only
↑ d = 6 only, CP odd

- Angular structure at order $1/\Lambda^2$

$$\begin{aligned} \mathcal{J}(q^2, \theta_1, \theta_2, \phi) = & J_1(1 + \cos^2 \theta_1 \cos^2 \theta_2 + \cos^2 \theta_1 + \cos^2 \theta_2) \\ & + J_2 \sin^2 \theta_1 \sin^2 \theta_2 + J_3 \cos \theta_1 \cos \theta_2 \\ & + (J_4 \sin \theta_1 \sin \theta_2 + J_5 \sin 2\theta_1 \sin 2\theta_2) \sin \phi \\ & + (J_6 \sin \theta_1 \sin \theta_2 + J_7 \sin 2\theta_1 \sin 2\theta_2) \cos \phi \\ & + J_8 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\phi + J_9 \sin^2 \theta_1 \sin^2 \theta_2 \cos 2\phi. \end{aligned}$$

- Decay width and cross-section only probe a specific combination

$$\frac{d\Gamma}{dq^2} \propto 4J_1 + J_2 \quad \sigma(q^2) \propto 4J_1 + J_2$$

- Angular asymmetries that probe other angular functions

$$\mathcal{A}_\phi^{(1)} = \frac{1}{d\Gamma/dq^2} \int_0^{2\pi} d\phi \operatorname{sgn}(\sin \phi) \frac{d^2\Gamma}{dq^2 d\phi} = \frac{9\pi}{32} \frac{J_4}{4J_1 + J_2},$$

$$\mathcal{A}_\phi^{(2)} = \frac{1}{d\Gamma/dq^2} \int_0^{2\pi} d\phi \operatorname{sgn}(\sin(2\phi)) \frac{d^2\Gamma}{dq^2 d\phi} = \frac{2}{\pi} \frac{J_8}{4J_1 + J_2},$$

$$\mathcal{A}_\phi^{(3)} = \frac{1}{d\Gamma/dq^2} \int_0^{2\pi} d\phi \operatorname{sgn}(\cos \phi) \frac{d^2\Gamma}{dq^2 d\phi} = \frac{9\pi}{32} \frac{J_6}{4J_1 + J_2},$$

$$\begin{aligned} \mathcal{A}_{c\theta_1, c\theta_2} &= \frac{1}{d\Gamma/dq^2} \int_{-1}^1 d \cos \theta_1 \operatorname{sgn}(\cos \theta_1) \int_{-1}^1 d \cos \theta_2 \operatorname{sgn}(\cos \theta_2) \frac{d^3\Gamma}{dq^2 d \cos \theta_1 d \cos \theta_2} \\ &= \frac{9}{16} \frac{J_3}{4J_1 + J_2}. \end{aligned}$$

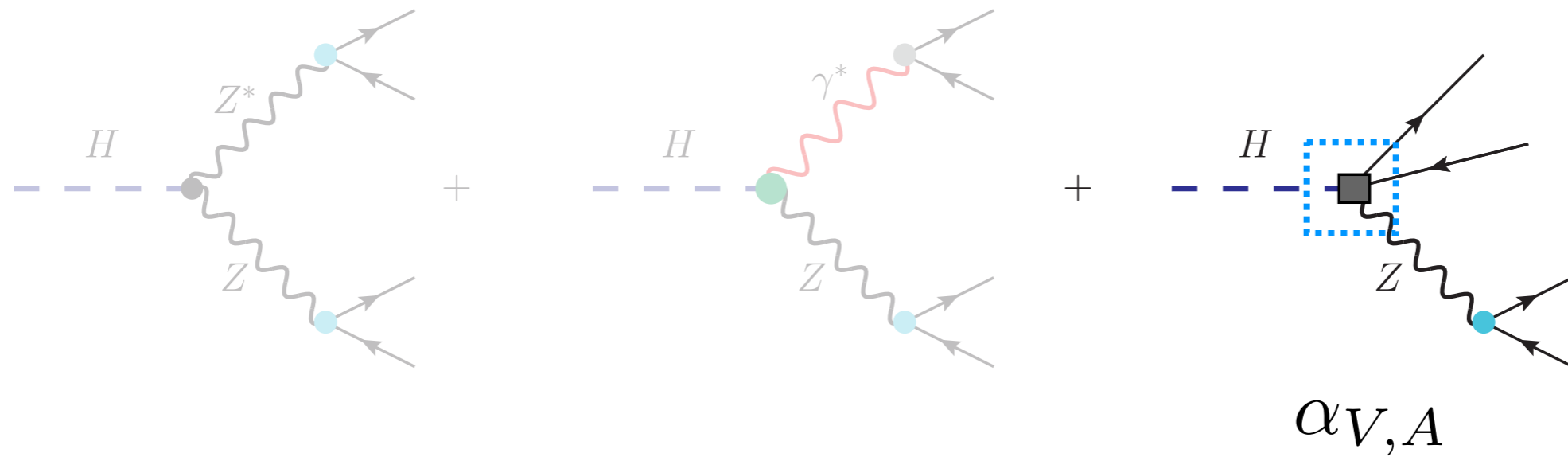
see also Buchalla, Catà, D'Ambrosio '13

- Enhancement of anomalous couplings in asymmetries is possible due to:
 - Di-lepton invariant mass
 - Smallness of the vector coupling of Z to fermions in SM

