

Jets Physics

Algorithms and Substructure Techniques

Matteo Cacciari
LPTHE Paris



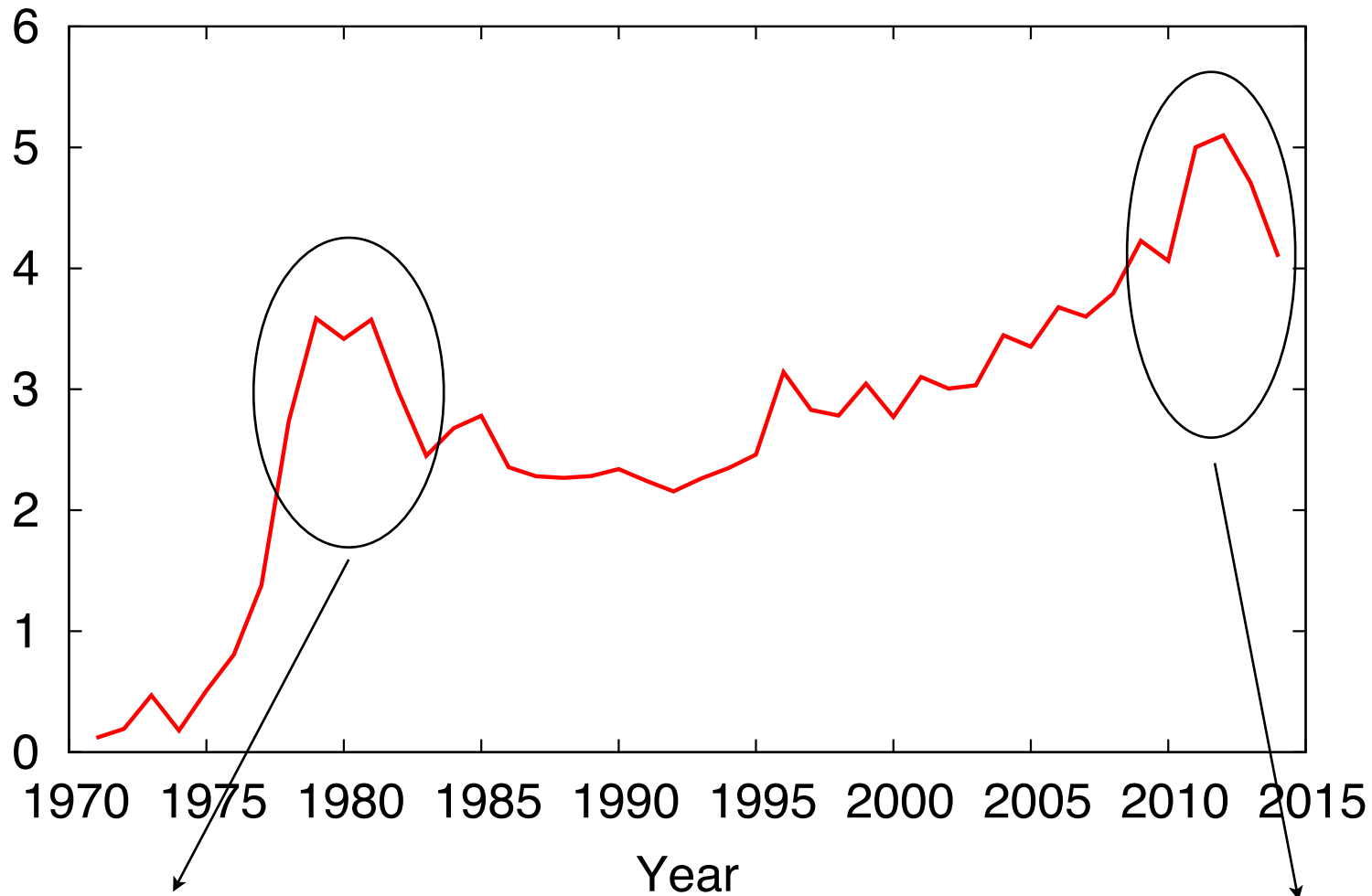
37th INTERNATIONAL CONFERENCE
ON HIGH ENERGY PHYSICS

2 - 9 - JULY - 2014 - VALENCIA



Jet revolutions

Percentage of papers in INSPIRE containing the word "jet"



First 'jet revolution'

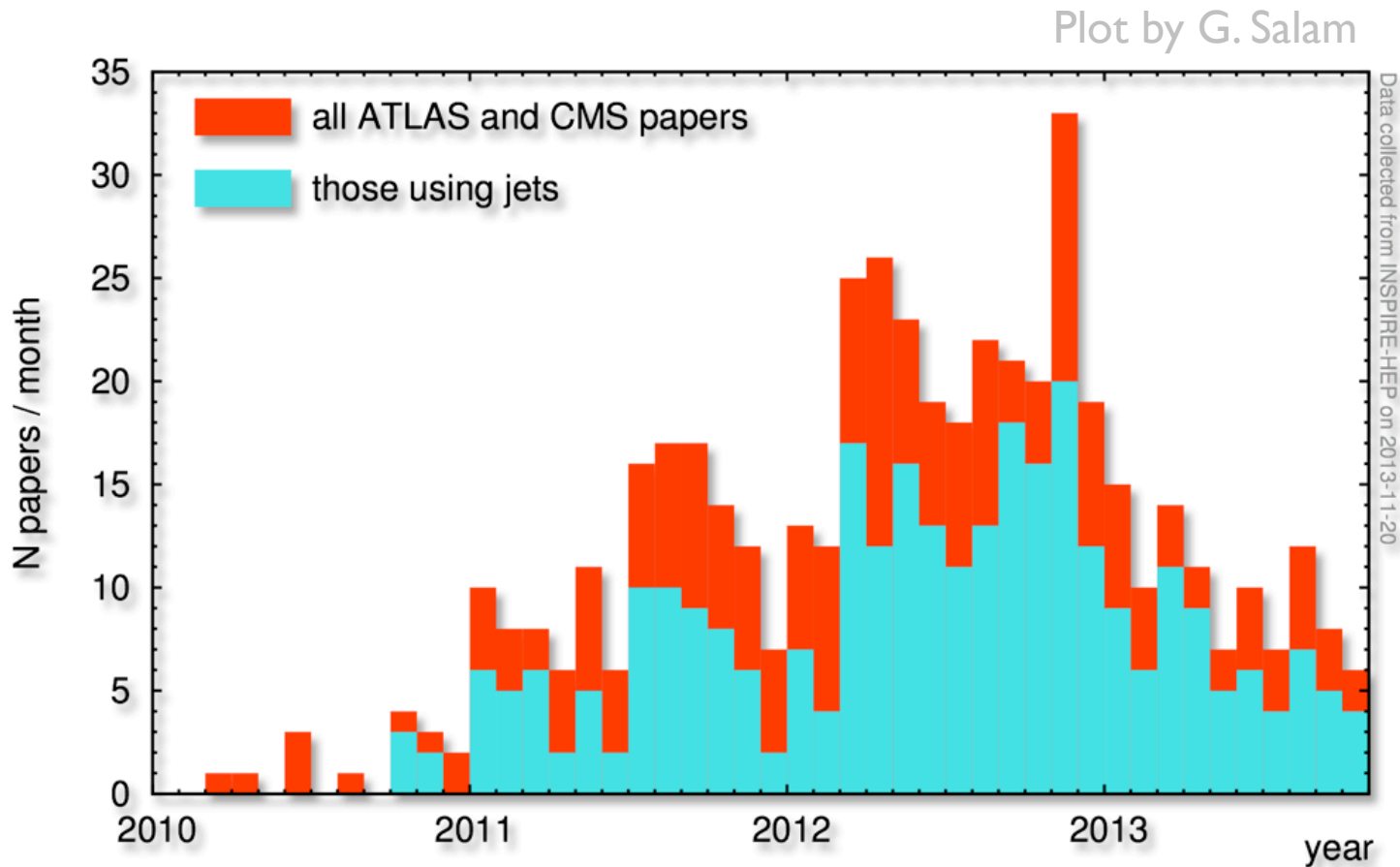
Second 'jet revolution'?

