



Scintillation Detectors

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Scintillation detector:



- Simple
- Versatile
- Rugged
- Cheap

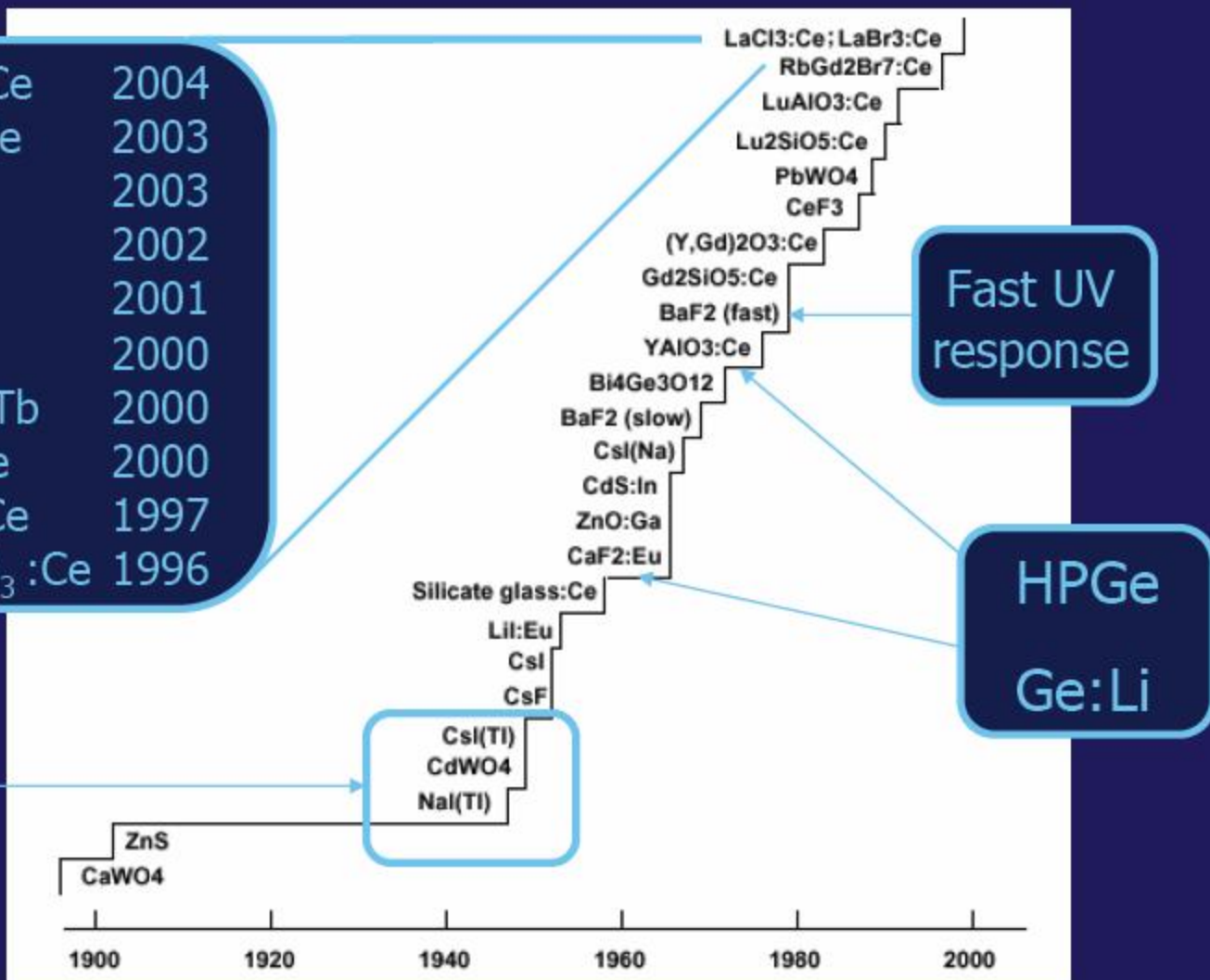


History:

- Crookes (1903): ZnS screen + microscope
- Regener, Crookes (1908): nature of α -particles . + Rutherford, Geiger (gas counter)
- Geiger, Marsden (1909): angular distribution of scattered α -particles
- Rutherford (1911): discovery of atomic nucleus
- Rutherford (1919): discovery of nuclear reactions, $^{14}\text{N}(\alpha, p)^{17}\text{O}$
- Cockcroft, Walton (1932): coincidence experiment, $^7\text{Li}(p, \alpha)\alpha$
- Krebs (1941): photo-sensitive Geiger-Muller counter
- Curran, Baker (1944): use of photomultiplier + scintillator(ZnS)
- Kallman (1947): first organic scintillator (naphthalene)
- Hofstadter (1948): NaI(Tl)
- several (1980' s): BGO
- Laval (1983): fast component of BaF_2
- several (1990' s): many new scintillation materials

$\text{Rb}_2\text{LiYBr}_6:\text{Ce}$	2004
$\text{Cs}_2\text{LiYCl}_6:\text{Ce}$	2003
$\text{LuI}_3:\text{Ce}$	2003
$\text{K}_2\text{LaI}_5:\text{Ce}$	2002
$\text{LaBr}_3:\text{Ce}$	2001
$\text{LaCl}_3:\text{Ce}$	2000
$\text{Lu}_2\text{O}_3:\text{Eu, Tb}$	2000
$\text{Lu}_2\text{Si}_2\text{O}_7:\text{Ce}$	2000
$\text{RbGd}_2\text{Br}_7:\text{Ce}$	1997
$^6\text{Li}_6\text{Gd}(\text{BO}_3)_3:\text{Ce}$	1996

Invention of the
photomultiplier tube



Scintillation materials

Luminescent materials: reemit part of the absorbed energy in the form of light

Emissions: fluorescence (prompt), delayed fluorescence and phosphorescence (delayed, different wavelength)

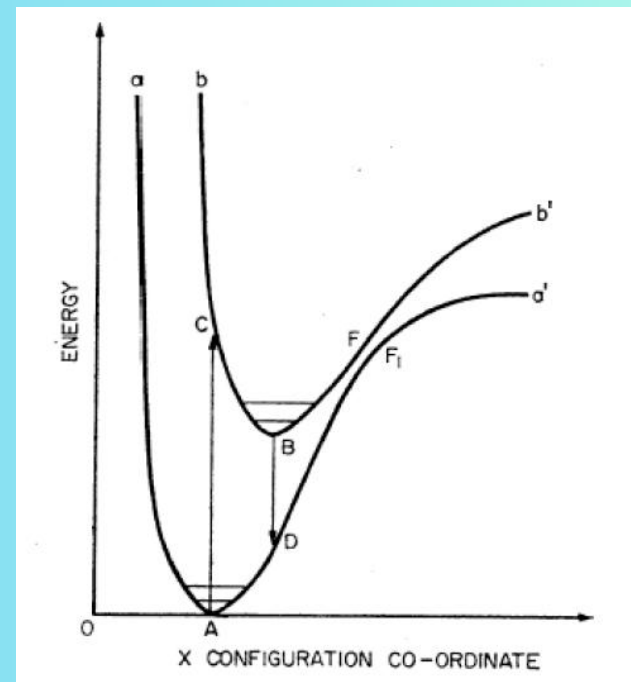
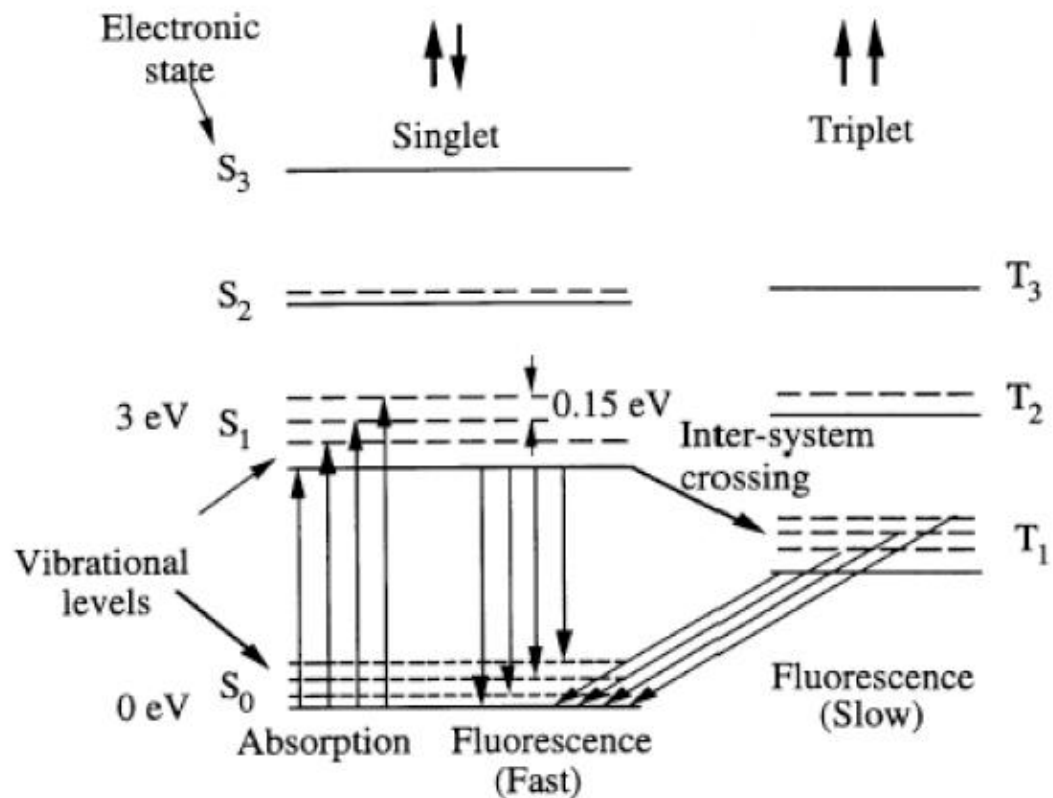
Scintillation material properties:

- transparency to its fluorescence
- luminous efficiency
- light spectral distribution
- light temporal distribution
- mechanical and chemical properties



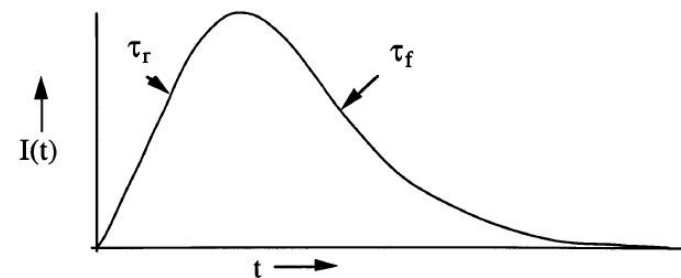
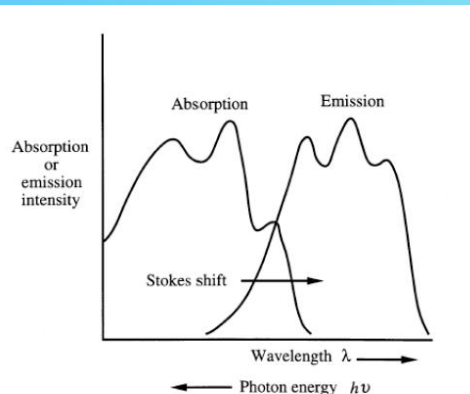
- Organic materials:
 - Crystals
 - Liquids
 - Plastics
- Inorganic crystals
- Glasses
- Gasses

