

# P-odd and Naïve-T-odd asymmetries in W+jet production and top-decay processes

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R.Frederix, K.Hagiwara, T.Yamada & HY, arXiv:1407.1016,  
K.Hagiwara, K.Hikasa & HY, Phys.Rev.Lett. 97 (2006) 221802,  
K.Hagiwara, K.Mawatari & HY, JHEP 0712 (2010) 041.

ICHEP2014, Valencia, Spain, 7/2-9 (2014)

# Outline

1. Parity-odd and naïve-T-odd observables
2. PQCD prediction in hard processes
3. Observability at collider experiments  
[W+jet @LHC]
4. Summary

# Naïve-T-reversal, T-reversal and Parity reversal

- In this talk, I consider the following basic transformation which is related with time and parity reversal in quantum theory.

Naïve-T (  $\tilde{T}$ ,  $T_N$  ) :

$$(\vec{p}, \vec{s}) \rightarrow (-\vec{p}, -\vec{s}) \quad \tilde{T}|i(\vec{p}, \vec{s})\rangle = |\tilde{i}(-\vec{p}, -\vec{s})\rangle$$

$$T : (\vec{p}, \vec{s}) \rightarrow (-\vec{p}, -\vec{s}) \quad T|i(\vec{p}, \vec{s})\rangle = \langle \tilde{i}(-\vec{p}, -\vec{s})|$$

$$P : (\vec{p}, \vec{s}) \rightarrow (-\vec{p}, \vec{s})$$

- Without spins of particles, naïve-T- and parity-reversal behave as the same.

# Naïve-T-odd and Unitarity of S-matrix

De Rujula, Kaplan, De Rafael(71)

- Unitarity of S-matrix  $SS^\dagger = 1$   $S_{fi} = \delta_{fi} + i(2\pi)^4 \delta^4(P_f - P_i) T_{fi}$

$$T_{fi} - T_{if}^* = i A_{fi} \quad \text{where } A_{fi} = \sum_n T_{nf}^* T_{ni} (2\pi)^4 \delta^4(P_n - P_i)$$

absorptive part

gives  $|T_{fi}|^2 = |T_{if}|^2 - 2 \text{Im}(T_{if}^* A_{fi}) + |A_{fi}|^2$

- Naïve-T-odd quantity

subtract  $|T_{\tilde{f}\tilde{i}}|^2$

$$|T_{fi}|^2 - |T_{\tilde{f}\tilde{i}}|^2 = \underbrace{(|T_{if}|^2 - |T_{\tilde{f}\tilde{i}}|^2)}_{\text{Time-reversal violation}} - 2 \text{Im}(T_{fi}^* A_{fi}) - |A_{fi}|^2$$

Time-reversal violation

→ emerges from the absorptive parts of the scattering amplitude

# Absorptive part of scattering amplitudes

In perturbation theory, the absorptive part of scattering amplitudes can be calculated by the imaginary part of the loop amplitudes.

$$\int d\Phi_2 \left( \text{Diagram 1} \right) \left( \text{Diagram 2} \right)^* = \text{Cut Diagram} = \text{Im} \left( \text{Diagram 3} \right)$$

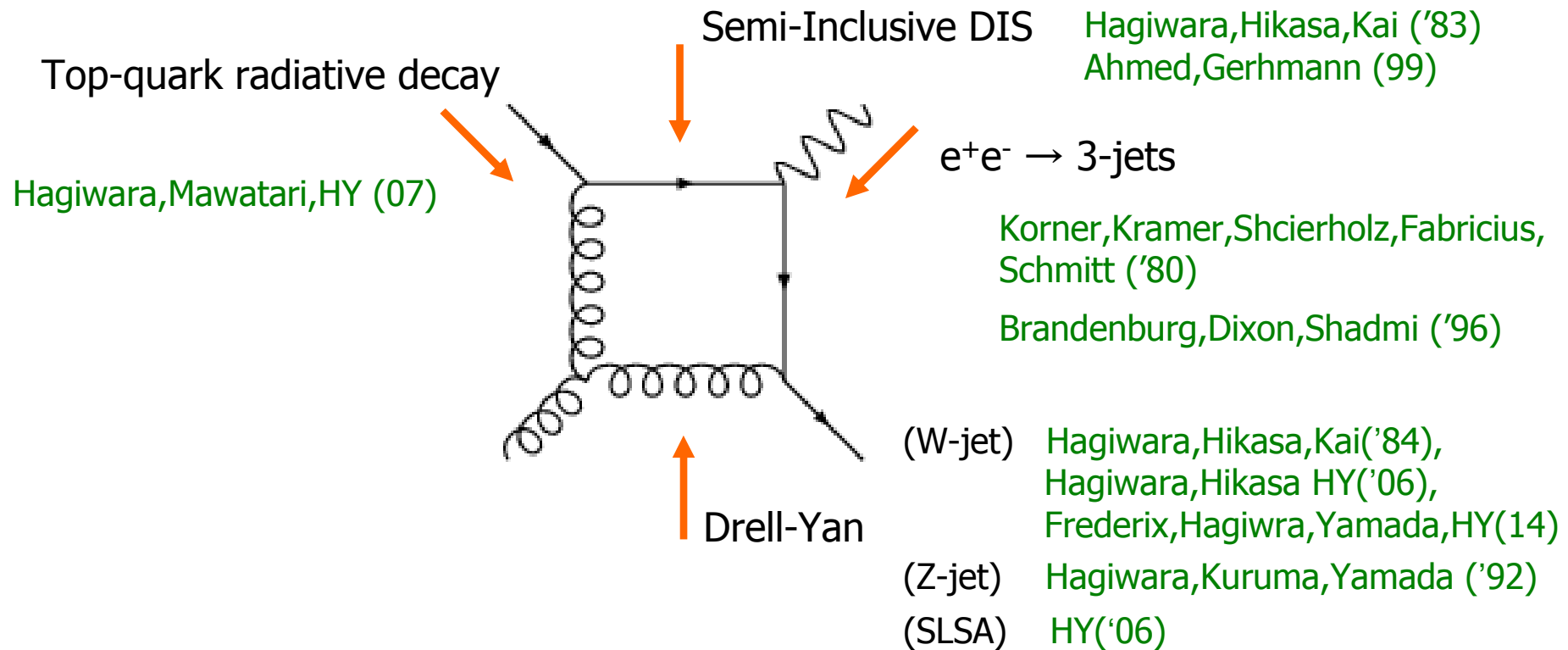
The diagrammatic equation illustrates the Cutkosky rule. On the left, the integral of the product of two diagrams over two-particle phase space is shown. The first diagram is a tree-level exchange with two incoming lines and two outgoing lines. The second diagram is a loop diagram with two incoming lines and two outgoing lines. The product is taken with the complex conjugate of the second diagram. This is equal to the imaginary part of a single loop diagram with a cut indicated by a dashed red line.

Cutkosky rule

Therefore, measurement of naïve-T-odd quantities can test the perturbative predictions for the imaginary part of scattering amplitudes; i.e. the scattering phase or the strong phase.

# pQCD prediction in hard processes

- Naïve-T-odd asymmetries in hard processes have been calculated in  $e^+e^- \rightarrow 3\text{jets}$ , Semi-Inclusive DIS, DY and top decay processes.

