



INTRODUCTION

- In high energy pp collisions, partons from incoming protons undergo interactions giving rise to outgoing high p_T partons which are observed as jets in the detector.
- Events with more than two partons (jets) in the final state include contribution from higher order QCD.
- The topology of the multijet events and kinematics of the outgoing partons are studied to test higher order QCD and to get a deeper insight to the underlying physics.
- Topological and kinematical variables are measured for 3-jet and 4-jet events using 5 fb^{-1} pp collision data at 7 TeV center of mass energy collected by CMS in 2011.
- Inclusive samples of events with 3 (or 4) jets are selected and variables are calculated from the leading n-jets in their center of mass system.

Analysis

- Jets are reconstructed using Particle Flow technique with Anti- k_T algorithm ($R=0.5$)
- Leading Jet p_T is supposed to lie in range 100-190 GeV and >500 GeV decided according to the efficiency of single jet triggers used. Non-leading jets are required to have p_T greater than 50 GeV. All the jets are required to have absolute rapidity less than 2.5
- Measured distributions are unfolded for detector effects using D'agostini's iterative method and compared with predictions from various Monte Carlos.
- Monte Carlo samples of PYTHIA6.4.26, PYTHIA8.153, HERWIG++2.5.0, MADGRAPH5.1.5.7 + PYTHIA6.4.26 are used with CTEQ6L1 PDF.

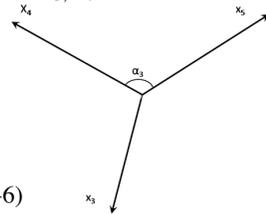
Variables Under Study

Three-Jet Events (1+2→3+4+5)

- Invariant Mass of the three jet system
- Scaled Energies of the jets ordered with respect to energies in center of mass frame (x_3, x_4).

$$x_i = \frac{2E_i}{\sqrt{s_{345}}}, x_3 + x_4 + x_5 = 2$$

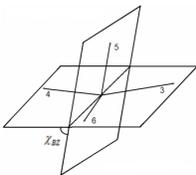
$$x_i = \frac{\sin \alpha_i}{\sum \sin \alpha_i}$$



Four-Jet Events (1+2→3+4+5+6)

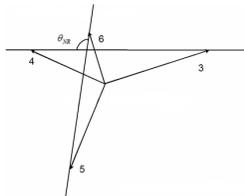
- Invariant Mass of the four jet system
- Bengtsson-Zerwas Angle** : Angle between planes containing the two leading jets and the two non leading jets.

$$\cos \chi_{BZ} = \frac{(\vec{p}_3 \times \vec{p}_4) \cdot (\vec{p}_5 \times \vec{p}_6)}{|\vec{p}_3 \times \vec{p}_4| |\vec{p}_5 \times \vec{p}_6|}$$



- Nachmann-Reiter Angle** : Angle between the momentum vector difference of the two leading jets and the two non-leading jets.

$$\cos \theta_{NR} = \frac{(\vec{p}_3 - \vec{p}_4) \cdot (\vec{p}_5 - \vec{p}_6)}{|\vec{p}_3 - \vec{p}_4| |\vec{p}_5 - \vec{p}_6|}$$



Systematic Uncertainty

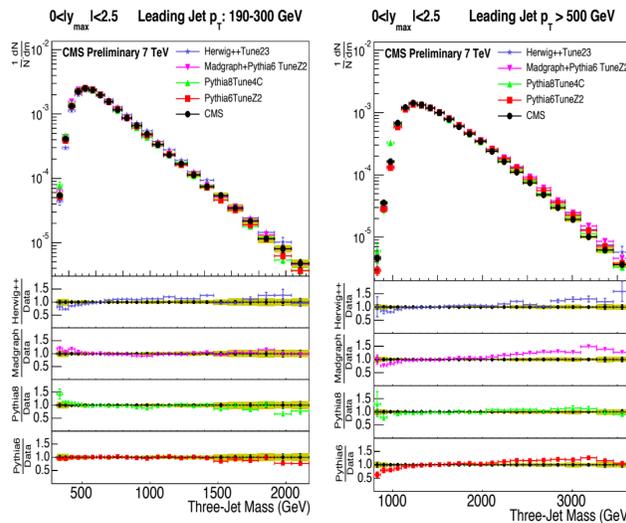
Calculated from the various sources as follows:

- Jet Energy Scale:** Uncertainty due to absolute determination of jet energy. This component varies over range of the variables and can be as high as 4-6% for 3-jet invariant mass and 7-10% for 4-jet invariant mass and is within 2% for dimensionless variables.
- Jet Energy Resolution:** Uncertainty due to detector resolution in jet energy measurement. This component goes up to 15% for 4-jet mass and 10% for 3-jet mass but lies within 6% for other variables.
- Response Matrix:** Uncertainty due to choice of response matrix for unfolding the measurements. This goes up to 10% for invariant mass but lies within 5% for other variables.
- Selection Uncertainty:** Uncertainty due to different jet identification criteria and event selection criteria. This is the smallest component of the systematic uncertainty and is typically less than 0.3%.

Three-jet Results

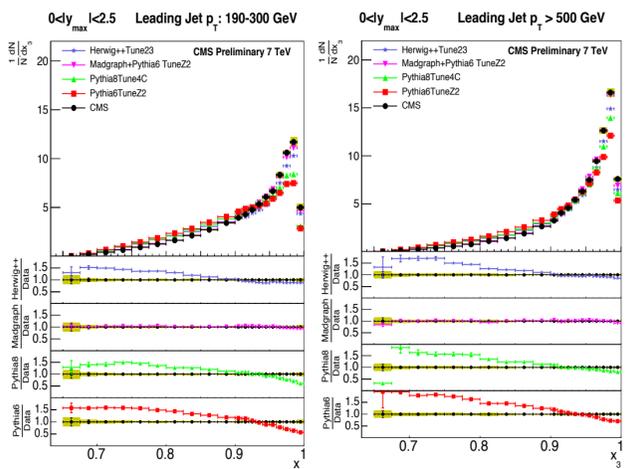
Invariant Mass

- The peak shifts to higher mass and gets broader at higher p_T .
- All models have trouble in explaining the turn-on at the low mass. Agreement gets better at higher mass.
- Pythia6 provides reasonable description at low p_T bins but not at high p_T .
- Madgraph is closer to data particularly at high p_T bins.
- Pythia8 has the worst agreement with data.
- Mean difference is at the level of 4-15%.



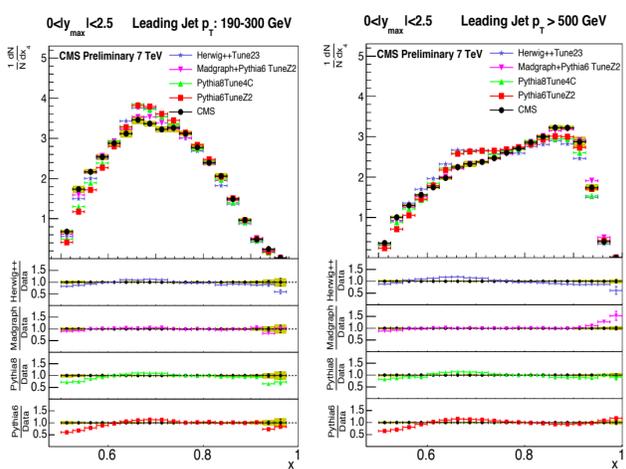
x_3

- The distributions peak close to 1 and the rise become sharper at higher p_T bins.
- Deviation from a linear increase is a feature of QCD which is seen in the data as well as in the MC. However the sharp turn over at large x_3 is not present in the MC
- None of the models can provide a good description of data.
- The deviation of the ratio from 1 can be as large as 50% in some bins (larger in Pythia)