Luminescence in organic materials

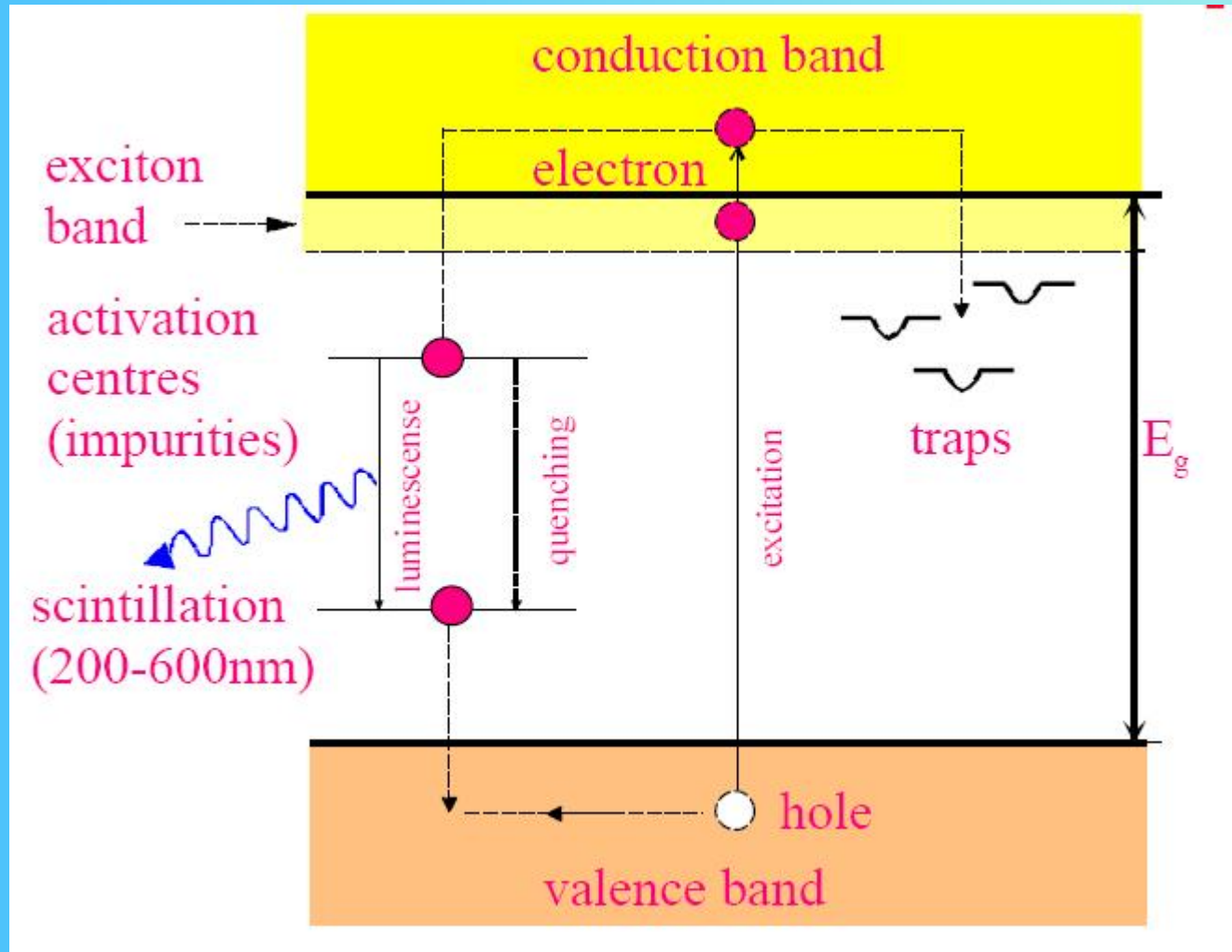


Several time components

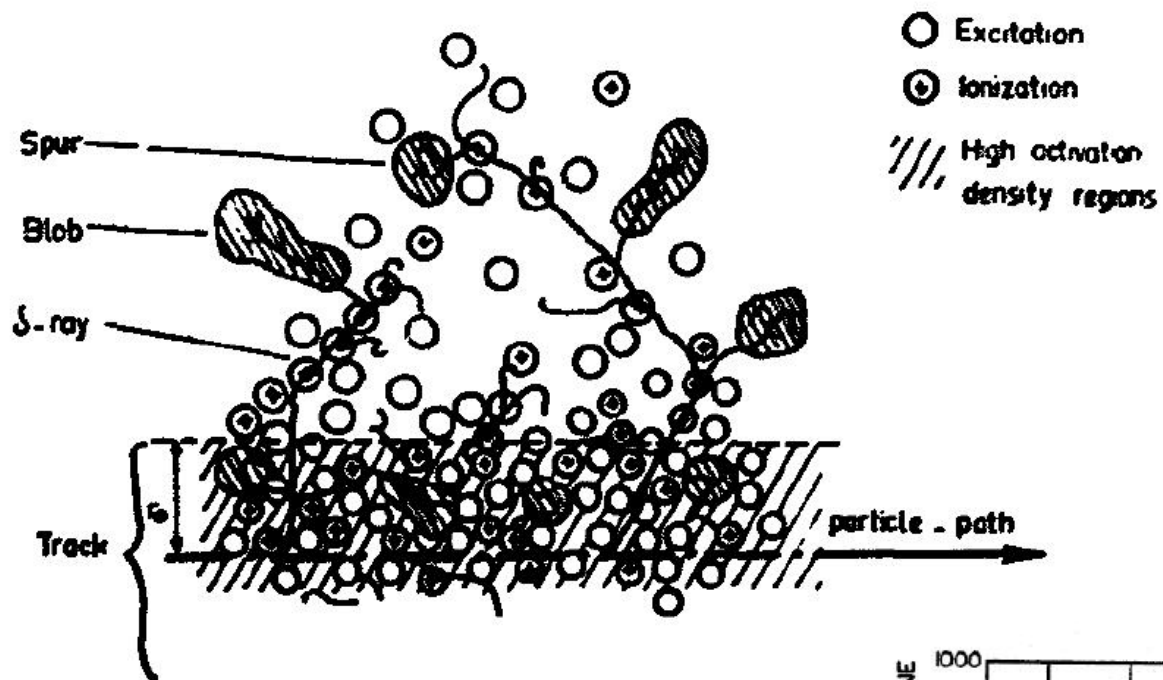
Material transparent to its own light



Luminescence in inorganic materials



Several mechanisms have been identified: luminescence of doping centers, self-activated luminescence and cross-luminescence

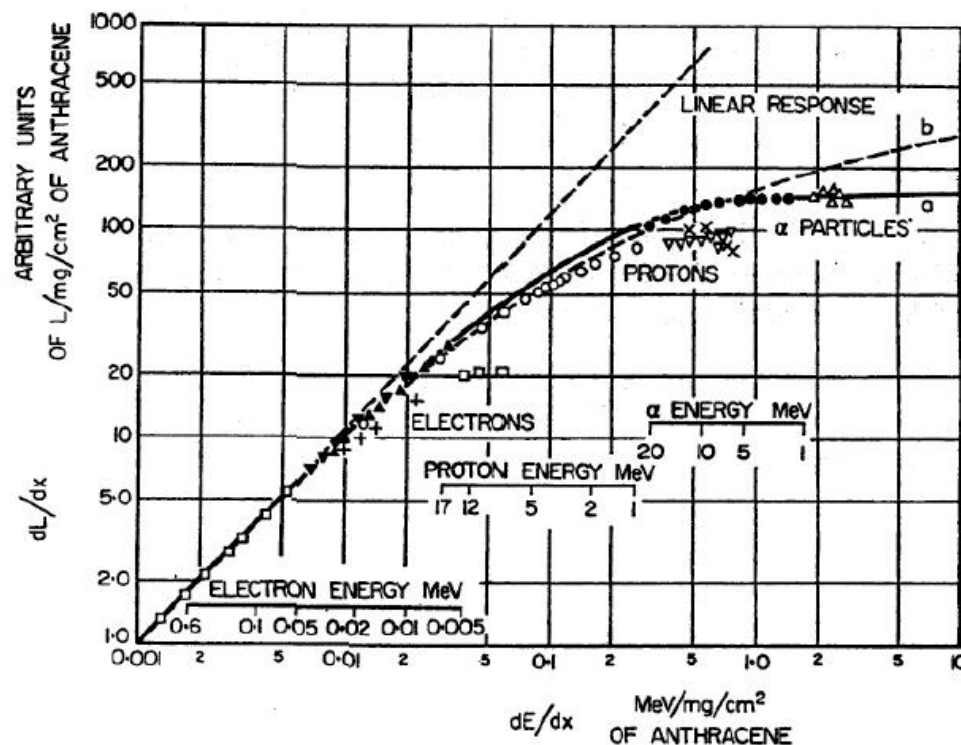


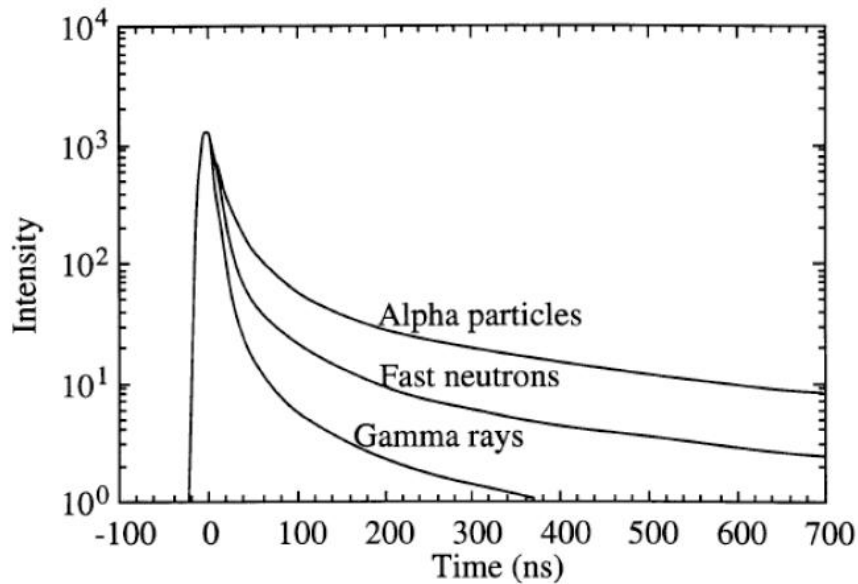
The non-radiative transfer mechanism between excited centers induces an energy-loss dependent light production

Simple parameterization:

$$\frac{dL}{dx} = \frac{A \frac{dE}{dx}}{1 + B \frac{dE}{dx}}$$

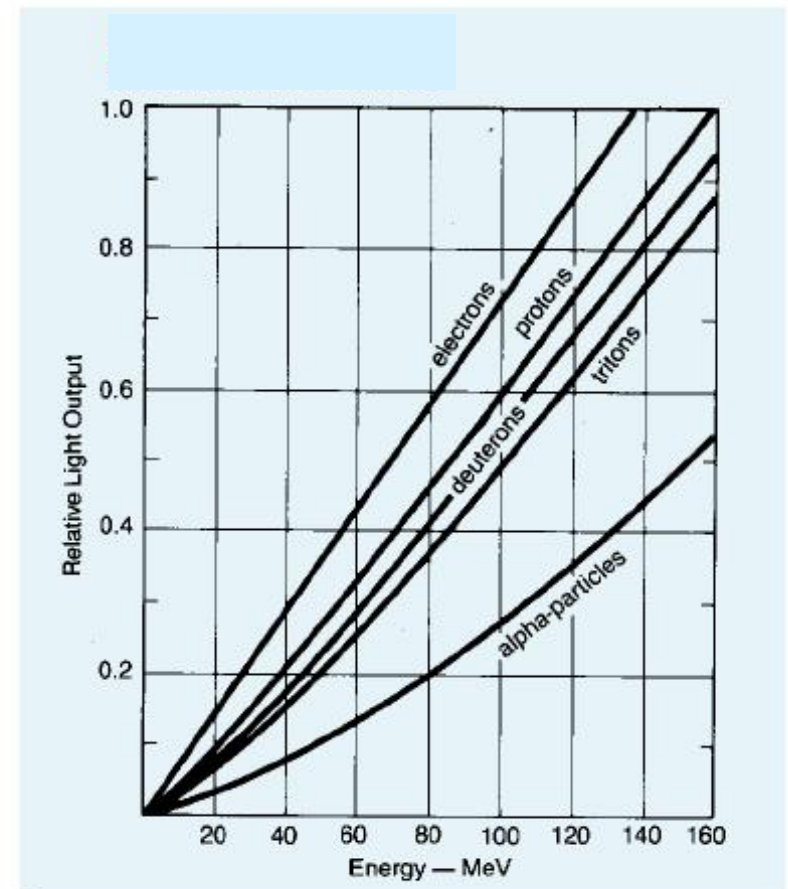
Birk's formula

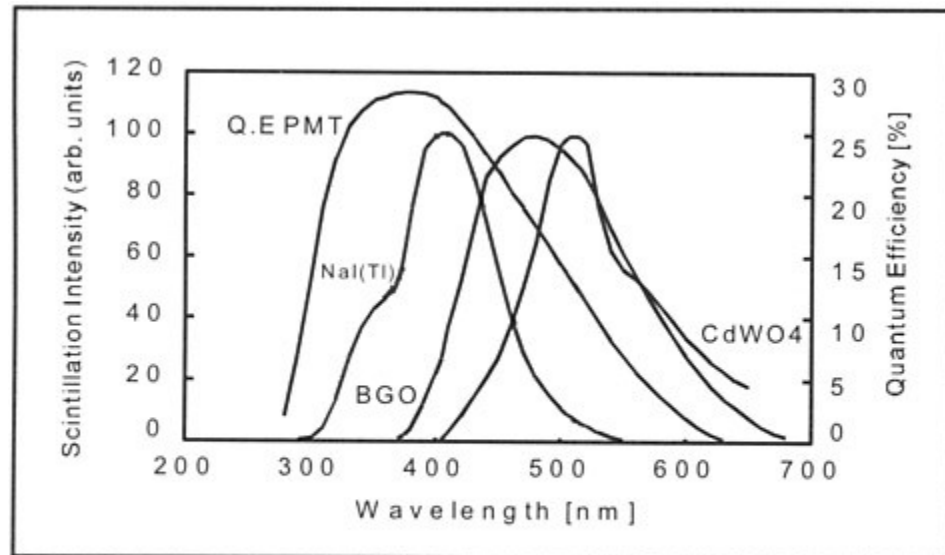
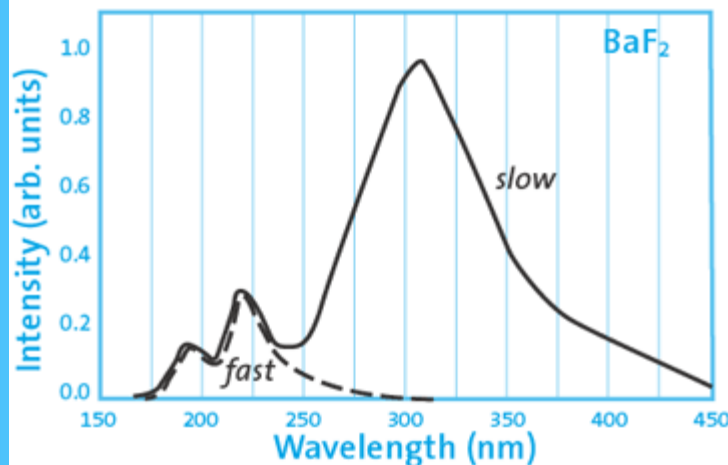