$$g_V \propto (1 - 4s_W^2)$$

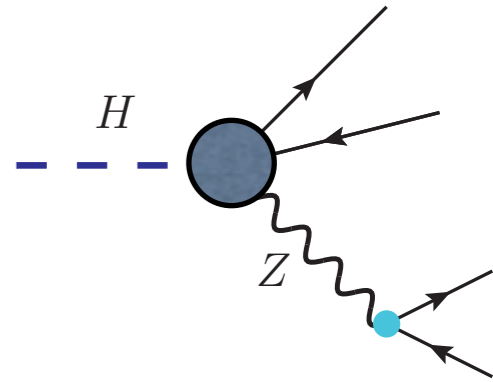
Main results

Contact $HZll$ couplings



$$H \rightarrow Zl^+l^- \rightarrow 4l$$

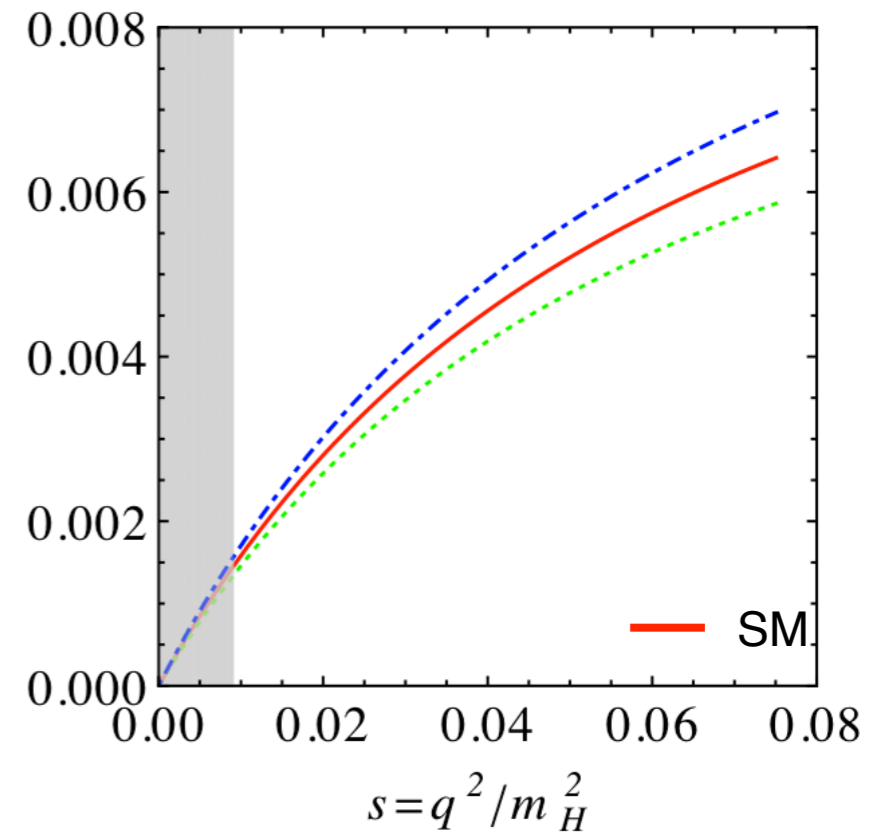
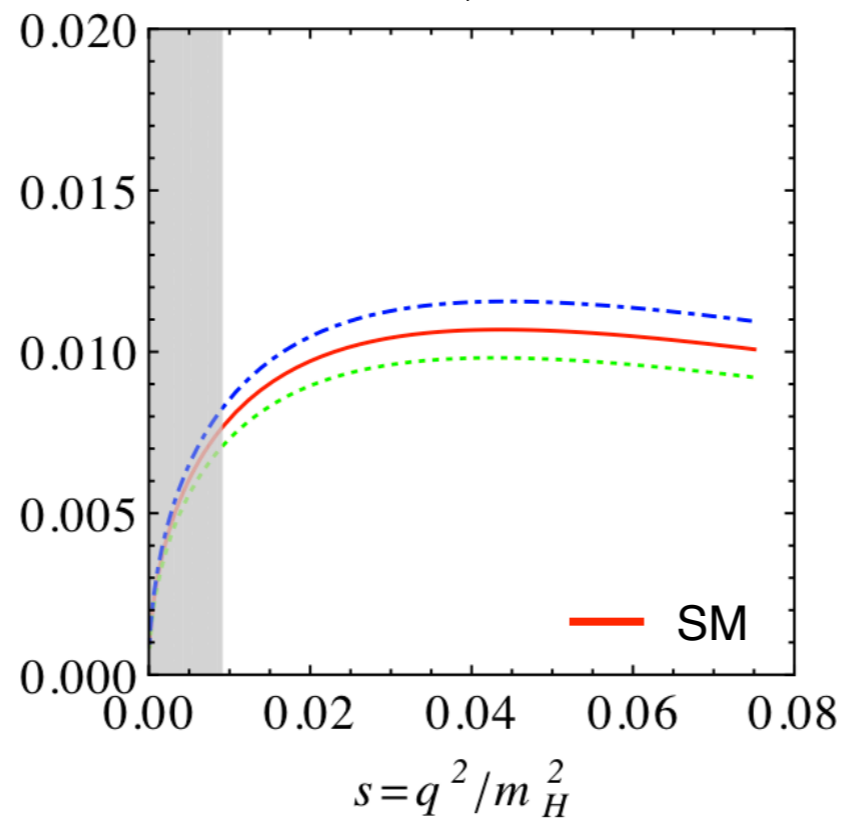
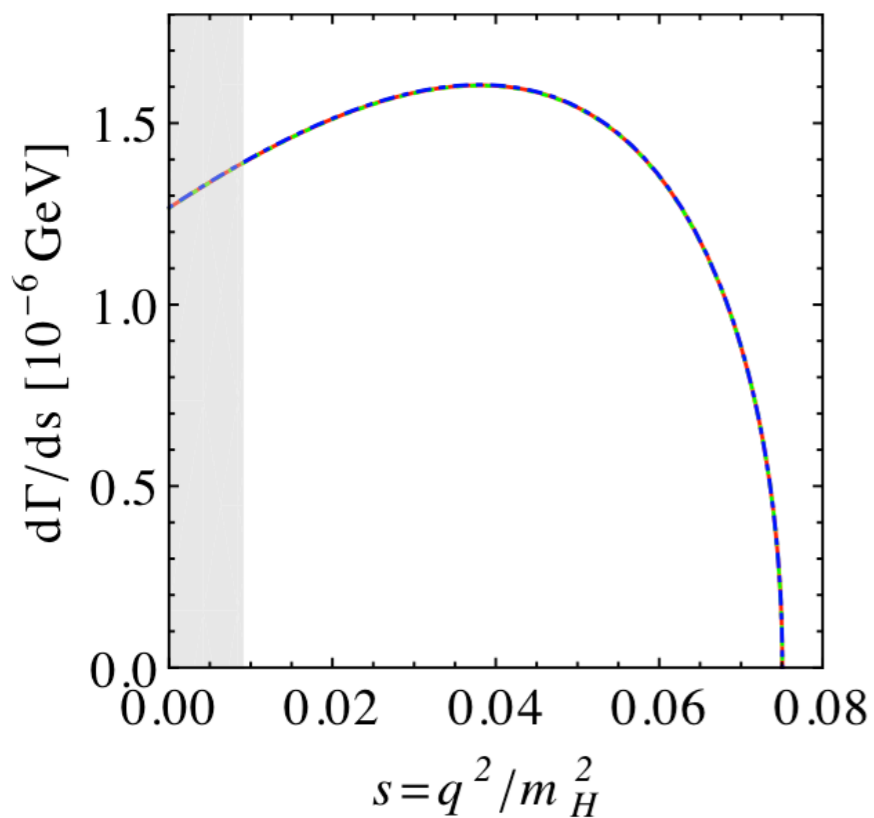
- Vector contact coupling $HZll$