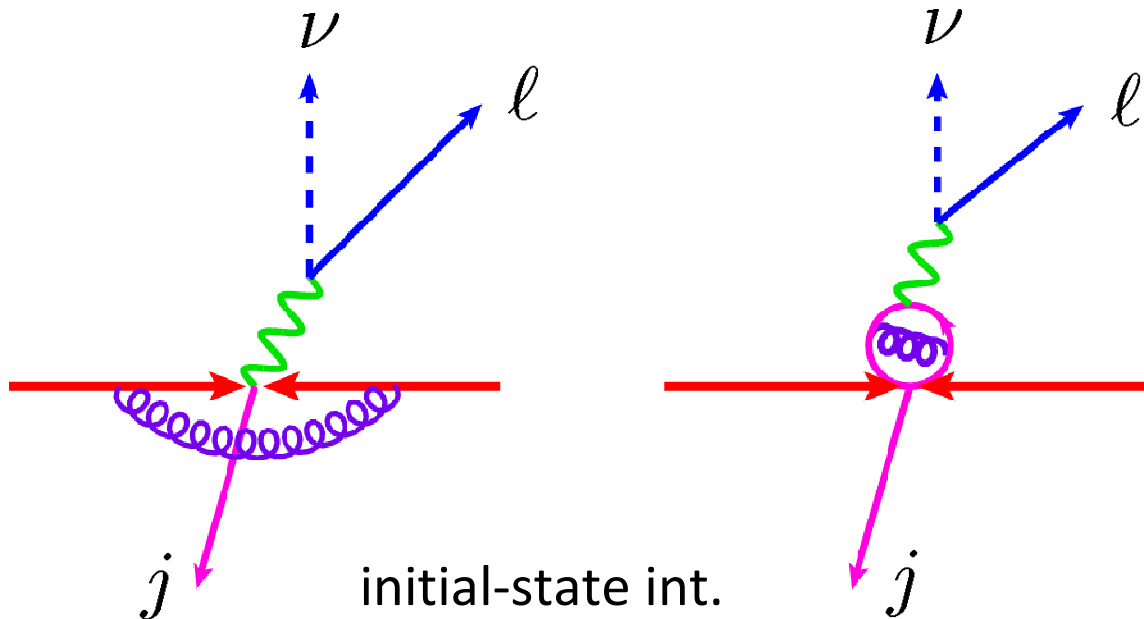


- So far, no experimental measurements for these asymmetries

# W+jet events, Top radiative decay at the LHC

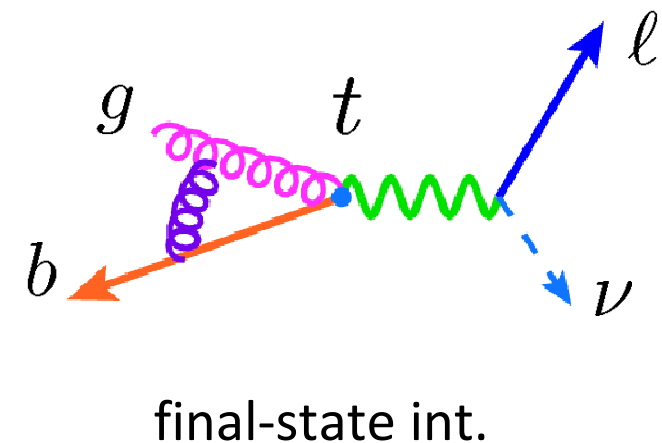
## W+jet:

- huge cross section  $\sim 10\text{nb}$
- simple event topology
- phases from initial-state int.



## Top-quark radiative decay:

- large cross section  $\sim 0.2\text{nb}$
- additional jet radiation
- complicated event topology
- phases from final-state int.



# W+jet : Lepton Angular Distributions

$$\begin{aligned}
 \frac{d^4\sigma}{dq_T^2 d\cos\hat{\theta} d\cos\theta d\phi} = & F_1(1 + \cos^2\theta) + F_2(1 - 3\cos\theta^2) + F_3 \sin 2\theta \cos\phi \\
 & + F_4 \sin^2\theta \cos 2\phi + F_5 \cos\theta + F_6 \sin\theta \cos\phi \\
 & + F_7 \sin\theta \sin\phi + F_8 \sin 2\theta \sin\phi + F_9 \sin^2\theta \sin 2\phi
 \end{aligned}$$

$\left. \begin{array}{l} \text{P-even} \\ \text{P-odd} \end{array} \right\}$

$$P : \phi \rightarrow -\phi$$

$q_T$ : transverse momentum of W boson

$\cos\hat{\theta}$ : scattering angle

$\theta, \phi$ : lepton decay angles in W-rest frame

$F_{1-9}(q_T, \cos\hat{\theta})$  : structure functions

**P-even :  $F_{1\sim 6}$**

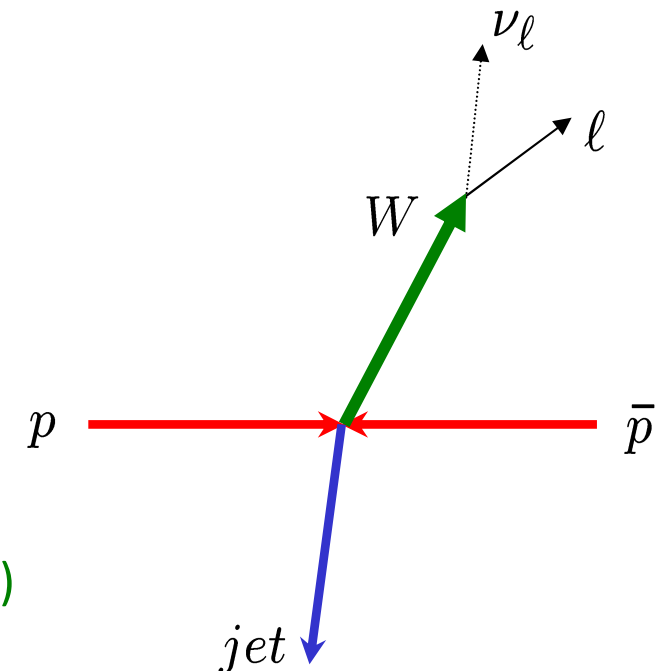
LO (Born): Chaichian et.al.('82)

NLO (one-loop): Mirkes('92)

**P-odd :  $F_{7\sim 9}$**

LO (one-loop): Hagiwara, Hikasa, Kai('84)

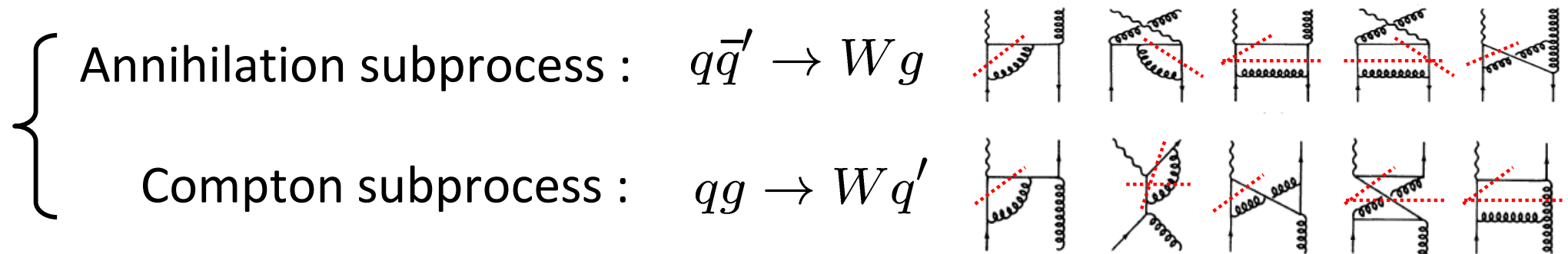
NLO: not known yet





# W+jet : pQCD prediction at one-loop level

Hagiwara, Hikasa, Kai('84)