As a consequence there is a particle type and energy dependence of scintillation pulse shape and light output

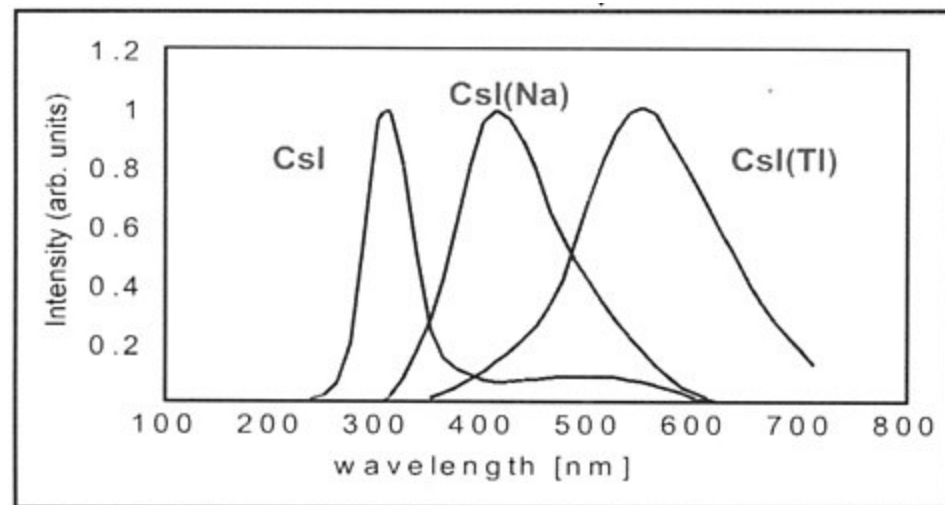
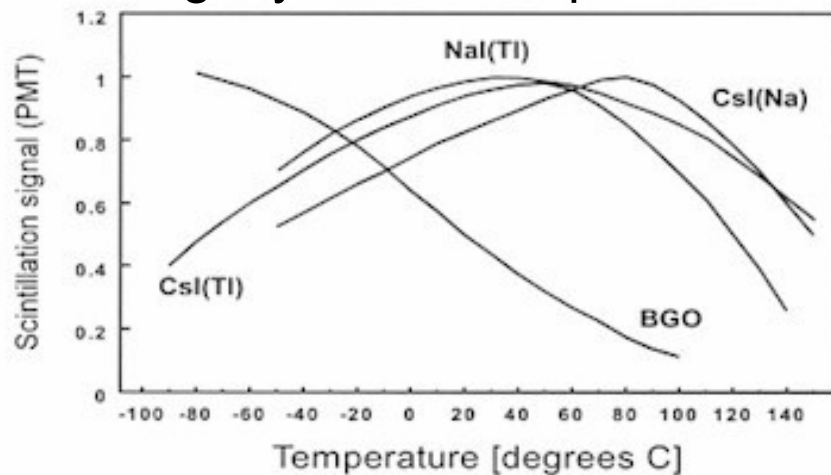
Both effects can be used to identify particles



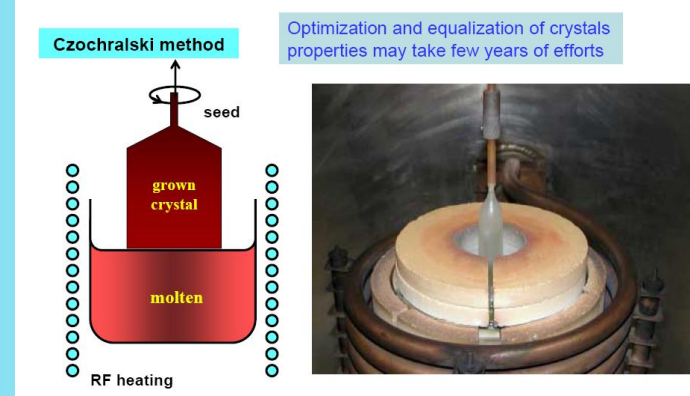


Emission spectra

Light yield vs. temperature



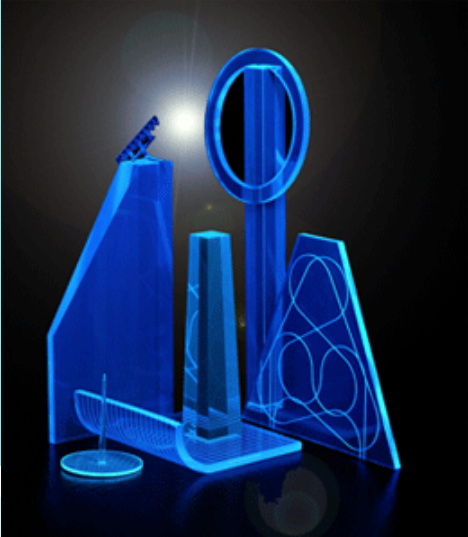
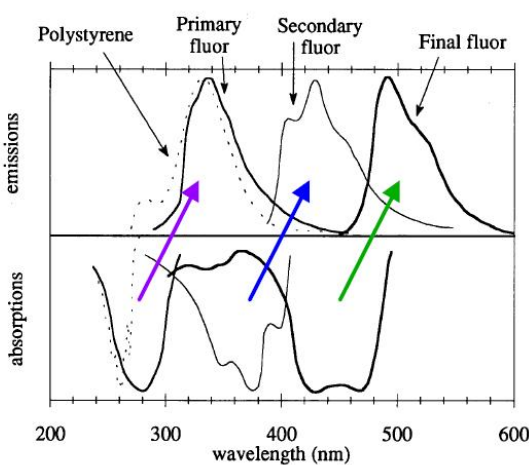
Properties of some inorganic scintillation crystals



	Density (g/cm ³)	Wavelength at max.(nm)	Refractive index	Decay time (ns)	Light yield (ph/MeV)
NaI(Tl)	3.67	415	1.85	230	38000
CsI(Tl)	4.51	540	1.80	680,3340	40000,25000
Bi₄Ge₃O₁₂	7.13	480	2.15	300	8200
BaF₂	4.89	220,310	1.56	0.6,630	1500,9500
CeF₃	6.16	310,340	1.68	5,27	4400
YAlO₃(Ce)	5.37	370	1.95	27	18000
Lu₂SiO₅(Ce)	7.4	420	1.82	47	25000
LaBr₃(Ce)	3.79	350	1.9	27	49000
Plastic BC-400	1.03	420	1.58	2.4	10000

Properties of some organic scintillation plastics

wavelength shifters →



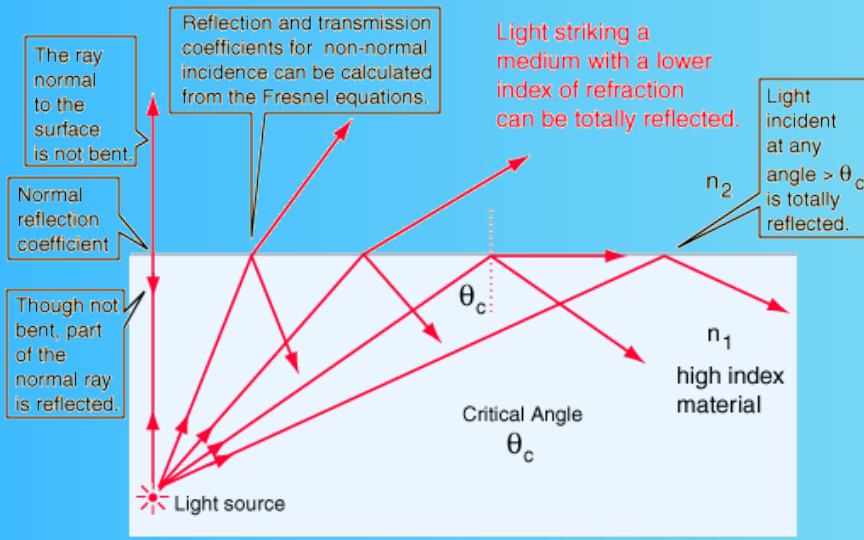
Scintillator	Light Output % Anthracene ¹	Wavelength of Maximum Emission, nm	Decay Con- stant, Main Component, ns	Bulk Light Attenuation Length, cm	Refractive Index	H/C Ratio	Loading Element % by weight	Density	Softening Point °C
BC-400	65	423	2.4	250	1.58	1.103	Benzephenone,1%*	1.032	70
BC-404	68	408	1.8	160	1.58	1.107		1.032	70
BC-408	64	425	2.1	380	1.58	1.104		1.032	70
BC-412	60	434	3.3	400	1.58	1.104		1.032	70
BC-414	68	392	1.8	100	1.58	1.110		1.032	70
BC-416	38	434	4.0	400	1.58	1.110		1.032	70
BC-418	67	391	1.4	100	1.58	1.100		1.032	70
BC-420	64	391	1.5	110	1.58	1.100		1.032	70
BC-422	55	370	1.6	8	1.58	1.102		1.032	70
BC-422Q	11	370	0.7	<8	1.58	1.102		1.032	70
BC-428	36	480	12.5	150	1.58	1.103	Deuterium,13.8%	1.032	70
BC-430	45	580	16.8	NA	1.58	1.108		1.032	70
BC-436	52	425	2.2	NA	1.61	0.960 D:C		1.130	100
BC-440	60	434	3.3	400	1.58	1.104		1.032	90
BC-440M	60	434	3.3	380	1.58	1.104	Lead,5% Boron,5%	1.039	100
BC-444	41	428	285	180	1.58	1.109		1.032	70
BC-444G	34	490	285	180	1.58	1.109		1.032	70
BC-452	32	424	2.1	150	1.58	1.134		1.080	60
BC-454 5%	48	425	2.2	120	1.58	1.169		1.026	60
BC-480	**	425	—	400	1.58	1.100		1.032	70
BC-482A	QE=.86	494	12.0	300	1.58	1.110		1.032	70
BC-490	55	425	2.3	NA	1.58	1.107		1.030	70
BC-498	65	423	2.4	NA	1.58	1.103		1.032	70

¹ Anthracene light output = 40-50% of NaI(Tl)