$$d\Gamma/ds$$

$$-\mathcal{A}_\phi^{(3)}$$

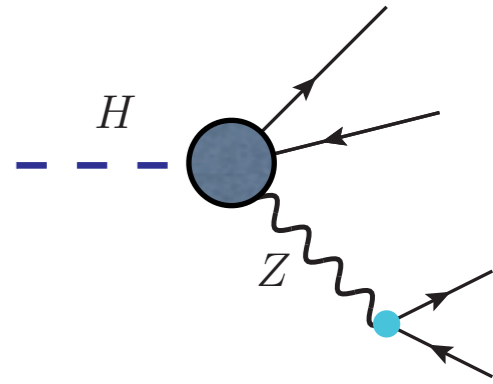
$$-\mathcal{A}_{c\theta_1 c\theta_2}$$



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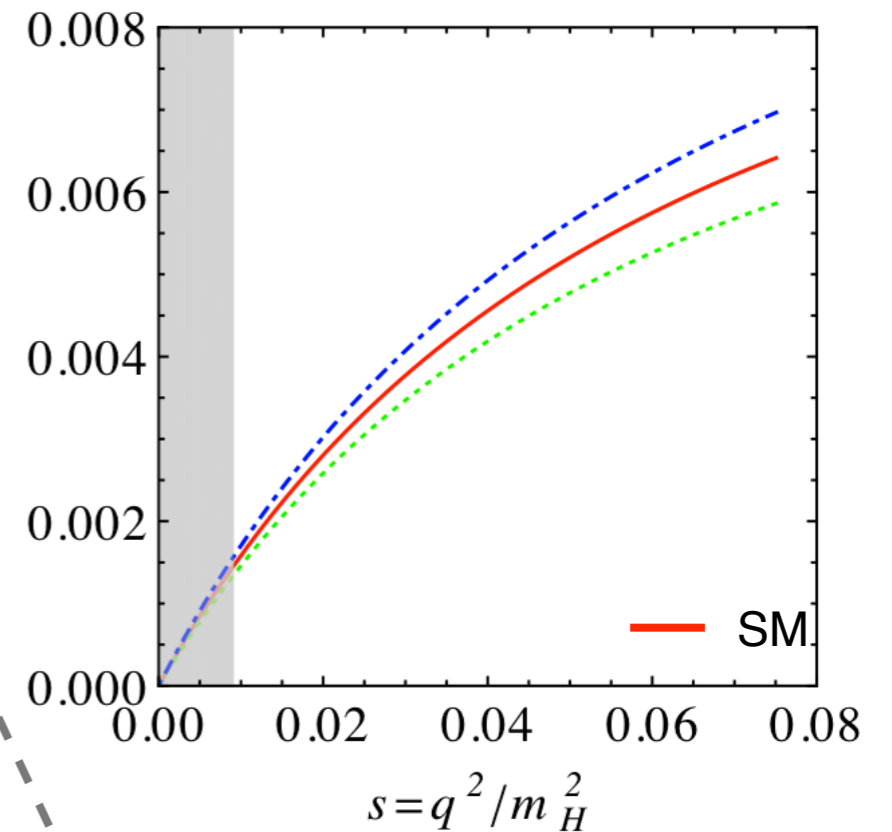
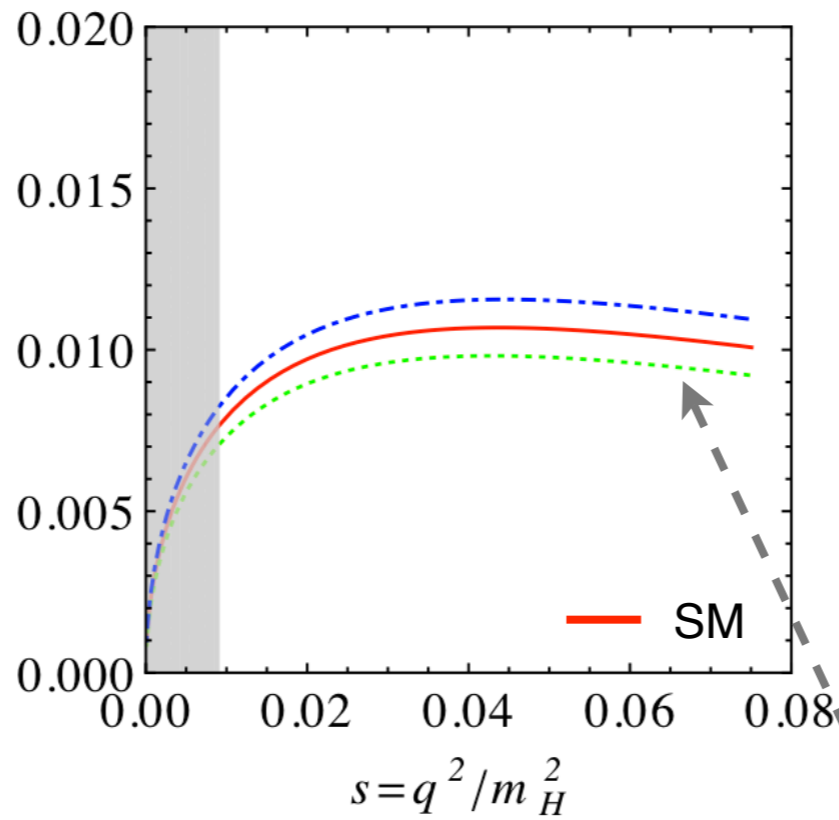
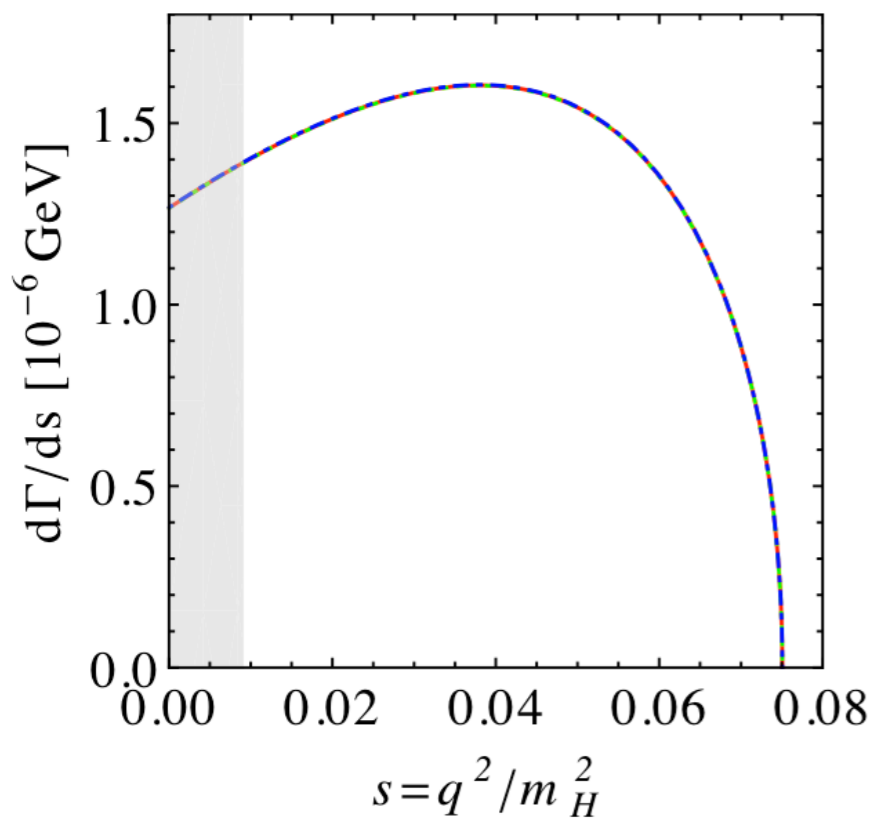