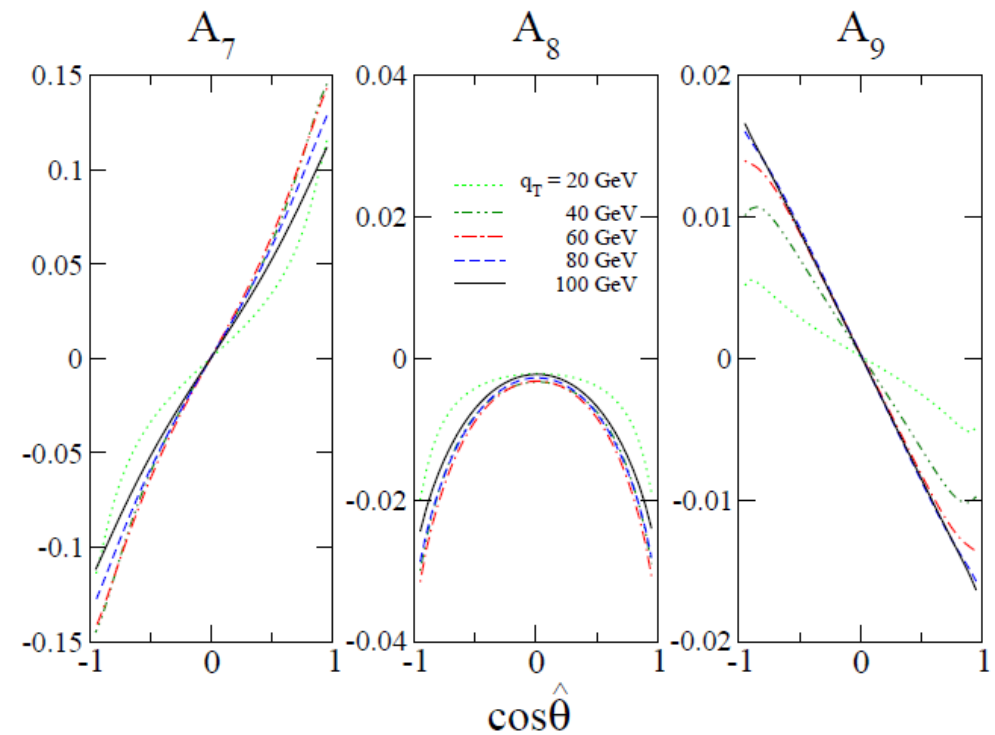


- Partonic asymmetry at the LHC

$$A_i(q_T^2, \cos \hat{\theta}) = F_i / F_1 \text{ for } i = 7, 8, 9$$

$pp, \sqrt{S} = 8 \text{ TeV}$  with CTEQ6M

in Collins-Soper frame  
 $A_7 \sim 10\text{-}15\%$   
 $A_8 \sim \text{a few } \%$   
 $A_9 \sim \text{a few } \%$



# W+jet : Measurement at the Tevatron and LHC

- In W+jet events, some of **P-even distributions** have been measured by CDF in Run-I.

→ agree with pQCD (NLO) within errors.

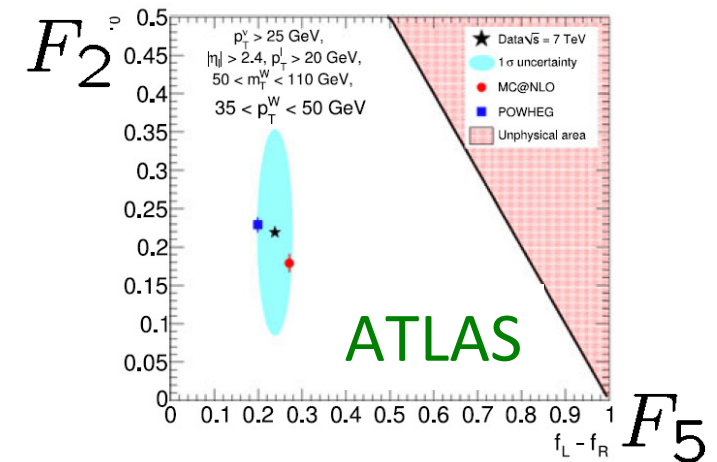
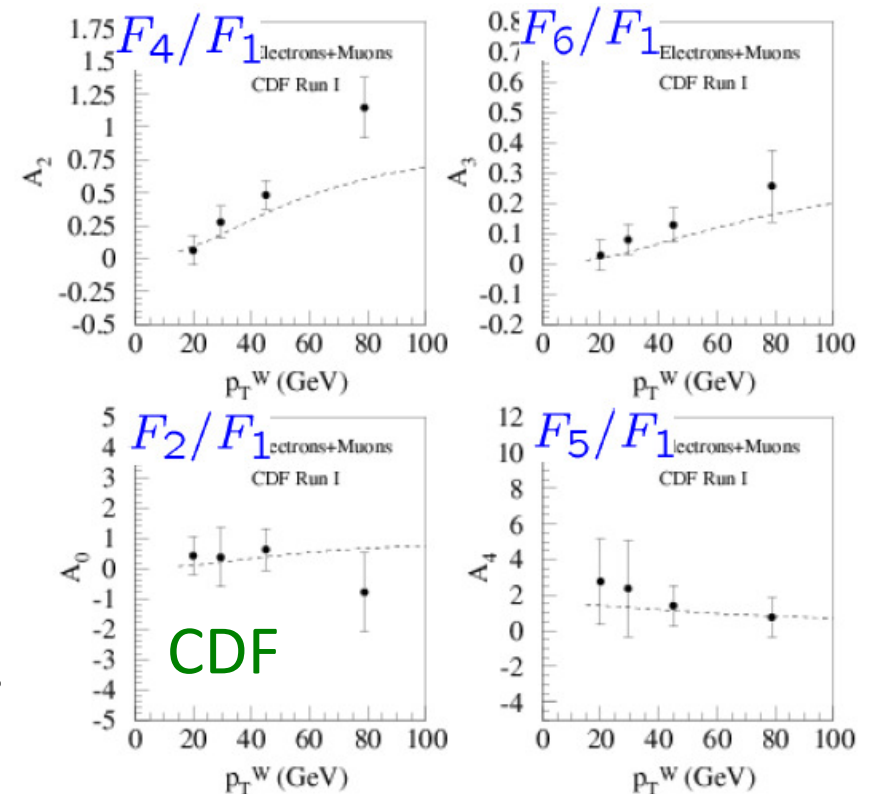
- At the LHC, only polar angular distributions has been measured, so far.

→ only helicity fraction of W-boson.  
no azimuthal angle,  
no interference of different helicity states.

- **P-odd distributions** have not been measured at all.

Frederix,Hagiwara,Yamada,HY(14)

- The aim of our study is to revisit the P-odd distribution in W+jet events at the LHC, and demonstrate its observability by using the NLO MC generator and fast detector simulation.



# Simulation study beyond the Born level

Frederix, Hagiwara, Yamada, HY(14)

- (NLO) Event Generator which handle the parity-odd distributions

{	<b>MG5_aMC@NLO</b> (automatic, multipurpose)	One-loop level ME, NLO matching with PS (NLO for P-even, LO for P-odd)
	<b>LO MC</b> (handmade, W+jet only)	LO for all $F_{1-9}$ , LO matching with PS

$$\text{P-even: } F_{1-6} \propto \alpha_s \sigma_0 + \alpha_s^2 \sigma_1 + \dots$$

$$\text{P-odd: } F_{7-9} \propto \alpha_s^2 \Delta \sigma_0 + \dots$$

Born

one-loop

→ HERWIG/PYTHIA + PGS/Delphes

to study QCD ISR/FSR and detector resolution effects.