(1% \approx 500 papers)

NB: Data not noise-subtracted

The pervasiveness of jets

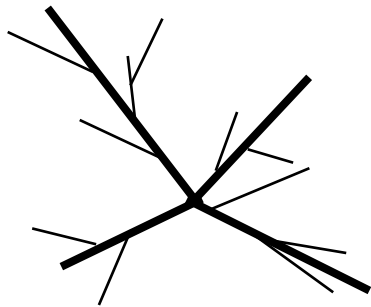
- ▶ ATLAS and CMS have each published **300+** papers since 2010
 - ▶ More than **a third** of these papers make use of **jets**
 - ▶ **60%** of the **searches** papers makes use of **jets**



(Source: INSPIRE.
Results may vary when
employing different search
keywords)

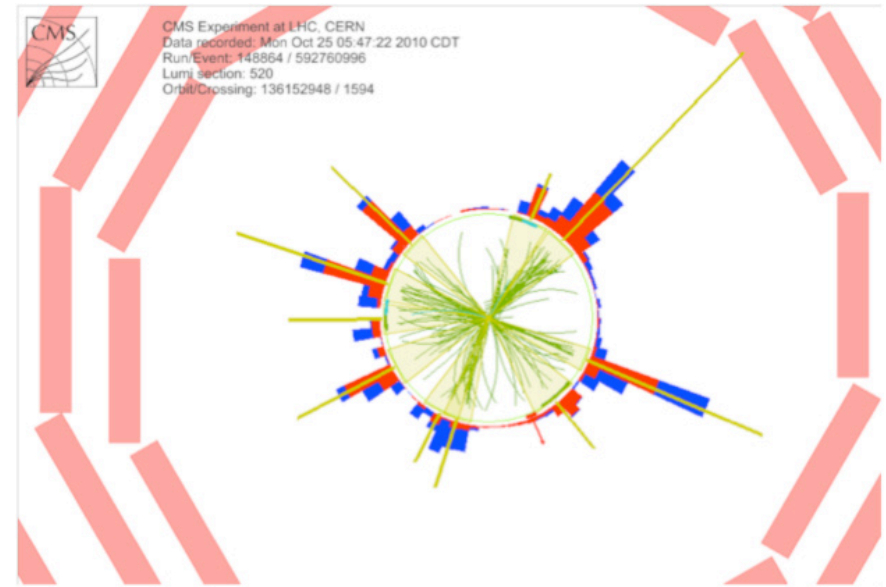
Why are jets so important?

Multileg + PS



QCD predictions

??



Real data

Jets

One purpose of a 'jet clustering' algorithm is to **reduce the complexity** of the final state, simplifying many hadrons to **simpler objects** that one can hope to **calculate**

From Wikipedia:

In [ancient Roman religion](#) and [myth](#), **Janus** ([Latin](#): *Ianus*, pronounced [ˈjaɲ.nus]) is the [god](#) of beginnings and transitions, and thereby of gates, doors, passages, endings and time. He is usually depicted as having two faces, since he looks to the future and to the past. The Romans named the month of January ([Ianuarius](#)) in his honor.



Like Janus, jets can serve **two** purposes:

▶ **Observables**

to be defined, calculated, measured

▶ **Tools**

to be used to extract specific properties of the final state

Requirements for jet algorithms

- ▶ In order to be most useful as an *observable*, a jet algorithm should be usable in perturbation theory and its jets not too affected by non-perturbative physics
 - ▶ Infrared and collinear safety
 - ▶ Controlled sensitivity to hadronisation and underlying event
 - ▶ Possibility to subtract effectively pile-up contamination
- ▶ Two main classes of jet algorithms:
 - ▶ cones
 - ▶ sequential recombination algorithms
 - ▶ Sequential recombination algorithms (k_t , Cambridge/Aachen, anti- k_t) provide a clustering history
 - ▶ When physically meaningful, the clustering history can be exploited to explore the substructure of a jet → jet as a tool

IRC safe algorithms

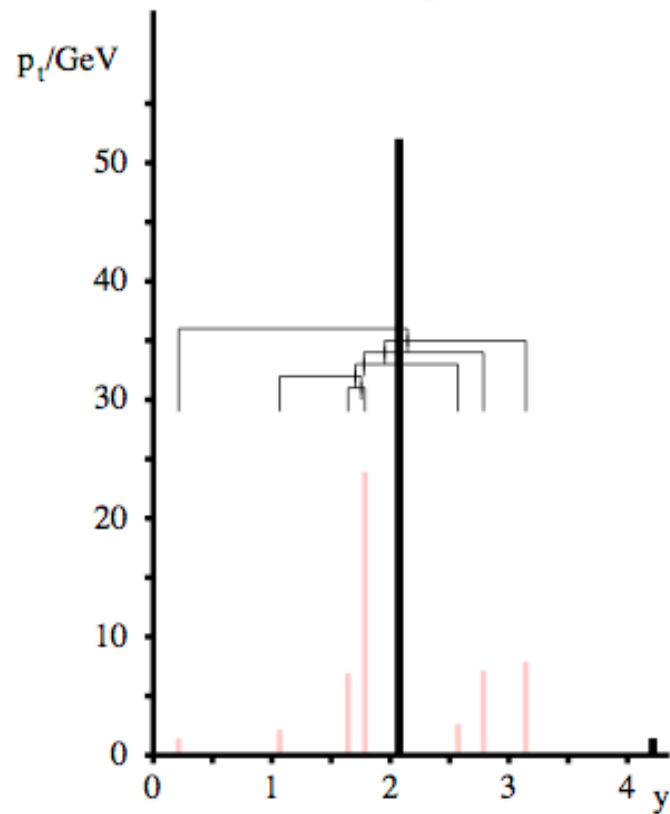
k_t	SR $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ hierarchical in rel p_t	Catani et al '91 Ellis, Soper '93	$N \ln N$
Cambridge/ Aachen	SR $d_{ij} = \Delta R_{ij}^2 / R^2$ hierarchical in angle	Dokshitzer et al '97 Wengler, Wobish '98	$N \ln N$
anti- k_t	SR $d_{ij} = \min(k_{ti}^{-2}, k_{tj}^{-2}) \Delta R_{ij}^2 / R^2$ gives perfectly conical hard jets	MC, Salam, Soyez '08 (Delsart, Loch)	$N^{3/2}$
SISCone	Seedless iterative cone with split-merge gives 'economical' jets	Salam, Soyez '07	$N^2 \ln N$

'second-generation' algorithms

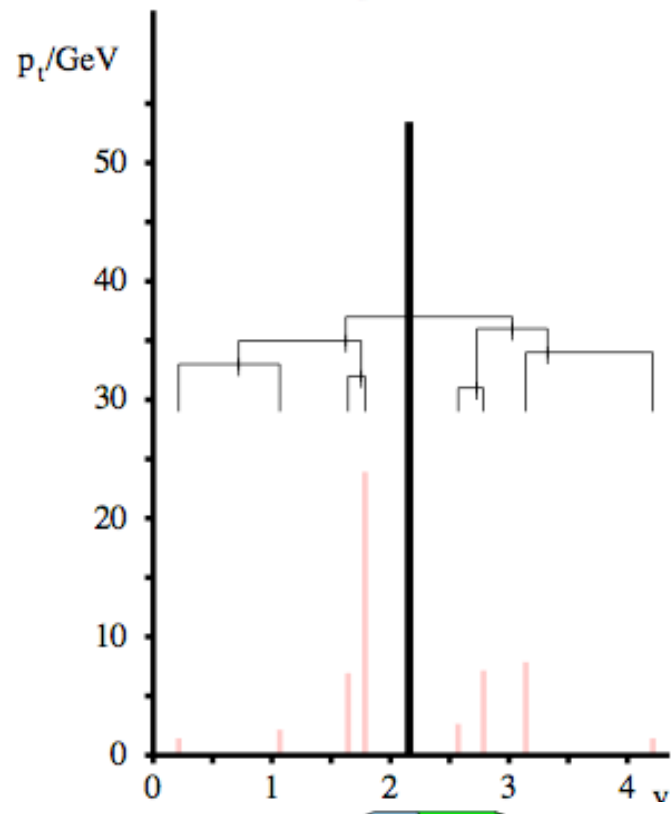
All (as well as many IRC unsafe ones) are available in FastJet, <http://fastjet.fr>