^{*} 0.1 to 5 weight % also available

^{**} Ratio of Cerenkov light to scintillator light = 10:1

Light collection and transmission

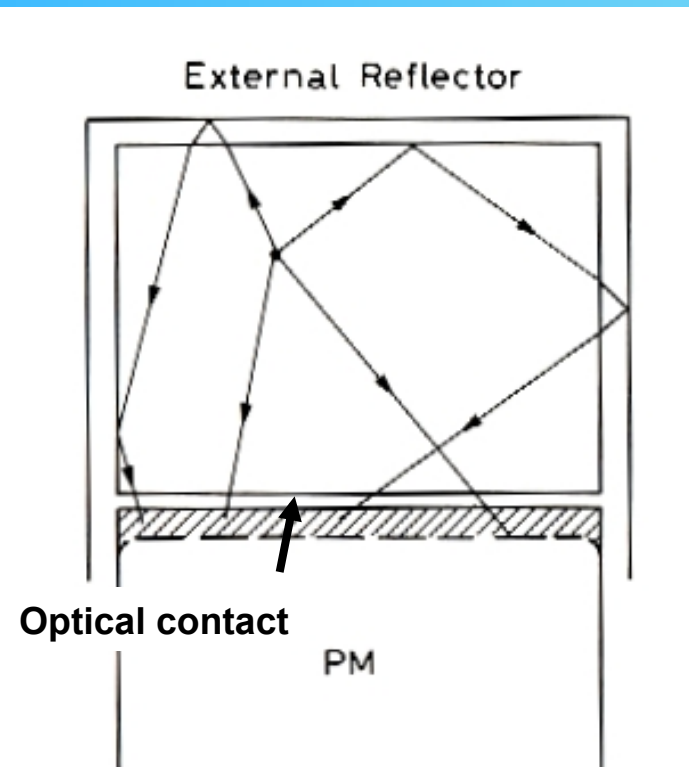
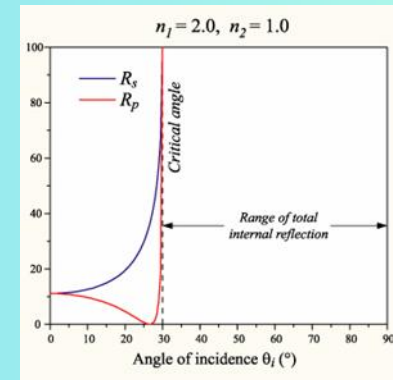


Snell law:

$$n_i \sin \theta_i = n_t \sin \theta_t$$

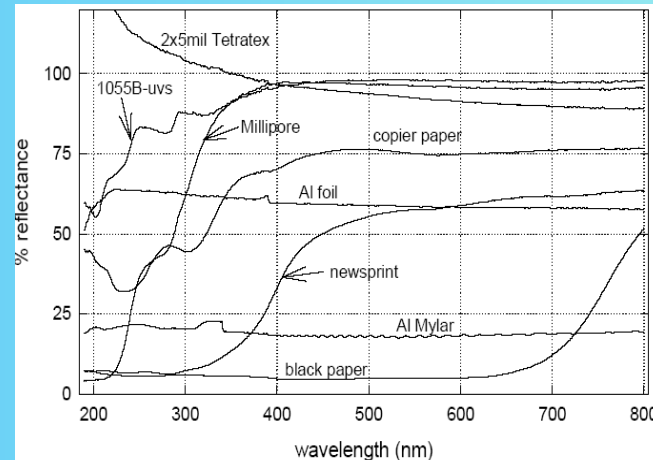
Fresnel formulae:

$$R_{para} = \frac{\tan^2(\theta_i - \theta_t)}{\tan^2(\theta_i + \theta_t)}, \quad R_{perp} = \frac{\sin^2(\theta_i - \theta_t)}{\sin^2(\theta_i + \theta_t)}$$



Reflector:

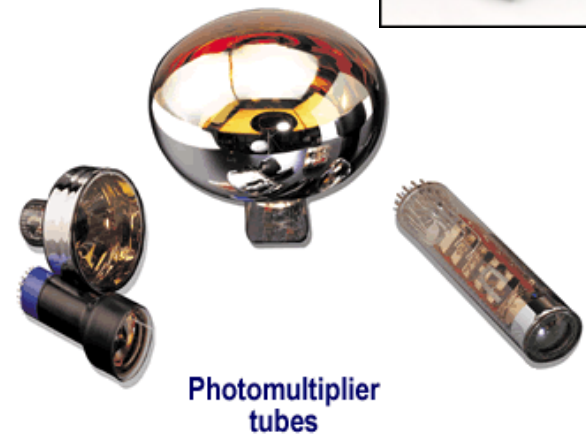
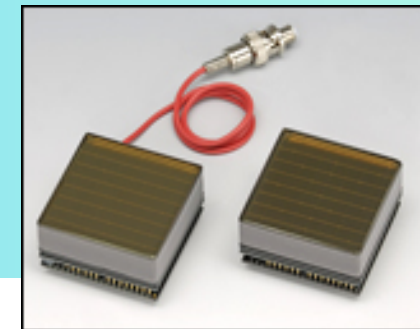
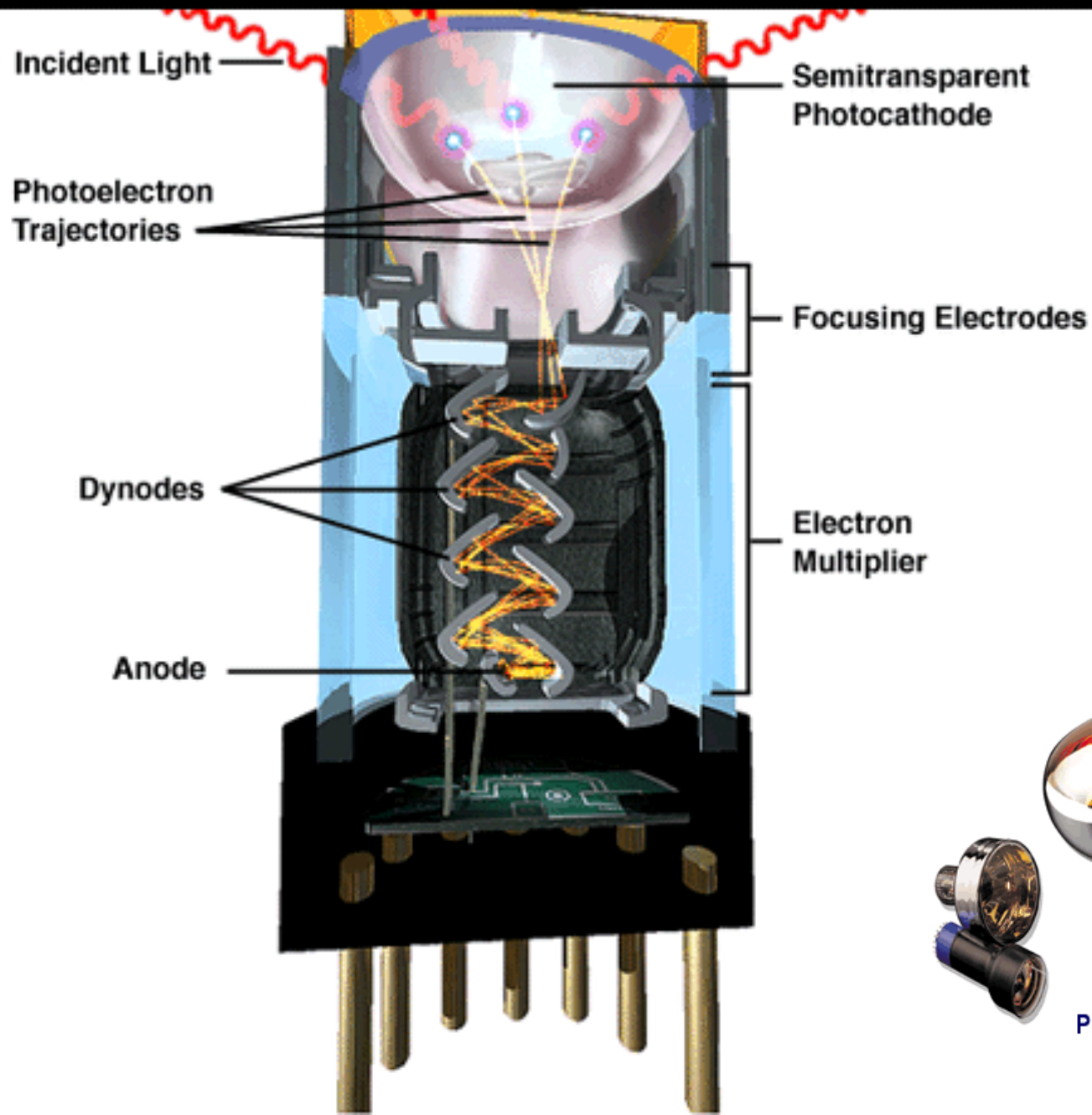
- mirror-like: $\theta_r = \theta_i$
- diffuse: θ_r random



Light-guide

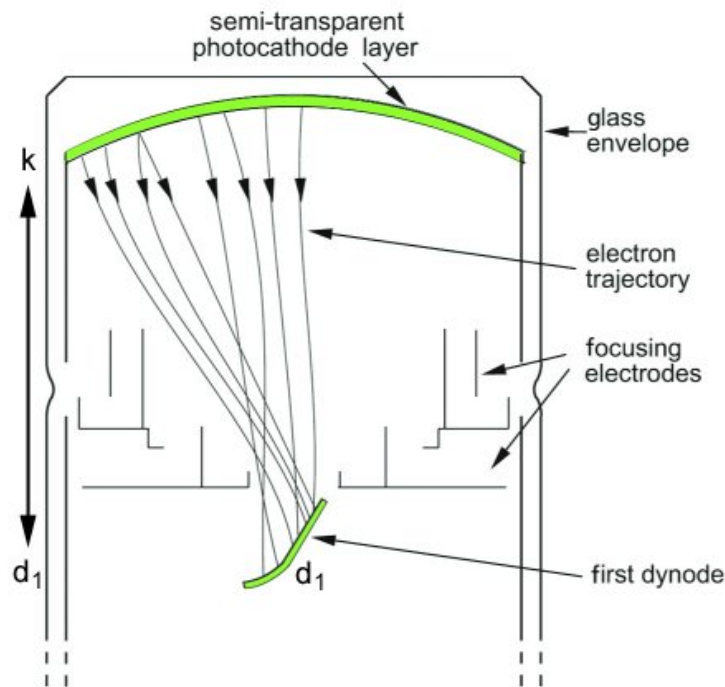


The Photomultiplier Tube

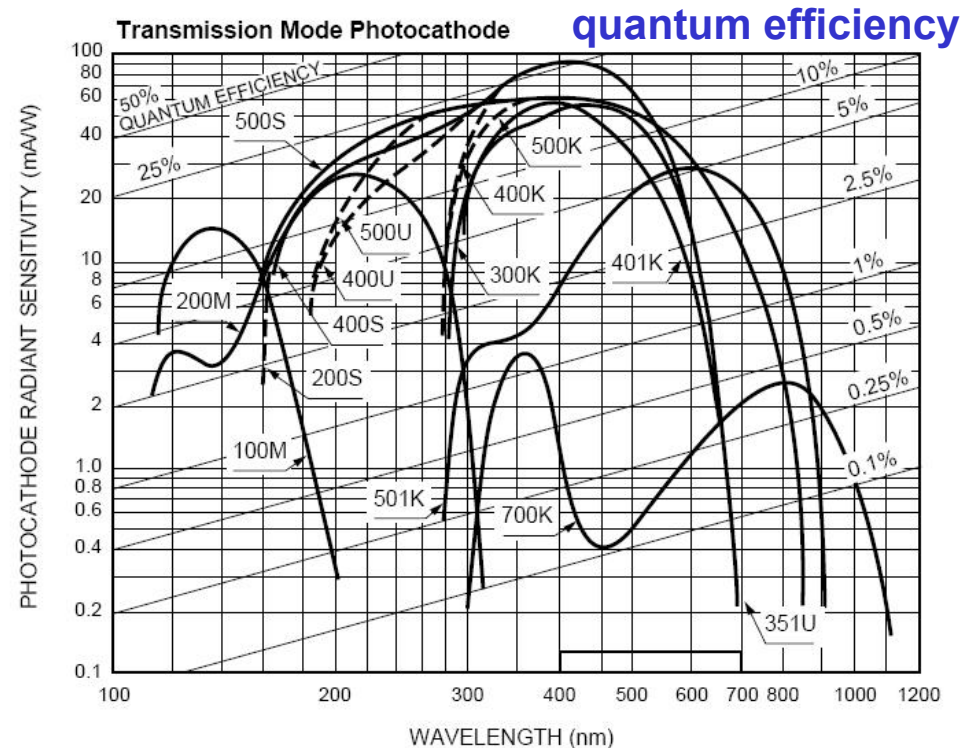
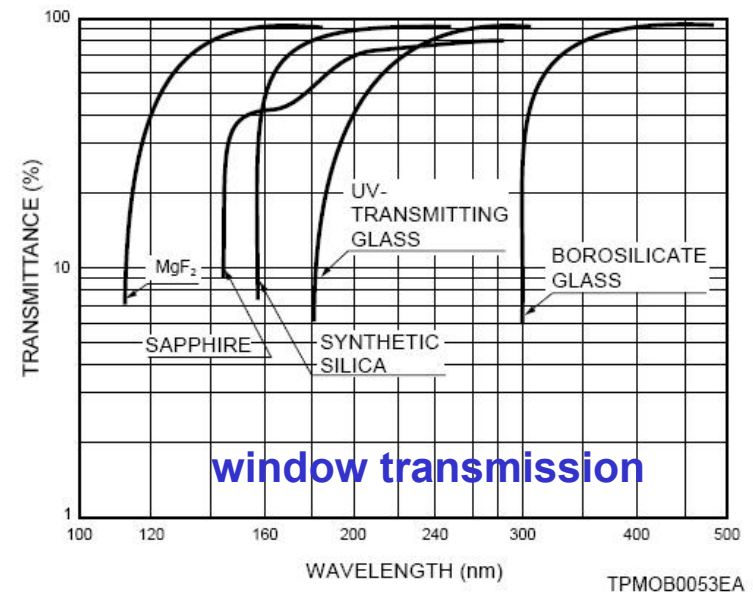


PMT window, photo-cathode and focusing electrodes:

- spectral sensitivity, gain, energy resolution and time resolution



Photoelectron trajectories between photocathode and first dynode.