- Vector contact coupling $HZll$

$$d\Gamma/ds$$

$$-\mathcal{A}_\phi^{(3)}$$

$$-\mathcal{A}_{c\theta_1 c\theta_2}$$



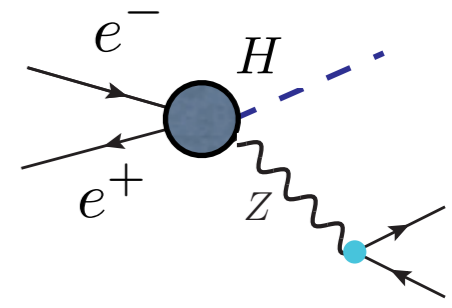
see also Buchalla, Catà, D'Ambrosio '13

$$-\mathcal{A}_\phi^{(3)} \simeq \frac{9\pi\sqrt{2}}{2} \frac{\bar{g}_V^2}{\bar{g}_A^2} \frac{\sqrt{s}}{1+16s} \left(1 + \hat{\alpha}_{\Phi\ell}^A + \frac{\bar{g}_A}{\bar{g}_V} \hat{\alpha}_{\Phi\ell}^V \right)$$

- No enhancement of the axial couplings

$$\hat{\alpha}_{\Phi\ell}^{V,A} \in [-5, 5] \times 10^{-3}$$

$$e^+e^- \rightarrow HZ \rightarrow Hll$$