Hierarchical substructure

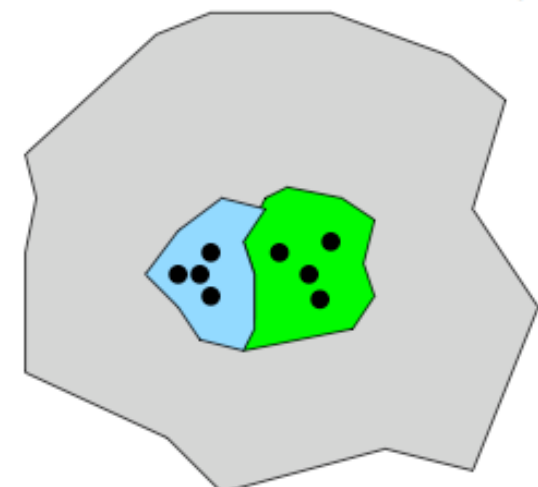
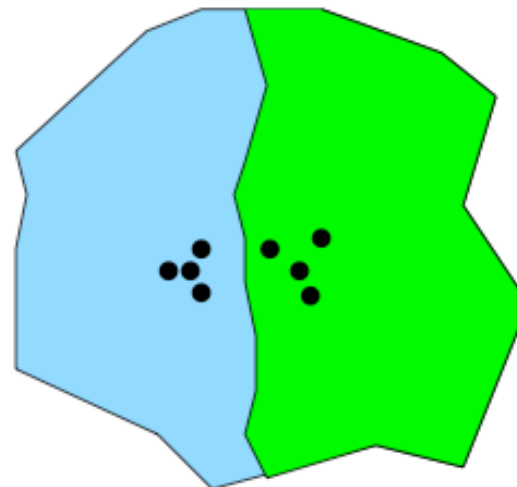
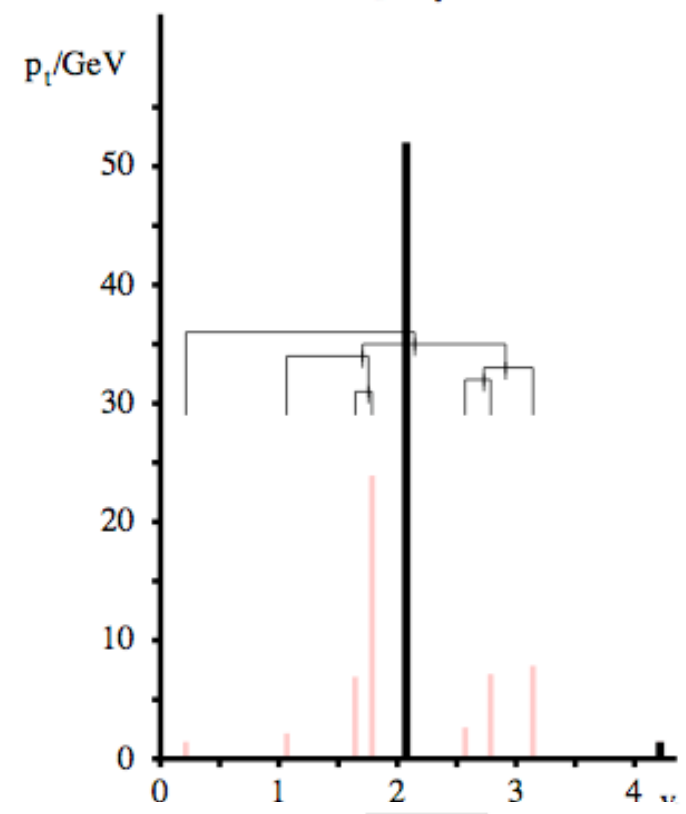
anti- k_t algorithm



k_t algorithm

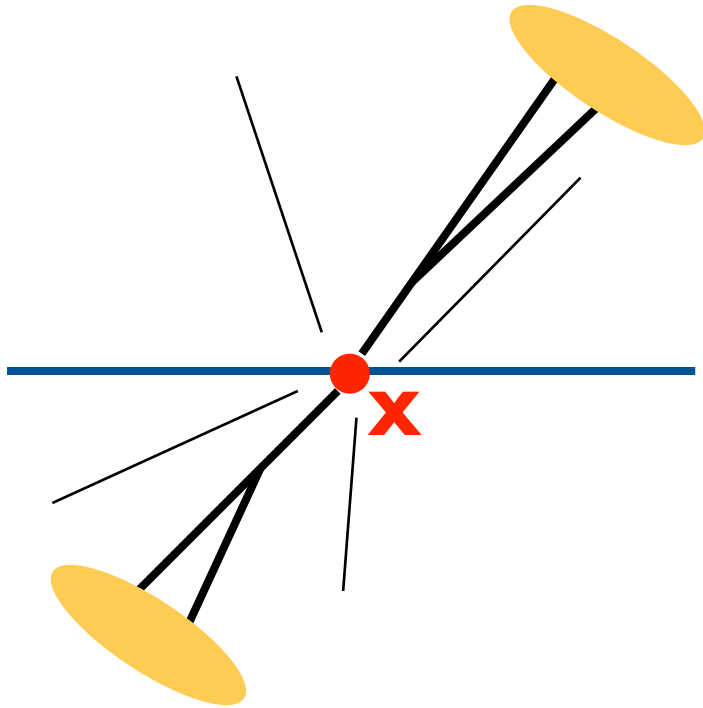


Cambridge/Aachen



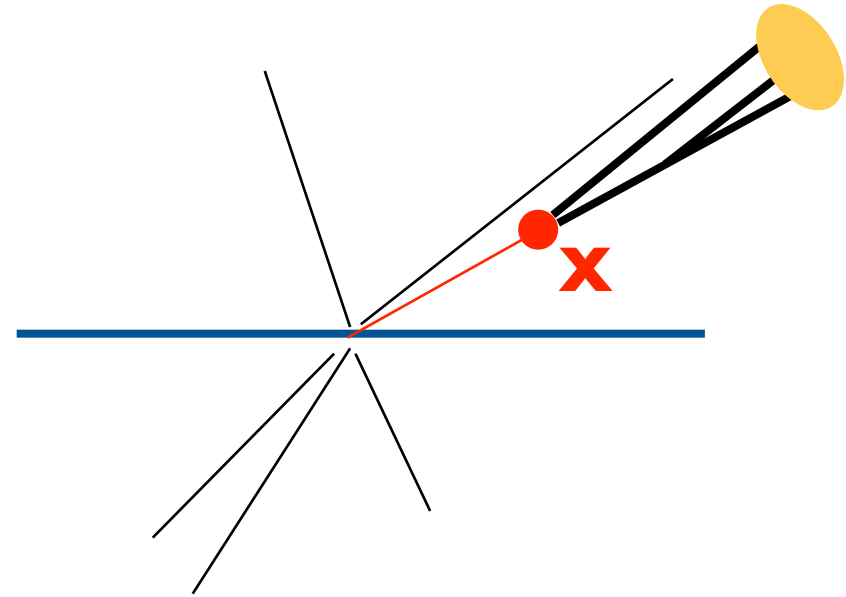
Slide by
Gavin Salam

Why boosted objects



Heavy particle X at **rest**

Easy to resolve jets and calculate invariant mass, but signal very likely swamped by background (eg $H \rightarrow bb$ v. $tt \rightarrow WbWb$)



Boosted heavy particle X

Cross section very much reduced, but acceptance better and some backgrounds smaller/reducible

Why jet substructure

- ▶ The substructure of a jet can be exploited to
 - ▶ **tag** a particular structure inside the jet, i.e. a massive particle
 - ▶ First examples: Higgs (2-prongs decay), top (3-prongs decay)
 - ▶ remove background contamination from the jet or its components, while keeping the bulk of the perturbative radiation
 - ▶ First examples: filtering, trimming, pruning
 - ▶ This operation is often generically denoted as **grooming**

Generic tagging/grooming

Fat-jet finding

Often anti-kt, $R \approx 1$



large p_t , large mass fat-jet,
signal or background

Tagging step



signal jet candidate, still
partly background-contaminated

grooming step



**final candidate, potentially with
little background contamination**

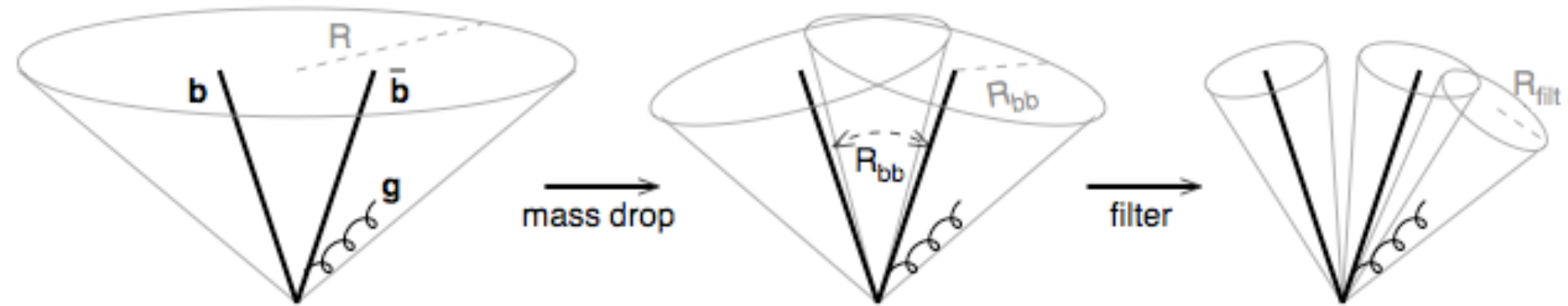
Note that in some taggers
(e.g. pruning) the tagging
and grooming steps are
not explicitly factorised