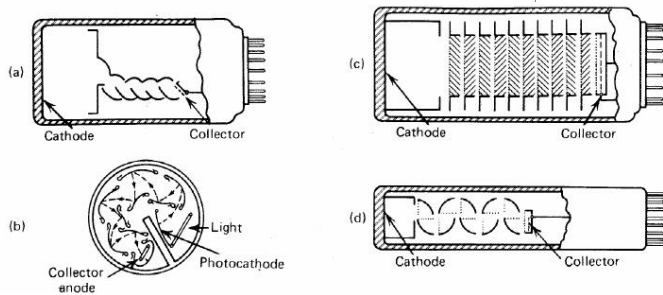
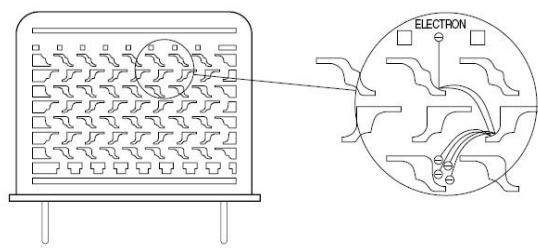


Fig. 4-8. Configurations of some common types of PM tubes. (a) Focused linear structure. (b) Circular grid. (c) Venetian blind. (d) Box-and-grid. (Courtesy of EMI GENCOM Inc., Plainview, NY.)

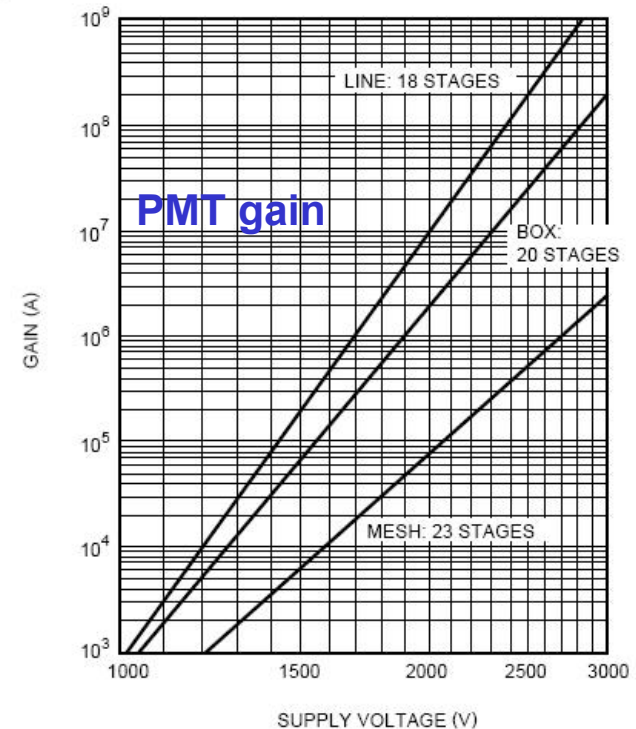
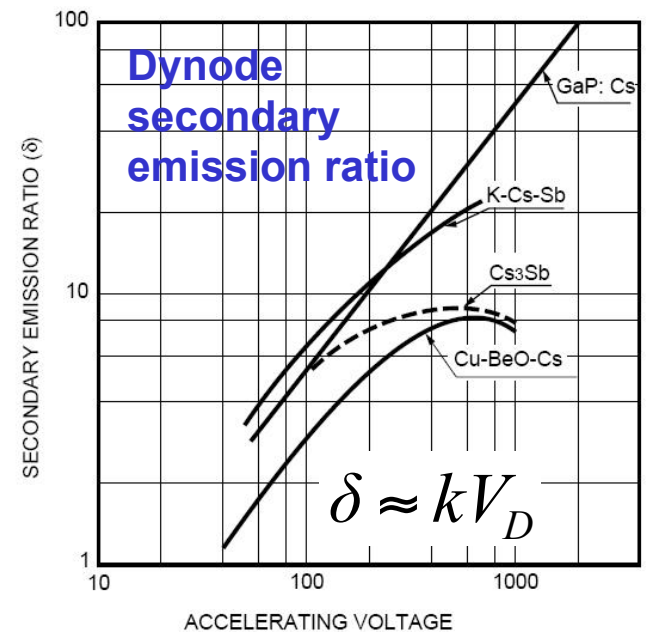


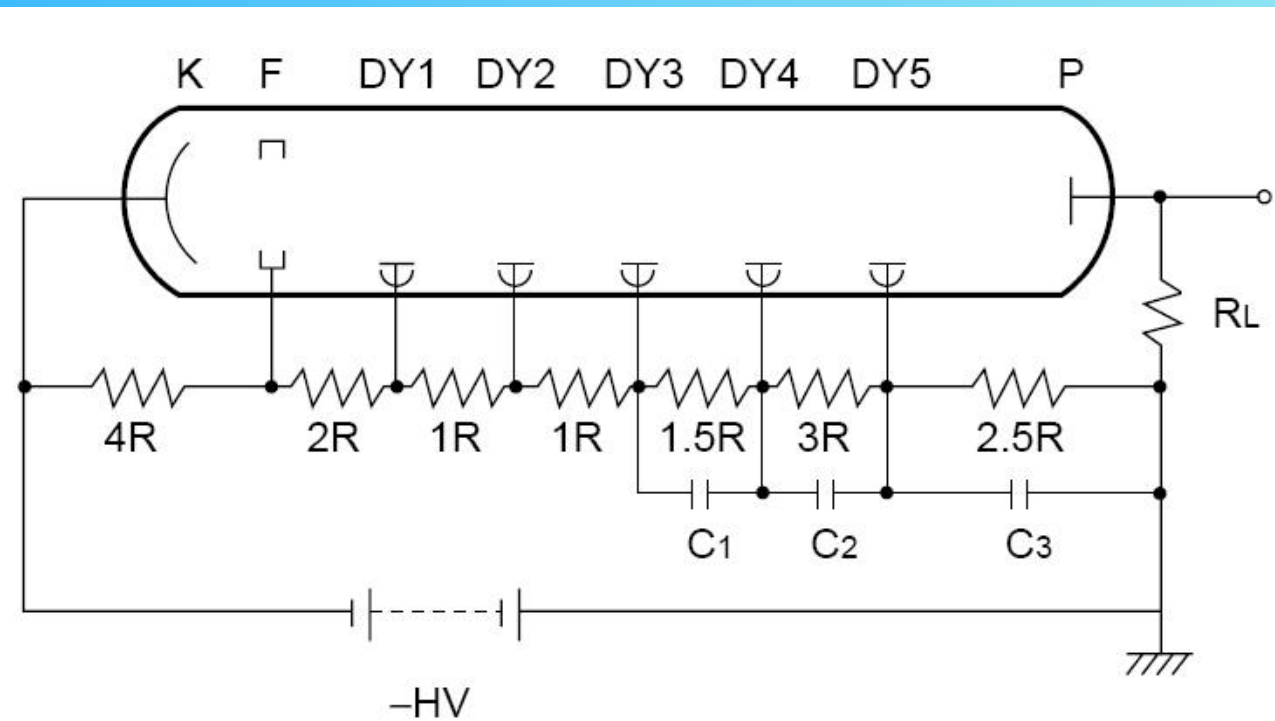
PMT dynode structure:

- gain & time resolution

$$G \approx \delta^n$$

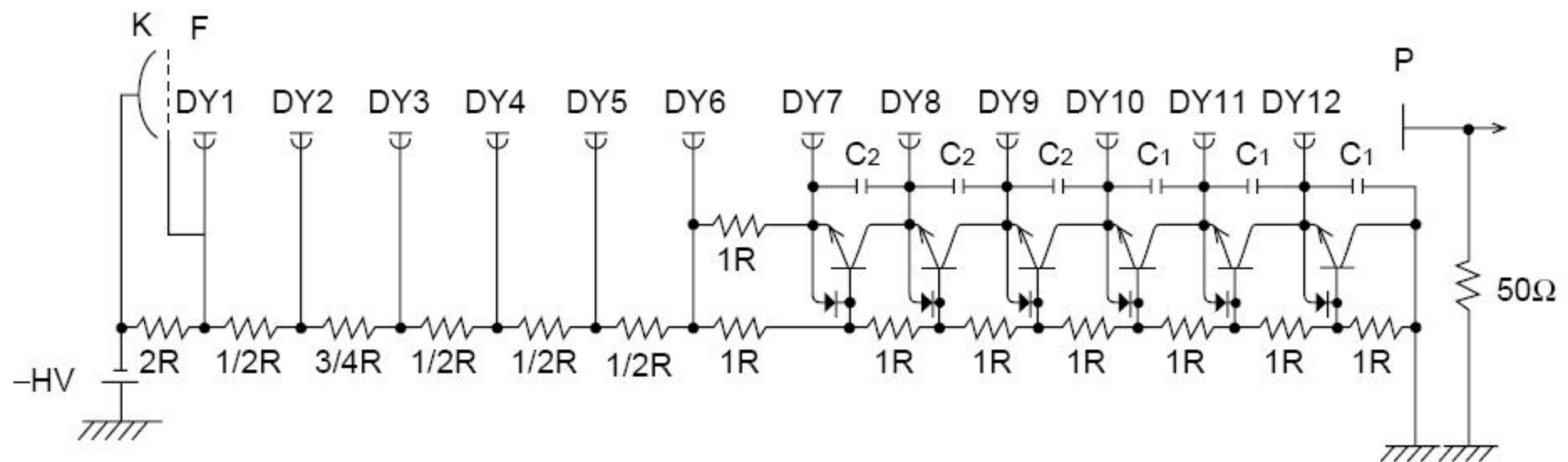
$$\frac{\Delta G}{G} \approx n \frac{\Delta V_D}{V_D}$$