x_4

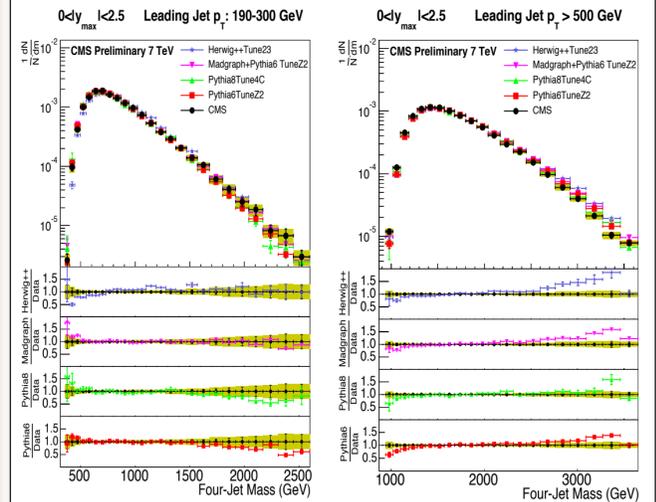
- The distribution peaks around 0.65 at the low p_T bin and peak shifts to higher values at larger p_T bins.
- The mean difference of the Pythia6 prediction from data typically is 10-15%
- Predictions from Herwig++ have similar level of discrepancy.
- Madgraph+Pythia6 is the closest to the data. (typically 5-7%)



Four-jet Results

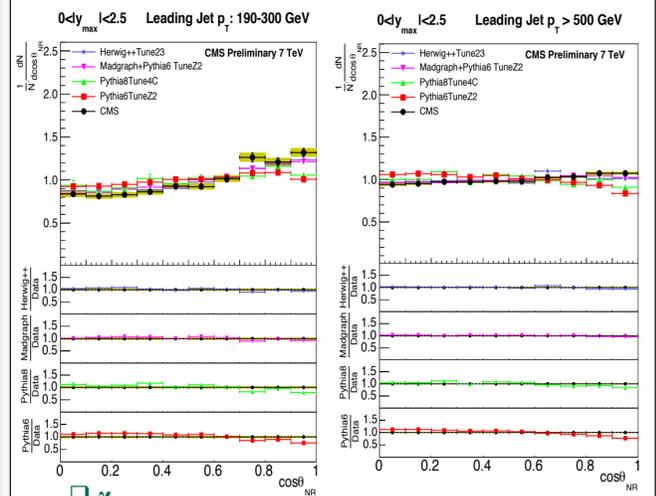
Invariant Mass

- Four-Jet invariant mass distribution is narrow and peaks around 500 GeV at the lowest p_T bin. It broadens and gets shifted to higher mass in higher p_T bins.
- Pythia6 and Herwig++ give better description of the data. The agreement gets better at higher p_T bins.
- Madgraph+Pythia6 also provides reasonable description of the data for $p_T > 300$ GeV



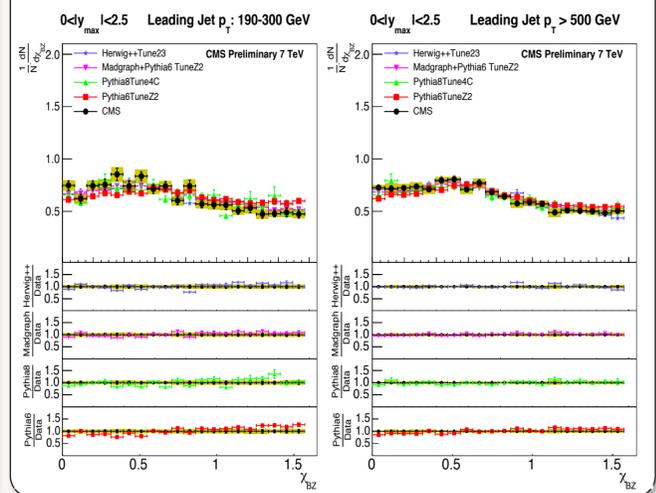
$\cos \theta_{NR}$

- Distribution of $\cos \theta_{NR}$ is rather flat at all p_T bins.
- Herwig++ provides a good description- mean deviation of the ratio from 1 is 3-8%.
- Madgraph+Pythia6 is also close to the data.



χ_{BZ}

- χ_{BZ} is plotted when the two leading (non-leading) jets are not back to back (angle $< 160^\circ$)
- Distribution is rather flat at all p_T bins.
- Madgraph+Pythia6 and Herwig++ are close to the data



Conclusions

- None of the models give satisfactory description of the data for all the variables (in different p_T bins)
- The difference can not be taken care of by changing the PDF's, model for underlying event or changing the Monte Carlo tunes.
- Madgraph+Pythia6 provides the best description among all the models tried.
- Missing higher orders are most likely the reason for the discrepancy.