Also, some tools may
actually not follow rigidly
this scheme

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$

The BDRS tagger/groomer

Butterworth, Davison, Rubin, Salam, 2008

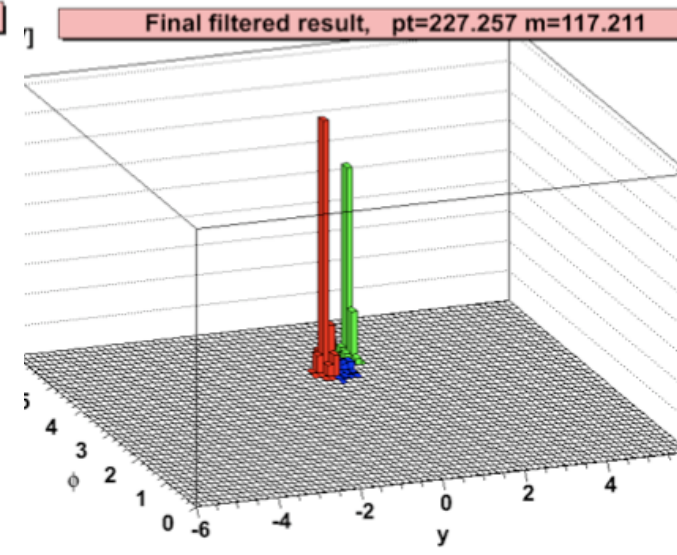
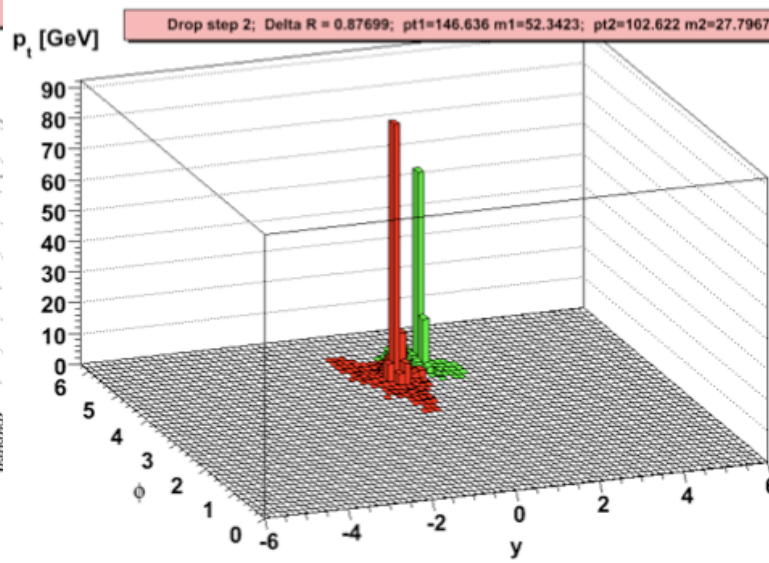
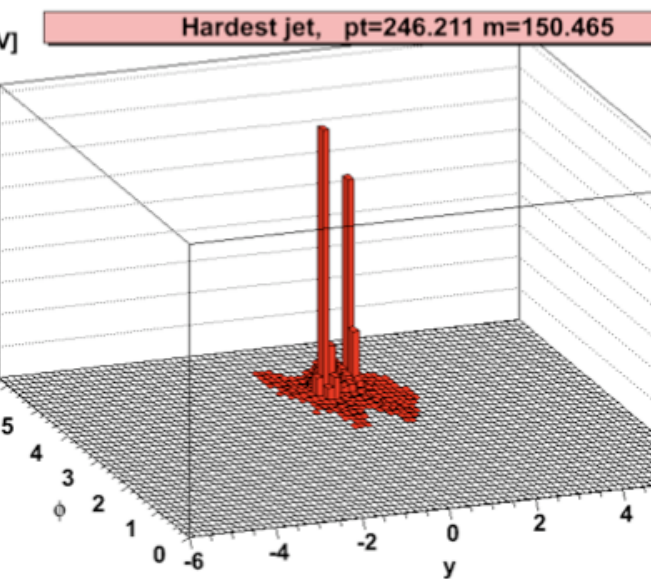
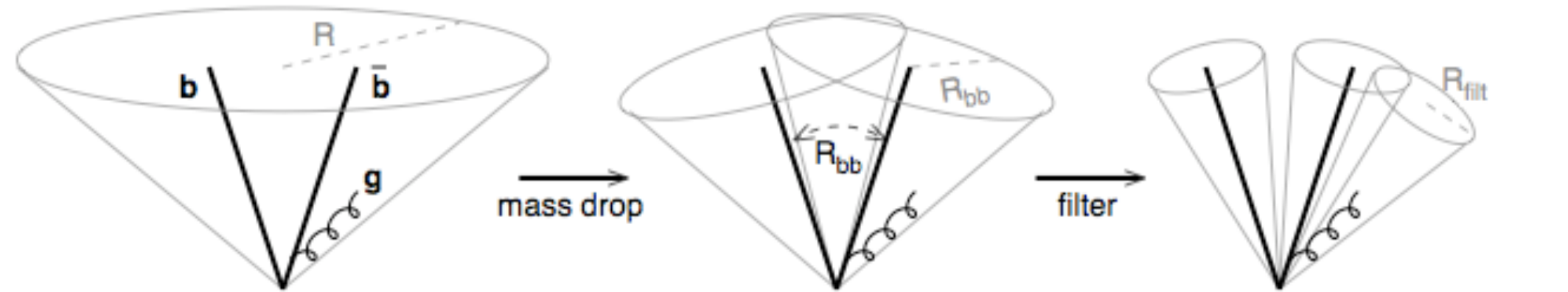


- ▶ A two-prongs tagger/groomer for boosted Higgs, which
 - ▶ Uses the **Cambridge/Aachen** algorithm
 - ▶ Employs a **Mass-Drop** condition, as well as an **asymmetry cut** to find the relevant splitting (i.e. '**tag**' the heavy particle)
 - ▶ Includes a post-processing step, using '**filtering**' (introduced in the same paper) to clean as much as possible the resulting jets of UE contamination ('**grooming**')

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$$

Visualisation of BDRS

Butterworth, Davison, Rubin, Salam, 2008



Cluster with a large R

Undo the clustering into subjects, until a large mass drop is observed: tagging step

Re-cluster with smaller R, and keep only 3 hardest jets: grooming step

The jet substructure maze

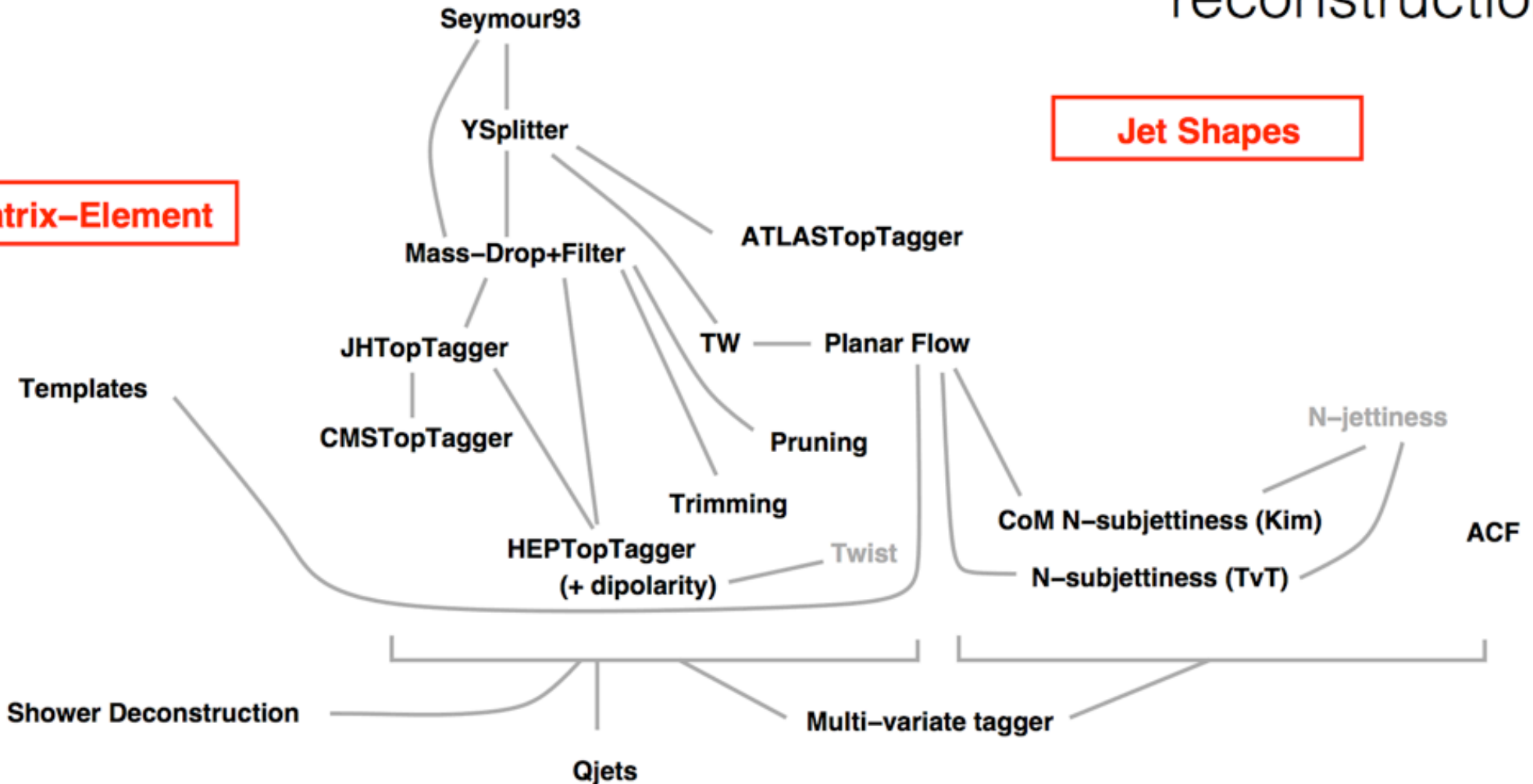
Slide by
G. Salam

Some of the tools developed
for boosted W/Z/H/top
reconstruction

Jet Declustering

Jet Shapes

Matrix-Element



First taggers/groomers

▶ Mass Drop + Filtering

Butterworth, Davison, Rubin, Salam, 2008

Decluster with mass drop and asymmetry conditions

Recluster constituents into subjects at distance scale R_{filt} , retain n_{filt} hardest subjects