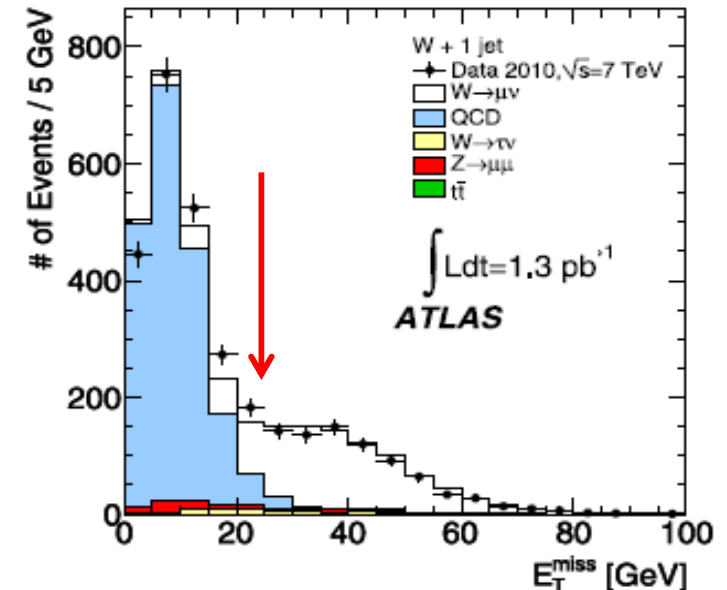
# Event selection and extraction of the P-odd term

- Huge  $W(\rightarrow l\nu)+\text{jet}$  cross section :  $O(1)$  nb
- Selection cuts:
 

$p_T^\mu > 25$ GeV, $ \eta_\mu  < 2.5$ :	0.94 nb
$E_T > 25$ GeV :	0.75 nb
$Q_T > 30$ GeV :	0.29 nb
$M_T^W > 60$ GeV :	0.29 nb
$p_T^j > 30$ GeV, $ \eta_j  < 5$ :	0.13 nb

$$0.13 \text{ nb} \times 20 \text{ fb}^{-1} = 2.6 \times 10^6 \text{ events}$$

- Background : QCD,  $Z \rightarrow \mu^+\mu^-$ ,  
 $W^+ \rightarrow \tau^+\nu_\tau$   
 $< 10\%$  level



- Extraction of the  $\mathbf{F}_7$  distribution

$$\sin \theta \sin \phi = p_\ell^\perp / (m_W/2) \quad \begin{array}{l} \text{lepton momentum component} \\ \text{perpendicular to the scattering plane} \end{array}$$

→ left-right asymmetry wrt. scatt. plane

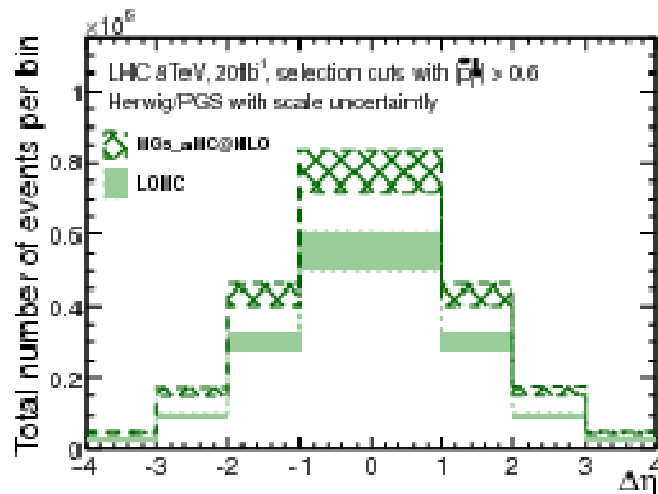
$$\cos \hat{\theta}$$

suffered from the two-fold ambiguity.

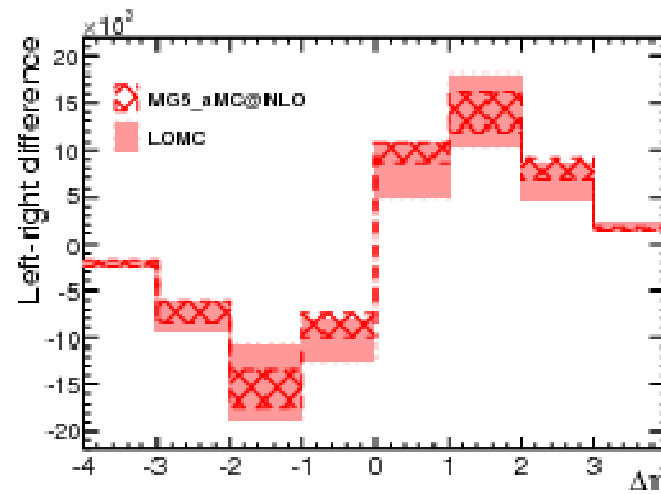
Instead, we propose to use  $\Delta\eta = \eta_\ell - \eta_{jet}$

# Results : MG5\_aMC@NLO vs. LOMC

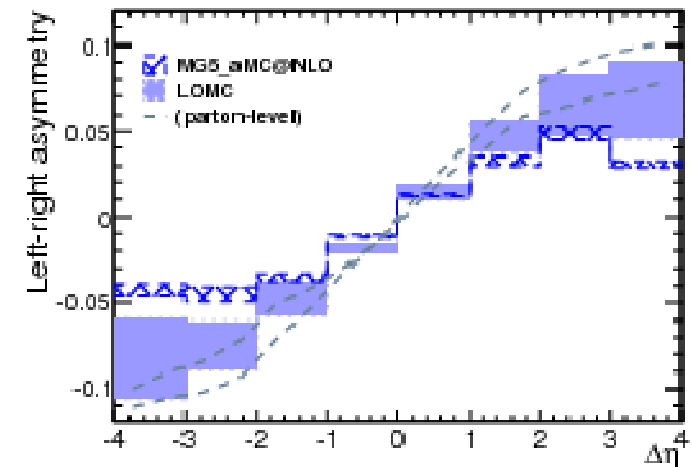
- $\Delta\eta$  ( $=\eta_l - \eta_j$ ) distributions [detector sim. by using HERWIG/PGS]



$$\sigma(p_\ell^\perp > 0) + \sigma(p_\ell^\perp < 0)$$



$$\sigma(p_\ell^\perp > 0) - \sigma(p_\ell^\perp < 0)$$



Asymmetry

- P-odd cross-section unchanged  $\rightarrow$  consistent with the order of calculation.
- Reduction of the asymmetry in MG5\_aMC@NLO,  
due to the K-factor ( $\sim 1.5 - 2$ ) in the denominator (total cross-section).
- Scale uncertainty is largely reduced in MG5\_aMC@NLO ( NLO matching with PS! )
- (Small) detector smearing by misidentifying hard jet from ISR/FSR jets.

# Prospects for the naïve-T-odd asymmetries

- At the LHC,
  - **W plus 1-jet event** is promising !  
one-loop analytic calc. is known, experimentally simple.
  - **Top-quark radiative decay**:  
one-loop analytic calc. also known,  
experimentally challenging (boosted top, subjet structure,,,) )
  - **W plus 2-jets / Z /  $\gamma$  ,,, :**  
analytic calc. not known, but now we have MG5\_aMC@NLO !!  
measurements at the 14TeV run will be interesting.
- At the ILC,
  - **Top-quark radiative decay** can be measured in a clean environment.
  - **Z  $\rightarrow$  3-jets decay** handedness may be measured, e.g. at the Giga-Z factory.