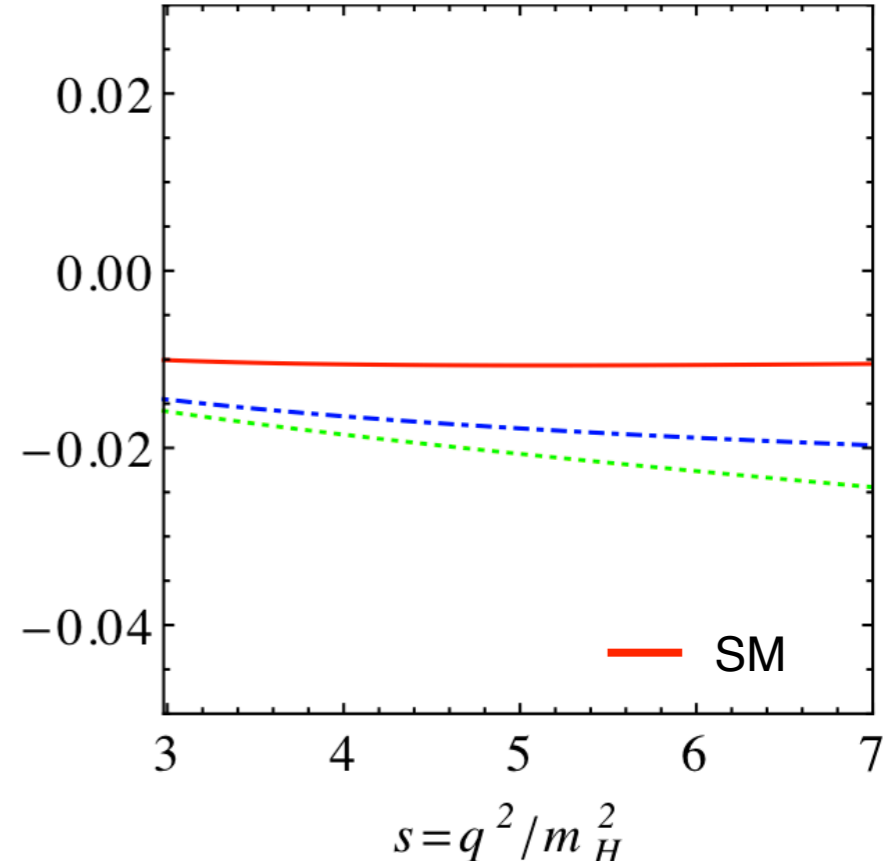
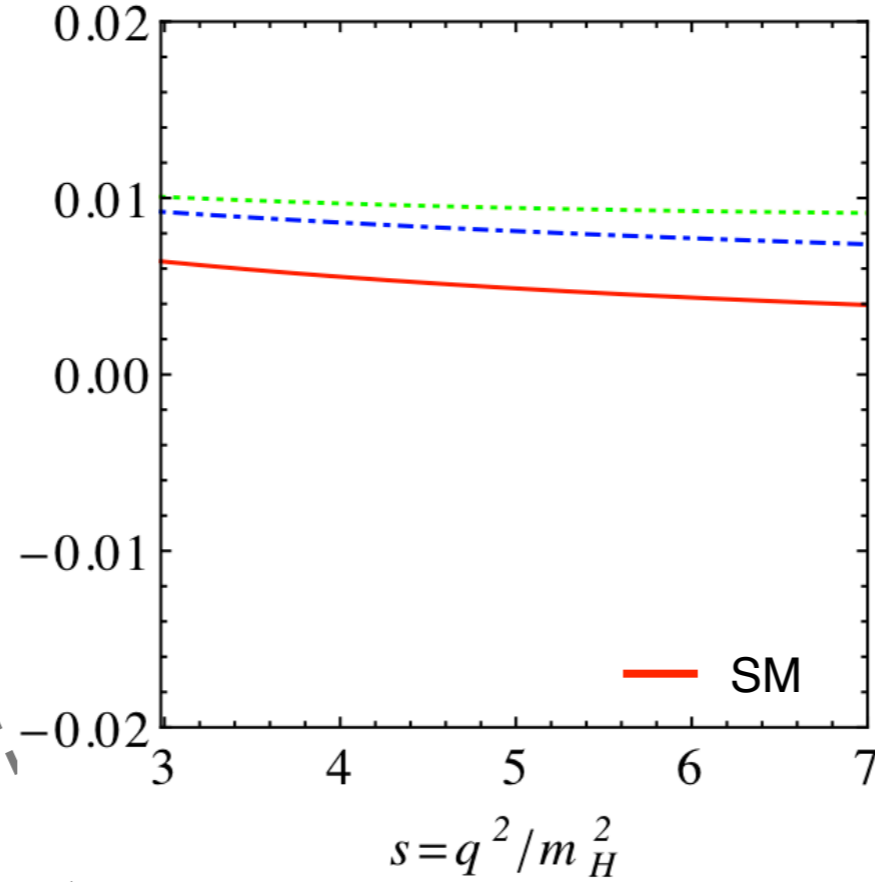
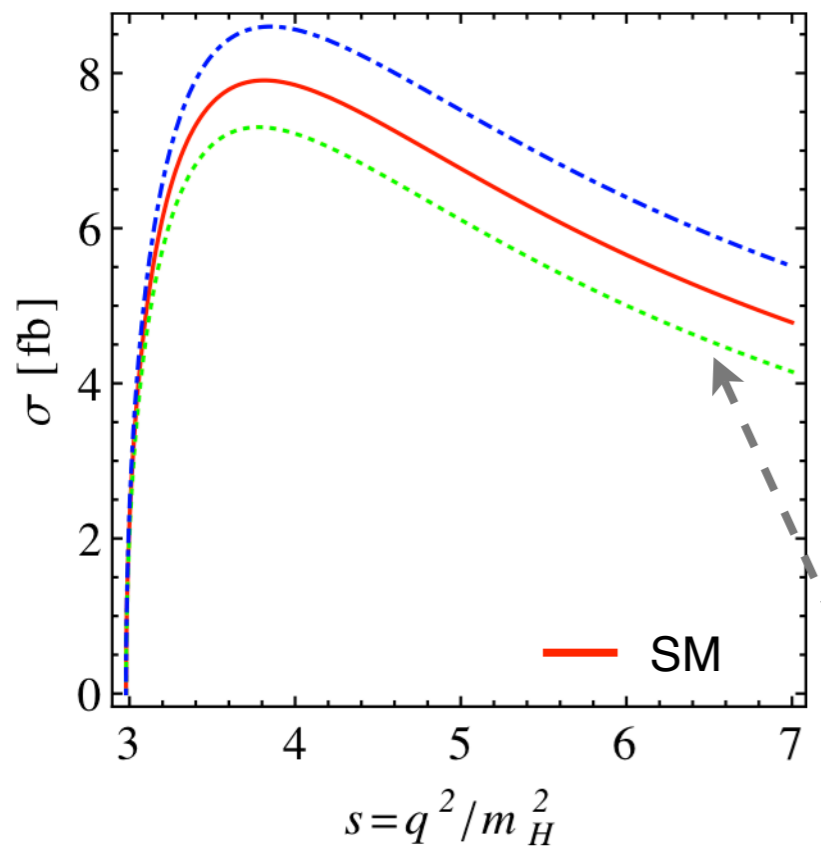


● Contact couplings $HZll$

σ

$-\mathcal{A}_\phi^{(3)}$

$-\mathcal{A}_{c\theta_1 c\theta_2}$

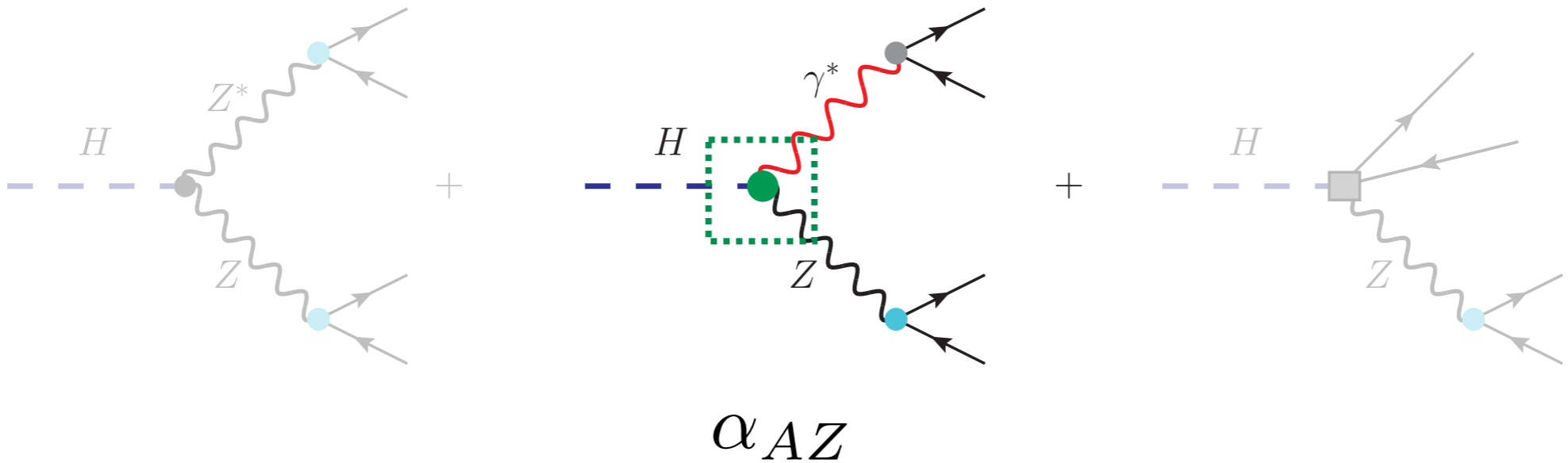


$$\sigma \simeq \sqrt{2} m_H^2 G_F \bar{g}_A^4 \frac{s+3}{s-1} \left[1 - 2(1+2s) \hat{\alpha}_{\Phi l}^A \right]$$

$$\hat{\alpha}_{\Phi l}^{V,A} \in [-5, 5] \times 10^{-3}$$

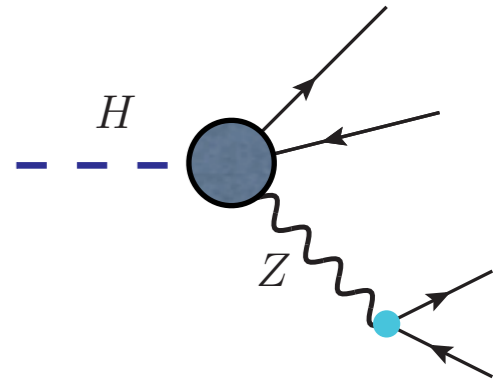
● Enhanced contribution of axial couplings to the cross-section