▶ Jet 'trimming'

Krohn, Thaler, Wang, 2009

Recluster constituents into subjects at distance scale R_{trim} , retain subjects with $p_{t,\text{subject}} > \epsilon_{\text{trim}} p_{t,\text{jet}}$

▶ Jet 'pruning'

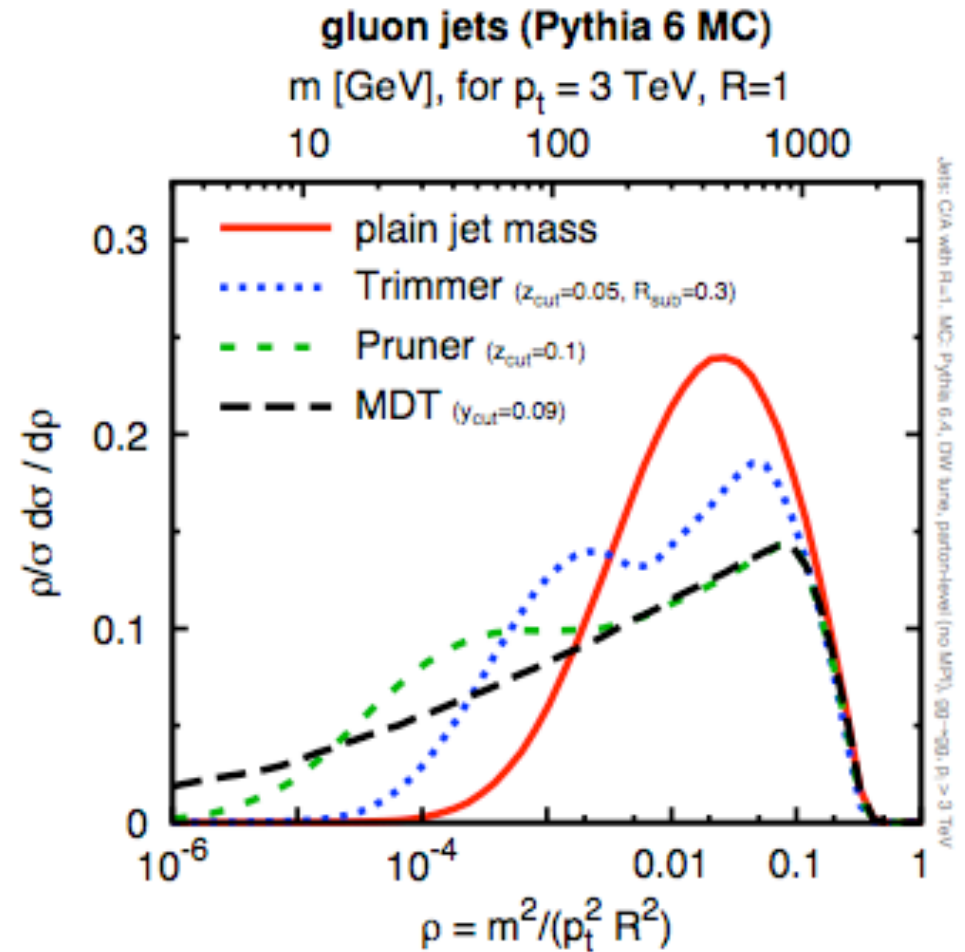
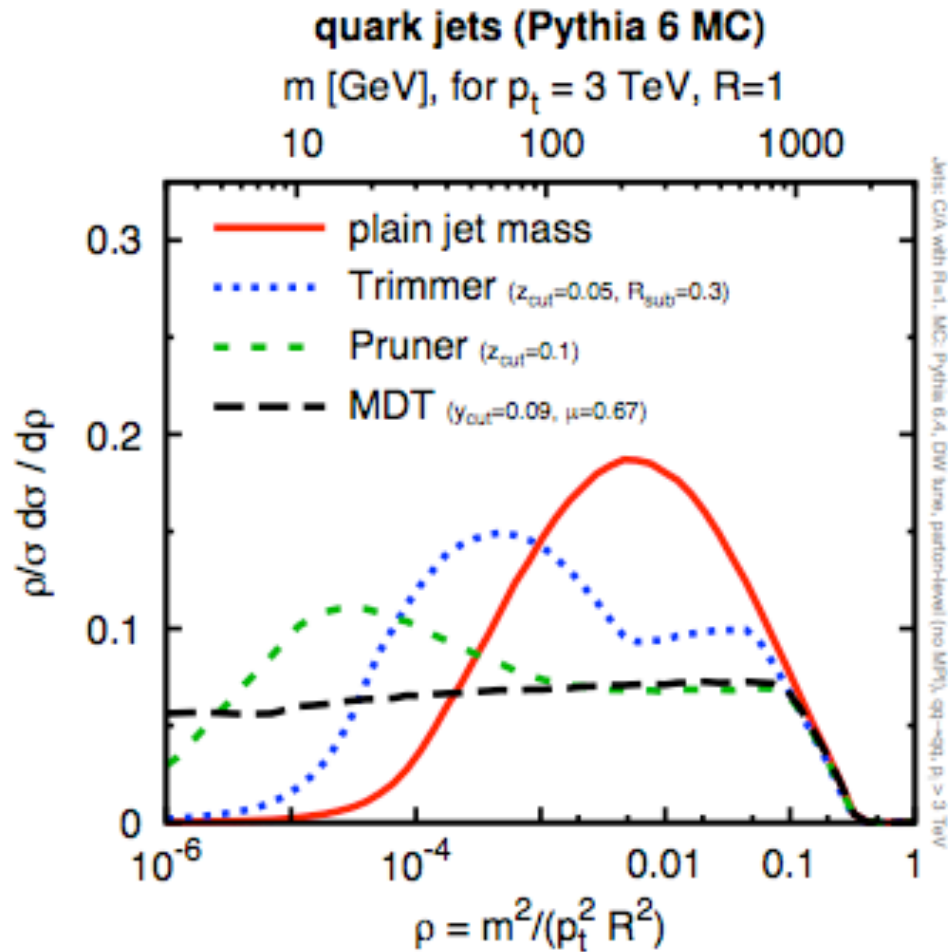
S. Ellis, Vermilion, Walsh, 2009

While building up the jet, discard softer subjects when $\Delta R > R_{\text{prune}}$ and $\min(p_{t1}, p_{t2}) < \epsilon_{\text{prune}} (p_{t1} + p_{t2})$

Aim: limit contamination from QCD background while retaining bulk of perturbative radiation

Robustness of substructure tools

Dasgupta, Fregoso, Marzani, Salam, 2008



Tools that are considered (or can be seen in Monte Carlo tests) to behave ‘similarly’ could cease to do so in different parameter regions

Analytic calculations of jet substructure

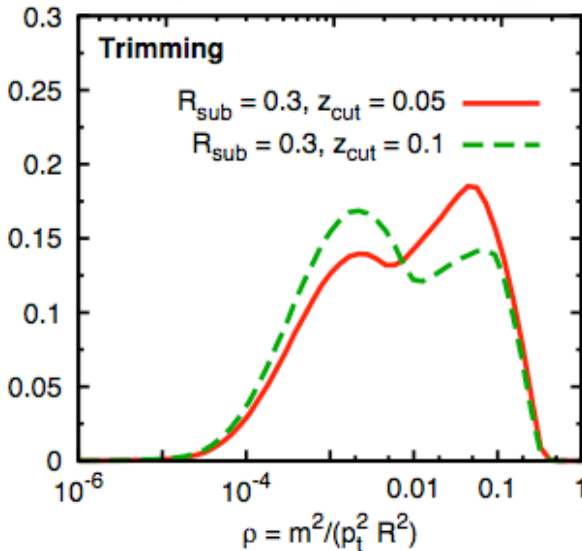
Dasgupta, Fregoso, Marzani, Salam, 2013

Monte Carlo

Pythia 6 MC: gluon jets

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



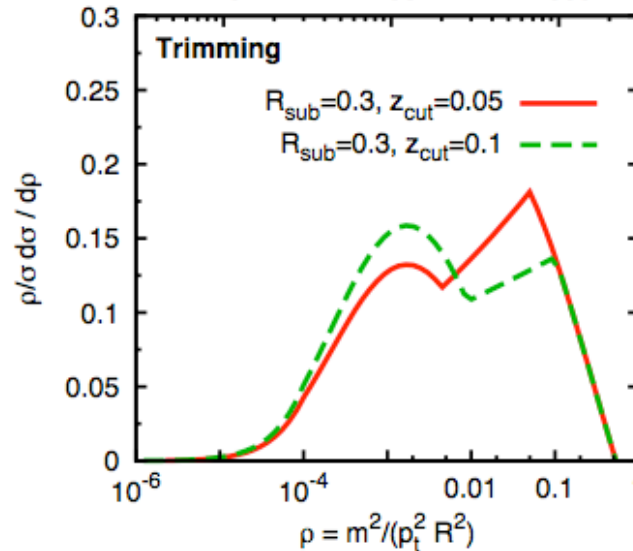
Analytic

(resummed pQCD)