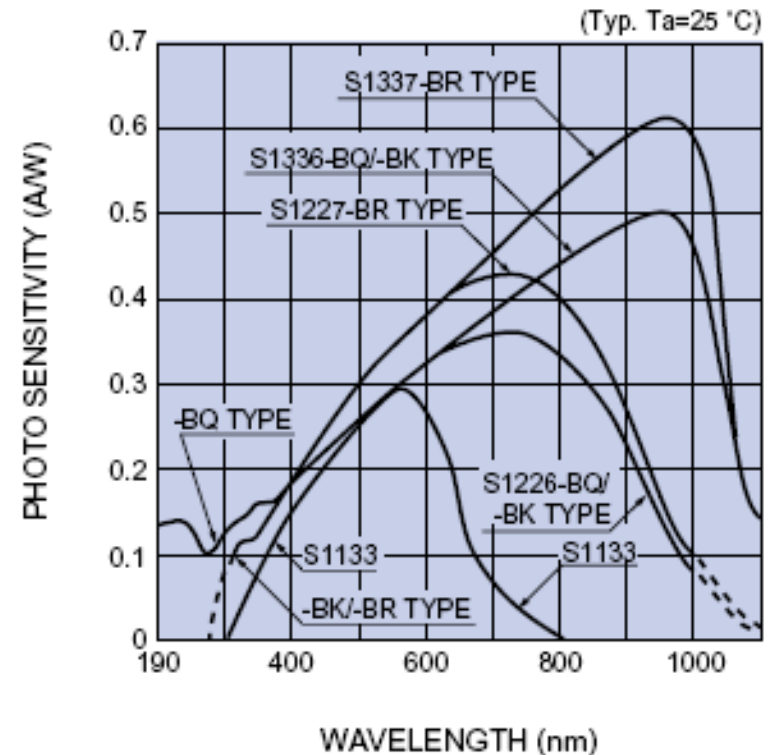
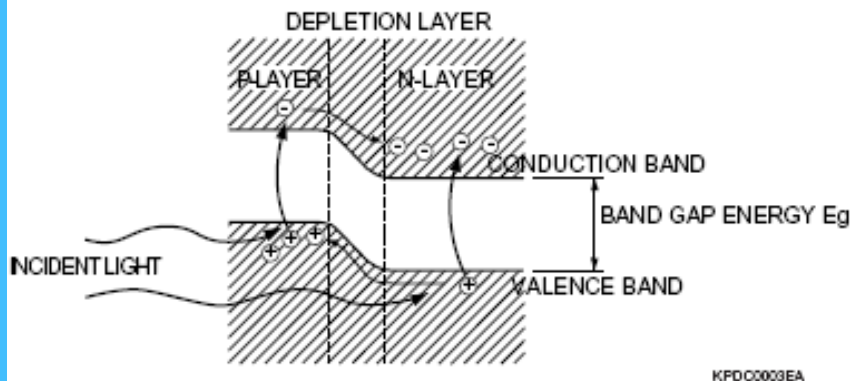
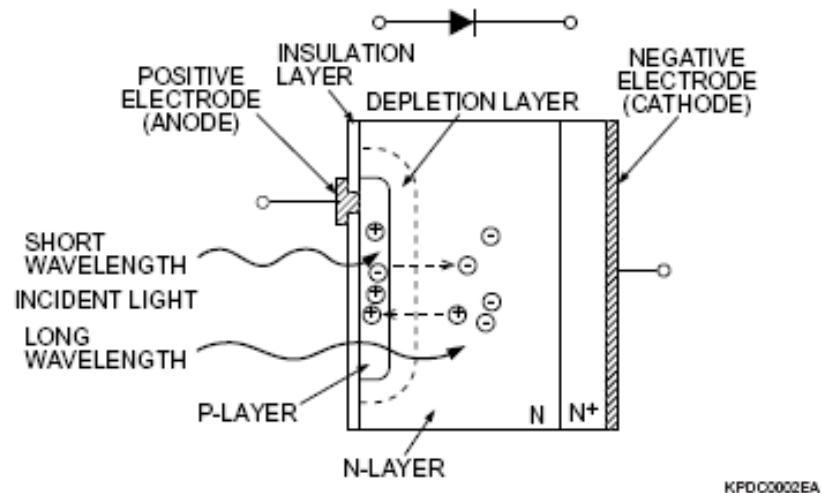


**PMT base -
voltage divider:**

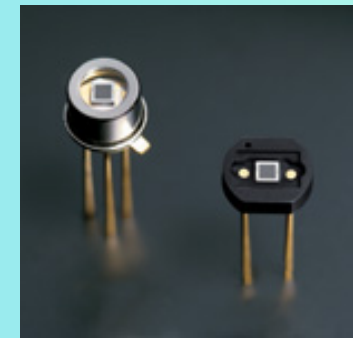
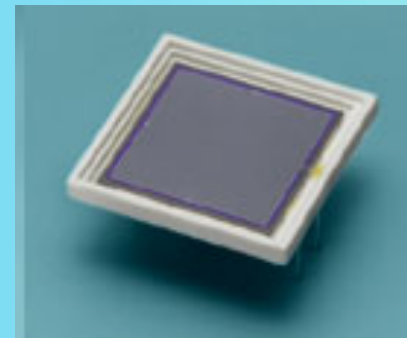
- linearity

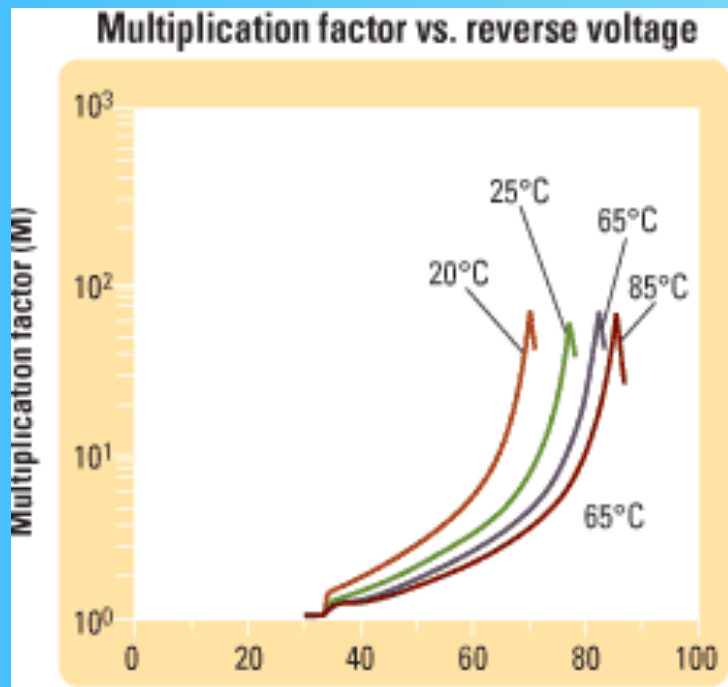
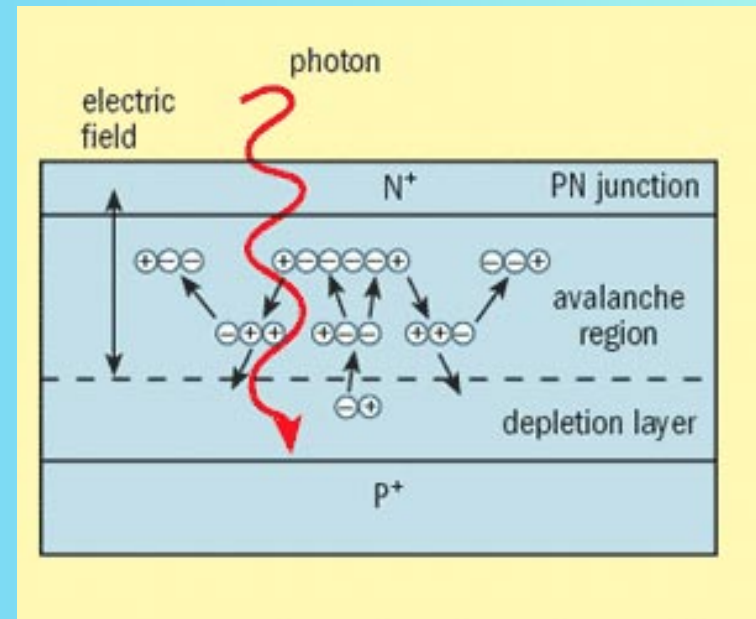
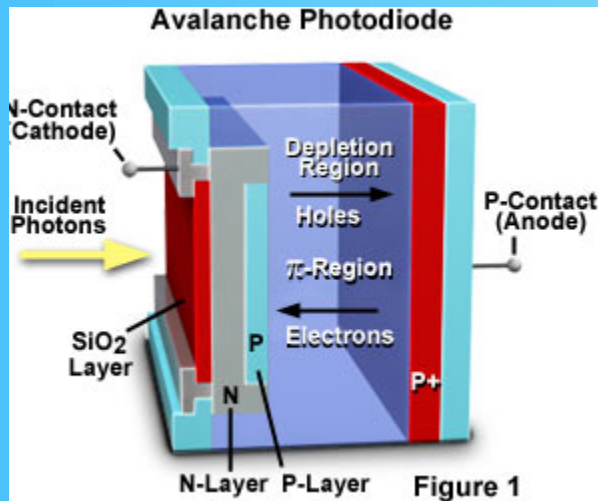


Semiconductor photo-sensors



Si Photo-Diodes (PD):
very small current proportional
to photon intensity

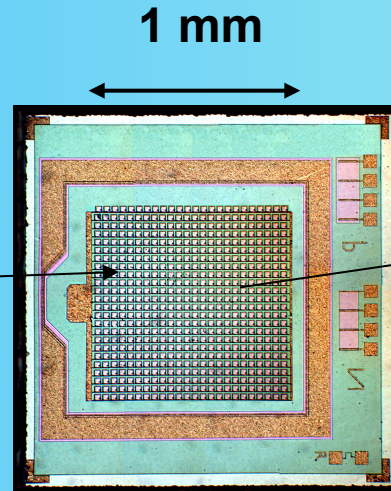
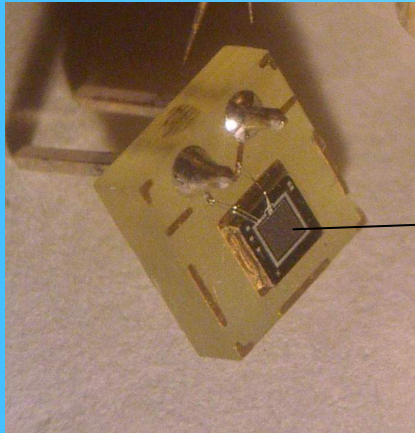




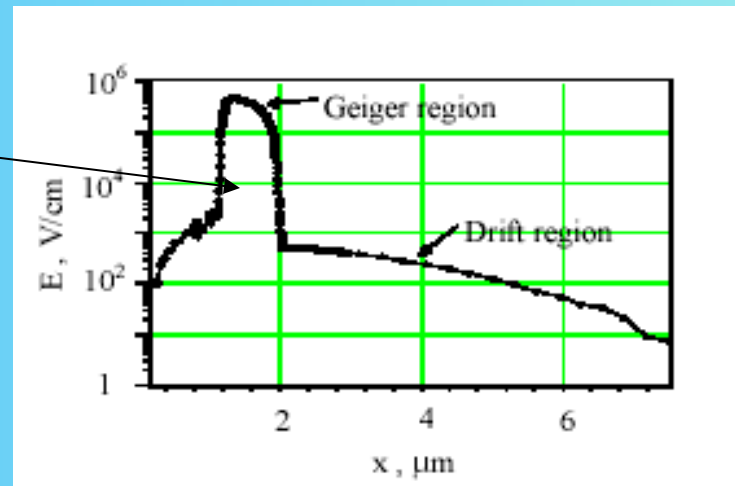
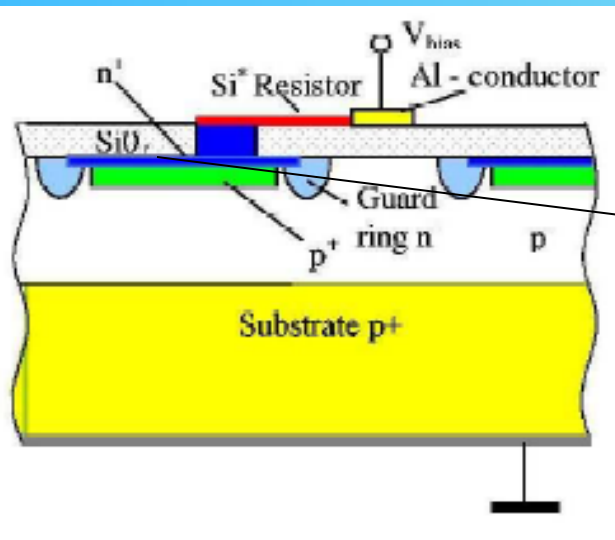
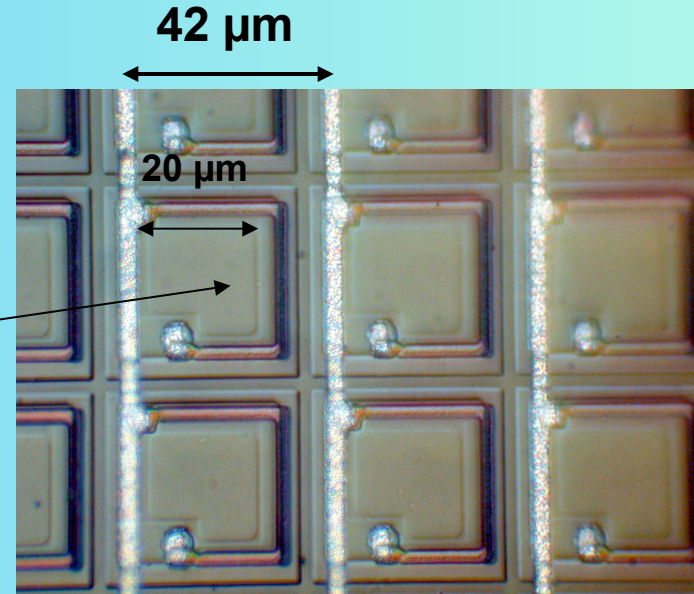
Avalanche Photo-Diodes (APD):
 initial current amplified by
 avalanche process, still
 proportional to initial photon
 intensity

Silicon Photomultipliers (Si-PMT, SPM, MPPC, DAPD, ...)

single photon counting



24*24=576 pixels



$$N_{hits} = N_{cells} \times \left(1 - (1 - P_{cell})^{N_{photons}}\right)$$

**Very high
amplification,
current
independent
from initial
photon
intensity
(Geiger mode)**

Scintillation detector energy resolution:

1. Light yield variations of scintillation material: statistical (intrinsic) and non-proportionality of light production
2. Light collection variations: statistical, geometrical dependency
3. Light conversion variations: statistical (quantum efficiency), non-uniformity of photo cathode
4. Electron multiplication and collection variations (single photon response)
5. Read-out electronic noise

Scintillation detector linearity:

1. Light yield linearity
2. Electron multiplication linearity
3. Read-out electronic linearity

Scintillation detector noise:

1. Scintillation material activity and after-glow
2. Photo-multiplier dark current
3. Read-out electronic noise

Can we predict/influence the expected resolution?