HAZ coupling

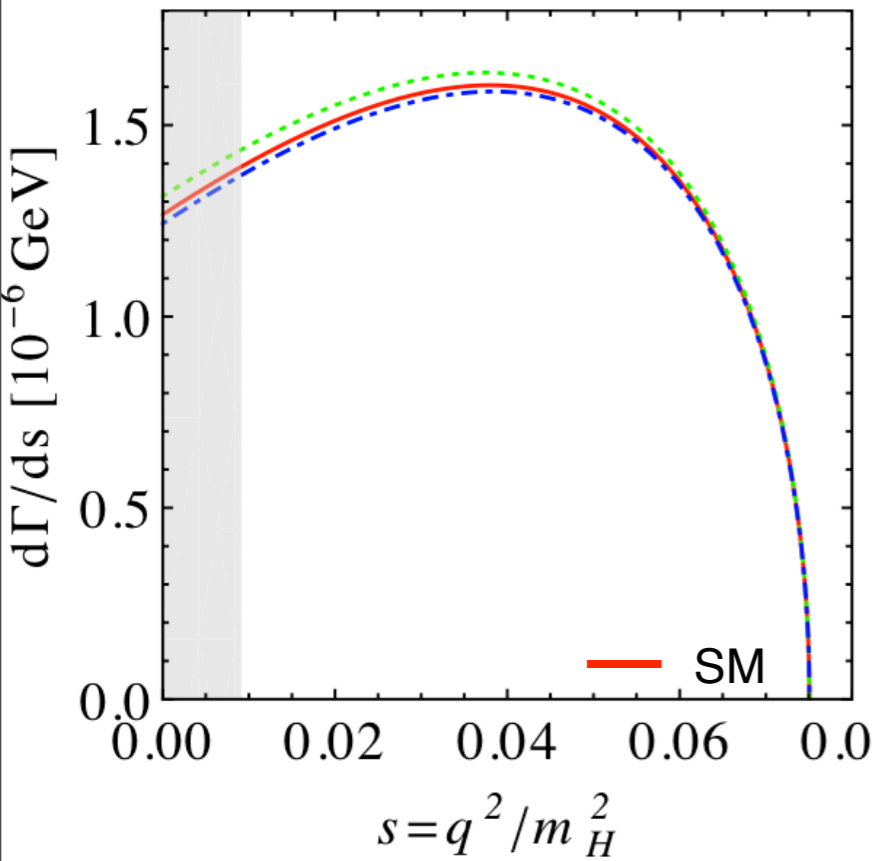


$$H \rightarrow Zl^+l^- \rightarrow 4l$$

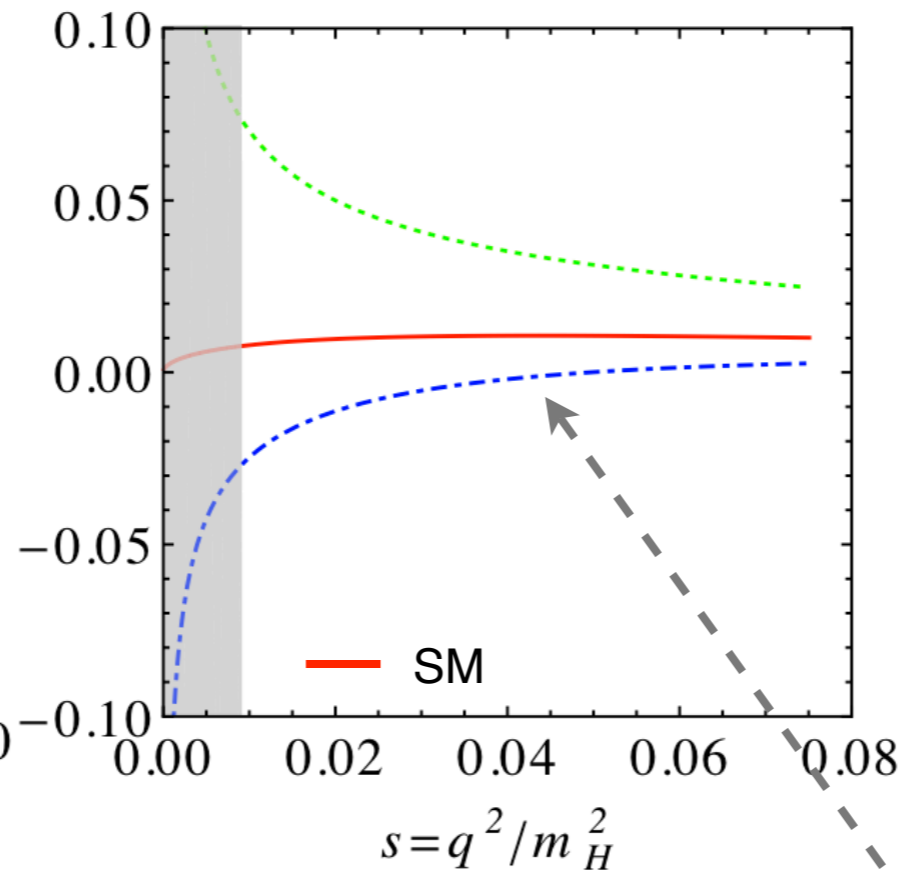
- Contact couplings HAZ



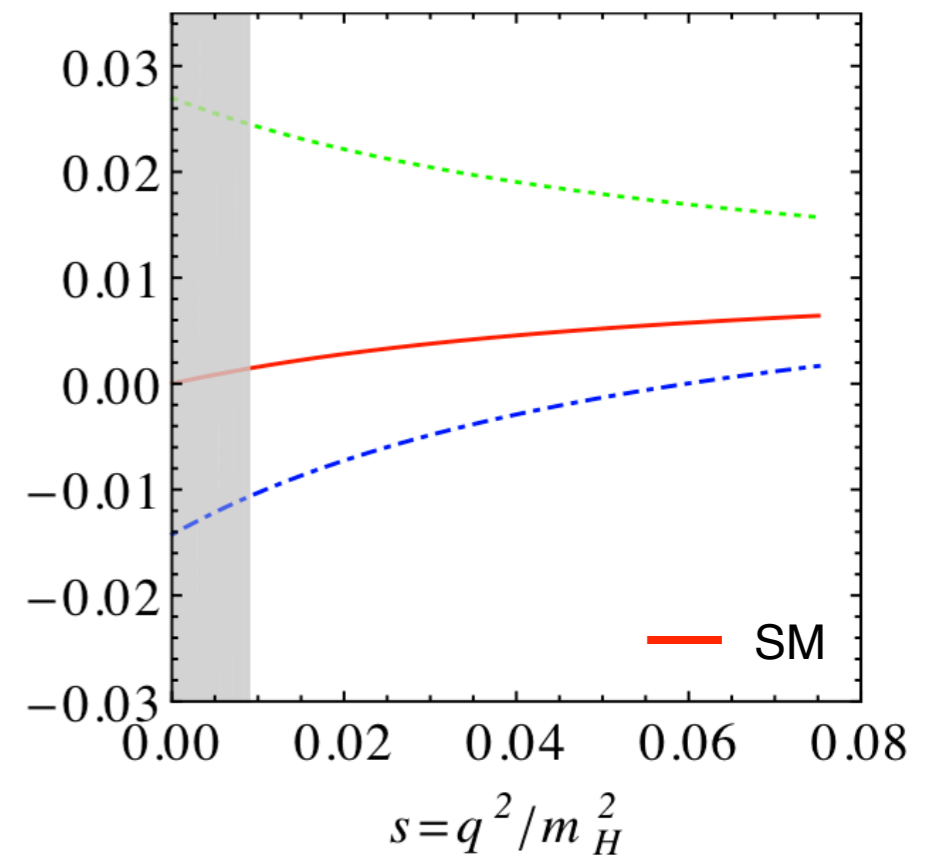
$$d\Gamma/ds$$



$$-\mathcal{A}_\phi^{(3)}$$