Analytic Calculation: gluon jets

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



- ▶ Analytical understanding of ‘kinks’ in distributions
- ▶ Check of Monte Carlo predictions
- ▶ Other analytical investigations: Rubin 2010 (filtering), Walsh, Zuberi 2011 (jet substructure with SCET), Feige Schwartz, Stewart, Thaler 2012 (N-subjettiness), Dasgupta, Marzani, Powling 2013 (groomed jet mass), ...

$$\frac{1}{\sigma} \frac{d\sigma}{dm^2}^{(\text{trim, LO})} = \frac{\alpha_s C_F}{\pi} \int_0^1 dz p_{gq}(z) \int \frac{d\theta^2}{\theta^2} \delta(m^2 - z(1-z)p_t^2 \theta^2) \times$$

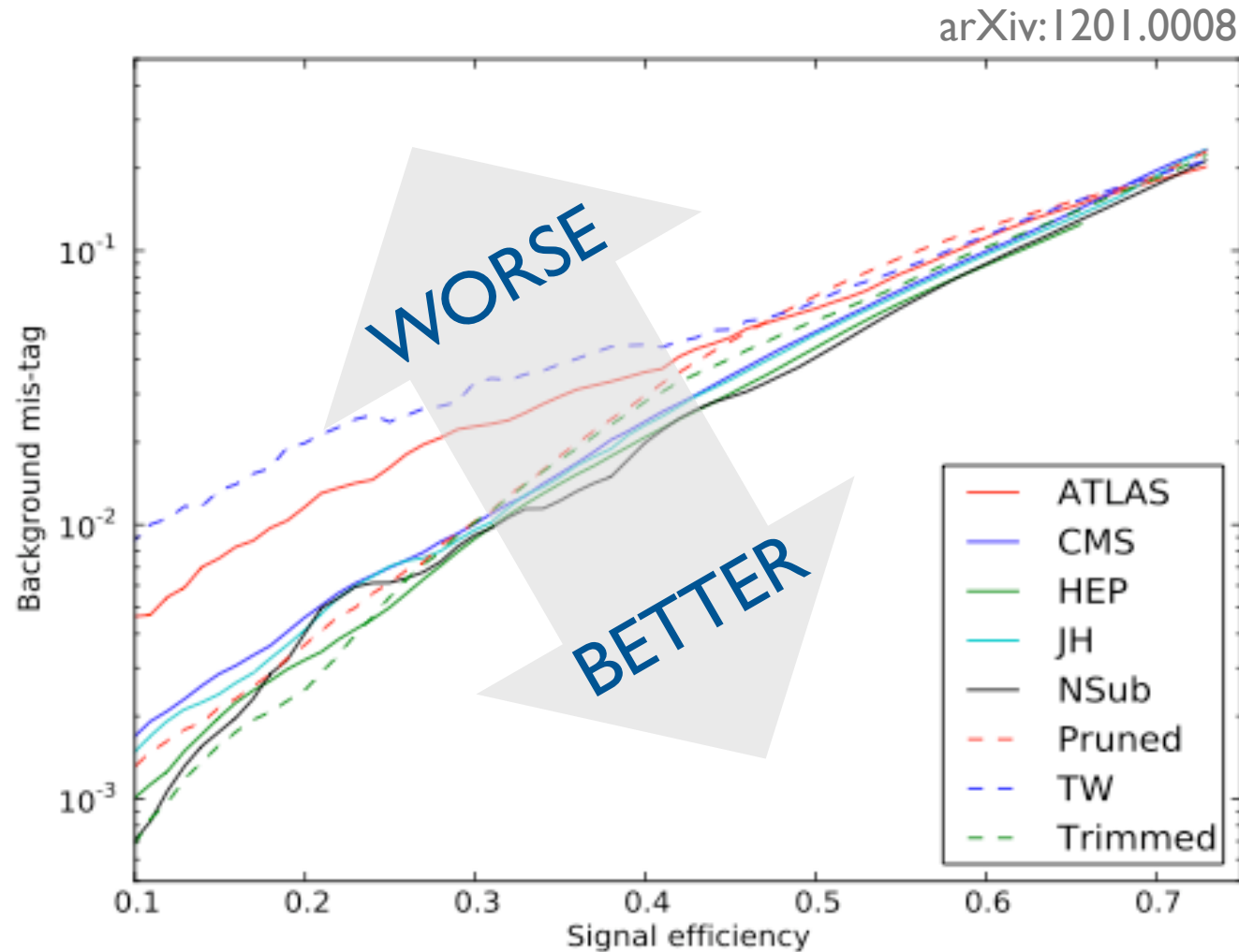
$$\times \left[\Theta(z - z_{\text{cut}}) \Theta(1 - z - z_{\text{cut}}) \Theta(\theta^2 - R_{\text{sub}}^2) + \Theta(R_{\text{sub}}^2 - \theta^2) \right] \Theta(R^2 - \theta^2)$$

Alternatives to (standard) substructure

- ▶ If what we are interested in is the structure of the constituents of a jet, the “jet” itself is not the most important feature.
- ▶ A different algorithm, or simply the study of the constituents in a certain patch will also do. Selected alternatives are:
 - ▶ Use of jet-shapes to characterise certain features
 - ▶ e.g. *N-subjettiness*: how many subjects a jets appears to have
Thaler, van Tilburg, 2011
 - ▶ Alternative ways of clustering
 - ▶ e.g. *Qjets*: the clustering history not deterministic, but controlled by random probabilities of merging. Can be combined with, e.g. pruning
Ellis, Hornig, Roy, Krohn, Schwartz, 2012
 - ▶ Use information from matrix element
 - ▶ e.g. *shower deconstruction*: use analytic shower calculations to estimate probability that a certain configuration comes from signal or from background
Soper, Spannowsky, 2011
 - ▶ Use event shapes mimicking jet properties
 - ▶ e.g. *JetsWithoutJets*, mimicking trimming
Bertolini, Chen, Thaler, 2013

Performance comparisons

Many of the substructure-based tools have been systematically compared, for instance in the context of the proceedings of the BOOST conferences



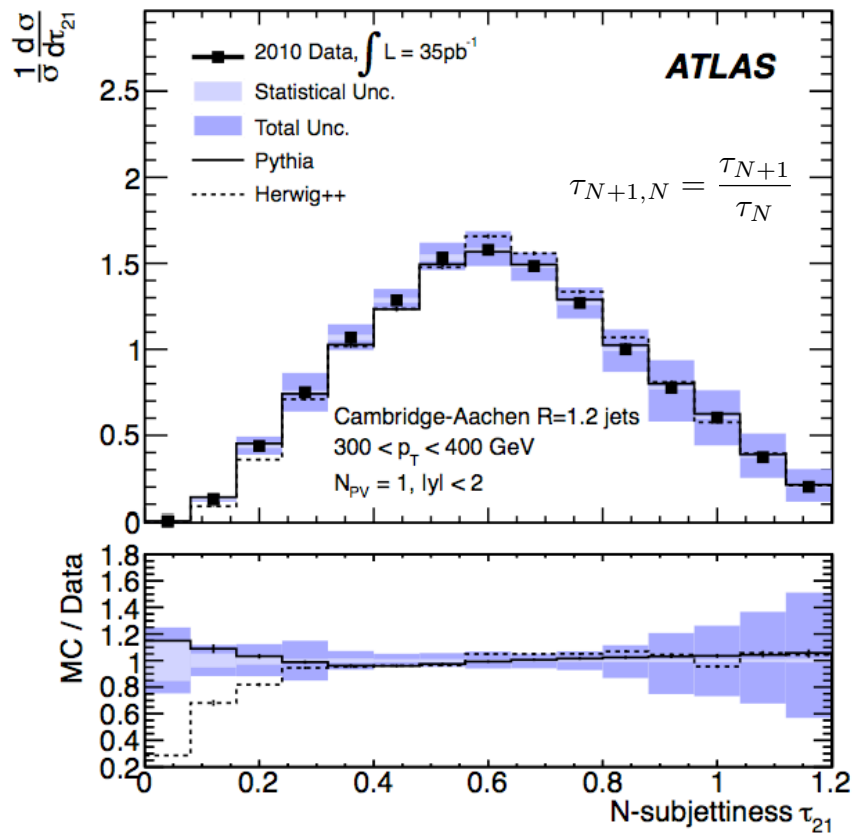
Efficiency-mistag curves for many top taggers.