# Summary

- **Naïve-T-odd asymmetry** emerges from the **absorptive part** of scattering amplitudes. In **hard processes**, it can be predicted by perturbation calculation, and comparison with experimental measurement would be an interesting test.
- We study the naïve-T-odd (P-odd) asymmetry in W+jet production at the LHC, using the NLO-EG **MG5\_aMC@NLO**: QCD PS and detector effects for the measurement are estimated, and theoretical uncertainties by scale variation and due to the lack of NLO P-odd distributions are argued.
- If observed, it will be a first confirmation of the imaginary part of scattering amplitudes at the one-loop level.





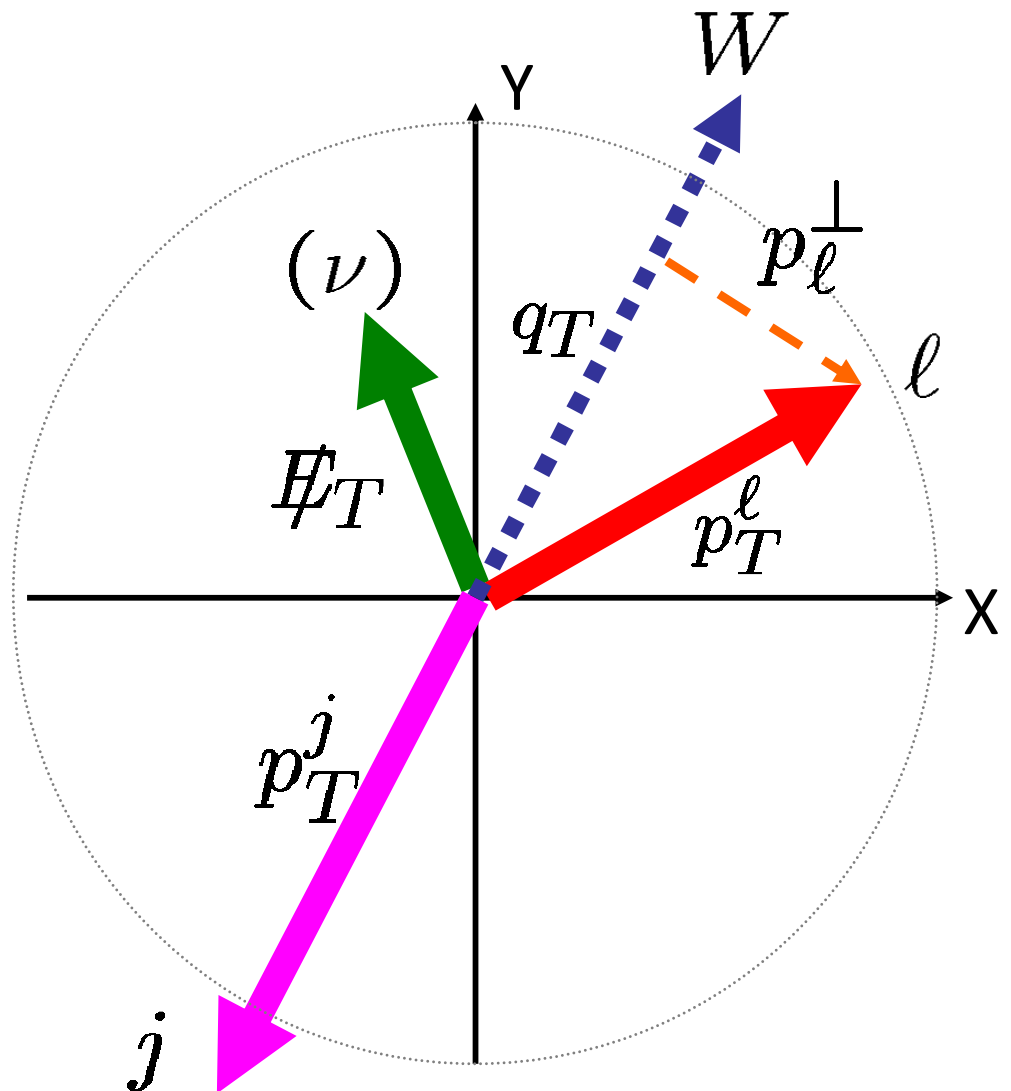
# Measurement at collider experiments

- Events display in the transverse plane

$(p^y)_l$  is invariant under the Lorentz Boost from lab. frame to the W-rest frame

$$\begin{aligned} p_\ell^\perp &= p_y^\ell (W \text{ rest - frame}) \\ &= \frac{m_W}{2} \sin \theta \sin \phi \end{aligned}$$

Missing  $E_T$  resolution may be crucial for the accuracy of  $(p^l)_y$  measurement



# One-loop calculation

Origin of the imaginary part in the loop (Feynman) integrals;

$$\left\{ \begin{array}{l} \log(x - i\epsilon) \rightarrow -i\pi \theta(-x) \\ \text{Li}_2(x - i\epsilon) \rightarrow i\pi \ln(x) \theta(x - 1) \end{array} \right. \quad \frac{1}{\Delta - i\epsilon} \rightarrow \text{P} \frac{1}{\Delta} + i\pi \delta(\Delta)$$

in the integrand

Methods of calculation;

1. Analytic calculation by standard **Feynman parameter integrals**
2. Express by **loop scalar functions** and use the fortran code “FF”

Passarino, Veltman ('79), Oldenborgh ('91)

- **IR divergences** are regulated by using gluon mass scheme or DR.
- Check of the results by the gauge invariance

# $\tilde{T}$ -odd asymmetry in hadron physics

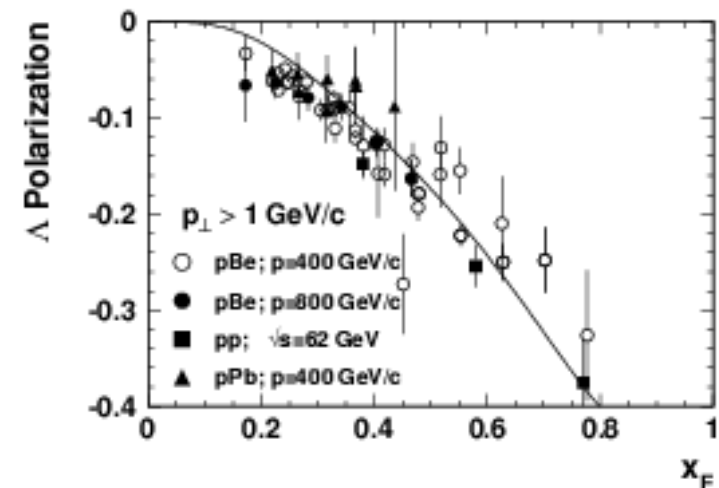
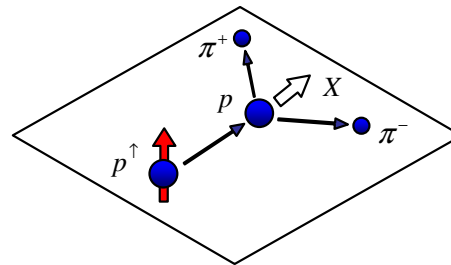
(P-even, pure QCD effect)