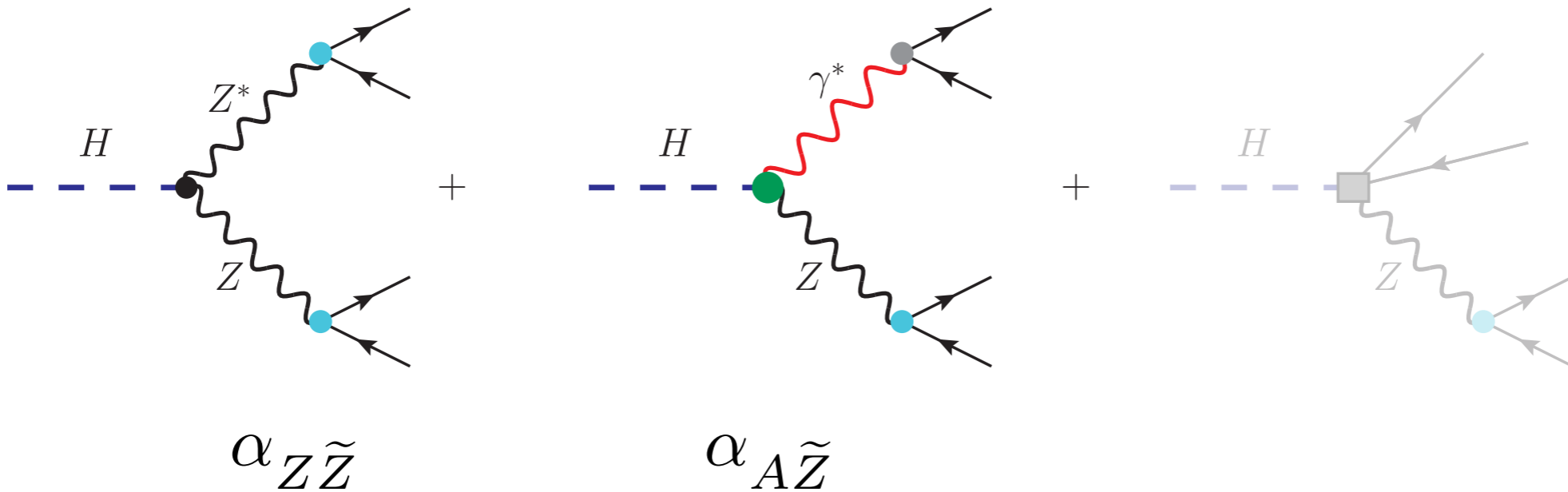
$$-\mathcal{A}_{c\theta_1 c\theta_2}$$



$$-\mathcal{A}_\phi^{(3)} \simeq \frac{9\pi\sqrt{2}\bar{g}_V^2}{2\bar{g}_A^2} \frac{\sqrt{s}}{1+16s} \left(1 - \frac{g_{em} Q_l \hat{\alpha}_{AZ}}{8\bar{g}_V s} \right)$$