Improvements upon earlier tools have become hard to obtain

Experimental validation

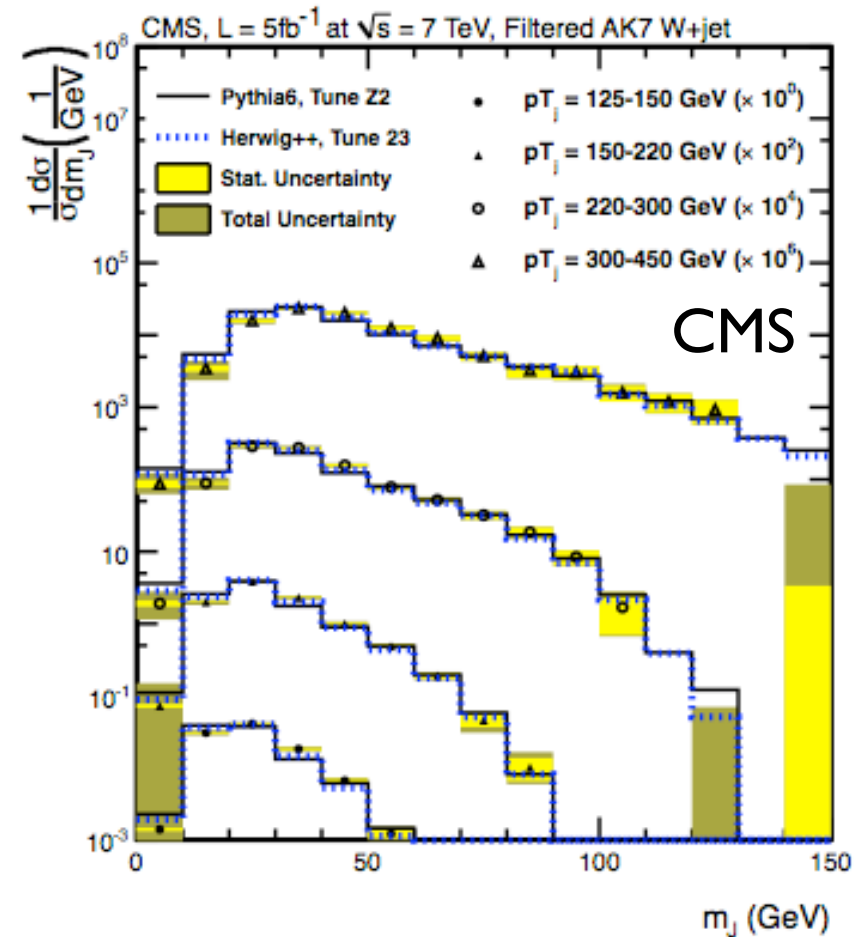
ATLAS and CMS have extensively validated the new grooming techniques, and also produced the first results using them

arXiv:1203.4606



N-subjettiness

arXiv:1303.4811



Filtered jet mass

Jet substructure in experiments

Slide by G. Salam

Extensive experimental work

Last 12 ATLAS & CMS preprints citing jet substructure work

Jet Cross-Section Measurements In CMS

CMS Collaboration

[Inspire](#). [arXiv:1306.6604](#) (ps, pdf). Int.J.Mod.Phys. A28 (2013) 1330030.

Performance of jet substructure techniques for large- R jets in proton-proton collisions at $\sqrt{s} = 7$ TeV using the ATLAS detector

ATLAS Collaboration

[Inspire](#). [arXiv:1306.4945](#) (ps, pdf). JHEP 1309 (2013) 076. 16 cites [\[co\]](#)

Measurement of jet shapes in top pair events at $\sqrt{s} = 7$ TeV using the ATLAS detector

ATLAS Collaboration

[Inspire](#). [arXiv:1307.5749](#) (ps, pdf).

Searches for New Physics in Multijet Final States

for the CMS Collaboration

[Inspire](#). [arXiv:1307.2518](#) (ps, pdf).

Search for Single and Pair-Production of Dijet Resonances with the CMS Detector

CMS Collaboration

[Inspire](#). [arXiv:1307.1400](#) (ps, pdf). J.Phys.Conf.Ser. 455 (2013) 012034. 1 cites [\[co\]](#)

Search for dark matter in events with a hadronically decaying W or Z boson and missing transverse momentum in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector

ATLAS Collaboration

[Inspire](#). [arXiv:1309.4017](#) (ps, pdf). 5 cites [\[co\]](#)

Searches for anomalous $t\bar{t}$ production in pp collisions at $\sqrt{s} = 8$ TeV

CMS Collaboration

[Inspire](#). [arXiv:1309.2030](#) (ps, pdf). 6 cites [\[co\]](#)

Search for heavy resonances decaying to top quarks for the CMS Collaboration

[Inspire](#). [arXiv:1310.8183](#) (ps, pdf).

Search for the standard model Higgs boson produced in association with a W or a Z boson and decaying to bottom quarks

CMS Collaboration

[Inspire](#). [arXiv:1310.3687](#) (ps, pdf). 3 cites [\[co\]](#)

Search for the SM Higgs Boson Produced in Association with a Vector Boson and Decaying to Bottom Quarks

for the CMS Collaboration

[Inspire](#). [arXiv:1310.3551](#) (ps, pdf).

Inclusive search for a vector-like T quark with charge 2/3 in pp collisions at $\sqrt{s} = 8$ TeV

CMS Collaboration

[Inspire](#). [arXiv:1311.7667](#) (ps, pdf).

Search for top-quark partners with charge 5/3 in the same-sign dilepton final state

CMS Collaboration

[Inspire](#). [arXiv:1312.2391](#) (ps, pdf).

Certainly incomplete
list of phenomenology
papers

Discovering baryon-number violating neutralino decays at the LHC

Jonathan M. Butterworth, John R. Ellis, Are R. Raklev, Gavin P. Salam, [arXiv:0906.0728](#)

Stop Reconstruction with Tagged Tops

Tilman Plehn, Michael Spannowsky, Michihisa Takeuchi, Dirk Zerwas, [arXiv:1006.2833](#)

Boosted Semileptonic Tops in Stop Decays

Tilman Plehn, Michael Spannowsky, Michihisa Takeuchi, [arXiv:1102.0557](#)

Scale-invariant resonance tagging in multijet events and new physics in Higgs pair production

Maxime Gouzevitch, Alexandra Oliveira, Juan Rojo, Rogerio Rosenfeld, Gavin P. Salam, Veronica Sanz, [arXiv:1303.6636](#)

Pulling Out All the Stops: Searching for RPV SUSY with Stop-Jets

Yang Bai, Andrey Katz, Brock Tweedie, [arXiv:1309.6631](#)

Measuring boosted tops in semi-leptonic $t\bar{t}$ events for the standard model and beyond

Mihailo Backovic, Ofir Gabizon, Jose Juknevich, Gilad Perez, Yotam Soreq, [arXiv:1311.2962](#)

Reconstructing singly produced top partners in decays to Wb

Nicolas Gutierrez Ortiz, James Ferrando, Deepak Kar, Michael Spannowsky, [arXiv:1403.7490](#)

Hadronic b' search at the LHC with top and W taggers

Shuo Yang, Ji Jiang, Qi-Shu Yan, Xiaoran Zhao, [arXiv:1405.2514](#)

- ▶ **“Plain” jet clustering is mainstream**
 - ▶ All main algorithms implemented in a standardized, efficient and public way, used by all LHC collaborations and phenomenologists
- ▶ **Jet substructure techniques also largely mature**
 - ▶ tens of different approaches:
 - ▶ risk of fragmentation and poor readability
 - ▶ use of standard, public tools rather than *ad hoc* ones helps consolidation of the field
 - ▶ are further improvements in performance becoming hard to achieve?
 - ▶ many approaches only tested at MC level: robustness?
 - ▶ analytical control should become a must

Substructure TODO

- ▶ There may still be room for further improvement in jet substructure techniques
- ▶ To avoid fragmenting the field, and make progress efficient, we should
 - ▶ Introduce techniques motivated by analytical arguments, not simply MC testing
 - ▶ Ensure that they enjoy a **good analytical calculability**
 - ▶ very little reason to introduce today a novel substructure technique that does not enjoy a decent calculability, unless HUGE improvement can be shown (and still, it should be justifiable and robust)
 - ▶ Provide a **public implementation** (e.g. in the FastJet contrib project, <http://fastjet.hepforge.org/contrib>, public repository for third-party contributions)