- Large  $\tilde{T}$ -odd asymmetries have been observed in hadron spin physics

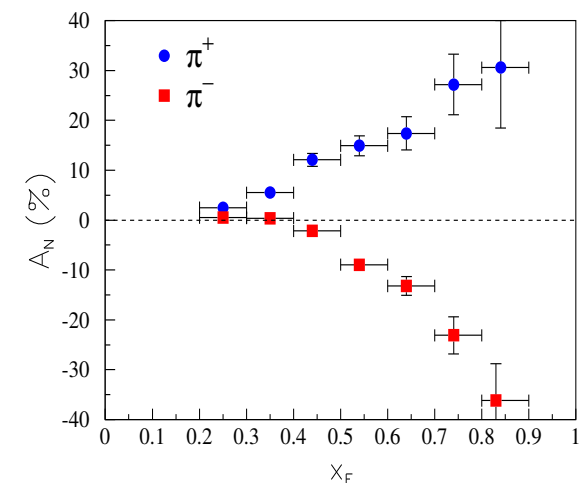
1.  $\Lambda$ -polarization  $\sim \langle \vec{p}_p \times \vec{p}_\Lambda \cdot \vec{s}_\Lambda \rangle$   
in  $p + N \rightarrow \Lambda^\uparrow + X$

2.  $A_N$  in  $p + p^\uparrow \rightarrow \pi + X$

$$A_N = \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow} \sim \langle \vec{p}_p \times \vec{s}_p \cdot \vec{p}_\pi \rangle$$



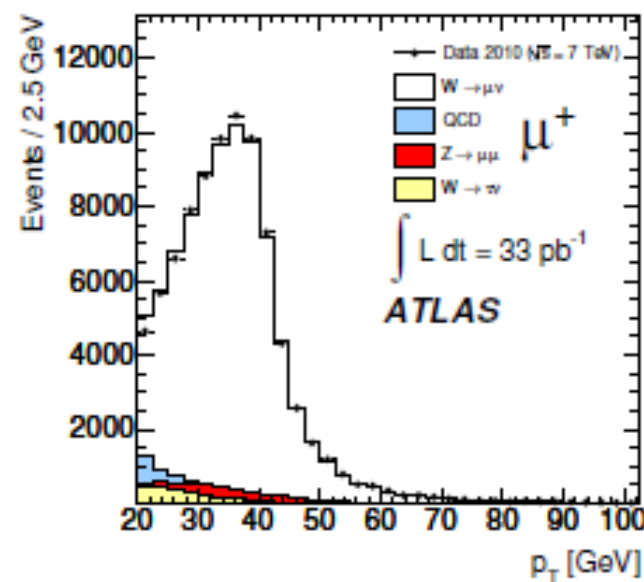
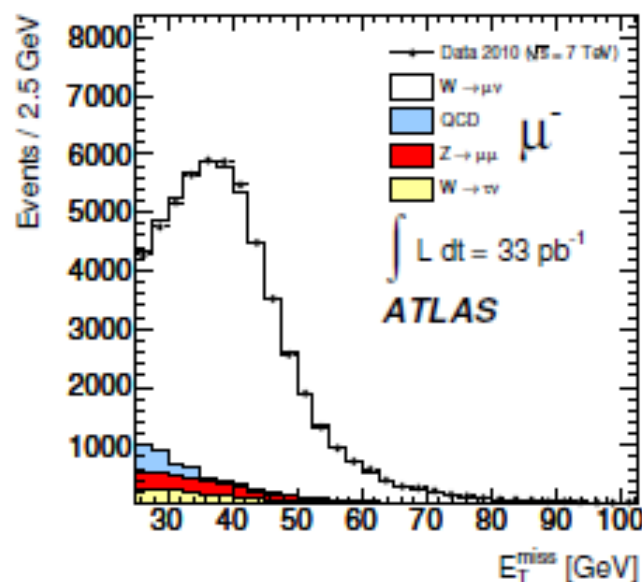
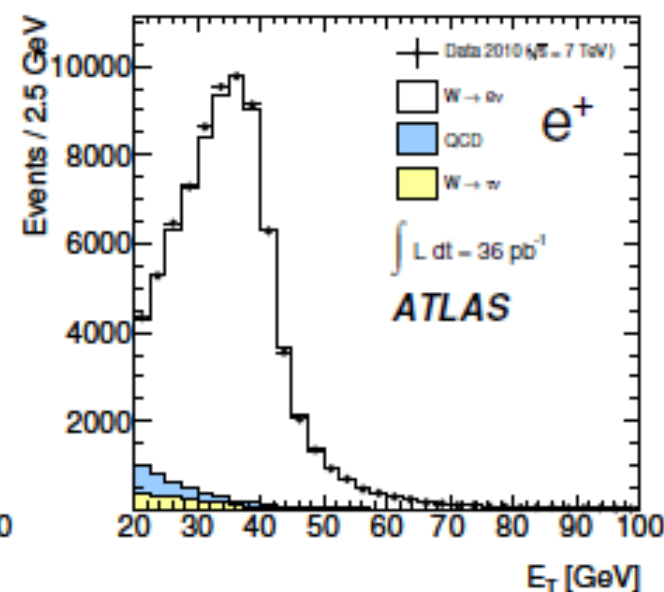
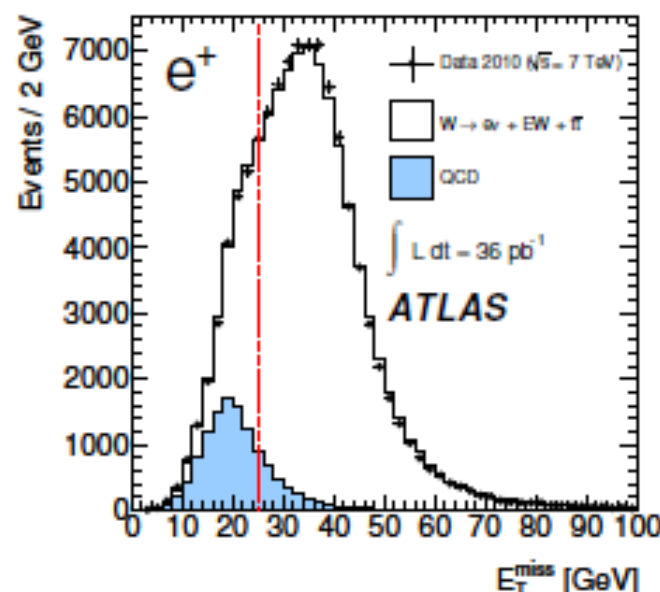
FNAL-E704:



- STSA needs **chirality-flip** amplitude, in addition to the **complex phase**
- Non-perturbative QCD effects inside nucleon
  - Transverse-momentum-dependent PDF
  - Higher-twist effects