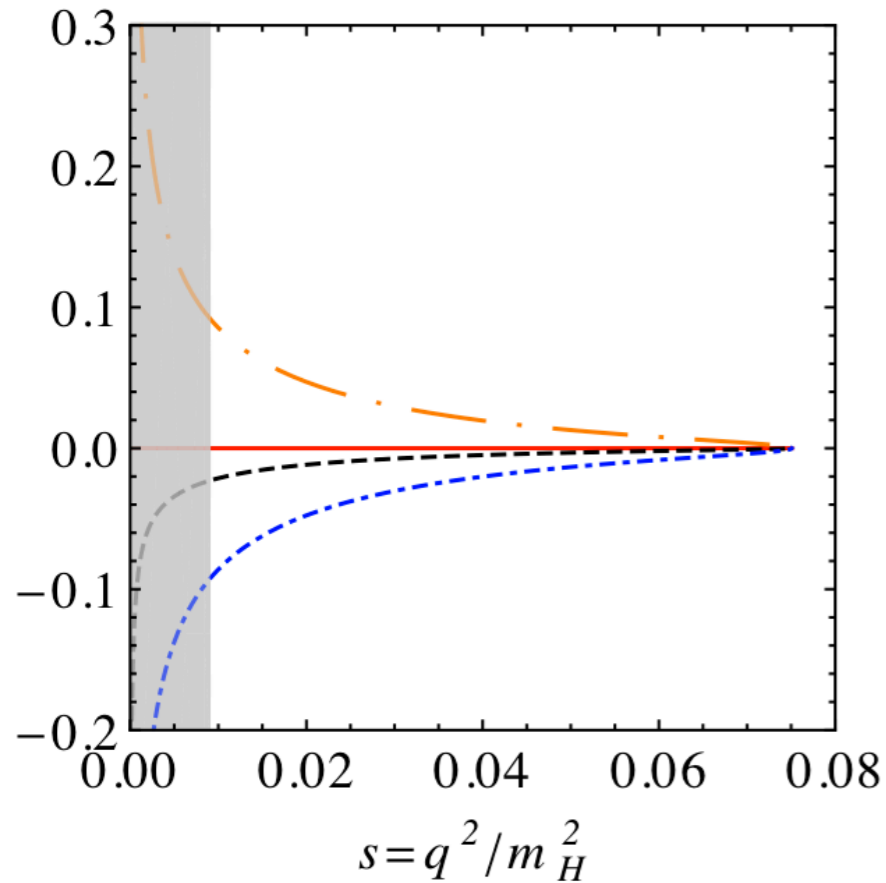
$$\hat{\alpha}_{AZ} \in [-1.3, 2.6] \times 10^{-2}$$

CP odd couplings

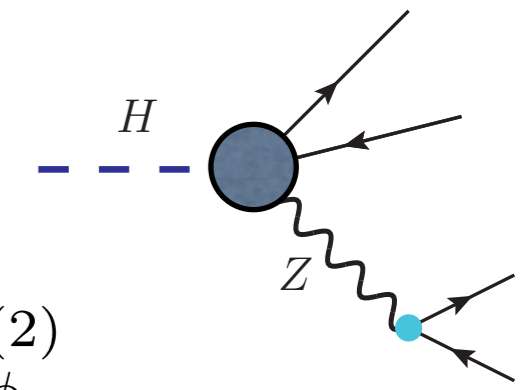
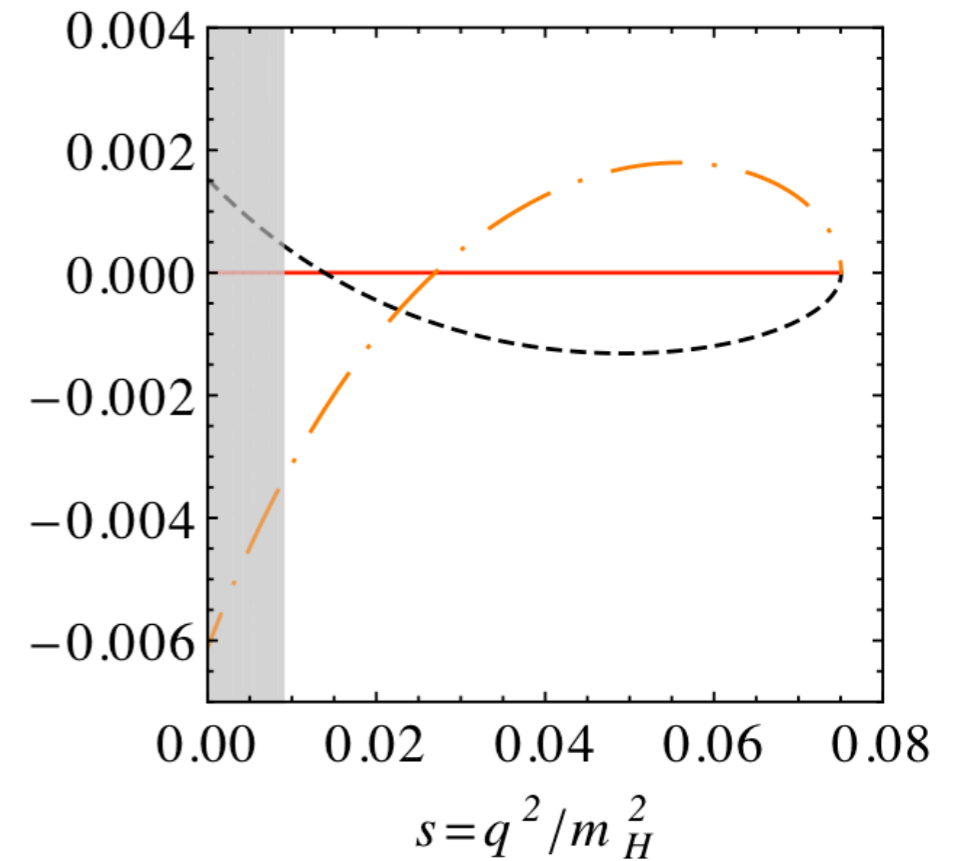


$$H \rightarrow Z \ell^+ \ell^- \rightarrow 4\ell$$

$$\mathcal{A}_\phi^{(1)}$$



$$\mathcal{A}_\phi^{(2)}$$



- Dominated by $\alpha_{A\tilde{Z}}$

$$(\hat{\alpha}_{Z\tilde{Z}}, \hat{\alpha}_{A\tilde{Z}}) = (4, -4) \times 10^{-2} \quad \text{.....}$$

$$(\hat{\alpha}_{Z\tilde{Z}}, \hat{\alpha}_{A\tilde{Z}}) = (4, 4) \times 10^{-2} \quad \text{- - -}$$

$$(\hat{\alpha}_{Z\tilde{Z}}, \hat{\alpha}_{A\tilde{Z}}) = (-2, -1) \times 10^{-2} \quad \text{---}$$

- Interplay between $\alpha_{A\tilde{Z}}$ and $\alpha_{Z\tilde{Z}}$

$$\mathcal{A}_\phi^{(2)} \simeq \frac{16\sqrt{1-12s}}{\pi(1+16s)} \left(s\alpha_{Z\tilde{Z}} + \frac{\bar{g}_V g_{em} Q_\ell}{4\bar{g}_A^2} \hat{\alpha}_{A\tilde{Z}} \right)$$

Conclusions

- Some angular asymmetries are much more sensitive to anomalous couplings than the decay width or the cross section.
- Relatively large effects from HAZ are still allowed.
- Effects of $HZll$ couplings are small (couplings are quite constrained by data).
[see also Buchalla, Catà, D'Ambrosio '13](#)
- Interesting asymmetries are small in absolute terms (<10%)
- e^+e^- is in general better suited for the study of $HZll$ anomalous couplings.