Soft Drop declustering

Larkoski, Marzani, Soyeur, Thaler, van Tilburg, 2014

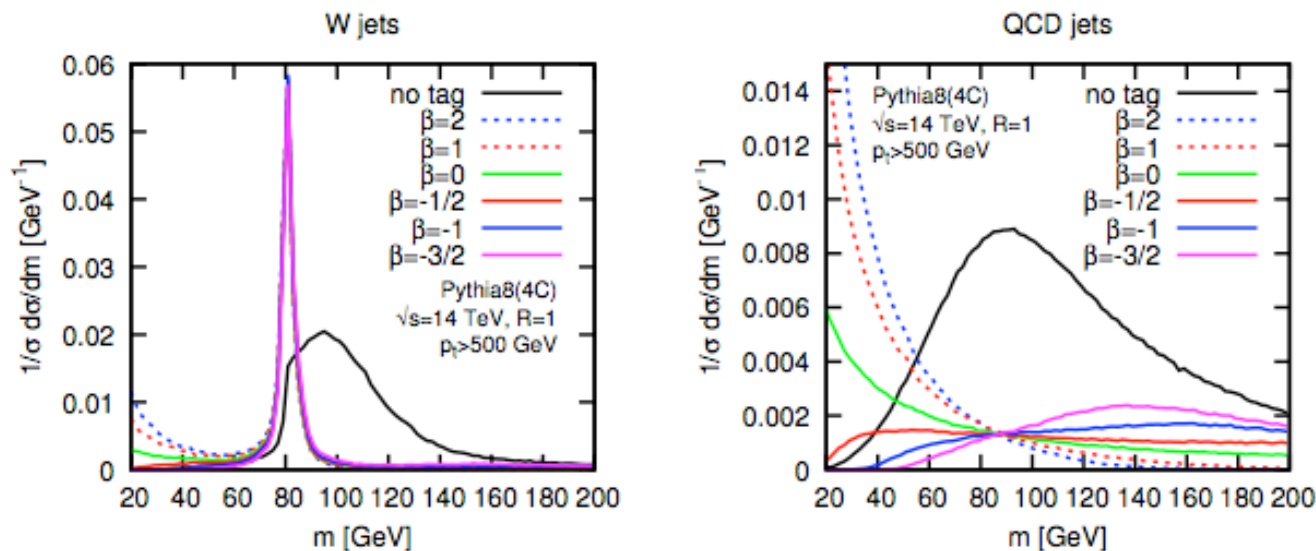
Decluster and drop softer constituent unless

$$\text{Soft Drop Condition: } \frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{\text{cut}} \left(\frac{\Delta R_{12}}{R_0} \right)^\beta$$

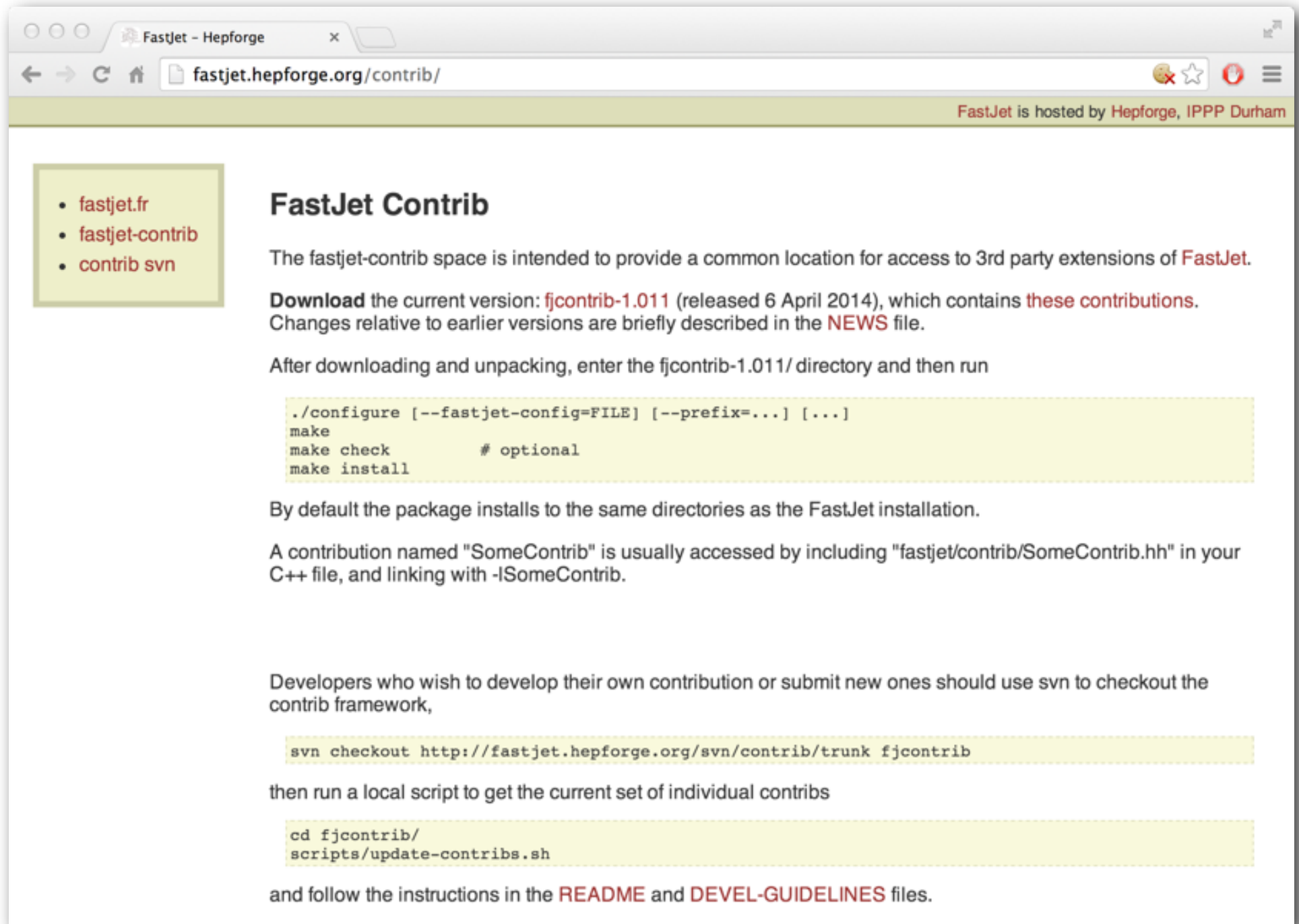
i.e. remove wide-angle soft radiation from a jet

The paper contains

- ✓ analytical calculations and comparisons to Monte Carlos
- ✓ study of effect of non-perturbative corrections
- ✓ performance studies



Example of SoftDrop performance when used as a boosted W tagger



The screenshot shows a web browser window with the address bar containing `fastjet.hepforge.org/contrib/`. The page title is "FastJet - Hepforge". A navigation menu on the left lists [fastjet.fr](#), [fastjet-contrib](#), and [contrib svn](#). The main content area has a heading "FastJet Contrib" and a paragraph explaining the purpose of the space. It includes instructions for downloading the current version (fjcontrib-1.011) and running the configuration script. A code block shows the commands for configuration and installation. Further instructions describe how to use contributions and how to develop new ones using svn. A second code block shows the svn checkout command and a local script to update contributions. The page concludes with a reference to the README and DEVEL-GUIDELINES files.

FastJet is hosted by Hepforge, IPPP Durham

- [fastjet.fr](#)
- [fastjet-contrib](#)
- [contrib svn](#)

FastJet Contrib

The fastjet-contrib space is intended to provide a common location for access to 3rd party extensions of **FastJet**.

Download the current version: **fjcontrib-1.011** (released 6 April 2014), which contains **these contributions**. Changes relative to earlier versions are briefly described in the **NEWS** file.

After downloading and unpacking, enter the `fjcontrib-1.011/` directory and then run

```
./configure [--fastjet-config=FILE] [--prefix=...] [...]  
make  
make check          # optional  
make install
```

By default the package installs to the same directories as the FastJet installation.

A contribution named "SomeContrib" is usually accessed by including "fastjet/contrib/SomeContrib.hh" in your C++ file, and linking with `-lSomeContrib`.

Developers who wish to develop their own contribution or submit new ones should use svn to checkout the contrib framework,

```
svn checkout http://fastjet.hepforge.org/svn/contrib/trunk fjcontrib
```

then run a local script to get the current set of individual contribs

```
cd fjcontrib/  
scripts/update-contribs.sh
```

and follow the instructions in the **README** and **DEVEL-GUIDELINES** files.

FastJet Contrib

FastJet is hosted by Hepforge, IPPP Durham

Version 1.011 of FastJet Contrib is distributed with the following packages

- fastjet.fr
- fastjet-contrib
- contrib svn

Package	Version	Information
ConstituentSubtractor	1.0.0	README NEWS
EnergyCorrelator	1.0.1	README NEWS
GenericSubtractor	1.2.0	README NEWS
JetCleanser	1.0.0	README NEWS
JetFFMoments	1.0.0	README NEWS
JetsWithoutJets	1.0.0	README NEWS
Nsubjettiness	1.0.3	README NEWS
ScJet	1.1.0	README NEWS
SubjetCounting	1.0.1	README NEWS
VariableR	1.0.1	README NEWS