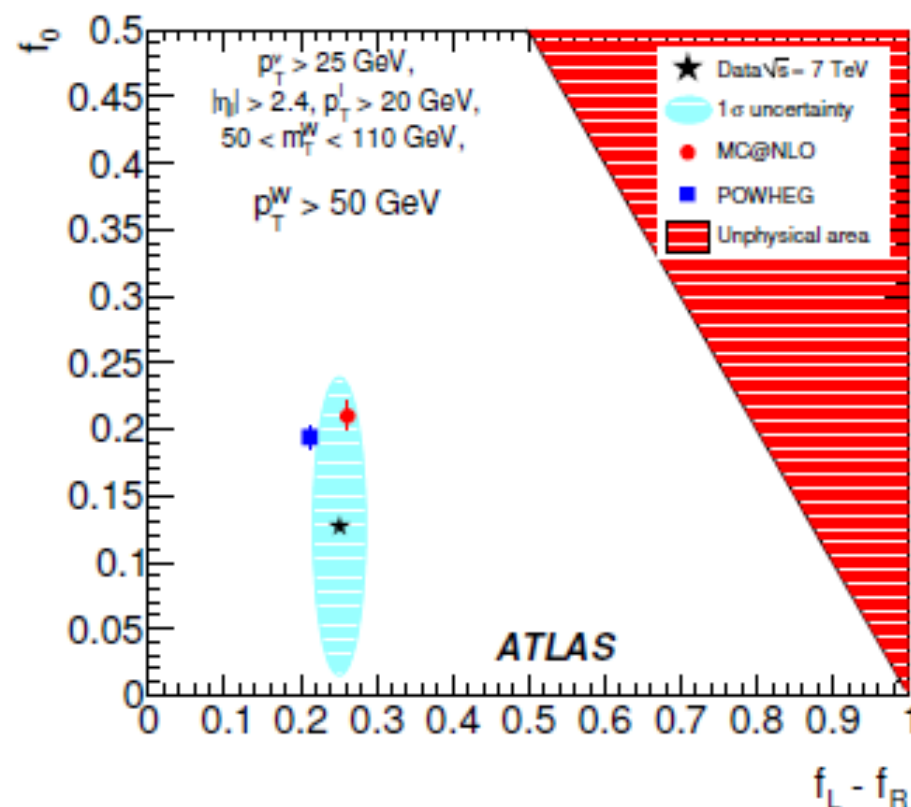
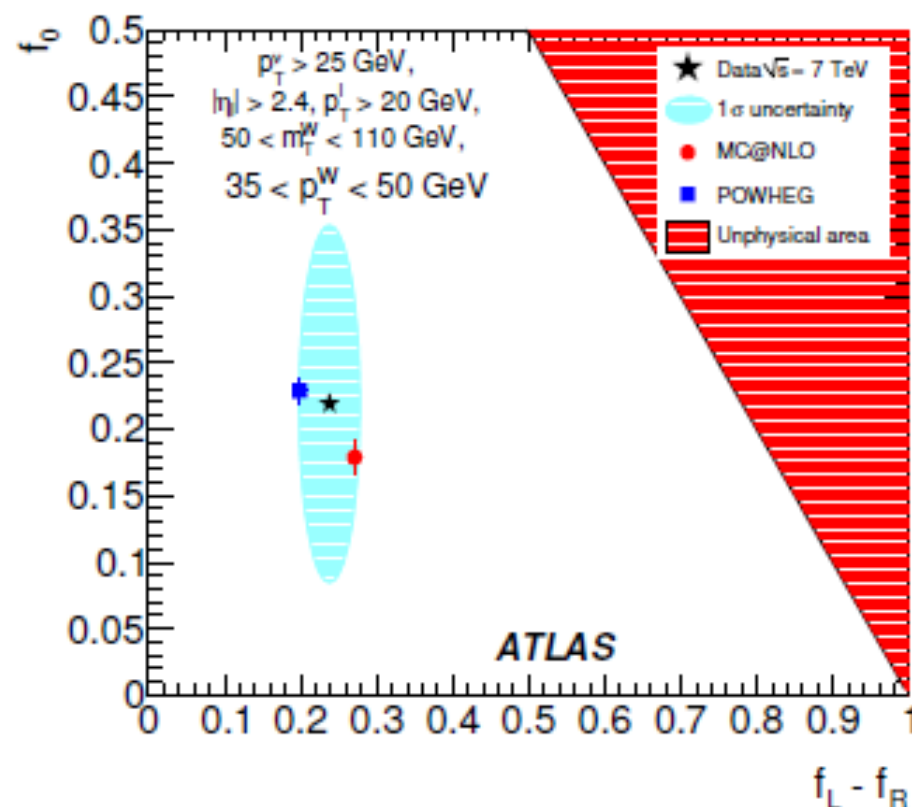
# $W \rightarrow \ell \nu$ selection

- ★ Single lepton triggers with high efficiency
- ★  $p_{T,\ell} > 20 \text{ GeV}$   
 $|\eta_e| < 2.47, |\eta_\mu| < 2.4$   
 (elec. excl. calo crack)  
 isolated leptons  
 $E_T^{\text{miss}} > 25 \text{ GeV}$   
 $m_T > 40 \text{ GeV}$
- ★ QCD from data fitting  
 $E_T^{\text{miss}}$  (e) and studying control regions in  $iso - E_T^{\text{miss}}$  plane ( $\mu$ )
- ★ 131 – 140 K candidates with 7 – 9 % background



# W polarization at high $p_T$

- ★ Helicity fractions,  $f_0$  and  $f_L - f_R$ , measured from angular distribution in transverse plane:  $\cos\theta_{2D} = \vec{p}_T^{\ell^*} \cdot \vec{p}_T^W / |\vec{p}_T^{\ell^*}| |\vec{p}_T^W|$
- ✓ Measurements done for  $35 < p_T^W < 50 \text{ GeV}$  and  $p_T^W > 50 \text{ GeV}$  regions



- ★  $f_L - f_R$  measured with 12–14% syst. uncertainty, dominated by hadronic recoil scale uncertainty (statistical uncertainty in 6–8% range)
- ★ Results compared to NLO QCD predictions from MC@NLO, POWHEG MCs