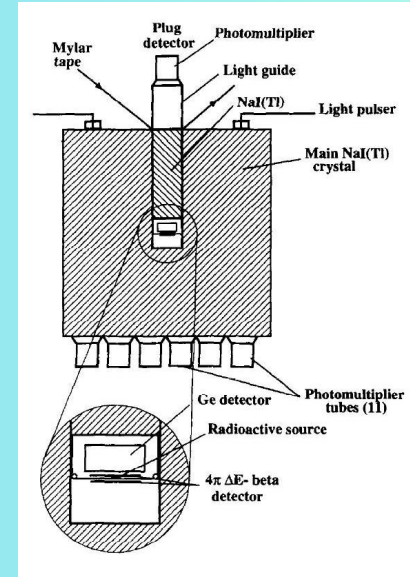
The energy resolution in an scintillation detector for γ -rays will be given by the statistical fluctuations in:

1. the energy of secondaries generated (non-proportionality)
2. the number of scintillation photons per energy deposited (intrinsic)
3. the fraction of photons collected at the photocathode (transport, absorption)
4. the fraction of photo-electrons collected at the 1st dynode (quantum efficiency, collection)
5. the PMT gain (multiplication, collection)
6. the electronic noise

$$\frac{FWHM}{E} = \sqrt{\frac{\alpha_{2,3}}{E} + \beta_{4,5} + \chi_1(E)}$$

5.9% @ 1.33 MeV

Figure 1 is a scatter plot showing the energy difference ΔE (keV) on the y-axis versus the energy E (keV) on the x-axis. The y-axis ranges from -30 to 70 keV, and the x-axis ranges from 0 to 4000 keV. The data points are labeled with isotope symbols: ^{108}Ca , ^{203}Hg , ^{112}Sn , ^{85}Sr , ^{137}Cs , ^{86}Y , ^{46}Sc , ^{60}Co , ^{24}Na , ^{46}Sc , ^{60}Co , ^{24}Na , ^{86}Y , ^{24}Na , ^{60}Co , ^{86}Y , and ^{24}Na . The points show a general trend of increasing ΔE with increasing E , with some outliers.

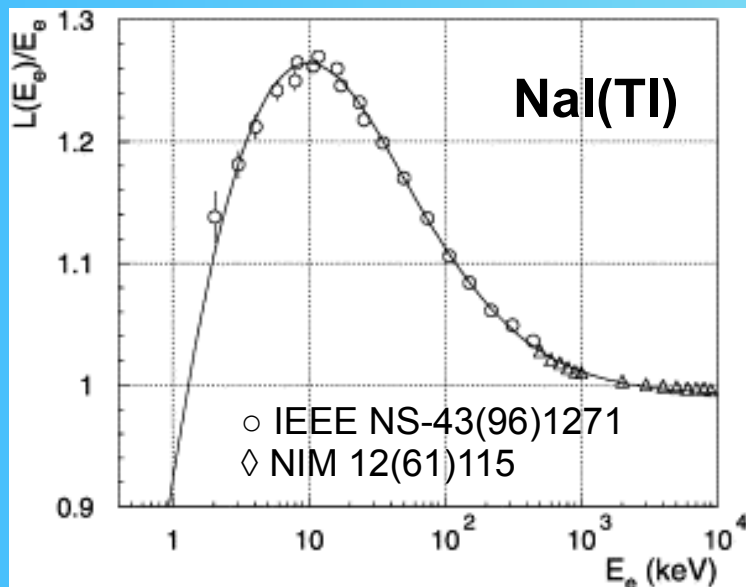


3.2% @ 1.33 MeV

3.8% @ 1.33 MeV

3.1% @ 1.33 MeV

Light yield non-proportionality



LaBr₃ negligible?

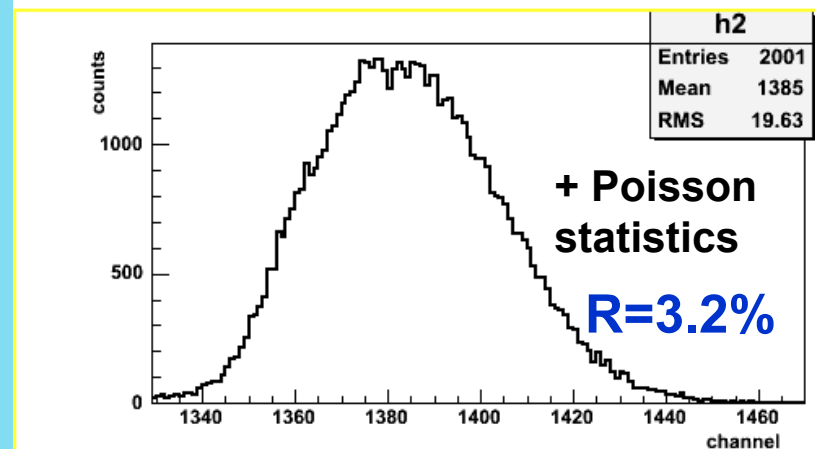
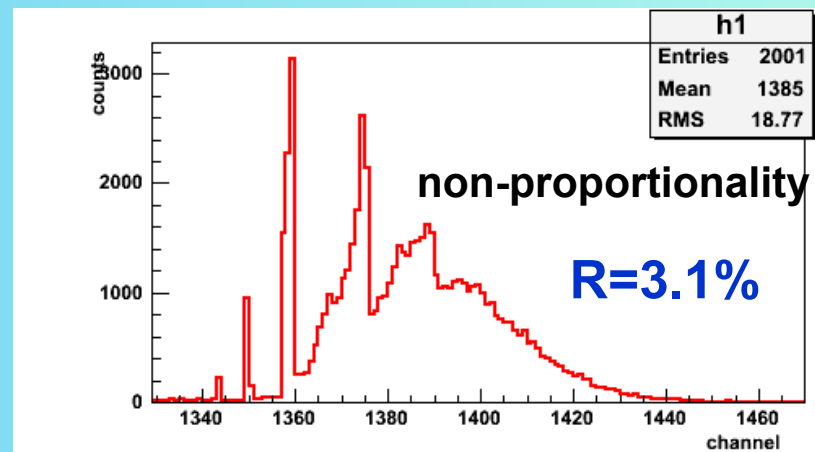
Light yield statistics

- assumed Poisson

$$Y_{NaI}^{scin} = 38 \text{ ph / keV} \rightarrow 1.0\%$$

$$Y_{LaBr_3}^{scin} = 63 \text{ ph / keV} \rightarrow 0.8\%$$

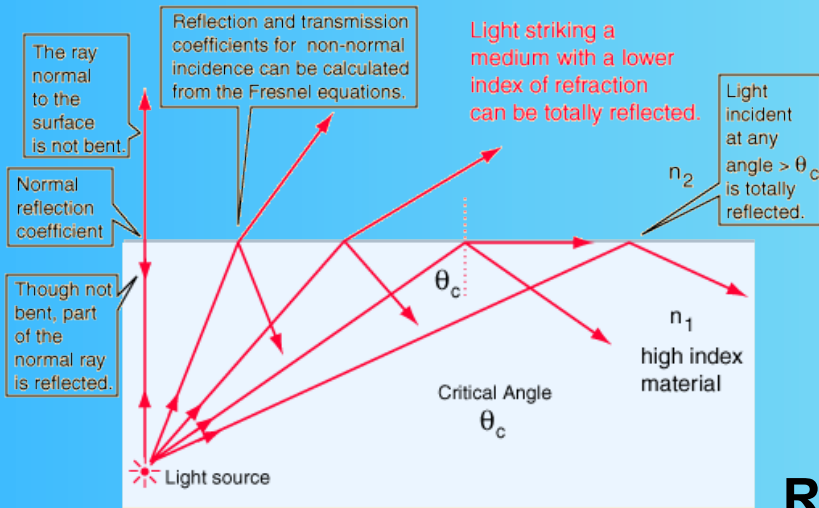
GEANT3 MC simulation



$$R = \frac{2.35}{\sqrt{E \times Y^{scin}}}$$

Simulation of light transport and collection with Geant4

- Influence of geometry, reflector type, surface treatment, refractive index matching, light-guide, ...

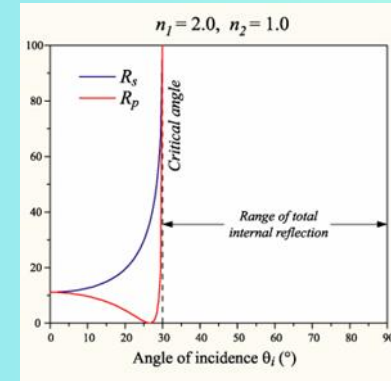


Snell law:

$$n_i \sin \theta_i = n_t \sin \theta_t$$

Fresnel formulae:

$$R_{\parallel} = \frac{\tan^2(\theta_i - \theta_t)}{\tan^2(\theta_i + \theta_t)}, \quad R_{\perp} = \frac{\sin^2(\theta_i - \theta_t)}{\sin^2(\theta_i + \theta_t)}$$

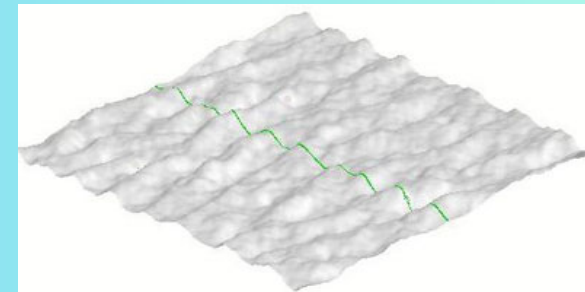
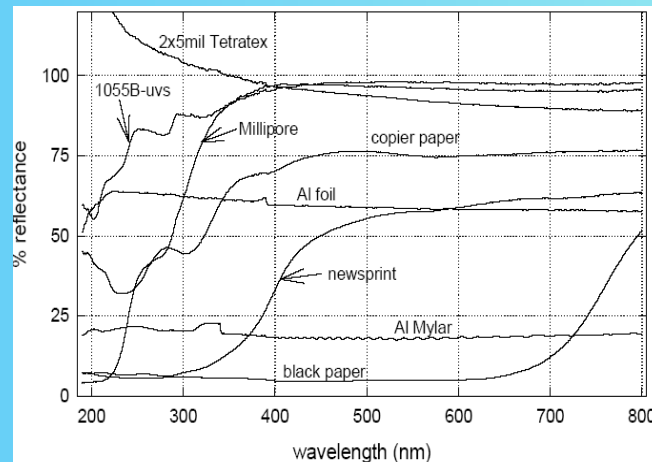
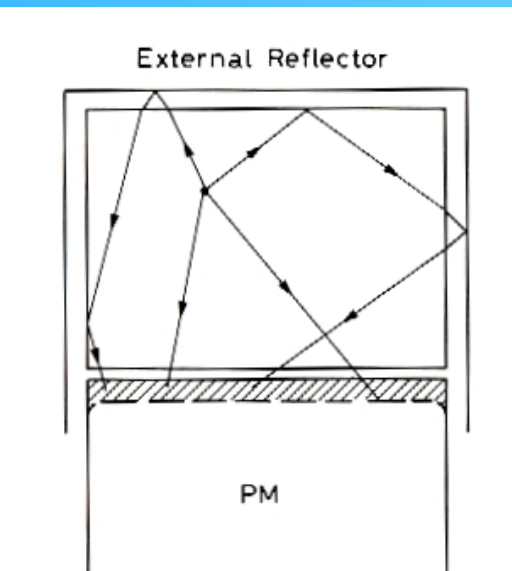


Reflector:

- mirror-like: $\theta_r = \theta_i$
- diffuse: θ_r random

Surface state:

- polished
- rough



Geant4 MC simulations

Nal module

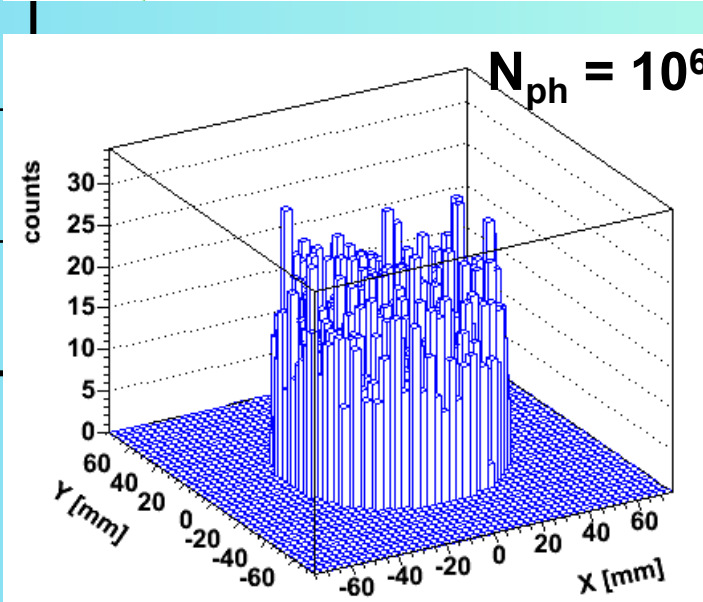
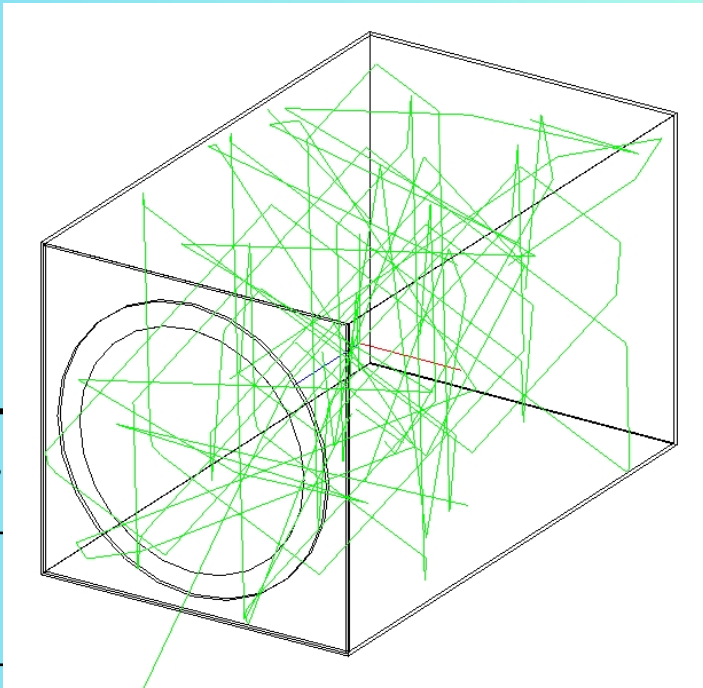
$n_{\text{Nal}} = 1.85, n_{\text{PMT}}=1.47, n_{\text{LG}} = 1.60$

$\lambda_{\text{Nal}} = 1 \text{ m} ?$

Specular reflector: $\rho=1$

Diffusse reflector: $\rho=1$ (Lambertian)

	Specular reflector	Diffuse reflector
Point source $\lambda_{\text{abs}} = 1 \text{ m}$	12.5%	16.3%
Extended source $\lambda_{\text{abs}} = 1 \text{ m}$	12.1%	16.5%
Extended source $\lambda_{\text{abs}} = 20 \text{ cm}$	4.4%	4.3%
Extended source $\lambda_{\text{abs}} = 1 \text{ m}$ Light guide $n = 1.6$	13.7%	18.0%



Geant4 MC simulation

Light transport contribution to the energy resolution

$$E_{\gamma} = 1.33 \text{ MeV}, Y_{\text{scint}} = 38 \text{ ph/keV}$$

No Poisson statistics,
no non-proportionality

$$LF = \frac{N^{\text{cathode}}}{E_{\gamma} \times Y^{\text{scin}}}$$

Nal module

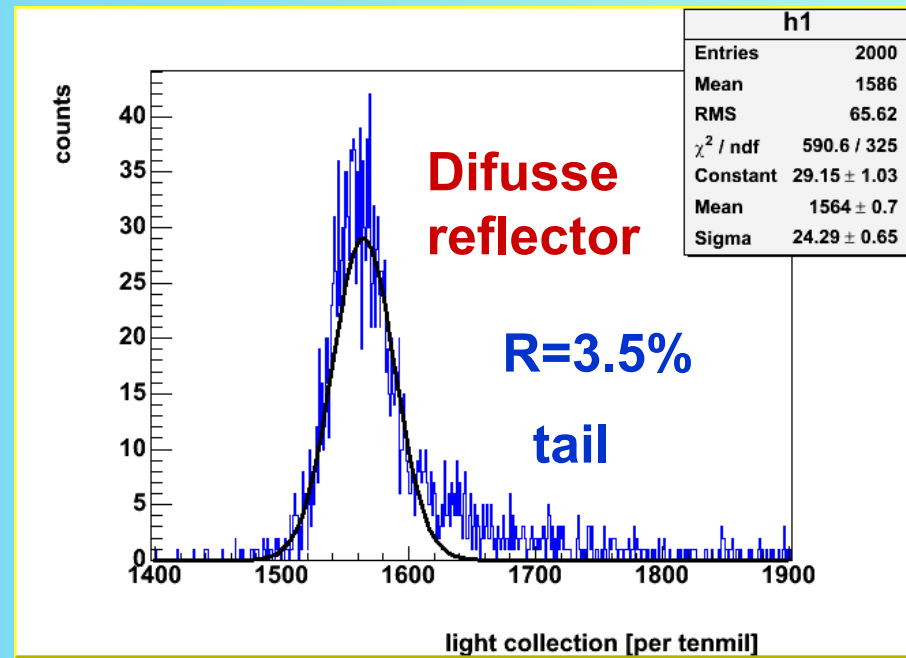
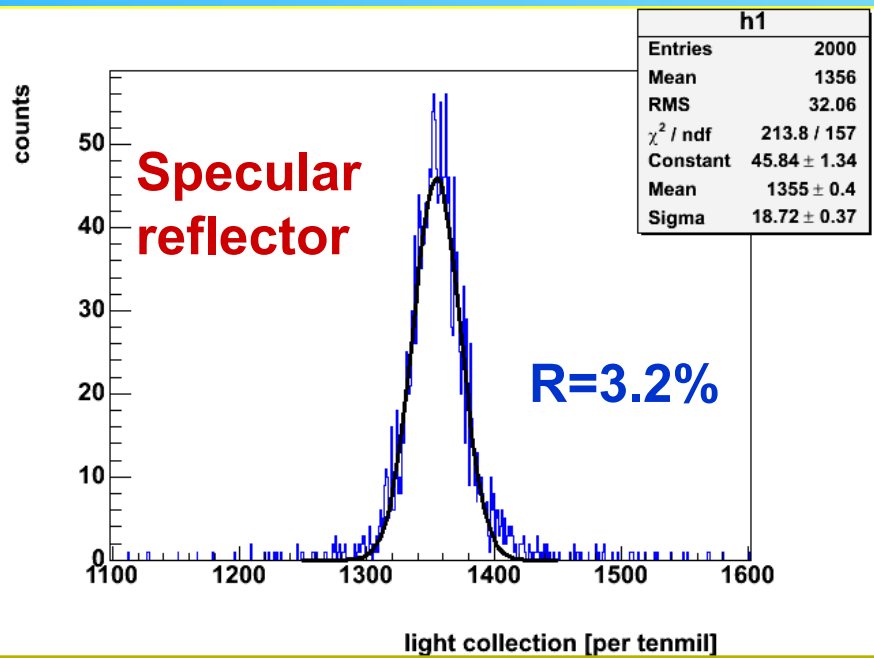
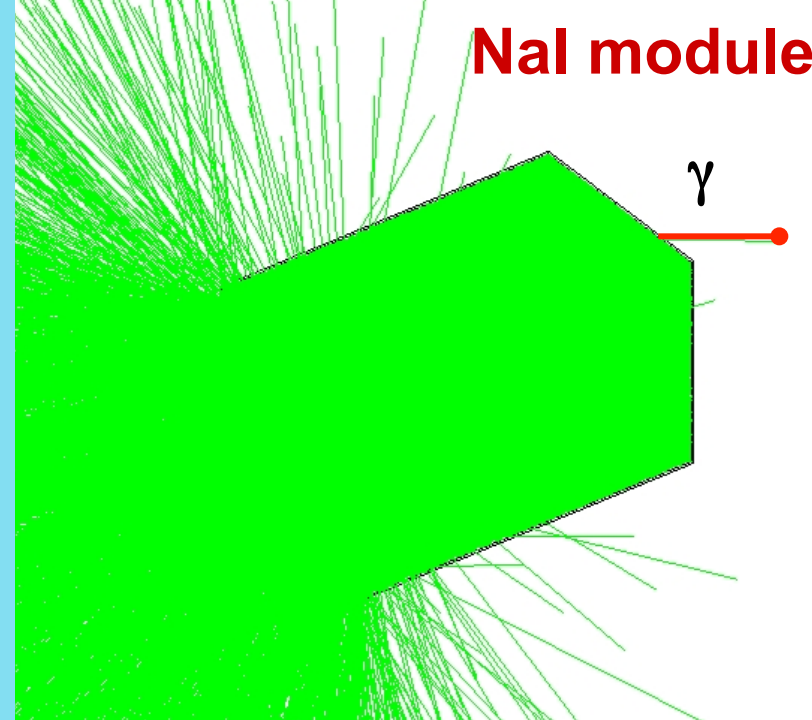
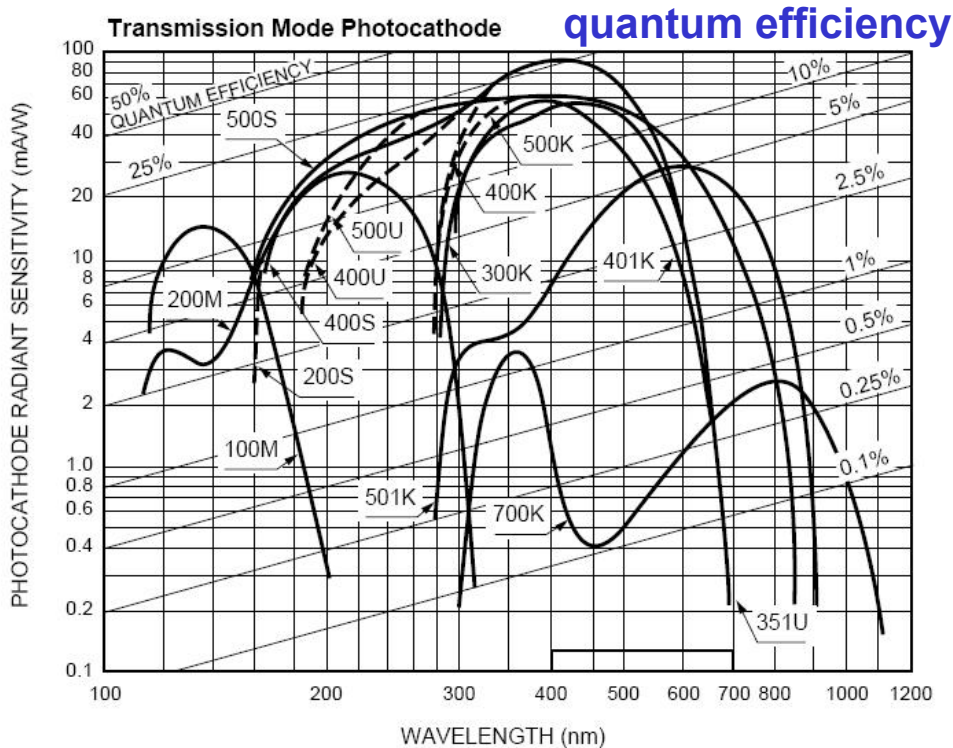


Photo-electron conversion

Binomial distribution



x : success, N : trials, p : probability

$$P(x) = \frac{N!}{x!(N-x)!} p^x (1-p)^{N-x}$$

$$\bar{x} = Np$$

$$\sigma^2 = \bar{x}(1-p)$$

$$R = 2.35 \sqrt{\frac{(1-QE)}{N_{ph} \times QE}}$$