# Parity-odd asymmetries

$$A_i(q_T^2, \cos \hat{\theta}) = F_i / F_1 \text{ for } i = 7, 8, 9$$

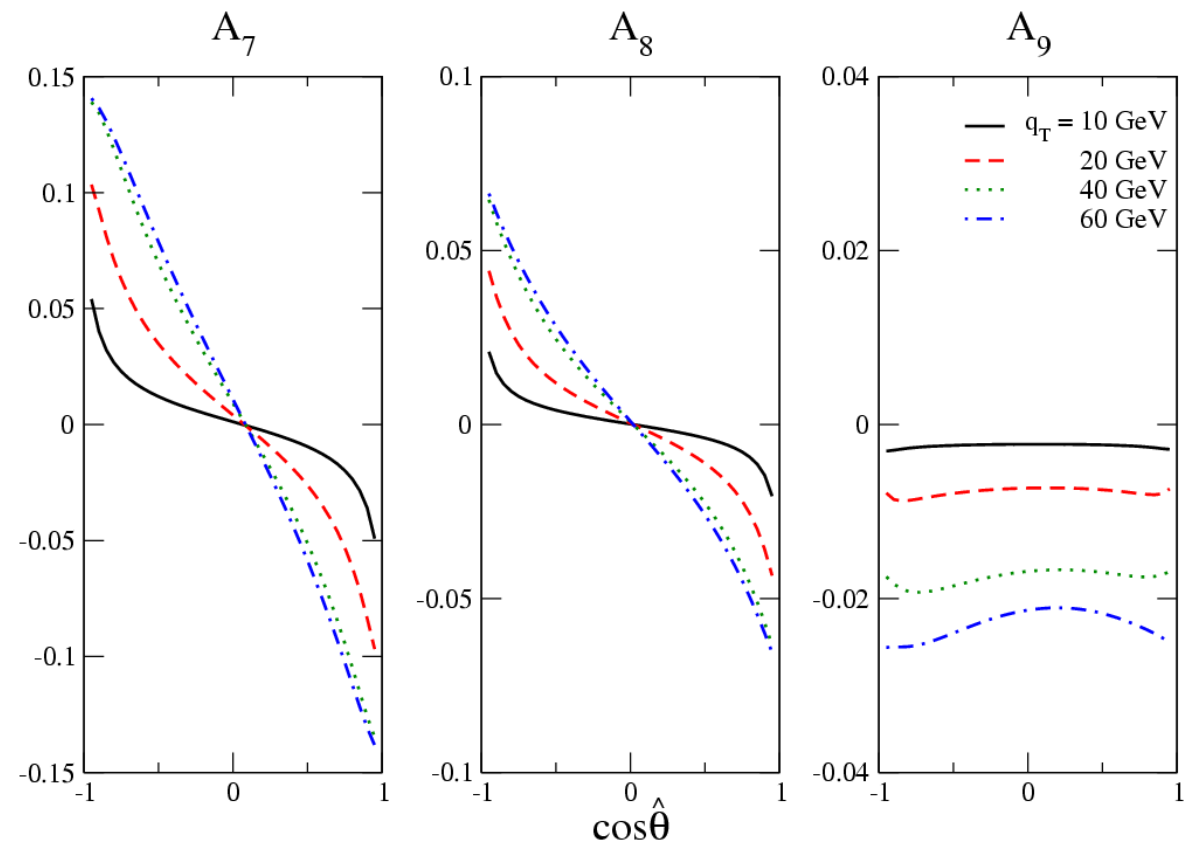
Tevatron

$p\bar{p}$ ,  $\sqrt{S} = 1.96$  TeV  
with CTEQ6M

$A_7 \sim 5\text{-}15\%$ ,

$A_8 \sim \text{a few to } 5\%$ ,

$A_9 \sim \text{a few } \%$



$\sin \theta \sin \phi$

$\sin 2\theta \sin \phi$

$\sin^2 \theta \sin 2\phi$

# Measurement at Tevatron

Hagiwara, Hikasa, HY (06)

- Left-right asymmetry  $\longleftrightarrow A_7$

$$A_{LR}(\Delta\eta, q_T) = [N(p_y^\ell > 0) - N(p_y^\ell < 0)]/N_{sum}$$

$\sim 5\%$  at large  $\Delta\eta$

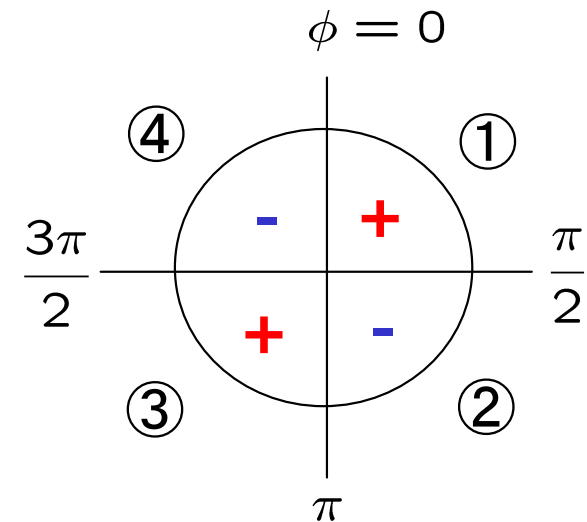
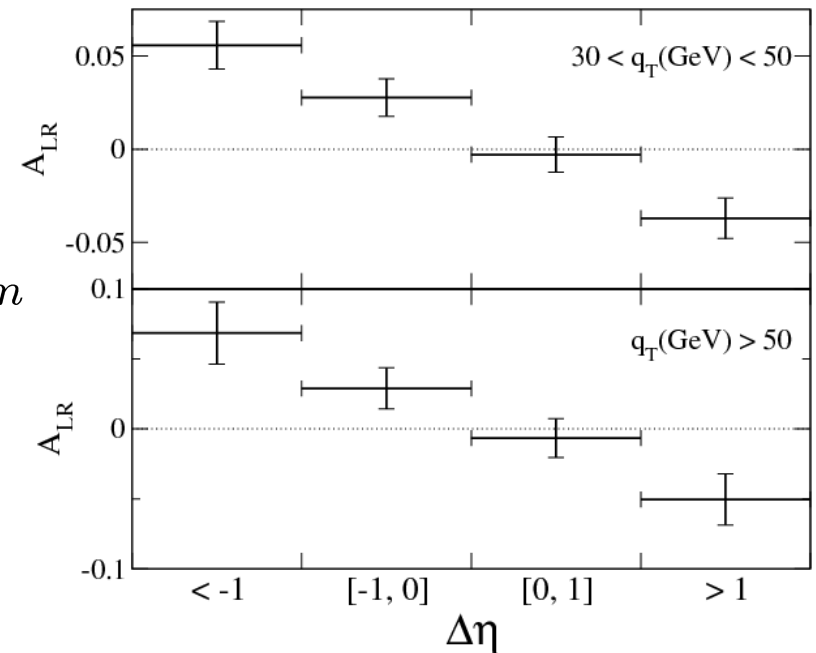
more than  $5\sigma$  deviation  
from zero-asymmetry is expected

- $\text{sign}(\sin 2\varphi)$  asymmetry  $\longleftrightarrow A_9$

$$A_Q = [\textcircled{1} - \textcircled{2} + \textcircled{3} - \textcircled{4}]/N_{sum}$$

$$\sim -0.9\% \pm 0.5 \text{ (} 2\sigma \text{)}$$

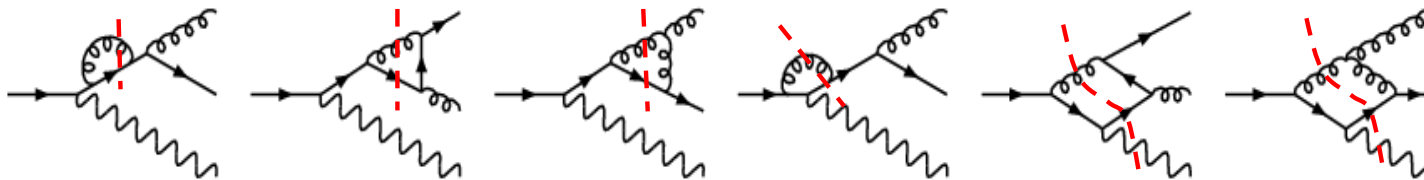
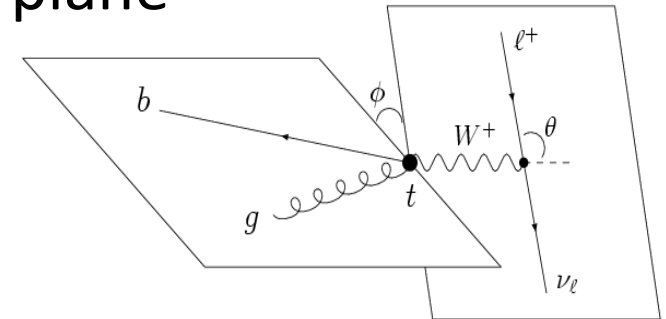
(combining all  $\Delta\eta$  and  $q_T$ )



# Top-quark radiative decay at one-loop level

- Extra radiation is required to define the decay plane

- One-loop diagrams for the absorptive part:



- Lepton angular distributions:

$$\frac{d\Gamma}{dz_1 dz_2 d\cos\theta d\phi} = K \sum_{\lambda, \lambda'} H_{\lambda\lambda'}(z_1, z_2) L_{\lambda\lambda'}(\theta, \phi)$$

$$= K \left[ F_1(1 + \cos^2\theta) + F_2(1 - 3\cos^2\theta) + F_3 \sin 2\theta \cos\phi + F_4 \sin^2\theta \cos 2\phi \right. \\ \left. + F_5 \cos\theta + F_6 \sin\theta \cos\phi + F_7 \sin\theta \sin\phi + F_8 \sin 2\theta \sin\phi + F_9 \sin^2\theta \sin 2\phi \right]$$

